

Description

Each phase has two rounds, round 1 and round 2.

$R[p, t]$ is a *multi-set* of received values in round t at phase p .

$\text{MAJ}(R)$ = the number of occurrence of the majority non-? value in a multi-set R .

$\text{MAJV}(R)$ = the majority non-? value in a multi-set R .

Line 33 makes sure that every node flips the coin same number of times.

(i, p, 1, *) == round-1 messages == State messages

(i, p, 2, *) == round-2 messages == Vote messages

The verbose version of Weak-MVC and its helper function

Algorithm 4 IDK-BC: Code for node i

Local Variables: /* These variables can be accessed and modified by any thread at i . */

x	▷input at node i , $\{0, 1\}$
$v[t, 1]$	▷a vector of local state at round 1, $\{0, 1\}$
$v[t, 2]$	▷a vector of local state at round 2, $\{0, 1, ?\}$
p	▷phase, integer

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/* All messages tagged with seq */
When IDK-BC( $v, seq$ ) is invoked:
/* Initial Phase */
1: Send ( $i, 0, 1, v$ ) to all
2: wait until  $|R[0, 1]| \geq n - f$ 
3: if  $\text{MAJ}(R[0, 1]) \geq \lfloor \frac{n}{2} \rfloor + f + 1$  then
4:   Send ( $i, \text{MAJV}(R[0, 1]), DEC$ ) to all
5:   Return  $\text{MAJV}(R[0, 1])$ 
6: else if  $\text{MAJ}(R[0, 1]) \geq \lfloor \frac{n}{2} \rfloor + 1$  then
7:    $v[0, 2] \leftarrow 1$ 
8: else
9:    $v[0, 2] \leftarrow ?$ 
An optimization for increasing 1's,
  which might not be necessary.
10: Send ( $i, 0, 2, v[0, 2]$ ) to all
11: wait until  $|R[0, 2]| \geq n - f$ 
12: if  $\text{MAJ}(R[0, 2]) \geq f + 1$  then
13:    $m \leftarrow \text{FindReturnValue}(0, 2)$ 
14:   Send ( $i, m, DEC$ ) to all
15:   Return  $m$ 
16: else if  $\text{MAJ}(R[0, 2]) \geq 1$  then
17:    $v[1, 1] \leftarrow \text{MAJV}(R[0, 2])$ 
18: else
19:    $v[1, 1] \leftarrow 0$ 

/* Same as BO-BC except for the return step*/
20:  $p \leftarrow 1$ 
21: while  $TRUE$  do
  /* Round 1 */
22: Send ( $i, p, 1, v[p, 1]$ ) to all
23: wait until  $|R[p, 1]| \geq n - f$ 
24: if  $\text{MAJ}(R[p, 1]) \geq \lfloor \frac{n}{2} \rfloor + f + 1$  then
25:    $m \leftarrow \text{FindReturnValue}(p, 1)$ 
26:   Send ( $i, m, DEC$ ) to all
27:   Return  $m$ 
28: else if  $\text{MAJ}(R[p, 1]) \geq \lfloor \frac{n}{2} \rfloor + 1$  then
29:    $v[p, 2] \leftarrow \text{MAJV}(R[p, 1])$ 
30: else
31:    $v[p, 2] \leftarrow ?$ 
  /* Round 2 */
32: Send ( $i, p, 2, v[p, 2]$ ) to all
33:  $randBit \leftarrow \text{COMMONCOINFLIP}()$ 
34: wait until  $|R[p, 2]| \geq n - f$ 
35: if  $\text{MAJ}(R[p, 2]) \geq f + 1$  then
36:    $m \leftarrow \text{FindReturnValue}(p, 2)$ 
37:   Send ( $i, m, DEC$ ) to all
38:   Return  $m$ 
39: else if  $\text{MAJ}(R[p, 2]) \geq 1$  then
40:    $v[p + 1, 1] \leftarrow \text{MAJV}(R[p, 2])$ 
41: else
42:    $v[p + 1, 1] \leftarrow randBit$ 
43:    $p \leftarrow p + 1$  ▷Proceed to next phase

/* Helper procedure */
Procedure FindReturnValue( $p, r$ )
44: if  $\text{MAJV}(R[p, r]) = 1$  then
45:   if  $\text{MAJ}(R[0, 1]) \geq \lfloor \frac{n}{2} \rfloor + 1$  then
46:      $m \leftarrow \text{MAJV}(R[0, 1])$ 
47:   else
48:      $m \leftarrow$  proposal from  $j$  who has 1 in  $R[0, 2]$ 
49:   Return  $m$ 
50: else
51:   Return  $\perp$ 

/* Event handler: executing in background */
Upon receiving ( $j, p, t, b$ ) from node  $j$ :
52: Add  $b$  to  $R[p, t]$ 
Upon receiving ( $j, b, DEC$ ) from node  $j$ :
53: Return  $b$ 

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