

1

$$A_{01} = \begin{pmatrix} \cos(q1) & 0 & \sin(q1) & 33 \cos(q1) \\ \sin(q1) & 0 & -\cos(q1) & 33 \sin(q1) \\ 0 & 1 & 0 & 147 \\ 0 & 0 & 0 & 1 \end{pmatrix} \quad (1)$$

$$A_{12} = \begin{pmatrix} \cos(q2) & -\sin(q2) & 0 & 155 \cos(q2) \\ \sin(q2) & \cos(q2) & 0 & 155 \sin(q2) \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \quad (2)$$

$$A_{23} = \begin{pmatrix} \cos(q3) & -\sin(q3) & 0 & 135 \cos(q3) \\ \sin(q3) & \cos(q3) & 0 & 135 \sin(q3) \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \quad (3)$$

$$A_{34} = \begin{pmatrix} -\sin(q4) & -\cos(q4) & 0 & -\frac{568 \sin(q4)}{5} \\ \cos(q4) & -\sin(q4) & 0 & \frac{568 \cos(q4)}{5} \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \quad (4)$$

$$A_{45} = \begin{pmatrix} \cos(q5) & -\sin(q5) & 0 & 0 \\ \sin(q5) & \cos(q5) & 0 & 0 \\ 0 & 0 & 1 & \frac{1429}{25} \\ 0 & 0 & 0 & 1 \end{pmatrix} \quad (5)$$

$$A_{01} = \begin{pmatrix} \cos(q1) & -\sin(q1) & 0 & 0 \\ \sin(q1) & \cos(q1) & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \quad (6)$$

$$A_{02} = \begin{pmatrix} \cos(q_1) \cos(q_2) & -\cos(q_1) \sin(q_2) & \sin(q_1) & 33 \cos(q_1) \\ \cos(q_2) \sin(q_1) & -\sin(q_1) \sin(q_2) & -\cos(q_1) & 33 \sin(q_1) \\ \sin(q_2) & \cos(q_2) & 0 & 147 \\ 0 & 0 & 0 & 1 \end{pmatrix} \quad (7)$$

$$A_{03} = \begin{pmatrix} \cos(q_2 + q_3) \cos(q_1) & -\sin(q_2 + q_3) \cos(q_1) & \sin(q_1) & \cos(q_1) (155 \cos(q_2) + 33) \\ \cos(q_2 + q_3) \sin(q_1) & -\sin(q_2 + q_3) \sin(q_1) & -\cos(q_1) & \sin(q_1) (155 \cos(q_2) + 33) \\ \sin(q_2 + q_3) & \cos(q_2 + q_3) & 0 & 155 \sin(q_2) + 147 \\ 0 & 0 & 0 & 1 \end{pmatrix} \quad (8)$$

$$A_{04} = \begin{pmatrix} \cos(q_2 + q_3 + q_4) \cos(q_1) & -\sin(q_2 + q_3 + q_4) \cos(q_1) & \sin(q_1) & \cos(q_1) (135 \cos(q_2 + q_3) + 155 \cos(q_2) + 33) \\ \cos(q_2 + q_3 + q_4) \sin(q_1) & -\sin(q_2 + q_3 + q_4) \sin(q_1) & -\cos(q_1) & \sin(q_1) (135 \cos(q_2 + q_3) + 155 \cos(q_2) + 33) \\ \sin(q_2 + q_3 + q_4) & \cos(q_2 + q_3 + q_4) & 0 & 135 \sin(q_2 + q_3) + 155 \sin(q_2) + 147 \\ 0 & 0 & 0 & 1 \end{pmatrix} \quad (9)$$

$$\mathfrak{N} A_{05} = \begin{pmatrix} -\sin(q_1) \sin(q_5) - \frac{\cos(q_5) (\sin(q_1 + q_2 + q_3 + q_4) - \sin(q_1 - q_2 - q_3 - q_4))}{2} & \sin(q_5) \left( \frac{\sin(q_1 + q_2 + q_3 + q_4)}{2} - \frac{\sin(q_1 - q_2 - q_3 - q_4)}{2} \right) - \cos(q_5) \sin(q_1) & -\frac{\cos(q_1 + q_2 + q_3 + q_4)}{2} - \frac{\cos(q_1 - q_2 - q_3 - q_4)}{2} \\ \cos(q_1) \sin(q_5) + \cos(q_5) \left( \frac{\cos(q_1 + q_2 + q_3 + q_4)}{2} - \frac{\cos(q_1 - q_2 - q_3 - q_4)}{2} \right) & \cos(q_1) \cos(q_5) - \frac{\sin(q_5) (\cos(q_1 + q_2 + q_3 + q_4) - \cos(q_1 - q_2 - q_3 - q_4))}{2} & -\frac{\sin(q_1 + q_2 + q_3 + q_4)}{2} - \frac{\sin(q_1 - q_2 - q_3 - q_4)}{2} \\ \frac{\cos(q_2 + q_3 + q_4 + q_5)}{2} + \frac{\cos(q_2 + q_3 + q_4 - q_5)}{2} & \frac{\sin(q_2 + q_3 + q_4 - q_5)}{2} - \frac{\sin(q_2 + q_3 + q_4 + q_5)}{2} & -\sin(q_2 + q_3 + q_4) \\ 0 & 0 & 0 \end{pmatrix} \quad (10)$$

$$w_1 = ( 0 \quad 0 \quad 1 \quad 0 ) \quad (11)$$

$$w_2 = ( \sin(q_2) \quad \cos(q_2) \quad 0 \quad 147 ) \quad (12)$$

$$w_3 = ( \sin(q_2 + q_3) \quad \cos(q_2 + q_3) \quad 0 \quad 155 \sin(q_2) + 147 ) \quad (13)$$

$$w_4 = ( \sin(q_2 + q_3 + q_4) \quad \cos(q_2 + q_3 + q_4) \quad 0 \quad 135 \sin(q_2 + q_3) + 155 \sin(q_2) + 147 ) \quad (14)$$

$$w_5 = ( \frac{\cos(q_2 + q_3 + q_4 + q_5)}{2} + \frac{\cos(q_2 + q_3 + q_4 - q_5)}{2} \quad \frac{\sin(q_2 + q_3 + q_4 - q_5)}{2} - \frac{\sin(q_2 + q_3 + q_4 + q_5)}{2} \quad -\sin(q_2 + q_3 + q_4) \quad \frac{568 \cos(q_2 + q_3 + q_4)}{5} + 135 \sin(q_2 + q_3) + 155 \sin(q_2) + 147 )$$

$$(15)$$

$$p_1 = g \, m1 \, rz1 \quad (16)$$

$$p_2 = g \, m2 \, (ry2 \cos(q2) + rx2 \sin(q2) + 147) \quad (17)$$

$$p_3 = g \, m3 \, (155 \sin(q2) + ry3 \cos(q2 + q3) + rx3 \sin(q2 + q3) + 147) \quad (18)$$

$$p_4 = g \, m4 \, (135 \sin(q2 + q3) + 155 \sin(q2) + ry4 \cos(q2 + q3 + q4) + rx4 \sin(q2 + q3 + q4) + 147) \quad (19)$$

$$\begin{aligned} p_5 &= \frac{g \, m5 \, (1136 \cos(q2+q3+q4)+1350 \sin(q2+q3)+1550 \sin(q2)+5 \, rx5 \cos(q2+q3+q4+q5)-5 \, ry5 \sin(q2+q3+q4+q5)+5 \, rx5 \cos(q2+q3+q4-q5)+5 \, ry5 \sin(q2+q3+q4-q5)-10 \, rz5 \sin(q2+q3+q4)+1470)}{10} \\ P_1 &= \frac{g \, (1470 \, m2+1470 \, m3+1470 \, m4+1470 \, m5+10 \, m1 \, rz1+1350 \, m4 \sin(q2+q3)+1350 \, m5 \sin(q2+q3)+1550 \, m3 \sin(q2)+1550 \, m4 \sin(q2)+1550 \, m5 \sin(q2)+1136 \, m5 \cos(q2+q3+q4)+10 \, m2 \, ry2 \cos(q2)+10 \, m2 \, rx2 \sin(q2))}{10} \\ P_2 &= \frac{g \, (1470 \, m2+1470 \, m3+1470 \, m4+1470 \, m5+1350 \, m4 \sin(q2+q3)+1350 \, m5 \sin(q2+q3)+1550 \, m3 \sin(q2)+1550 \, m4 \sin(q2)+1550 \, m5 \sin(q2)+1136 \, m5 \cos(q2+q3+q4)+10 \, m2 \, ry2 \cos(q2)+10 \, m2 \, rx2 \sin(q2))}{10} \\ P_3 &= \frac{g \, (1470 \, m3+1470 \, m4+1470 \, m5+1350 \, m4 \sin(q2+q3)+1350 \, m5 \sin(q2+q3)+1550 \, m3 \sin(q2)+1550 \, m4 \sin(q2)+1550 \, m5 \sin(q2)+1136 \, m5 \cos(q2+q3+q4)+5 \, m5 \, rx5 \cos(q2+q3+q4-q5)+5 \, m5 \, ry5 \sin(q2+q3+q4-q5))}{10} \\ P_4 &= 147 \, g \, m4 + 147 \, g \, m5 + 155 \, g \, m4 \sin(q2) + 155 \, g \, m5 \sin(q2) + \frac{568 \, g \, m5 \cos(q2+q3+q4)}{5} + 135 \, g \, m4 \sin(q2 + q3) + 135 \, g \, m5 \sin(q2 + q3) + \\ \mathfrak{C} \quad &\frac{g \, m5 \, rx5 \cos(q2+q3+q4+q5)}{2} - \frac{g \, m5 \, ry5 \sin(q2+q3+q4+q5)}{2} + \frac{g \, m5 \, rx5 \cos(q2+q3+q4-q5)}{2} + \frac{g \, m5 \, ry5 \sin(q2+q3+q4-q5)}{2} + g \, m4 \, ry4 \cos(q2 + q3 + q4) + g \, m4 \, rx4 \sin(q2 + q3 + q4) - \\ &g \, m5 \, rz5 \sin(q2 + q3 + q4) \\ P_5 &= \frac{g \, m5 \, (1136 \cos(q2+q3+q4)+1350 \sin(q2+q3)+1550 \sin(q2)+5 \, rx5 \cos(q2+q3+q4+q5)-5 \, ry5 \sin(q2+q3+q4+q5)+5 \, rx5 \cos(q2+q3+q4-q5)+5 \, ry5 \sin(q2+q3+q4-q5)-10 \, rz5 \sin(q2+q3+q4)+1470)}{10} \end{aligned}$$

$$W_1 = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} \quad (20)$$

$$W_2 = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} \quad (21)$$

$$W_3 = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} \tag{22}$$

$$W_4 = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} \tag{23}$$

$$W_5 = \begin{pmatrix} 0 \\ \cos(q2) \\ 0 \\ 0 \\ 0 \end{pmatrix} \tag{24}$$

$$W_6 = \begin{pmatrix} 0 \\ -\sin(q2) \\ 0 \\ 0 \\ 0 \end{pmatrix} \tag{25}$$

$$W_7 = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} \tag{26}$$

$$W_8 = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} \tag{27}$$

$\mathfrak{S}_4$

$$W_9 = \begin{pmatrix} 0 \\ \cos(q_2 + q_3) \\ \cos(q_2 + q_3) \\ 0 \\ 0 \end{pmatrix} \tag{28}$$

$$W_{10} = \begin{pmatrix} 0 \\ -\sin(q_2 + q_3) \\ -\sin(q_2 + q_3) \\ 0 \\ 0 \end{pmatrix} \tag{29}$$

$$W_{11} = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} \tag{30}$$

$$W_{12} = \begin{pmatrix} 0 \\ 155 \cos(q_2) \\ 0 \\ 0 \\ 0 \end{pmatrix} \tag{31}$$

$$W_{13} = \begin{pmatrix} 0 \\ \cos(q_2 + q_3 + q_4) \\ \cos(q_2 + q_3 + q_4) \\ \cos(q_2 + q_3 + q_4) \\ 0 \end{pmatrix} \tag{32}$$

$$W_{14} = \begin{pmatrix} 0 \\ -\sin(q_2 + q_3 + q_4) \\ -\sin(q_2 + q_3 + q_4) \\ -\sin(q_2 + q_3 + q_4) \\ 0 \end{pmatrix} \tag{33}$$

$$W_{15} = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} \quad (34)$$

$$W_{16} = \begin{pmatrix} 0 \\ 135 \cos(q_2 + q_3) + 155 \cos(q_2) \\ 135 \cos(q_2 + q_3) \\ 0 \\ 0 \end{pmatrix} \quad (35)$$

$$W_{17} = \begin{pmatrix} 0 \\ -\frac{\sin(q_2+q_3+q_4+q_5)}{2} - \frac{\sin(q_2+q_3+q_4-q_5)}{2} \\ -\frac{\sin(q_2+q_3+q_4+q_5)}{2} - \frac{\sin(q_2+q_3+q_4-q_5)}{2} \\ -\frac{\sin(q_2+q_3+q_4+q_5)}{2} - \frac{\sin(q_2+q_3+q_4-q_5)}{2} \\ \frac{\sin(q_2+q_3+q_4-q_5)}{2} - \frac{\sin(q_2+q_3+q_4+q_5)}{2} \end{pmatrix} \quad (36)$$

$$W_{18} = \begin{pmatrix} 0 \\ \frac{\cos(q_2+q_3+q_4-q_5)}{2} - \frac{\cos(q_2+q_3+q_4+q_5)}{2} \\ \frac{\cos(q_2+q_3+q_4-q_5)}{2} - \frac{\cos(q_2+q_3+q_4+q_5)}{2} \\ \frac{\cos(q_2+q_3+q_4-q_5)}{2} - \frac{\cos(q_2+q_3+q_4+q_5)}{2} \\ -\frac{\cos(q_2+q_3+q_4+q_5)}{2} - \frac{\cos(q_2+q_3+q_4-q_5)}{2} \end{pmatrix} \quad (37)$$

$$W_{19} = \begin{pmatrix} 0 \\ -\cos(q_2 + q_3 + q_4) \\ -\cos(q_2 + q_3 + q_4) \\ -\cos(q_2 + q_3 + q_4) \\ 0 \end{pmatrix} \quad (38)$$

$$W_{20} = \begin{pmatrix} 0 \\ 135 \cos(q_2 + q_3) - \frac{568 \sin(q_2 + q_3 + q_4)}{5} + 155 \cos(q_2) \\ 135 \cos(q_2 + q_3) - \frac{568 \sin(q_2 + q_3 + q_4)}{5} \\ -\frac{568 \sin(q_2 + q_3 + q_4)}{5} \\ 0 \end{pmatrix} \quad (39)$$

$$W_{1_R} = \begin{pmatrix} -\sin(q_2) \\ 0 \\ 0 \\ 0 \end{pmatrix} \quad (40)$$

$$W_{2_R} = \begin{pmatrix} \cos(q_2 + q_3) \\ \cos(q_2 + q_3) \\ 0 \\ 0 \end{pmatrix} \quad (41)$$

$$W_{3_R} = \begin{pmatrix} -\sin(q_2 + q_3) \\ -\sin(q_2 + q_3) \\ 0 \\ 0 \end{pmatrix} \quad (42)$$

$$W_{4_R} = \begin{pmatrix} 155 \cos(q_2) \\ 0 \\ 0 \\ 0 \end{pmatrix} \quad (43)$$

$$W_{5_R} = \begin{pmatrix} \cos(q_2 + q_3 + q_4) \\ \cos(q_2 + q_3 + q_4) \\ \cos(q_2 + q_3 + q_4) \\ 0 \end{pmatrix} \quad (44)$$

$$W_{6_R} = \begin{pmatrix} -\sin(q_2 + q_3 + q_4) \\ -\sin(q_2 + q_3 + q_4) \\ -\sin(q_2 + q_3 + q_4) \\ 0 \end{pmatrix} \quad (45)$$

$$W_{7_R} = \begin{pmatrix} -\frac{\sin(q_2+q_3+q_4+q_5)}{2} & -\frac{\sin(q_2+q_3+q_4-q_5)}{2} \\ -\frac{\sin(q_2+q_3+q_4+q_5)}{2} & -\frac{\sin(q_2+q_3+q_4-q_5)}{2} \\ -\frac{\sin(q_2+q_3+q_4+q_5)}{2} & -\frac{\sin(q_2+q_3+q_4-q_5)}{2} \\ \frac{\sin(q_2+q_3+q_4-q_5)}{2} & \frac{\sin(q_2+q_3+q_4+q_5)}{2} \end{pmatrix} \quad (46)$$

$$W_{8_R} = \begin{pmatrix} \frac{\cos(q_2+q_3+q_4-q_5)}{2} & \frac{\cos(q_2+q_3+q_4+q_5)}{2} \\ \frac{\cos(q_2+q_3+q_4-q_5)}{2} & \frac{\cos(q_2+q_3+q_4+q_5)}{2} \\ \frac{\cos(q_2+q_3+q_4-q_5)}{2} & \frac{\cos(q_2+q_3+q_4+q_5)}{2} \\ -\frac{\cos(q_2+q_3+q_4+q_5)}{2} & -\frac{\cos(q_2+q_3+q_4-q_5)}{2} \end{pmatrix} \quad (47)$$

$\infty$