

Question 1

1)

ab \ cd	00	01	11	10
00	$a'b'c'd'$	$a'b'cd$	$a'bc'd$	$a'bc'd'$
01	$a'bc'd'$	$a'bc'd$	$a'bcd$	$a'bcd'$
11	$abc'd'$	$abc'd$	$abcd$	$abcd'$
10	$abc'd$	$abc'd'$	$abcd$	$abcd'$

$$F_2(A, B, C, D) = \sum m(3, 5, 7, 8, 9, 10, 11, 13, 15)$$

ab \ cd	00	01	11	10
00			1	
01		1	1	
11		1	1	
10	1	1	1	1

$\rightarrow bd$ (circled 1s at (01,11), (11,11))
 $\rightarrow ab'$ (circled 1s at (10,00), (10,01), (10,11), (10,10))
 $\rightarrow cd$ (circled 1s at (01,11), (11,11), (10,11))

$$F_2 = ab' + bd + cd$$

$$F_1(A, B, C, D) = \sum m(0, 1, 4, 5, 8, 9, 12, 13)$$

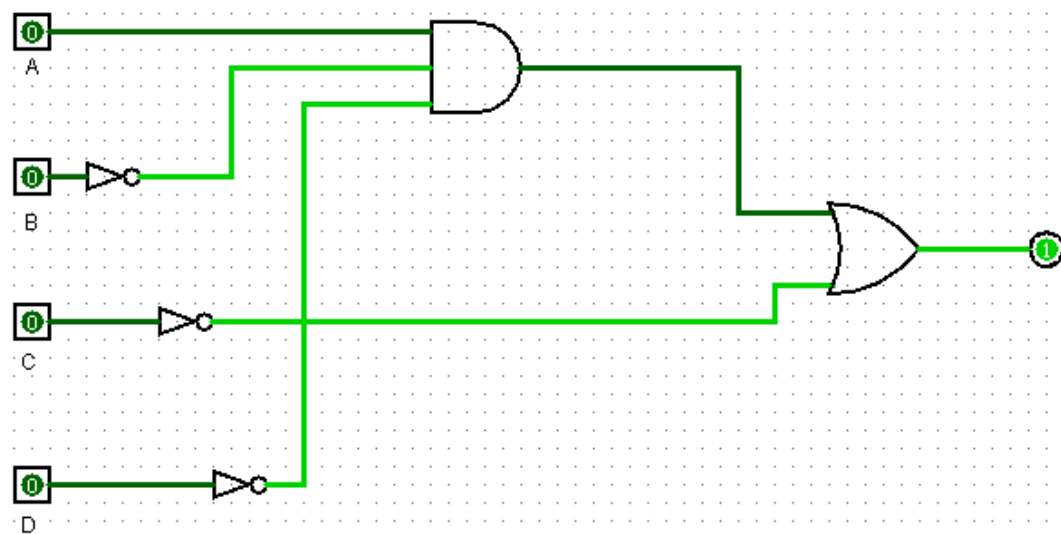
ab \ cd	00	01	11	10
00	1	1	0	0
01	1	1	0	0
11	1	1	0	0
10	1	1	0	1

$\rightarrow c'$ (circled 1s at (00,00), (01,00), (11,00), (10,00))
 $\rightarrow ab'd'$ (circled 1s at (10,00), (10,01))

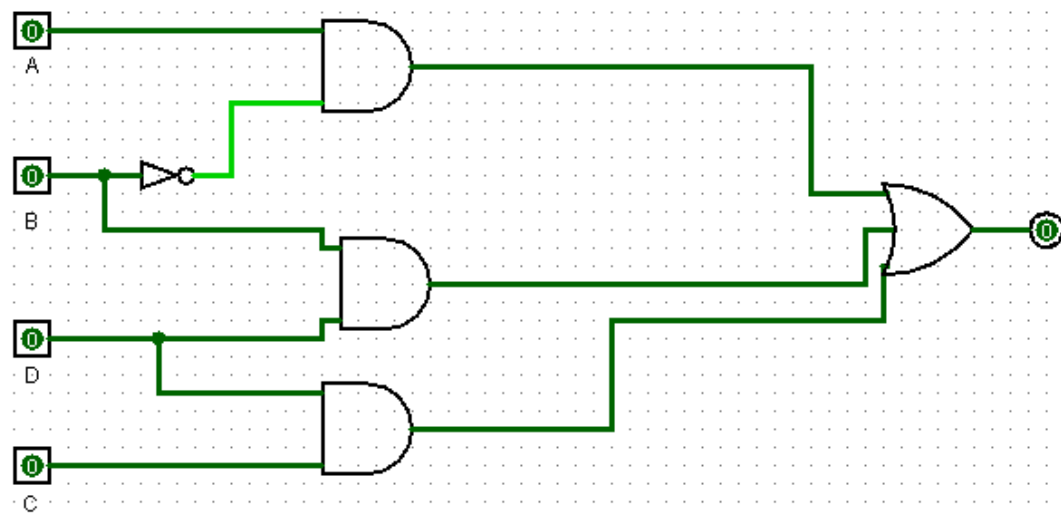
$$F_1 = c' + ab'd'$$

Question1.3

F1

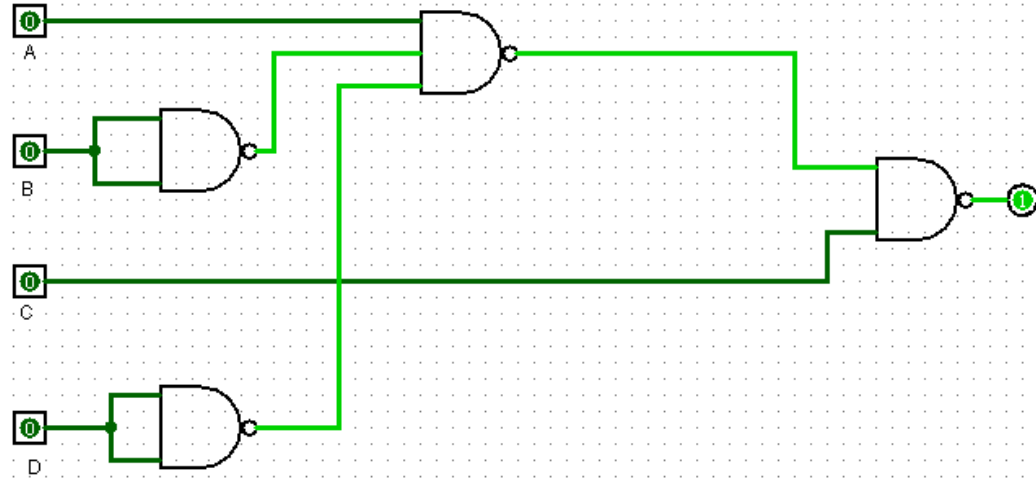


F2

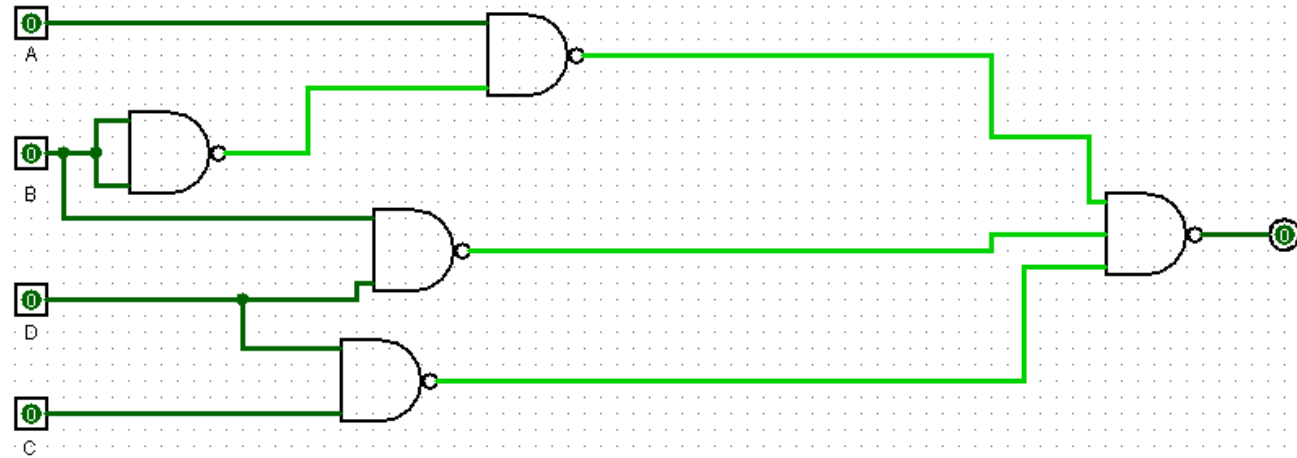


Question1.4

F1



F2



Question 2

A	B	C	D	AB'	AD	BC	CD'	AB'CD	F	
0	0	0	0	0	0	0	0	1	1	$\rightarrow A'B'C'D'm_0$
0	0	0	1	0	0	0	0	0	0	
0	0	1	0	0	0	0	1	0	1	$\rightarrow A'B'CD'm_2$
0	0	1	1	0	0	0	0	0	0	
0	1	0	0	0	0	0	0	0	0	
0	1	0	1	0	0	0	0	0	0	
0	1	1	0	0	0	0	1	0	1	$\rightarrow A'BCD'm_6$
0	1	1	1	0	0	1	0	0	1	$\rightarrow A'BCD'm_7$
1	0	0	0	1	0	0	0	0	1	$\rightarrow ABC'D'm_8$
1	0	0	1	1	1	0	0	0	1	$\rightarrow ABC'D'm_9$
1	0	1	0	1	0	1	1	0	1	$\rightarrow ABC'D'm_{10}$
1	0	1	1	1	1	1	0	0	1	$\rightarrow ABC'D'm_{11}$
1	1	0	0	0	0	0	0	0	0	
1	1	0	1	0	1	0	1	0	1	$\rightarrow ABC'D'm_{13}$
1	1	1	0	0	0	1	0	0	1	$\rightarrow ABCD'm_{14}$
1	1	1	1	0	1	1	0	0	1	$\rightarrow ABCD'm_{15}$

$$F = A'B'C'D' + A'B'CD' + ABCD' + A'BCD + AB'C'D' + AB'CD + ABC'D' + ABCD + AB'CD + ABC'D + ABCD$$

2)

AB \ CD	00	01	11	10
00	$A'B'C'D'$	$A'B'CD$	$AB'C'D$	$A'BCD$
01	$A'B'CD'$	$A'B'CD$	$A'BCD$	$A'BCD'$
11	$AB'C'D'$	$AB'CD$	$AB'CD$	$AB'CD'$
10	$AB'C'D'$	$AB'CD$	$AB'CD$	$AB'CD'$

3)

AB \ CD	00	01	11	10
00	1)	0	0	(1
01	0	0	1	1
11	0	1	1	1
10	1)	1	1	(1

$$F = B'D' + BC + AD$$

→ BC

↓ AD

4)

AB \ CD	00	01	11	10
00	1	0	0	1
01	0	0	1	1
11	0	1	1	1
10	1	1	1	1

$$F' = (A'B'D + A'BC' + BC'D')$$

Question 2.5

