

Answer 1

$$xy + x'z + yz = xy + x'z + \overset{1}{(x+x')} \cdot yz$$

$$= xy + x'z + (xyz + x'yz)$$

$$= (xy + xyz) + (x'z + x'yz)$$

$$= x'z \underset{\underset{1}{\vee}}{(1+y)} + xy \underset{\underset{1}{\vee}}{(1+z)}$$

$$= xy(1) + x'z(1)$$

$$= \underline{\underline{xy + x'z}}$$

$$xy + x'z + yz = xy + x'z$$

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Answer 2

$$(x+y) \cdot (x'+z) \cdot (y+z) = (x+y) \cdot (x'+z)$$

\Downarrow

$$((x \cdot x') + (x \cdot z) + (x' \cdot y) + (y \cdot z)) \cdot (y+z) = (x+y) \cdot (x'+z)$$

$$(x \cdot x' / y) + (x \cdot y / z) + (x \cdot z \cdot y) + (x \cdot z \cdot z) + (x' \cdot y \cdot y) + (x' \cdot y \cdot z) + (y \cdot z \cdot y) + (y \cdot z \cdot z)$$

$\begin{matrix} 0 & 0 & yz & xz & x'y & x'yz & yz & yz \end{matrix}$

$$\Rightarrow xyz + x'yz + xz + x'y + yz + yz = (x+y) \cdot (x'+z)$$

\Downarrow

$$\Rightarrow yz(x+x') + yz + yz + x'y + xz = (x+y) \cdot (x'+z)$$

\downarrow
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$$\Rightarrow yz + yz + yz + x'y + xz = (x+y) \cdot (x'+z)$$

$\underbrace{\hspace{2cm}}_{\text{same}}$

$$\Rightarrow yz + x'y + xz = (x+y) \cdot (x'+z)$$

$$(x \cdot x') + (xz) + (x'y) \cdot (yz)$$

Proof

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Answer 3

a)

A	B	C	D	B'D	A'D	BD	F	
0	0	0	0	0	0	0	0	$A+B+C+D \rightarrow M_0$
0	0	0	1	1	1	0	1	$A'B'C'D \rightarrow m_1$
0	0	1	0	0	0	0	0	$A+B+C'+D \rightarrow M_2$
0	0	1	1	1	1	0	1	$A'B'CD \rightarrow m_3$
0	1	0	0	0	0	0	0	$A+B'+C+D \rightarrow M_4$
0	1	0	1	0	1	1	1	$A'BC'D \rightarrow m_5$
0	1	1	0	0	0	0	0	$A+B'+C'+D \rightarrow M_6$
0	1	1	1	0	1	1	1	$A'BCD \rightarrow m_7$
1	0	0	0	0	0	0	0	$A'+B+C+D \rightarrow M_8$
1	0	0	1	1	0	0	1	$AB'C'D \rightarrow m_9$
1	0	1	0	0	0	0	0	$A'+B+C'+D \rightarrow M_{10}$
1	0	1	1	1	0	0	1	$AB'CD \rightarrow m_{11}$
1	1	0	0	0	0	0	0	$A'+B'+C+D \rightarrow M_{12}$
1	1	0	1	0	0	1	1	$ABC'D \rightarrow m_{13}$
1	1	1	0	0	0	0	0	$A'+B'+C'+D \rightarrow M_{14}$
1	1	1	1	0	0	1	1	$ABCD \rightarrow m_{15}$

Sum of minterms

$$F(A,B,C,D) = A'B'C'D + A'B'CD + A'BC'D + A'BCD + AB'C'D + AB'CD + ABC'D + ABCD$$

$$= \Sigma (1, 3, 5, 7, 9, 11, 13, 15)$$

Product of Maxterms

$$F(A,B,C,D) = (A+B+C+D) \cdot (A+B+C'+D) \cdot (A+B'+C+D) \cdot (A+B'+C'+D) \cdot (A'+B+C+D) \cdot (A'+B+C'+D) \cdot (A'+B'+C+D) \cdot (A'+B'+C'+D)$$

$$= \Pi (0, 2, 4, 6, 8, 10, 12, 14)$$

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answer 3

$$b) F(A, B, C, D) = B'D + A'D + BD$$

$$= (B'D) \cdot \underbrace{(C+C')}_1 + (A'D) \cdot \underbrace{(C+C')}_1 + B \cdot D \cdot \underbrace{(C+C')}_1$$

$$= (B'DC) + (B'DC') + (A'DC) + (A'DC') + (BDC) + (BDC')$$

$$= (B'DC)(\underbrace{A+A'}_1) + (B'DC')(\underbrace{A+A'}_1) + (A'DC)(\underbrace{B+B'}_1) + (A'DC')(\underbrace{B+B'}_1) + (BDC)(\underbrace{A+A'}_1) + (BDC')(\underbrace{A+A'}_1)$$

$$= (B'DCA) + (B'DCA') + (B'DC'A) + (B'DC'A') + (A'DCB) + (A'DCB') + (A'DC'B) + (A'DC'B') + (BDC A) + (BDC A') + (BDC'A) + (BDC'A')$$

$$\Sigma(1, 3, 5, 7, 9, 11, 13, 15)$$

$$\Sigma(1, 3, 5, 7, 9, 11, 13, 15) = \Pi(0, 2, 4, 6, 8, 10, 12, 14)$$

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