# Disadoption Contagion: Conceptual Framing and Methods

(compiled for the KFP project)

## Overview

This note formalizes "disadoption contagion" for the Korean Family Planning (KFP) data and outlines estimands and models that leverage the general time—by—state information encoded in TOA\_derivado\_general. The aim is to (i) clarify concepts and operational definitions for adoption vs. disadoption, (ii) collapse 21 detailed states to three meta-states when needed, and (iii) propose regression designs—event—history for *stable* disadoption and panel/transition models for *temporary* disadoption—. Conceptual scaffolding follows my document (see §4.3 and Eq. (7))

### 1 Introduction

## 1.1 Adoption vs. Disadoption in the classical framework

Classical diffusion treats adoption as a one–off, irreversible event per ego ("time of adoption", TOA). In real usage data, contraceptive behavior fluctuates: egos can move from a modern method to traditional/no use and later revert. Thus, while the *adoption* construct is convenient for event–history modeling, observed trajectories reveal multiple episodes of adopting and disadopting across time.

#### 1.2 What is observed in TOA\_derivado\_general

With the period-by-ego status matrix ( $1047 \times 11$ ) and complete state labels (21 categories), heatmaps and random trajectories show frequent switching. This richer object validates the standard TOA reconstruction (so it is *consistent* with Valente's prior work, see Table 10-2 from Valente's 2010 book) while enabling analyses beyond a single adoption event: repeated adoptions, disadoptions, and state sojourns.

#### 1.3 Collapsing to three meta-states

For interpretability and to focus on behavioral macro-shifts, I collapse states to:

```
Modern = {Loop, Pill, Condom, Vasectomy, TL, Injection}
Traditional = {Rhythm, Withdrawal, etc.}
NoUse = {NormalB, Want More, No more, Pregnant, Infertile, Abortion, ...}.
```

This yields a categorical process  $S_{it} \in \{Modern, Traditional, NoUse\}$  for ego i at period t.

#### 1.4 Disadoption as recurrent events

Under this view, *disadoption* is any transition leaving Modern:

$$\mathsf{Modern} \to \mathsf{Traditional}$$
 or  $\mathsf{Modern} \to \mathsf{NoUse}$ .

These transitions can be recurrent: the same ego can disadopt, then re-adopt, multiple times.

#### 1.5 Exposure to disadoption

Mirroring adoption exposure, I define disadoption exposure as the local prevalence of alters who have *left* modern use. A convenient construction (Eq. (7) in my document) uses the gap between the *maximum adoption exposure* attained and the current adoption exposure at t:

$$E_i^D(t) = E_i^{\max} - E_i(t),$$

where  $E_i(t)$  is the standard cohesion exposure to *current* modern users among *i*'s alters, and  $E_i^{\max} := \max_{u \leq t} E_i(u)$ . Intuitively, when many neighbors who *used to* be modern stop being modern,  $E_i(t)$  falls below its past peak and  $E_i^D(t)$  grows.

## 1.6 Temporary vs. Stable disadoption

- Temporary disadoption: any period with  $S_{it} \neq \text{Modern}$  after being modern earlier, regardless of eventual return.
- Stable disadoption: the *last* exit from Modern followed by no return up to the observation horizon; formally, the terminal transition Modern → {Traditional, NoUse} with no subsequent Modern.

### 1.7 Implications for modeling

- For **stable** disadoption, an event-history (survival / discrete-time hazard) design aligns with the single "terminal" event per ego.
- For **temporary** disadoption, a panel transition model (multinomial or binary flows per period) captures repeated moves with time-varying exposures.

### 2 Methods

#### 2.1 Notation and inputs from TOA\_derivado\_general

Let  $\mathcal{N}_i$  be *i*'s alters (per period),  $A_{ij}(t) \in \{0,1\}$  the adjacency matrix, and  $M_j(t) = \mathbf{1}\{S_{jt} = \mathsf{Modern}\}$ , that is, if *j* has adopted a modern method. Define the (cohesion) adoption exposure for ego *i* at *t*:

$$E_i(t) = \frac{\sum_{j \in \mathcal{N}_i} A_{ij}(t) M_j(t-1)}{\sum_{j \in \mathcal{N}_i} A_{ij}(t)}$$
 (lagged by one period).

Then  $E_i^{\max}(t) = \max_{u \le t} E_i(u)$  and the disadoption exposure

$$E_i^D(t) = E_i^{\max}(t) - E_i(t) \in [0, 1].$$

Optionally incorporate homophily/SE weighting, or village—level terms (e.g., cumulative disadoptions in the village at t) as additional covariates.

## 2.2 Stable disadoption: discrete-time event history

Define the at-risk set  $\mathcal{R}_t = \{i : S_{i,t-1} = \mathsf{Modern}\}$  and event indicator  $Y_{it} = \mathbf{1}\{S_{i,t} \neq \mathsf{Modern}\}$ , restricted to the last exit from Modern (one terminal event per ego). The logit hazard:

logit 
$$\Pr\{Y_{it} = 1 \mid \mathcal{F}_{t-1}\} = \alpha_t + \beta_D E_i^D(t) + \beta_E E_i(t) + \gamma_{\text{deg}}^{\top} \mathbf{d}_i(t) + \gamma_{\text{med media}_i} + \gamma_{\text{kids children}_i} + \delta_g \text{CumDisadopt}_{q(i)}(t) + \varepsilon_i,$$

where  $\mathcal{F}_{t-1}$  is the information set available up to time t-1,  $\alpha_t$  is a period effect (or linear trend t),  $\mathbf{d}_i(t) = \{\deg_{\mathrm{in}}, \deg_{\mathrm{out}}\}$ , and  $\mathrm{CumDisadopt}_{g(i)}(t)$  is the village-level cumulative number (or share) of disadopters up to t. Interpretation:

- $\beta_D > 0$  implies that larger falls from past peak adoption exposure among *i*'s neighbors (i.e., more neighbors who *used to* be modern and no longer are) increase *i*'s terminal disadoption hazard.
- $\beta_E < 0$  (often) reflects protection against disadoption when current neighbor modern use is high.

This mirrors adoption models (Valente 2010) but reverses the risk set and uses  $E_i^D(t)$  as the social signal of disadoption pressure.

#### 2.3 Temporary disadoption: panel/transition designs

Because egos can leave and re—enter Modern repeatedly, period—by—period transitions can be used. Two practical options:

(T1) Binary flow from Modern. Among i with  $S_{i,t-1} = Modern$ , model

$$\text{logit } \Pr\{S_{it} \neq \mathsf{Modern}\} = \alpha_t + \beta_D E_i^D(t) + \beta_E E_i(t) + \gamma^\top \mathbf{X}_i(t),$$

with  $\mathbf{X}_i(t)$  as above. This estimates any exit from Modern (temporary or stable). Clustered SEs by ego or random effects can account for repeated observations.

(T2) Multinomial three-way flow. For all i,

$$\Pr\{S_{it} = s \mid S_{i,t-1}\} = \operatorname{softmax}_s \Big(\alpha_{s,t} + \beta_{D,s} E_i^D(t) + \beta_{E,s} E_i(t) + \gamma_s^\top \mathbf{X}_i(t)\Big), \quad s \in \{\mathsf{Modern}, \mathsf{Traditional}, \mathsf{NoUse}\}.$$

This distinguishes Modern  $\rightarrow$  Traditional vs. Modern  $\rightarrow$  NoUse and can quantify possibly different social signals behind each pathway (e.g., method substitution vs. cessation).

## 2.4 Constructing $E^D$ in practice

To construct the disadoption exposure  $E^D$ , I need to:

- 1. Build  $M_i(t)$  from the collapsed meta-states in TOA\_derivado\_general.
- 2. Compute  $E_i(t)$  with period-t-1 neighbor states and the relevant adjacency (cohesion; optionally SE-weighted).
- 3. Track  $E_i^{\text{max}}(t)$  and form  $E_i^D(t) = E_i^{\text{max}}(t) E_i(t)$ .
- 4. Optionally normalize by degree or smooth via moving maxima to reduce noise in short runs.

#### 2.5 Controls and identification notes

- Period dynamics: use  $\alpha_t$  (FE) or a parametric trend  $(t, t^2)$ . The FE absorbs common shocks (program intensity, information waves).
- Village context: include village FE and/or village—level cumulative disadoption to net out local saturation.
- Degrees & media/children: mirror the adoption models so comparisons are on like–for–like covariate sets.
- Repeated observations: cluster by ego; for multinomial/panel logit, use random effects or GEE for robustness.
- Interpretation:  $\beta_D$  captures social signal of leaving modern methods;  $\beta_E$  captures contemporaneous anchor to stay.

## 3 Intuition and reading the coefficients

Why  $E^D$  works. When many of your alters who had been modern switch away, your current adoption exposure drops below what you previously experienced. That gap is a direct signal that "people like me are leaving," which can create social permission or pressure to disadopt. Conversely, a high  $E_i(t)$  anchors continued use by indicating strong modern adherence now.

## 4 Reporting

- For stable disadoption, odds ratios (or discrete-time hazards) for  $E^D$  and E with period/village FE and the usual covariates can be reported.
- $\bullet$  For temporary disadoption, transition probability matrices by period, and marginal effects from (T1)/(T2) can be provided.
- Contrasts with adoption models to show asymmetries (e.g.,  $|\beta_D|$  vs.  $|\beta_E|$ ) can be made.