



Networks Decide for Us:

When networks shape behavior more than intentions

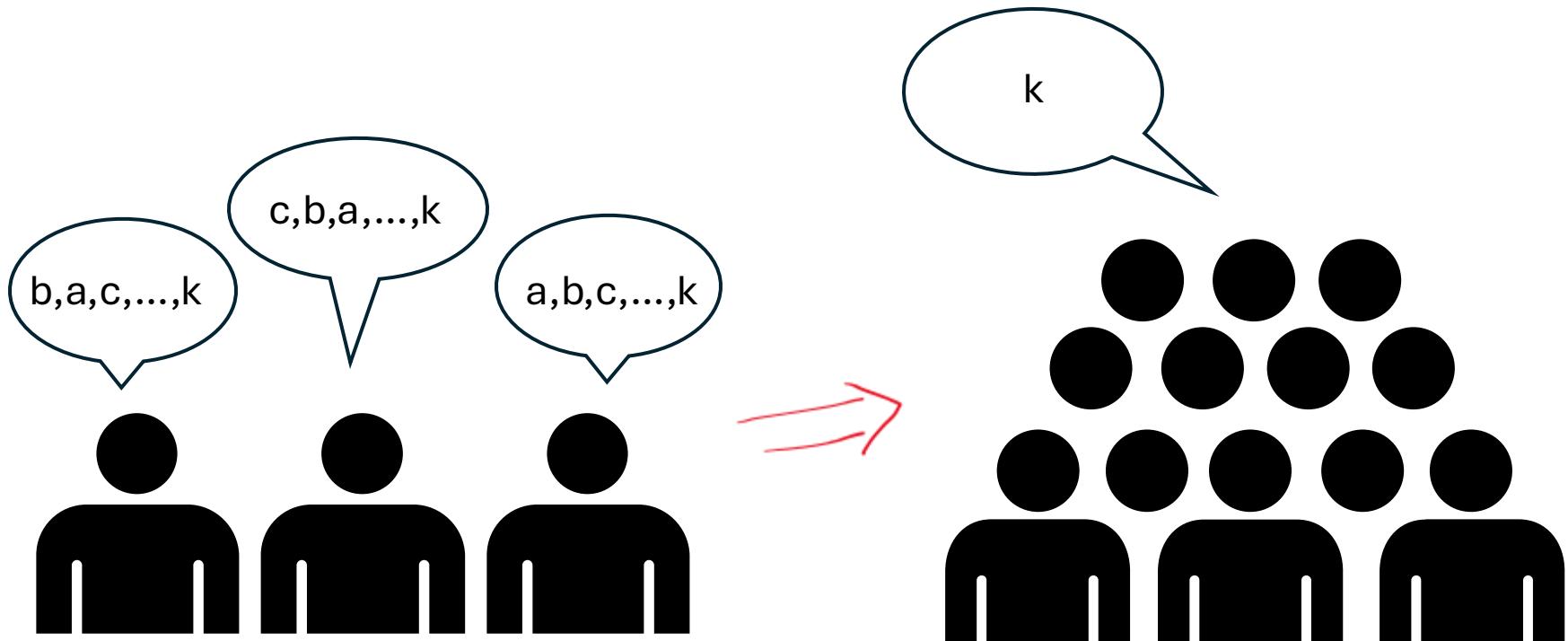
Aníbal Olivera M.

PhD(c) in Social Complexity Sciences, CICS, Santiago, Chile.

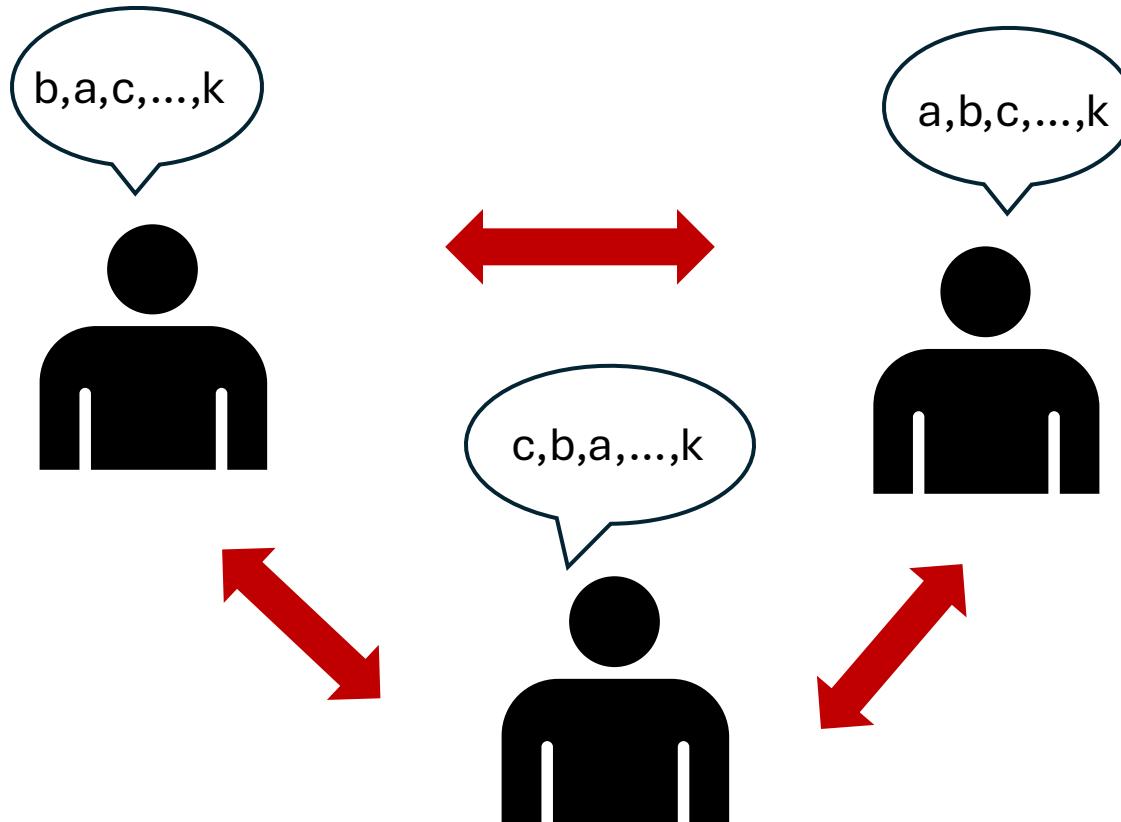
1. Motivation
 1. Collective behaviors
 2. Previous works
 3. Addressing the flaws
2. The model
 1. Rational choice
 2. Social reinforcement with selective influence
3. Setting up
 1. Imputing a Network Structure to a Survey
 2. Running the simulations
4. Results up
 1. Heatmaps
 2. Regression tables
5. Conclusion

Motivation

Collective behaviors

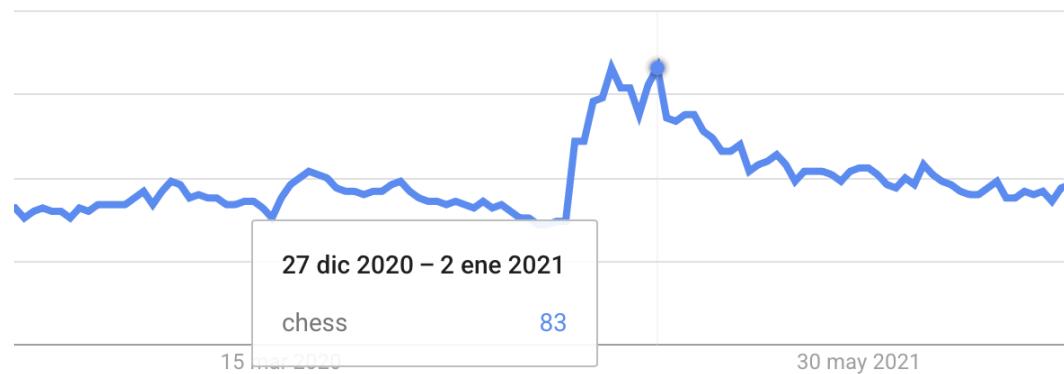


Collective behaviors



Some examples

Google Trends: Chess



Some examples

The screenshot shows a news article from The Guardian. At the top, there's a navigation bar with links for Opinion, Sport, Culture, Lifestyle, and a menu icon. Below that is a secondary navigation bar with links for Banking, Money, Markets, Project Syndicate, B2B, and Retail. The main title of the article is "GameStop: how Reddit amateurs took aim at Wall Street's short-sellers" by Rob Davies. A subtitle reads "Analysis: Understanding short-selling enabled amateur traders to beat hedge funds at their own game". Below the text is a photograph of a GameStop store front at night. To the right of the article, there's a sidebar titled "Most viewed" featuring several thumbnail images and titles of other popular articles.

Opinion | Sport | Culture | Lifestyle | ☰

Banking Money Markets Project Syndicate B2B Retail

• This article is more than 4 years old

Analysis

GameStop: how Reddit amateurs took aim at Wall Street's short-sellers

Rob Davies

Analysis: Understanding short-selling enabled amateur traders to beat hedge funds at their own game

The Guardian

Int ▾

Most viewed

- US military kills two in strike on alleged d trafficking boat in Pa
- Jewish figures across globe call on UN and leaders to sanction Is
- Live Nato chief says Donald Trump is 'the only one who can get this done' on Ukraine war - US pol live
- Trump says he has finished paying himself \$250m in past investigations
- Stephen Colbert on White House East Wing demolition: 'So deep and unsettling'

Some examples

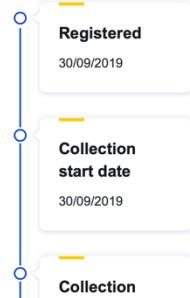
Home > Initiatives > Save bees and farmers ! Towards a bee-friendly agriculture for a healthy environment

Save bees and farmers ! Towards a bee-friendly agriculture for a healthy environment



Commission registration number: ECI(2019)000016

Initiative progress



Information from the European Commission

30/09/2019

[Commission Decision on the registration of the citizens' initiative](#)

Answer of the European Commission

05/04/2023

[Commission's answer and follow-up](#)

Communication

English [Download](#)

Available languages (23) ▾

Some examples

[HOME](#) [SEARCH](#)

The New York Times

U.S. Find Alternatives to Rare Earths	U.S. Expands Antidrug Campaign With Strike on Boat in Pacific Near Colombia	Former Biden and Senate Counsel to Lead Progressive Legal Group	Maine U.S. Senate Candidate Says He Covered Up Tattoo That Had Nazi Imagery	The NATO chief and Trump will discuss support for Ukraine.	Nancy Pelosi Hasn't 2026 Plans. Scott Wi Anyway.
---	---	---	---	--	--

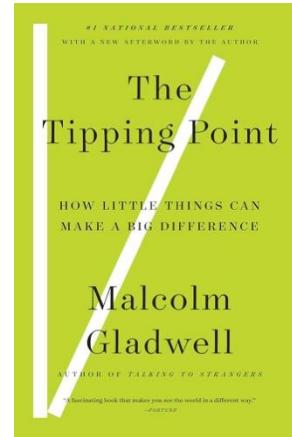
Crowd Scientists Say Women's March in Washington Had 3 Times as Many People as Trump's Inauguration

By TIM WALLACE and ALICIA PARLAPIANO UPDATED JAN. 22, 2017



Collective behaviors

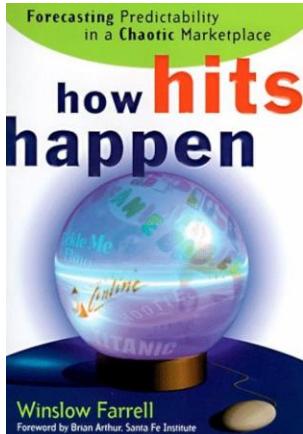
1. Hush Puppies rapid growth in 95'
2. East New York and Brownsville crime reduction
3. Abrupt growth of fax users
4. Book: Divine Secrets of the Ya-Ya Sisterhood



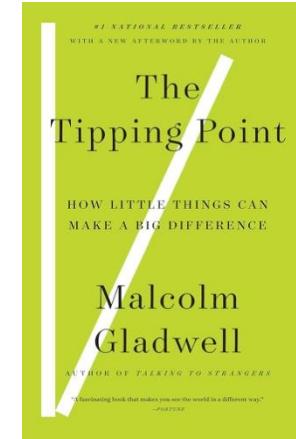
[1]

Collective behaviors

1. Hush Puppies rapid growth in 95'
2. East New York and Brownsville crime reduction
3. Abrupt growth of fax users
4. Book: Divine Secrets of the Ya-Ya Sisterhood



[2]



[1]

1. Movies: The Full Monty
2. Market Share: AT&T
3. Literature: Hootie & the Blowfish

How are those collective behaviors studied?

Two main pathways of research - Collective Actions [3]

Collective action: “*any action which provides a collective good.*”

1. (**Pre Olson**): people with shared interests would naturally act together. It was the *inaction* that required explanation.
2. **The Logic of Collective Action** (65'), Olson argued that self-interested individuals will not act to achieve their common interests. Collective action is "*Irrational*".
3. **Individual Decision Models**: pure economic models, costs and benefits. Types of *incentives*: material (money, jobs), solidary (social status, friendship, praise), and purposive (the moral satisfaction of "doing the right thing").
4. **Collectivity Models**: they examine how individual actions are aggregated into a collective outcome through social *interaction* and *coordination*.
 - 4.1 **Critical Mass Theory**: collective action depends not on the "average" member, but on a small core of highly interested and resourceful individuals.
 - 4.2 Granovetter's **Threshold Model** (78'): an individual's willingness to act depends on the number of others who are already participating.

Two main pathways of research - Collective Actions [3]

Threshold Models [4] :

*“The **threshold** is simply that point where the perceived benefits to an individual of doing the thing in question exceed the perceived costs.”*

	<u>The Group's Thresholds</u>	<u>Final Result</u>
Case A:	[0, 1, 2, 3, 4, 5, 6, 7, 8, 9]	Total Actors = 10
Case B:	[0, 2, 2, 3, 4, 5, 6, 7, 8, 9]	Total Actors = 1

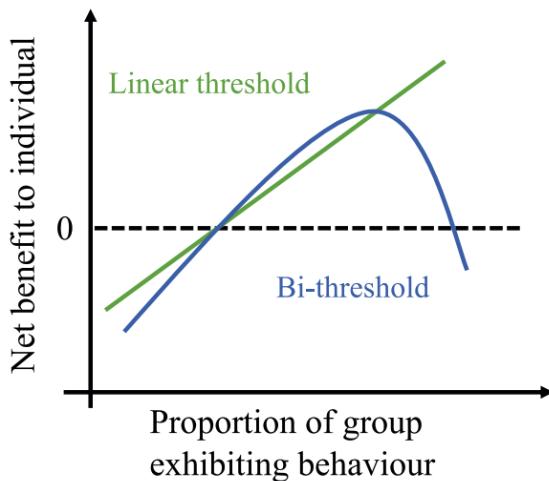
Almost identical group composition produces opposite results.

*“... the analysis is meant to apply to any appropriate binary decision.
(...) Rumors, Strikes, Voting, **Diffusion of Innovation**, etc.”*

Two main pathways of research - Collective Actions [3]

Threshold Models [4] :

*“The **threshold** is simply that point where the perceived benefits to an individual of doing the thing in question exceed the perceived costs.”*



Thresholds denote the point where utility is positive, **not preferences**.

Two main pathways of research - Diffusion of Innovations [5]

Diffusion of Innovations [4]: “*a theoretical approach used to explain how new ideas and practices spread within and between communities.*”

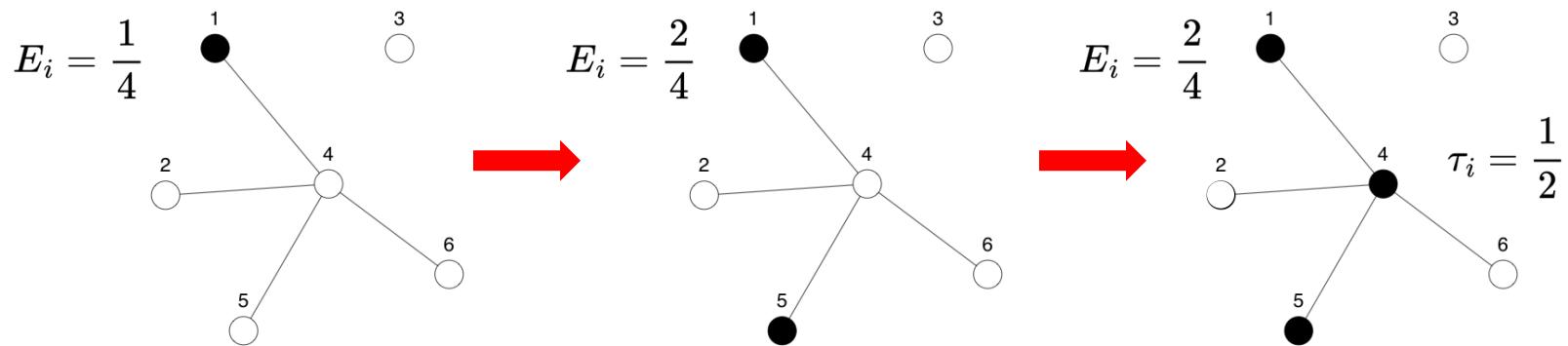
1. Roger's **S-shaped** curve of adoption (70'). Innovators - Early Adopters - Early Majority - Late Majority -Laggards. It answered *who* adopts and *when*, and the *why* was largely attributed to psychological profiles.
2. Granovetter's **Threshold Model** (78'): adoption act depends on the number of others who are already participating. No relational structure.
3. Valente's **Network Threshold Model** (95'): Your decision to adopt a new technology isn't based on national statistics; it's based on your personal social network.

$$E_i \equiv \frac{\sum_{j \neq i} \mathbf{X}_{ij} a_j}{\sum_{j \neq i} \mathbf{X}_{ij}}, \quad a_i = \begin{cases} 1 & \text{if } \tau_i \leq E_i \\ 0 & \text{otherwise} \end{cases}$$

Two main pathways of research

Valente's Network Threshold Model [5] :

$$E_i \equiv \frac{\sum_{j \neq i} \mathbf{X}_{ij} a_j}{\sum_{j \neq i} \mathbf{X}_{ij}}, \quad a_i = \begin{cases} 1 & \text{if } \tau_i \leq E_i \\ 0 & \text{otherwise} \end{cases}$$



Two main pathways of research

Table 10–2. Event History Analysis of Factors Associated with Adoption for the Three Diffusion Network Datasets

	Medical Innovation	Brazilian Farmers	Korean Family Planning
No.	947	10,092	7,103
Time	132.7**	5.14	4.34
Cumulative adoption	0.03	2.27	0.32
Number sent	1.04	0.99	1.02
Number received	1.05	1.01	1.05**
Cohesion exposure	1.05	1.93**	2.08**
Structural equivalence exposure	1.04	5.01**	1.34
Science orientation	0.65**		
Journal subscriptions	1.67		
Cosmopolitan-ness		1.00	
Income		1.14**	
Number of children			1.23**
Media exposure			1.03*



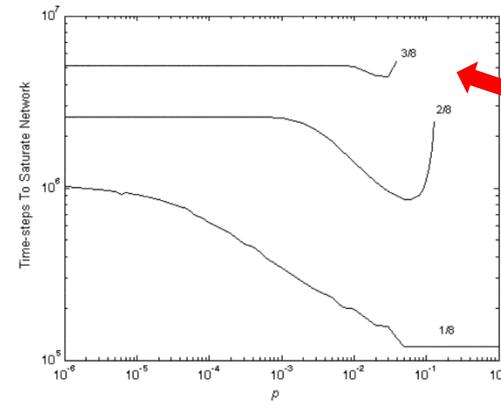
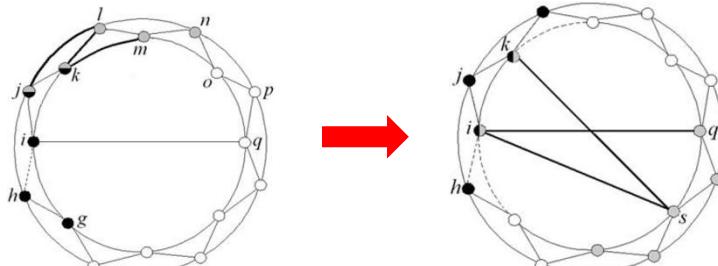
Coefficients are adjusted odds ratios for likelihood of adoption. Estimates adjusted for clustering within community.

* $p < .05$; ** $p < .01$.

Previous works

Centola [6] called it **Complex Contagion**.

- While the rewiring is higher:
- We get an abrupt barrier in diffusion:

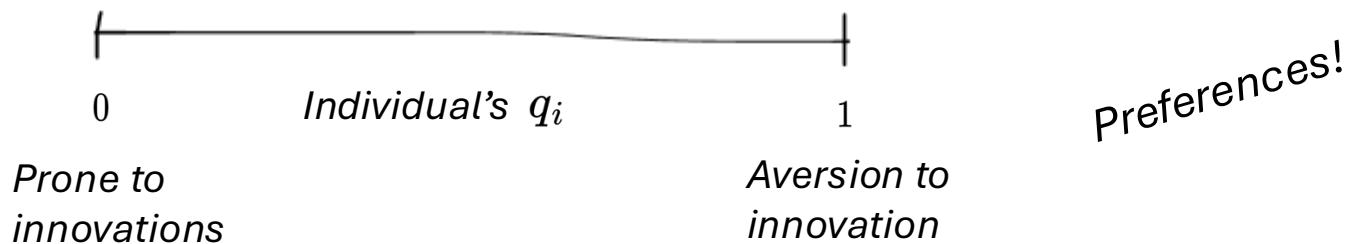


Pure structural
phase transition

Previous works

Others [4, 5] use *Percolation Theory* instead to construct a word-of-mouth diffusion model.

- An innovation has an *Intrinsic Utility Level* (IUL) $\Gamma \in [0, 1]$
- Individuals are entirely characterized by
 - 1) their network position
 - 2) an attribute of *Minimum Utility Requirement* (MUR) $q_t^i \in [0, 1]$



Previous works

Others [4, 5] use *Percolation Theory* instead to construct a word-of-mouth diffusion model.

- An innovation has an *Intrinsic Utility Level* (IUL) $\Gamma \in [0, 1]$
- Individuals are entirely characterized by
 - 1) their network position
 - 2) an attribute of *Minimum Utility Requirement* (MUR) $q_t^i \in [0, 1]$
- There is an influence driven by adopters

$$q_t^i = q_0^i \left(\frac{1}{\sum_{j \neq i} \mathbf{X}_{ij} a_j} \right)^\alpha, \quad \alpha > 0$$

- Finally adopt if $q_t^i \leq \Gamma$.

Their fails

But the models use only synthetic data:

1. Small World topology
2. Random MUR from a distribution $X \sim U(0, 1)$
3. Global influence parameter α

$$q_t^i = q_0^i \left(\frac{1}{\sum_{j \neq i} \mathbf{X}_{ij} a_j} \right)^\alpha$$


When it comes to peer influence, those dyads that are more similar to each other have greater influence [8].

Their fails

But the models use only synthetic data:

1. Small World topology
2. Random MUR from a distribution $X \sim U(0, 1)$
3. Global influence parameter α

Some criticism has arisen due to the ‘*structural reductionism*’ of these works:

- “*This literature often treats agents as cognition-free ‘structural dopes,’ operating like **relay stations** whose only purpose is to automatically respond to external stimuli.*” [6]
- **Fewer attention to more realistic setups.**

Addressing the flaws

We want to see the effect of word-of-mouth diffusion with:

1. Plausible network topologies
2. The right MUR distribution
3. Tie-specific influence parameter $\alpha = \alpha_{ij}$

The model

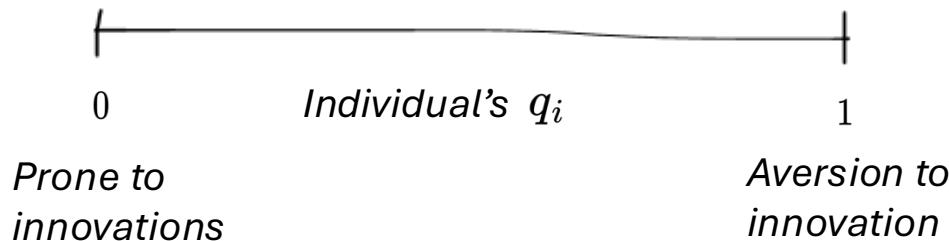
3. Tie-specific influence parameter $\alpha = \alpha_{ij}$

The model

1. Let's assume an 'innovation' has an *Intrinsic Utility Level* (IUL) $\Gamma \in [0, 1]$, which characterize the attractiveness of that innovation.



2. And individuals with *Minimum Utility Requirement* (MUR) $q_i \in [0, 1]$.

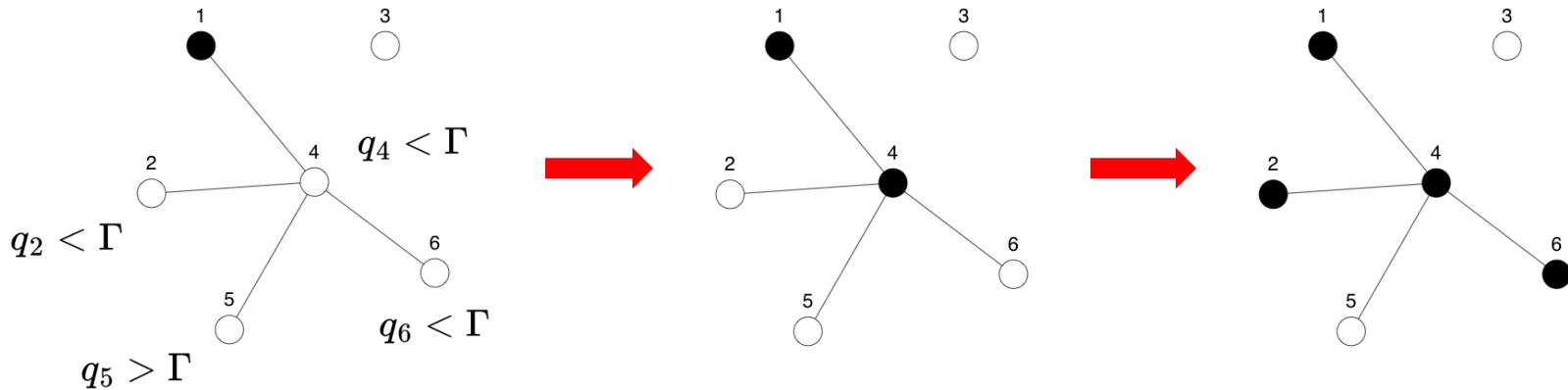


The model

Adoption can happen in two ways:

- 1) Rational Choice: i adopt if $\text{Minimum Utility Requirement} \leq \text{Intrinsic Utility Level}$

$$q_i \leq \Gamma \quad \Rightarrow a_i = 1$$



The model

2) Selective Social Influence:

$$E_i \equiv \frac{\sum_{j \neq i} \mathbf{X}_{ij} a_j}{\sum_{j \neq i} \mathbf{X}_{ij}}, \quad a_i = \begin{cases} 1 & \text{if } \tau_i \leq E_i \\ 0 & \text{otherwise} \end{cases}$$

The model

2) Selective Social Influence:

$$\tilde{E}_i \equiv \frac{\sum_{j \neq i} \mathbf{X}_{ij} \tilde{a}_j}{\sum_{j \neq i} \mathbf{X}_{ij}}, \quad a_i = \begin{cases} 1 & \text{if } \tau_i \leq \tilde{E}_i \\ 0 & \text{otherwise} \end{cases}$$

Here, \tilde{a}_i accounts for those infected individuals who are *influential*:

$$\tilde{a}_i = 1 \Leftrightarrow a_i = 1 \wedge U_{ij} \leq \sigma(h - d_{ij}), \quad U_{ij} \sim \text{Unif}(0, 1).$$

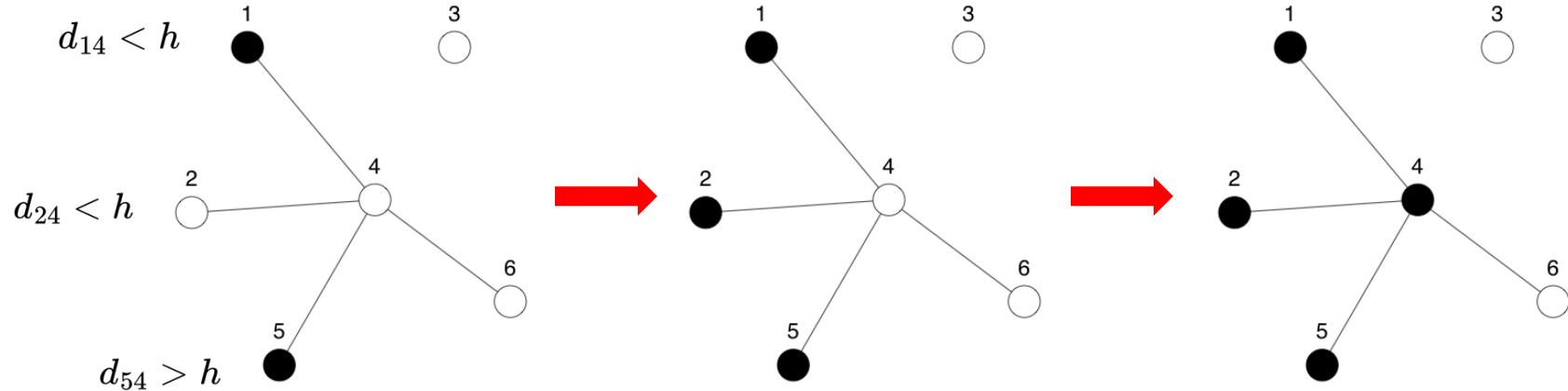
where:

1. d_{ij} is the social distance between individuals i and j ,
2. h is the *Maximum Social Proximity* (MSP), which measures the flexibility to be influenced by a person with different demographics.

The model

2) Selective Social Influence:

Let's set $\tau_4 = 0.5$; then, because the variability among the ties [6]...



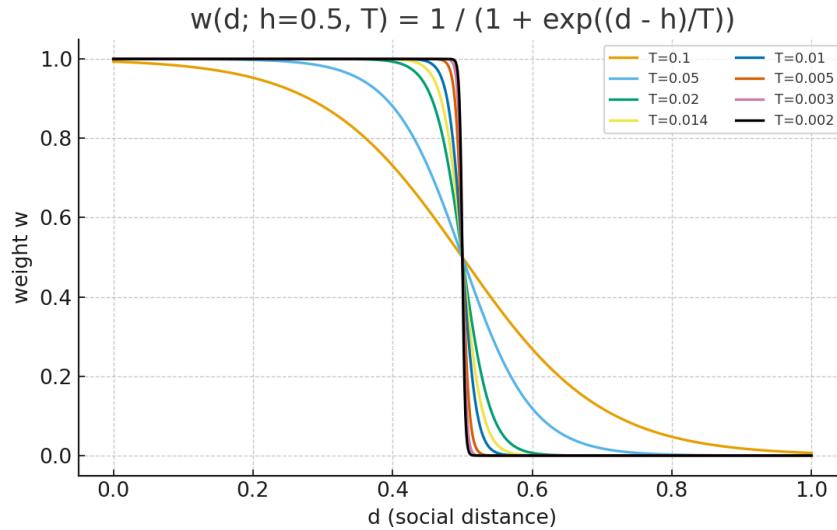
The model

2) Selective Social Influence:

$$\tilde{a}_i = 1 \Leftrightarrow a_i = 1 \wedge U_{ij} \leq \sigma(h - d_{ij}), \quad U_{ij} \sim \text{Unif}(0, 1).$$

Where:

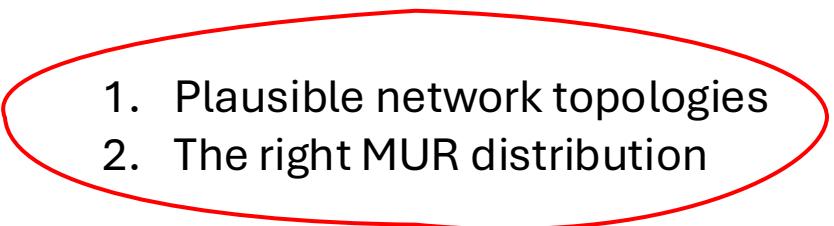
$$\sigma(z) = \frac{1}{1 + \exp(-z/T)}$$



Setting up

—

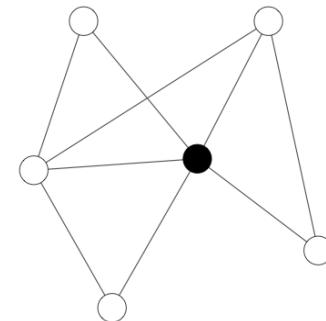
Diffusion of Innovations

- 
1. Plausible network topologies
 2. The right MUR distribution

Imputing network structure to a Survey

Following McPherson and Smith (2019) [7], **you can impute a network structure** on any other survey if:

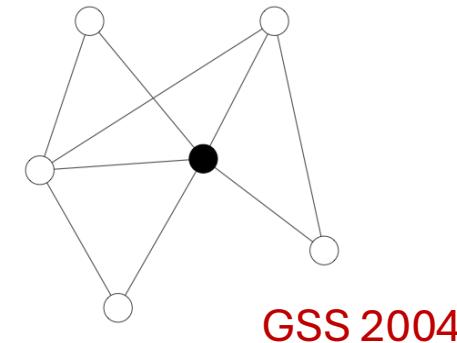
- 1) There is a survey with representative EGO-data,
- 2) Both are representative of the same population,
- 3) Both have some basic demographic variables.



Imputing network structure to a Survey

General Social Survey (GSS 2004):

1. Representative of the US population
2. Demographics:
Age - Sex - Years of Educ – Race - Religion
3. EGO data



American Trends Panel (ATP 2014):

1. Representative of the US population
2. Demographics:
Age - Sex - Years of Educ – Race - Religion
3. EGO data ‘Openness to Innovations’ items

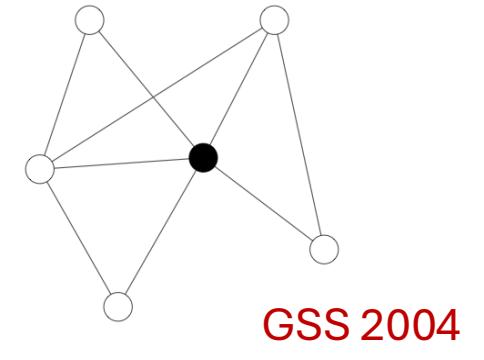
	id ₁	id ₂	id ₃	...
Age	36	27	41	...
Educ	12	15	16	...
q_i	.54	.67	.32	...
...

ATP 2014

Imputing network structure to a Survey

General Social Survey (GSS 2004):

1. Representative of the US population
2. Demographics:
Age - Sex - Years of Educ – Race - Religion
3. EGO data



American Trends Panel (ATP 2014):

1. Representative of the US population
2. Demographics:
Age - Sex - Years of Educ – Race - Religion
3. EGO data ‘*Openness to Innovations*’ items

GSS 2004



Homophilic strength
in the m -th
social dimension

Imputing network structure to a Survey

General Social Survey ([GSS 2004](#)):

1. Representative of the US population

2. Demographics:

Age - Sex - Years of Educ – Race - Religion

3. EGO data

American Trends Panel ([ATP 2014](#)):

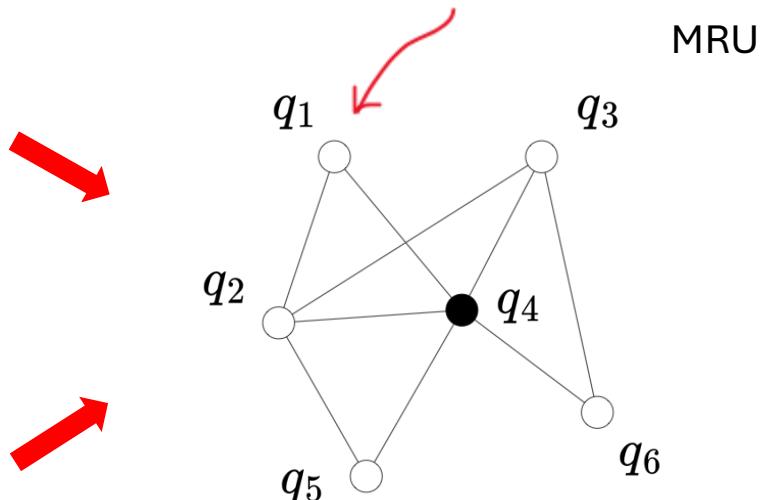
1. Representative of the US population

2. Demographics:

Age - Sex - Years of Educ – Race - Religion

3. EGO data ‘Openness to Innovations’ items

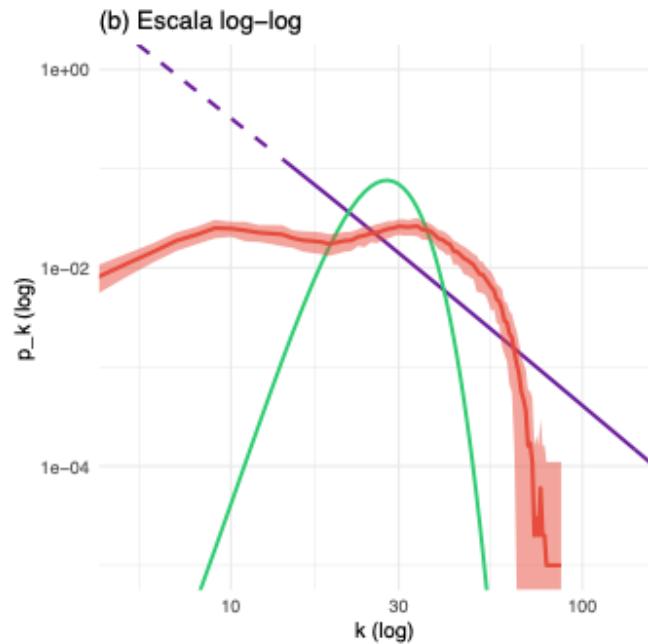
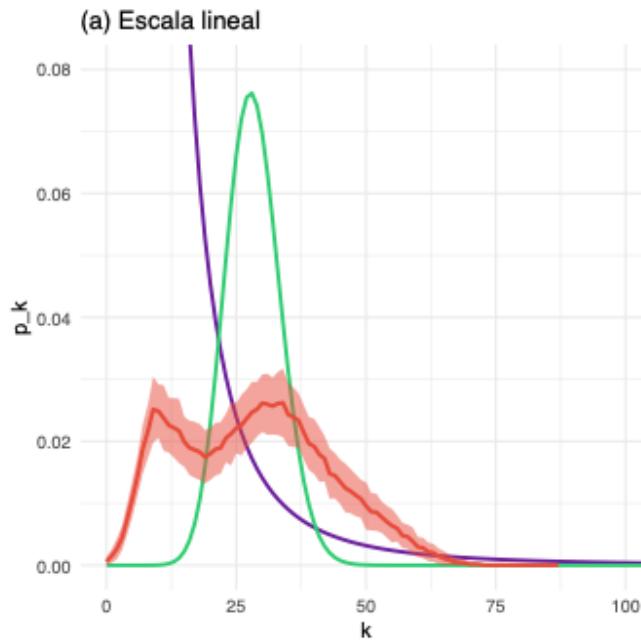
Nodes have ‘*Openness to Innovations Score*’



ATP 2014 +
Network structure

Imputing network structure to a Survey

We can use that procedure to create networks with the **right topology** [8] via ERGM.



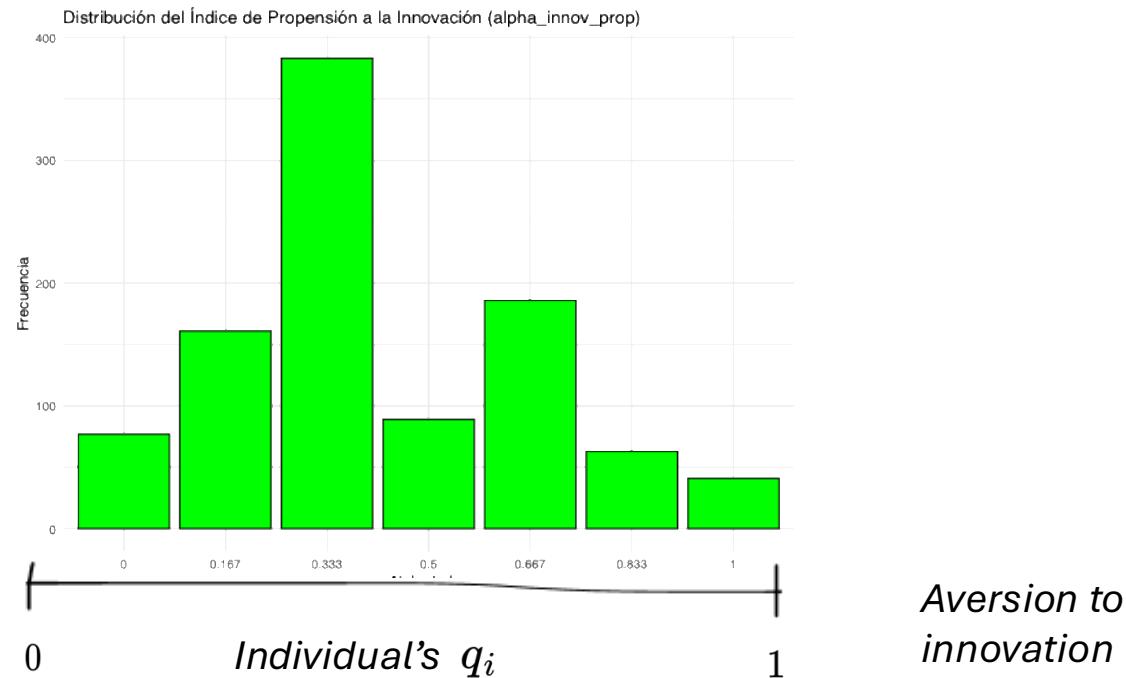
Imputing network structure to a Survey

Items to create the ‘*Openness to Innovations Score*’ from ATP 2014 (**binary**):

1. Usually try new products before others do. → pro-innov.
2. Prefer my tried and trusted brands. → anti-innov.
3. Like being able to tell others about new brands and products I have tried. → pro-innov.
4. Like the variety of trying new products. → pro-innov.
5. Feel more comfortable using familiar brands and products. → anti-innov.
6. Wait until I hear about others' experiences before I try new products. → anti-innov.

Imputing network structure to a Survey

Items to create the ‘*Openness to Innovations Score*’ from ATP 2014 (**binary**):



Comprehensive Simulation Methodology

Using the ATP-networks (N=1000 nodes):

Parameter Space Exploration:

- **IUL** (Γ): 41 levels (0.0 to 1.0).
- **MSP** (h): 13 levels (0.0 to 1.0).
- **Thresholds** (τ_i): Normally distributed $\tau_i \sim \mathcal{N}(\mu_\tau, \sigma_\tau)$
 - Means (μ_τ): 4 levels (0.3, 0.4, 0.5, 0.6).
 - SD (σ_τ): 4 levels (0.08, 0.12, 0.16, 0.20).
- **Seeding Strategies:**
Random, Central, Marginal, Closeness, and Eigenvalue.

Scale of Simulation:

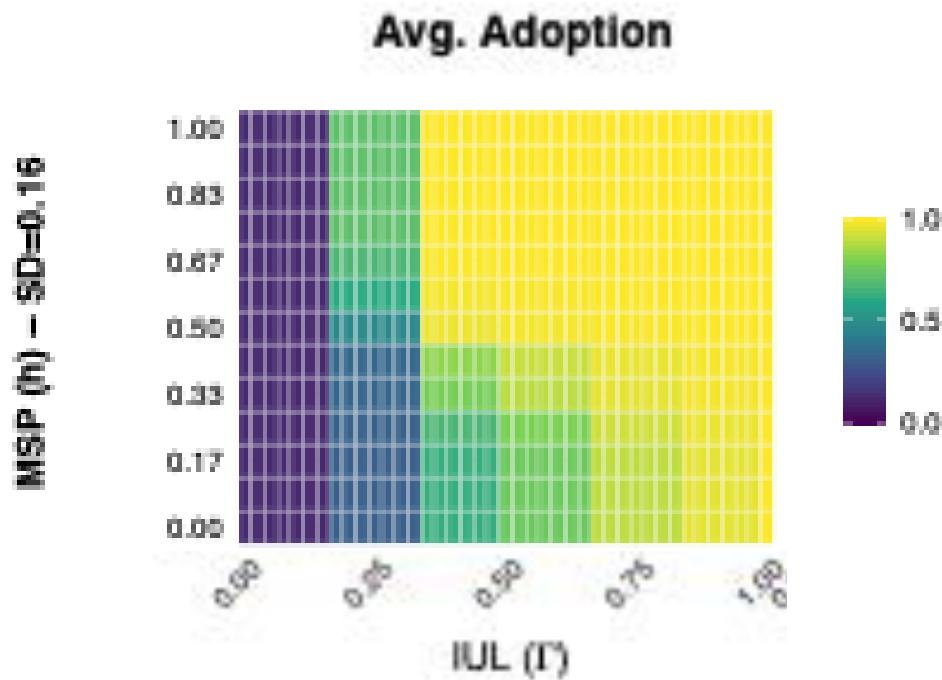
- 96 simulations for each combination of parameters
- Total simulations: $41 \times 13 \times 4 \times 4 \times 5 \times 96 \approx 4 \times 10^6$!

Results

-

Diffusion of Innovation

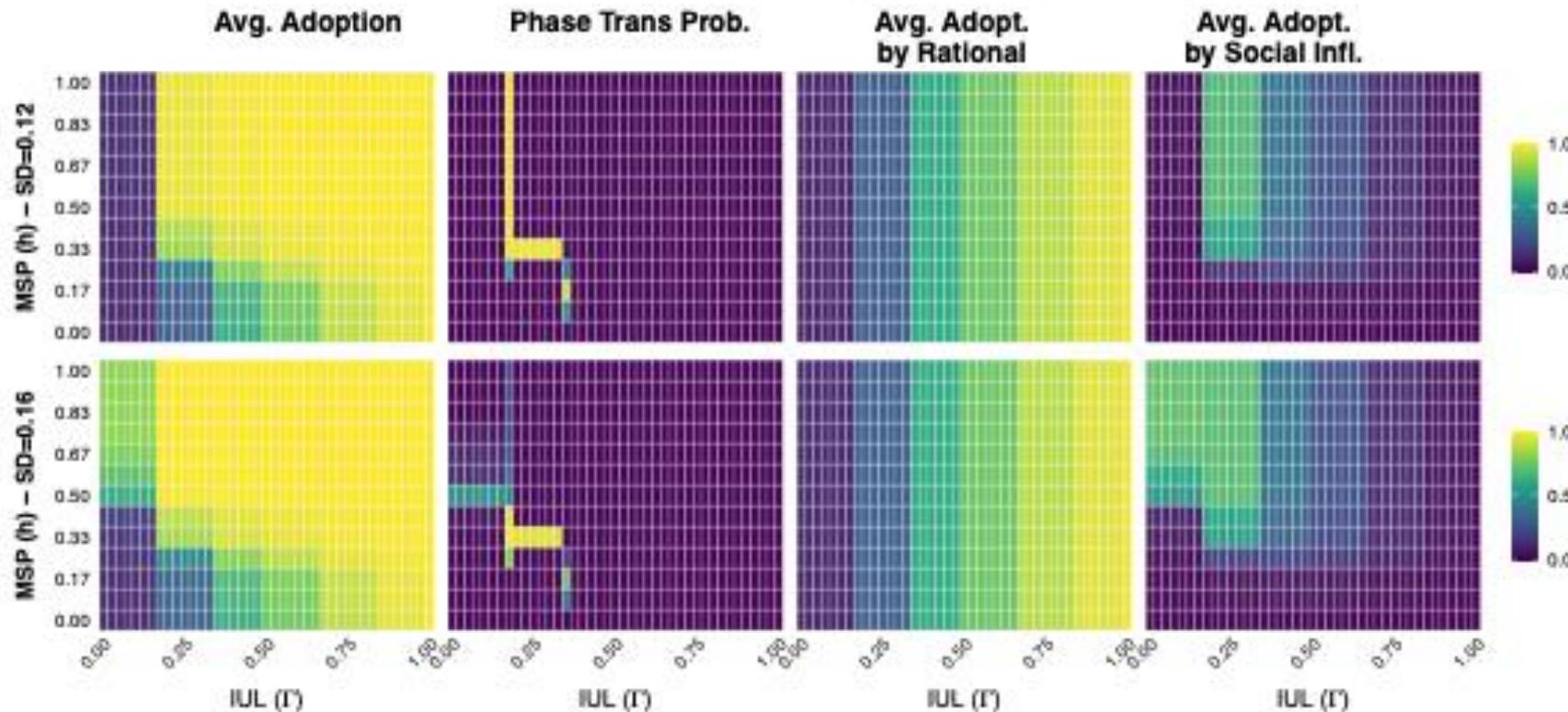
Results



Results

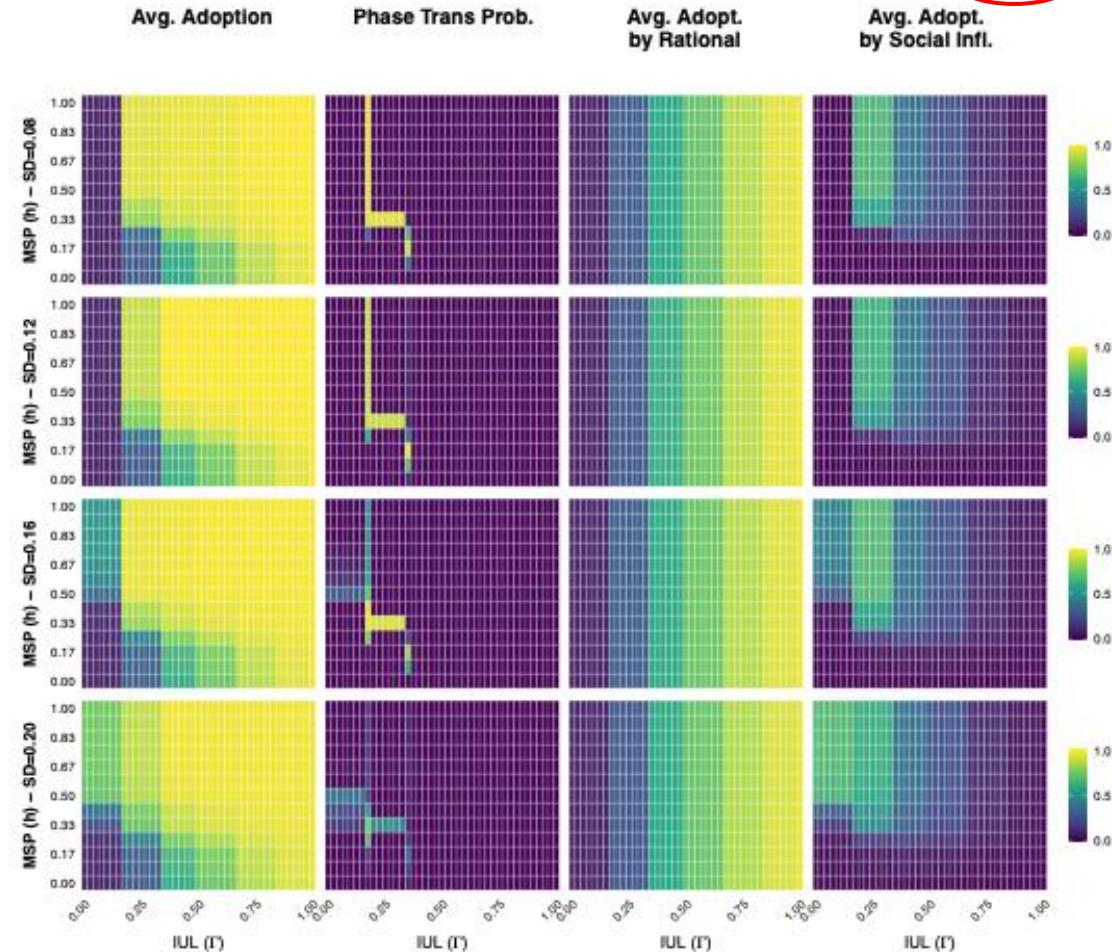
Consolidated Heatmaps for ATP-net – Mean threshold = 0.40

Thresholds $\sim N(\mu=0.40, SD=var)$. 96 runs per (IUL,h) per individual panel. Seeding strategy: random



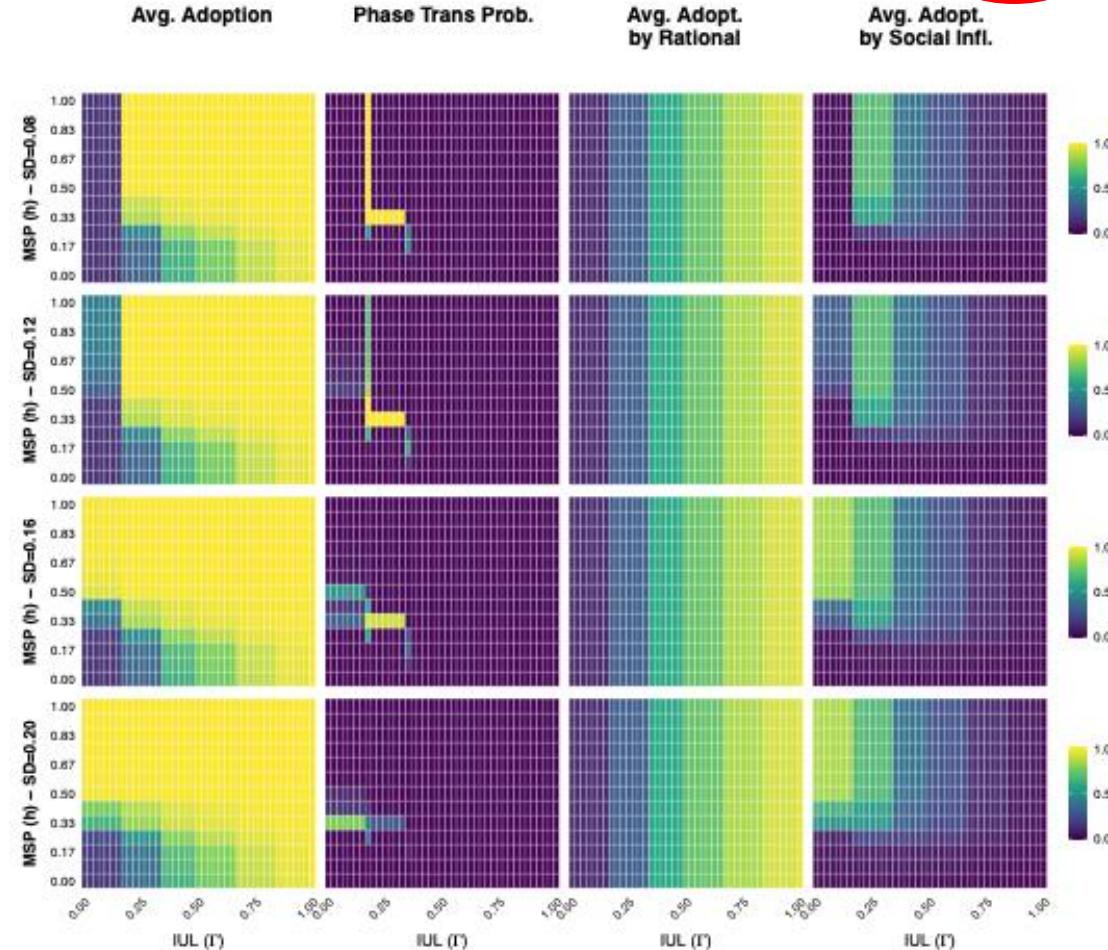
Consolidated Heatmaps for ATP-net – Mean threshold = 0.40

Thresholds ~ $N(\mu=0.40, SD=\text{var})$. 96 runs per (IUL,h) per individual panel. Seeding strategy: marginal



Consolidated Heatmaps for ATP-net – Mean threshold = 0.40

Thresholds ~ $N(\mu=0.40, SD=var)$. 96 runs per (IUL,h) per individual panel. Seeding strategy: central



Conclusions – 1st part

Conclusions – 1st part

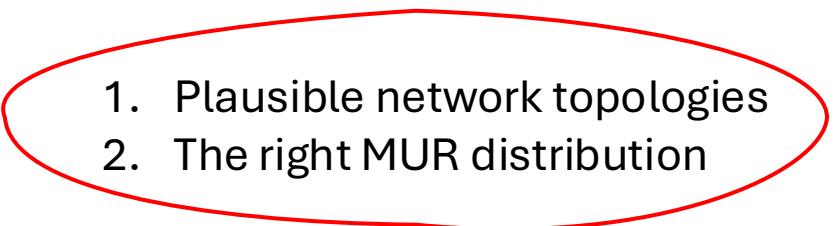
So, what have we learned?

- Social influence plays a relevant role in adoption, even for configurations where the innovation is **not particularly attractive**.
- The model offers consistent results across several parameter configurations.
- The regimens where social influence is on are separated abruptly by **first-order phase transitions**.
- There are non-structural barriers to word-of-mouth diffusion.

Setting up

—

Collective Action

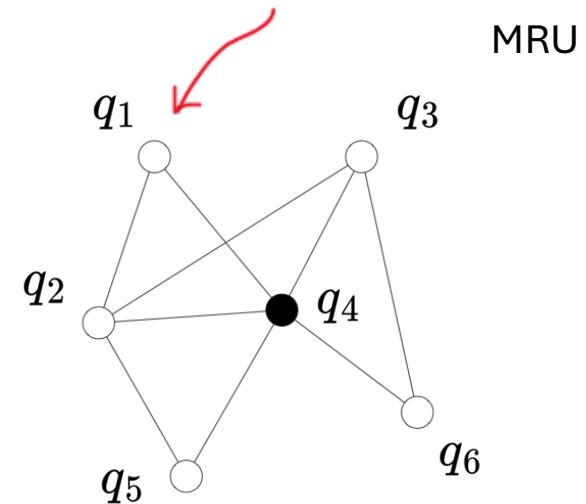
- 
1. Plausible network topologies
 2. The right MUR distribution

Imputing network structure to a Survey

General Social Survey (GSS 2004):

1. Representative of the US population
2. Demographics:
Age - Sex - Years of Educ – Race - Religion
3. EGO data
4. ‘*Collective Action Propensity Score*’ items

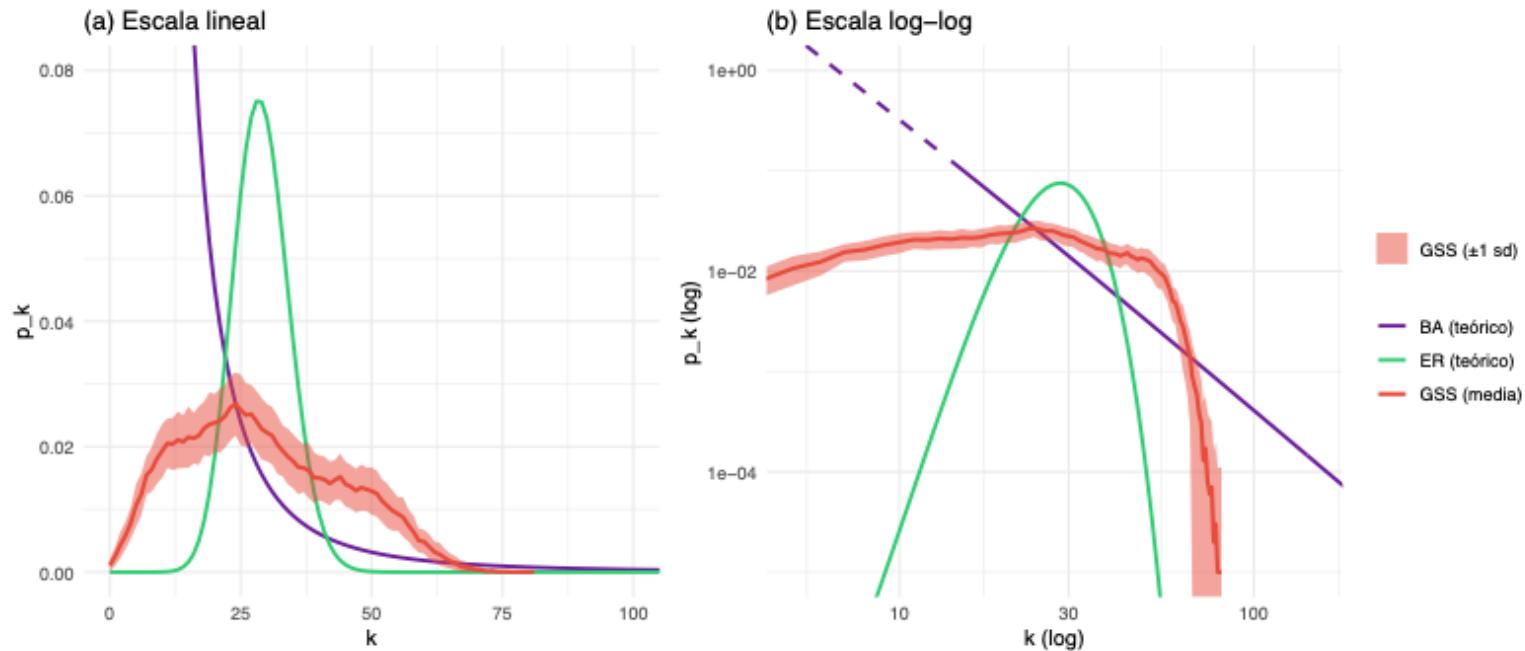
‘*Collective Action Propensity Score*’



GSS 2004 +
Network structure

Imputing network structure to a Survey

We can use that procedure to create networks with the **right topology** [8] via ERGM.



Imputing network structure to a Survey

Here are some forms of political and social action that people can take.

Please indicate, for each one,

- (0) whether you have done any of these things in the **past year**,
- (1) have done it in the **more distant past**,
- (2) have not done it but **might do it**,
- (3) or have not done it and **would never**, under any circumstances, do it.

1. Signed a petition
2. Boycotted, or deliberately bought, certain products for political, ethical or environmental reasons.
3. Took part in a demonstration.
4. Attended a political meeting or rally.
5. Contacted, or attempted to contact, a politician or a civil servant to express your views.
6. Donated money or raised funds for a social or political activity.

Imputing network structure to a Survey

Here are some forms of political and social action that people can take.

Please indicate, for each one,

- (0) whether you have done any of these things in the **past year**,
- (1) have done it in the **more distant past**,
- (2) have not done it but **might do it**,
- (3) or have not done it and **would never**, under any circumstances, do it.

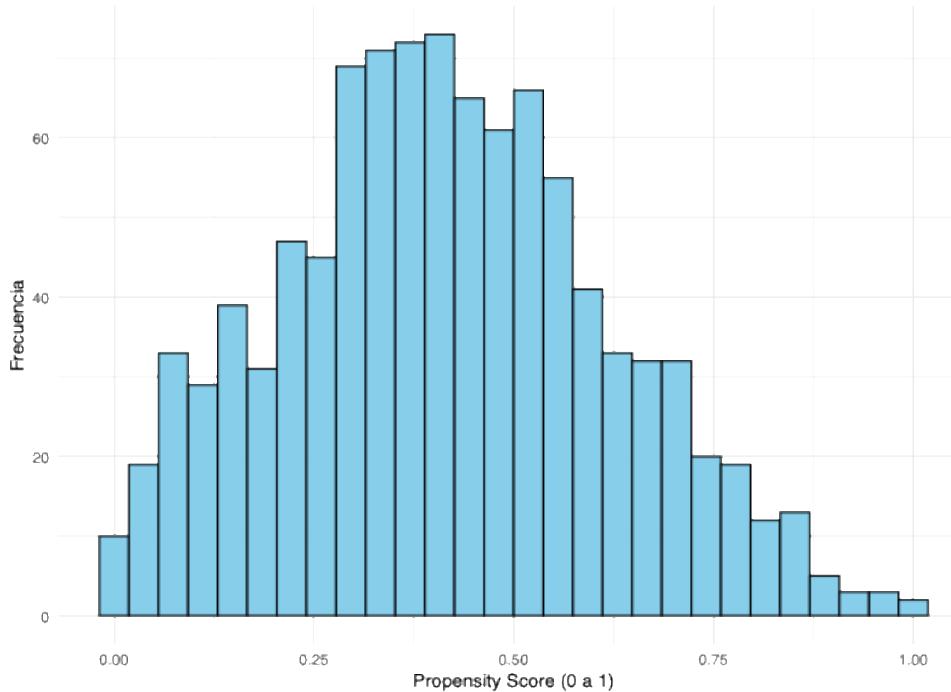
7. Contacted or appeared in the media to express your views.

8. Joined an Internet political forum or discussion group.

9. Suppose a law were being considered by the Congress that you considered to be unjust or harmful. If such a case arose, how likely is it that you, acting along or together with others, would be able to try to do something about it?

- 0) Very likely 1) Fairly likely 2) Not very likely 3) Not at all likely

Imputing network structure to a Survey



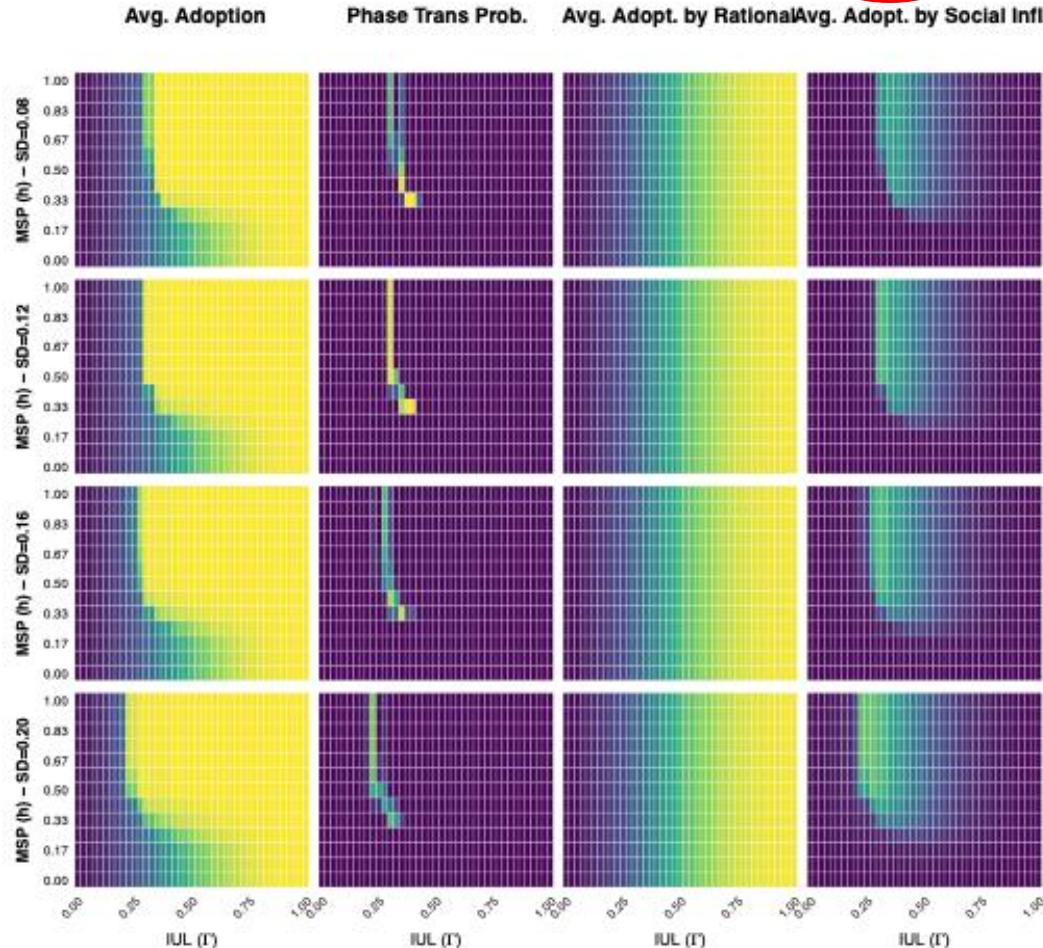
Results

-

Collective Action

Consolidated Heatmaps for GSS–net – Mean threshold = 0.50

Thresholds $\sim N(\cdot, 0.50, SD=var)$. N/A runs per cell. Seeding strategy: random



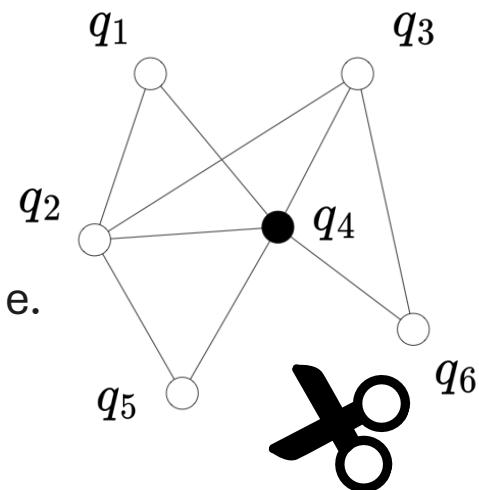
Diffusion of Innovation
results remain almost
the same for
Collective Action!

Setup

Using the ATP-networks (N=1000 nodes):

Parameter Space Exploration:

- ~~IUL (Γ)~~: 41 levels (0.0 to 1.0).
- ~~MSP (h)~~: 13 levels (0.0 to 1.0).
- **Thresholds (τ_i)**: Normally distributed $\tau_i \sim \mathcal{N}(\mu_\tau, \sigma_\tau)$
 - Means (μ_τ): 4 levels (0.3, 0.4, 0.5, 0.6).
 - SD (σ_τ): 4 levels (0.08, 0.12, 0.16, 0.20).
- **Seeding Strategies:**
Random, Central, Marginal, Closeness, and Eigenvalue.
- **Network Structure:**
Pseudo-empirical ATP/GSS, Erdös-Rényi.



Results – 2nd part

Family: binomial
Link function: logit

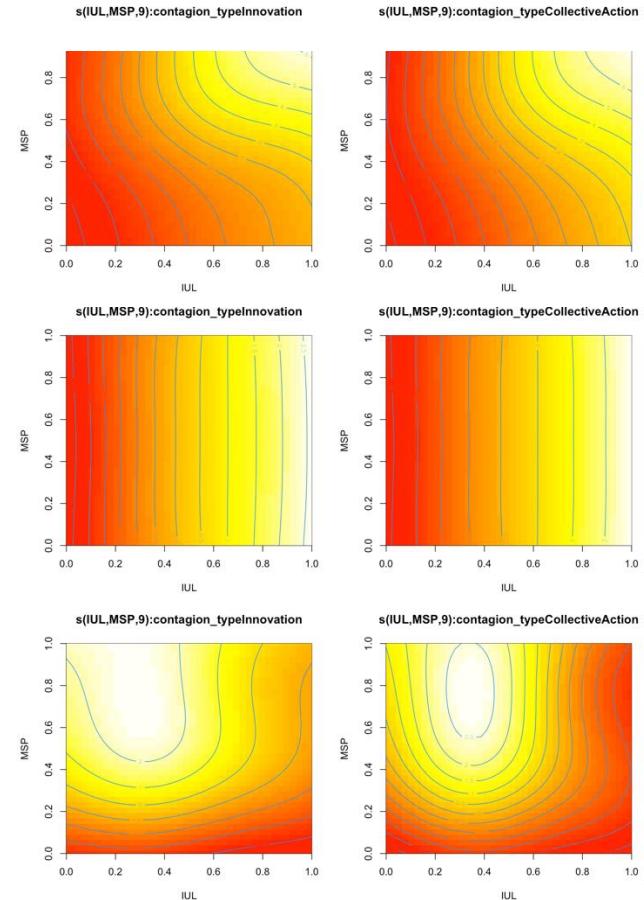
Formula:
 $\text{adopt_total} \sim s(\text{IUL}, \text{MSP}, k = 10, \text{by} = \text{contagion_type}) + \tau_{\text{mean}} + \tau_{\text{sd}} + \text{seed_type} + \text{network_type}$

Family: binomial
Link function: logit

Formula:
 $\text{adopt_rational} \sim s(\text{IUL}, \text{MSP}, k = 10, \text{by} = \text{contagion_type}) + \tau_{\text{mean}} + \tau_{\text{sd}} + \text{seed_type} + \text{network_type}$

Family: binomial
Link function: logit

Formula:
 $\text{adopt_social} \sim s(\text{IUL}, \text{MSP}, k = 10, \text{by} = \text{contagion_type}) + \tau_{\text{mean}} + \tau_{\text{sd}} + \text{seed_type} + \text{network_type}$



Results – 2nd part

Family: binomial
Link function: logit

Formula:
adopt_total ~ s(IUL, MSP, k = 10, by = contagion_type) + tau_mean + tau_sd + seed_type + network_type

Parametric coefficients:

	Estimate	OR	Std.Error	z value	Pr(> z)
(Intercept)	5.304	-	1.997e-04	26557	<2e-16 ***
tau_mean	-6.739	-	2.609e-04	-25829	<2e-16 ***
tau_sd	5.717	-	6.079e-04	9405	<2e-16 ***
seed_typecentral	0.137	1.147	8.527e-05	1610	<2e-16 ***
seed_typecloseness	0.132	1.141	8.525e-05	1548	<2e-16 ***
seed_typeeigen	0.134	1.145	8.526e-05	1581	<2e-16 ***
seed_typemarginal	-0.185	0.831	8.450e-05	-2189	<2e-16 ***
network_typeER	-0.376	0.687	5.41e-05	-6957	<2e-16 ***

Approximate significance of smooth terms:

	k'	edf	k-index	p-value
s(IUL,MSP):contagion_typeInnovation	9	9	0.95	0.005 **
s(IUL,MSP):contagion_typeCollectiveAction	9	9	0.95	<2e-16 ***

R-sq.(adj) = 0.855 Deviance explained = 84.4%
fREML = 8.5075e+08 Scale est. = 1 n = 170560

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Family: binomial
Link function: logit

Formula:
adopt_social ~ s(IUL, MSP, k = 10, by = contagion_type) + tau_mean + tau_sd + seed_type + network_type

Parametric coefficients:

	Estimate	OR	Std.Error	z value	Pr(> z)
(Intercept)	-0.543	-	1.422e-04	-3822.5	<2e-16 ***
tau_mean	-5.784	-	2.337e-04	-24751.3	<2e-16 ***
tau_sd	4.703	-	5.550e-04	8474.5	<2e-16 ***
seed_typecentral	0.047	1.048	7.781e-05	608.9	<2e-16 ***
seed_typecloseness	0.045	1.046	7.783e-05	579.1	<2e-16 ***
seed_typeeigen	0.047	1.048	7.781e-05	607.8	<2e-16 ***
seed_typemarginal	-0.080	0.922	7.874e-05	-1027.2	<2e-16 ***
network_typeER	-0.340	0.711	4.951e-05	-6886.1	<2e-16 ***

Approximate significance of smooth terms:

	k'	edf	k-index	p-value
s(IUL,MSP):contagion_typeInnovation	9	9	0.92	<2e-16 ***
s(IUL,MSP):contagion_typeCollectiveAction	9	9	0.92	<2e-16 ***

R-sq.(adj) = 0.67 Deviance explained = 69%
fREML = 9.2894e+08 Scale est. = 1 n = 170560

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Conclusions – 2nd part

Conclusions – 2nd part

Family: binomial
Link function: logit

Formula:
 $\text{adopt_social} \sim s(\text{IUL}, \text{MSP}, k = 10, \text{by} = \text{contagion_seed_type} + \text{network_type})$

Parametric coefficients:

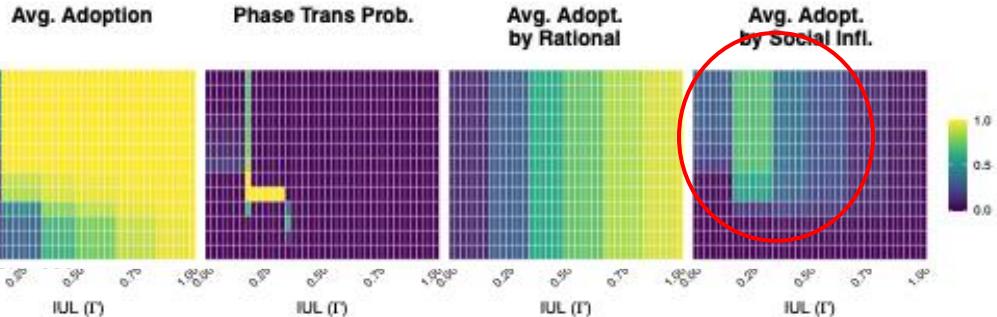
	Estimate	OR	Std.Error	z value	
(Intercept)	-0.543	-	1.422e-04	-382	
tau_mean	-5.784	-	2.337e-04	-2475	
tau_sd	4.703	-	5.550e-04	847	
seed_typecentral	0.047	1.048	7.781e-05	60	
seed_typecloseness	0.045	1.046	7.783e-05	57	
seed_typeeigen	0.047	1.048	7.781e-05	60	***
seed_typermarginal	-0.080	0.922	7.874e-05	-1027.2	<2e-16 ***
network_typeER	-0.340	0.711	4.951e-05	-6886.1	<2e-16 ***

Approximate significance of smooth terms:

	k'	edf	k-index	p-value
s(IUL,MSP):contagion_typeInnovation	9	9	0.92	<2e-16 ***
s(IUL,MSP):contagion_typeCollectiveAction	9	9	0.92	<2e-16 ***

R-sq.(adj) = 0.67 Deviance explained = 69%
fREML = 9.2894e+08 Scale est. = 1 n = 170560

Consolidated Heatmaps for ATP-net – Mean threshold = 0.40
Thresholds ~ N(mu=0.40, SD=var). 96 runs per (IUL,h) per individual panel. Seeding strategy: central



There are cases when the network decides for us!

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Thanks!



All the results are available
on the GitHub repository !

References

1. Gladwell, M. (2002). “*The tipping point: how little things can make a big difference*”. Back Bay Books, Boston, 1st back bay pbk. edition.
2. Farrell, W. (1998). “*How hits happen: forecasting predictability in a chaotic Marketplace*”. HarperBusiness, New York, 1st edition.
3. Oliver, P. E. (1993). Formal models of collective action. *Annual Review of Sociology*, 19, 271–300.
4. Granovetter, M. (1978). Threshold models of collective behavior. *American Journal of Sociology*, 83(6), 1420–1443.
5. Valente, T. W. (1996). Social network thresholds in the diffusion of innovations. *Social Networks*, 18(1), 69–89.
6. Centola, D. and Macy, M. (2007). Complex Contagions and the Weakness of Long Ties. *American Journal of Sociology*, 113(3):702–734.
7. Tur, E. M., Zeppini, P., and Frenken, K. (2018). “*Diffusion with social reinforcement: The role of individual preferences*”. *Physical Review E*, 97(2):022302.

References

8. Tur, E. M., Zeppini, P., and Frenken, K. (2024). “*Diffusion in small worlds with homophily and social reinforcement: A theoretical model*”. Social Networks, 76:12–21
9. Goldberg, A. (2021). “*Associative Diffusion and the Pitfalls of Structural Reductionism*”. American Sociological Review, 86(6):1205–1210.
10. McPherson, M. and Smith, J. A. (2019). “*Network Effects in Blau Space: Imputing Social Context from Survey Data*”. Socius: Sociological Research for a Dynamic World.
11. Smith, J. A., McPherson, M., and Smith-Lovin, L. (2014). "Social Distance in the United States: Sex, Race, Religion, Age, and Education Homophily among Confidants, 1985 to 2004." American Sociological Review, 79(3), 432–456.
12. Centola, D. (2011). An Experimental Study of Homophily in the Adoption of Health Behavior. Science, 334(6060):1269–1272.

Phase Transitions

