

$$\theta(t) = 2 \arcsin \left\{ \sin \frac{\theta_0}{2} \operatorname{sn}(u, k) \right\} \quad (1)$$

$$k = \sin^2 \frac{\theta_0}{2} \quad (2)$$

$$u = K \left(\sin^2 \frac{\theta_0}{2} \right) - \omega_0 t \quad (3)$$

$$\operatorname{sn}(u, k) = \frac{\vartheta(0, \tau)}{\vartheta_{10}(0, \tau)} \frac{\vartheta_{10}(u \vartheta(0, \tau)^{-2}, \tau)}{\vartheta_{01}(u \vartheta(0, \tau)^{-2}, \tau)} \quad (4)$$

$$\vartheta(z, \tau) = \sum_{n=-\infty}^{\infty} \exp(\pi i n^2 \tau + 2\pi i n z) \quad (5)$$

$$\vartheta_{01}(z, \tau) = \vartheta(z + \frac{1}{2}, \tau) \quad (6)$$

$$\vartheta_{10}(z, \tau) = \exp(\frac{1}{4}\pi i \tau + \pi i z) \vartheta(z + \frac{1}{2}\tau, \tau) \quad (7)$$

$$K(m) = \int_0^1 \frac{dz}{\sqrt{(1-z^2)(1-mz^2)}} \quad (8)$$