EEL 4837 Programming for Electrical Engineers II

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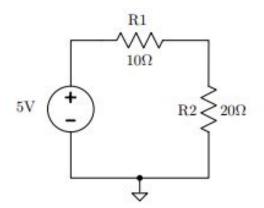
Excursion 1 – Circuit Analysis Tool

Readings:

- Excursion 1 Description

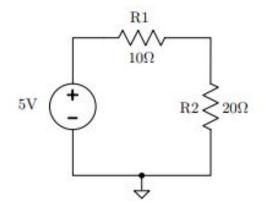
Electronic Circuit

- Electronic circuit: a collection of interconnected electronic components
- A circuit has a well-defined deterministic functionality when running:
 - Voltage sources
 - Current sources
 - Resistors
 - Inductors
 - Capacitors
 - Diodes
 - Transistors
 - O ...



Electronic Circuit (cont.)

- The functionality of a circuit is fully characterized by:
 - The **current** through each component
 - The voltage drop/rise through each component
 - The voltage potential at each of the interconnections relative to an arbitrary ground node

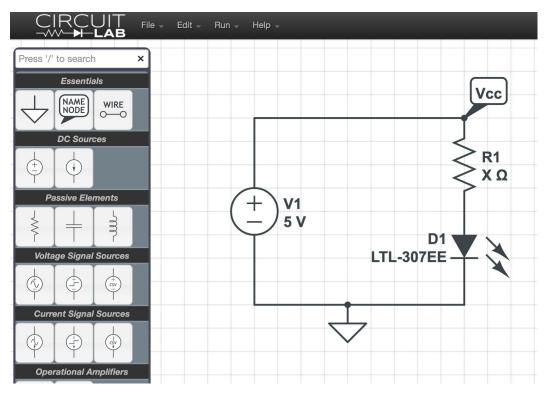


Circuit Analysis

- **Circuit analysis**: a sequence of methods to answer some questions about circuit
 - E.g., what is the voltage drop/rise across a resistor?
- To do that, we may need:
 - Measuring tools
 - E.g., Galvanometer, voltmeter, ohmmeter, etc
 - Theories
 - E.g., Ohm's Law, Voltage Law, Current Law, etc

Circuit Simulation

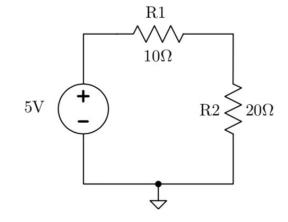
- **Circuit simulation**: a technique to check and verify the design of circuits prior to manufacturing and deployment.
- Almost replaced physical prototype
- What can we do with simulation?
 - Model a linear circuit with a single matrix algebraic equation



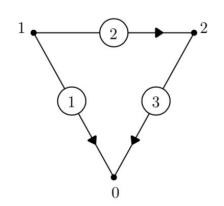
From: <u>CircuitLab</u>

Schematic Diagrams and Digraphs

• Schematic diagram: a graphical representation of an electrical circuit

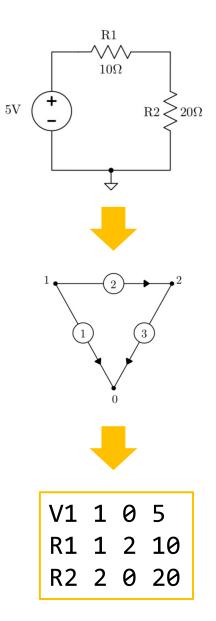


 Directed graph (digraph): can represent a circuit more abstractly (from graph theory)



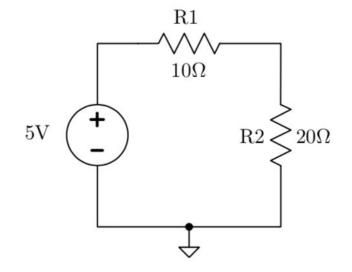
Circuit Netlist

- Netlist: describes the connectivity of an electronic circuit
- It consists of:
 - A list of electronic components
 - A list of nodes they are connected to
- Format:
 - Branch label
 - First character indicates component type
 - Source node label
 - Destination node label
 - Numeric component value



Circuit Netlist Conventions

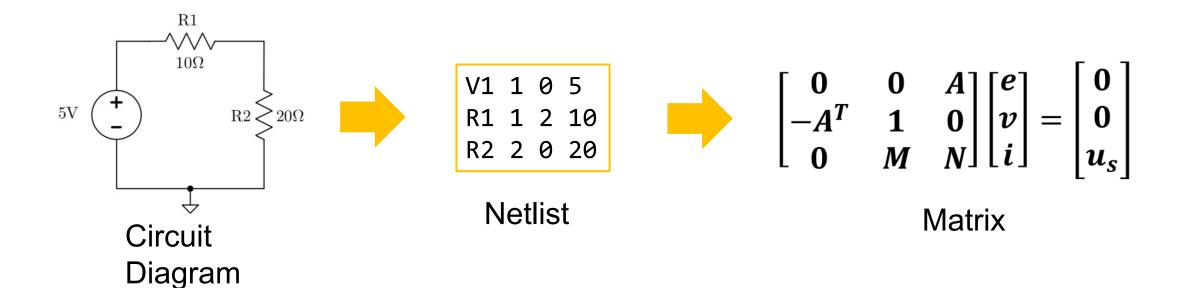
- Ground node is always labeled as 0, while other node can be labeled in any order
- Use positive numeric values
 - Current travels from source to destination.
 - Voltage drops from source to destination.



V1 1 0 5 R1 1 2 10 R2 2 0 20

Data Structure for Circuits

How can we represent a circuit in a program?



Excursion 1 Goal

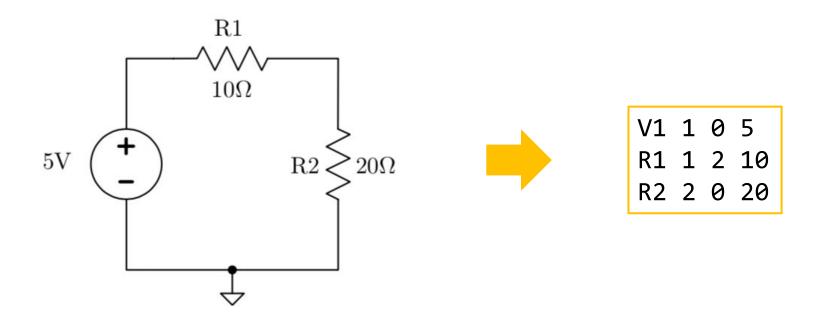
- An elementary interactive circuit analysis tool to:
 - Read a circuit from a file
 - Compute the currents and voltages across different components
 - Outputs them into a file
- You can assume that the given circuits only contain:
 - Voltage sources
 - Resistors

Steps Overview

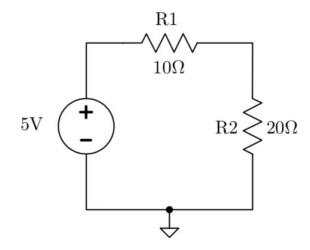
- 1. Read a netlist as input to represent a circuit
- 2. Use KCL, KVL, and Ohm's law to construct three matrix equations
- 3. Combine all the matrix equations to solve all the unknown parameters (**e**, **v**, **i** of each part)
- 4. Output voltages and currents

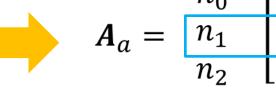
Step 1: Read a Netlist

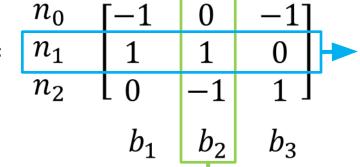
- Based on a circuit diagram, create its corresponding netlist as input
 - You'll be reading a netlist from a text file



Represent the netlist with an incidence matrix





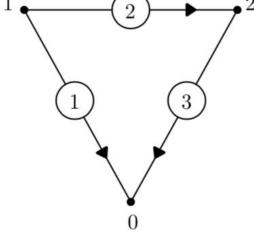




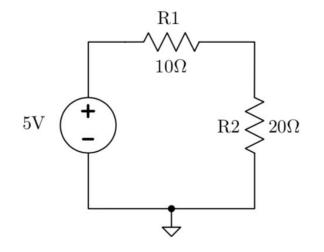
• Assume "1" is source and "-1" is destination.

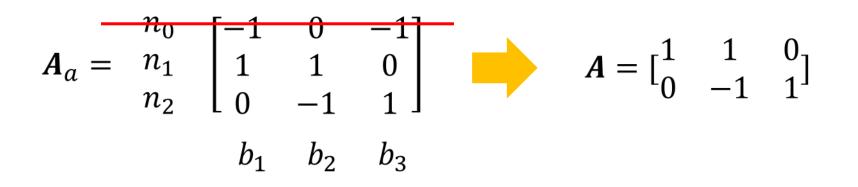
branch (aka element)

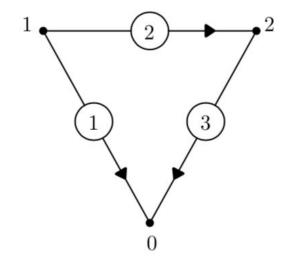
• In each column, we put a "1" in the source node row and "-1" in the destination node row.



• We can further remove the row for one node (usually the ground node) to get a *reduced incidence matrix*.

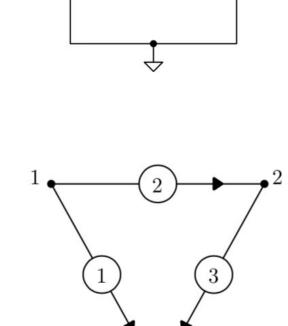






- Kirchoff's Current Law (KCL): the algebraic sum of currents that leave any node is zero.
- um of

- KCL equation for each node:
 - Assume leaving is positive and coming is negative:
 - At Node 0: branch currents i_1 and i_3 are coming, so $-i_1-i_3=0$
 - At Node 1: branch currents i_1 and i_2 are leaving, so $i_1+i_2=0$
 - At Node 2: branch current i_2 is coming, while i_3 is leaving, so $-i_2+i_3=0$



R1

 10Ω

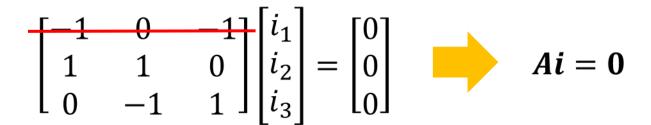
• (Cont.) Now we have:

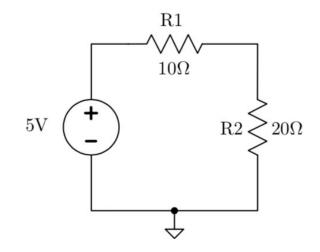
$$-i_1 - i_3 = 0$$

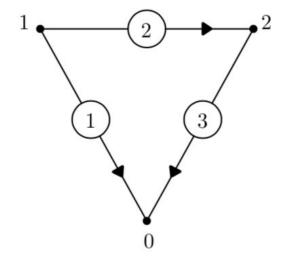
$$i_1 + i_2 = 0$$

$$-i_2 + i_3 = 0$$

Represent these equations with matrices:







- Kirchhoff's Voltage Law (KVL): the voltage drop between any two nodes is equal to the difference of the two node voltages.
- KVL equation for each pair of nodes:
 - Voltage drop between n0 and n1 (branch 1):

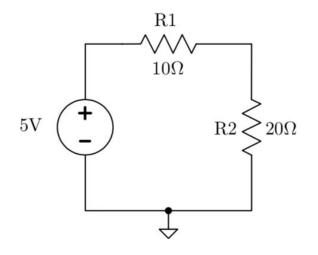
$$v_1 = e_1 - 0$$

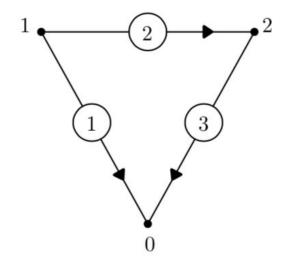
Voltage drop between n1 and n2 (branch 2):

$$v_2 = e_1 - e_2$$

Voltage drop between n0 and n2 (branch 3):

$$v_3 = e_2 - 0$$





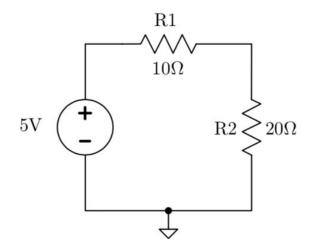
• (Cont.) Now we have:

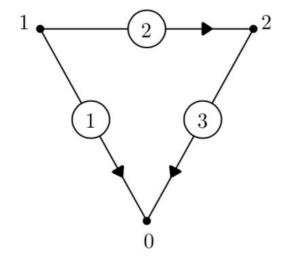
$$v_1 = e_1 - 0$$

 $v_2 = e_1 - e_2$
 $v_3 = e_2 - 0$

• Represent these equations with matrices:

$$\begin{bmatrix} v_1 \\ v_2 \\ v_2 \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 1 & -1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} e_1 \\ e_2 \end{bmatrix} \qquad \boldsymbol{v} = \boldsymbol{A}^T \boldsymbol{e}$$





Comparison between KCL and KVL:

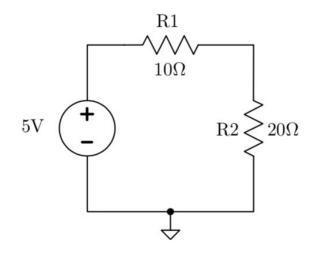
KCL

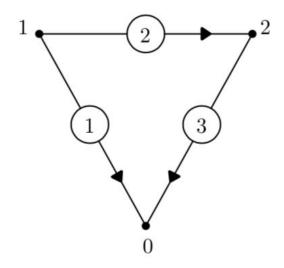
$$Ai = 0$$

KVL

$$\begin{bmatrix} v_1 \\ v_2 \\ v_3 \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 1 & -1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} e_1 \\ e_2 \end{bmatrix}$$

$$v = A^T e$$



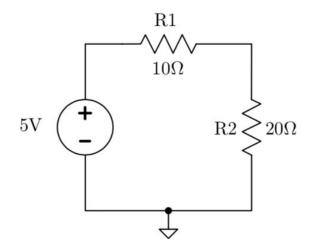


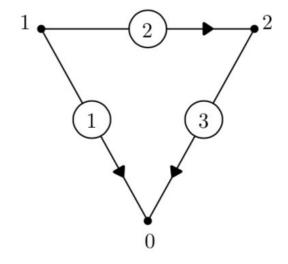
Combine the KCL and KVL equations:

$$Ai = 0$$
 $v = A^T e$



$$\begin{bmatrix} \mathbf{0} & \mathbf{0} & A \\ -A^T & \mathbf{1} & \mathbf{0} \end{bmatrix} \begin{bmatrix} e \\ v \\ i \end{bmatrix} = \begin{bmatrix} \mathbf{0} \\ \mathbf{0} \end{bmatrix}$$



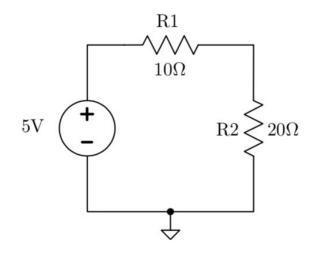


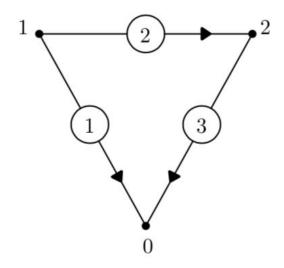
- Ohm's law: the current through a conductor between two points is directly proportional to the voltage across the two points.
 - $I = \frac{V}{R}$
- Ohm's law equation for each component:

$$v_1 = 5$$

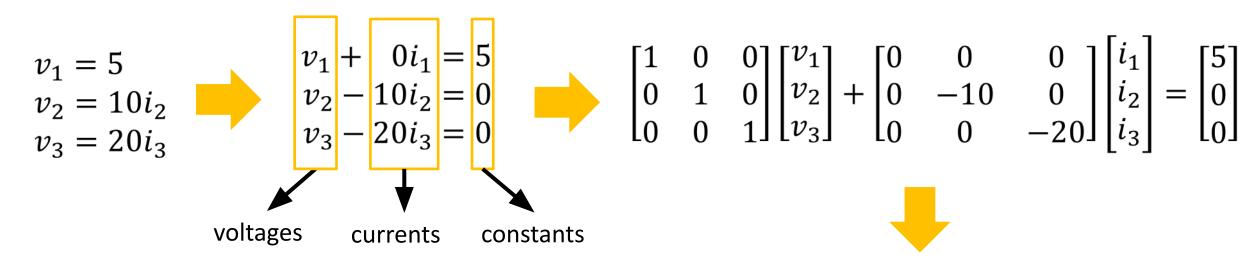
$$v_2 = 10i_2$$

$$v_3 = 20i_3$$





• (Continue) Represent these equations with matrices:



Format: $av_b + bi_b = u_s$

$$Mv + Ni = u_s$$

Step 3: Calculate Unknown Parameters

- Now, what do we have?
 - KCL + KVL:

$$\begin{bmatrix} \mathbf{0} & \mathbf{0} & A \\ -A^T & \mathbf{1} & \mathbf{0} \end{bmatrix} \begin{bmatrix} e \\ v \\ i \end{bmatrix} = \begin{bmatrix} \mathbf{0} \\ \mathbf{0} \end{bmatrix}$$

Ohm's Law:

$$Mv + Ni = u_s$$

Combine all the equations to create the combined matrix:

$$\begin{bmatrix} \mathbf{0} & \mathbf{0} & A \\ -A^T & \mathbf{1} & \mathbf{0} \\ \mathbf{0} & M & N \end{bmatrix} \begin{bmatrix} e \\ v \\ i \end{bmatrix} = \begin{bmatrix} \mathbf{0} \\ \mathbf{0} \\ u_s \end{bmatrix}$$

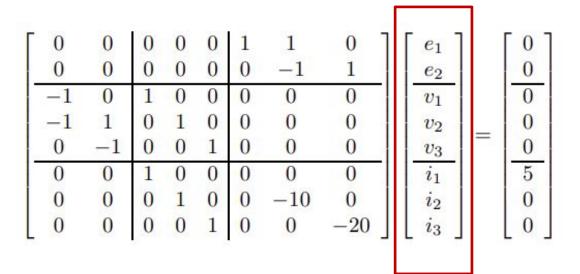
$$Tw = u$$

Step 3: Calculate Unknown Parameters

$$\begin{bmatrix} \mathbf{0} & \mathbf{0} & A \\ -A^T & \mathbf{1} & \mathbf{0} \\ \mathbf{0} & M & N \end{bmatrix} \begin{bmatrix} e \\ v \\ i \end{bmatrix} = \begin{bmatrix} \mathbf{0} \\ \mathbf{0} \\ u_s \end{bmatrix}$$



Put everything we know into the matrices



Final goal: calculate e, v, and i!

Steps Review

- 1. Read a netlist as input to represent a circuit
- 2. Use KCL, KVL and Ohm's law to construct three matrix equations
 - Construct A, M, N, and u_s to represent the netlist.
- 3. Combine all the matrix equations to solve all the unknown parameters (e, v, i of each part)
 - Use Gauss Elimination, LU Factorization, etc.
- 4. Output voltages and currents

Bigger Example

- Input:
 - V1106
 - R1126
 - R2 2 0 3.33
 - R3 2 3 3
 - R4 3 0 11
 - R5344
 - R6407
 - R7457
 - R8507

Bigger Example

```
0
                                              0
                                   0
                                         0
                                   0
                                         0
                                              0
\mathbf{A} = 0
              0
                                   0
                                              0
                                              0
              0
                         0
                                   0
                    0
                              0
                      0
                          0
             0
                      0
     0
                          0
                      0
                          0
                              0
             0
                      0
                                  0
                          0
                              0
                                      0
\mathbf{M} = 0
     0
             0
                      0
                                  0
                                      0
             0
                      0
                          0
     0
             0
                      0
```

Bigger Example

	0	0	0	0	0	0	0	0	0	6
	0	-6	0	0	0	0	0	0	0	0
	0	0	-3.33	0	0	0	0	0	0	0
	0	0	0	-3	0	0	0	0	0	0
•	$\mathbf{N} = 0$	0	0	0	-11	0	0	0	0	$u_s = 0$
	0	0	0	0	0	-4	0	0	0	0
	0	0	0	0	0	0	-7	0	0	0
	0	0	0	0	0	0	0	-7	0	0
	0	0	0	0	0	0	0	0	-7	0

Excursion 1 Quiz