

1) Solve the following set of equations using an LU decomposition. Then move on the find the inverse of the coefficient matrix A.

$$\begin{aligned}3.0 x_1 - 0.1 x_2 - 0.2 x_3 &= 7.85 \\0.1 x_1 + 7.0 x_2 - 0.3 x_3 &= -19.3 \\0.3 x_1 - 0.2 x_2 + 10.0 x_3 &= 71.4\end{aligned}$$

Solution:

Part-1:

Input matrix A and b

3.000000	-0.100000	-0.200000	7.850000
0.100000	7.000000	-0.300000	-19.299999
0.300000	-0.200000	10.000000	71.400002

matrix U after elimination

3.000000	-0.100000	-0.200000
0.000000	7.003333	-0.293333
0.000000	0.000000	10.012042

matrix L and y after forward elimination

1.000000	0.000000	0.000000	7.850000
0.033333	1.000000	0.000000	-19.561666
0.100000	-0.027130	1.000000	70.084295

solution x

3.000000	-2.500000	7.000000
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Part-2:

Input matrix A and b

3.000000	-0.100000	-0.200000
0.100000	7.000000	-0.300000
0.300000	-0.200000	10.000000

matrix U after elimination

3.000000	-0.100000	-0.200000
0.000000	7.003333	-0.293333
0.000000	0.000000	10.012042

matrix L after elimination

1.000000	0.000000	0.000000
0.033333	1.000000	0.000000
0.100000	-0.027130	1.000000

matrix inverse

0.332489	0.004944	0.006798
-0.005182	0.142903	0.004183
-0.010078	0.002710	0.099880