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#### **Topics**

Image classification recap

Multilayer perceptrons

Representation learning and deep learning

Convolutional neural networks

### Image Classification Recap

We are concerned with image classification





cat



### Image Classification Recap

We've covered the family of parametric models

How they can be used for classification

Predict vector w of class scores

How they can be trained

- Optimize cross-entropy loss using SGD
- Using regularization strategies



### Image Classification Recap

Performance has been lackluster so far

Test accuracies using HOG features and softmax classifier

- ▶ About 42% on TinyCifar10Dataset
- ▶ About 48% on Cifar10Dataset

Two directions for improvements

- Better classifier
- Better features





# Multilayer Perceptrons Motivation

Recall that softmax classifier is linear

Restricted to linear decision boundaries

But classes not linearly separable in HOG feature space

Unable to reach low training error



# Multilayer Perceptrons Motivation

Multilayer Perceptrons (MLPs) are a powerful alternative

MLPs are universal approximators

- ► Can approximate any function to any degree (regression)
- ► Can represent arbitrary decision boundaries (classification)

Trained in the same SGD & loss function framework



Neural Networks

#### A (artificial) neural network

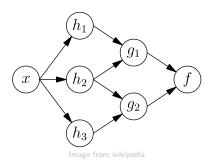
- ▶ Is a directed computational graph
- Vertices (neurons) are scalar functions of input
- Edges define data flow

#### And thus a function $f: \mathbf{x} \in \mathbb{R}^D \mapsto \mathbf{w} \in \mathbb{R}^T$

- That is composed of other functions (neurons)
- Neurons operate on (subset of) x and/or neuron output

### Multilayer Perceptrons Feedforward Neural Networks

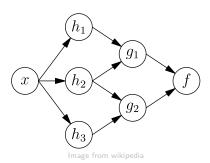
In feedforward neural networks this graph is acyclic Neurons at same level in hierarchy form a layer



Feedforward Neural Networks

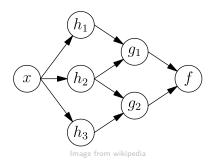
D input units (x) and T output units (f)

Flexible number of hidden units (h,g)



#### Feedforward Neural Networks

Input units only provide data (no computations)



#### MLPs are feedforward neural networks

- ▶ With one input layer and one output layer
- ▶ Neurons in layer l connected to all neurons in layer l-1
- ► Such layers are called fully-connected or dense

### Every (non-input) neuron i computes $n_i(\mathbf{a}_i^{\top}\mathbf{x}_l + b_i)$

- ▶ Linear transformation of input  $x_l$  (varies per layer)
- lacktriangle Followed by some activation function  $n_i$



Activation Functions

#### Activation function of output units depends on problem

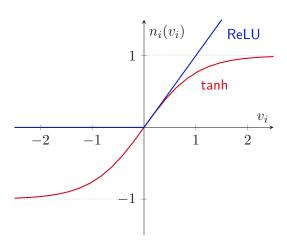
- Identity for regression
- ▶ Softmax for classification unless  $L(\theta)$  includes it

#### Common hidden layer activation functions (non-linearities)

- $n_i(v_i) = \tanh(v_i)$
- $n_i(v_i) = \max(0, v_i)$  (Rectified Linear Unit, ReLU)

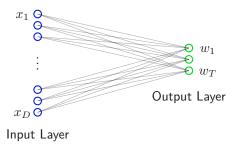


**Activation Functions** 



Architectures

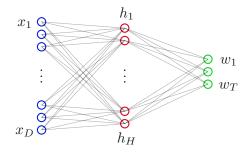
#### MLPs without hidden units are linear models



Architectures

Most MLPs have single hidden layer with H neurons

▶ Depth of 2 (two layers with parameters)



# Multilayer Perceptrons Capacity

Representational capacity depends on (hyperparameters)

- Number of hidden units H
- ► Type of non-linearities (usually ReLU)

Neural networks (including MLPs and CNNs) work best if

- ▶ They have enough capacity to overfit
- Are regularized properly to avoid this



# Multilayer Perceptrons Capacity

Networks with higher capacity perform better

▶ Because larger networks are easier to train

Recall what we learned about gradient descent limitations

- Applies only for sufficiently large networks
- ▶ Particularly, smaller networks have bad local minima



# Multilayer Perceptrons Capacity

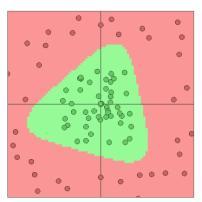


Image from cs.stanford.edu



## Representation Learning and Deep Learning Motivation

CIFAR10 dataset, HOG features, MLP :  $\approx 60\%$  test accuracy

- Much better than before
- ▶ But still far from state of the art (90% and more)

HOG features are limiting factor



### Representation Learning

#### Could extract additional features

- ▶ Features that retain color information
- ▶ HOG features obtained using different extractor settings
- Other features (SIFT, LBP, ...)

#### Standard approach until breakthrough of deep learning

- ▶ Limitations of features remain limiting factor
- Works only to some extent



### Representation Learning

#### Recall that manually designed features are low-level

- ► Capture basic properties of image
- ► Such as contrast changes, dominant colors

We want task-specific high-level features

- ▶ Features with semantic meaning
- ► E.g. presence of wheel for car classification



### Representation Learning

We cannot design reliable high-level feature extractors

- ▶ But we can try to learn them
- ► This task is called representation learning

Representation is feature vector used for classification

► Representation learning = learning to extract features

In our applications, input are images after preprocessing



# Representation Learning Challenges

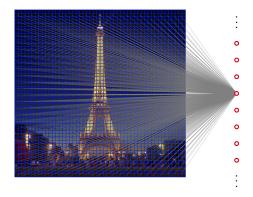
MLPs are not suited for this task

Not designed for images

Number of parameters increases quickly with D and H

- $ightharpoonup D \cdot H$  weights in first hidden layer
- $\blacktriangleright~224$  by 224 RGB image and H=500 : 75 million

# Representation Learning Challenges



# Representation Learning Challenges

#### Can think of a two-layer MLP as

- ightharpoonup A stage that learns to extract H features from  ${f x}$
- ▶ A stage that trains a linear classifier on these features

#### Must learn high-level features in single step

- ► This does not work in general
- Similar difficulty as solving original problem



# Representation Learning Deep Learning

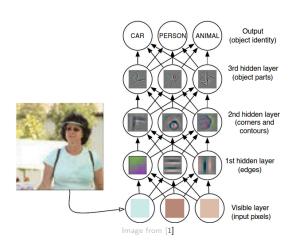
Deep learning solves this problem using divide and conquer

- Learn to extract features in hierarchical way
- ► Later features build upon earlier (simpler) ones

Hierarchy has many levels, hence the name deep learning



# Representation Learning Deep Learning



# Representation Learning Deep Learning

Cannot just use MLPs with several hidden layers

▶ Usually no improvements as depth exceeds 3

MLPs are unable to learn good image features either way

Not surprising since no understanding of images

We'll now switch to models that do





#### Convolutional Neural Networks

We'll now adapt above MLP architecture to images

- ► And other grid-like data
- Result is no longer a MLP



# Convolutional Neural Networks Input Layer

Should make use of spatial structure of images

▶ Not appropriate to flatten images to vector x

Retain structure by arranging input neurons accordingly

- ▶ If input images have size  $W_0 \times H_0$  and  $C_0$  channels
- ▶ Input neurons form  $W_0 \times H_0 \times C_0$  grid
- ▶  $W_0$  is width,  $H_0$  is height,  $C_0$  is depth of layer

# Convolutional Neural Networks Input Layer



Input Image



Input Layer

### Convolutional Neural Networks Locally Connected Layers

#### Spatially close pixels are highly correlated, others are not

- ▶ Nearby pixels correspond to same object (or part)
- ▶ Want to learn features using nearby pixels

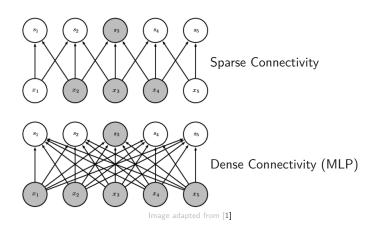
#### Realized by

- ▶ Arranging hidden layer neurons in  $W_l \times H_l$  grid
- ► With each neuron having a sparse connectivity



### Convolutional Neural Networks

Locally Connected Layers



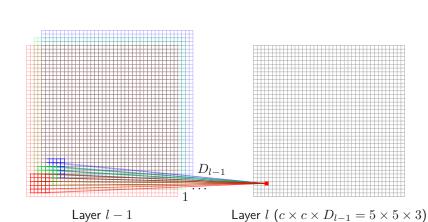
 $W_l$  and  $H_l$  depend on input width and height

• Usually  $W_l = W_{l-1}$  and  $H_l = H_{l-1}$ 

Connectivity c along with and height dimensions

▶ Is configurable but usually c = 3, that is  $3 \times 3$ 

Connectivity along depth dimension is always  $D_{l-1}$ 



#### Every neuron learns

- ▶ How to extract a feature
- ▶ By combining inputs in local neighborhood

### Operation is same as before, $n_i(\mathbf{A}_i \cdot \mathbf{X}_i + b_i)$

- ▶ Weights and inputs are now  $c \times c \times D_{l-1}$  matrices
- $ightharpoonup {f A}_i \cdot {f X}_i$  is dot product of matrices
- Input now varies with spatial location

Such layers are called locally connected layers

Every neuron extracts different feature (different parameters)



# Convolutional Neural Networks Convolutional Layers

Usually given feature is useful anywhere in image

► E.g. ability to detect car wheel anywhere in image

Enforced by parameter sharing between neurons

- ▶ Neurons compute  $n_i(\mathbf{A}_l \cdot \mathbf{X}_i + b_l)$
- Same parameters for all neurons in layer

## Convolutional Neural Networks Convolutional Layers

#### Now every neuron in layer

- ► Takes input in local neighborhood
- Computes linear combination with identical weights
- Adds bias and applies non-linearity

### First two operations equal to 3D convolution operation

- ► Hence such layers are called convolutional layers
- ► Fundamental layer of convolutional neural networks



# Convolutional Neural Networks Convolutional Layers

But layer can learn only single feature (not sufficient)

To overcome this problem, we replicate neurons  $\mathcal{D}_l$  times

- ▶ Resulting in  $W_l \times H_l \times D_l$  grid of neurons
- lacktriangle Only neurons with same depth  $D_l$  share parameters
- Every 2D depth slice is called feature map

Layer with  $D_l$  feature maps can learn  $D_l$  different features

 $ightharpoonup D_l$  is another hyperparameter

### Convolutional Neural Networks

Convolutional Layers

Number of weights  $A_l$  depends only on  $c, D_{l-1}, D_l$ 

- $c = 3, D_{l-1} = 3, D_l = 32 \implies 864$  weights
- $c = 3, D_{l-1} = 32, D_l = 64 \implies 18.5$ k weights

#### Few parameters per layer

- ► Can use several convolutional layers in network
- ▶ Layer l learns to combine layer l-1 features to new ones



### Convolutional Neural Networks

### Convolutional Neural Networks (CNNs, convnets)

- Are feedforward neural networks
- ► That include convolutional layers

CNNs are optimized for data with grid-like structure

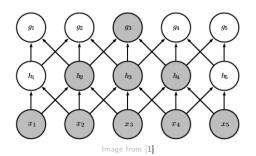
▶ Most important models for image analysis



### Convolutional Neural Networks Receptive Fields

#### Receptive field increases with depth

▶ Input region the neuron "sees" (indirect connection)



### Convolutional Neural Networks Receptive Fields

#### So in CNNs

- Direct connections are sparse
- ▶ But receptive field can span most/all of image

### Feature extraction approach is essentially part-based

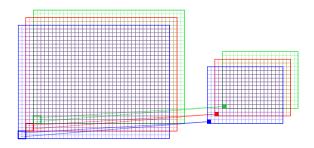
- ► Earlier layers learn more local features
- ► Learn local features (e.g. presence of eye or nose)
- ▶ Learn global features (e.g. presence of face) from those



# Convolutional Neural Networks Pooling Layers

#### Most CNNs include pooling layers

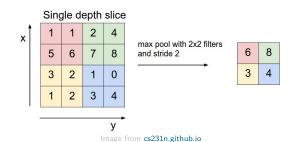
- ▶ Reduce spatial resolution (but not depth) of input
- ▶ To reduce number of parameters and computations



## Convolutional Neural Networks Pooling Layers

Most common form is  $2 \times 2$  max-pooling with stride 2

- $W_l = W_{l-1}/2$ ,  $H_l = H_{l-1}/2$ , and c = 2
- ▶ Output of neuron i is  $\max(\mathbf{X}_i)$  with  $\mathbf{X}_i \in \mathbb{R}^{2 \times 2}$



### Convolutional Neural Networks Layer Composition

Convolutional layers are fundamental layer type in CNNs Most CNNs also include pooling layers

Locally connected layers are used in some applications

▶ If features should vary with spatial location

Many other kinds of layers have been proposed

Most are not used in current CNNs



## Convolutional Neural Networks Layer Composition

#### Next lecture

- ▶ More on layer composition
- State-of-the-art CNN architectures



### Bibliography

[1] Deep learning, 2016, [Online]. Available: http://www.deeplearningbook.org.

