```
rsquare <- function(given, predicted) {</pre>
    sse <- sum((predicted - given)^2)</pre>
    sst <- sum(given^2)</pre>
    rsq <- 1 - sse / sst
    # For this post, impose floor...
    if (rsq < 0) rsq < -0
    return (rsq)
msd<-function(given, predicted) {</pre>
sqrt (mean ( (given-predicted) ^2) )
}
mtcarshp<-mtcars[,c("mpg","wt","drat","hp")]</pre>
 ntrain<-round(0.8*nrow(mtcarshp))</pre>
 ntest<-nrow (mtcarshp) -ntrain</pre>
 allidx<-1:nrow(mtcarshp)</pre>
 trainidx<-sample (allidx, ntrain, rep=FALSE)</pre>
 testidx<-allidx[-trainidx]
 traindata <-mtcarshp[trainidx,]
 testdata<-mtcarshp[testidx,]</pre>
lm.model<-lm(hp~mpg+wt+drat,data=traindata)</pre>
traindata$train.predicted.hp<-predict(lm.model,traindata[,c("mpg","wt","drat")])</pre>
#training error
train error<-rsquare(traindata$hp,traindata$train.predicted.hp)</pre>
train msd<-sqrt (mean ((traindata$hp-traindata$train.predicted.hp)^2))
#test error for lm
testdata$test.predicted.hp<-predict(lm.model,testdata[,c("mpq","wt","drat")])
test error<-rsquare(testdata$hp,testdata$test.predicted.hp)</pre>
test msd<-sqrt(mean((testdata$hp-testdata$test.predicted.hp)^2))</pre>
test error/ntest
model stats<-data.frame(#run names=c("proportion","rsquare","msd"),</pre>
lm.train=c(proportion=1, train error, train msd),
lm.test=c(proportion=1,test error,test msd),stringsAsFactors=F)
model stats
#require(magrittr)
#require(purrr)
#require(broom)
#require(tidyverse)
require(ggplot2)
require(glmnet)
y<-traindata$hp
x<-as.matrix(traindata[,c("mpg","wt","drat")])</pre>
lambdas < -10^seq(3, -2, by = -0.1)
glm.fit<-glmnet(x,y,alpha=0,lambda=lambdas)</pre>
all coef<-coef(glm.fit)</pre>
betas<-all coef[2:4,]</pre>
fitval<-x%*%betas
cv.glm.fit<-cv.glmnet(x,y,alpha=0,lambda=lambdas,nfolds=5)</pre>
cv.qlm.fit$lambda.min
traindata$train.penalized.hp<-predict(glm.fit,newx=as.matrix(traindata[,c("mpg","wt"
, "drat")]), s=cv.glm.fit$lambda.min, type='response')
```

```
model stats<-cbind(model stats,train.penalized.hp=c(proportion=1,rsquare=rsquare(tra</pre>
indata$hp,traindata$train.penalized.hp),msd=msd(traindata$hp,traindata$train.penaliz
ed.hp)))
#model stats<-rbind(model stats,c("train.penalized.hp",rsquare(traindata$hp,traindat
a$train.penalized.hp),
#+ msd(traindata$hp,traindata$train.penalized.hp))
proportion<-c(0,0,0,1) #c(NA,NA,NA,1)
traindata$tr.p.hp2<-predict(glm.fit,newx=as.matrix(traindata[,c("mpq","wt","drat")])</pre>
, s=0.98*cv.glm.fit$lambda.min,type='response')
sum((traindata$tr.p.hp2-traindata$hp)^2)
model stats<-cbind(model stats,tr.p.hp2=c(0.98,rsquare=rsquare(traindata$hp,traindat
a$tr.p.hp2), msd=msd(traindata$hp, traindata$tr.p.hp2)))
proportion<-c(proportion, 0.98)</pre>
traindata$tr.p.hp3<-predict(glm.fit,newx=as.matrix(traindata[,c("mpg","wt","drat")])</pre>
, s=0.88*cv.glm.fit$lambda.min,type='response')
sum((traindata$tr.p.hp3-traindata$hp)^2)
model stats<-cbind(model stats,tr.p.hp3=c(0.88,rsquare=rsquare(traindata$hp,traindat</pre>
a$tr.p.hp3), msd=msd(traindata$hp,traindata$tr.p.hp3)))
proportion<-c(proportion, 0.88)</pre>
traindata$tr.p.hp4<-predict(glm.fit,newx=as.matrix(traindata[,c("mpg","wt","drat")])</pre>
, s=0.80*cv.qlm.fit$lambda.min,type='response')
model stats<-cbind(model stats,tr.p.hp4=c(0.80,rsquare=rsquare(traindata$hp,traindat
a$tr.p.hp4), msd=msd(traindata$hp, traindata$tr.p.hp4)))
proportion<-c(proportion, 0.80)</pre>
sum((traindata$tr.p.hp4-traindata$hp)^2)
traindata$tr.p.hp5<-predict(glm.fit,newx=as.matrix(traindata[,c("mpg","wt","drat")])</pre>
,s=0.78*cv.qlm.fit$lambda.min,type='response')
model stats<-cbind(model stats,tr.p.hp5=c(0.78,rsquare=rsquare(traindata$hp,traindat
a$tr.p.hp5), msd=msd(traindata$hp, traindata$tr.p.hp5)))
proportion<-c(proportion, 0.78)</pre>
sum((traindata$tr.p.hp5-traindata$hp)^2)
traindata$tr.p.hp6<-predict(glm.fit,newx=as.matrix(traindata[,c("mpg","wt","drat")])</pre>
, s=0.76*cv.glm.fit$lambda.min,type='response')
model stats<-cbind(model stats,tr.p.hp6=c(0.76,rsquare=rsquare(traindata$hp,traindat
a$tr.p.hp6), msd=msd(traindata$hp, traindata$tr.p.hp6)))
proportion<-c(proportion, 0.76)</pre>
sum((traindata$tr.p.hp6-traindata$hp)^2)
traindata$tr.p.hp7<-predict(glm.fit,newx=as.matrix(traindata[,c("mpq","wt","drat")])</pre>
,s=0.66*cv.qlm.fit$lambda.min,type='response')
model stats<-cbind(model stats,tr.p.hp7=c(0.66,rsquare=rsquare(traindata$hp,traindat
a$tr.p.hp7), msd=msd(traindata$hp,traindata$tr.p.hp7)))
proportion<-c(proportion, 0.66)</pre>
sum((traindata$tr.p.hp7-traindata$hp)^2)
traindata$tr.p.hp8<-predict(glm.fit,newx=as.matrix(traindata[,c("mpg","wt","drat")])</pre>
, s=0.50*cv.glm.fit$lambda.min,type='response')
model stats<-cbind(model stats,tr.p.hp8=c(0.50,rsquare=rsquare(traindata$hp,traindat
a$tr.p.hp8), msd=msd(traindata$hp, traindata$tr.p.hp8)))
proportion<-c(proportion, 0.50)</pre>
sum((traindata$tr.p.hp8-traindata$hp)^2)
traindata$tr.p.hp9<-predict(glm.fit,newx=as.matrix(traindata[,c("mpq","wt","drat")])</pre>
, s=0.40*cv.qlm.fit$lambda.min,type='response')
model stats<-cbind(model stats,tr.p.hp9=c(0.40,rsquare=rsquare(traindata$hp,traindat
a$tr.p.hp9), msd=msd(traindata$hp, traindata$tr.p.hp9)))
```

```
proportion<-c(proportion, 0.40)</pre>
sum((traindata$tr.p.hp9-traindata$hp)^2)
traindata$tr.p.hp10<-predict(glm.fit,newx=as.matrix(traindata[,c("mpg","wt","drat")]
), s=0.20*cv.glm.fit$lambda.min,type='response')
model stats<-cbind(model stats,tr.p.hp10=c(0.20,rsquare=rsquare(traindata$hp,trainda
ta$tr.p.hp10), msd=msd(traindata$hp, traindata$tr.p.hp10)))
proportion<-c(proportion, 0.20)</pre>
sum((traindata$tr.p.hp10-traindata$hp)^2)
traindata$tr.p.hp11<-predict(glm.fit,newx=as.matrix(traindata[,c("mpg","wt","drat")]</pre>
),s=0.10*cv.qlm.fit$lambda.min,type='response')
model stats<-cbind(model stats,tr.p.hp11=c(0.10,rsquare=rsquare(traindata$hp,trainda
ta$tr.p.hp11), msd=msd(traindata$hp, traindata$tr.p.hp11)))
proportion<-c(proportion, 0.10)</pre>
sum((traindata$tr.p.hp11-traindata$hp)^2)
cv.glm.fit$lambda.min
traindata$tr.p.hp12<-predict(qlm.fit,newx=as.matrix(traindata[,c("mpq","wt","drat")]</pre>
), s=0.05*cv.qlm.fit$lambda.min,type='response')
model stats<-cbind(model stats,tr.p.hp12=c(0.05,rsquare=rsquare(traindata$hp,trainda
ta$tr.p.hp12), msd=msd(traindata$hp, traindata$tr.p.hp12)))
proportion<-c(proportion, 0.05)</pre>
sum((traindata$tr.p.hp12-traindata$hp)^2)
traindata$tr.p.hp13<-predict(glm.fit,newx=as.matrix(traindata[,c("mpg","wt","drat")]</pre>
), s=0*cv.glm.fit$lambda.min,type='response')
model stats<-cbind(model stats,tr.p.hp13=c(0.00,rsquare=rsquare(traindata$hp,trainda
ta$tr.p.hp13), msd=msd(traindata$hp, traindata$tr.p.hp13)))
proportion<-c(proportion, 0.0)</pre>
sum((traindata$tr.p.hp13-traindata$hp)^2)
traindata$tr.p.hp14<-predict(qlm.fit,newx=as.matrix(traindata[,c("mpq","wt","drat")]</pre>
), s=-0.05*cv.qlm.fit$lambda.min,type='response')
model stats<-cbind(model stats,tr.p.hp14=c(-0.05,rsquare=rsquare(traindata$hp,traind
ata$tr.p.hp14), msd=msd(traindata$hp,traindata$tr.p.hp14)))
proportion<-c(proportion, -0.05)</pre>
sum((traindata$tr.p.hp14-traindata$hp)^2)
traindata$tr.p.hp15<-predict(glm.fit,newx=as.matrix(traindata[,c("mpg","wt","drat")]</pre>
),s=-0.8*cv.glm.fit$lambda.min,type='response')
model stats<-cbind(model stats,tr.p.hp15=c(-0.8,rsquare=rsquare(traindata$hp,trainda
ta$tr.p.hp15), msd=msd(traindata$hp, traindata$tr.p.hp15)))
proportion<-c(proportion, -0.80)</pre>
sum((traindata$tr.p.hp15-traindata$hp)^2)
traindata$tr.p.hp16<-predict(glm.fit,newx=as.matrix(traindata[,c("mpg","wt","drat")]</pre>
),s=-0.90*cv.glm.fit$lambda.min,type='response')
model stats<-cbind(model stats,tr.p.hp16=c(-0.9,rsquare=rsquare(traindata$hp,trainda
ta$tr.p.hp16), msd=msd(traindata$hp, traindata$tr.p.hp16)))
proportion<-c(proportion, -0.90)</pre>
sum((traindata$tr.p.hp16-traindata$hp)^2)
traindata$tr.p.hp17<-predict(glm.fit,newx=as.matrix(traindata[,c("mpq","wt","drat")]</pre>
), s=-1*cv.qlm.fit$lambda.min,type='response')
model stats<-cbind(model stats,tr.p.hp17=c(-1,rsquare=rsquare(traindata$hp,traindata
$tr.p.hp17),msd=msd(traindata$hp,traindata$tr.p.hp17)))
proportion<-c(proportion,-1.0)</pre>
sum((traindata$tr.p.hp17-traindata$hp)^2)
```

```
traindata$tr.p.hp18<-predict(qlm.fit,newx=as.matrix(traindata[,c("mpq","wt","drat")]</pre>
), s=-2*cv.qlm.fit$lambda.min,type='response')
model stats<-cbind(model stats,tr.p.hp18=c(-2,rsquare=rsquare(traindata$hp,traindata
$tr.p.hp18), msd=msd(traindata$hp, traindata$tr.p.hp18)))
proportion<-c(proportion, -2.0)</pre>
sum((traindata$tr.p.hp18-traindata$hp)^2)
traindata$tr.p.hp19<-predict(qlm.fit,newx=as.matrix(traindata[,c("mpq","wt","drat")]</pre>
), s=-3*cv.qlm.fit$lambda.min,type='response')
model stats<-cbind(model stats,tr.p.hp19=c(-3,rsquare=rsquare(traindata$hp,traindata
$tr.p.hp19), msd=msd(traindata$hp, traindata$tr.p.hp19)))
proportion<-c(proportion, -3.0)</pre>
sum((traindata$tr.p.hp19-traindata$hp)^2)
traindata$tr.p.hp20<-predict(glm.fit,newx=as.matrix(traindata[,c("mpq","wt","drat")]
), s=-4*cv.qlm.fit$lambda.min,type='response')
model stats<-cbind(model stats,tr.p.hp20=c(-4,rsquare=rsquare(traindata$hp,traindata
$tr.p.hp20), msd=msd(traindata$hp, traindata$tr.p.hp20)))
proportion<-c(proportion,-4.0)
sum((traindata$tr.p.hp20-traindata$hp)^2)
testdata$test.penalized.hp<-predict(glm.fit,newx=as.matrix(testdata[,c("mpg","wt","d
rat")]),s=cv.glm.fit$lambda.min,type='response')
model stats<-cbind(model stats,test.penalized.hp=c(1,rsquare=rsquare(testdata$hp,tes
tdata$test.penalized.hp), msd=msd(testdata$hp, testdata$test.penalized.hp)))
#model stats<-rbind(model stats,c("test.penalized.hp",rsquare(testdata$hp,testdata$t
est.penalized.hp),
#+ msd(testdata$hp,testdata$test.penalized.hp))
proportion<-c(NA,NA,NA,1)</pre>
testdata$tst.p.hp2<-predict(glm.fit,newx=as.matrix(testdata[,c("mpg","wt","drat")]),
s=0.98*cv.qlm.fit$lambda.min,type='response')
sum((testdata$tst.p.hp2-testdata$hp)^2)
model stats<-cbind(model stats,tst.p.hp2=c(0.98,rsquare=rsquare(testdata$hp,testdata
$tst.p.hp2), msd=msd(testdata$hp, testdata$tst.p.hp2)))
proportion<-c(proportion, 0.98)</pre>
testdata$tst.p.hp3<-predict(glm.fit,newx=as.matrix(testdata[,c("mpg","wt","drat")]),
s=0.88*cv.qlm.fit$lambda.min,type='response')
sum((testdata$tst.p.hp3-testdata$hp)^2)
model stats<-cbind(model stats,tst.p.hp3=c(0.88,rsquare=rsquare(testdata$hp,testdata
$tst.p.hp3), msd=msd(testdata$hp, testdata$tst.p.hp3)))
proportion<-c(proportion, 0.88)</pre>
testdata$tst.p.hp4<-predict(glm.fit,newx=as.matrix(testdata[,c("mpg","wt","drat")]),
s=0.80*cv.qlm.fit$lambda.min,type='response')
model stats<-cbind(model stats,tst.p.hp4=c(0.80,rsquare=rsquare(testdata$hp,testdata
$tst.p.hp4), msd=msd(testdata$hp, testdata$tst.p.hp4)))
proportion<-c(proportion, 0.80)</pre>
sum((testdata$tst.p.hp4-testdata$hp)^2)
testdata$tst.p.hp5<-predict(glm.fit,newx=as.matrix(testdata[,c("mpg","wt","drat")]),
s=0.78*cv.qlm.fit$lambda.min,type='response')
model stats<-cbind(model stats,tst.p.hp5=c(0.78,rsquare=rsquare(testdata$hp,testdata
$tst.p.hp5), msd=msd(testdata$hp, testdata$tst.p.hp5)))
proportion<-c(proportion, 0.78)</pre>
sum((testdata$tst.p.hp5-testdata$hp)^2)
testdata$tst.p.hp6<-predict(qlm.fit,newx=as.matrix(testdata[,c("mpq","wt","drat")]),
s=0.76*cv.glm.fit$lambda.min,type='response')
```

```
model stats<-cbind(model stats,tst.p.hp6=c(0.76,rsquare=rsquare(testdata$hp,testdata
$tst.p.hp6), msd=msd(testdata$hp, testdata$tst.p.hp6)))
proportion<-c(proportion, 0.76)</pre>
sum((testdata$tst.p.hp6-testdata$hp)^2)
testdata$tst.p.hp7<-predict(glm.fit,newx=as.matrix(testdata[,c("mpg","wt","drat")]),
s=0.66*cv.qlm.fit$lambda.min,type='response')
model stats<-cbind(model stats,tst.p.hp7=c(0.66,rsquare=rsquare(testdata$hp,testdata
$tst.p.hp7), msd=msd(testdata$hp, testdata$tst.p.hp7)))
proportion<-c(proportion, 0.66)</pre>
sum((testdata$tst.p.hp7-testdata$hp)^2)
testdata$tst.p.hp8<-predict(glm.fit,newx=as.matrix(testdata[,c("mpg","wt","drat")]),
s=0.50*cv.qlm.fit$lambda.min,type='response')
model stats<-cbind(model stats,tst.p.hp8=c(0.50,rsquare=rsquare(testdata$hp,testdata
$tst.p.hp8), msd=msd(testdata$hp, testdata$tst.p.hp8)))
proportion<-c(proportion, 0.50)</pre>
sum((testdata$tst.p.hp8-testdata$hp)^2)
testdata$tst.p.hp9<-predict(glm.fit,newx=as.matrix(testdata[,c("mpg","wt","drat")]),
s=0.40*cv.qlm.fit$lambda.min,type='response')
model stats<-cbind(model stats,tst.p.hp9=c(0.40,rsquare=rsquare(testdata$hp,testdata
$tst.p.hp9), msd=msd(testdata$hp, testdata$tst.p.hp9)))
proportion<-c(proportion, 0.40)</pre>
sum((testdata$tst.p.hp9-testdata$hp)^2)
testdata$tst.p.hp10<-predict(glm.fit,newx=as.matrix(testdata[,c("mpg","wt","drat")])</pre>
, s=0.20*cv.glm.fit$lambda.min, type='response')
model stats<-cbind(model stats,tst.p.hp10=c(0.20,rsquare=rsquare(testdata$hp,testdat
a$tst.p.hp10), msd=msd(testdata$hp,testdata$tst.p.hp10)))
proportion<-c(proportion, 0.20)</pre>
sum((testdata$tst.p.hp10-testdata$hp)^2)
testdata$tst.p.hp11<-predict(qlm.fit,newx=as.matrix(testdata[,c("mpq","wt","drat")])</pre>
, s=0.10*cv.glm.fit$lambda.min,type='response')
model stats<-cbind(model stats,tst.p.hp11=c(0.10,rsquare=rsquare(testdata$hp,testdat
a$tst.p.hp11), msd=msd(testdata$hp, testdata$tst.p.hp11)))
proportion<-c(proportion, 0.10)</pre>
sum((testdata$tst.p.hp11-testdata$hp)^2)
cv.qlm.fit$lambda.min
testdata$tst.p.hp12<-predict(qlm.fit,newx=as.matrix(testdata[,c("mpq","wt","drat")])</pre>
, s=0.05*cv.qlm.fit$lambda.min,type='response')
model stats<-cbind(model stats,tst.p.hp12=c(0.05,rsquare=rsquare(testdata$hp,testdat
a$tst.p.hp12), msd=msd(testdata$hp, testdata$tst.p.hp12)))
proportion<-c(proportion, 0.05)</pre>
sum((testdata$tst.p.hp12-testdata$hp)^2)
testdata$tst.p.hp13<-predict(glm.fit,newx=as.matrix(testdata[,c("mpg","wt","drat")])
, s=0*cv.qlm.fit$lambda.min,type='response')
model stats<-cbind(model stats,tst.p.hp13=c(0.00,rsquare=rsquare(testdata$hp,testdat
a$tst.p.hp13), msd=msd(testdata$hp, testdata$tst.p.hp13)))
proportion<-c(proportion, 0.0)</pre>
sum((testdata$tst.p.hp13-testdata$hp)^2)
testdata$tst.p.hp14<-predict(qlm.fit,newx=as.matrix(testdata[,c("mpq","wt","drat")])
, s=-0.05*cv.glm.fit$lambda.min, type='response')
model stats<-cbind(model stats,tst.p.hp14=c(-0.05,rsquare=rsquare(testdata$hp,testda
ta$tst.p.hp14), msd=msd(testdata$hp, testdata$tst.p.hp14)))
proportion<-c(proportion, -0.05)</pre>
```

```
sum((testdata$tst.p.hp14-testdata$hp)^2)
testdata$tst.p.hp15<-predict(qlm.fit,newx=as.matrix(testdata[,c("mpq","wt","drat")])</pre>
, s=-0.8*cv.glm.fit$lambda.min,type='response')
model stats<-cbind(model stats,tst.p.hp15=c(-0.80,rsquare=rsquare(testdata$hp,testda
ta$tst.p.hp15), msd=msd(testdata$hp, testdata$tst.p.hp15)))
proportion<-c(proportion, -0.80)</pre>
sum((testdata$tst.p.hp15-testdata$hp)^2)
testdata$tst.p.hp16<-predict(qlm.fit,newx=as.matrix(testdata[,c("mpq","wt","drat")])</pre>
, s=-0.90*cv.glm.fit$lambda.min,type='response')
model stats<-cbind(model stats,tst.p.hp16=c(-0.90,rsquare=rsquare(testdata$hp,testda
ta$tst.p.hp16), msd=msd(testdata$hp, testdata$tst.p.hp16)))
proportion<-c(proportion, -0.90)</pre>
sum((testdata$tst.p.hp16-testdata$hp)^2)
testdata$tst.p.hp17<-predict(glm.fit,newx=as.matrix(testdata[,c("mpg","wt","drat")])</pre>
,s=-1*cv.qlm.fit$lambda.min,type='response')
model stats<-cbind(model stats,tst.p.hp17=c(-1.0,rsquare=rsquare(testdata$hp,testdat
a$tst.p.hp17), msd=msd(testdata$hp,testdata$tst.p.hp17)))
proportion<-c(proportion,-1.0)</pre>
sum((testdata$tst.p.hp17-testdata$hp)^2)
testdata$tst.p.hp18<-predict(glm.fit,newx=as.matrix(testdata[,c("mpg","wt","drat")])</pre>
, s=-2*cv.glm.fit$lambda.min, type='response')
model stats<-cbind(model stats,tst.p.hp18=c(-2.0,rsquare=rsquare(testdata$hp,testdat
a$tst.p.hp18), msd=msd(testdata$hp, testdata$tst.p.hp18)))
proportion<-c(proportion, -2.0)</pre>
sum((testdata$tst.p.hp18-testdata$hp)^2)
testdata$tst.p.hp19<-predict(qlm.fit,newx=as.matrix(testdata[,c("mpq","wt","drat")])
, s=-3*cv.glm.fit$lambda.min,type='response')
model stats<-cbind(model stats,tst.p.hp19=c(-3.0,rsquare=rsquare(testdata$hp,testdat
a$tst.p.hp19), msd=msd(testdata$hp,testdata$tst.p.hp19)))
proportion<-c(proportion, -3.0)</pre>
sum((testdata$tst.p.hp19-testdata$hp)^2)
testdata$tst.p.hp20<-predict(glm.fit,newx=as.matrix(testdata[,c("mpg","wt","drat")])
, s=-4*cv.glm.fit$lambda.min,type='response')
model stats<-cbind(model stats,tst.p.hp20=c(-4.0,rsquare=rsquare(testdata$hp,testdat
a$tst.p.hp20), msd=msd(testdata$hp, testdata$tst.p.hp20)))
proportion<-c(proportion, -4.0)</pre>
sum((testdata$tst.p.hp20-testdata$hp)^2)
#model stats<-rbind(model stats,proportion=proportion)</pre>
ggplot(as.data.frame(t(model stats[,20])),aes(x=proportion,y=rsquare))+geom point()
```