

Algorithm: $[A, b] := \text{GAUSSJORDAN_PART1}(A, b)$

Partition $A \rightarrow \left(\begin{array}{c|c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right), b \rightarrow \left(\begin{array}{c} b_T \\ \hline b_B \end{array} \right)$

where A_{TL} is 0×0 , b_T has 0 rows

while $m(A_{TL}) < m(A)$ **do**

Repartition

$$\left(\begin{array}{c|c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \rightarrow \left(\begin{array}{c|c|c} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ \hline A_{20} & a_{21} & A_{22} \end{array} \right), \left(\begin{array}{c} b_T \\ \hline b_B \end{array} \right) \rightarrow \left(\begin{array}{c} b_0 \\ \hline \beta_1 \\ \hline b_2 \end{array} \right)$$

$$\begin{aligned} a_{01} &:= a_{01}/\alpha_{11} & (= u_{01}) \\ a_{21} &:= a_{21}/\alpha_{11} & (= l_{21}) \\ A_{02} &:= A_{02} - a_{01}a_{12}^T & (= A_{02} - u_{01}a_{12}^T) \\ A_{22} &:= A_{22} - a_{21}a_{12}^T & (= A_{22} - l_{21}a_{12}^T) \\ b_0 &:= b_0 - \beta_1 a_{01} & (= b_0 - \beta_1 u_{01}) \\ b_2 &:= b_2 - \beta_1 a_{21} & (= b_2 - \beta_1 l_{21}) \\ a_{01} &:= 0 & \text{(zero vector)} \\ a_{21} &:= 0 & \text{(zero vector)} \end{aligned}$$

Continue with

$$\left(\begin{array}{c|c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \leftarrow \left(\begin{array}{c|c|c} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ \hline A_{20} & a_{21} & A_{22} \end{array} \right), \left(\begin{array}{c} b_T \\ \hline b_B \end{array} \right) \leftarrow \left(\begin{array}{c} b_0 \\ \hline \beta_1 \\ \hline b_2 \end{array} \right)$$

endwhile

Algorithm: $[A, b] := \text{GAUSSJORDAN_PART2}(A, b)$

Partition $A \rightarrow \left(\begin{array}{c|c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right), b \rightarrow \left(\begin{array}{c} b_T \\ \hline b_B \end{array} \right)$

where A_{TL} is 0×0 , b_T has 0 rows

while $m(A_{TL}) < m(A)$ **do**

Repartition

$$\left(\begin{array}{c|c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \rightarrow \left(\begin{array}{c|c|c} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ \hline A_{20} & a_{21} & A_{22} \end{array} \right), \left(\begin{array}{c} b_T \\ \hline b_B \end{array} \right) \rightarrow \left(\begin{array}{c} b_0 \\ \hline \beta_1 \\ \hline b_2 \end{array} \right)$$

$$\begin{aligned} \beta_1 &:= \beta_1/\alpha_{11} \\ \alpha_{11} &:= 1 \end{aligned}$$

Continue with

$$\left(\begin{array}{c|c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \leftarrow \left(\begin{array}{c|c|c} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ \hline A_{20} & a_{21} & A_{22} \end{array} \right), \left(\begin{array}{c} b_T \\ \hline b_B \end{array} \right) \leftarrow \left(\begin{array}{c} b_0 \\ \hline \beta_1 \\ \hline b_2 \end{array} \right)$$

endwhile