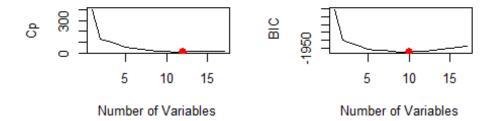
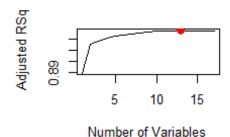
## **Abhishek Reddy Palle**

```
# In this question, we will predict the number of applications received
(Apps) using the other variables in the College data set (ISLR package).
library(ISLR)
library(leaps)
names(College)
## [1] "Private"
                      "Apps"
                                    "Accept"
                                                                 "Top10perc"
                                                  "Enroll"
## [6] "Top25perc"
                                                                 "Room, Board"
                      "F.Undergrad" "P.Undergrad" "Outstate"
                      "Personal"
                                                                 "S.F.Ratio"
## [11] "Books"
                                    "PhD"
                                                  "Terminal"
## [16] "perc.alumni" "Expend"
                                    "Grad.Rate"
dim(College)
## [1] 777 18
bss_fit <- regsubsets(Apps~., data = College, nvmax=17)</pre>
bss_summary = summary(bss_fit)
# (a) Perform best subset selection to the data. What is the best model
obtained according to Cp, BIC and adjusted R2? Show some plots to provide
evidence for your answer, and report the coefficients of the best model.
bss summary$rsq
## [1] 0.8900990 0.9157839 0.9183356 0.9212640 0.9237599 0.9247464 0.9257649
## [8] 0.9268725 0.9276780 0.9283103 0.9288011 0.9289945 0.9291223 0.9291632
## [15] 0.9291878 0.9291885 0.9291887
par(mfrow = c(2,2))
plot(bss_summary$cp ,xlab =" Number of Variables ",ylab="Cp", type="l")
points(which.min (bss_summary$cp), bss_summary$cp [which.min
(bss_summary$cp)], col ="red",cex =2, pch =20)
plot(bss_summary$bic ,xlab=" Number of Variables ",ylab=" BIC", type="l")
points (which.min (bss summary$bic ), bss summary$bic [which.min
(bss summary$bic )], col =" red", cex =2, pch =20)
#3
plot(bss_summary$adjr2 ,xlab =" Number of Variables ", ylab=" Adjusted
RSq", type="1")
```

```
points (which.max(bss summary$adjr2),
bss_summary$adjr2[which.max(bss_summary$adjr2)], col ="red",cex =2, pch =20)
coef(bss_fit , which.min (bss_summary$bic ))
     (Intercept)
                                                     Enroll
                                                                 Top10perc
##
                    PrivateYes
                                       Accept
## -100.51668243 -575.07060789
                                   1.58421887
                                                -0.56220848
                                                              49.13908916
##
       Top25perc
                      Outstate
                                   Room.Board
                                                        PhD
                                                                    Expend
##
    -13.86531103
                   -0.09466457
                                   0.16373674
                                               -10.01608705
                                                                0.07273776
##
       Grad.Rate
      7.33268904
##
```





# (b) Repeat (a) using forward stepwise selection and backwards stepwise selection. How does your answer compare to the results in (a)?

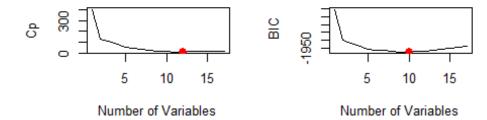
```
#Forward stepwise selection
for_ss <- regsubsets(Apps~., data = College, nvmax=17, method = "forward")
for_ss_summary = summary(for_ss)

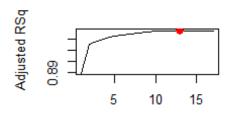
par(mfrow =c(2,2))

#1
plot(for_ss_summary$cp ,xlab =" Number of Variables ",ylab="Cp", type="l")
points(which.min (for_ss_summary$cp), for_ss_summary$cp [which.min
(for_ss_summary$cp)], col ="red",cex =2, pch =20)

#2</pre>
```

```
plot(for_ss_summary$bic ,xlab=" Number of Variables ",ylab=" BIC", type="l")
points (which.min (for_ss_summary$bic ), for_ss_summary$bic [which.min
(for_ss_summary$bic )], col =" red",cex =2, pch =20)
#3
plot(for_ss_summary$adjr2 ,xlab =" Number of Variables ", ylab=" Adjusted
RSq", type="1")
points (which.max(for_ss_summary$adjr2),
for ss summary$adjr2[which.max(for ss summary$adjr2)], col ="red",cex =2, pch
=20)
coef(for_ss , which.min (for_ss_summary$bic ))
##
     (Intercept)
                    PrivateYes
                                      Accept
                                                     Enroll
                                                                Top10perc
## -100.51668243 -575.07060789
                                  1.58421887
                                                -0.56220848
                                                              49.13908916
##
       Top25perc
                                  Room.Board
                                                        PhD
                                                                   Expend
                      Outstate
    -13.86531103
                   -0.09466457
                                                               0.07273776
##
                                  0.16373674
                                              -10.01608705
##
       Grad.Rate
      7.33268904
##
```

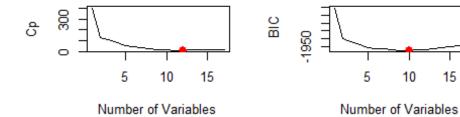


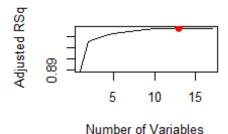


Number of Variables

```
#Backward stepwise selection
back_ss <- regsubsets(Apps~., data = College, nvmax=17, method = "backward")
back_ss_summary = summary(back_ss)
par(mfrow =c(2,2))</pre>
```

```
#1
plot(back ss summary$cp ,xlab =" Number of Variables ",ylab="Cp", type="l")
points(which.min (back_ss_summary$cp), back_ss_summary$cp [which.min
(back_ss_summary$cp)], col ="red",cex =2, pch =20)
#2
plot(back_ss_summary$bic ,xlab=" Number of Variables ",ylab=" BIC", type="l")
points (which.min (back_ss_summary$bic ), back_ss_summary$bic [which.min
(back ss summary$bic )], col =" red",cex =2, pch =20)
plot(back_ss_summary$adjr2 ,xlab =" Number of Variables ", ylab=" Adjusted
RSq", type="1")
points (which.max(back_ss_summary$adjr2),
back_ss_summary$adjr2[which.max(back_ss_summary$adjr2)], col ="red",cex =2,
pch = 20)
coef(back_ss , which.min (back_ss_summary$bic ))
##
     (Intercept)
                    PrivateYes
                                      Accept
                                                     Enroll
                                                                Top10perc
## -100.51668243 -575.07060789
                                  1.58421887
                                                -0.56220848
                                                              49.13908916
##
                                  Room.Board
       Top25perc
                      Outstate
                                                        PhD
                                                                   Expend
                   -0.09466457
##
                                              -10.01608705
                                                               0.07273776
    -13.86531103
                                  0.16373674
##
       Grad.Rate
      7.33268904
##
```





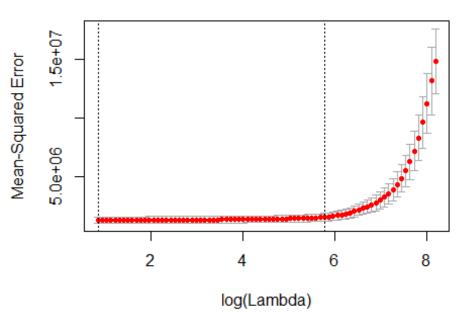
# (c) Fit a lasso model on the data. Use cross-validation to select the optimal value of lambda. Create plots of the cross-validation error as a function of D. Report the resulting coefficient estimates.

```
library(glmnet)
## Loading required package: Matrix
## Loading required package: foreach
## Loaded glmnet 2.0-16

x = model.matrix(Apps~.,College)[,-1]
y = College$Apps
grid = 10^seq (10,-2, length =100)
lasso.mod = glmnet(x,y,alpha =1, lambda =grid)
dim(coef(lasso.mod))
## [1] 18 100

cv.out = cv.glmnet(x,y,alpha =1)
plot(cv.out)
```

## 17 17 15 14 10 4 4 3 2 1 1 1



```
bestlam =cv.out$lambda.min
bestlam
## [1] 2.3456
```

```
predict(lasso.mod, s=bestlam, type="coefficients")[1:18,]
##
     (Intercept)
                    PrivateYes
                                      Accept
                                                    Enroll
                                                               Top10perc
## -471.91198713 -491.00658329
                                  1.56900019
                                               -0.75108809
                                                             47.98058884
##
      Top25perc
                   F. Undergrad
                                 P.Undergrad
                                                              Room.Board
                                                  Outstate
##
    -12.73328855
                    0.04062555
                                  0.04399959
                                                              0.14925171
                                               -0.08298682
##
           Books
                      Personal
                                         PhD
                                                  Terminal
                                                               S.F.Ratio
##
      0.01455346
                    0.02878410
                                 -8.37861131
                                               -3.25247875
                                                             14.44887626
##
     perc.alumni
                        Expend
                                   Grad.Rate
##
                    0.07703557
                                  8.25050995
     -0.05217050
# (d) Fit a ridge regression model on the data. Use cross-validation to
select the optimal value of lambda. Create plots of the cross-validation
error as a function of lambda. Report the resulting coefficient estimates.
library(glmnet)
x=model.matrix(Apps~.,College)[,-1]
v=College$Apps
grid =10<sup>seq</sup> (10,-2, length =100)
ridge.mod = glmnet(x,y,alpha =0, lambda =grid)
coef(ridge.mod)
## 18 x 100 sparse Matrix of class "dgCMatrix"
      [[ suppressing 100 column names 's0', 's1', 's2' ... ]]
##
##
## (Intercept)
                3.001624e+03
                              3.001619e+03
                                            3.001613e+03
                                                          3.001605e+03
## PrivateYes
               -1.451161e-03 -1.918346e-03 -2.535939e-03 -3.352359e-03
## Accept
                5.761598e-07 7.616485e-07
                                            1.006854e-06
                                                          1.331001e-06
## Enroll
                1.364210e-06 1.803403e-06 2.383992e-06
                                                          3.151494e-06
## Top10perc
                2.875188e-05 3.800824e-05 5.024462e-05
                                                          6.642037e-05
## Top25perc
                2.657756e-05 3.513393e-05 4.644496e-05
                                                          6.139744e-05
## F.Undergrad
               2.513585e-07
                              3.322809e-07
                                            4.392555e-07
                                                          5.806695e-07
## P.Undergrad
                              5.176450e-07
                                            6.842956e-07
                3.915797e-07
                                                          9.045976e-07
## Outstate
                              2.467155e-08
                                            3.261432e-08
                1.866318e-08
                                                          4.311419e-08
## Room.Board
                2.251252e-07 2.976019e-07 3.934120e-07
                                                          5.200671e-07
## Books
                1.201804e-06 1.588712e-06
                                            2.100182e-06
                                                          2.776315e-06
## Personal
                3.951405e-07
                              5.223521e-07
                                            6.905181e-07
                                                          9.128232e-07
## PhD
                3.581707e-05 4.734801e-05 6.259123e-05
                                                          8.274182e-05
## Terminal
                3.756761e-05
                             4.966213e-05
                                            6.565035e-05
                                                          8.678579e-05
## S.F.Ratio
                3.616432e-05 4.780710e-05
                                            6.319812e-05
                                                          8.354411e-05
## perc.alumni -1.089892e-05 -1.440773e-05 -1.904617e-05 -2.517790e-05
## Expend
                7.441500e-08
                              9.837219e-08
                                            1.300422e-07
                                                          1.719079e-07
## Grad.Rate
                1.278832e-05 1.690539e-05
                                            2.234792e-05
                                                          2.954262e-05
##
## (Intercept)
                3.001594e+03
                              3.001580e+03
                                            3.001561e+03
                                                          3.001536e+03
## PrivateYes
               -4.431617e-03 -5.858329e-03 -7.744351e-03 -1.023755e-02
                                                          4.064662e-06
## Accept
                1.759503e-06 2.325957e-06
                                            3.074774e-06
## Enroll
                4.166086e-06
                              5.507313e-06
                                            7.280330e-06
                                                          9.624145e-06
## Top10perc
               8.780372e-05 1.160712e-04 1.534389e-04
                                                          2.028367e-04
```

```
## Top25perc
                8.116369e-05
                               1.072934e-04
                                              1.418353e-04
                                                            1.874973e-04
## F.Undergrad
                7.676100e-07
                               1.014734e-06
                                             1.341415e-06
                                                            1.773268e-06
## P.Undergrad
                1.195823e-06
                               1.580805e-06
                                              2.089726e-06
                                                            2.762485e-06
## Outstate
                5.699438e-08
                               7.534314e-08
                                             9.959906e-08
                                                            1.316639e-07
## Room.Board
                6.874975e-07
                               9.088300e-07
                                              1.201418e-06
                                                            1.588200e-06
## Books
                3.670119e-06
                               4.851673e-06
                                              6.413610e-06
                                                            8.478387e-06
## Personal
                1.206697e-06
                               1.595179e-06
                                              2.108726e-06
                                                            2.787601e-06
## PhD
                1.093796e-04
                               1.445931e-04
                                              1.911431e-04
                                                            2.526790e-04
## Terminal
                1.147255e-04
                               1.516600e-04
                                              2.004851e-04
                                                            2.650284e-04
## S.F.Ratio
                1.104402e-04
                               1.459952e-04
                                              1.929967e-04
                                                            2.551294e-04
## perc.alumni -3.328367e-05 -4.399901e-05 -5.816401e-05 -7.688925e-05
                                              3.971276e-07
## Expend
                2.272519e-07
                               3.004131e-07
                                                            5.249778e-07
## Grad.Rate
                3.905356e-05
                               5.162644e-05
                                             6.824699e-05
                                                            9.021829e-05
##
## (Intercept)
                3.001503e+03
                               3.001460e+03
                                              3.001402e+03
                                                            3.001326e+03
## PrivateYes
               -1.353340e-02 -1.789027e-02 -2.364975e-02 -3.126334e-02
## Accept
                5.373230e-06
                               7.103069e-06
                                             9.389796e-06
                                                            1.241268e-05
## Enroll
                1.272251e-05
                               1.681834e-05
                                              2.223273e-05
                                                            2.939015e-05
## Top10perc
                2.681372e-04
                               3.544599e-04
                                             4.685722e-04
                                                            6.194198e-04
## Top25perc
                2.478594e-04
                               3.276538e-04
                                             4.331360e-04
                                                            5.725749e-04
## F.Undergrad
                                             4.096420e-06
                2.344147e-06
                               3.098810e-06
                                                            5.415182e-06
## P.Undergrad
                3.651827e-06
                               4.827473e-06
                                             6.381587e-06
                                                            8.435998e-06
## Outstate
                1.740515e-07
                               2.300851e-07
                                              3.041578e-07
                                                            4.020766e-07
## Room.Board
                2.099501e-06
                               2.775406e-06
                                              3.668904e-06
                                                            4.850042e-06
## Books
                1.120788e-05
                               1.481607e-05
                                              1.958583e-05
                                                            2.589105e-05
## Personal
                3.685027e-06
                               4.871357e-06
                                              6.439591e-06
                                                            8.512663e-06
                                              5.837096e-04
## PhD
                3.340251e-04
                               4.415587e-04
                                                            7.716211e-04
## Terminal
                3.503502e-04
                               4.631391e-04
                                              6.122372e-04
                                                            8.093319e-04
## S.F.Ratio
                3.372647e-04
                               4.458416e-04
                                              5.893720e-04
                                                            7.791076e-04
## perc.alumni -1.016428e-04 -1.343654e-04 -1.776223e-04 -2.348049e-04
                                              1.212748e-06
## Expend
                6.939872e-07
                               9.174057e-07
                                                            1.603168e-06
## Grad.Rate
                1.192629e-04
                               1.576579e-04
                                              2.084133e-04
                                                            2.755082e-04
##
## (Intercept)
                3.001226e+03
                               3.001093e+03
                                              3.000917e+03
                                                            3.000685e+03
## PrivateYes
               -4.132789e-02 -5.463231e-02 -7.221943e-02 -9.546761e-02
## Accept
                1.640870e-05
                               2.169111e-05
                                             2.867397e-05
                                                            3.790460e-05
## Enroll
                3.885167e-05
                               5.135896e-05
                                              6.789237e-05
                                                            8.974770e-05
## Top10perc
                8.188276e-04
                               1.082426e-03
                                              1.430876e-03
                                                            1.891486e-03
## Top25perc
                7.569010e-04
                               1.000562e-03
                                             1.322656e-03
                                                            1.748423e-03
## F.Undergrad
                7.158475e-06
                               9.462948e-06
                                             1.250923e-05
                                                            1.653605e-05
                                              1.948720e-05
## P.Undergrad
                1.115175e-05
                               1.474169e-05
                                                            2.576015e-05
## Outstate
                5.315179e-07
                               7.026289e-07
                                             9.288227e-07
                                                            1.227829e-06
## Room.Board
                6.411413e-06
                               8.475410e-06
                                              1.120382e-05
                                                            1.481048e-05
## Books
                3.422599e-05
                               4.524395e-05
                                              5.980845e-05
                                                            7.906082e-05
## Personal
                1.125307e-05
                               1.487560e-05
                                             1.966414e-05
                                                            2.599393e-05
## PhD
                1.020022e-03
                               1.348383e-03
                                              1.782437e-03
                                                            2.356195e-03
## Terminal
                1.069872e-03
                               1.414279e-03
                                              1.869542e-03
                                                            2.471334e-03
## S.F.Ratio
                1.029921e-03
                               1.361472e-03
                                              1.799746e-03
                                                            2.379089e-03
  perc.alumni -3.103958e-04 -4.103208e-04 -5.424126e-04 -7.170248e-04
## Expend
                2.119270e-06 2.801507e-06
                                            3.703354e-06
                                                            4.895487e-06
```

```
## Grad.Rate
                3.642021e-04
                               4.814477e-04
                                              6.364350e-04
                                                            8.413111e-04
##
## (Intercept)
                3.000378e+03
                               2.999972e+03
                                             2.999436e+03
                                                            2.998728e+03
## PrivateYes
               -1.261987e-01 -1.668205e-01 -2.205150e-01 -2.914872e-01
## Accept
                5.010642e-05
                               6.623559e-05
                                              8.755580e-05
                                                            1.157371e-04
## Enroll
                1.186377e-04
                               1.568258e-04
                                              2.073038e-04
                                                            2.740246e-04
## Top10perc
                                                            5.775095e-03
                2.500350e-03
                               3.305170e-03
                                              4.368985e-03
##
  Top25perc
                 2.311225e-03
                               3.055152e-03
                                              4.038464e-03
                                                            5.338147e-03
## F.Undergrad
                2.185897e-05
                               2.889502e-05
                                              3.819533e-05
                                                            5.048815e-05
## P.Undergrad
                               4.501237e-05
                                              5.949950e-05
                                                            7.864750e-05
                3.405202e-05
## Outstate
                 1.623083e-06
                               2.145560e-06
                                              2.836199e-06
                                                            3.749103e-06
## Room.Board
                1.957804e-05
                               2.588008e-05
                                              3.421030e-05
                                                            4.522114e-05
                                                            2.413779e-04
## Books
                1.045095e-04
                               1.381480e-04
                                              1.826106e-04
## Personal
                3.436086e-05
                               4.542027e-05
                                              6.003807e-05
                                                            7.935833e-05
## PhD
                                                            7.193391e-03
                 3.114610e-03
                               4.117083e-03
                                              5.442109e-03
## Terminal
                 3.266802e-03
                               4.318245e-03
                                              5.707987e-03
                                                            7.544785e-03
## S.F.Ratio
                 3.144893e-03
                               4.157149e-03
                                              5.495133e-03
                                                            7.263589e-03
  perc.alumni -9.478422e-04 -1.252952e-03 -1.656261e-03 -2.189360e-03
## Expend
                6.471320e-06
                               8.554309e-06
                                              1.130760e-05
                                                            1.494678e-05
## Grad.Rate
                1.112132e-03
                               1.470116e-03
                                              1.943308e-03
                                                            2.568767e-03
##
## (Intercept)
                2.997791e+03
                               2.996553e+03
                                              2.994917e+03
                                                            2.992756e+03
## PrivateYes
               -3.852928e-01 -5.092713e-01 -6.731164e-01 -8.896277e-01
## Accept
                               2.022187e-04
                                              2.672862e-04
                                                            3.532756e-04
                1.529861e-04
## Enroll
                3.622115e-04
                               4.787650e-04
                                              6.327988e-04
                                                            8.363477e-04
## Top10perc
                7.633556e-03
                               1.008975e-02
                                              1.333568e-02
                                                            1.762483e-02
                                                            1.628995e-02
## Top25perc
                7.055903e-03
                               9.326068e-03
                                              1.232603e-02
## F.Undergrad
                6.673569e-05
                               8.820898e-05
                                              1.165867e-04
                                                            1.540852e-04
## P.Undergrad
                1.039545e-04
                               1.373994e-04
                                              1.815948e-04
                                                            2.399893e-04
                4.955772e-06
                               6.550676e-06
## Outstate
                                              8.658624e-06
                                                            1.144447e-05
## Room.Board
                5.977467e-05
                               7.900985e-05
                                              1.044311e-04
                                                            1.380250e-04
## Books
                3.190478e-04
                               4.216934e-04
                                              5.573333e-04
                                                            7.365512e-04
## Personal
                1.048922e-04
                               1.386355e-04
                                              1.832228e-04
                                                            2.421309e-04
## PhD
                9.507918e-03
                               1.256660e-02
                                              1.660827e-02
                                                            2.194811e-02
## Terminal
                9.972299e-03
                               1.318024e-02
                                              1.741903e-02
                                                            2.301913e-02
## S.F.Ratio
                9.600896e-03
                               1.268983e-02
                                              1.677172e-02
                                                            2.216514e-02
## perc.alumni -2.893997e-03 -3.825329e-03 -5.056223e-03 -6.682916e-03
## Expend
                 1.975666e-05
                               2.611346e-05
                                              3.451403e-05
                                                            4.561430e-05
## Grad.Rate
                3.395458e-03
                               4.488071e-03
                                              5.932048e-03
                                                            7.840215e-03
##
## (Intercept)
                2.989901e+03
                               2.986129e+03
                                              2.981149e+03
                                                            2.974575e+03
## PrivateYes
               -1.175699e+00 -1.553617e+00 -2.052764e+00 -2.711842e+00
## Accept
                4.669028e-04
                               6.170317e-04
                                              8.153543e-04
                                                            1.077282e-03
## Enroll
                1.105296e-03
                               1.460603e-03
                                              1.929898e-03
                                                            2.549582e-03
## Top10perc
                2.329173e-02
                               3.077762e-02
                                              4.066407e-02
                                                            5.371687e-02
## Top25perc
                2.152679e-02
                               2.844392e-02
                                              3.757810e-02
                                                            4.963573e-02
## F.Undergrad
                2.036293e-04
                               2.690773e-04
                                              3.555148e-04
                                                            4.696386e-04
## P.Undergrad
                3.171323e-04
                               4.190218e-04
                                              5.535581e-04
                                                            7.311360e-04
## Outstate
                1.512592e-05
                               1.999033e-05
                                              2.641689e-05
                                                            3.490560e-05
## Room.Board
                1.824143e-04
                               2.410594e-04
                                              3.185240e-04
                                                            4.208216e-04
```

```
## Books
                              1.286015e-03
                9.733094e-04
                                             1.698915e-03
                                                            2.243908e-03
## Personal
                3.199451e-04
                              4.227080e-04
                                             5.583750e-04
                                                            7.374059e-04
## PhD
                2.900181e-02
                               3.831720e-02
                                             5.061558e-02
                                                            6.684535e-02
## Terminal
                3.041632e-02
                              4.018479e-02
                                             5.308040e-02
                                                            7.009669e-02
## S.F.Ratio
                2.929038e-02
                               3.870160e-02
                                             5.112883e-02
                                                            6.753273e-02
## perc.alumni -8.832477e-03 -1.167262e-02 -1.542458e-02 -2.038004e-02
## Expend
                               7.965214e-05
                                             1.052357e-04
                6.027981e-05
                                                            1.390111e-04
## Grad.Rate
                1.036150e-02
                               1.369241e-02
                                             1.809202e-02
                                                            2.390169e-02
##
## (Intercept)
                2.965902e+03
                               2.954465e+03
                                             2.939425e+03
                                                            2.919615e+03
## PrivateYes
               -3.581768e+00 -4.729432e+00 -6.233352e+00 -8.219727e+00
## Accept
                1.423113e-03
                               1.879542e-03
                                             2.479281e-03
                                                            3.271232e-03
## Enroll
                3.367556e-03
                              4.446752e-03
                                             5.865580e-03
                                                            7.737187e-03
## Top10perc
                7.094314e-02
                              9.366509e-02
                                             1.234633e-01
                                                            1.627915e-01
## Top25perc
                               8.652428e-02
                                             1.140658e-01
                                                            1.503747e-01
                6.554521e-02
## F.Undergrad
                6.202569e-04
                               8.189357e-04
                                             1.080537e-03
                                                            1.425229e-03
## P.Undergrad
                9.654103e-04
                               1.274283e-03
                                             1.680920e-03
                                                            2.216118e-03
## Outstate
                4.611527e-05
                               6.091304e-05
                                             8.010652e-05
                                                            1.056102e-04
## Room.Board
                5.558679e-04
                               7.340686e-04
                                             9.681769e-04
                                                            1.277205e-03
## Books
                2.962898e-03
                               3.910821e-03
                                             5.157797e-03
                                                            6.799542e-03
                                             1.694603e-03
## Personal
                9.735283e-04
                              1.284717e-03
                                                            2.233476e-03
## PhD
                8.825141e-02
                              1.164640e-01
                                             1.535431e-01
                                                            2.023430e-01
## Terminal
                9.253728e-02
                               1.221084e-01
                                             1.610165e-01
                                                            2.121783e-01
## S.F.Ratio
                8.917556e-02
                               1.177127e-01
                                             1.554149e-01
                                                            2.049711e-01
## perc.alumni -2.692313e-02 -3.555925e-02 -4.699018e-02 -6.203821e-02
## Expend
                1.835826e-04
                               2.423682e-04
                                             3.198170e-04
                                                            4.218074e-04
## Grad.Rate
                3.157065e-02
                              4.168924e-02
                                             5.503211e-02
                                                            7.261216e-02
##
                2.893589e+03
## (Intercept)
                              2.859464e+03
                                             2.814835e+03
                                                            2.756666e+03
## PrivateYes
               -1.083054e+01 -1.425580e+01 -1.873878e+01 -2.458760e+01
                                             7.480629e-03
## Accept
                4.313543e-03
                              5.683450e-03
                                                           9.832733e-03
## Enroll
                1.019896e-02
                               1.343185e-02
                                             1.766852e-02
                                                            2.320551e-02
## Top10perc
                2.144716e-01
                               2.822545e-01
                                             3.709371e-01
                                                            4.865871e-01
## Top25perc
                1.980678e-01
                               2.605879e-01
                                             3.423264e-01
                                                            4.488189e-01
## F.Undergrad
                1.878546e-03
                               2.473743e-03
                                             3.253545e-03
                                                            4.272338e-03
## P.Undergrad
                2.919218e-03
                               3.841059e-03
                                             5.046534e-03
                                                            6.617502e-03
## Outstate
                1.391149e-04
                               1.830451e-04
                                             2.404990e-04
                                                            3.153944e-04
## Room.Board
                1.683756e-03
                               2.217793e-03
                                             2.917902e-03
                                                            3.833352e-03
## Books
                8.955991e-03
                               1.178274e-02
                                             1.547823e-02
                                                            2.029249e-02
## Personal
                2.940897e-03
                               3.867519e-03
                                             5.077710e-03
                                                            6.652156e-03
## PhD
                2.663877e-01
                               3.502451e-01
                                             4.597107e-01
                                                            6.020334e-01
## Terminal
                2.793131e-01
                               3.671995e-01
                                             4.818947e-01
                                                            6.309656e-01
                               3.556459e-01
## S.F.Ratio
                2.701274e-01
                                             4.676333e-01
                                                            6.138398e-01
##
  perc.alumni -8.187126e-02 -1.079857e-01 -1.423270e-01 -1.874110e-01
                              7.319621e-04
                                             9.625494e-04
## Expend
                5.559164e-04
                                                            1.263709e-03
## Grad.Rate
                9.575097e-02
                              1.261645e-01
                                             1.660685e-01
                                                            2.183030e-01
##
                              2.583797e+03
                                             2.459083e+03
## (Intercept)
                2.681184e+03
                                                           2.300896e+03
## PrivateYes
               -3.218693e+01 -4.200761e+01 -5.461044e+01 -7.063796e+01
## Accept
                1.290158e-02 1.688954e-02 2.204524e-02 2.866700e-02
```

```
## Enroll
                3.041616e-02
                               3.976299e-02
                                              5.180667e-02
                                                             6.720679e-02
## Top10perc
                6.367677e-01
                               8.307198e-01
                                              1.079430e+00
                                                            1.395473e+00
## Top25perc
                 5.869311e-01
                               7.649916e-01
                                              9.927957e-01
                                                             1.281364e+00
## F.Undergrad
                               7.316479e-03
                5.598483e-03
                                              9.528407e-03
                                                            1.235378e-02
## P.Undergrad
                8.655572e-03
                               1.128410e-02
                                              1.464823e-02
                                                            1.891113e-02
## Outstate
                4.126165e-04
                               5.381488e-04
                                              6.991516e-04
                                                            9.039448e-04
## Room.Board
                 5.026378e-03
                               6.574448e-03
                                              8.572188e-03
                                                            1.113233e-02
## Books
                 2.653542e-02
                               3.458251e-02
                                              4.487442e-02
                                                             5.790499e-02
## Personal
                8.690125e-03
                               1.131056e-02
                                              1.465064e-02
                                                            1.885968e-02
## PhD
                7.861062e-01
                               1.022544e+00
                                              1.323529e+00
                                                            1.702228e+00
## Terminal
                8.236776e-01
                               1.071060e+00
                                              1.385717e+00
                                                            1.781174e+00
## S.F.Ratio
                8.039645e-01
                               1.049912e+00
                                              1.365901e+00
                                                            1.768257e+00
##
  perc.alumni -2.464668e-01 -3.235980e-01 -4.239498e-01 -5.538557e-01
## Expend
                1.655575e-03
                               2.163013e-03
                                              2.816057e-03
                                                             3.649908e-03
## Grad.Rate
                2.864733e-01
                               3.750986e-01
                                              4.897532e-01
                                                             6.371694e-01
##
##
  (Intercept)
                2.102699e+03
                               1.858193e+03
                                              1.562357e+03
                                                            1.212892e+03
## PrivateYes
               -9.078521e+01 -1.157402e+02 -1.460801e+02 -1.821231e+02
## Accept
                 3.710153e-02
                               4.773555e-02
                                              6.097600e-02
                                                            7.721862e-02
## Enroll
                8.670785e-02
                               1.111015e-01
                                              1.411562e-01
                                                            1.775092e-01
## Top10perc
                1.792445e+00
                               2.283925e+00
                                              2.881583e+00
                                                            3.592695e+00
## Top25perc
                1.642289e+00
                               2.086509e+00
                                              2.622293e+00
                                                            3.252482e+00
## F.Undergrad
                1.592648e-02
                               2.038706e-02
                                              2.586886e-02
                                                            3.247677e-02
## P.Undergrad
                2.424391e-02
                               3.080575e-02
                                              3.871160e-02
                                                            4.798583e-02
## Outstate
                 1.161831e-03
                               1.482801e-03
                                              1.876995e-03
                                                            2.354183e-03
## Room.Board
                1.438485e-02
                               1.847328e-02
                                              2.354723e-02
                                                            2.975085e-02
## Books
                7.418981e-02
                               9.420610e-02
                                              1.182961e-01
                                                            1.465317e-01
## Personal
                2.408536e-02
                               3.044880e-02
                                              3.800512e-02
                                                            4.668916e-02
## PhD
                 2.171534e+00
                               2.741839e+00
                                              3.417595e+00
                                                            4.192702e+00
## Terminal
                2.270499e+00
                               2.863871e+00
                                              3.564872e+00
                                                            4.365507e+00
## S.F.Ratio
                2.274636e+00
                               2.902360e+00
                                              3.665465e+00
                                                            4.570278e+00
  perc.alumni -7.209162e-01 -9.339432e-01 -1.202659e+00 -1.537056e+00
##
## Expend
                4.704175e-03
                               6.020961e-03
                                              7.641498e-03
                                                            9.601295e-03
## Grad.Rate
                8.252645e-01
                               1.063036e+00
                                              1.360278e+00
                                                            1.727082e+00
##
                8.119302e+02
                               3.676396e+02 -1.048738e+02 -5.840186e+02
##
  (Intercept)
               -2.237438e+02 -2.701898e+02 -3.199612e+02 -3.708258e+02
## PrivateYes
## Accept
                9.680577e-02
                               1.199816e-01
                                              1.468575e-01
                                                            1.774035e-01
## Enroll
                2.205249e-01
                               2.701413e-01
                                              3.257407e-01
                                                             3.860895e-01
                                              6.354404e+00
                                                            7.413996e+00
## Top10perc
                4.417174e+00
                               5.344901e+00
                                                            6.415854e+00
## Top25perc
                 3.971227e+00
                               4.760922e+00
                                              5.590446e+00
## F.Undergrad
                4.025977e-02
                               4.918130e-02
                                              5.909490e-02
                                                            6.973446e-02
## P.Undergrad
                5.850527e-02
                               6.994230e-02
                                              8.172671e-02
                                                            9.305006e-02
                               3.592227e-03
## Outstate
                 2.923321e-03
                                              4.366961e-03
                                                             5.249677e-03
## Room.Board
                3.720795e-02
                               4.600595e-02
                                              5.618143e-02
                                                            6.770887e-02
## Books
                1.785530e-01
                               2.134149e-01
                                              2.494996e-01
                                                             2.845599e-01
## Personal
                5.625145e-02
                               6.619958e-02
                                              7.577062e-02
                                                            8.396591e-02
## PhD
                 5.045248e+00
                               5.932914e+00
                                              6.791138e+00
                                                            7.536361e+00
## Terminal
                 5.240559e+00
                               6.142699e+00
                                              7.000602e+00
                                                            7.722594e+00
## S.F.Ratio
                5.609676e+00
                               6.757072e+00
                                              7.962231e+00
                                                            9.151880e+00
```

```
## perc.alumni -1.946351e+00 -2.437586e+00 -3.014132e+00 -3.674509e+00
## Expend
                1.192436e-02
                               1.461787e-02
                                             1.766922e-02
                                                            2.104743e-02
## Grad.Rate
                2.173117e+00
                               2.706728e+00
                                             3.333853e+00
                                                            4.056757e+00
##
## (Intercept) -1.043992e+03 -1.458263e+03 -1.804182e+03 -2.066353e+03
## PrivateYes
               -4.200536e+02 -4.648071e+02 -5.025740e+02 -5.318671e+02
## Accept
                                             2.894948e-01
                2.114821e-01
                               2.489066e-01
                                                            3.332152e-01
## Enroll
                4.494218e-01
                               5.134601e-01
                                             5.757010e-01
                                                            6.336451e-01
## Top10perc
                8.483925e+00
                               9.530257e+00
                                             1.052380e+01
                                                            1.144745e+01
## Top25perc
                               7.841425e+00
                                             8.337870e+00
                7.184314e+00
                                                            8.636505e+00
## F.Undergrad
                8.072989e-02
                               9.162011e-02
                                             1.019144e-01
                                                            1.111174e-01
## P.Undergrad
                1.029346e-01
                               1.103401e-01
                                             1.143603e-01
                                                            1.143717e-01
## Outstate
                6.236439e-03
                               7.305875e-03
                                             8.407063e-03
                                                            9.454535e-03
## Room.Board
                8.050435e-02
                               9.438862e-02
                                             1.091033e-01
                                                            1.243056e-01
                3.159534e-01
## Books
                               3.409711e-01
                                             3.573767e-01
                                                            3.637870e-01
## Personal
                8.965814e-02
                               9.181531e-02
                                             8.971699e-02
                                                            8.312910e-02
## PhD
                8.076269e+00
                               8.323631e+00
                                             8.216664e+00
                                                            7.731740e+00
## Terminal
                8.207483e+00
                               8.360791e+00
                                             8.115584e+00
                                                            7.447622e+00
## S.F.Ratio
                1.023339e+01
                               1.112056e+01
                                             1.174331e+01
                                                            1.205718e+01
## perc.alumni -4.410776e+00 -5.211799e+00 -6.060334e+00 -6.930192e+00
                2.470949e-02
                               2.860713e-02
                                             3.269798e-02
                                                            3.694744e-02
## Expend
## Grad.Rate
                4.872354e+00
                               5.769915e+00
                                             6.729143e+00
                                                            7.718258e+00
##
## (Intercept) -2.239443e+03 -2.326351e+03 -2.339483e+03 -2.293252e+03
## PrivateYes
               -5.518657e+02 -5.634574e+02 -5.672886e+02 -5.651963e+02
## Accept
                3.800196e-01
                              4.302041e-01
                                             4.838692e-01
                                                            5.415447e-01
## Enroll
                6.844843e-01
                               7.257911e-01
                                             7.549247e-01
                                                            7.696982e-01
## Top10perc
                1.231498e+01
                               1.314437e+01
                                             1.399350e+01
                                                            1.492178e+01
## Top25perc
                8.719261e+00
                               8.579376e+00
                                             8.233177e+00
                                                            7.693607e+00
## F.Undergrad
                1.187470e-01
                               1.243525e-01
                                             1.275520e-01
                                                            1.279847e-01
## P.Undergrad
                1.101826e-01
                               1.020863e-01
                                             9.089490e-02
                                                            7.777716e-02
## Outstate
                1.030837e-02
                               1.077920e-02
                                             1.065072e-02
                                                            9.652874e-03
## Room.Board
                1.395062e-01
                               1.541583e-01
                                             1.676565e-01
                                                            1.793774e-01
## Books
                3.599089e-01
                               3.465923e-01
                                             3.255758e-01
                                                            2.990406e-01
## Personal
                7.253859e-02
                               5.891017e-02
                                             4.376305e-02
                                                            2.867105e-02
## PhD
                6.894306e+00
                               5.767155e+00
                                             4.452005e+00
                                                            3.046101e+00
## Terminal
                6.386378e+00
                               5.007848e+00
                                             3.424575e+00
                                                            1.760167e+00
## S.F.Ratio
                1.209978e+01
                               1.191289e+01
                                             1.163805e+01
                                                            1.139402e+01
## perc.alumni -7.799258e+00 -8.622008e+00 -9.368269e+00 -9.984593e+00
## Expend
                4.131960e-02
                               4.578365e-02
                                             5.027078e-02
                                                            5.471620e-02
## Grad.Rate
                8.693721e+00
                               9.606567e+00
                                             1.040288e+01
                                                            1.104309e+01
##
## (Intercept) -2.202704e+03 -2.084290e+03 -1.949206e+03 -1.805760e+03
## PrivateYes
               -5.606455e+02 -5.533251e+02 -5.465423e+02 -5.407085e+02
## Accept
                6.037569e-01
                               6.707425e-01
                                             7.422987e-01
                                                            8.176940e-01
## Enroll
                7.673029e-01
                               7.460597e-01
                                             7.046287e-01
                                                            6.449477e-01
## Top10perc
                1.596728e+01
                               1.723459e+01
                                             1.872919e+01
                                                            2.048255e+01
## Top25perc
                6.972337e+00
                               6.084209e+00
                                             5.044212e+00
                                                            3.869387e+00
## F.Undergrad
                1.254490e-01
                               1.199131e-01
                                             1.117175e-01
                                                            1.012262e-01
## P.Undergrad
                6.407257e-02 5.125971e-02
                                             4.038183e-02
                                                            3.212733e-02
```

```
## Outstate
                7.599283e-03 4.210320e-03 -4.361216e-04 -6.268056e-03
                                                          2.022578e-01
## Room.Board
                1.889080e-01 1.957722e-01 2.001440e-01
## Books
                2.696155e-01
                              2.391602e-01
                                            2.098600e-01
                                                          1.827551e-01
## Personal
                1.497891e-02 4.003623e-03 -3.891415e-03 -8.631141e-03
## PhD
                1.643095e+00
                              3.111222e-01 -8.959688e-01 -1.964431e+00
## Terminal
                1.490101e-01 -1.316956e+00 -2.554886e+00 -3.538636e+00
## S.F.Ratio
                             1.126906e+01
                                            1.145528e+01
                1.120432e+01
                                                          1.172025e+01
## perc.alumni -1.039968e+01 -1.060097e+01 -1.052992e+01 -1.017522e+01
## Expend
                5.904154e-02 6.315135e-02
                                            6.690717e-02
                                                          7.017382e-02
## Grad.Rate
                1.150245e+01 1.178011e+01
                                            1.187639e+01
                                                          1.180568e+01
##
## (Intercept) -1.660613e+03 -1.517138e+03 -1.378126e+03 -1.246208e+03
## PrivateYes -5.348672e+02 -5.299185e+02 -5.259011e+02 -5.225365e+02
## Accept
                8.963028e-01 9.763456e-01 1.055837e+00
                                                          1.132347e+00
## Enroll
                5.658504e-01 4.699828e-01
                                            3.594529e-01
                                                          2.392115e-01
## Top10perc
                2.256065e+01 2.491605e+01 2.748685e+01
                                                          3.017251e+01
## Top25perc
                2.547772e+00
                              1.099547e+00 -4.520017e-01 -2.060498e+00
## F.Undergrad
                8.924180e-02
                              7.672094e-02 6.482096e-02
                                                          5.441166e-02
## P.Undergrad
                2.690040e-02
                              2.446828e-02
                                            2.434292e-02
                                                          2.583796e-02
## Outstate
               -1.328091e-02 -2.108063e-02 -2.927710e-02 -3.746180e-02
## Room.Board
                              1.999132e-01
                                            1.964290e-01
                2.019966e-01
                                                          1.920703e-01
## Books
                1.579315e-01
                              1.357697e-01
                                            1.162840e-01
                                                          9.935594e-02
## Personal
               -1.012061e-02 -9.031903e-03 -6.037431e-03 -1.891095e-03
## PhD
               -2.913702e+00 -3.755372e+00 -4.506115e+00 -5.176592e+00
## Terminal
               -4.251564e+00 -4.706505e+00 -4.934534e+00 -4.983937e+00
## S.F.Ratio
                1.220338e+01
                             1.276267e+01
                                            1.333607e+01
                                                          1.386374e+01
## perc.alumni -9.602712e+00 -8.838767e+00 -7.939901e+00 -6.967000e+00
## Expend
                7.294585e-02 7.515295e-02 7.680655e-02
                                                          7.795251e-02
## Grad.Rate
                1.162342e+01 1.135576e+01
                                            1.104009e+01
                                                          1.070623e+01
##
## (Intercept) -1.123888e+03 -1.012783e+03 -913.94835456 -826.99736562
## PrivateYes -5.195540e+02 -5.167427e+02 -514.02650361 -511.46633915
## Accept
                1.203749e+00
                              1.268440e+00
                                              1.32554820
                                                             1.37516661
## Enroll
                1.131081e-01 -1.298535e-02
                                             -0.13479022
                                                            -0.24930224
## Top10perc
                3.285961e+01
                              3.544319e+01
                                             37.83907977
                                                            40.00784506
## Top25perc
               -3.672347e+00 -5.228199e+00
                                             -6.67978792
                                                           -8.00010082
## F.Undergrad
               4.631037e-02 4.062809e-02
                                              0.03728163
                                                             0.03586360
## P.Undergrad
                2.826309e-02
                                              0.03375669
                              3.103741e-02
                                                             0.03620796
## Outstate
               -4.526283e-02 -5.239849e-02
                                              -0.05869930
                                                            -0.06411550
## Room.Board
                1.872442e-01
                             1.823499e-01
                                              0.17764696
                                                             0.17327607
## Books
                8.485524e-02
                              7.253803e-02
                                                             0.05355615
                                              0.06219630
## Personal
                2.759499e-03
                              7.404768e-03
                                              0.01171931
                                                             0.01556643
## PhD
               -5.771209e+00 -6.294093e+00
                                              -6.74729818
                                                            -7.13727588
## Terminal
               -4.905766e+00 -4.749943e+00
                                              -4.55665726
                                                            -4.35364685
## S.F.Ratio
                1.432001e+01
                             1.468453e+01
                                             14.95828735
                                                            15.14733557
## perc.alumni -5.983495e+00 -5.038068e+00
                                              -4.16612125
                                                            -3.38214013
## Expend
                7.868238e-02
                             7.907562e-02
                                              0.07922345
                                                             0.07918792
## Grad.Rate
                1.038301e+01 1.008311e+01
                                              9.81592001
                                                             9.58026314
##
## (Intercept) -753.28822577 -692.11373494 -640.86788169 -599.03612139
```

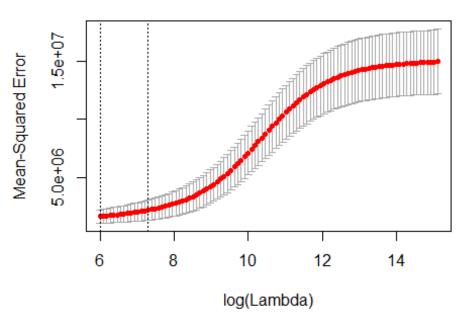
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## PrivateYes
                -508.95287354 -506.54977167 -504.41689891 -502.53082427
## Accept
                   1.41686360
                                  1.45118499
                                                1.47959696
                                                               1.50259631
## Enroll
                  -0.35373409
                                 -0.44604226
                                                -0.52706158
                                                              -0.59621253
## Top10perc
                  41.88632597
                                 43.46814236
                                               44.80196206
                                                              45.89581751
## Top25perc
                  -9.15553164
                                -10.13809652
                                               -10.97066941
                                                              -11.65784920
## F.Undergrad
                   0.03616475
                                  0.03760631
                                                0.03968098
                                                               0.04205273
## P.Undergrad
                   0.03823363
                                  0.03982386
                                                0.04106082
                                                               0.04198650
## Outstate
                  -0.06863348
                                 -0.07232103
                                                -0.07530760
                                                              -0.07768552
## Room.Board
                   0.16938050
                                  0.16601715
                                                0.16311030
                                                               0.16067042
## Books
                   0.04655094
                                  0.04095334
                                                               0.03288578
                                                0.03644576
## Personal
                   0.01879932
                                  0.02142721
                                                0.02358055
                                                               0.02529262
## PhD
                  -7.45949941
                                 -7.72008191
                                                -7.93307674
                                                              -8.10262469
## Terminal
                                 -3.99761613
                                                -3.85556809
                                                              -3.73904265
                  -4.16370623
## S.F.Ratio
                  15.27689427
                                 15.36155302
                                               15.40751864
                                                              15.43027045
   perc.alumni
                                 -2.14083469
                                                              -1.27310742
##
                  -2.70716550
                                                -1.66401003
## Expend
                   0.07907971
                                  0.07894462
                                                0.07877944
                                                               0.07862053
## Grad.Rate
                   9.38772754
                                  9.23438255
                                                9.10753698
                                                               9.00682496
##
## (Intercept) -565.93241041 -539.61642150 -518.83668369 -503.09448370
## PrivateYes
                -500.87592417 -499.48621216 -498.34469883 -497.40998332
## Accept
                   1.52071649
                                  1.53504316
                                                1.54630392
                                                               1.55483604
## Enroll
                  -0.65317376
                                 -0.69987628
                                                -0.73770495
                                                              -0.76699616
  Top10perc
                  46.76519645
                                 47.45697849
                                               48.00307048
                                                              48.41749265
  Top25perc
                 -12.20824480
                                -12.64839655
                                               -12.99727434
                                                              -13.26405131
## F.Undergrad
                   0.04440861
                                  0.04659999
                                                0.04854416
                                                               0.05014443
## P.Undergrad
                   0.04265623
                                  0.04314293
                                                0.04349538
                                                               0.04374464
## Outstate
                  -0.07954675
                                                -0.08212718
                                                              -0.08298876
                                 -0.08099957
                                  0.15709570
## Room.Board
                   0.15869563
                                                0.15581189
                                                               0.15483153
## Books
                   0.03013345
                                  0.02799823
                                                0.02634917
                                                               0.02511358
## Personal
                   0.02660925
                                  0.02763117
                                                0.02842147
                                                               0.02900635
## PhD
                  -8.23365331
                                 -8.33556080
                                                -8.41443219
                                                              -8.47301799
## Terminal
                  -3.64701175
                                 -3.57464094
                                                -3.51831111
                                                              -3.47619076
## S.F.Ratio
                  15.44156191
                                 15.44420669
                                               15.44192424
                                                              15.43959147
   perc.alumni
                  -0.96224314
                                 -0.71441463
                                                -0.51828778
                                                              -0.36857065
##
  Expend
                   0.07849033
                                  0.07837943
                                                0.07828706
                                                               0.07822280
## Grad.Rate
                   8.93045478
                                  8.87125786
                                                8.82547563
                                                               8.79248754
##
## (Intercept) -491.02115481 -481.25296842 -474.09675513 -468.37823221
## PrivateYes
                -496.69865637 -496.15524903 -495.78686337 -495.46990089
## Accept
                   1.56134911
                                  1.56657487
                                                 1.57037976
                                                               1.57342391
## Enroll
                  -0.78972459
                                 -0.80827042
                                                -0.82190613
                                                               -0.83293277
## Top10perc
                  48.73383014
                                 48.98870976
                                               49.17293410
                                                              49.32167492
## Top25perc
                 -13.46893193
                                -13.63322040
                                               -13.75355389
                                                             -13.84963169
## F.Undergrad
                   0.05144140
                                  0.05254153
                                                0.05337216
                                                               0.05405741
## P.Undergrad
                   0.04392375
                                  0.04405842
                                                0.04415063
                                                               0.04422150
## Outstate
                  -0.08364474
                                 -0.08415210
                                                -0.08452506
                                                              -0.08481543
## Room.Board
                   0.15408038
                                  0.15346445
                                                0.15302332
                                                               0.15266006
## Books
                   0.02418557
                                  0.02344931
                                                0.02292695
                                                               0.02250281
## Personal
                   0.02944411
                                  0.02979663
                                                0.03004294
                                                               0.03024412
## PhD
                  -8.51723703
                                 -8.55291705
                                                -8.57846765
                                                              -8.59908438
```

```
## Terminal
                  -3.44448941
                                 -3.41901063
                                               -3.40094464
                                                              -3.38619805
## S.F.Ratio
                  15.43471108
                                15.42775084
                                               15.41933783
                                                              15.41385709
##
  perc.alumni
                  -0.25298023
                                 -0.16035411
                                                -0.09148242
                                                              -0.03745197
## Expend
                   0.07817436
                                 0.07812618
                                                0.07809507
                                                               0.07806537
## Grad.Rate
                   8.76788370
                                 8.74712195
                                                8.73272168
                                                               8.72061765
##
  (Intercept) -463.91980972 -461.02111173 -458.34025487 -456.44652837
## PrivateYes
                -495.23105966 -495.11642787
                                             -494.93282045
                                                            -494.81566173
## Accept
                   1.57578864
                                 1.57730842
                                                1.57874959
                                                               1.57976411
## Enroll
                  -0.84158303
                                 -0.84714316
                                                -0.85245946
                                                              -0.85622367
## Top10perc
                  49.43730296
                                49.51060748
                                               49.58148153
                                                              49.63148611
## Top25perc
                 -13.92421114
                               -13.97241791
                                              -14.01806211
                                                             -14.05006991
## F.Undergrad
                   0.05460602
                                 0.05496090
                                                0.05530371
                                                               0.05554883
## P.Undergrad
                   0.04427393
                                 0.04430365
                                                0.04433646
                                                               0.04435735
## Outstate
                  -0.08503650
                                 -0.08517874
                                                -0.08531769
                                                              -0.08541079
## Room.Board
                   0.15237501
                                 0.15220337
                                                0.15202450
                                                               0.15190020
## Books
                   0.02217631
                                 0.02196800
                                                0.02176842
                                                               0.02162334
## Personal
                   0.03040016
                                 0.03049064
                                                0.03058891
                                                               0.03065658
## PhD
                  -8.61505414
                                 -8.62524452
                                               -8.63477946
                                                              -8.64159239
## Terminal
                  -3.37481733
                                 -3.36763436
                                                -3.36077039
                                                              -3.35585393
## S.F.Ratio
                  15.40887244
                                15.40299688
                                               15.40200143
                                                              15.40084137
   perc.alumni
                   0.00448985
                                 0.03192099
                                                0.05740087
                                                               0.07492396
  Expend
##
                   0.07804044
                                 0.07802653
                                                0.07801279
                                                               0.07800149
## Grad.Rate
                   8.71102185
                                 8.70498909
                                                8.69950463
                                                               8.69529939
##
   (Intercept) -455.20105116 -453.98456323 -452.86297188 -451.84835886
                -494.74972770 -494.67935924 -494.59702893 -494.51499270
## PrivateYes
## Accept
                   1.58042733
                                 1.58107161
                                                1.58167350
                                                               1.58222178
## Enroll
                  -0.85868268
                                 -0.86108039
                                                -0.86334136
                                                              -0.86542543
## Top10perc
                  49.66388915
                                49.69546400
                                               49.72537149
                                                              49.75293930
## Top25perc
                 -14.07104685
                               -14.09143941
                                              -14.11038988
                                                             -14.12750748
## F.Undergrad
                                                               0.05615822
                   0.05570944
                                 0.05586697
                                                0.05601734
## P.Undergrad
                   0.04437017
                                 0.04438371
                                                0.04439723
                                                               0.04440950
## Outstate
                  -0.08547123
                                 -0.08553156
                                                -0.08558732
                                                              -0.08563580
## Room.Board
                   0.15182225
                                 0.15174238
                                                0.15166282
                                                               0.15158682
## Books
                   0.02152805
                                 0.02144149
                                                0.02136005
                                                               0.02128466
## Personal
                   0.03069906
                                 0.03074167
                                                0.03078510
                                                               0.03082703
## PhD
                  -8.64605668
                                 -8.65033865
                                               -8.65432575
                                                              -8.65797767
## Terminal
                  -3.35268272
                                 -3.34962934
                                                -3.34675317
                                                              -3.34409686
## S.F.Ratio
                  15.39928193
                                15.39797135
                                               15.39783801
                                                              15.39831030
   perc.alumni
                   0.08653536
                                 0.09804528
                                                0.10855891
                                                               0.11783496
## Expend
                   0.07799458
                                 0.07798773
                                                0.07798042
                                                               0.07797237
## Grad.Rate
                   8.69255472
                                 8.69002005
                                                8.68759740
                                                               8.68521947
##
## (Intercept) -450.93718935 -450.12509864 -449.40828988 -448.78203801
## PrivateYes
                -494.44372716 -494.38698125 -494.34369837 -494.31092043
## Accept
                   1.58271243
                                 1.58314568
                                                1.58352431
                                                               1.58385256
## Enroll
                  -0.86731493
                                 -0.86900691
                                                -0.87050793
                                                              -0.87183019
  Top10perc
                  49.77774680
                                49.79963953
                                               49.81867734
                                                              49.83505781
## Top25perc
                 -14.14268361
                               -14.15596655
                                              -14.16748474
                                                             -14.17740294
```

```
## F.Undergrad
                   0.05628848
                                  0.05640780
                                                 0.05651630
                                                                0.05661440
## P.Undergrad
                   0.04441994
                                  0.04442850
                                                 0.04443533
                                                                0.04444067
## Outstate
                  -0.08567637
                                 -0.08570968
                                                -0.08573690
                                                               -0.08575920
## Room.Board
                   0.15151662
                                  0.15145333
                                                 0.15139718
                                                                0.15134787
## Books
                   0.02121738
                                  0.02115933
                                                 0.02111048
                                                                0.02107003
## Personal
                   0.03086568
                                  0.03090023
                                                 0.03093052
                                                                0.03095675
## PhD
                  -8.66127163
                                 -8.66418687
                                                -8.66671380
                                                               -8.66886205
## Terminal
                  -3.34170848
                                 -3.33962422
                                                -3.33785463
                                                               -3.33638505
## S.F.Ratio
                  15.39869727
                                 15.39869024
                                                15.39829058
                                                               15.39762940
   perc.alumni
                                  0.13310284
                                                 0.13936925
                                                                0.14485142
##
                   0.12596523
## Expend
                   0.07796379
                                  0.07795514
                                                 0.07794689
                                                                0.07793936
## Grad.Rate
                   8.68290574
                                  8.68071987
                                                 8.67872326
                                                                8.67695243
##
## (Intercept) -448.23991308 -447.77403369 -447.37579398 -447.03658576
## PrivateYes
                -494.28566020
                              -494.26563405 -494.24931729
                                                            -494.23574722
## Accept
                   1.58413542
                                  1.58437807
                                                 1.58458556
                                                                1.58476260
## Enroll
                  -0.87298890
                                 -0.87400038
                                                -0.87488088
                                                               -0.87564584
##
  Top10perc
                  49.84904766
                                 49.86093457
                                                49.87099879
                                                               49.87949892
##
  Top25perc
                 -14.18589778
                                -14.19314405
                                               -14.19930682
                                                              -14.20453726
## F.Undergrad
                   0.05670268
                                                 0.05685247
                                                                0.05691543
                                  0.05678179
## P.Undergrad
                   0.04444476
                                  0.04444782
                                                 0.04445003
                                                                0.04445156
## Outstate
                  -0.08577755
                                 -0.08579271
                                                -0.08580527
                                                               -0.08581569
## Room.Board
                   0.15130484
                                  0.15126744
                                                 0.15123502
                                                                0.15120696
## Books
                   0.02103687
                                  0.02100986
                                                 0.02098793
                                                                0.02097018
## Personal
                   0.03097926
                                  0.03099848
                                                 0.03101481
                                                                0.03102865
## PhD
                  -8.67065946
                                 -8.67214544
                                                -8.67336362
                                                               -8.67435648
## Terminal
                  -3.33518427
                                 -3.33421412
                                                -3.33343638
                                                               -3.33281648
## S.F.Ratio
                  15.39684653
                                 15.39604270
                                               15.39527541
                                                               15.39457095
   perc.alumni
                   0.14962049
                                  0.15374478
                                                 0.15729384
                                                                0.16033700
##
  Expend
                   0.07793270
                                  0.07792694
                                                 0.07792202
                                                                0.07791786
##
  Grad.Rate
                   8.67541692
                                  8.67410665
                                                 8.67300081
                                                                8.67207451
##
   (Intercept) -446.74830401 -446.50361548 -446.29605124 -446.11999448
## PrivateYes
                -494.22430860 -494.21458243 -494.20626019 -494.19910151
## Accept
                   1.58491344
                                  1.58504187
                                                 1.58515120
                                                                1.58524428
## Enroll
                  -0.87630955
                                 -0.87688492
                                                -0.87738348
                                                               -0.87781541
## Top10perc
                  49.88666627
                                 49.89270385
                                               49.89778753
                                                               49.90206822
## Top25perc
                 -14.20897065
                                -14.21272600
                                               -14.21590665
                                                              -14.21860143
## F.Undergrad
                   0.05697139
                                  0.05702103
                                                 0.05706499
                                                                0.05710387
## P.Undergrad
                   0.04445255
                                  0.04445312
                                                 0.04445338
                                                                0.04445340
## Outstate
                  -0.08582434
                                 -0.08583154
                                                -0.08583752
                                                               -0.08584251
## Room.Board
                   0.15118272
                                  0.15116179
                                                 0.15114373
                                                                0.15112815
## Books
                   0.02095584
                                  0.02094428
                                                 0.02093498
                                                                0.02092752
## Personal
                   0.03104034
                                  0.03105021
                                                 0.03105852
                                                                0.03106553
## PhD
                  -8.67516240
                                 -8.67581455
                                                -8.67634098
                                                               -8.67676502
## Terminal
                  -3.33232477
                                 -3.33193652
                                                -3.33163139
                                                               -3.33139275
## S.F.Ratio
                  15.39393765
                                 15.39337506
                                               15.39287905
                                                               15.39244418
  perc.alumni
                   0.16294053
                                  0.16516527
                                                 0.16706547
                                                                0.16868856
## Expend
                   0.07791437
                                  0.07791146
                                                 0.07790904
                                                                0.07790702
## Grad.Rate
                   8.67130271
                                  8.67066221
                                                 8.67013233
                                                                8.66969506
```

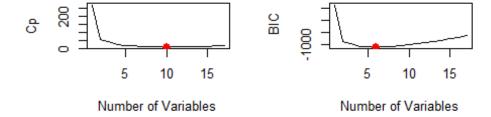
```
cv.out = cv.glmnet(x,y,alpha =0)
plot(cv.out)
```

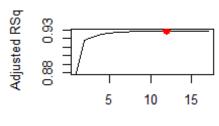




```
bestlam =cv.out$lambda.min
bestlam
## [1] 400.4766
predict(ridge.mod, s=bestlam, type="coefficients")[1:18,]
##
     (Intercept)
                    PrivateYes
                                                    Enroll
                                                               Top10perc
                                      Accept
## -1.512577e+03 -5.297867e+02 9.789533e-01 4.663570e-01 2.500038e+01
##
                   F.Undergrad
                                                              Room.Board
       Top25perc
                                 P.Undergrad
                                                  Outstate
   1.048650e+00 7.633057e-02 2.446417e-02 -2.134950e-02
##
                                                            1.997989e-01
##
           Books
                      Personal
                                         PhD
                                                  Terminal
                                                               S.F.Ratio
   1.351305e-01 -8.933673e-03 -3.779999e+00 -4.713986e+00 1.278148e+01
##
##
     perc.alumni
                        Expend
                                   Grad.Rate
## -8.809281e+00 7.520720e-02 1.134540e+01
# (e) Now split the data set into a training set and a test set.
# i. Fit the best models obtained in the best subset selection (according to
Cp, BIC or adjusted R2) to the training set, and report the test error
obtained.
set.seed(1)
train= sample(c(TRUE, FALSE), nrow(College), rep=TRUE)
test=(!train)
```

```
regfit.best = regsubsets(Apps~., data=College[train,], nvmax=18)
regfit.summary = summary(regfit.best)
par(mfrow = c(2,2))
#1
plot(regfit.summary$cp ,xlab =" Number of Variables ",ylab="Cp", type="l")
points(which.min (regfit.summary$cp), regfit.summary$cp [which.min
(regfit.summary$cp)], col ="red",cex =2, pch =20)
#2
plot(regfit.summary$bic ,xlab=" Number of Variables ",ylab=" BIC", type="l")
points (which.min (regfit.summary$bic ), regfit.summary$bic [which.min
(regfit.summary$bic )], col =" red",cex =2, pch =20)
#3
plot(regfit.summary$adjr2 ,xlab =" Number of Variables ", ylab=" Adjusted
RSq", type="1")
points (which.max(regfit.summary$adjr2),
regfit.summary$adjr2[which.max(regfit.summary$adjr2)], col ="red",cex =2, pch
=20)
#building an "X" matrix from test data
test.mat = model.matrix(Apps~.,data=College[test,])
coefi=coef(regfit.best,id=which.min (regfit.summary$bic))
pred=test.mat[,names(coefi)]%*%coefi
mean((College$Apps[test]-pred)^2)
## [1] 1635683
```

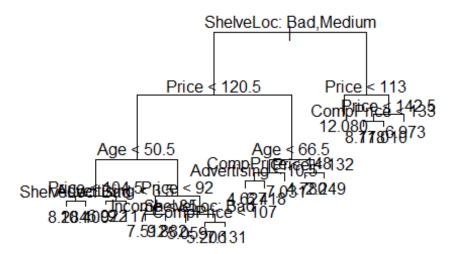




Number of Variables

```
# ii. Fit a lasso model to the training set, with lambda chosen by cross
validation. Report the test error obtained.
library(glmnet)
set.seed (1)
lasso.mod =glmnet (x[train ,],y[train],alpha =1, lambda =grid)
cv.out =cv.glmnet (x[train ,],y[train],alpha =1)
bestlam = cv.out$lambda.min
lasso.pred = predict (lasso.mod ,s=bestlam ,newx=x[test ,])
mean(( lasso.pred - y[test])^2)
## [1] 1612366
# iii. Fit a ridge regression model to the training set, with 🛭 chosen by
cross validation. Report the test error obtained.
ridge.mod = glmnet(x[train,], y[train],alpha =0, lambda =grid)
ridge.pred = predict(ridge.mod ,s=4 , newx = x[test ,])
mean(( ridge.pred -y[test])^2)
## [1] 1547703
# iv. Compare the test errors obtained in the above analysis (i-iii) and
determine the optimal model.
# The following are the test errors for the above three models :
# best subset selection - 1635683
```

```
# Lasso model - 1612366
# ridge model - 1547703
# Ridge regression model is the optimal model.
# In the lab, a classification tree was applied to the Carseats data set
after converting Sales into a binary response variable. This question will
seek to predict Sales using regression trees and related approaches, treating
the response as a quantitative variable (that is, without the conversion).
# (a) Split the data set into a training set and a test set.
library(ISLR)
set.seed(1)
train <- sample(1:nrow(Carseats), nrow(Carseats) / 2)</pre>
Carseats train <- Carseats[train, ]</pre>
Carseats_test <- Carseats[-train, ]</pre>
# (b) Fit a regression tree to the training set. Plot the tree, and interpret
the results. Then compute the test MSE.
library(tree)
tree_carseats <- tree(Sales ~ ., data = Carseats_train)</pre>
summary(tree_carseats)
##
## Regression tree:
## tree(formula = Sales ~ ., data = Carseats_train)
## Variables actually used in tree construction:
## [1] "ShelveLoc"
                     "Price"
                                   "Age"
                                                  "Advertising" "Income"
## [6] "CompPrice"
## Number of terminal nodes: 18
## Residual mean deviance: 2.36 = 429.5 / 182
## Distribution of residuals:
      Min. 1st Qu. Median
                              Mean 3rd Qu.
                                               Max.
## -4.2570 -1.0360 0.1024 0.0000 0.9301 3.9130
plot(tree_carseats)
text(tree_carseats, pretty = 0)
```

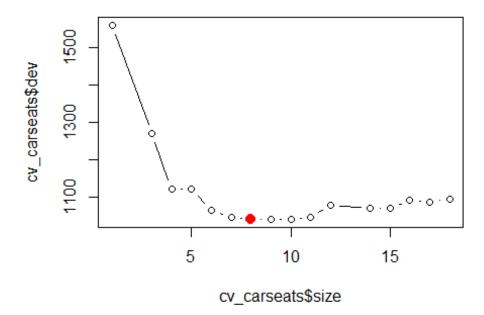


```
yhat <- predict(tree_carseats, Carseats_test)
mean((yhat - Carseats_test$Sales)^2)

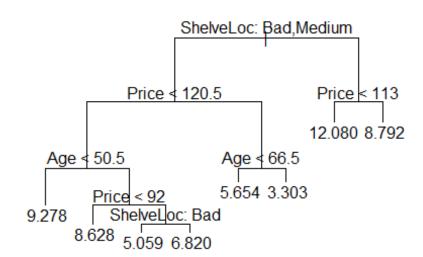
## [1] 4.148897

# (c) Prune the tree obtained in (b). Use cross validation to determine the optimal level of tree complexity. Plot the pruned tree and interpret the results. Compute the test MSE of the pruned tree. Does pruning improve the test error?

cv_carseats <- cv.tree(tree_carseats)
plot(cv_carseats$size, cv_carseats$dev, type = "b")
tree_min <- which.min(cv_carseats$dev)
points(tree_min, cv_carseats$dev[tree_min], col = "red", cex = 2, pch = 20)</pre>
```

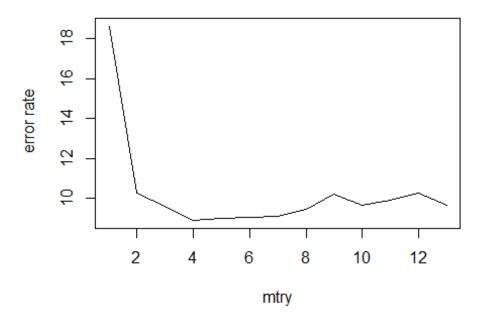


```
prune_carseats <- prune.tree(tree_carseats, best = 8)
plot(prune_carseats)
text(prune_carseats, pretty = 0)</pre>
```



```
##(d) Use the bagging approach to analyze the data. What test MSE do you
obtain? Determine which variables are most important.
library(randomForest)
## randomForest 4.6-14
## Type rfNews() to see new features/changes/bug fixes.
bag.carseats <- randomForest(Sales ~ ., data = Carseats_train, mtry = 10,</pre>
ntree = 500)
yhat.bag <- predict(bag.carseats, newdata = Carseats test)</pre>
mean((yhat.bag - Carseats_test$Sales)^2)
## [1] 2.553118
importance(bag.carseats)
##
               IncNodePurity
## CompPrice
                  130.725006
## Income
                   77.495031
## Advertising
                  124.129450
## Population
                  62.078103
## Price
                  505.500563
## ShelveLoc
                  325.698430
## Age
                  192.250330
## Education
                  40.007558
## Urban
                    8.741943
## US
                   14.682941
# We may conclude that "Price" and "ShelveLoc" are the two most important
variables.
# (e) Use random forests to analyze the data. What test MSE do you obtain?
Determine which variables are most important.
rf.carseats <- randomForest(Sales ~ ., data = Carseats_train, mtry = 3, ntree</pre>
= 500, importance = TRUE)
yhat.rf <- predict(rf.carseats, newdata = Carseats_test)</pre>
mean((yhat.rf - Carseats_test$Sales)^2)
## [1] 3.286144
importance(rf.carseats)
##
                  %IncMSE IncNodePurity
## CompPrice
                8.3370363
                              129.69721
## Income
                4.0540506
                              127.70485
## Advertising 11.9343057
                              139.03662
## Population 0.6266783
                              97.93305
## Price
               38.4595875
                              388.45041
## ShelveLoc 29.8867032
                            234.02006
```

```
## Age
              18.1019639
                             197.17165
## Education 2.3638614
                              63.07024
## Urban
              -0.5623597
                              15.93606
## US
               6.2576901
                              32.71135
# We may conclude that, in this case also, "Price" and "ShelveLoc" are the
two most important variables.
library (MASS)
library (randomForest)
set.seed (100)
train = sample (1: nrow(Boston), nrow(Boston)/2)
x_train = Boston[train, -14]
x_test = Boston[-train, -14]
y train = Boston[train, 14]
y test = Boston[-train, 14]
test_error1 = rep(0,13)
for (i in 1:13){
bag.boston = randomForest(x_train, y_train, mtry= i, ntree =100, importance
yhat.bag = predict(bag.boston, newdata = Boston[-train,])
test_error1[i] = mean(( yhat.bag - y_test)^2)
test error1
## [1] 18.611813 10.282254 9.624311 8.896569 8.990730 9.052735
                                                                    9.084105
## [8] 9.429814 10.228730 9.661823 9.908464 10.251536 9.673689
mtry = 1:13
plot(mtry, test_error1, xlab =" mtry ", ylab=" error rate",type="l")
```



```
test_error2 = rep(0,196)
for (i in 5:200){
bag.boston = randomForest(medv~., data=Boston[train,] , mtry= 6, ntree = i ,
importance =TRUE)
yhat.bag = predict (bag.boston, newdata = Boston[-train,])
test_error2[i-4] = mean(( yhat.bag - y_test)^2)
}
ntree = 5:200
plot(ntree, test_error2, xlab = " ntree ", ylab=" error rate",type="l")
```

