

2. a.  $S \rightarrow aSa$   $S \rightarrow 0S0$  ~~For  $010010$ :~~  
 ~~$S \rightarrow 0Sa$~~   $S \rightarrow 1S1$   ~~$S \rightarrow \epsilon$~~   
 ~~$S \rightarrow \epsilon$~~   $S \rightarrow \epsilon$

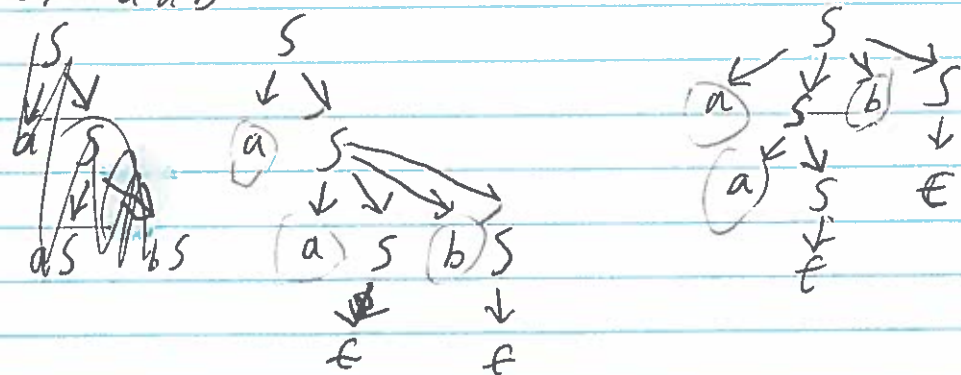
For  $010010$ :  
 $S \rightarrow 0S0 \rightarrow 0(1S1)0 \rightarrow 01(0S0)10 \rightarrow 010010$

b.  $S \rightarrow TY$   
 $T \rightarrow aTb$   
 $Y \rightarrow cY$   
 $S \rightarrow \epsilon$   
 $T \rightarrow \epsilon$   
 $Y \rightarrow \epsilon$

c.  $S \rightarrow TY$   
 $T \rightarrow aT$   
 $Y \rightarrow bYc$   
 $S \rightarrow \epsilon$   
 $T \rightarrow \epsilon$   
 $Y \rightarrow \epsilon$

d.  $S \rightarrow abS$   $S \rightarrow Sab$   
 $S \rightarrow \epsilon$   $S \rightarrow \epsilon$

4. a.  $aab$



b.  $S \rightarrow aS \rightarrow aaSbS \rightarrow aabS \rightarrow aab$   
 $S \rightarrow aSbS \rightarrow aaSbS \rightarrow aabS \rightarrow aab$

c.  $S \rightarrow aS \rightarrow aaSbS \rightarrow aaSb \rightarrow aab$   
 $S \rightarrow aSbS \rightarrow aSb \rightarrow aaSb \rightarrow aab$

EC. For the grammar  $S \rightarrow aS | aSbS | \epsilon$ , there are three results for each transition in the rule. Two of those,  $aSbS$  and  $\epsilon$ , have the same number of a's and b's, while the remaining result,  $aS$ , has more a's than b's. With these three results for the grammar  $S \rightarrow aS | aSbS | \epsilon$ , there ~~will~~ will always be at least as many a's as b's, because there is no result to the rule that can cause there to be more b's than a's.