

Probability Practice Assignment

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R Probability Practice

Part A.

1. Define the probabilities and given data:

- $P(RC) = 0.3$ #Random Clickers
- $P(TC) = 1 - P(RC) = 0.7$ #Truthful Clickers
- $P(Yes|RC) = 0.5$
- $P(Yes) = 0.65$

2. Rule of total probability (What fraction of people who are truthful clickers answered yes)

$$P(A) = \sum_{i=1}^n P(A|B_i)P(B_i)$$

$$P(Yes) = P(Yes|RC)P(RC) + P(Yes|TC)P(TC)$$

- $0.65 = (0.5 * 0.3) + P(Yes|TC) * 0.7$
- $0.65 = 0.15 + P(Yes|TC) * 0.7$
- $0.50 = P(Yes|TC) * 0.7$
- $P(Yes|TC) = 0.7143$

Fraction of people who are truthful clickers that answered yes is 71.43%

Part B.

1. Define the probabilities and given data:

- $P(\text{Positive Test}|\text{Has Disease}) = 0.993$
- $P(\text{Negative Test}|\text{Doesn't Have Disease}) = 0.9999$
- $P(\text{Has Disease}) = 0.000025$
- $P(\text{Doesn't Have Disease}) = 1 - P(\text{Has Disease}) = 0.999975$

2. What is the probability that they have the disease if the person tests positive?

$$P(\text{Has Disease}|\text{Positive Test})$$

$$P(\text{Has Disease}|\text{Positive Test}) = \frac{P(\text{Positive Test}|\text{Has Disease}) \cdot P(\text{Has Disease})}{P(\text{Positive Test})}$$

- First find $P(\text{Positive Test})$ using rule of total probabilities

$$P(\text{Positive Test}) = P(\text{Positive Test}|\text{Has Disease}) \cdot P(\text{Has Disease}) + P(\text{Positive Test}|\text{Doesn't Have Disease}) \cdot P(\text{Doesn't Have Disease})$$

- $P(\text{Positive Test}) = 0.0001248$
- Use Bayes Theorem
- $P(\text{Has Disease}|\text{Positive Test}) = 0.1988$

The probability that a person who tested positive actually has the disease is around 19.88%