

## Aryan Patel ABI Project

```
In [235... import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
import sklearn.preprocessing
import sklearn.pipeline
```

## Reading in the data

```
In [236... training_data = pd.read_csv('/Users/aryanpatel/abiprojecttrain.csv')

test_data = pd.read_csv('/Users/aryanpatel/abiprojecttest.csv')

training_data.head()
```

```
Out[236]:
```

	SalePrice	LotFrontage	LotArea	Street	LotShape	YearBuilt	BsmtUnfSF	TotalBsmtSF
0	163990	65	8461	Pave	Reg	2005	728	728
1	412500	110	13688	Pave	IR1	2003	556	1572
2	126000	60	8160	Pave	Reg	1940	444	756
3	280000	109	14154	Pave	Reg	2006	1063	1063
4	105000	51	6120	Pave	Reg	1931	506	715

5 rows × 24 columns

```
In [237... trainview = training_data.shape
testview = test_data.shape

print(trainview,testview)

(901, 24) (226, 24)
```

```
In [238... #checking if null values
nvalues = training_data.isna().sum()
print(nvalues)
```

```

SalePrice      0
LotFrontage    0
LotArea        0
Street         0
LotShape       0
YearBuilt      0
BsmtUnfSF      0
TotalBsmtSF    0
CentralAir     0
X1stFlrSF      0
X2ndFlrSF      0
GrLivArea      0
BsmtFullBath   0
BsmtHalfBath   0
FullBath       0
HalfBath       0
BedroomAbvGr   0
KitchenAbvGr   0
TotRmsAbvGrd   0
Fireplaces     0
GarageYrBlt    0
GarageCars     0
GarageArea     0
WoodDeckSF     0
dtype: int64

```

```

In [239... for i, (col_name, dtype) in enumerate(training_data.dtypes.items()):
           print(f"Column {i}: {col_name} - {dtype}")

```

```

Column 0: SalePrice - int64
Column 1: LotFrontage - int64
Column 2: LotArea - int64
Column 3: Street - object
Column 4: LotShape - object
Column 5: YearBuilt - int64
Column 6: BsmtUnfSF - int64
Column 7: TotalBsmtSF - int64
Column 8: CentralAir - object
Column 9: X1stFlrSF - int64
Column 10: X2ndFlrSF - int64
Column 11: GrLivArea - int64
Column 12: BsmtFullBath - int64
Column 13: BsmtHalfBath - int64
Column 14: FullBath - int64
Column 15: HalfBath - int64
Column 16: BedroomAbvGr - int64
Column 17: KitchenAbvGr - int64
Column 18: TotRmsAbvGrd - int64
Column 19: Fireplaces - int64
Column 20: GarageYrBlt - int64
Column 21: GarageCars - int64
Column 22: GarageArea - int64
Column 23: WoodDeckSF - int64

```

```
In [240... #sklearn preprocessing on training data
from sklearn.compose import ColumnTransformer
from sklearn.pipeline import Pipeline
from sklearn.preprocessing import StandardScaler, OneHotEncoder, FunctionTransformer
from sklearn.compose import make_column_selector as selector

X_train = training_data.drop(columns=['SalePrice'])
y_train = training_data['SalePrice']

X_test = test_data.drop(columns=['SalePrice'])
y_test = test_data['SalePrice']

numerical_features = selector(dtype_include=np.int64)
categorical_features = selector(dtype_include=object)

numerical_transformer = Pipeline(steps=[
    ('scaler', StandardScaler())
])

categorical_transformer = Pipeline(steps=[
    ('onehot', OneHotEncoder())
])

preprocessor = ColumnTransformer(
    transformers=[
        ('num', numerical_transformer, numerical_features),
        ('cat', categorical_transformer, categorical_features)
    ])

pipeline = Pipeline(steps=[
    ('preprocessor', preprocessor)
])

X_train_processed = pipeline.fit_transform(X_train)

X_test_processed = pipeline.transform(X_test)

y_train_processed = np.log1p(y_train)
y_test_processed = np.log1p(y_test)
```

```
In [241... X_train_processed
```

```
Out[241]: array([[ -0.23492683, -0.18862751,  1.04590173, ...,  1.          ,
                0.          ,  1.          ],
                [ 1.66023998,  0.41400605,  0.98098096, ...,  0.          ,
                0.          ,  1.          ],
                [-0.44550092, -0.22333053, -1.06402334, ...,  1.          ,
                1.          ,  0.          ],
                ...,
                [ 0.18622135, -0.12648489,  1.07836211, ...,  1.          ,
                0.          ,  1.          ],
                [-0.8666491 ,  0.54901349,  1.07836211, ...,  0.          ,
                0.          ,  1.          ],
                [-0.31915647, -0.18413111,  1.01344134, ...,  1.          ,
                0.          ,  1.          ]])
```

## 1st Model Simple multiple linear regression.

```
In [242... from sklearn.linear_model import LinearRegression
from sklearn.metrics import mean_squared_error

linear_regression = LinearRegression()

linear_regression.fit(X_train_processed, y_train_processed)

y_train_pred = linear_regression.predict(X_train_processed)
y_test_pred = linear_regression.predict(X_test_processed)

train_mse = mean_squared_error(y_train_processed, y_train_pred)
test_mse = mean_squared_error(y_test_processed, y_test_pred)

print("Training MSE (Regular Regression) is :", train_mse)
print("Test MSE (Regular Regression) is :", test_mse)

residual_model0_test = y_test_processed - y_test_pred

Training MSE (Regular Regression) is : 0.02462790457299441
Test MSE (Regular Regression) is : 0.06428908586018621
```

2nd model elastic net regression

```
In [243... from sklearn.linear_model import ElasticNet
from sklearn.model_selection import GridSearchCV
from sklearn.metrics import mean_squared_error

#tried many values for all params but this resulted in best from my testing
param_grid = {
    'alpha': [ 0.1, 0.5, 1.0, 10, 100],
    'l1_ratio': [ 0.1, 0.5, 0.9, 0.99]
}

elastic_net = ElasticNet(max_iter=10000)

grid_search = GridSearchCV(elastic_net, param_grid, cv=10, scoring='neg_mean_
grid_search.fit(X_train_processed, y_train_processed)

best_elastic_net = grid_search.best_estimator_

print("Best Hyperparameters are :")
print(grid_search.best_params_)

best_elastic_net.fit(X_train_processed, y_train_processed)

y_train_pred = best_elastic_net.predict(X_train_processed)
y_test_pred = best_elastic_net.predict(X_test_processed)

train_mse_elastic = mean_squared_error(y_train_processed, y_train_pred)
test_mse_elastic = mean_squared_error(y_test_processed, y_test_pred)

print("Training MSE (Elastic Net) is :", train_mse_elastic)
print("Test MSE (Elastic Net) is :", test_mse_elastic)

residual_model1_test = y_test_processed - y_test_pred

Best Hyperparameters are :
{'alpha': 0.1, 'l1_ratio': 0.1}
Training MSE (Elastic Net) is : 0.027969114268482042
Test MSE (Elastic Net) is : 0.05836975904396832
```

```
In [244... #checking coef of the elastic net model
print("Coefficients:")
for i, coef in enumerate(best_elastic_net.coef_):
    print(f"Feature {i}: {coef}")
```

## Coefficients:

Feature 0: 0.012009936379842032  
Feature 1: 0.00915587177911959  
Feature 2: 0.06871359699411492  
Feature 3: -0.0  
Feature 4: 0.07209034881414104  
Feature 5: 0.027057832403221745  
Feature 6: 0.01473509275927689  
Feature 7: 0.09133413203771718  
Feature 8: 0.023115725619931318  
Feature 9: 0.0  
Feature 10: 0.03089444644838244  
Feature 11: 0.016131089285058575  
Feature 12: -0.005068347350476139  
Feature 13: -0.04120539122186395  
Feature 14: 0.024635013991695466  
Feature 15: 0.04700034380389149  
Feature 16: 0.028394537079765143  
Feature 17: 0.029396977086362894  
Feature 18: 0.026853033978358063  
Feature 19: 0.008634288309406574  
Feature 20: -0.0  
Feature 21: 0.0  
Feature 22: 0.0  
Feature 23: 0.0  
Feature 24: -0.0  
Feature 25: -0.0  
Feature 26: -0.0  
Feature 27: 0.0

Third model SVM (poly)

```
In [245... from sklearn.svm import SVR
from sklearn.model_selection import GridSearchCV
from sklearn.metrics import mean_squared_error

#tried large range of param but these resulted in best mse from what I have
param_grid = {
    'C': [0.01,0.1, 1, 10],
    'epsilon': [0.01,0.1, 0.5, 1.0]
}

svm_model = SVR(kernel='poly',degree=3)

grid_search = GridSearchCV(svm_model, param_grid, cv=5, scoring='neg_mean_sq
grid_search.fit(X_train_processed, y_train_processed)

best_svm_model = grid_search.best_estimator_

best_svm_model.fit(X_train_processed, y_train_processed)

y_train_pred_svm = best_svm_model.predict(X_train_processed)
y_test_pred_svm = best_svm_model.predict(X_test_processed)

train_mse_svm = mean_squared_error(y_train_processed, y_train_pred_svm)
test_mse_svm = mean_squared_error(y_test_processed, y_test_pred_svm)

print("Training MSE (SVM):", train_mse_svm)
print("Test MSE (SVM):", test_mse_svm)
print("Best hyperparameters:", grid_search.best_params_)

residual_model2_test = y_test_processed - y_test_pred_svm

Training MSE (SVM): 0.009404704464279212
Test MSE (SVM): 0.02839727450036488
Best hyperparameters: {'C': 1, 'epsilon': 0.1}
```

Model 4 # neural network

```
In [246... from sklearn.model_selection import train_test_split

# Creating validation data for neural network from full training data
X_train_nn, X_valid_nn, y_train_nn, y_valid_nn = train_test_split(X_train_pr
```

```
In [247... x_train_processed_view = X_train_processed.shape

print(x_train_processed_view)
```

(901, 28)

In [248...

```
import tensorflow as tf

tf.keras.backend.clear_session()
tf.random.set_seed(42)

ann_model = tf.keras.Sequential([
    tf.keras.layers.Dense(70, activation="relu", input_shape=(28,)),
    tf.keras.layers.Dense(35, activation="relu", kernel_initializer="he_norm",
    tf.keras.layers.Dropout(0.001),
    tf.keras.layers.Dense(20, activation="relu", kernel_initializer="he_norm",
    tf.keras.layers.Dense(1)
])

ann_model.summary()
```

/Users/aryanpatel/anaconda3/lib/python3.11/site-packages/keras/src/layers/core/dense.py:88: UserWarning: Do not pass an `input\_shape`/`input\_dim` argument to a layer. When using Sequential models, prefer using an `Input(shape)` object as the first layer in the model instead.

```
super().__init__(activity_regularizer=activity_regularizer, **kwargs)
```

**Model: "sequential"**

Layer (type)	Output Shape	Para
dense (Dense)	(None, 70)	2,
dense_1 (Dense)	(None, 35)	2,
dropout (Dropout)	(None, 35)	
dense_2 (Dense)	(None, 20)	
dense_3 (Dense)	(None, 1)	

**Total params: 5,256 (20.53 KB)****Trainable params: 5,256 (20.53 KB)****Non-trainable params: 0 (0.00 B)**

In [249...



























```
tf.random.set_seed(42)
optimizer = tf.keras.optimizers.Adam(learning_rate=0.001)
ann_model.compile(loss='mean_squared_error', optimizer=optimizer)

tensorboard_callback = tf.keras.callbacks.TensorBoard(log_dir="logs")
```






























```
In [250... tf.random.set_seed(42)
history = ann_model.fit(X_train_nn, y_train_nn, epochs=500,
                        validation_data=(X_valid_nn, y_valid_nn),
                        callbacks=[tensorboard_callback])
```



























```
Epoch 1/500
22/22 ————— 1s 9ms/step - loss: 135.8865 - val_loss: 94.4918
Epoch 2/500
22/22 ————— 0s 3ms/step - loss: 75.0217 - val_loss: 19.7875
Epoch 3/500
22/22 ————— 0s 3ms/step - loss: 15.0995 - val_loss: 8.4906
Epoch 4/500
22/22 ————— 0s 3ms/step - loss: 9.0276 - val_loss: 7.3393
Epoch 5/500
22/22 ————— 0s 3ms/step - loss: 7.1921 - val_loss: 6.1159
Epoch 6/500
22/22 ————— 0s 3ms/step - loss: 6.0626 - val_loss: 5.5420
Epoch 7/500
22/22 ————— 0s 3ms/step - loss: 5.3429 - val_loss: 5.0790
Epoch 8/500
22/22 ————— 0s 3ms/step - loss: 4.8309 - val_loss: 4.7204
Epoch 9/500
22/22 ————— 0s 3ms/step - loss: 4.4587 - val_loss: 4.4249
Epoch 10/500
22/22 ————— 0s 3ms/step - loss: 4.1340 - val_loss: 4.1709
Epoch 11/500
22/22 ————— 0s 3ms/step - loss: 3.8795 - val_loss: 3.9637
Epoch 12/500
22/22 ————— 0s 3ms/step - loss: 3.6638 - val_loss: 3.7702
Epoch 13/500
22/22 ————— 0s 3ms/step - loss: 3.4717 - val_loss: 3.6229
Epoch 14/500
22/22 ————— 0s 5ms/step - loss: 3.3473 - val_loss: 3.4721
Epoch 15/500
22/22 ————— 0s 4ms/step - loss: 3.1963 - val_loss: 3.3444
Epoch 16/500
22/22 ————— 0s 3ms/step - loss: 3.0701 - val_loss: 3.2171
Epoch 17/500
22/22 ————— 0s 4ms/step - loss: 2.9589 - val_loss: 3.1103
Epoch 18/500
22/22 ————— 0s 4ms/step - loss: 2.8393 - val_loss: 3.0081
Epoch 19/500
22/22 ————— 0s 4ms/step - loss: 2.7480 - val_loss: 2.9278
Epoch 20/500
22/22 ————— 0s 3ms/step - loss: 2.6516 - val_loss: 2.8357
Epoch 21/500
22/22 ————— 0s 3ms/step - loss: 2.5595 - val_loss: 2.7551
Epoch 22/500
22/22 ————— 0s 3ms/step - loss: 2.4777 - val_loss: 2.6795
Epoch 23/500
22/22 ————— 0s 3ms/step - loss: 2.4193 - val_loss: 2.6035
Epoch 24/500
22/22 ————— 0s 3ms/step - loss: 2.3299 - val_loss: 2.5249
```

```
Epoch 25/500
22/22  0s 3ms/step - loss: 2.2429 - val_loss: 2.4531
Epoch 26/500
22/22  0s 5ms/step - loss: 2.1851 - val_loss: 2.3768
Epoch 27/500
22/22  0s 4ms/step - loss: 2.1146 - val_loss: 2.3139
Epoch 28/500
22/22  0s 3ms/step - loss: 2.0527 - val_loss: 2.2424
Epoch 29/500
22/22  0s 3ms/step - loss: 1.9853 - val_loss: 2.1848
Epoch 30/500
22/22  0s 3ms/step - loss: 1.9334 - val_loss: 2.1290
Epoch 31/500
22/22  0s 4ms/step - loss: 1.8908 - val_loss: 2.0790
Epoch 32/500
22/22  0s 4ms/step - loss: 1.8400 - val_loss: 2.0123
Epoch 33/500
22/22  0s 4ms/step - loss: 1.7687 - val_loss: 1.9529
Epoch 34/500
22/22  0s 4ms/step - loss: 1.7256 - val_loss: 1.8996
Epoch 35/500
22/22  0s 4ms/step - loss: 1.6939 - val_loss: 1.8462
Epoch 36/500
22/22  0s 9ms/step - loss: 1.6221 - val_loss: 1.7897
Epoch 37/500
22/22  0s 3ms/step - loss: 1.5770 - val_loss: 1.7452
Epoch 38/500
22/22  0s 3ms/step - loss: 1.5315 - val_loss: 1.7066
Epoch 39/500
22/22  0s 3ms/step - loss: 1.4883 - val_loss: 1.6506
Epoch 40/500
22/22  0s 3ms/step - loss: 1.4479 - val_loss: 1.6058
Epoch 41/500
22/22  0s 3ms/step - loss: 1.4058 - val_loss: 1.5621
Epoch 42/500
22/22  0s 3ms/step - loss: 1.3715 - val_loss: 1.5159
Epoch 43/500
22/22  0s 3ms/step - loss: 1.3272 - val_loss: 1.4765
Epoch 44/500
22/22  0s 3ms/step - loss: 1.3072 - val_loss: 1.4415
Epoch 45/500
22/22  0s 3ms/step - loss: 1.2597 - val_loss: 1.4014
Epoch 46/500
22/22  0s 3ms/step - loss: 1.2213 - val_loss: 1.3656
Epoch 47/500
22/22  0s 3ms/step - loss: 1.2040 - val_loss: 1.3295
Epoch 48/500
22/22  0s 3ms/step - loss: 1.1715 - val_loss: 1.2948
Epoch 49/500
22/22  0s 3ms/step - loss: 1.1440 - val_loss: 1.2578
Epoch 50/500
22/22  0s 3ms/step - loss: 1.1129 - val_loss: 1.2264
Epoch 51/500
```




























```

22/22  0s 4ms/step - loss: 1.0735 - val_loss: 1.1939
Epoch 52/500
22/22  0s 3ms/step - loss: 1.0362 - val_loss: 1.1638
Epoch 53/500
22/22  0s 3ms/step - loss: 1.0239 - val_loss: 1.1290
Epoch 54/500
22/22  0s 4ms/step - loss: 0.9928 - val_loss: 1.1025
Epoch 55/500
22/22  0s 4ms/step - loss: 0.9637 - val_loss: 1.0724
Epoch 56/500
22/22  0s 4ms/step - loss: 0.9288 - val_loss: 1.0448
Epoch 57/500
22/22  0s 9ms/step - loss: 0.9086 - val_loss: 1.0189
Epoch 58/500
22/22  0s 3ms/step - loss: 0.8814 - val_loss: 0.9954
Epoch 59/500
22/22  0s 3ms/step - loss: 0.8589 - val_loss: 0.9700
Epoch 60/500
22/22  0s 4ms/step - loss: 0.8414 - val_loss: 0.9455
Epoch 61/500
22/22  0s 4ms/step - loss: 0.8254 - val_loss: 0.9168
Epoch 62/500
22/22  0s 4ms/step - loss: 0.8045 - val_loss: 0.8924
Epoch 63/500
22/22  0s 4ms/step - loss: 0.7751 - val_loss: 0.8740
Epoch 64/500
22/22  0s 4ms/step - loss: 0.7546 - val_loss: 0.8544
Epoch 65/500
22/22  0s 3ms/step - loss: 0.7459 - val_loss: 0.8273
Epoch 66/500
22/22  0s 3ms/step - loss: 0.7154 - val_loss: 0.8118
Epoch 67/500
22/22  0s 3ms/step - loss: 0.6965 - val_loss: 0.7833
Epoch 68/500
22/22  0s 3ms/step - loss: 0.6785 - val_loss: 0.7717
Epoch 69/500
22/22  0s 3ms/step - loss: 0.6617 - val_loss: 0.7458
Epoch 70/500
22/22  0s 3ms/step - loss: 0.6736 - val_loss: 0.7284
Epoch 71/500
22/22  0s 3ms/step - loss: 0.6288 - val_loss: 0.7084
Epoch 72/500
22/22  0s 3ms/step - loss: 0.6184 - val_loss: 0.6981
Epoch 73/500
22/22  0s 3ms/step - loss: 0.6107 - val_loss: 0.6910
Epoch 74/500
22/22  0s 3ms/step - loss: 0.5800 - val_loss: 0.6605
Epoch 75/500
22/22  0s 3ms/step - loss: 0.5688 - val_loss: 0.6402
Epoch 76/500
22/22  0s 3ms/step - loss: 0.5456 - val_loss: 0.6244
Epoch 77/500
22/22  0s 3ms/step - loss: 0.5484 - val_loss: 0.6103

```



























```
Epoch 78/500
22/22  0s 7ms/step - loss: 0.5243 - val_loss: 0.5933
Epoch 79/500
22/22  0s 4ms/step - loss: 0.5083 - val_loss: 0.5766
Epoch 80/500
22/22  0s 3ms/step - loss: 0.4935 - val_loss: 0.5661
Epoch 81/500
22/22  0s 3ms/step - loss: 0.4879 - val_loss: 0.5517
Epoch 82/500
22/22  0s 3ms/step - loss: 0.4655 - val_loss: 0.5380
Epoch 83/500
22/22  0s 3ms/step - loss: 0.4666 - val_loss: 0.5235
Epoch 84/500
22/22  0s 3ms/step - loss: 0.4433 - val_loss: 0.5144
Epoch 85/500
22/22  0s 3ms/step - loss: 0.4384 - val_loss: 0.5008
Epoch 86/500
22/22  0s 3ms/step - loss: 0.4405 - val_loss: 0.4959
Epoch 87/500
22/22  0s 3ms/step - loss: 0.4344 - val_loss: 0.4800
Epoch 88/500
22/22  0s 3ms/step - loss: 0.4182 - val_loss: 0.4741
Epoch 89/500
22/22  0s 3ms/step - loss: 0.4169 - val_loss: 0.4514
Epoch 90/500
22/22  0s 3ms/step - loss: 0.4150 - val_loss: 0.4573
Epoch 91/500
22/22  0s 3ms/step - loss: 0.4088 - val_loss: 0.4332
Epoch 92/500
22/22  0s 3ms/step - loss: 0.3817 - val_loss: 0.4365
Epoch 93/500
22/22  0s 4ms/step - loss: 0.3800 - val_loss: 0.4125
Epoch 94/500
22/22  0s 3ms/step - loss: 0.3573 - val_loss: 0.4049
Epoch 95/500
22/22  0s 3ms/step - loss: 0.3486 - val_loss: 0.3951
Epoch 96/500
22/22  0s 3ms/step - loss: 0.3320 - val_loss: 0.4026
Epoch 97/500
22/22  0s 3ms/step - loss: 0.3374 - val_loss: 0.3841
Epoch 98/500
22/22  0s 4ms/step - loss: 0.3263 - val_loss: 0.3711
Epoch 99/500
22/22  0s 3ms/step - loss: 0.3086 - val_loss: 0.3722
Epoch 100/500
22/22  0s 3ms/step - loss: 0.3150 - val_loss: 0.3500
Epoch 101/500
22/22  0s 3ms/step - loss: 0.3006 - val_loss: 0.3571
Epoch 102/500
22/22  0s 3ms/step - loss: 0.3330 - val_loss: 0.3414
Epoch 103/500
22/22  0s 4ms/step - loss: 0.3121 - val_loss: 0.3460
Epoch 104/500
```

```


22/22  0s 3ms/step - loss: 0.3210 - val_loss: 0.3289
Epoch 105/500
22/22  0s 3ms/step - loss: 0.3142 - val_loss: 0.3445
Epoch 106/500
22/22  0s 3ms/step - loss: 0.2899 - val_loss: 0.3094
Epoch 107/500
22/22  0s 3ms/step - loss: 0.2671 - val_loss: 0.3127
Epoch 108/500
22/22  0s 3ms/step - loss: 0.2613 - val_loss: 0.2974
Epoch 109/500
22/22  0s 3ms/step - loss: 0.2469 - val_loss: 0.2971
Epoch 110/500
22/22  0s 5ms/step - loss: 0.2521 - val_loss: 0.2882
Epoch 111/500
22/22  0s 3ms/step - loss: 0.2432 - val_loss: 0.2959
Epoch 112/500
22/22  0s 6ms/step - loss: 0.2309 - val_loss: 0.2756
Epoch 113/500
22/22  0s 3ms/step - loss: 0.2204 - val_loss: 0.2715
Epoch 114/500
22/22  0s 3ms/step - loss: 0.2196 - val_loss: 0.2650
Epoch 115/500
22/22  0s 3ms/step - loss: 0.2130 - val_loss: 0.2583
Epoch 116/500
22/22  0s 3ms/step - loss: 0.2170 - val_loss: 0.2620
Epoch 117/500
22/22  0s 3ms/step - loss: 0.2145 - val_loss: 0.2504
Epoch 118/500
22/22  0s 3ms/step - loss: 0.1996 - val_loss: 0.2475
Epoch 119/500
22/22  0s 3ms/step - loss: 0.1981 - val_loss: 0.2715
Epoch 120/500
22/22  0s 3ms/step - loss: 0.2082 - val_loss: 0.2384
Epoch 121/500
22/22  0s 3ms/step - loss: 0.1941 - val_loss: 0.2335
Epoch 122/500
22/22  0s 3ms/step - loss: 0.1974 - val_loss: 0.2484
Epoch 123/500
22/22  0s 3ms/step - loss: 0.2039 - val_loss: 0.2265
Epoch 124/500
22/22  0s 3ms/step - loss: 0.1930 - val_loss: 0.2299
Epoch 125/500
22/22  0s 3ms/step - loss: 0.1983 - val_loss: 0.2334
Epoch 126/500
22/22  0s 3ms/step - loss: 0.1835 - val_loss: 0.2160
Epoch 127/500
22/22  0s 3ms/step - loss: 0.1748 - val_loss: 0.2107
Epoch 128/500
22/22  0s 3ms/step - loss: 0.1753 - val_loss: 0.2084
Epoch 129/500
22/22  0s 3ms/step - loss: 0.1719 - val_loss: 0.2155
Epoch 130/500
22/22  0s 4ms/step - loss: 0.1761 - val_loss: 0.2040


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Epoch 131/500
22/22  0s 3ms/step - loss: 0.1591 - val_loss: 0.2021
Epoch 132/500
22/22  0s 8ms/step - loss: 0.1611 - val_loss: 0.1978
Epoch 133/500
22/22  0s 4ms/step - loss: 0.1578 - val_loss: 0.1923
Epoch 134/500
22/22  0s 3ms/step - loss: 0.1507 - val_loss: 0.1890
Epoch 135/500
22/22  0s 3ms/step - loss: 0.1598 - val_loss: 0.1846
Epoch 136/500
22/22  0s 3ms/step - loss: 0.1566 - val_loss: 0.1875
Epoch 137/500
22/22  0s 3ms/step - loss: 0.1874 - val_loss: 0.1923
Epoch 138/500
22/22  0s 3ms/step - loss: 0.1709 - val_loss: 0.1841
Epoch 139/500
22/22  0s 3ms/step - loss: 0.1610 - val_loss: 0.1907
Epoch 140/500
22/22  0s 4ms/step - loss: 0.1671 - val_loss: 0.2076
Epoch 141/500
22/22  0s 3ms/step - loss: 0.2089 - val_loss: 0.1946
Epoch 142/500
22/22  0s 3ms/step - loss: 0.1782 - val_loss: 0.2015
Epoch 143/500
22/22  0s 3ms/step - loss: 0.2193 - val_loss: 0.2368
Epoch 144/500
22/22  0s 3ms/step - loss: 0.1932 - val_loss: 0.1688
Epoch 145/500
22/22  0s 3ms/step - loss: 0.1565 - val_loss: 0.1671
Epoch 146/500
22/22  0s 3ms/step - loss: 0.1263 - val_loss: 0.1648
Epoch 147/500
22/22  0s 3ms/step - loss: 0.1241 - val_loss: 0.1587
Epoch 148/500
22/22  0s 3ms/step - loss: 0.1221 - val_loss: 0.1637
Epoch 149/500
22/22  0s 8ms/step - loss: 0.1295 - val_loss: 0.1590
Epoch 150/500
22/22  0s 3ms/step - loss: 0.1188 - val_loss: 0.1562
Epoch 151/500
22/22  0s 3ms/step - loss: 0.1190 - val_loss: 0.1608
Epoch 152/500
22/22  0s 3ms/step - loss: 0.1150 - val_loss: 0.1784
Epoch 153/500
22/22  0s 3ms/step - loss: 0.1278 - val_loss: 0.1411
Epoch 154/500
22/22  0s 3ms/step - loss: 0.1370 - val_loss: 0.1459
Epoch 155/500
22/22  0s 3ms/step - loss: 0.1182 - val_loss: 0.1615
Epoch 156/500
22/22  0s 3ms/step - loss: 0.1197 - val_loss: 0.1503
Epoch 157/500


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22/22  0s 3ms/step - loss: 0.1053 - val\_loss: 0.1550  
Epoch 158/500


22/22  0s 3ms/step - loss: 0.1185 - val\_loss: 0.1369  
Epoch 159/500


22/22  0s 3ms/step - loss: 0.1126 - val\_loss: 0.1458  
Epoch 160/500


22/22  0s 3ms/step - loss: 0.1082 - val\_loss: 0.1489  
Epoch 161/500


22/22  0s 3ms/step - loss: 0.1068 - val\_loss: 0.1972  
Epoch 162/500


22/22  0s 3ms/step - loss: 0.1531 - val\_loss: 0.1404  
Epoch 163/500


22/22  0s 3ms/step - loss: 0.1150 - val\_loss: 0.1443  
Epoch 164/500


22/22  0s 3ms/step - loss: 0.1167 - val\_loss: 0.2093  
Epoch 165/500


22/22  0s 6ms/step - loss: 0.1534 - val\_loss: 0.1384  
Epoch 166/500


22/22  0s 5ms/step - loss: 0.1149 - val\_loss: 0.1406  
Epoch 167/500


22/22  0s 4ms/step - loss: 0.1156 - val\_loss: 0.1390  
Epoch 168/500


22/22  0s 3ms/step - loss: 0.1030 - val\_loss: 0.1347  
Epoch 169/500


22/22  0s 3ms/step - loss: 0.0929 - val\_loss: 0.1340  
Epoch 170/500


22/22  0s 4ms/step - loss: 0.0965 - val\_loss: 0.1322  
Epoch 171/500


22/22  0s 4ms/step - loss: 0.0983 - val\_loss: 0.1292  
Epoch 172/500


22/22  0s 4ms/step - loss: 0.0921 - val\_loss: 0.1241  
Epoch 173/500


22/22  0s 3ms/step - loss: 0.0902 - val\_loss: 0.1241  
Epoch 174/500


22/22  0s 3ms/step - loss: 0.1062 - val\_loss: 0.1281  
Epoch 175/500


22/22  0s 3ms/step - loss: 0.1106 - val\_loss: 0.1311  
Epoch 176/500


22/22  0s 3ms/step - loss: 0.0977 - val\_loss: 0.1260  
Epoch 177/500


22/22  0s 4ms/step - loss: 0.1023 - val\_loss: 0.1275  
Epoch 178/500


22/22  0s 3ms/step - loss: 0.1080 - val\_loss: 0.1284  
Epoch 179/500

22/22  0s 3ms/step - loss: 0.1071 - val\_loss: 0.1195  
Epoch 180/500



























22/22  0s 3ms/step - loss: 0.1199 - val\_loss: 0.1203  
Epoch 181/500

22/22  0s 3ms/step - loss: 0.1115 - val\_loss: 0.1309  
Epoch 182/500

22/22  0s 4ms/step - loss: 0.1157 - val\_loss: 0.1313  
Epoch 183/500




























22/22  0s 8ms/step - loss: 0.1138 - val\_loss: 0.1240



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Epoch 184/500
22/22  0s 3ms/step - loss: 0.0929 - val_loss: 0.1242
Epoch 185/500
22/22  0s 3ms/step - loss: 0.0902 - val_loss: 0.1300
Epoch 186/500
22/22  0s 3ms/step - loss: 0.0893 - val_loss: 0.1289
Epoch 187/500
22/22  0s 3ms/step - loss: 0.0823 - val_loss: 0.1187
Epoch 188/500
22/22  0s 3ms/step - loss: 0.0871 - val_loss: 0.1284
Epoch 189/500
22/22  0s 3ms/step - loss: 0.0905 - val_loss: 0.1085
Epoch 190/500
22/22  0s 5ms/step - loss: 0.0881 - val_loss: 0.1154
Epoch 191/500
22/22  0s 3ms/step - loss: 0.0905 - val_loss: 0.1232
Epoch 192/500
22/22  0s 3ms/step - loss: 0.0899 - val_loss: 0.1326
Epoch 193/500
22/22  0s 3ms/step - loss: 0.0944 - val_loss: 0.1366
Epoch 194/500
22/22  0s 3ms/step - loss: 0.1081 - val_loss: 0.1163
Epoch 195/500
22/22  0s 4ms/step - loss: 0.0942 - val_loss: 0.1136
Epoch 196/500
22/22  0s 4ms/step - loss: 0.0764 - val_loss: 0.1073
Epoch 197/500
22/22  0s 3ms/step - loss: 0.0763 - val_loss: 0.1129
Epoch 198/500
22/22  0s 3ms/step - loss: 0.0725 - val_loss: 0.1127
Epoch 199/500
22/22  0s 9ms/step - loss: 0.0740 - val_loss: 0.1127
Epoch 200/500
22/22  0s 3ms/step - loss: 0.0686 - val_loss: 0.1163
Epoch 201/500
22/22  0s 3ms/step - loss: 0.0748 - val_loss: 0.1160
Epoch 202/500
22/22  0s 3ms/step - loss: 0.0747 - val_loss: 0.1112
Epoch 203/500
22/22  0s 3ms/step - loss: 0.0736 - val_loss: 0.1043
Epoch 204/500
22/22  0s 3ms/step - loss: 0.0708 - val_loss: 0.1050
Epoch 205/500
22/22  0s 3ms/step - loss: 0.0782 - val_loss: 0.1066
Epoch 206/500
22/22  0s 3ms/step - loss: 0.0800 - val_loss: 0.1021
Epoch 207/500
22/22  0s 3ms/step - loss: 0.0707 - val_loss: 0.1050
Epoch 208/500
22/22  0s 3ms/step - loss: 0.0648 - val_loss: 0.1084
Epoch 209/500
22/22  0s 3ms/step - loss: 0.0693 - val_loss: 0.1050
Epoch 210/500
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22/22  0s 3ms/step - loss: 0.0698 - val_loss: 0.1167
Epoch 211/500
22/22  0s 4ms/step - loss: 0.0850 - val_loss: 0.1142
Epoch 212/500
22/22  0s 3ms/step - loss: 0.0723 - val_loss: 0.1008
Epoch 213/500
22/22  0s 3ms/step - loss: 0.0695 - val_loss: 0.1043
Epoch 214/500
22/22  0s 3ms/step - loss: 0.0790 - val_loss: 0.1019
Epoch 215/500
22/22  0s 8ms/step - loss: 0.0760 - val_loss: 0.1136
Epoch 216/500
22/22  0s 3ms/step - loss: 0.0723 - val_loss: 0.1010
Epoch 217/500
22/22  0s 3ms/step - loss: 0.0743 - val_loss: 0.1141
Epoch 218/500
22/22  0s 4ms/step - loss: 0.0977 - val_loss: 0.1206
Epoch 219/500
22/22  0s 3ms/step - loss: 0.0856 - val_loss: 0.1258
Epoch 220/500
22/22  0s 3ms/step - loss: 0.0917 - val_loss: 0.1116
Epoch 221/500
22/22  0s 3ms/step - loss: 0.0716 - val_loss: 0.1046
Epoch 222/500
22/22  0s 3ms/step - loss: 0.0842 - val_loss: 0.1057
Epoch 223/500
22/22  0s 3ms/step - loss: 0.0748 - val_loss: 0.0969
Epoch 224/500
22/22  0s 3ms/step - loss: 0.0859 - val_loss: 0.1011
Epoch 225/500
22/22  0s 4ms/step - loss: 0.0733 - val_loss: 0.0949
Epoch 226/500
22/22  0s 3ms/step - loss: 0.0687 - val_loss: 0.0963
Epoch 227/500
22/22  0s 3ms/step - loss: 0.0715 - val_loss: 0.0984
Epoch 228/500
22/22  0s 3ms/step - loss: 0.0709 - val_loss: 0.0930
Epoch 229/500
22/22  0s 3ms/step - loss: 0.0728 - val_loss: 0.0996
Epoch 230/500
22/22  0s 10ms/step - loss: 0.0656 - val_loss: 0.0986
Epoch 231/500
22/22  0s 3ms/step - loss: 0.0835 - val_loss: 0.1009
Epoch 232/500
22/22  0s 3ms/step - loss: 0.0729 - val_loss: 0.1240
Epoch 233/500
22/22  0s 3ms/step - loss: 0.0722 - val_loss: 0.1207
Epoch 234/500
22/22  0s 3ms/step - loss: 0.0717 - val_loss: 0.1381
Epoch 235/500
22/22  0s 3ms/step - loss: 0.0892 - val_loss: 0.1468
Epoch 236/500
22/22  0s 3ms/step - loss: 0.0803 - val_loss: 0.1351



























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Epoch 237/500
22/22  0s 3ms/step - loss: 0.0860 - val_loss: 0.1250
Epoch 238/500
22/22  0s 3ms/step - loss: 0.0791 - val_loss: 0.1014
Epoch 239/500
22/22  0s 3ms/step - loss: 0.0872 - val_loss: 0.1089
Epoch 240/500
22/22  0s 3ms/step - loss: 0.0742 - val_loss: 0.1596
Epoch 241/500
22/22  0s 3ms/step - loss: 0.0926 - val_loss: 0.1696
Epoch 242/500
22/22  0s 3ms/step - loss: 0.1002 - val_loss: 0.1091
Epoch 243/500
22/22  0s 3ms/step - loss: 0.0860 - val_loss: 0.0929
Epoch 244/500
22/22  0s 3ms/step - loss: 0.0736 - val_loss: 0.1016
Epoch 245/500
22/22  0s 3ms/step - loss: 0.0706 - val_loss: 0.0964
Epoch 246/500
22/22  0s 6ms/step - loss: 0.0709 - val_loss: 0.1338
Epoch 247/500
22/22  0s 3ms/step - loss: 0.0715 - val_loss: 0.1179
Epoch 248/500
22/22  0s 4ms/step - loss: 0.0841 - val_loss: 0.0849
Epoch 249/500
22/22  0s 3ms/step - loss: 0.0752 - val_loss: 0.1002
Epoch 250/500
22/22  0s 3ms/step - loss: 0.0718 - val_loss: 0.0987
Epoch 251/500
22/22  0s 3ms/step - loss: 0.0806 - val_loss: 0.1275
Epoch 252/500
22/22  0s 3ms/step - loss: 0.0715 - val_loss: 0.1024
Epoch 253/500
22/22  0s 3ms/step - loss: 0.0856 - val_loss: 0.0891
Epoch 254/500
22/22  0s 4ms/step - loss: 0.0695 - val_loss: 0.1137
Epoch 255/500
22/22  0s 4ms/step - loss: 0.0847 - val_loss: 0.0984
Epoch 256/500
22/22  0s 4ms/step - loss: 0.0743 - val_loss: 0.1175
Epoch 257/500
22/22  0s 3ms/step - loss: 0.0659 - val_loss: 0.0905
Epoch 258/500
22/22  0s 3ms/step - loss: 0.0743 - val_loss: 0.0844
Epoch 259/500
22/22  0s 3ms/step - loss: 0.0631 - val_loss: 0.0866
Epoch 260/500
22/22  0s 12ms/step - loss: 0.0574 - val_loss: 0.0896
Epoch 261/500
22/22  0s 4ms/step - loss: 0.0555 - val_loss: 0.1030
Epoch 262/500
22/22  0s 4ms/step - loss: 0.0591 - val_loss: 0.0924
Epoch 263/500

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22/22  0s 3ms/step - loss: 0.0562 - val_loss: 0.0850
Epoch 264/500
22/22  0s 5ms/step - loss: 0.0563 - val_loss: 0.0856
Epoch 265/500
22/22  0s 4ms/step - loss: 0.0548 - val_loss: 0.0849
Epoch 266/500
22/22  0s 4ms/step - loss: 0.0569 - val_loss: 0.0893
Epoch 267/500
22/22  0s 4ms/step - loss: 0.0572 - val_loss: 0.0880
Epoch 268/500
22/22  0s 4ms/step - loss: 0.0750 - val_loss: 0.0991
Epoch 269/500
22/22  0s 4ms/step - loss: 0.0592 - val_loss: 0.0956
Epoch 270/500
22/22  0s 4ms/step - loss: 0.0577 - val_loss: 0.0839
Epoch 271/500
22/22  0s 3ms/step - loss: 0.0519 - val_loss: 0.0848
Epoch 272/500
22/22  0s 4ms/step - loss: 0.0497 - val_loss: 0.0848
Epoch 273/500
22/22  0s 4ms/step - loss: 0.0546 - val_loss: 0.0884
Epoch 274/500
22/22  0s 4ms/step - loss: 0.0564 - val_loss: 0.0875
Epoch 275/500
22/22  0s 4ms/step - loss: 0.0504 - val_loss: 0.0867
Epoch 276/500
22/22  0s 3ms/step - loss: 0.0508 - val_loss: 0.1479
Epoch 277/500
22/22  0s 3ms/step - loss: 0.0816 - val_loss: 0.0886
Epoch 278/500
22/22  0s 7ms/step - loss: 0.0668 - val_loss: 0.0838
Epoch 279/500
22/22  0s 3ms/step - loss: 0.0722 - val_loss: 0.0908
Epoch 280/500
22/22  0s 3ms/step - loss: 0.0611 - val_loss: 0.1087
Epoch 281/500
22/22  0s 5ms/step - loss: 0.0790 - val_loss: 0.0911
Epoch 282/500
22/22  0s 4ms/step - loss: 0.0678 - val_loss: 0.1236
Epoch 283/500
22/22  0s 4ms/step - loss: 0.0726 - val_loss: 0.1323
Epoch 284/500
22/22  0s 4ms/step - loss: 0.0720 - val_loss: 0.1257
Epoch 285/500
22/22  0s 4ms/step - loss: 0.0772 - val_loss: 0.0782
Epoch 286/500
22/22  0s 4ms/step - loss: 0.0669 - val_loss: 0.1052
Epoch 287/500
22/22  0s 4ms/step - loss: 0.0789 - val_loss: 0.0948
Epoch 288/500
22/22  0s 4ms/step - loss: 0.0691 - val_loss: 0.0844
Epoch 289/500
22/22  0s 4ms/step - loss: 0.0567 - val_loss: 0.1192
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Epoch 290/500
22/22  0s 4ms/step - loss: 0.0617 - val_loss: 0.0951
Epoch 291/500
22/22  0s 6ms/step - loss: 0.0665 - val_loss: 0.0725
Epoch 292/500
22/22  0s 3ms/step - loss: 0.0520 - val_loss: 0.0904
Epoch 293/500
22/22  0s 4ms/step - loss: 0.0536 - val_loss: 0.0829
Epoch 294/500
22/22  0s 3ms/step - loss: 0.0490 - val_loss: 0.0827
Epoch 295/500
22/22  0s 4ms/step - loss: 0.0472 - val_loss: 0.0902
Epoch 296/500
22/22  0s 4ms/step - loss: 0.0511 - val_loss: 0.0872
Epoch 297/500
22/22  0s 4ms/step - loss: 0.0479 - val_loss: 0.0753
Epoch 298/500
22/22  0s 4ms/step - loss: 0.0471 - val_loss: 0.0755
Epoch 299/500
22/22  0s 4ms/step - loss: 0.0442 - val_loss: 0.0777
Epoch 300/500
22/22  0s 5ms/step - loss: 0.0613 - val_loss: 0.0824
Epoch 301/500
22/22  0s 4ms/step - loss: 0.0626 - val_loss: 0.0791
Epoch 302/500
22/22  0s 4ms/step - loss: 0.0554 - val_loss: 0.0810
Epoch 303/500
22/22  0s 4ms/step - loss: 0.0649 - val_loss: 0.0812
Epoch 304/500
22/22  0s 8ms/step - loss: 0.0557 - val_loss: 0.0821
Epoch 305/500
22/22  0s 4ms/step - loss: 0.0486 - val_loss: 0.0912
Epoch 306/500
22/22  0s 4ms/step - loss: 0.0543 - val_loss: 0.0806
Epoch 307/500
22/22  0s 3ms/step - loss: 0.0543 - val_loss: 0.0791
Epoch 308/500
22/22  0s 3ms/step - loss: 0.0571 - val_loss: 0.0856
Epoch 309/500
22/22  0s 4ms/step - loss: 0.0480 - val_loss: 0.0843
Epoch 310/500
22/22  0s 3ms/step - loss: 0.0612 - val_loss: 0.1209
Epoch 311/500
22/22  0s 5ms/step - loss: 0.0607 - val_loss: 0.1151
Epoch 312/500
22/22  0s 3ms/step - loss: 0.0641 - val_loss: 0.0843
Epoch 313/500
22/22  0s 3ms/step - loss: 0.0567 - val_loss: 0.0988
Epoch 314/500
22/22  0s 3ms/step - loss: 0.0666 - val_loss: 0.0801
Epoch 315/500
22/22  0s 3ms/step - loss: 0.0724 - val_loss: 0.0896
Epoch 316/500
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22/22  0s 3ms/step - loss: 0.0617 - val_loss: 0.1338
Epoch 317/500
22/22  0s 6ms/step - loss: 0.0783 - val_loss: 0.1361
Epoch 318/500
22/22  0s 3ms/step - loss: 0.0853 - val_loss: 0.1020
Epoch 319/500
22/22  0s 3ms/step - loss: 0.0833 - val_loss: 0.1216
Epoch 320/500
22/22  0s 3ms/step - loss: 0.0856 - val_loss: 0.2157
Epoch 321/500
22/22  0s 3ms/step - loss: 0.1153 - val_loss: 0.0735
Epoch 322/500
22/22  0s 3ms/step - loss: 0.0875 - val_loss: 0.0943
Epoch 323/500
22/22  0s 4ms/step - loss: 0.0676 - val_loss: 0.0906
Epoch 324/500
22/22  0s 3ms/step - loss: 0.0589 - val_loss: 0.0986
Epoch 325/500
22/22  0s 3ms/step - loss: 0.0578 - val_loss: 0.0773
Epoch 326/500
22/22  0s 3ms/step - loss: 0.0476 - val_loss: 0.0751
Epoch 327/500
22/22  0s 3ms/step - loss: 0.0478 - val_loss: 0.1060
Epoch 328/500
22/22  0s 3ms/step - loss: 0.0514 - val_loss: 0.0872
Epoch 329/500
22/22  0s 3ms/step - loss: 0.0455 - val_loss: 0.0734
Epoch 330/500
22/22  0s 3ms/step - loss: 0.0528 - val_loss: 0.0789
Epoch 331/500
22/22  0s 7ms/step - loss: 0.0456 - val_loss: 0.0835
Epoch 332/500
22/22  0s 3ms/step - loss: 0.0403 - val_loss: 0.0784
Epoch 333/500
22/22  0s 3ms/step - loss: 0.0394 - val_loss: 0.0838
Epoch 334/500
22/22  0s 3ms/step - loss: 0.0476 - val_loss: 0.0818
Epoch 335/500
22/22  0s 4ms/step - loss: 0.0440 - val_loss: 0.0743
Epoch 336/500
22/22  0s 3ms/step - loss: 0.0443 - val_loss: 0.0767
Epoch 337/500
22/22  0s 5ms/step - loss: 0.0420 - val_loss: 0.0832
Epoch 338/500
22/22  0s 3ms/step - loss: 0.0479 - val_loss: 0.0770
Epoch 339/500
22/22  0s 4ms/step - loss: 0.0493 - val_loss: 0.0780
Epoch 340/500
22/22  0s 3ms/step - loss: 0.0501 - val_loss: 0.0775
Epoch 341/500
22/22  0s 3ms/step - loss: 0.0534 - val_loss: 0.0796
Epoch 342/500
22/22  0s 3ms/step - loss: 0.0523 - val_loss: 0.0828


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Epoch 343/500
22/22  0s 5ms/step - loss: 0.0573 - val_loss: 0.0851
Epoch 344/500
22/22  0s 4ms/step - loss: 0.0504 - val_loss: 0.0975
Epoch 345/500
22/22  0s 3ms/step - loss: 0.0530 - val_loss: 0.1334
Epoch 346/500
22/22  0s 3ms/step - loss: 0.0664 - val_loss: 0.0943
Epoch 347/500
22/22  0s 3ms/step - loss: 0.0626 - val_loss: 0.0797
Epoch 348/500
22/22  0s 3ms/step - loss: 0.0590 - val_loss: 0.0810
Epoch 349/500
22/22  0s 4ms/step - loss: 0.0553 - val_loss: 0.0968
Epoch 350/500
22/22  0s 3ms/step - loss: 0.0680 - val_loss: 0.0793
Epoch 351/500
22/22  0s 3ms/step - loss: 0.0574 - val_loss: 0.1175
Epoch 352/500
22/22  0s 3ms/step - loss: 0.0699 - val_loss: 0.1002
Epoch 353/500
22/22  0s 3ms/step - loss: 0.0631 - val_loss: 0.0691
Epoch 354/500
22/22  0s 3ms/step - loss: 0.0455 - val_loss: 0.0798
Epoch 355/500
22/22  0s 8ms/step - loss: 0.0568 - val_loss: 0.0791
Epoch 356/500
22/22  0s 3ms/step - loss: 0.0467 - val_loss: 0.0822
Epoch 357/500
22/22  0s 3ms/step - loss: 0.0478 - val_loss: 0.0852
Epoch 358/500
22/22  0s 3ms/step - loss: 0.0558 - val_loss: 0.2329
Epoch 359/500
22/22  0s 3ms/step - loss: 0.1643 - val_loss: 0.1272
Epoch 360/500
22/22  0s 4ms/step - loss: 0.1095 - val_loss: 0.0966
Epoch 361/500
22/22  0s 3ms/step - loss: 0.0887 - val_loss: 0.1265
Epoch 362/500
22/22  0s 3ms/step - loss: 0.0878 - val_loss: 0.0767
Epoch 363/500
22/22  0s 3ms/step - loss: 0.0514 - val_loss: 0.0809
Epoch 364/500
22/22  0s 3ms/step - loss: 0.0426 - val_loss: 0.0851
Epoch 365/500
22/22  0s 3ms/step - loss: 0.0420 - val_loss: 0.1046
Epoch 366/500
22/22  0s 3ms/step - loss: 0.0543 - val_loss: 0.0752
Epoch 367/500
22/22  0s 4ms/step - loss: 0.0409 - val_loss: 0.0846
Epoch 368/500
22/22  0s 6ms/step - loss: 0.0400 - val_loss: 0.0854
Epoch 369/500


```


22/22  0s 4ms/step - loss: 0.0465 - val\_loss: 0.0792  
Epoch 370/500


22/22  0s 4ms/step - loss: 0.0380 - val\_loss: 0.0739  
Epoch 371/500


22/22  0s 3ms/step - loss: 0.0406 - val\_loss: 0.1145  
Epoch 372/500


22/22  0s 3ms/step - loss: 0.0685 - val\_loss: 0.0687  
Epoch 373/500


22/22  0s 5ms/step - loss: 0.0487 - val\_loss: 0.0793  
Epoch 374/500


22/22  0s 3ms/step - loss: 0.0410 - val\_loss: 0.0886  
Epoch 375/500


22/22  0s 3ms/step - loss: 0.0425 - val\_loss: 0.0875  
Epoch 376/500


22/22  0s 3ms/step - loss: 0.0496 - val\_loss: 0.0670  
Epoch 377/500


22/22  0s 3ms/step - loss: 0.0407 - val\_loss: 0.0844  
Epoch 378/500


22/22  0s 4ms/step - loss: 0.0462 - val\_loss: 0.0966  
Epoch 379/500


22/22  0s 4ms/step - loss: 0.0441 - val\_loss: 0.0776  
Epoch 380/500


22/22  0s 10ms/step - loss: 0.0442 - val\_loss: 0.0698  
Epoch 381/500


22/22  0s 4ms/step - loss: 0.0376 - val\_loss: 0.0806  
Epoch 382/500


22/22  0s 3ms/step - loss: 0.0432 - val\_loss: 0.0718  
Epoch 383/500


22/22  0s 4ms/step - loss: 0.0423 - val\_loss: 0.0870  
Epoch 384/500


22/22  0s 4ms/step - loss: 0.0443 - val\_loss: 0.0828  
Epoch 385/500


22/22  0s 4ms/step - loss: 0.0622 - val\_loss: 0.0756  
Epoch 386/500


22/22  0s 3ms/step - loss: 0.0403 - val\_loss: 0.0877  
Epoch 387/500


22/22  0s 4ms/step - loss: 0.0425 - val\_loss: 0.0874  
Epoch 388/500


22/22  0s 4ms/step - loss: 0.0534 - val\_loss: 0.0783  
Epoch 389/500


22/22  0s 3ms/step - loss: 0.0469 - val\_loss: 0.0784  
Epoch 390/500


22/22  0s 3ms/step - loss: 0.0528 - val\_loss: 0.0847  
Epoch 391/500

22/22  0s 3ms/step - loss: 0.0527 - val\_loss: 0.1048  
Epoch 392/500



























22/22  0s 3ms/step - loss: 0.0532 - val\_loss: 0.1728  
Epoch 393/500

22/22  0s 3ms/step - loss: 0.0935 - val\_loss: 0.0804  
Epoch 394/500

22/22  0s 9ms/step - loss: 0.0813 - val\_loss: 0.0824  
Epoch 395/500




























22/22  0s 3ms/step - loss: 0.0569 - val\_loss: 0.0753



Epoch 396/500  
22/22  0s 3ms/step - loss: 0.0739 - val\_loss: 0.1312  
Epoch 397/500  
22/22  0s 4ms/step - loss: 0.0626 - val\_loss: 0.0888  
Epoch 398/500  
22/22  0s 3ms/step - loss: 0.0628 - val\_loss: 0.0716  
Epoch 399/500  
22/22  0s 3ms/step - loss: 0.0385 - val\_loss: 0.0694  
Epoch 400/500  
22/22  0s 3ms/step - loss: 0.0475 - val\_loss: 0.0823  
Epoch 401/500  
22/22  0s 3ms/step - loss: 0.0426 - val\_loss: 0.1081  
Epoch 402/500  
22/22  0s 3ms/step - loss: 0.0579 - val\_loss: 0.0663  
Epoch 403/500  
22/22  0s 3ms/step - loss: 0.0423 - val\_loss: 0.0790  
Epoch 404/500  
22/22  0s 8ms/step - loss: 0.0367 - val\_loss: 0.1120  
Epoch 405/500  
22/22  0s 4ms/step - loss: 0.0623 - val\_loss: 0.0860  
Epoch 406/500  
22/22  0s 3ms/step - loss: 0.0457 - val\_loss: 0.0673  
Epoch 407/500  
22/22  0s 5ms/step - loss: 0.0539 - val\_loss: 0.1150  
Epoch 408/500  
22/22  0s 4ms/step - loss: 0.0546 - val\_loss: 0.0796  
Epoch 409/500  
22/22  0s 3ms/step - loss: 0.0422 - val\_loss: 0.0822  
Epoch 410/500  
22/22  0s 4ms/step - loss: 0.0493 - val\_loss: 0.0725  
Epoch 411/500  
22/22  0s 3ms/step - loss: 0.0375 - val\_loss: 0.0905  
Epoch 412/500  
22/22  0s 3ms/step - loss: 0.0450 - val\_loss: 0.0761  
Epoch 413/500  
22/22  0s 3ms/step - loss: 0.0403 - val\_loss: 0.0808  
Epoch 414/500  
22/22  0s 3ms/step - loss: 0.0384 - val\_loss: 0.0729  
Epoch 415/500  
22/22  0s 3ms/step - loss: 0.0369 - val\_loss: 0.0712  
Epoch 416/500  
22/22  0s 6ms/step - loss: 0.0397 - val\_loss: 0.0816  
Epoch 417/500  
22/22  0s 4ms/step - loss: 0.0369 - val\_loss: 0.0775  
Epoch 418/500  
22/22  0s 3ms/step - loss: 0.0363 - val\_loss: 0.0780  
Epoch 419/500  
22/22  0s 3ms/step - loss: 0.0514 - val\_loss: 0.0705  
Epoch 420/500  
22/22  0s 4ms/step - loss: 0.0488 - val\_loss: 0.0720  
Epoch 421/500  
22/22  0s 3ms/step - loss: 0.0404 - val\_loss: 0.0735  
Epoch 422/500





























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22/22  0s 4ms/step - loss: 0.0416 - val_loss: 0.0872
Epoch 423/500
22/22  0s 3ms/step - loss: 0.0578 - val_loss: 0.0822
Epoch 424/500
22/22  0s 3ms/step - loss: 0.0389 - val_loss: 0.0836
Epoch 425/500
22/22  0s 3ms/step - loss: 0.0431 - val_loss: 0.0732
Epoch 426/500
22/22  0s 3ms/step - loss: 0.0377 - val_loss: 0.0753
Epoch 427/500
22/22  0s 7ms/step - loss: 0.0367 - val_loss: 0.0693
Epoch 428/500
22/22  0s 3ms/step - loss: 0.0358 - val_loss: 0.0684
Epoch 429/500
22/22  0s 4ms/step - loss: 0.0362 - val_loss: 0.0695
Epoch 430/500
22/22  0s 3ms/step - loss: 0.0367 - val_loss: 0.0746
Epoch 431/500
22/22  0s 3ms/step - loss: 0.0418 - val_loss: 0.0837
Epoch 432/500
22/22  0s 3ms/step - loss: 0.0475 - val_loss: 0.0718
Epoch 433/500
22/22  0s 3ms/step - loss: 0.0339 - val_loss: 0.0740
Epoch 434/500
22/22  0s 3ms/step - loss: 0.0427 - val_loss: 0.0652
Epoch 435/500
22/22  0s 3ms/step - loss: 0.0416 - val_loss: 0.0621
Epoch 436/500
22/22  0s 3ms/step - loss: 0.0323 - val_loss: 0.0697
Epoch 437/500
22/22  0s 4ms/step - loss: 0.0354 - val_loss: 0.0694
Epoch 438/500
22/22  0s 3ms/step - loss: 0.0385 - val_loss: 0.0668
Epoch 439/500
22/22  0s 5ms/step - loss: 0.0391 - val_loss: 0.0719
Epoch 440/500
22/22  0s 3ms/step - loss: 0.0384 - val_loss: 0.0686
Epoch 441/500
22/22  0s 3ms/step - loss: 0.0359 - val_loss: 0.0699
Epoch 442/500
22/22  0s 3ms/step - loss: 0.0420 - val_loss: 0.0770
Epoch 443/500
22/22  0s 3ms/step - loss: 0.0377 - val_loss: 0.1001
Epoch 444/500
22/22  0s 4ms/step - loss: 0.0531 - val_loss: 0.1103
Epoch 445/500
22/22  0s 3ms/step - loss: 0.0547 - val_loss: 0.1378
Epoch 446/500
22/22  0s 3ms/step - loss: 0.0620 - val_loss: 0.1884
Epoch 447/500
22/22  0s 3ms/step - loss: 0.0792 - val_loss: 0.1174
Epoch 448/500
22/22  0s 5ms/step - loss: 0.0643 - val_loss: 0.0915



























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Epoch 449/500
22/22  0s 4ms/step - loss: 0.0530 - val_loss: 0.0679
Epoch 450/500
22/22  0s 3ms/step - loss: 0.0438 - val_loss: 0.0756
Epoch 451/500
22/22  0s 3ms/step - loss: 0.0398 - val_loss: 0.0797
Epoch 452/500
22/22  0s 4ms/step - loss: 0.0512 - val_loss: 0.0745
Epoch 453/500
22/22  0s 4ms/step - loss: 0.0410 - val_loss: 0.0697
Epoch 454/500
22/22  0s 3ms/step - loss: 0.0385 - val_loss: 0.0883
Epoch 455/500
22/22  0s 3ms/step - loss: 0.0438 - val_loss: 0.1095
Epoch 456/500
22/22  0s 3ms/step - loss: 0.0504 - val_loss: 0.1006
Epoch 457/500
22/22  0s 5ms/step - loss: 0.0525 - val_loss: 0.0661
Epoch 458/500
22/22  0s 3ms/step - loss: 0.0375 - val_loss: 0.0658
Epoch 459/500
22/22  0s 10ms/step - loss: 0.0405 - val_loss: 0.0734
Epoch 460/500
22/22  0s 3ms/step - loss: 0.0464 - val_loss: 0.0778
Epoch 461/500
22/22  0s 4ms/step - loss: 0.0431 - val_loss: 0.1107
Epoch 462/500
22/22  0s 4ms/step - loss: 0.0475 - val_loss: 0.1175
Epoch 463/500
22/22  0s 3ms/step - loss: 0.0544 - val_loss: 0.1012
Epoch 464/500
22/22  0s 4ms/step - loss: 0.0554 - val_loss: 0.0760
Epoch 465/500
22/22  0s 4ms/step - loss: 0.0568 - val_loss: 0.0689
Epoch 466/500
22/22  0s 4ms/step - loss: 0.0443 - val_loss: 0.0742
Epoch 467/500
22/22  0s 3ms/step - loss: 0.0443 - val_loss: 0.0727
Epoch 468/500
22/22  0s 3ms/step - loss: 0.0447 - val_loss: 0.1047
Epoch 469/500
22/22  0s 3ms/step - loss: 0.0405 - val_loss: 0.1012
Epoch 470/500
22/22  0s 6ms/step - loss: 0.0484 - val_loss: 0.0748
Epoch 471/500
22/22  0s 3ms/step - loss: 0.0456 - val_loss: 0.0916
Epoch 472/500
22/22  0s 4ms/step - loss: 0.0549 - val_loss: 0.0778
Epoch 473/500
22/22  0s 3ms/step - loss: 0.0395 - val_loss: 0.0675
Epoch 474/500
22/22  0s 4ms/step - loss: 0.0425 - val_loss: 0.0854
Epoch 475/500

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```

22/22  0s 3ms/step - loss: 0.0391 - val_loss: 0.1319
Epoch 476/500
22/22  0s 4ms/step - loss: 0.0628 - val_loss: 0.0674
Epoch 477/500
22/22  0s 4ms/step - loss: 0.0388 - val_loss: 0.0710
Epoch 478/500
22/22  0s 4ms/step - loss: 0.0378 - val_loss: 0.0663
Epoch 479/500
22/22  0s 4ms/step - loss: 0.0489 - val_loss: 0.0953
Epoch 480/500
22/22  0s 4ms/step - loss: 0.0477 - val_loss: 0.0846
Epoch 481/500
22/22  0s 11ms/step - loss: 0.0406 - val_loss: 0.0901
Epoch 482/500
22/22  0s 4ms/step - loss: 0.0433 - val_loss: 0.0735
Epoch 483/500
22/22  0s 3ms/step - loss: 0.0347 - val_loss: 0.0716
Epoch 484/500
22/22  0s 4ms/step - loss: 0.0318 - val_loss: 0.0820
Epoch 485/500
22/22  0s 4ms/step - loss: 0.0342 - val_loss: 0.0741
Epoch 486/500
22/22  0s 4ms/step - loss: 0.0373 - val_loss: 0.0718
Epoch 487/500
22/22  0s 4ms/step - loss: 0.0399 - val_loss: 0.0740
Epoch 488/500
22/22  0s 3ms/step - loss: 0.0354 - val_loss: 0.0813
Epoch 489/500
22/22  0s 3ms/step - loss: 0.0306 - val_loss: 0.0924
Epoch 490/500
22/22  0s 3ms/step - loss: 0.0360 - val_loss: 0.0839
Epoch 491/500
22/22  0s 8ms/step - loss: 0.0481 - val_loss: 0.0688
Epoch 492/500
22/22  0s 4ms/step - loss: 0.0352 - val_loss: 0.0690
Epoch 493/500
22/22  0s 4ms/step - loss: 0.0392 - val_loss: 0.0826
Epoch 494/500
22/22  0s 4ms/step - loss: 0.0417 - val_loss: 0.0684
Epoch 495/500
22/22  0s 4ms/step - loss: 0.0375 - val_loss: 0.0786
Epoch 496/500
22/22  0s 3ms/step - loss: 0.0462 - val_loss: 0.0732
Epoch 497/500
22/22  0s 4ms/step - loss: 0.0419 - val_loss: 0.0861
Epoch 498/500
22/22  0s 4ms/step - loss: 0.0397 - val_loss: 0.0771
Epoch 499/500
22/22  0s 9ms/step - loss: 0.0418 - val_loss: 0.0802
Epoch 500/500
22/22  0s 4ms/step - loss: 0.0390 - val_loss: 0.0664

```

```
In [251... tf.random.set_seed(42)
y_test_pred = ann_model.predict(X_test_processed)
nnmse = mean_squared_error(y_test_processed, y_test_pred, squared=True)

y_test_pred1 = ann_model.predict(X_test_processed).ravel()

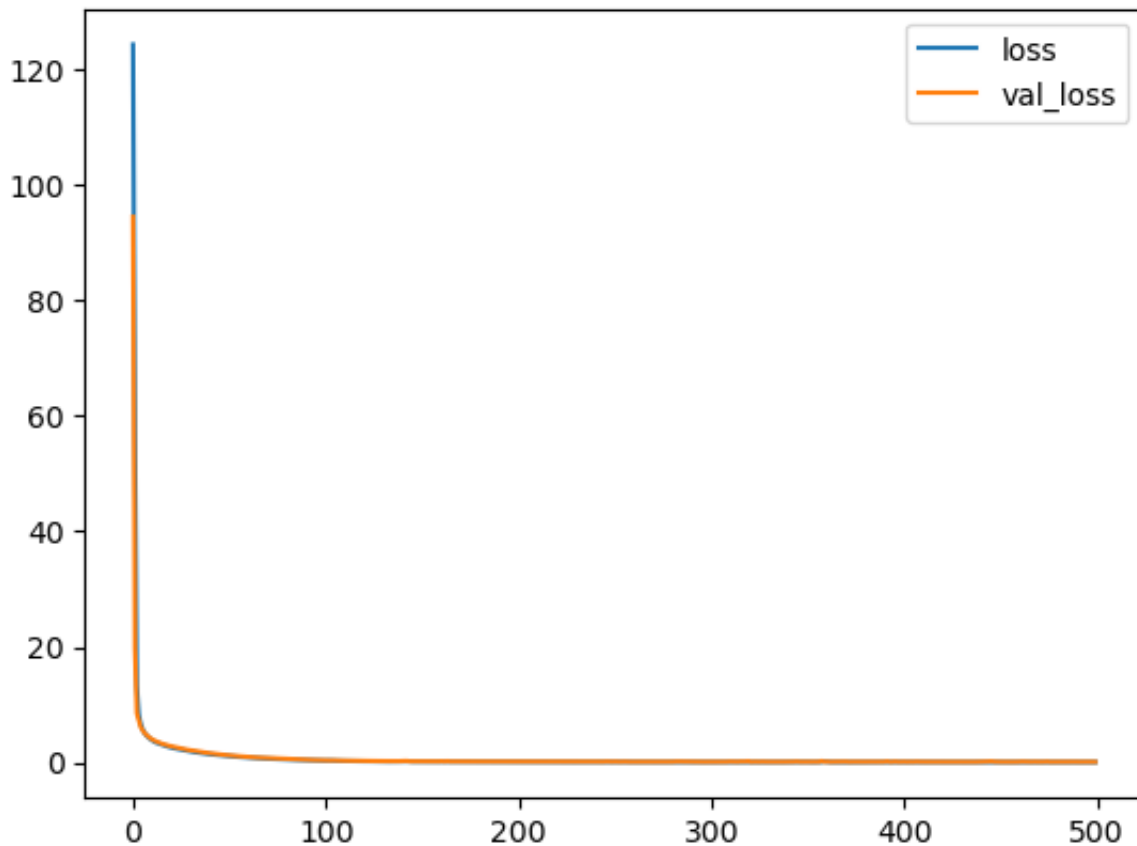
y_test_processed1 = y_test_processed.ravel()

residual_nn_test = y_test_processed1 - y_test_pred1
print("Test MSE (NN):", nnmse)
```

8/8 ————— 0s 8ms/step  
8/8 ————— 0s 1ms/step  
Test MSE (NN): 0.06664396783777125

```
In [252... pd.DataFrame(history.history).plot()
```

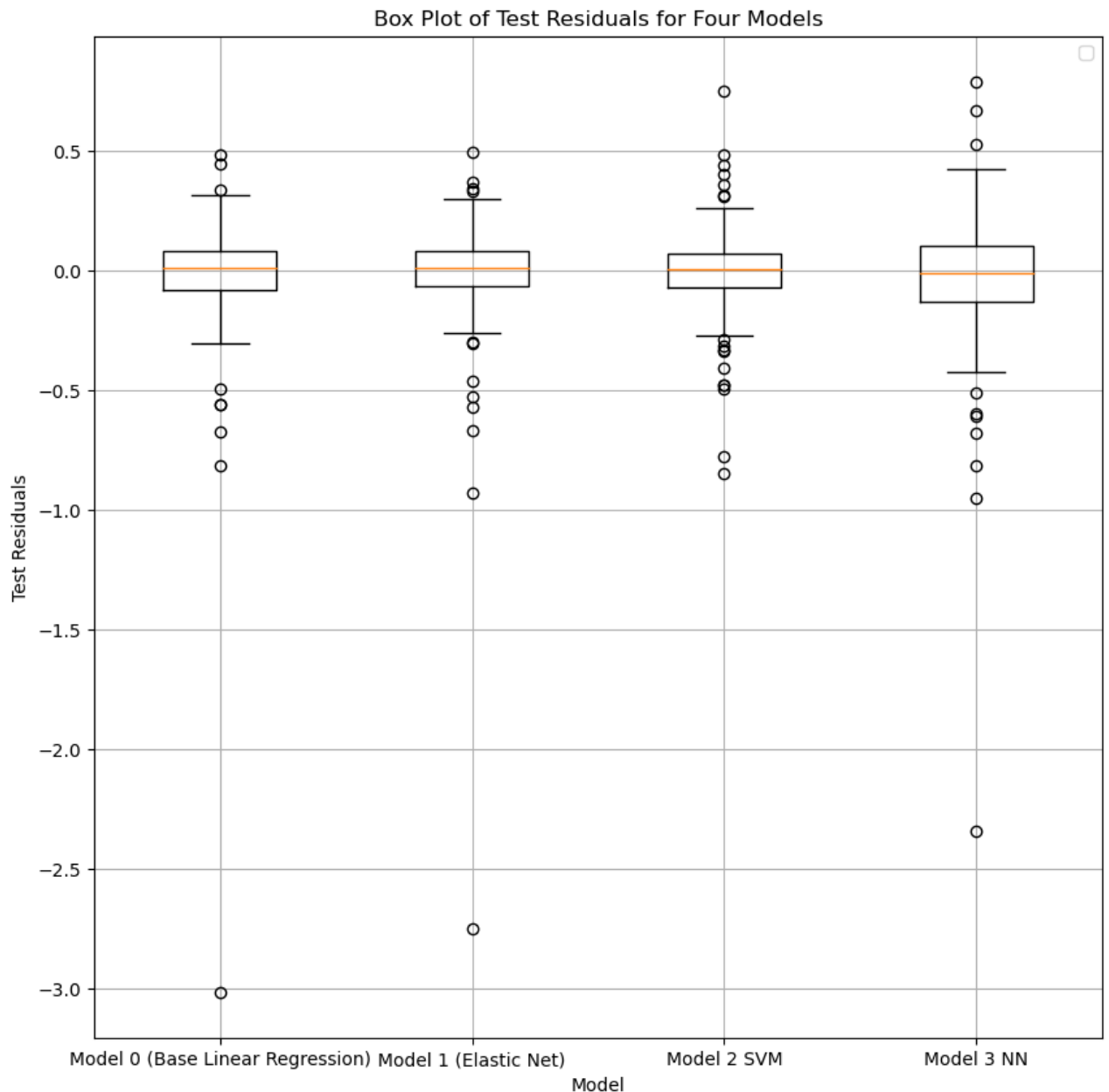
Out[252]: <Axes: >



```
In [253... residuals_data = [residual_model0_test, residual_model1_test, residual_model

plt.figure(figsize=(10, 10))
plt.boxplot(residuals_data, labels=['Model 0 (Base Linear Regression)', 'Mod
plt.xlabel('Model')
plt.ylabel('Test Residuals')
plt.title('Box Plot of Test Residuals for Four Models')
plt.grid(True)
plt.legend()
plt.show()
```

No artists with labels found to put in legend. Note that artists whose label start with an underscore are ignored when legend() is called with no argument.



Order of best models in prediction accuracy based on residuals and test mse

1. SVM
2. Elastic Net / NN tied (as sometimes NN can have different accuracy each time trained sometimes it is below the test mse of Elastic net but does take around 1 min to compile so Elastic Net is the better option)
3. Base Regression.