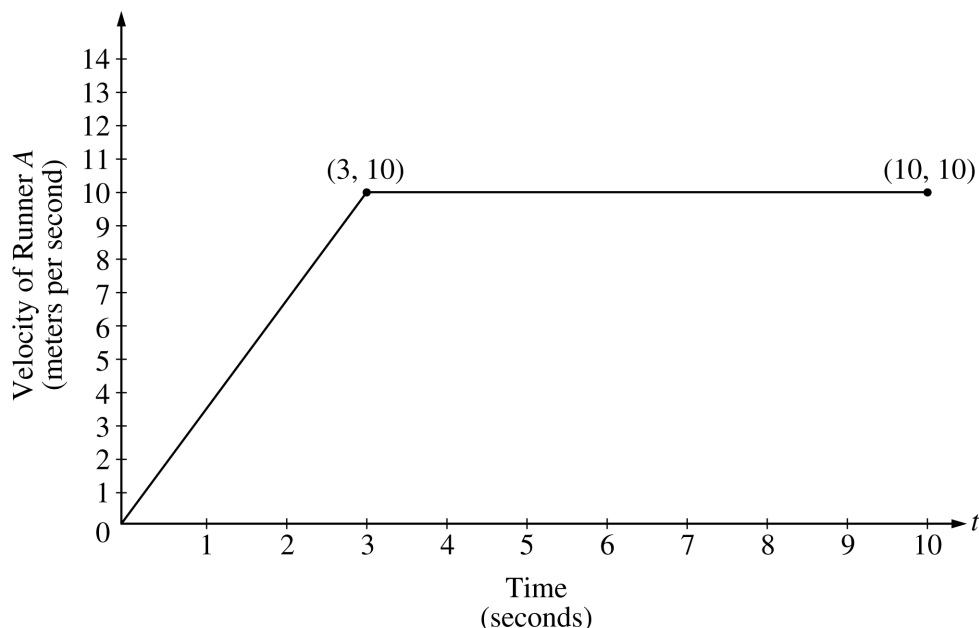


2000 AP® CALCULUS BC FREE-RESPONSE QUESTIONS



2. Two runners, A and B , run on a straight racetrack for $0 \leq t \leq 10$ seconds. The graph above, which consists of two line segments, shows the velocity, in meters per second, of Runner A . The velocity, in meters per second, of Runner B is given by the function v defined by $v(t) = \frac{24t}{2t + 3}$.
- Find the velocity of Runner A and the velocity of Runner B at time $t = 2$ seconds. Indicate units of measure.
 - Find the acceleration of Runner A and the acceleration of Runner B at time $t = 2$ seconds. Indicate units of measure.
 - Find the total distance run by Runner A and the total distance run by Runner B over the time interval $0 \leq t \leq 10$ seconds. Indicate units of measure.

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3. The Taylor series about $x = 5$ for a certain function f converges to $f(x)$ for all x in the interval of convergence. The n th derivative of f at $x = 5$ is given by $f^{(n)}(5) = \frac{(-1)^n n!}{2^n (n + 2)}$, and $f(5) = \frac{1}{2}$.
- Write the third-degree Taylor polynomial for f about $x = 5$.
 - Find the radius of convergence of the Taylor series for f about $x = 5$.
 - Show that the sixth-degree Taylor polynomial for f about $x = 5$ approximates $f(6)$ with error less than $\frac{1}{1000}$.

END OF PART A OF SECTION II

2000 AP® CALCULUS BC FREE-RESPONSE QUESTIONS

CALCULUS BC

SECTION II, Part B

Time—45 minutes

Number of problems—3

No calculator is allowed for these problems.

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4. A moving particle has position $(x(t), y(t))$ at time t . The position of the particle at time $t = 1$ is $(2, 6)$, and the velocity vector at any time $t > 0$ is given by $\left(1 - \frac{1}{t^2}, 2 + \frac{1}{t^2}\right)$.
- (a) Find the acceleration vector at time $t = 3$.
 - (b) Find the position of the particle at time $t = 3$.
 - (c) For what time $t > 0$ does the line tangent to the path of the particle at $(x(t), y(t))$ have a slope of 8 ?
 - (d) The particle approaches a line as $t \rightarrow \infty$. Find the slope of this line. Show the work that leads to your conclusion.
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5. Consider the curve given by $xy^2 - x^3y = 6$.
- (a) Show that $\frac{dy}{dx} = \frac{3x^2y - y^2}{2xy - x^3}$.
 - (b) Find all points on the curve whose x -coordinate is 1, and write an equation for the tangent line at each of these points.
 - (c) Find the x -coordinate of each point on the curve where the tangent line is vertical.
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