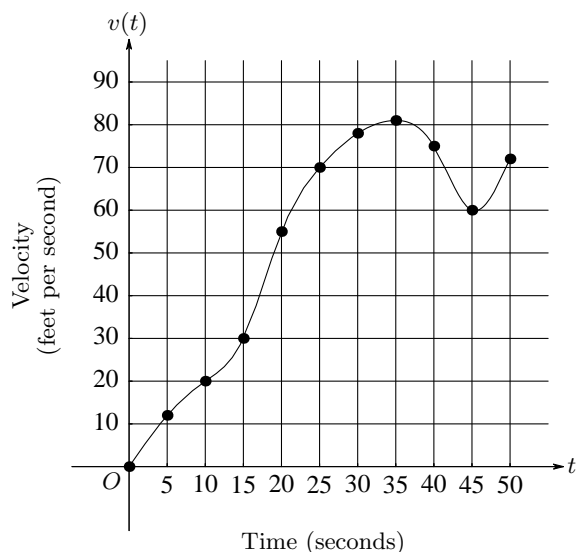


## 1998 AP Calculus AB Free-Response Questions

2. Let  $f$  be the function given by  $f(x) = 2xe^{2x}$ .
- (a) Find  $\lim_{x \rightarrow -\infty} f(x)$  and  $\lim_{x \rightarrow \infty} f(x)$ .
  - (b) Find the absolute minimum value of  $f$ . Justify that your answer is an absolute minimum.
  - (c) What is the range of  $f$ ?
  - (d) Consider the family of functions defined by  $y = bxe^{bx}$ , where  $b$  is a nonzero constant. Show that the absolute minimum value of  $bxe^{bx}$  is the same for all nonzero values of  $b$ .
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# 1998 AP Calculus AB Free-Response Questions



$t$ (seconds)	$v(t)$ (feet per second)
0	0
5	12
10	20
15	30
20	55
25	70
30	78
35	81
40	75
45	60
50	72

3. The graph of the velocity  $v(t)$ , in ft/sec, of a car traveling on a straight road, for  $0 \leq t \leq 50$ , is shown above. A table of values for  $v(t)$ , at 5 second intervals of time  $t$ , is shown to the right of the graph.
- During what intervals of time is the acceleration of the car positive? Give a reason for your answer.
  - Find the average acceleration of the car, in ft/sec<sup>2</sup>, over the interval  $0 \leq t \leq 50$ .
  - Find one approximation for the acceleration of the car, in ft/sec<sup>2</sup>, at  $t = 40$ . Show the computations you used to arrive at your answer.
  - Approximate  $\int_0^{50} v(t) dt$  with a Riemann sum, using the midpoints of five subintervals of equal length. Using correct units, explain the meaning of this integral.

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