

Begin your response to **QUESTION 4** on this page.

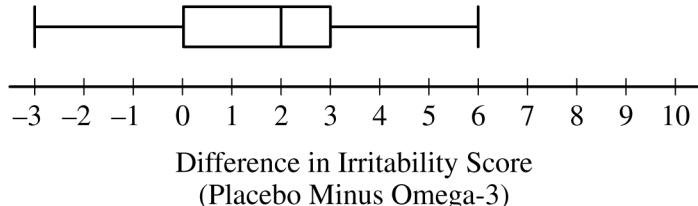
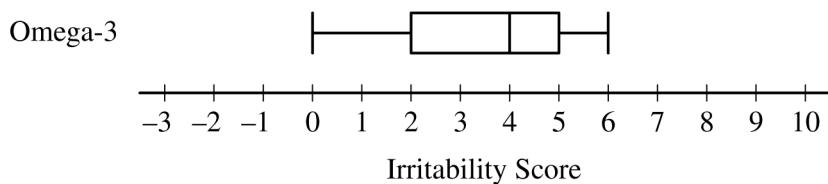
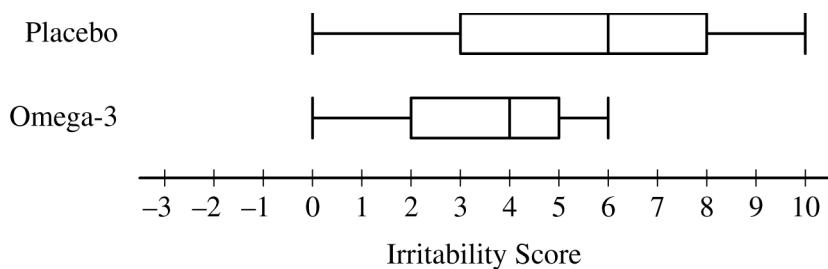
4. A medical researcher completed a study comparing an omega-3 fatty acids supplement to a placebo in the treatment of irritability in patients with a certain medical condition. Nineteen patients with the medical condition volunteered to participate in the study. The study was conducted using the following weekly schedule.

- Week 1: Each patient took a randomly assigned treatment, omega-3 supplement or placebo.
- Week 2: The patients did not take either the omega-3 supplement or the placebo. This was necessary to reduce the possibility of any carryover effect from the assigned treatment taken during week 1.
- Week 3: Each patient took the treatment, omega-3 supplement or placebo, that they did not take during week 1.

At the end of week 1 and week 3, each patient's irritability was given a score on a scale of 0 to 10, with 0 representing no irritability and 10 representing the highest level of irritability.

For each patient, the two irritability scores and the difference in their scores (placebo minus omega-3) were recorded. The results are summarized in the table and boxplots.

	<i>n</i>	Mean	Standard Deviation
Placebo	19	5.421	2.987
Omega-3	19	3.632	1.739
Difference (placebo minus omega-3)	19	1.789	2.485



GO ON TO THE NEXT PAGE.

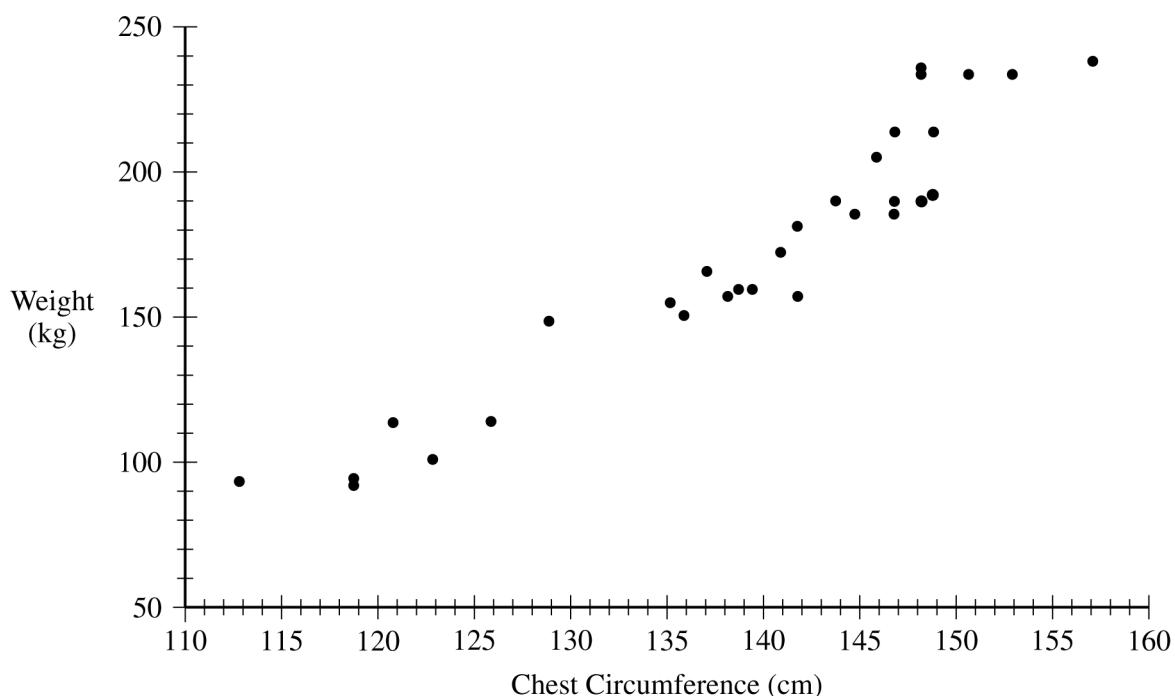
Continue your response to **QUESTION 4** on this page.

The researcher claims the omega-3 supplement will decrease the mean irritability score of all patients with the medical condition similar to the volunteers who participated in the study. Is there convincing statistical evidence to support the researcher's claim at a significance level of $\alpha = 0.05$? Complete the appropriate inference procedure to support your answer.

GO ON TO THE NEXT PAGE.

Begin your response to **QUESTION 5** on this page.

5. Wildlife biologists are interested in the health of tule elk, a species of deer found in California. An important measurement of tule elk health is their weight. The weight of a tule elk is difficult to measure in the wild. However, chest circumference, which is believed to be related to the weight of a tule elk, can easily be measured from a safe distance using a harmless laser. A study was done to investigate whether chest circumference, in centimeters (cm), could be used to accurately estimate the weight, in kilograms (kg), of male tule elk. For the study, wildlife biologists captured 30 male tule elk, measured their chest circumference and weight, and then released the elk. The data for the 30 male tule elk are shown in the scatterplot.



- (a) Describe the relationship between chest circumference and weight of male tule elk in context.

GO ON TO THE NEXT PAGE.

Question 4: Focus on Inference**4 points****General Scoring Notes**

- This question is scored in three sections. Each section is initially scored by determining if it meets the criteria for essentially correct (E), partially correct (P), or incorrect (I). The first section includes statements of the null and alternative hypotheses and identification of the appropriate hypothesis test. The second section includes verifying the conditions for the test identified in the first section and calculating the value of the test statistic and the corresponding p -value. The third section includes the conclusion for the test identified in the first section. The response is then categorized based on the scores assigned to each section and awarded an integer score between 0 and 4 (see the table at the end of the question).
- The model solution represents an ideal response to each section of the question, and the scoring criteria identify the specific components of the model solution that are used to determine the score.

Model Solution

Section 1 Let μ_d represent the true mean difference (placebo minus omega-3) of irritability scores for all people with this medical condition.

The null hypothesis is $H_0: \mu_d = 0$ and the alternative hypothesis is $H_a: \mu_d > 0$.

The appropriate inference procedure is a matched pairs t -test for a mean difference.

Scoring

Essentially correct (E) if the response satisfies the following four components:

- Identifies a paired t -test for a population mean difference by name or by formula
- States the hypotheses using a single mean (e.g., μ_d, μ)
- States the correct equality for the null hypothesis (e.g., $H_0: \mu_d = 0$) AND states the correct direction for the alternative hypothesis (e.g., $H_a: \mu_d > 0$)
- Provides sufficient context for the parameter, by including reference to the *population* mean difference *AND* the sampling units (people with the medical condition) *AND* the response variable (irritability score)

Partially correct (P) if the response satisfies three of the four components.

Incorrect (I) if the response does not meet the criteria for E or P.

Additional Notes:

- A response that states the null hypothesis as $H_0: \mu_d \leq 0$ may satisfy component 3.
- A response that states the name of the procedure as t -test, or one-sample t -test may satisfy component 1.
- To satisfy component 2, the hypotheses must be stated in terms of a mean. If a symbol other than μ or \bar{X} is used to denote the mean, it must be clearly defined as a mean (but does not need to reflect the context of irritability score). It is acceptable to use μ_0 to denote the mean.

Scoring for Question 4	Score
Complete Response Three sections essentially correct	4
Substantial Response Two sections essentially correct and one section partially correct	3
Developing Response Two sections essentially correct and no section partially correct <i>OR</i> One section essentially correct and one or two sections partially correct <i>OR</i> Three sections partially correct	2
Minimal Response One section essentially correct and no section partially correct <i>OR</i> No section essentially correct and two sections partially correct	1