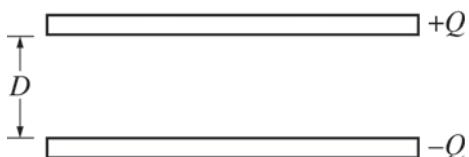


**2015 AP® PHYSICS C: ELECTRICITY AND MAGNETISM FREE-RESPONSE QUESTIONS****PHYSICS C: ELECTRICITY AND MAGNETISM  
SECTION II  
Time—45 minutes  
3 Questions**

**Directions:** Answer all three questions. The suggested time is about 15 minutes for answering each of the questions, which are worth 15 points each. The parts within a question may not have equal weight. Show all your work in this booklet in the spaces provided after each part.

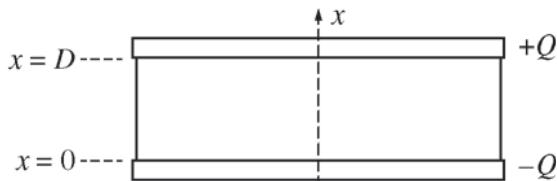


E&M.1.

A parallel-plate capacitor is constructed of two parallel metal plates, each with area  $A$  and separated by a distance  $D$ . The plates of the capacitor are each given a charge of magnitude  $Q$ , as shown in the figure above. Ignore edge effects.

(a)

- On the figure above, draw an arrow to indicate the direction of the electric field between the plates.
- On the figure above, draw an appropriate Gaussian surface that will be used to derive an expression for the magnitude of the electric field  $E$  between the plates.
- Using Gauss's law and the Gaussian surface from part (a)-ii, derive an expression for the magnitude of the electric field  $E$  between the plates. Express your answer in terms of  $A$ ,  $D$ ,  $Q$ , and physical constants, as appropriate.



The space between the plates is now filled with a dielectric material that is engineered so that its dielectric constant varies with the distance from the bottom plate to the top plate, defined by the  $x$ -axis indicated in the diagram above. As a result, the electric field between the plates is given by  $\vec{E} = -\frac{Q}{\epsilon_0 \kappa_0 e^{-x/D} A} \hat{i}$ , where  $\kappa_0$  is a positive constant. Express all algebraic answers to the remaining parts in terms of  $A$ ,  $D$ ,  $Q$ ,  $\kappa_0$ ,  $x$ , and physical constants, as appropriate.

- (b) Determine an expression for the dielectric constant  $\kappa$  as a function of  $x$ .

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(c)

- i. Write, but do NOT solve, an equation that could be used to determine the potential difference  $V$  between the plates of the capacitor.
- ii. Using the equation from part (c)-i, derive an expression for the potential difference  $V_D - V_0$ , where  $V_D$  is the potential of the top plate and  $V_0$  is the potential of the bottom plate.

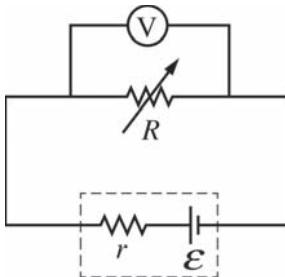
(d) Determine the capacitance of the capacitor.

(e) The energy stored in the capacitor that has a varying dielectric is  $U_V$ . A second capacitor that has a constant dielectric of value  $\kappa_0$  is also given a charge  $Q$ . The energy stored in the second capacitor is  $U_C$ . How do the values of  $U_V$  and  $U_C$  compare?

$U_V < U_C$         $U_V > U_C$         $U_V = U_C$

Justify your answer.

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E&M.2.

A student performs an experiment to determine the emf  $\mathcal{E}$  and internal resistance  $r$  of a given battery. The student connects the battery in series to a variable resistance  $R$ , with a voltmeter across the variable resistor, as shown in the figure above, and measures the voltmeter reading  $V$  as a function of the resistance  $R$ . The data are shown in the table below.

Trial #	Resistance ( $\Omega$ )	Voltage (V)	$1/R$ ( $1/\Omega$ )	$1/V$ ( $1/V$ )
1	0.50	5.6	2.00	0.179
2	1.0	7.4	1.00	0.135
3	2.0	9.4	0.50	0.106
4	3.0	10.6	0.33	0.094
5	5.0	10.9	0.20	0.092
6	10	11.4	0.10	0.088

(a)

- Derive an expression for the measured voltage  $V$ . Express your answer in terms of  $R$ ,  $\mathcal{E}$ ,  $r$ , and physical constants, as appropriate.
- Rewrite your expression from part (a)-i to express  $1/V$  as a function of  $1/R$ .