

2002 AP[®] CALCULUS AB FREE-RESPONSE QUESTIONS

3. An object moves along the x -axis with initial position $x(0) = 2$. The velocity of the object at time $t \geq 0$ is given by $v(t) = \sin\left(\frac{\pi}{3}t\right)$.

(a) What is the acceleration of the object at time $t = 4$?

(b) Consider the following two statements.

Statement I: For $3 < t < 4.5$, the velocity of the object is decreasing.

Statement II: For $3 < t < 4.5$, the speed of the object is increasing.

Are either or both of these statements correct? For each statement provide a reason why it is correct or not correct.

(c) What is the total distance traveled by the object over the time interval $0 \leq t \leq 4$?

(d) What is the position of the object at time $t = 4$?

END OF PART A OF SECTION II

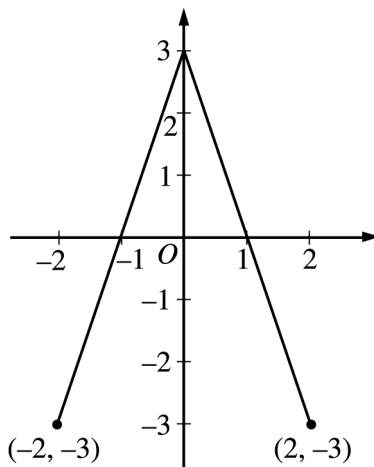
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CALCULUS AB SECTION II, Part B

Time—45 minutes

Number of problems—3

No calculator is allowed for these problems.



Graph of f

4. The graph of the function f shown above consists of two line segments. Let g be the function given by $g(x) = \int_0^x f(t) dt$.
- (a) Find $g(-1)$, $g'(-1)$, and $g''(-1)$.
 - (b) For what values of x in the open interval $(-2, 2)$ is g increasing? Explain your reasoning.
 - (c) For what values of x in the open interval $(-2, 2)$ is the graph of g concave down? Explain your reasoning.
 - (d) On the axes provided, sketch the graph of g on the closed interval $[-2, 2]$.
(Note: The axes are provided in the pink test booklet only.)