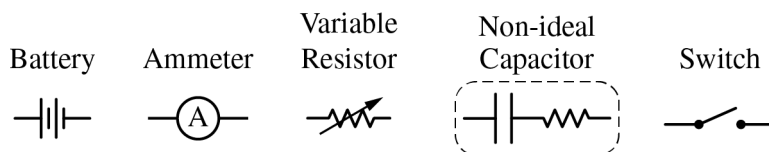


Begin your response to **QUESTION 2** on this page.

2. A non-ideal capacitor has internal resistance that can be modeled as an ideal capacitor in series with a small resistor of resistance  $r_C$ . A group of students performs an experiment to determine the internal resistance of a capacitor. A circuit is to be constructed with the following available equipment: a single ideal battery of potential difference  $\Delta V_0$ , a single ammeter, a single variable resistor of resistance  $R$ , a single uncharged non-ideal capacitor of capacitance  $C$ , and one or more switches as needed.



- (a) Using the symbols shown, draw a schematic diagram of a circuit that can charge the capacitor and may also be used to study the current through the capacitor as it discharges through the resistor.

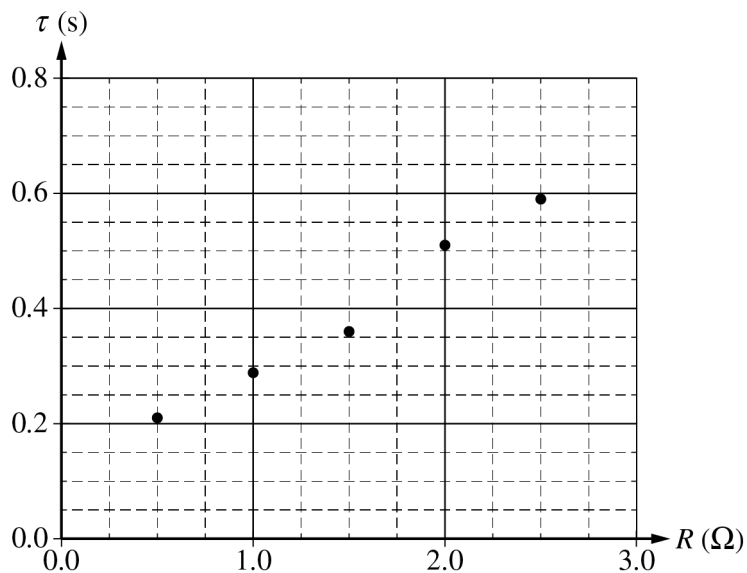
The capacitor is fully charged by the battery. At time  $t = 0$ , the capacitor starts discharging through the resistor.

- (b) Show that the current  $I$  through the capacitor as a function of time  $t$  is  $I(t) = I_0 e^{\frac{-t}{(R+r_C)C}}$  as the capacitor discharges.

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Continue your response to **QUESTION 2** on this page.

- (c) The students determine the time constant  $\tau$  for the circuit as a function of the resistance  $R$ . The students' data are shown in the following graph.



- Draw the best-fit line for the data.
- Using the best-fit line, calculate a value for the internal resistance  $r_C$  of the capacitor.

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Continue your response to **QUESTION 2** on this page.

- (d) The ammeter is found to be nonideal. Is the actual value for the internal resistance  $r_C$  for the capacitor greater than, less than, or equal to the experimental internal resistance of the capacitor calculated in part (c)?

\_\_\_ Greater than      \_\_\_ Less than      \_\_\_ Equal to

Briefly justify your answer using features of the graph in part (c).

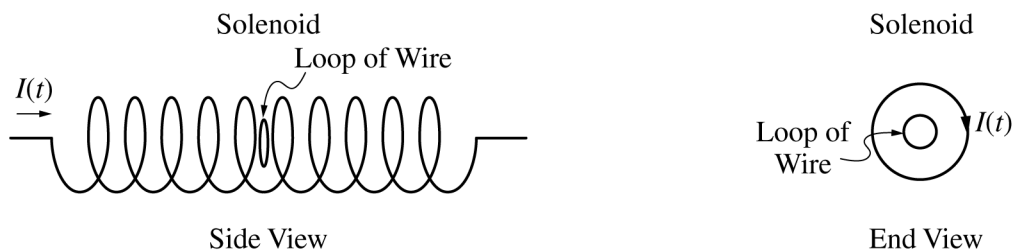
- (e) The values of the variable resistor in the original experiment ranged from  $0.5\ \Omega$  to  $2.5\ \Omega$ . The experiment is repeated with values ranging from  $3.0\ \Omega$  to  $6.0\ \Omega$ . Would the slope of the best-fit line be more steep, be less steep, or remain unchanged compared to the graph in part (c)?

\_\_\_ More steep      \_\_\_ Less steep      \_\_\_ Remain unchanged

Briefly justify your answer.

**GO ON TO THE NEXT PAGE.**

Begin your response to **QUESTION 3** on this page.



Note: Figures not drawn to scale.

3. A single loop of wire with resistance  $3.0\ \Omega$  and radius  $0.10\ \text{m}$  is placed inside a solenoid, with the normal to the loop parallel to the axis of the solenoid. The solenoid has 500 turns, is  $0.25\ \text{m}$  long, and is connected to a power supply that is not shown. At time  $t = 0$ , the power supply is turned on, and the current  $I$  in the solenoid as a function of  $t$  is given by the equation  $I(t) = \beta t$ , where  $\beta = 5.0\ \text{A/s}$ . The direction of the current in the solenoid is clockwise, as shown in the end view.

- (a) At time  $t = 2.0\ \text{s}$ , is the induced current in the loop, as seen from the end view shown, clockwise, counterclockwise, or zero?

\_\_\_ Clockwise      \_\_\_ Counterclockwise      \_\_\_ Zero

Justify your answer.

- (b) Calculate the current in the loop of wire at time  $t = 2.0\ \text{s}$ .

**GO ON TO THE NEXT PAGE.**