2. The rate at which people enter an amusement park on a given day is modeled by the function E defined by

$$E(t) = \frac{15600}{\left(t^2 - 24t + 160\right)}.$$

The rate at which people leave the same amusement park on the same day is modeled by the function L defined by

$$L(t) = \frac{9890}{\left(t^2 - 38t + 370\right)}.$$

Both $E(t)$ and $L(t)$ are measured in people per hour and time t is measured in hours after midnight. These functions are valid for $9 \leq t \leq 23$, the hours during which the park is open. At time $t = 9$, there are no people in the park.

(a) How many people have entered the park by 5:00 P.M. ($t = 17$)? Round your answer to the nearest whole number.

(b) The price of admission to the park is \$15 until 5:00 P.M. ($t = 17$). After 5:00 P.M., the price of admission to the park is \$11. How many dollars are collected from admissions to the park on the given day? Round your answer to the nearest whole number.

(c) Let $H(t) = \int_9^t (E(x) - L(x))\, dx$ for $9 \leq t \leq 23$. The value of $H(17)$ to the nearest whole number is 3725. Find the value of $H'(17)$, and explain the meaning of $H(17)$ and $H'(17)$ in the context of the amusement park.

(d) At what time t, for $9 \leq t \leq 23$, does the model predict that the number of people in the park is a maximum?

GO ON TO THE NEXT PAGE.

3. An object moves along the x-axis with initial position $x(0) = 2$. The velocity of the object at time $t \geq 0$ is given by $v(t) = \sin\left(\dfrac{\pi}{3}t\right)$.

    (a) What is the acceleration of the object at time $t = 4$?

    (b) Consider the following two statements.

    > Statement I: For $3 < t < 4.5$, the velocity of the object is decreasing.
    > Statement II: For $3 < t < 4.5$, the speed of the object is increasing.

    Are either or both of these statements correct? For each statement provide a reason why it is correct or not correct.

    (c) What is the total distance traveled by the object over the time interval $0 \leq t \leq 4$?

    (d) What is the position of the object at time $t = 4$?

END OF PART A OF SECTION II