

# # EXERCISE 1.5

We have:

$$rot(90,x) = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad rot(\alpha,z) = \begin{bmatrix} \cos\alpha & -\sin\alpha & 0 & 0 \\ \sin\alpha & \cos\alpha & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$rot(\beta,y) = \begin{bmatrix} \cos\beta & 0 & \sin\beta & 0 \\ 0 & 1 & 0 & 0 \\ -\sin\beta & 0 & \cos\beta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$rot(90,x) \cdot rot(\alpha,z) = \begin{bmatrix} \cos\alpha & -\sin\alpha & 0 & 0 \\ 0 & 0 & -1 & 0 \\ \sin\alpha & \cos\alpha & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$rot(\beta,y) \cdot rot(90,x) = \begin{bmatrix} \cos\beta & \sin\beta & 0 & 0 \\ 0 & 0 & -1 & 0 \\ -\sin\beta & \cos\beta & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\text{As } rot(90,x) \cdot rot(\alpha,z) = rot(\beta,y) \cdot rot(90,x) \Rightarrow \begin{cases} \cos\alpha = \cos\beta \\ -\sin\alpha = \sin\beta \end{cases} \Rightarrow \alpha = -\beta$$

# # EXERCISE 1.6

- 1)  $rot(90,y) \cdot trans(5.0,0.0,-2.0)$
- 2)  $trans(-4.0,0.0,2.0) \cdot scale(0.5)$
- 3)  $scale(0.5) \cdot trans(-4.0,0.0,2.0)$
- 4)  $trans(-2.0,0.0,4.0) \cdot scale(0.5) \cdot rot(180,y)$

