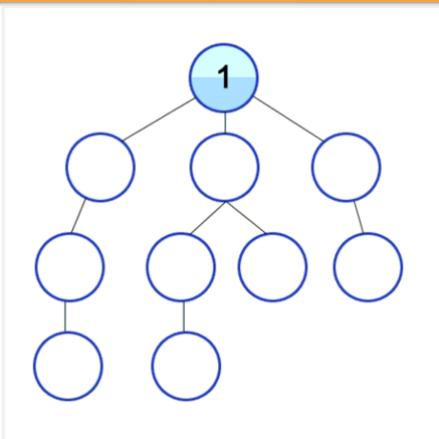
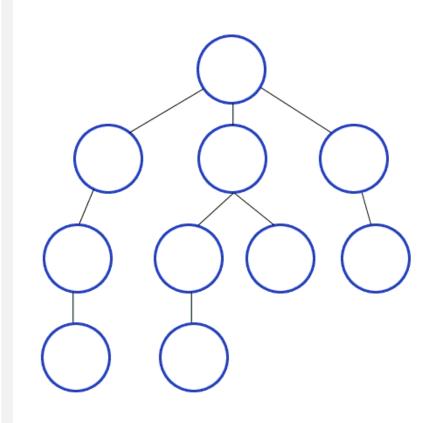


4.4 DFS คืออะไร

- The **Depth First Search** is fundamental search algorithm used to explore node and edges of a graph.
- It runs with a time O(V+E)
- Often used as a building block in other algorithms.







BFS DFS

https://commons.wikimedia.org/wiki/File:Depth-First-Search.gif



วัตถุประสงค์ & ขั้นตอนการทำงาน

- สำรวจตามความลึกของกราฟ
- โดยหาเส้นทางที่ลึกที่สุดจากการเดินจาก เวอร์เห็กซ์ น ไปยัง เวอร์เห็กซ์ v ซึ่งเป็นเวอร์เห็กซ์ข้างเคียงที่ยังไม่ได้เดินผ่าน ทำเช่นนี้จนกระทั่งไม่มี edge ที่สามารถเดินต่อไปได้อีก จากนั้นจึงทำการเดินกลับ (backtrack) ไปยัง source
- A DFS plunges depth first into a graph without regards for which edge it takes next until it cannot go any further at which point it backtracks and continues.



<u>ขั้นตอน(ภาษาอังกฤษ)</u>

- Edges are explored out of the most recently discovered vertex v that still has unexplored edge leaving it.
- 2. When all of v's edges have been explored, the search backtracks to explore edges leaving the vertex from which v has discovered. Until we have discovered all the vertices that are reachable from the original source vertex

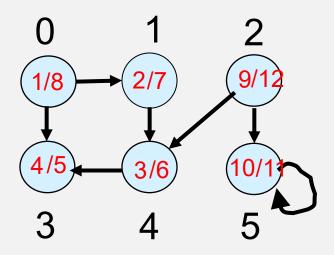




$$S = 0$$

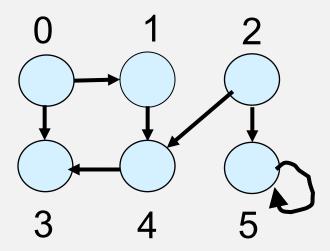




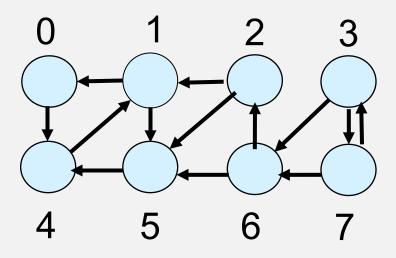






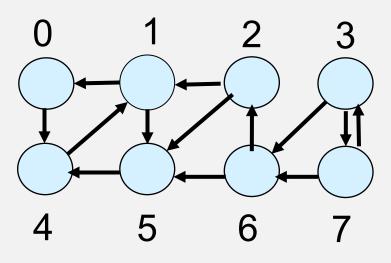


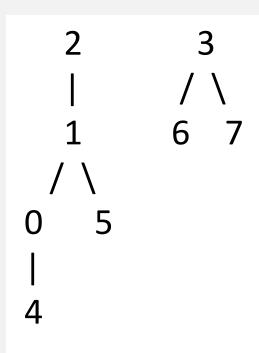






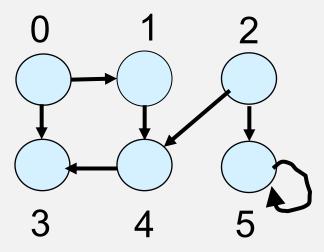
DFS trees







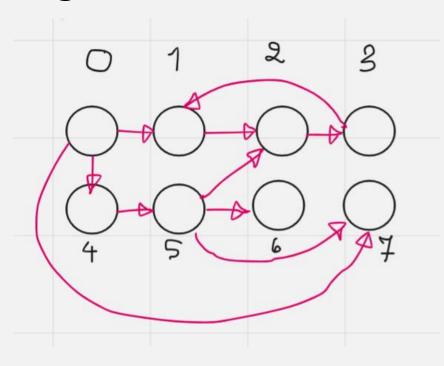
Edge Classification

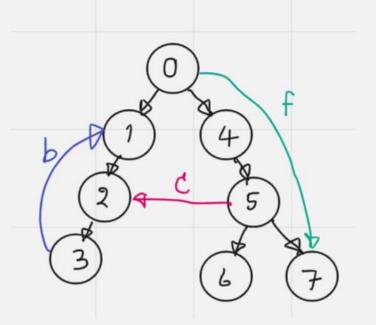


$$S = 0$$



Edge Classification





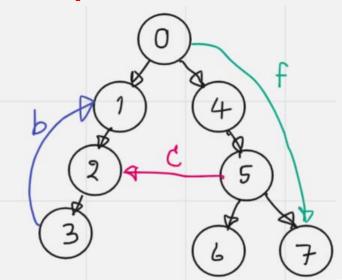
11



Edge Classification

- **1. Tree edges**: are edges in the dfs forest G". Edge (u,v) is a tree edge if v was discovered by exploring edge(u,v).
- 2. Back edge: are those edges (u,v) connecting a vertex u to an ancestor v in a dfs tree. Self-loop are considered to be back edges.

which point from a node to one of its ancestors



Classification of Edge

3. Forward edges: are those non tree edge (u,v) connecting a vertex u to a descendent v in a dfs tree.

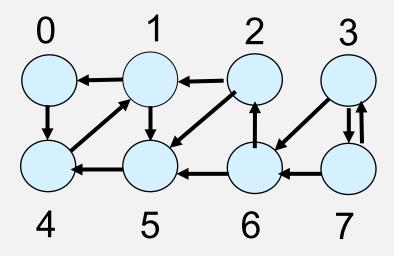
which point from a node of the tree to one of its descendants

4. Cross edge: are all other edges. They can go between vertices in the same depth-first search tree, as long as one vertex is not ancestor of the other, or they can go between vertices in difference dfs tree.

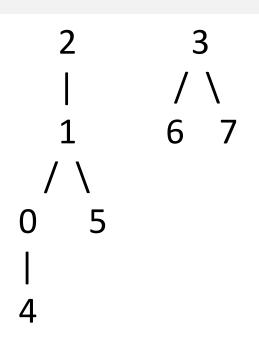
14



DFS trees



- 1. Tree edges
- 2. Back edges
- 3. Forward edges
- 4. Cross edges





0

3

5

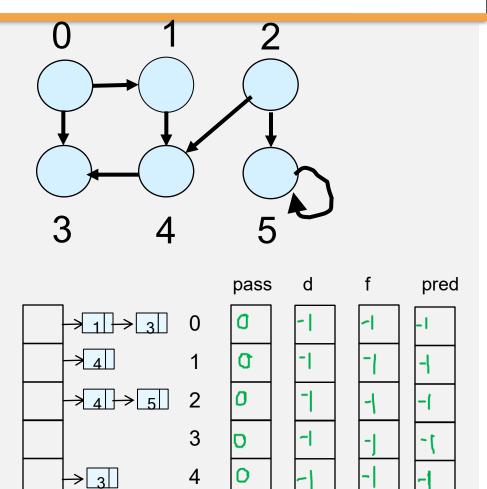
→1

5

4.4.2 Algorithm DFS (G)

```
DFS(G)
```

```
time=0;
for (u=0;u<6;u++)
       pass[u]=0
       pred[u]=d[u]=f[u]=-1;
u=S //สมมุติ s คือ โหนด 0
DFS Visit(u)
for (u=0;u<6;u++)
      if (pass[u]=0)
         DFS Visit(u)
```





```
// time=0 is global
 DFS_Visit(u)
 pass[u]=1
                                                                       3
d[u]=++time;
for each v \in adj[u]
          if (pass[v] == 0)
                    pred[v] = u
                                                                                   f
                                                                                         pred
                                                                     pass
                                                                            d
                                                    \rightarrow 1 \rightarrow 3
                                           0
                                                                0
                    DFS Visit(v)
                                                    → 4
                                                    \rightarrow 4 \rightarrow 5
                                           3
                                                                 3
 pass[u]=1
                                           4
                                                    \rightarrow \boxed{3}
                                                                 4
                                                    <del>)</del> 1
                                           5
                                                                 5
f[u]=++time;
```



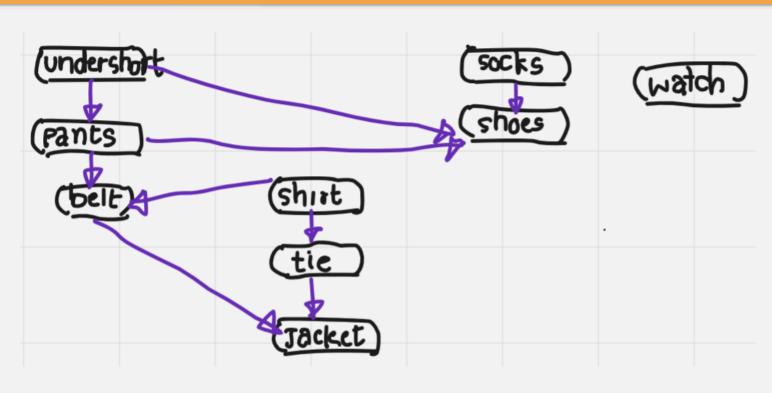
4.4.3 Topological sort

Topological sort of a DAG G=(V,E) is a linear ordering of all its vertices such that if G contains an edge(u,v), then u appears before v in the ordering. (If the graph is not acyclic, then no linear ordering is possible.)

Topological sort คือการนำเวอร์ทิซของกราฟกราฟหนึ่งมา

- •เรียงเป็นเส้นตรงแบบมีลำดับ
- •มีข้อกำหนดว่ากราฟนั้นจะต้องมีคุณสมบัติเป็น directed acyclic graph หรือ DAG (คือกราฟที่ไม่มีไซเคิล)





4.4.4 Algorithm Topological_sort(G)

Topological_sort(G)

- 1) call DFS(G) to computer finishing times f[v] for each vertex v.
 - ทำ DFS กราฟ

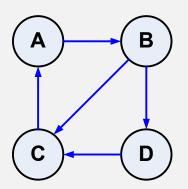


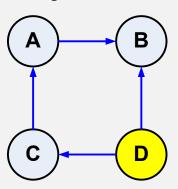
- 2) as each vertex is finished, insert it onto the front of a linked list
- เมื่อ DFS แล้ว ให้นำ vertex ที่มี finish time สูงสุดใส่ ไว้ตำแหน่งแรกของ linklist
- finish time ที่มีค่ารองลงมาให้นำไปใส่ไว้ตำแหน่งที่ 2 ของ linklist และทำเช่นนี้โดยเรียงจากมากไปน้อย
- 3) return the link list of vertices.



4.4.5 Strongly connected components

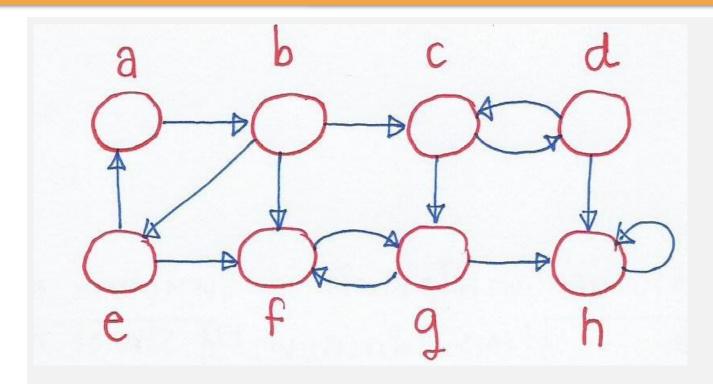
A digraph is *strongly connected* if every two vertices are reachable from each other. The *strongly connected components* of a graph are the equivalence classes of vertices under the "are *mutually reachable*" relation.













4.4.6 Strongly-Connected-Component Algorithm

- 1) call DFS(G) to compute finishing times f[u] for each vertex u
- 2) compute GT (transpose graph)
- **3)** call DES(GT), but the main loop of DFS, consider the vertices in order of decreasing f[u] (as computed in line 1)
- 4) output the vertices of each tree