Ca_bot Inverse Kinematics

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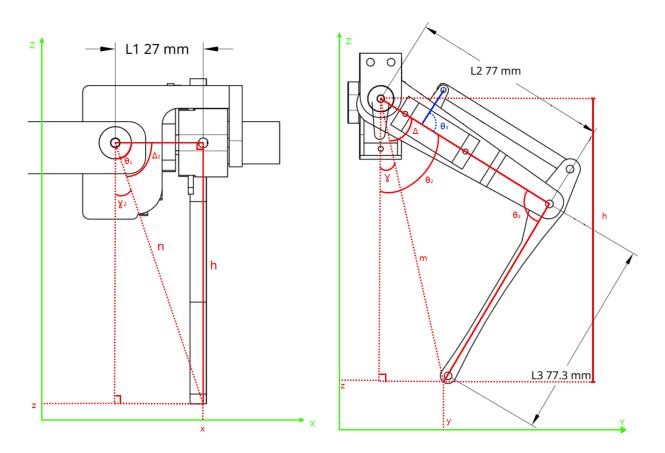


Figure 1: We use trigonometry to compute the inverse kinematics of the leg

We want to find the values of the angles θ_1 , θ_2 and θ_3 given the x, y and z position of the leg (see Figure 1).

For θ_1 , we first need to compute the angles γ_2 and Δ_2 . Using the Pythagorean theorem, we have :

$$n = \sqrt{z^2 + x^2}$$
$$h = \sqrt{n^2 - L1^2}$$

Which allow us to compute γ_2 :

$$\gamma_2 = \arcsin(\frac{x}{n})$$

And Δ_2 using Al-Kashi's theorem :

$$\Delta_2 = \arccos(\frac{-h^2 + n^2 + L1^2}{2 \cdot n \cdot L1})$$

Then,

$$\theta_1 = \gamma_2 + \Delta_2$$

Same process for θ_2 , this time we need to compute γ and Δ . Using the Pythagorean theorem, we have :

$$m = \sqrt{y^2 + h^2}$$

Thus,

$$\gamma = \arcsin(\frac{y}{m})$$

And using Al-Kashi's theorem again:

$$\Delta = \arccos(\frac{-L3^2 + m^2 + L2^2}{2 \cdot m \cdot L2})$$

Then,

$$\theta_2 = \gamma + \Delta$$

Eventually, we find θ_3 using Al-Kashi's theorem again :

$$\theta_3 = \arccos(\frac{-m^2 + L2^2 + L3^2}{2 \cdot L2 \cdot L3})$$

Note: The blue θ_3 on Figure 1 is the actual angle being actuated, but as we have a parallel mechanism here, it is actually the same value as the red one.