C/O AND SNOWLINE LOCATIONS IN PROTOPLANETARY DISKS: THE EFFECT OF RADIAL DRIFT AND VISCOUS GAS ACCRETION

Ana-Maria A. Piso¹, Karin I. Öberg¹, Tilman Birnstiel¹, Ruth A. Murray-Clay² Draft version August 7, 2015

ABSTRACT

The C/O ratio is a defining feature of both gas giant atmospheric and protoplanetary disk chemistry. In disks, the C/O ratio is regulated by the presence of snowlines of major volatiles at different distances from the central star. We explore the effect of radial drift of solids and viscous gas accretion onto the central star on the snowline locations of the main C and O carriers in a protoplanetary disk, H₂O, CO_2 and CO. We estimate the resulting C/O ratio in gas and dust throughout the disk. We determine the snowline locations for a range of fixed initial particle sizes, in both an active and a passive disk. We find that grains with sizes ~ 0.5 cm $\lesssim s \lesssim 7$ m for a passive disk and ~ 0.001 cm $\lesssim s \lesssim 7$ m for an active disk desorb at a size-dependent location in the disk, which is independent of the particle's initial position. The snowline radius decreases for larger particles, up to sizes of ~ 7 m. Compared to a static disk, we find that radial drift and gas accretion move the H₂O and CO₂ snowlines inwards by up to 60 %, and the CO snowline by up to 50 %. We thus determine an inner limit on the snowline locations when radial drift and gas accretion are accounted for.

1. INTRODUCTION

The chemical composition of protoplanetary disks affects planet formation efficiencies and the composition of nascent planets. Gas giants accrete their envelopes from the nebular gas. As such, planet compositions are tightly linked to the structure and evolution of the protoplanetary disk in which they form. It is thus essential to understand the disk chemistry and dynamics well enough to (1) predict the types of planet compositions that result from planet formation in different parts of the disk, and (2) backtrack the planet formation location based on planet compositions.

The structures of protoplanetary disks are complex, and affected by a multitude of chemical and dynamical processes (see review by Henning & Semenov 2013). From the chemistry perspective, volatile compounds are particularly important. Their snowline locations determine their relative abundance in gaseous and solid form in the disk, and thus the chemical composition of nascent giant planets. Based on protostellar and comet abundances, some of the most important volatile molecules are H₂O, CO₂, CO, N₂. Recent observations of protoplanetary disks have provided valuable information about the abundances and snowline locations of some of these compounds. For example, the CO snowline has been detected in the disks around HD 163296 (Qi et al. 2011) and TW Hya (Qi et al. 2013). Observations of TW Hya have also revealed a H₂O snowline (Zhang et al. 2013), and more such snowline detections are expected in future ALMA cycles. These observations are currently lacking an interpretive framework that takes into account all important dynamical and chemical processes. Furthermore, such a framework is crucial to connect observed snowline locations to planet formation.

An important consequence of snowline formations in

disks is that disks are expected to present different carbon-to-oxygen (C/O) ratios in the gas and in icy dust mantles at different disk radii. This effect was quantified by Öberg et al. (2011), who considered the fact that the main carries of carbon and oxygen, i.e. H₂O, CO₂ and CO, have different condensation temperatures. This changes the relative abundance of C and O in gaseous and solid form as a function of the snowline location of the volatiles mentioned above. Öberg et al. (2011) calculated analytically the C/O ratio in gas in dust as a function of semimajor axis for passive protoplanetary disks and found a gas C/O ratio of order unity between the CO₂ and CO snowlines, where oxygen gas is highly depleted. Claims of detections of superstellar C/O ratios also exist for exoplanet atmospheres (e.g., WASP-12b, Madhusudhan et al. 2011).

Öberg et al. (2011) assumed a static disk with passive chemistry. In reality, additional dynamical and chemical processes affect the snowline locations and the resulting C/O ratio. Several works have addressed some of these effects. Madhusudhan et al. (2014) use a steady-state active disk model that includes planetary migration and use the C/O ratio to constrain migration mechanisms. Ali-Dib et al. (2014) calculate the C/O ratio throughout the disk by incorporating the evolution of solids, i.e. radial drift, sublimation and grain coagulation, as well as the diffusion of volatile vapors. Ali-Dib et al. (2014) use the 1+1D α -disk model of Hughes & Armitage (2010), in which the gas drifts outwards in the disk midplane, and thus small particles that are well-coupled to the gas will also advect outward. Their model assumes a cyclical conversion between H₂O or CO dust and vapor: large enough particles that are decoupled from the gas drift inwards and start desorbing. Once their sublimation is complete, back-diffusion moves the H₂O or CO vapor ouwards to their respective snowlines, where they instantly condense into mm-sized particles that diffuse outwards with the gas while coagulating into larger particles. Once the grains become large enough to de-

¹ Harvard-Smithsonian Center for Astrophysics, 60 Garden

Street, Cambridge, MA 02138

² Department of Physics, University of California, Santa Barbara, CA 93106

couple from the gas and drift inwards, the cycle restarts. This approach leads Ali-Dib et al. (2014) to find that the gaseous C/O ratio increases with time inside the H₂O snowline, approaching unity at 2 AU after $\sim 10^4 - 10^5$ years. Thiabaud et al. (2015) consider additional carbon carrier volatile species in their chemical network, such as CH_4 , and find that the gas C/O ratio may be enriched by up to four times the Solar value in the outer parts of the disk where CH₄ and CO are the only gaseous carriers of C and O. They also include nitrogen carriers such as N_2 or NH₃, and perform similar calculations for nitrogen.

Each of these studies have considered a specific combination of dynamical and chemical effects. One combination that has not yet been considered is the combination of radial drift and viscous gas accretion. Studying these two dynamical processes makes it possible to quantify their separate effect on snowline locations and the C/O ratio at various disk radii.

In this paper, we perform a systematic study to understand the detailed qualitative and quantitative effects of radial drift and gas accretion on the H₂O, CO₂ and CO snowline locations, and the resulting C/O ratio in gas and dust throughout the protoplanetary disk. More importantly, we obtain a limit on how close to the star the snowline locations can be pushed by radial drift and gas accretion.

This paper is organized as follows. In Section 2, we present our disk, radial drift and desorption models, as well as the timescales relevant to the coupled driftdesorption process. We calculate the H₂O, CO₂ and CO snowline locations as a function of particle size for a passive and an active disk in Section 3, and the resulting C/O ratio throughout the disk in Section 4. In Section 5, we discuss the generality of our results, as well as additional effects on the snowline locations. Finally, we summarize our findings in Section 6.

2. MODEL FRAMEWORK

We present our protoplanetary disk model for both a passive and an active disk in section 2.1. In section 2.2, we describe our analytic model for the radial drift of solids. We summarize our ice desorption model in section 2.3. Finally, we discuss the relevant timescales for dynamical effects that affect snowline locations in section 2.4.

2.1. Disk Model

To understand the separate effects of radial drift, radial movement of gas throughout the disk due to gas accretion, and accretion heating, we use four separate disk models: passive disk, which is only irradiated by the central star and does not experience gas accretion or accretional heating; active disk with passive temperature profile (hereafter active disk), in which the gas is accreting onto the central star causing the gas surface density to decrease with time, but which does not experience accretion heating; active disk at steady-state with accretion heating (hereafter active disk accretionally heated), for which the mass flux M is constant in time and independent of semimajor axis and the temperature profile is calculated using both accretional heating and stellar irradiation; and static disk, which has a passive temperature profile and does not take into account gas accretion

onto the central star or radial drift.

Passive disk. We adopt a minimum mass solar nebula (MMSN) disk model for a passive disk similar to the prescription of Chiang & Youdin (2010). The gas surface density and midplane temperature are

$$\Sigma = 2000 (r/AU)^{-1} \text{ g cm}^{-2}$$
 (1a)

$$T = 120 (r/AU)^{-3/7} K,$$
 (1b)

where r is the semimajor axis. Our surface density profile is flatter than the $\Sigma \propto r^{-3/2}$ used by Chiang & Youdin (2010). Our choice is inspired by observations of protoplanetary disks at radii larger than ~ 20 AU (e.g., Andrews et al. 2010), which suggest that typical disks may have surface density profiles with $\Sigma \propto r^{-1}$.

Active disk. We model the active disk as a thin disk with an α -viscosity prescription (Shakura & Sunyaev 1973):

$$\nu = \alpha c H. \tag{2}$$

Here ν is the kinematic viscosity, $\alpha < 1$ is a dimensionless coefficient and we choose $\alpha = 0.01$, and c, H are the isothermal sound speed and disk scale height, respectively:

$$c = \sqrt{\frac{k_{\rm B}T}{\mu m_{\rm p}}}$$

$$H = \frac{c}{\Omega_{\rm k}},$$
(3a)

$$H = \frac{c}{\Omega_{k}}, \tag{3b}$$

where $k_{\rm B}$ is the Boltzmann constant, μ is the mean molecular weight of the gas, $m_{\rm p}$ is the proton mass, and $\Omega_{\rm k} \equiv \sqrt{GM_*/r^3}$ is the Keplerian angular velocity, with G the gravitational constant and M_* the stellar mass. We choose $M_* = M_{\odot}$ and $\mu = 2.35$, corresponding to the Solar composition of hydrogen and helium. The temperature profile for the active disk is assumed to be the same as for the passive disk and given by Equation (1b). From Equations (2) and (3), the viscosity can thus be expressed as a power-law in radius, $\nu \propto r^{\gamma}$, with $\gamma = 15/14 \approx 1$ for our choice of parameters. Following Hartmann et al. (1998), we define $R \equiv r/r_c$ and $\nu_c \equiv \nu(r_c)$, where r_c is a characteristic disk radius. We choose $r_{\rm c}=100$ AU. The gas surface density is given by the self-similar solution

$$\Sigma(R, \overline{T}) = \frac{M}{2\pi r_{\rm c}^2 R^{\gamma}} \overline{T}^{-(5/2 - \gamma)/(2 - \gamma)} \exp\left[-\frac{R^{(2 - \gamma)}}{\overline{T}}\right],\tag{4}$$

where M is the total disk mass and

$$\overline{T} \equiv \frac{t}{t_c} + 1$$
 (5a)

$$t_{\rm c} \equiv \frac{1}{3(2-\gamma)^2} \frac{r_{\rm c}^2}{\nu_{\rm c}},$$
 (5b)

where t is time. We choose $M = 0.1 M_{\odot}$ (e.g., Birnstiel et al. 2012), but we note that our results are insensitive to this choice (see Section 5).

Active disk accretionally heated. the midplane temperature self-consistently for an active disk is non-trivial. We thus use instead the Shakura-Sunyaev thin disk steady-state solution to derive the midplane temperature profile, $T_{\rm act}$. The equations governing the evolution of the steady-state disk are listed in Appendix A. We assume an interstellar opacity for the dust grains given by Bell & Lin (1994), but reduced by a factor of 100. This reduction is due to the fact that disk opacities are lower than the interstellar one. While this scaling is consistent with more detailed models of grain opacities in disks (e.g., Mordasini et al. 2014), realistic disk opacities are much less sensitive to changes in temperature than the interstellar opacity if substantial grain growth has occurred. However, the disk temperature does not vary significantly across the small region of the disk where accretion heating is important $(r \leq 1$ AU). Moreover, using an analytic opacity formula is more convenient since it results in a constant gas surface density in the inner disk region (see below). Our opacity law is thus

$$\kappa = \kappa_0 T_{\text{act}}^2,$$
(6)

where $\kappa_0 = 2 \times 10^{-6}$. By solving the Equation set (A1) we find

$$T_{\rm act} = \frac{1}{4r} \left(\frac{3G\kappa_0 \dot{M}^2 M_* \mu m_{\rm p} \Omega_{\rm k}}{\pi^2 \alpha k_{\rm B} \sigma} \right)^{1/3}.$$
 (7)

Since both accretion heating and stellar irradiation contribute to the thermal evolution of the disk, we compute the midplane temperature for our steady-state active disk as

$$T^4 = T_{\text{act}}^4 + T_{\text{pas}}^4,$$
 (8)

where to avoid notation confusion $T_{\rm pas}=T$ from Equation (1b), the temperature profile for a passive disk. We can then easily determine c and H from Equation (3), as well as the viscosity ν from Equation (2) for a given α . For consistency, we choose $\alpha=0.01$ as in the previous case. Finally, we determine Σ from Equation (A1g), where we choose $\dot{M}=10^{-8}M_{\odot}~{\rm yr}^{-1}$ based on disk observations (e.g., Andrews et al. 2010). In the inner portion of our disk ($r\lesssim 1$ AU for our fiducial model with $M=10^{-8}M_{\odot}~{\rm yr}^{-1}$), our choice of opacity (Equation 6) implies that the disk has a constant surface density with radius (see Equations A1).

Static disk. To compare our results with those of Öberg et al. (2011), we also use a static disk model, with Σ and T described by Equations (1a) and (1b).

2.2. Radial Drift

Solid particles orbit their host star at the Keplerian velocity $v_k \equiv \Omega_k r$. The gas, however, experiences an additional pressure gradient, which causes it to rotate at sub-Keplerian velocity (Weidenschilling 1977). Dust grains that are large enough thus experience a headwind, which removes angular momentum, causing the solids to spiral inwards and fall onto the host star. Small particles are well-coupled to the gas, while large planetesimals are decoupled from the gas. From the review by Chiang & Youdin (2010), the extent of coupling is quantified by the dimensionless stopping time, $\tau_s \equiv \Omega_k t_s$, where t_s is

$$t_{\rm s} = \left\{ \begin{array}{ll} \rho_{\rm s} s/(\rho c), & s < 9\lambda/4 \;\; {\rm Epstein \; drag} \\ 4\rho_{\rm s} s^2/(9\rho c\lambda), & s < 9\lambda/4, \, {\rm Re} \lesssim 1 \;\; {\rm Stokes \; drag}. \end{array} \right.$$

(9)

Here ρ is the gas midplane density, $\rho_{\rm s}=2~{\rm g~cm^{-3}}$ is the density of a solid particle, s is the particle size, λ is the mean free path, and Re is the Reynolds number.

For a passive disk, the radial drift velocity can be approximated as

$$\dot{r} \approx -2\eta \Omega_{\rm k} r \left(\frac{\tau_{\rm s}}{1+\tau_{\rm s}^2}\right),$$
 (10)

where

$$\eta \equiv -\frac{\partial P/\partial \ln r}{2\rho v_k^2} \approx \frac{c^2}{2v_k^2} \tag{11}$$

and $P = \rho c^2$ is the disk midplane pressure.

For an active disk, the radial drift velocity has an additional term due to the radial movement of the gas (Birnstiel et al. 2012), i.e.

$$\dot{r} \approx -2\eta \Omega_{\rm k} r \left(\frac{\tau_{\rm s}}{1+\tau_{\rm s}^2}\right) + \frac{\dot{r}_{\rm gas}}{1+\tau_{\rm s}^2},$$
 (12)

where $\dot{r}_{\rm gas}$ is the radial gas accretion velocity and can be expressed as (e.g., Frank et al. 2002)

$$\dot{r}_{\rm gas} = -\frac{3}{\Sigma\sqrt{r}}\frac{\partial}{\partial r}(\nu\Sigma\sqrt{r}) \tag{13}$$

with Σ from Equation (4). For the active disk steadystate solution (see Section 2.1), $\dot{r}_{\rm gas}$ can be expressed more simply using the definition of the mass flux, $\dot{M} = -2\pi r \dot{r}_{\rm gas} \Sigma$, with \dot{M} fixed and Σ obtained from Equation (A1g).

2.3. Volatile Desorption

In order for a volatile species to thermally desorb, it has to overcome the binding energy that keeps it on the grain surface. Following Hollenbach et al. (2009), the desorption rate per molecule for a species x can be expressed as

$$R_{\text{des.x}} = \nu_x \exp\left(-E_x/T_{\text{grain}}\right),\tag{14}$$

where E_x is the adsorption binding energy in units of Kelvin, $T_{\rm grain}$ is the grain temperature, and $\nu_x = 1.6 \times 10^{11} \sqrt{(E_x/\mu_x)} \, {\rm s}^{-1}$ is the molecule's vibrational frequency in the surface potential well, with μ_x the dimensionless mean molecular weight. We assume that the dust and gas have the same temperature in the disk midplane, hence $T_{\rm grain} = T$. For H₂O, CO₂ and CO, the binding energies E_x are assumed to be 5800 K, 2000 K and 850 K, respectively (Öberg et al. 2011). We use the desorption rate, $R_{\rm des}$, to estimate the desorption timescale for particles of different sizes as described in section 2.4.

2.4. Relevant Timescales

We can estimate the extent to which radial drift and gas accretion affect desorption by comparing the timescales for desorption, drift and accretion, for solids of different sizes and compositions.

Desorption timescale. We assume that the solid bodies are perfect spheres and are entirely composed of only one volatile species, i.e. either H₂O, CO₂ or CO ³. The

 $^{^3}$ We discuss the validity of these simplifications in section 5.

timescale to desorb a single layer of molecules can then be estimated as

$$t_{\rm des} = \frac{\rho_{\rm s}}{3\mu_x m_{\rm p}} \frac{s}{N_x R_{\rm des,x}},\tag{15}$$

where $N_x \approx 10^{15}$ sites cm⁻² is the number of adsorption sites of volatile x per cm² (Hollenbach et al. 2009).

Radial drift timescale. To order of magnitude, the radial drift timescale can be estimated as

$$t_{\text{drift}} \sim \left| \frac{r}{\dot{r}} \right|,$$
 (16)

where \dot{r} is the radial drift velocity given by Equation (10) for a passive disk and by Equation (12) for an active disk.

Gas accretion timescale. The timescale for gas accretion onto the central star for an active disk is (e.g., Armitage 2010)

$$t_{\rm gas,acc} \sim \frac{r^2}{\nu} \sim \frac{1}{2\alpha\eta\Omega_{\rm k}},$$
 (17)

with the latter expression derived from Equations (2) and (11).

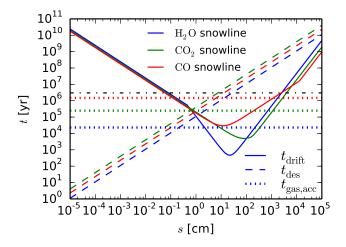


FIG. 1.— Relevant timescales for dynamical effects in the desorption process: $t_{\rm drift}$ (solid lines), $t_{\rm des}$ (dashed lines) and $t_{\rm gas,acc}$ (dotted lines). The timescales are calculated at three representative locations, i.e. the H₂O, CO₂ and CO snowlines in the static disk. For our choice of parameters, the snowlines are located at $\sim\!0.7$ AU (blue lines), $\sim\!8.6$ AU (green lines) and $\sim\!59$ AU (red lines), respectively. The horizontal dot-dashed line represents a typical disk lifetime of 3 Myr. The particle size ordering at the minimum $t_{\rm drift}$ is not monotonic in snowline distance due to different drag regimes for those particle sizes at the snowline locations (Epstein drag at the H₂O and CO₂ snowlines, and Stokes drag at the CO snowline). Similarly, the ordering of $t_{\rm des}$ is not monotonic in snowline distance due to the non-monotony in mean molecular weight between H₂O, CO₂ and CO (18 $m_{\rm p}$, 44 $m_{\rm p}$ and 28 $m_{\rm p}$, respectively). Radial drift and gas accretion affect desorption in the regions where their respective timescales, i.e. $t_{\rm drift}$ and $t_{\rm gas,acc}$, are comparable to the desorption timescale $t_{\rm des}$

For simplicity, we calculate the radial drift timescale, $t_{\rm drift}$, for a passive disk in this section, but most of our conclusions hold true for an active disk as well. Figure 1 shows $t_{\rm des}$, $t_{\rm drift}$ and $t_{\rm gas,acc}$ as a function of particle size at three different locations in the disk, corresponding to the $\rm H_2O$, $\rm CO_2$ and $\rm CO$ snowlines in the static disk. As expected, micron-sized particles desorb on very short

timescales of $\sim 1-1000$ years in the close vicinity of their respective snowlines, since the desorption rate depends exponentially on temperature and hence on disk location (see Equation 14). On the other hand, their radial drift timescale exceeds the typical disk lifetime of a few Myr by several orders of magnitude due to their strong coupling with the gas. Thus for small particles in a passive disk, the snowline locations and the C/O ratio are the same as for a static disk (see Figure 1 from Oberg et al. 2011). This is not true for an active disk, however, where gas accretion causes even micron-sized particles to drift significantly before desorbing, as we show in section 3. At the other extreme, kilometer-sized particles are unaffected by gas drag and have long desorption timescales (≫1 Myr), and the snowline locations and C/O ratio remain unchanged in this case as well. This is true for both passive and active disks, since large planetesimals are decoupled from the gas and hence unaffected by gas accretion onto the host star.

Of particular interest for our purposes is the particle size regime for which (1) $t_{\rm drift} \lesssim t_{\rm des} \lesssim t_{\rm d}$ ($t_{\rm d}=3$ Myr is the disk lifetime), i.e. for ~ 0.5 cm $\lesssim s \lesssim 1000$ cm, or (2) $t_{\rm gas,acc} \lesssim t_{\rm des} \lesssim t_{\rm d}$, i.e. for ~ 0.1 cm $\lesssim s \lesssim 10$ cm. In these cases, radial drift or gas accretion (or both) are faster than thermal desorption. We note that $t_{\rm gas,acc} < t_{\rm d}$ always holds true. Particles of sizes that satisfy the requirements above will drift significantly due to radial drift or gas accretion before desorbing, thus moving the H_2O , CO_2 and CO snowlines closer towards the central star and changing the C/O ratio throughout the disk. We quantify these effects in sections 3 and 4.

3. SNOWLINE LOCATIONS

In this section we use the model described in section 2 to quantify the effects of radial drift (passive disk) or radial drift and gas accretion (active disk) on the snowline location, for dust particles of different sizes composed of either H₂O, CO₂ or CO. Specifically, we determine a particle's final location (i.e., where the particle either fully desorbs or remains at its initial size due to having a desorption timescale longer than the time at which we stop the simulation) as a function of its initial position in the disk, after the gas disk has dissipated. The disk lifetime, $t_{\rm d}$, is particularly relevant since this is the timescale on which giant planets form. The snowline locations at $t = t_{\rm d}$ throughout the protoplanetary disk determine the disk C/O ratio in gas at this time, and thus the C/O ratio in giant planet atmospheres that have formed in situ, before planetesimal accretion or core dredging.

For each species x, we determine the final location in the disk of a particle of initial size s_0 by solving the following system of coupled differential equations:

$$\frac{ds}{dt} = -\frac{3\mu_x m_{\rm p}}{\rho_{\rm s}} N_x R_{\rm des,x}$$
 (18a)

$$\frac{dr}{dt} = \dot{r},\tag{18b}$$

where the desorption rate $R_{\text{des},x}$ for each particle type (i.e., composed of H_2O , CO_2 or CO) is evaluated at T = T(r), and the radial drift velocity \dot{r} is given by Equation (10) for a passive disk and Equation (12) for an active disk. Equations (18a) and (18b) describe the

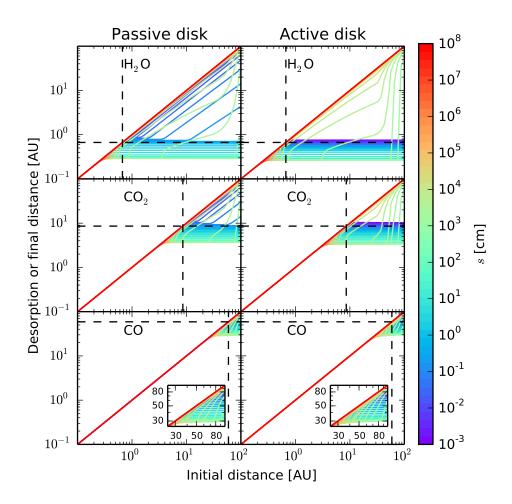


Fig. 2.— Desorption distance (if a grain fully desorbs; horizontal lines) or final distance (if a grain does not fully desorb; diagonal lines for particles that do not drift and non-horizontal, non-diagonal lines for particles that drift), as a function of a particle's initial location in the disk, for a range of particle sizes, and for both a passive disk (left panels) and an active disk (right panels). The desorption distance is calculated for particles composed of H_2O (top panels), CO_2 (middle panels) and CO (bottom panels). The particle size increases from 10^{-3} cm to 10^8 cm as indicated by the color bar. For a particle of a given initial size that entirely desorbs during $t_d = 3$ Myr, the desorption distance is the same regardless of the particle's initial location.

coupled desorption and radial drift, and can be derived straightforwardly from Equation (15). Our initial conditions are $s(t_0) = s_0$ and $r(t_0) = r_0$, where t_0 is the initial time at which we start the integration and r_0 is the initial location of the particle. We choose $t_0 = 1$ year, but our result is independent on the initial integration time as long as $t_0 \ll t_{\rm d}$. The desorption timescale $t_{\rm des}$ will then satisfy $s(t_{\rm des}) = 0$, from which we can determine the desorption distance $r_{\rm des} = r(t_{\rm des})$.

We define the final position of a grain as the disk lower than the state of the sta

We define the final position of a grain as the disk location it has reached after $t_{\rm d}=3$ Myr, or the radius at which it completely desorbs if that happens after a time shorter than 3 Myr. Figure 2 shows our results for $\rm H_2O$, $\rm CO_2$ and $\rm CO$ particles, for both a passive and an active disk. The results for the accretionally heated active disk are quantitatively similar with those of the active disk for the $\rm CO_2$ and $\rm CO$ particles, but they are different for the $\rm H_2O$ grains, since accretion heating will push the $\rm H_2O$ snowline outwards (see Section 4). Kilometer-sized bodies do not drift or desorb during the disk lifetime neither

for a passive nor for an active disk. Similarly, micron-to mm-sized particles in the passive disk do not drift and only desorb if they are located inside the static snowlines. In an active disk, however, micron-to mm-sized grains do drift significantly since they move at the same velocity as the accreting gas. For $0.5~{\rm cm} \lesssim s_0 \lesssim 700~{\rm cm}$ in a passive disk and $0.001~{\rm cm} \lesssim s_0 \lesssim 700~{\rm cm}$ in an active disk, we notice that particles of initial size s_0 desorb at a particle size dependent radius $r_{\rm des}$ regardless of their original location in the disk. In fact, the only grains that will both drift and evaporate are those that reach their fixed final location (represented by the horizontal curves in Figure 2) within the disk lifetime. We show in section 4 that this result is essential in determining the C/O ratio throughout the disk for different particle sizes.

Intuitively, this fixed $r_{\rm des}$ should be the location in the disk for which $t_{\rm drift} \sim t_{\rm des}$, given an initial particle size. We can calculate this location analytically by equating Equations (15) and (16) and solving for $r = r_{\rm des}(s)$ for a given particle size s. Figure 3 shows $r_{\rm des}$ calculated ana-

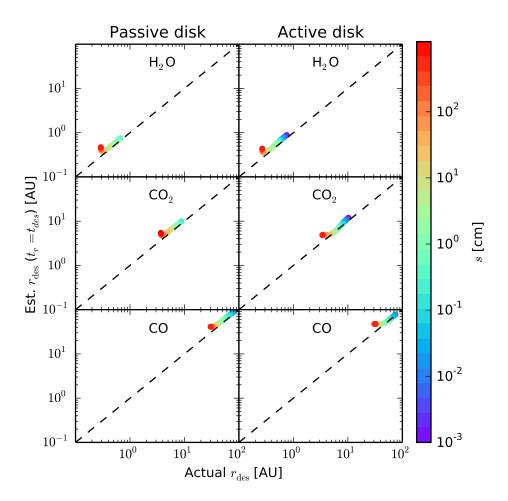


Fig. 3.— Desorption distance estimated from analytic calculations (see text) as a function of the desorption distance calculated numerically, for the range of particle sizes that desorb at a fixed distance regardless of their initial location (see Figure 2 and text). The estimate is performed for a passive disk (left panels) and an active disk (right panels). The particles are composed of H_2O (top panels), CO_2 (middle panels) and CO (bottom panels). The analytic approximation is in good agreement with the numerical result for most cases, with the exception of larger particles, $s \gtrsim 10$ cm (see text).

lytically using the prescription above as a function of the actual desorption distance calculated numerically. We display this result for the range of particle sizes that desorb at a fixed distance in a passive and an active disk (see Figure 2). We notice that the analytic approximation accurately reproduces the numerical result for most cases of interest, but it slightly deviates for particles larger than $s \gtrsim 10$ cm. For small particles with $\tau_{\rm s} \ll 1$, $t_{\rm drift}$ is a power-law in r (for our parameters, $t_{\rm drift} \propto r^{-1/14}$ for the passive disk in the Epstein drag regime), and the Equation set (18) has an explicit analytic solution (see Appendix B). Once particles are large enough so that $\tau_{\rm s} \sim 1$, $t_{\rm drift}$ has a more complicated dependence on r (see Equation 9), and the coupled drift-desorption differential equations have to be integrated numerically to obtain an accurate result.

4. C/O RATIO ESTIMATES

We now use our model and the results of Section 3 to determine the H₂O, CO₂ and CO snowline locations in disks with static chemistry that experience radial drift of solids and gas accretion onto the central star. Using this and assuming a fixed abundance relative to hydrogen for each of these volatiles, we can then estimate the C/O ratio throughout the disk as a function of the particle size. Realistic grain size distributions in disks are dominated by large grains (e.g., D'Alessio et al. 2001, Birnstiel et al. 2012). Thus for a given grain size distribution with a maximum particle size, we can pick out the appropriate minimum snowline locations from Figures 2 and 5, as we show later in this section.

Figure 4, left panels, shows the size evolution with time for H_2O particles of various initial sizes, starting at three different initial locations in a passive disk. Once solid H_2O particles begin to evaporate, they do so almost instantly for all explored particle sizes and initial locations. The right panels of Figure 4 show that the drifting grains lose most of their mass in a very narrow distance range; moreover, this distance is the same for a given initial particle size, no matter where the particle started drifting at the time t_0 when the simulation is started. Figure 4 thus demonstrates that solid particles that drift and fully

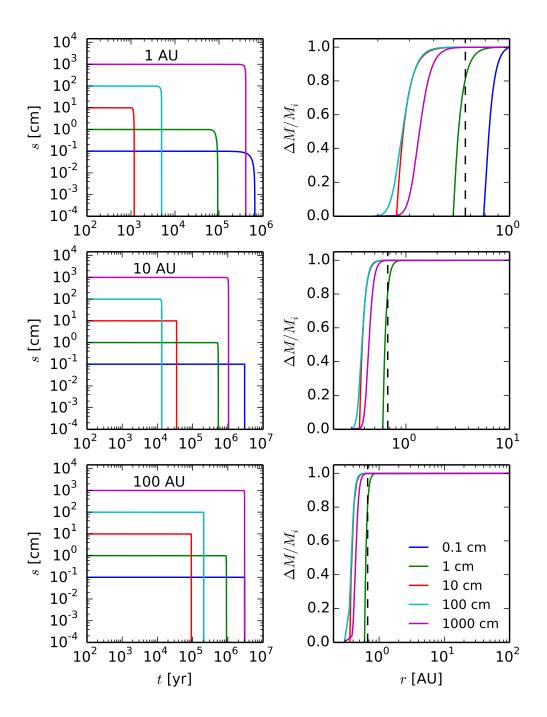


Fig. 4.— Left panels: size of desorbing H₂O particles as a function of time, for different initial particle sizes and for three initial locations in a passive disk: 1 AU (top left), 10 AU (middle left) and 100 AU (bottom left). Particles desorb almost instantaneously. Right panel: fractional mass of the desorbing particles as a function of the particle's location as it drifts, for different initial particle sizes, and at the same initial locations presented in the left panel. Particles lose most of their mass very close to the distance at which they fully desorb. The static H₂O snowline is shown for reference (dashed vertical lines).

desorb during the lifetime of the protoplanetary disk do so (1) instantaneously, and (2) at a fixed stellocentric distance, regardless of their initial location in the disk.

It follows that the H₂O, CO₂ and CO snowlines are fixed for a given initial particle size and disk model (passive

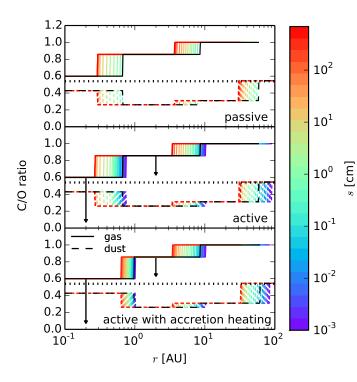


Fig. 5.— Estimated C/O ratio in gas (solid lines) and in dust (dashed lines) for a passive disk (top panel), an active disk (middle panel) and an active disk accretionally heated (bottom panel), for the range of particle sizes that desorb at a fixed distance regardless of their initial location in the disk. The particle size increases from 0.001 cm to \sim 700 cm as indicated by the color bar. The horizontal dotted line represents the stellar value of 0.54. The black lines represent the C/O ratio in gas (solid black line) and dust (dashed black line) for a static disk, with the temperature profile given by Equation (1b) for the top two panels and by Equation (8). The snowline location moves inward as the particle size increases. The curves exterior to the to static snowline represent the desorption distance for particles in the size range corresponding to the color bar, but they do not form snowlines since readsorption is not taken into account. For both active disks, the movement of desorbed CO₂ gas inside the CO₂ snowline, and of desorbed CO₂ and H₂O gas inside the H₂O snowline due to gas accretion will increase the amount of oxygen gas inside the respective snowlines and thus reduce the gas C/O ratio, with the decrease more significant interior to the H₂O snowline.

or active)⁴. The C/O ratio will then only depend on disk properties, grain size, and the abundance of H_2O , CO_2 and CO relative to the H_2 abundance in the disk midplane, and *not* directly on the disk age when only considering drift, accretion and desorption.

We use the relative number densities of C and O in their different molecular forms (H_2O , CO_2 and CO) from Table 1 of Öberg et al. (2011). Figure 5 shows the estimated C/O ratio in gas and dust as a function of semimajor axis for a passive disk, an active disk, and an active disk accretionally heated. The C/O ratio for a static disk is shown as a guideline. We note that particles desorbing outside the static snowline will not form snowlines, since our calculation of the desorption distance does not account for readsorption (Hollenbach et al. 2009).

Before discussing the quantitative aspects of this plot, it is essential to acknowledge that our estimates for the C/O ratios in the active disks ignore the movement of the desorbed ices with the accreting gas — the relative fluxes of the volatiles in gaseous and solid form will affect the relative abundance of C and O in gas and dust throughout the disk. As demonstrated in Figure 4, this will not affect the snowline locations for particles of a given size, but will change the shape of the C/O curves in between the various snowlines. Specifically, the gas C/O ratios may be significantly lower inside the $\rm H_2O$ and $\rm CO_2$ snowlines for the active disks, depending on the gas accretion rate, due to the additional oxygen contained by $\rm H_2O$ and $\rm CO_2$ vapor that moves together with the accreting gas and crosses their respective snowlines.

We thus present this result for the C/O ratio primarily as a visual comparison with previous work (Öberg et al. 2011) and note that our estimates for the C/O ratio in the active disks are not quantitatively accurate at all disk locations. Future work will address this issue.

For the passive disk, only grains larger than ~ 0.5 cm drift, desorb and thus move the snowline compared to the static disk. In contrast, even ~micron-sized grains drift and desorb for the active disk, since they flow towards the host star together with the accreting gas. For the same particle size, the snowline locations are slightly closer to the central star in the active disk, due to the fact that the accreting gas adds an additional component to the drift velocity of the solids (cf. Equation 12). The addition of accretional heating in the steady-state active disk moves the H₂O snowline outwards. This is due to the fact that accretional heating dominates in the inner disk, where high temperatures cause the grains to evaporate further away from the star. Once $r \gtrsim 1-2$ AU, stellar irradiation dominates the thermal evolution of the disk, and therefore the CO₂ and CO snowlines locations are the same as in the active disk.

Perhaps the most interesting feature is the fact that the snowlines are pushed inwards as the grain size increases. While the plot only shows the snowlines and C/O ratio for particle sizes up to ~ 7 m, we have found that bodies larger than ~ 7 m evaporate at the same location as the meter-sized planetesimals. This is due to the fact that large bodies lose their mass as they desorb until they reach the same size as the smaller, meter-sized particles, thus eventually following the same evolutionary track as the meter-sized bodies and evaporating at the same location. However, the contribution of kilometer-sized bodies to the snowline location is modest, since they only drift if they are located very close to the snowline. Thus the innermost snowlines (depicted in red in Figure 5) set the limit on how close in the H₂O, CO₂ and CO snowlines can be pushed due to radial drift and gas accretion on to the host star.

For our choice of parameters, the minimum snow-line radii are: $r_{\rm H_2O}\approx 0.3$ AU for the passive disk, $r_{\rm H_2O}\approx 0.26$ AU for the active disk and $r_{\rm H_2O}\approx 0.63$ AU for the active disk accretionally heated; $r_{\rm CO_2}\approx 3.7$ AU for the passive disk, $r_{\rm CO_2}\approx 3.4$ AU for both active disks; $r_{\rm CO}\approx 30$ AU for the passive and both active disks. For comparison, $r_{\rm H_2O}\approx 0.67$ AU, $r_{\rm CO_2}\approx 8.6$ AU and $r_{\rm CO}\approx 59$ AU for the static disk. Radial drift and gas accretion therefore push the snowline locations by up to $\sim\!60$ % for H₂O and CO₂, and by up to $\sim\!50$ % for CO. We note that the H₂O snowline in all disks is significantly

 $^{^4}$ Both of these conclusions remain valid for an active disk and for particles composed of CO_2 or CO.

closer to the host star compared with Solar system models, which place the H_2O snowline between ~ 2.7 to ~ 3.1 AU (Hayashi 1981, Podolak & Zucker 2004, Martin & Livio 2012). This is partially because we choose a colder disk model, as well as the fact that gas accretion rates decrease over time, moving the snowline location outwards (see also Garaud & Lin 2007 and Section 5.2). Observations of the CO snowline in TW Hya (Qi et al. 2013) have found its location at a disk midplane temperature of 17 K (at 30 AU for the TW Hya specific temperature profile). The inferred desorption temperature corresponds to the CO desorption temperature in a static disk, or to desorption from very small grains in an active disk, i.e. from grains that are too small to drift substantially. This suggests that the outer TW Hya disk is dominated by small grains, since larger particles would push the snowline location inwards, and therefore to higher desorption temperatures. This may seem contradictory to observations of grain growth in disks in general and in TW Hya in particular (Wilner et al. 2000). However, recent observations have revealed that grain growth is concentrated to the inner disk (Pérez et al. 2012) and outer disk snowlines may therefore be close to the ones expected in a static disk.

5. DISCUSSION

5.1. Generality of Results: Dependence on Disk Parameters

In this section we investigate how variations in our fiducial parameters, the total disk mass, disk age, and disk structure, affect the calculated snowline locations and the C/O ratio. All previous results assumed a disk lifetime $t_{\rm d}=3$ Myr, the typical disk life time and the expected time scale for giant planets to accrete their gaseous atmopsheres (e.g., Pollack et al. 1996, Piso & Youdin 2014). Some gas accretion may occur at earlier times, however, before the core is fully formed (e.g., Rafikov 2006). Recent models such as aerodynamic pebble accretion (Lambrechts & Johansen 2012) suggest that rapid core growth on timescales of 10⁵ years is possible. The composition of giant planet atmospheres, and specifically their C/O ratio, can thus depend on the abundance of H_2O , CO_2 and CO in gas at earlier times than t_d in the disk evolution.

Figure 6 shows the particle desorption or final distance as a function of a particle's initial location in the disk, for ice particles of initial sizes of 10 cm and 1 m, composed of either H₂O, CO₂ or CO. These sizes are important since radial drift timescales are shortest for particles within this size range (see Figure 1) — these are the particles whose drift and desorption evolution should be most strongly affected by variations in disk conditions. We stop the simulations after 10⁴ yr, 10⁵ yr, 1 Myr and $t_{\rm d} = 3$ Myr, respectively. The most important result of these plots is that particles of a given size always desorb at the same disk radii, the 3 Myr snowline, regardless of simulation stopping time. Particles that start at large stellocentric distances do not desorb within the shorter timeframes, e.g. 10^4 or 10^5 years, but they do evaporate at a fixed radius if their initial location is closer to the host star. While the amount of material that moves through the disk changes with time, the radius at which particles desorb and the snowline locations are thus independent of the time elapsed, and our results are valid throughout the time evolution of the protoplanetary disk.

We choose as a fiducial model a total disk mass $M=0.1M_{\odot}$. Observationally, disk masses span at least an order of magnitude around Solar type stars (Andrews et al. 2013). We thus explore the effect of disk mass on the location of snowlines. Figure 7 shows the desorption or final distance as a function on the initial location of a $\rm H_2O$ particle with initial size of 1 m, for two total disk masses: $M=0.1M_{\odot}$, our fiducial model, and $M=0.01M_{\odot}$. The simulations are stopped after the same timeframes as those in Figure 6. The location of the $\rm H_2O$ snowline is the same for both disks (the same holds true for the $\rm CO_2$ and $\rm CO$ snowlines). The C/O ratio is thus insensitive to the choice of M.

We also apply our active disk model to a transition disk, i.e. a protoplanetary disk with an inner cavity significantly depleted of gas. We choose a disk with an inner gap of radius $r_0 = 4$ ÅU, consistent with observations of TW Hya (Zhang et al. 2013), and with the gas surface density in the gap reduced by a factor of 1000. Figure 8 shows the desorption or final distance for a H₂O particle of initial size of 1 m, with the simulation stopped at the same timescales as in Figures 6 and 7. Particles that start at an initial distance interior to the gap drift towards the original snowline, while grains located exterior to the gap stop shortly after crossing the gap edge, due to the decrease in gas pressure inside the cavity, thus forming a snowline at ~ 3.8 AU. This is qualitatively consistent with the observations of Zhang et al. (2013), which show that the H₂O snowline is pushed outwards in a transition disk compared to a full disk. Our model framework is thus generally valid for more complicated disk structures as well.

5.2. Model Extensions

Our goals in this paper were (1) to gain a detailed qualitative and quantitative understanding of the effect of radial drift and gas accretion onto the central star on snowline locations and the C/O ratio in disks, and (2) to obtain a limit on how close in the snowlines can be pushed due to drift and gas accretion. We have thus used a simplified model and out of necessity neglected potentially significant dynamical and chemical processes. In what follows, we discuss these limitations and their effects. We note that our future work will address some of these issues.

We summarize in Table 1 the potential physical and chemical processes occurring in disks and their effect on snowline locations compared to a static disk. For the sake of completeness, Table 1 also includes the processes addressed in this paper, i.e. radial drift and gas accretion. The neglected effects are discussed in more detail below.

1. Particle growth. While our model assumes a range of particle sizes, each size is considered fixed for a given grain throughout its drift and evolution. However, grain growth has been observed in protoplanetary disks (e.g., Ricci et al. 2010, Pérez et al. 2012), as well as theoretically constrained (e.g., Birnstiel et al. 2010, Birnstiel et al. 2012). In Section 4 we have shown that larger grains move the snowline locations closer in, but those locations

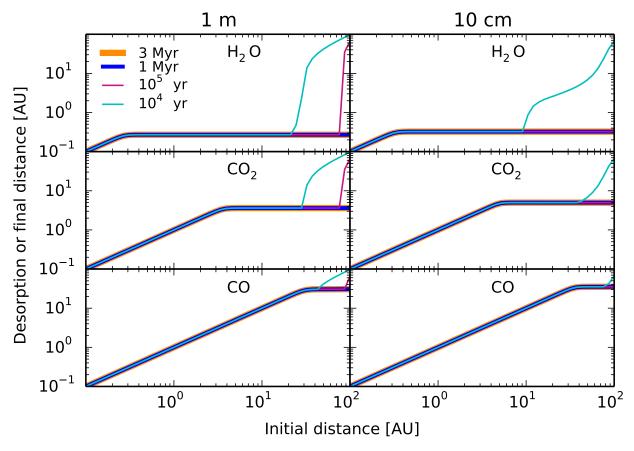


Fig. 6.— Desorption / final distance as a function of initial position in the disk for particles of initial size $s_0 = 1$ m (left panels) and $s_0 = 10$ cm (right panels), for grains composed of H₂O (top panels), CO₂ (middle panels) and CO (bottom panels). The evolution is shown at four representative timescales: 10^4 yr (cyan curve), 10^5 yr (purple curve), 1 Myr (blue curve), and 3 Myr, the disk lifetime (orange curve). For a given particle size, the desorption distance, and hence the H₂O, CO₂ and CO snowlines, have the same location regardless of the time at which the simulation is stopped.

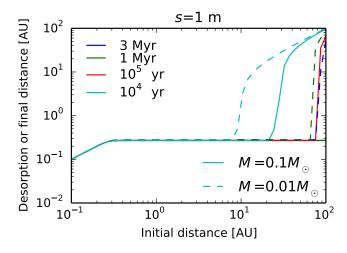


Fig. 7.— Desorption / final distance as a function of initial position in the disk for $\rm H_2O$ particles of initial size of 1 m, for total disk masses $M=0.1M_{\odot}$ (solid lines) and $M=0.01M_{\odot}$ (dashed lines). The timescales at which we stop the simulations are 10^4 yr (cyan curve), 10^5 yr (red curve), 1 Myr (green curve) and 3 Myr (blue curve). A lower disk mass does not change the snowline location.

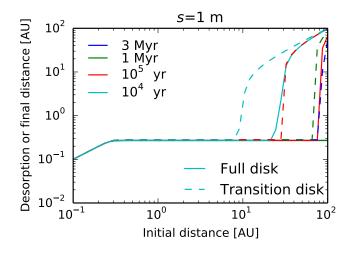


FIG. 8.— Desorption / final distance as a function of initial position in the disk for $\rm H_2O$ particles of initial size of 1 m, for our fiducial disk (solid lines) and for a transition disk with an inner cavity at $r_0 = 4$ AU (dashed lines). The timescales of the simulations and their color code are the same as in Figure 7. Particles that start inside the cavity drift towards the original snowline, while particles that start outside the gap stop shortly after crossing the gap edge, due to being trapped in a pressure maximum.

remain fixed above a certain particle size. Par-

TABLE 1
THE EFFECTS OF DYNAMICAL AND CHEMICAL PROCESSES ON SNOWLINE SHAPES AND LOCATIONS

Process	Effect
Radial drift	← ^a
Gas accretion	←
Particle growth	$\rightarrow \leftarrow$
Turbulent diffusion	$\rightarrow \leftarrow$
Particle fragmentation	$\rightarrow \leftarrow$
Grain morphology	\rightarrow
Particle composition	$\rightarrow \leftarrow$
Disk gaps and holes	\rightarrow
Accretion rate evolution	$\rightarrow \leftarrow$
Stellar luminosity evolution	←
Non-static chemistry	$\rightarrow \leftarrow$

^aThe arrows signify how a process affects the snowline: \leftarrow means that the snowline is pushed closer to the host star compared to the static snowline, \rightarrow means that the snowline is pushed further from the host star compared to the static snowline. The presence of both arrows means that the process may have both effects on the snowline location.

ticle growth will thus initially push the snowlines inwards. This is consistent with particle growth models, which predict a maximum particle size often around or below the particle sizes that drift the fastest (Birnstiel et al. 2012). As the largest grains contain most of the solid mass, grain growth models should produce snowlines corresponding to our snowline location estimates for the largest grains in the particle size distribution. However, once the solids grow larger than km-sized and form planetesimals, they are no longer affected by drift or desorption, and the snowline reduces to that of a static disk. It follows that grain growth will eventually push the snowline location outwards.

- 2. Turbulent diffusion. The radial drift model presented in Section 2.2 only considers a laminar flow and thus ignores turbulence. However, the disk gas also experiences turbulent diffusion (e.g., Birnstiel et al. 2012, Ali-Dib et al. 2014). Turbulence causes eddies and vertical mixing, which are likely to reduce the radial drift velocity of the solids. Additionally, the flow of H₂O, CO₂ and CO vapor will diffuse radially. Back-diffusion across the snowline will change the shape of the snowline, as well as the C/O ratio in gas and dust both inside and outside of the snowline, due to the reduction of gas-phase volatile abundance interior to the snowline.
- 3. Particle fragmentation. Frequent particle collisions in disks cause them to fragment (e.g., Birnstiel et al. 2012). The fragmentation of meterto km-sized particles will move the snowlines outwards, as smaller particles desorb faster and further out from the host star (cf. Figures 2 and 5). Large boulders, which neither drift nor desorb, may become e.g. meter-sized due to collisions and subsequent fragmentation, which will cause them to drift significantly before desorbing, pushing the snowlines inwards. Thus fragmentation can move the snowline locations in either radial direction—

- specifically, fragmentation leads to a certain grain size distribution, and the largest particles in this size distribution are the ones that determine the position of the snowline.
- 4. Grain morphology. Our model assumes that the ice particles are perfect, homogeneous spheres. However, this is not a very good approximation, since grain growth can be fractal rather than compact (Zsom et al. 2010, Okuzumi et al. 2012, Krijt et al. 2015). The inhomogeneity due to cracks in the grain structure will cause the particles to desorb faster. They will therefore drift less before evaporating and will move the snowlines outwards.
- 5. Particle composition. The ice particles in our model are assumed to be fully made of either H₂O, CO₂ or CO. More realistically, grains may have a layered structure, such as an interior composed of non-volatile materials (e.g., sillicates) covered by an icy layer. The ice thus only constitutes a fraction of the total particle mass, which accelerates its desorption and pushes the snowlines outwards. The grains may also be composed of a mixture of H₂O, CO₂ and CO ices, which will increase the binding energies of the more volatiles species, moving the snowlines inwards.
- 6. Disk gaps and holes. The snowline locations will be different for transition disks, which have inner cavities significantly depleted of gas (e.g., Espaillat et al. 2012), or pre-transitional disks, which have a gap between an inner and outer full disk (e.g., Kraus et al. 2011). The decrease in gas pressure in these gaps or holes will reduce the particles' drift velocity close to the gap edge, thus slowing them down and pushing the snowline outwards.
- 7. Accretion rate evolution. Our steady-state active disk model assumes a constant mass accretion rate M. However, M decreases over time, which lowers the accretional component of the disk temperature (Equation 7), thus pushing the snowline location inwards if the disk is optically thick (Garaud & Lin 2007). Once \dot{M} reaches low enough values for the snowline to become optically thin, the snowline location moves outwards (Garaud & Lin 2007). Our choice of $\dot{M}=10^{-8}M_{\odot}~{\rm yr}^{-1}$ roughly corresponds to the mass accretion rate during the quasi-static accretion phase of the disk evolution predicted by Garaud & Lin (2007). This is the timescale on which giant planets accrete most of their gaseous envelope; thus the implications of our results for the atmospheric composition of gas giants are robust.
- 8. Stellar luminosity evolution. As the host star contracts during its pre-main sequence phase, its luminosity decreases, which reduces the disk temperature and pushes the snowline locations inwards. Kennedy et al. (2006) found that the snowline may move inward by a factor of $\sim 15-20$ due to the stellar contraction.

9. Time dependent chemistry. As the goal of this paper was to explore only the dynamical effects on snowline locations and the C/O ratio in disks, we have assumed a simple, static chemical model. In reality, the chemistry in most of the disk is expected to be time-dependent. In the inner disk, chemistry approaches equilibrium due to intense sources of ionizing radiation (e.g., Ilgner et al. 2004), while in the outer disk high energy radiation and cosmic rays are the key drivers of chemistry, which is no longer in equilibrium (e.g., van Dishoeck 2006). A multitude of chemical evolution models have been developed (see references in Henning & Semenov 2013), many of which contain tens or hundreds of chemical reactions. Due to the complexity of these chemical models, most of them are decoupled from disk dynamics. The effect of disk chemistry on snowline locations, shape, time evolution, or the C/O ratio is therefore difficult to estimate.

6. SUMMARY

We study the effect of radial drift of solids and viscous gas accretion onto the central star on the H₂O, CO₂ and CO snowline locations and the C/O ratio in a protoplanetary disk, assuming static chemistry. We develop a simplified model to describe the coupled driftdesorption process and determine the time evolution of particles of different sizes throughout the disk. We assume that the solid particles are perfect, homogeneous spheres, fully composed of either H₂O, CO₂ or CO. We apply our model to a passive disk, an active disk with a passive temperature profile (hereafter active disk), and a steady-state active disk that also takes into account stellar irradiation. We determine the desorption or final location of drifting particles after a time equal to the disk lifetime, and use this result to set an inner limit for the location of the H₂O, CO₂ and CO snowlines. Our results can be summarized as follows:

- 1. Radial drift and gas accretion affect desorption and move the snowline locations compared to a static disk for particles with sizes $\sim\!0.5$ cm $\lesssim s \lesssim 7$ m for a passive disk and $\sim\!0.001$ cm $\lesssim s \lesssim 7$ m for an active disk.
- 2. Particles with sizes in the above range desorb almost instantaneously once desorption has begun, and at a fixed location in the disk that only depends on the particle size and the gas accretion rate. Thus for each particle size there is a fixed and uniquely determined H₂O, CO₂ or CO snowline.
- 3. The results of the numerical simulation are in agreement with the analytic solution of the drift-desorption system of differential equations if the stopping time $\tau_{\rm s} \ll 1$. We present an explicit analytic solution for the desorption distance in this regime.

- 4. The snowline locations move inwards as the particle size increases; the innermost snowline is set by particles with initial size $s \sim 7$ m in our model. Gas accretion causes even micron-sized particles to drift, desorb and move the snowline location compared to a static disk. A steady-state disk that includes accretion heating moves the H₂O snowline outwards compared to an active disk, but has no effect on the CO₂ and CO snowline locations, for our particular choice of mass accretion rate \dot{M} and midplane opacity κ .
- 5. Since realistic grain size distributions are dominated in mass by the largest particles, the H₂O, CO₂ and CO snowlines are those created by the largest drifting particles in our model. This corresponds to the innermost snowlines that we determine. Our model thus sets a limit on how close to the central star the snowlines can be pushed by radial drift and gas accretion.
- 6. For our fiducial model, the innermost H₂O, CO₂ and CO snowlines are located at 0.3 AU, 3.7 AU and 30 AU for a passive disk, 0.26 AU, 3.4 AU and 30 AU for an active disk, and 0.63 AU, 3.4 AU and 30 AU for a steady-state active disk. Compared to a static disk, radial drift and gas accretion move the snowlines by up to 60 % for H₂O and CO₂, and by up to 50 % for CO.
- 7. Our C/O estimates find that the C/O ratio may be enhanced compared to the stellar value throughout most of the disk, with the C/O ratio reaching its maximum value between the CO₂ and CO snowlines. This is consistent with possible detections of superstellar C/O ratios in some exoplanet atmospheres. We note, however, that our results for the C/O ratio do not take into account the radial movement of the desorbed ices with the accreting gas in the active disks.
- 8. The snowline locations are independent of the time at which we stop our simulation and of the total disk mass, as long as the disk midplane remains optically thick. Our results are thus valid throughout the evolution of the gas disk, not only after the disk has dissipated, which has implications on the composition of nascent giant planets.

Our model does not address additional effects, such as gas diffusion, grain composition and morphology, or complex time-dependent chemical processes. Future work will address some of these dynamical and chemical processes, with the goal of obtaining more realistic results for the snowline locations, shapes and time evolution, and the resulting effect on the C/O ratio.

APPENDIX

STEADY-STATE ACTIVE DISK SOLUTION

Following Shakura & Sunyaev (1973) and Armitage (2010), the steady-state solution for a geometrically thin, optically thick actively accreting disk with an α -prescription for viscosity is governed by the following set of equations:

$$\nu = \alpha c H \tag{A1a}$$

$$c^2 = \frac{k_{\rm B}T_{\rm act}}{\mu m_{\rm p}} \tag{A1b}$$

$$\rho = \frac{1}{\sqrt{2\pi}} \frac{\Sigma}{H}$$

$$H = \frac{c}{\Omega_k}$$
(A1c)

$$H = \frac{c}{\Omega_k} \tag{A1d}$$

$$T_{\rm act}^4 = \frac{3}{4}\tau T_{\rm surf}^4 \tag{A1e}$$

$$\tau = \frac{1}{2} \Sigma \kappa \tag{A1f}$$

$$\nu\Sigma = \frac{\dot{M}}{3\pi} \tag{A1g}$$

$$\sigma T_{\rm surf}^4 = \frac{9}{8} \nu \Sigma \Omega_{\rm k}^2 \tag{A1h}$$

$$\kappa = \kappa_0 T_{\text{act}}^2,$$
(A1i)

where T_{surf} is the surface temperature of the disk and the other quantities are defined in the main text. This is a system of nine equations with nine unknowns $(\nu, c, H, T_{\rm act}, \rho, \Sigma, \tau, T_{\rm surf}, \kappa)$ that can be solved numerically once α and κ_0 are specified.

DESORPTION DISTANCE ANALYTIC SOLUTION

For a particle of size s that desorbs and satisfies $\tau_{\rm s} \ll 1$ ($\tau_{\rm s}$ is the dimensionless stopping time, defined in Section 2.2), we can derive an explicit analytic solution for the particle's desorption distance in a passive disk. For $\tau_{\rm s} \ll 1$, a particle is in the Epstein drag regime (see Equation 9) and its drift velocity \dot{r} (Equation 10) can be approximated as

$$\dot{r} \approx -2\eta \Omega_{\rm k} r \tau_{\rm s}.$$
 (B1)

By using Equations (15) and (16) and setting $t_{\text{drift}} = t_{\text{des}}$, we can express a particle's desorption distance as

$$r_{\text{des}} = \left(\frac{d}{qC} \mathcal{W}\left[\frac{(B/A)^{-q/d}qC}{d}\right]\right)^{\frac{1}{q}},\tag{B2}$$

where W is the Lambert-W function, q = 3/7 is the power-law coefficient in Equation (1b), $d = -\frac{1}{2} + p - q$ with p = 1the power-law coefficient in Equation (1a), and

$$A = \frac{\rho_0}{\rho_0} \frac{r_0^2}{sc_0} r_0^d \tag{B3a}$$

$$A = \frac{\rho_0}{\rho_s} \frac{r_0^2}{sc_0} r_0^d$$

$$B = \frac{\rho_s s}{3\mu_x N_x \nu_x}$$
(B3a)

$$C = \frac{E_{\rm x}}{T_0} r_0^{-q},$$
 (B3c)

(B3d)

where $r_0 = 1$ AU, $\rho_0 = \rho(r_0)$ and $c_0 = c(r_0)$.

REFERENCES

Ali-Dib, M., Mousis, O., Petit, J.-M., & Lunine, J. I. 2014, ApJ,

785, 125 Andrews, S. M., Rosenfeld, K. A., Kraus, A. L., & Wilner, D. J.

2013, ApJ, 771, 129

Andrews, S. M., Wilner, D. J., Hughes, A. M., Qi, C., & Dullemond, C. P. 2010, ApJ, 723, 1241

Armitage, P. J. 2010, Astrophysics of Planet Formation Bell, K. R. & Lin, D. N. C. 1994, ApJ, 427, 987

Birnstiel, T., Dullemond, C. P., & Brauer, F. 2010, A&A, 513,

A79 Birnstiel, T., Klahr, H., & Ercolano, B. 2012, A&A, 539, A148 Chiang, E. & Youdin, A. N. 2010, Annual Review of Earth and Planetary Sciences, 38, 493 D'Alessio, P., Calvet, N., & Hartmann, L. 2001, ApJ, 553, 321

Espaillat, C., Ingleby, L., Hernández, J., Furlan, E., D'Alessio, P., Calvet, N., Andrews, S., Muzerolle, J., Qi, C., & Wilner, D. 2012, ApJ, 747, 103

Frank, J., King, A., & Raine, D. J. 2002, Accretion Power in Astrophysics: Third Edition

Garaud, P. & Lin, D. N. C. 2007, ApJ, 654, 606 Hartmann, L., Calvet, N., Gullbring, E., & D'Alessio, P. 1998, ApJ, 495, 385 Hayashi, C. 1981, Progress of Theoretical Physics Supplement,

70, 35

Henning, T. & Semenov, D. 2013, Chemical Reviews, 113, 9016

Hollenbach, D., Kaufman, M. J., Bergin, E. A., & Melnick, G. J. 2009, ApJ, 690, 1497

Hughes, A. L. H. & Armitage, P. J. 2010, ApJ, 719, 1633

Ilgner, M., Henning, T., Markwick, A. J., & Millar, T. J. 2004,

A&A, 415, 643 Kennedy, G. M., Kenyon, S. J., & Bromley, B. C. 2006, ApJ, 650,

Kraus, A. L., Ireland, M. J., Martinache, F., & Hillenbrand, L. A. 2011, ApJ, 731, 8
Krijt, S., Ormel, C. W., Dominik, C., & Tielens, A. G. G. M. 2015, A&A, 574, A83

Lambrechts, M. & Johansen, A. 2012, A&A, 544, A32 Madhusudhan, N., Amin, M. A., & Kennedy, G. M. 2014, ApJ,

Madhusudhan, N., Harrington, J., Stevenson, K. B., Nymeyer, S., Campo, C. J., Wheatley, P. J., Deming, D., Blecic, J., Hardy, R. A., Lust, N. B., Anderson, D. R., Collier-Cameron, A., Britt, C. B. T., Bowman, W. C., Hebb, L., Hellier, C., Maxted, P. F. L., Pollacco, D., & West, R. G. 2011, Nature, 469, 64 Martin, R. G. & Livio, M. 2012, MNRAS, 425, L6 Mordasini, C., Klahr, H., Alibert, Y., Miller, N., & Henning, T. 2014, A&A, 566, A141

2014, A&A, 566, A141

Öberg, K. I., Murray-Clay, R., & Bergin, E. A. 2011, ApJ, 743, L16

Okuzumi, S., Tanaka, H., Kobayashi, H., & Wada, K. 2012, ApJ, 752, 106

752, 106
Pérez, L. M., Carpenter, J. M., Chandler, C. J., Isella, A.,
Andrews, S. M., Ricci, L., Calvet, N., Corder, S. A., Deller,
A. T., Dullemond, C. P., Greaves, J. S., Harris, R. J., Henning,
T., Kwon, W., Lazio, J., Linz, H., Mundy, L. G., Sargent, A. I.,
Storm, S., Testi, L., & Wilner, D. J. 2012, ApJ, 760, L17
Piso, A.-M. A. & Youdin, A. N. 2014, ApJ, 786, 21
Podolak, M. & Zucker, S. 2004, Meteoritics and Planetary
Science, 39, 1859
Pollack, J. B., Hubickyj, O., Bodenheimer, P., Lissauer, J. J.,
Podolak, M., & Greenzweig, Y. 1996, Icarus, 124, 62

Qi, C., D'Alessio, P., Öberg, K. I., Wilner, D. J., Hughes, A. M., Andrews, S. M., & Ayala, S. 2011, ApJ, 740, 84

Qi, C., Öberg, K. I., Wilner, D. J., D'Alessio, P., Bergin, E., Andrews, S. M., Blake, G. A., Hogerheijde, M. R., & van Dishoeck, E. F. 2013, Science, 341, 630 Rafikov, R. R. 2006, ApJ, 648, 666 Ricci, L., Testi, L., Natta, A., & Brooks, K. J. 2010, A&A, 521,

Shakura, N. I. & Sunyaev, R. A. 1973, A&A, 24, 337 Thiabaud, A., Marboeuf, U., Alibert, Y., Leya, I., & Mezger, K. 2015, A&A, 574, A138 van Dishoeck, E. F. 2006, Proceedings of the National Academy

Wall Dishoeck, E. F. 2006, Proceedings of the National Academy of Science, 103, 12249
Weidenschilling, S. J. 1977, MNRAS, 180, 57
Wilner, D. J., Ho, P. T. P., Kastner, J. H., & Rodríguez, L. F. 2000, ApJ, 534, L101
Zhang, K., Pontoppidan, K. M., Salyk, C., & Blake, G. A. 2013, ApJ, 766, 82

Zsom, A., Ormel, C. W., Güttler, C., Blum, J., & Dullemond, C. P. 2010, A&A, 513, A57