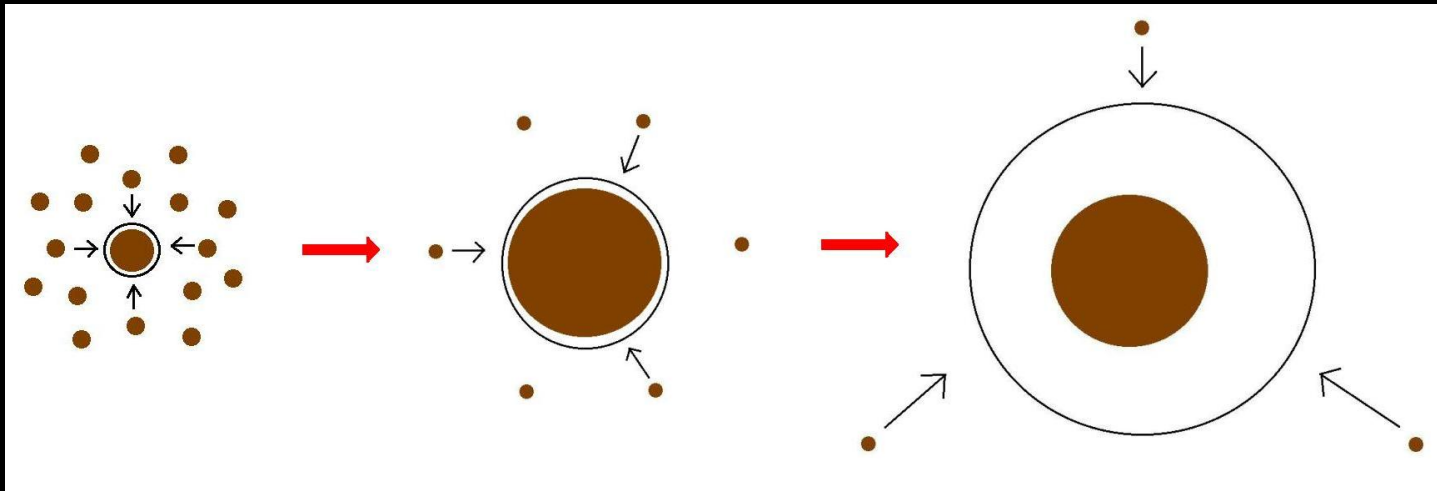


# Minimum Core Masses for Giant Planet Formation

Ana-Maria Piso<sup>1</sup>

Andrew Youdin<sup>2</sup>, Ruth Murray-Clay<sup>1,3</sup>



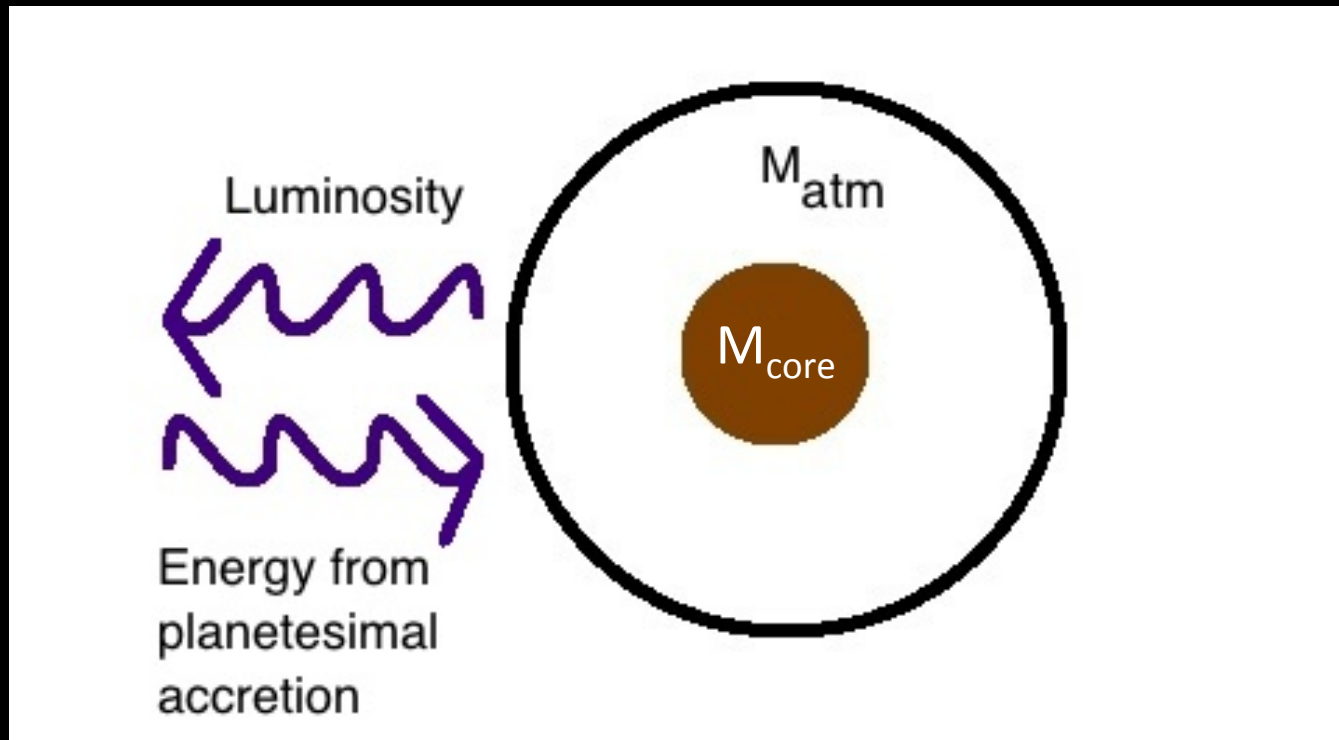
<sup>1</sup>Harvard-Smithsonian Center for Astrophysics

<sup>2</sup>Steward Observatory, University of Arizona

<sup>3</sup>University of California Santa Barbara

# Core Accretion at high planetesimal accretion rates yields steady state

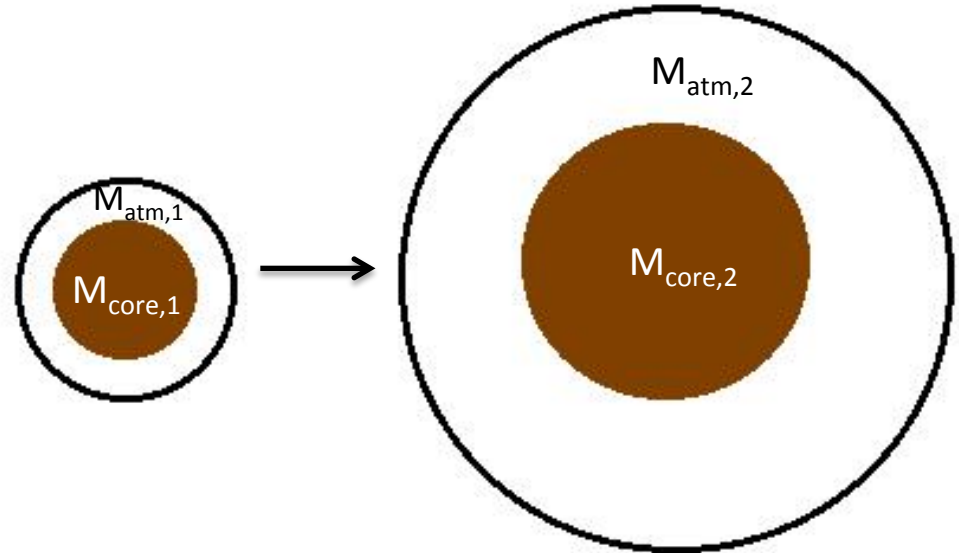
=>  $M_{\text{atm}}$  is a function of  $M_{\text{core}}$



# Planetesimal accretion

ONE  $M_{\text{atm}}$  for each  
 $M_{\text{core}}$

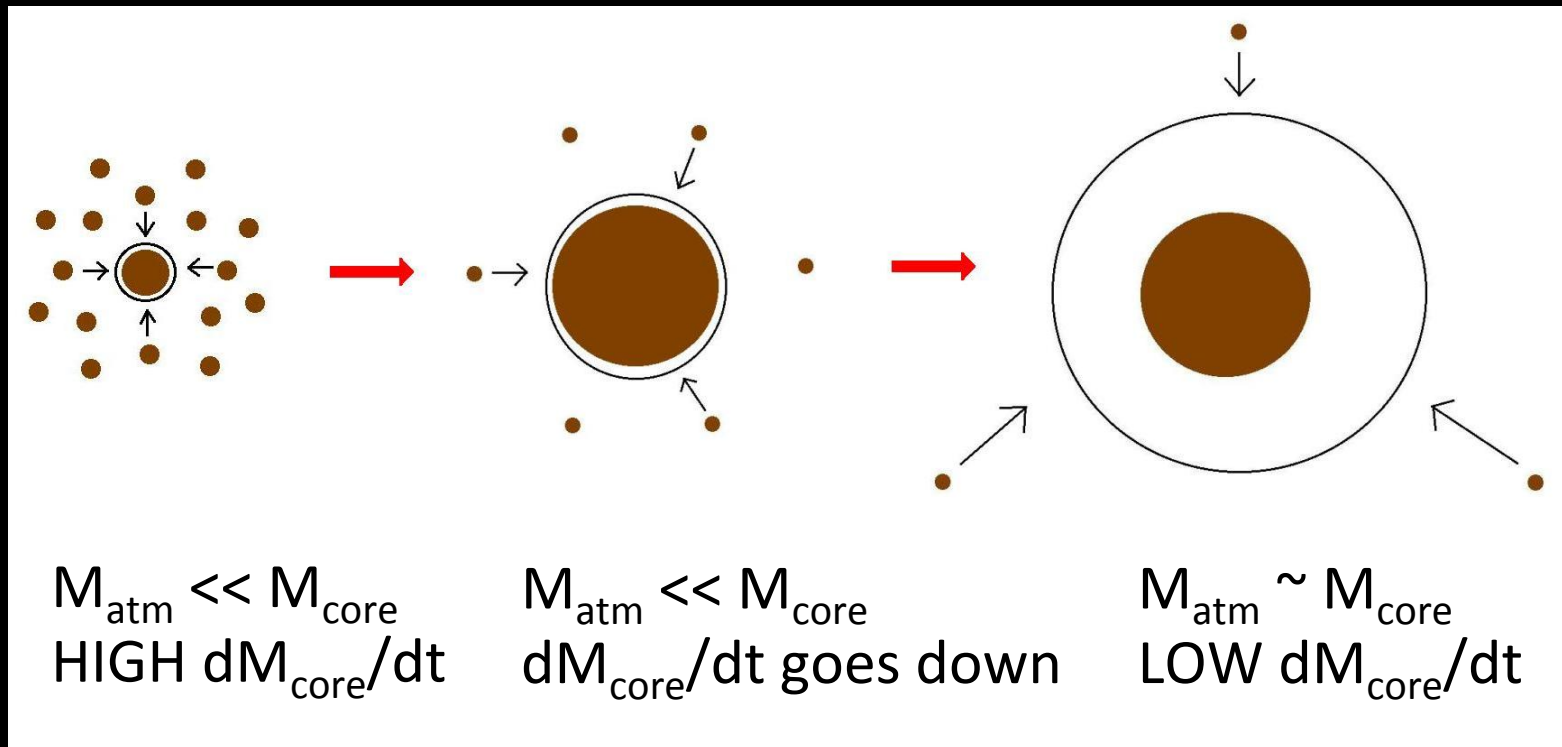
=> ONE core mass for  
which  $M_{\text{atm}} \sim M_{\text{core}} =$   
“critical core mass”



larger cores hold fractionally  
larger atmospheres

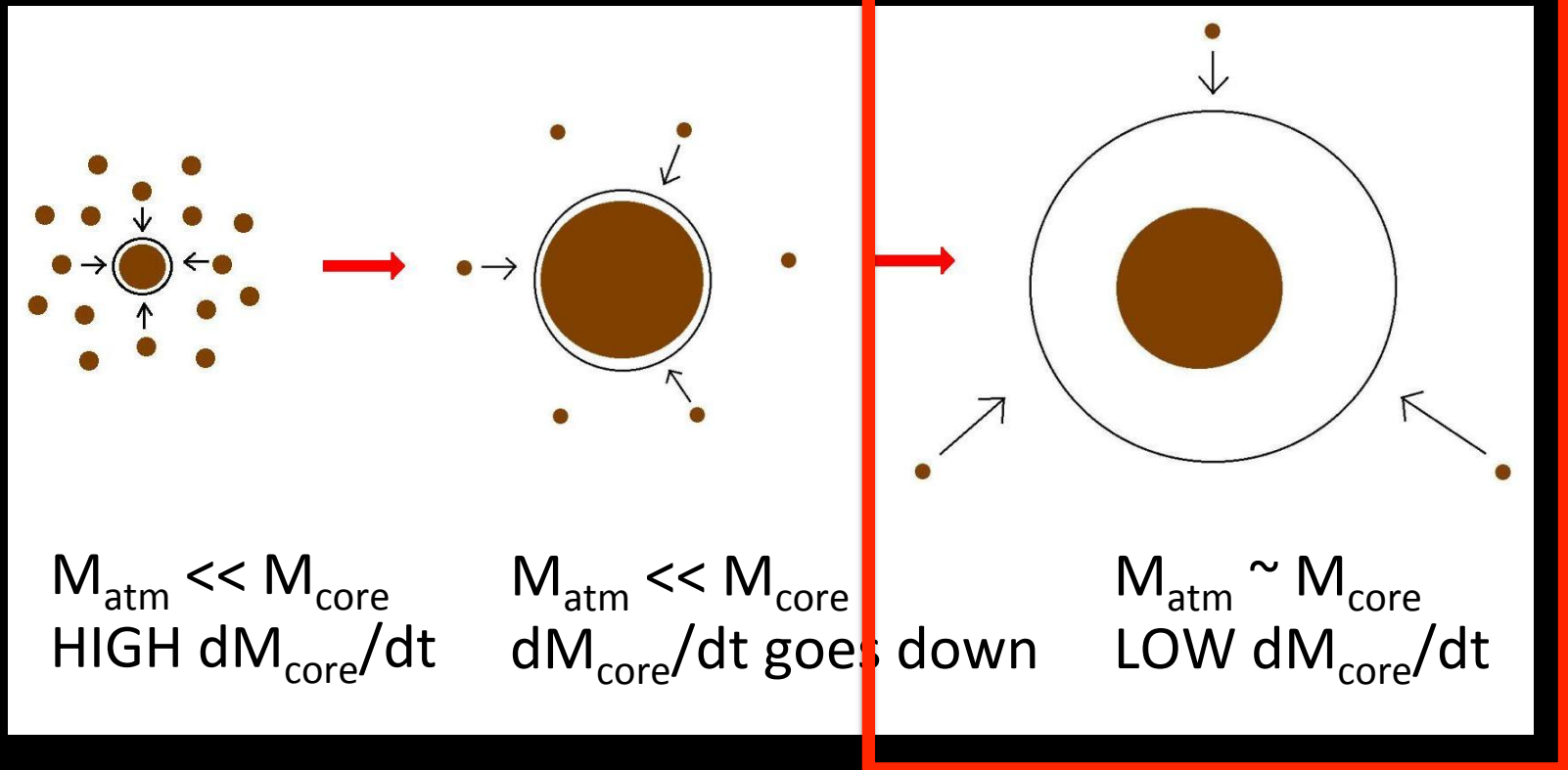
# Planetesimal accretion is not constant at a given location throughout disk life

- e.g., Pollack+96, Ikoma+00



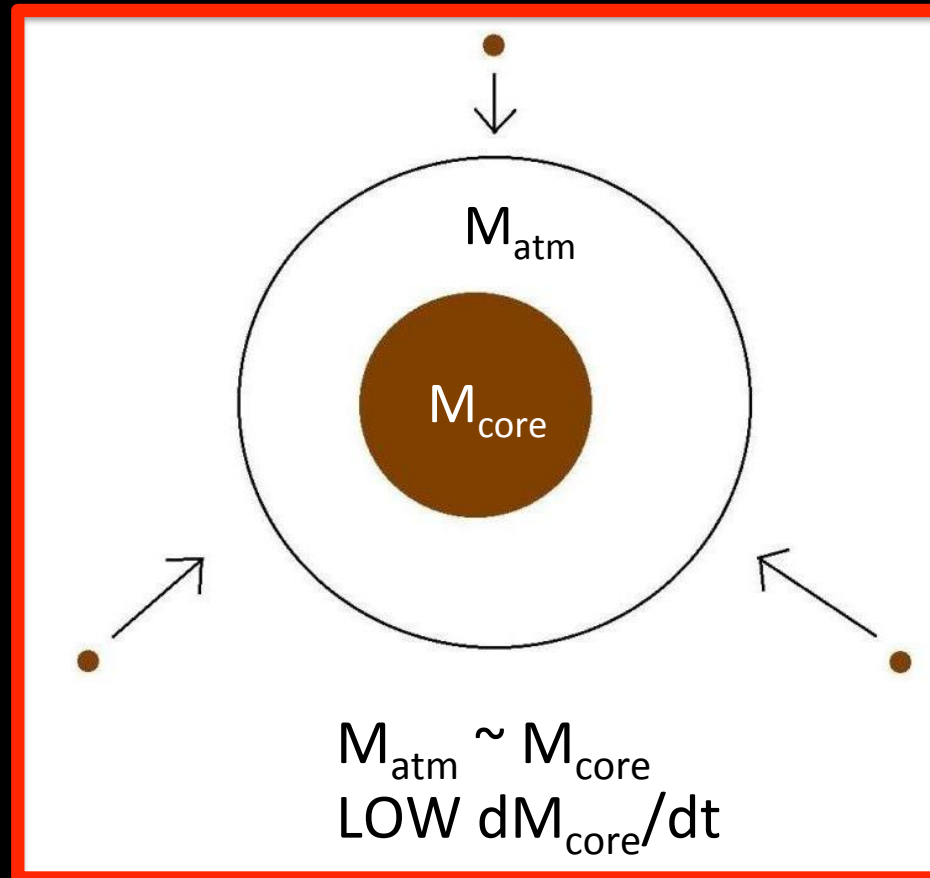
# Planetesimal accretion is not constant at a given location throughout disk life

- e.g., Pollack+96, Ikoma+00



# Low planetesimal accretion regime

⇒ Atmospheric evolution dominated by  
**Kelvin-Helmholtz** contraction



# Kelvin-Helmholtz contraction

$M_{\text{atm}}$  is a function of **time**

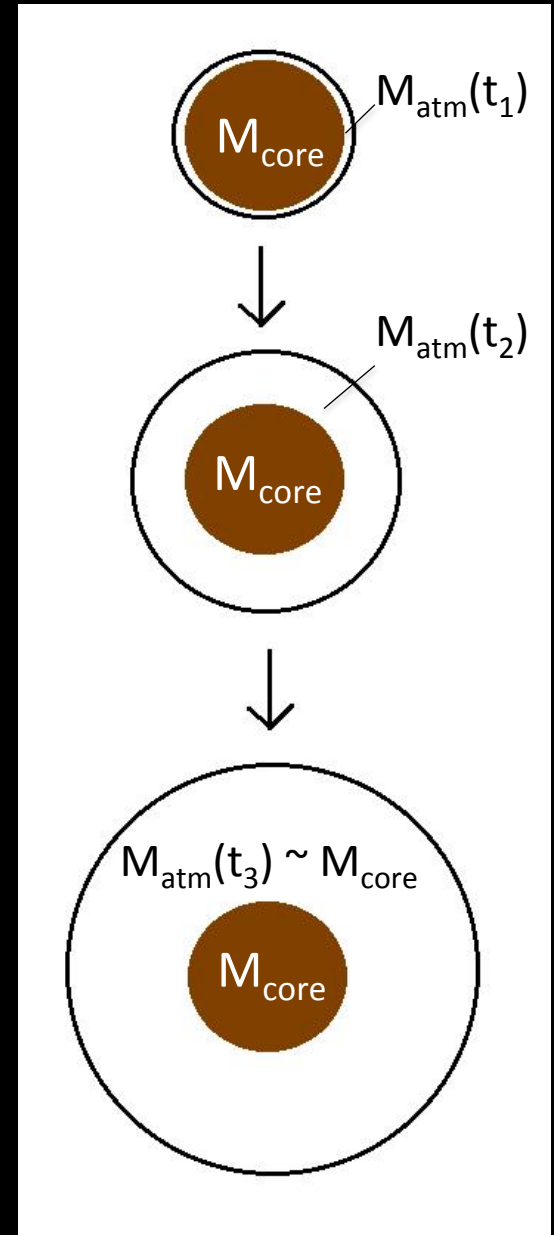
=> EVERY core can have

$$M_{\text{atm}} \sim M_{\text{core}}$$

=> “critical core mass”

$M_{\text{crit}} = M_{\text{core}}$  for which

$$M_{\text{atm}}(t_{\text{disk}}) \sim M_{\text{core}}$$



# GOAL

Determine the minimum core mass,  $M_{\text{crit}}$ , to form a giant planet during the disk lifetime in the low planetesimal accretion regime when atmosphere dominated by KH contraction

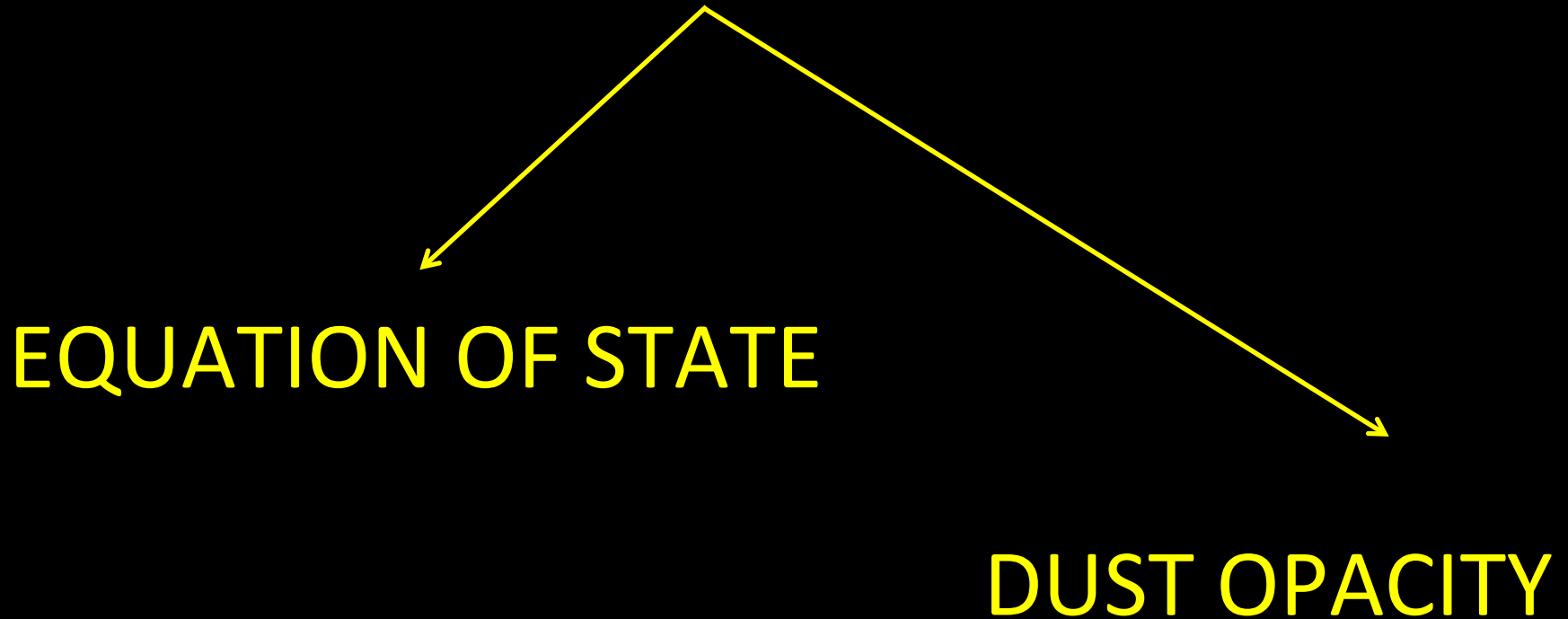
Calculate  $M_{\text{crit}}$  with  
REALISTIC EQUATION OF STATE  
REALISTIC DUST OPACITIES



# Model Assumptions

- Negligible planetesimal accretion => solid core of **fixed mass**  $M_c$
- Atmosphere is **embedded in the gas disk, spherically symmetric** and in **hydrostatic balance**
- Two layer atmosphere: **inner convective** region and **outer radiative** region
- **Constant luminosity** throughout the radiative region
- **Static profiles** connected by global **cooling equation**,  
 $L \sim -dE/dt$

Atmospheric evolution and  $M_{\text{crit}}$  are  
highly dependent on



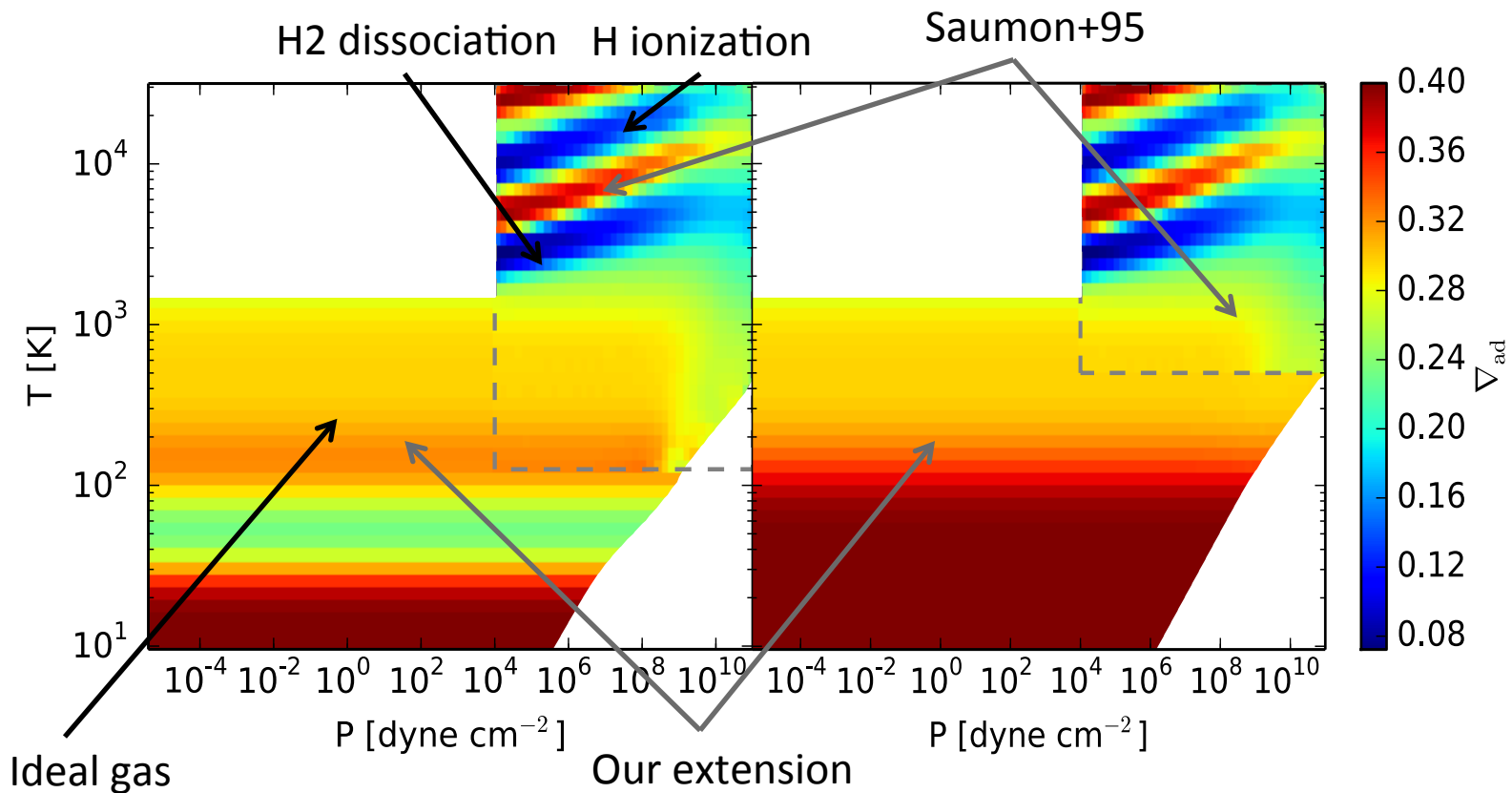
Atmospheric evolution and  $M_{\text{crit}}$  are  
highly dependent on



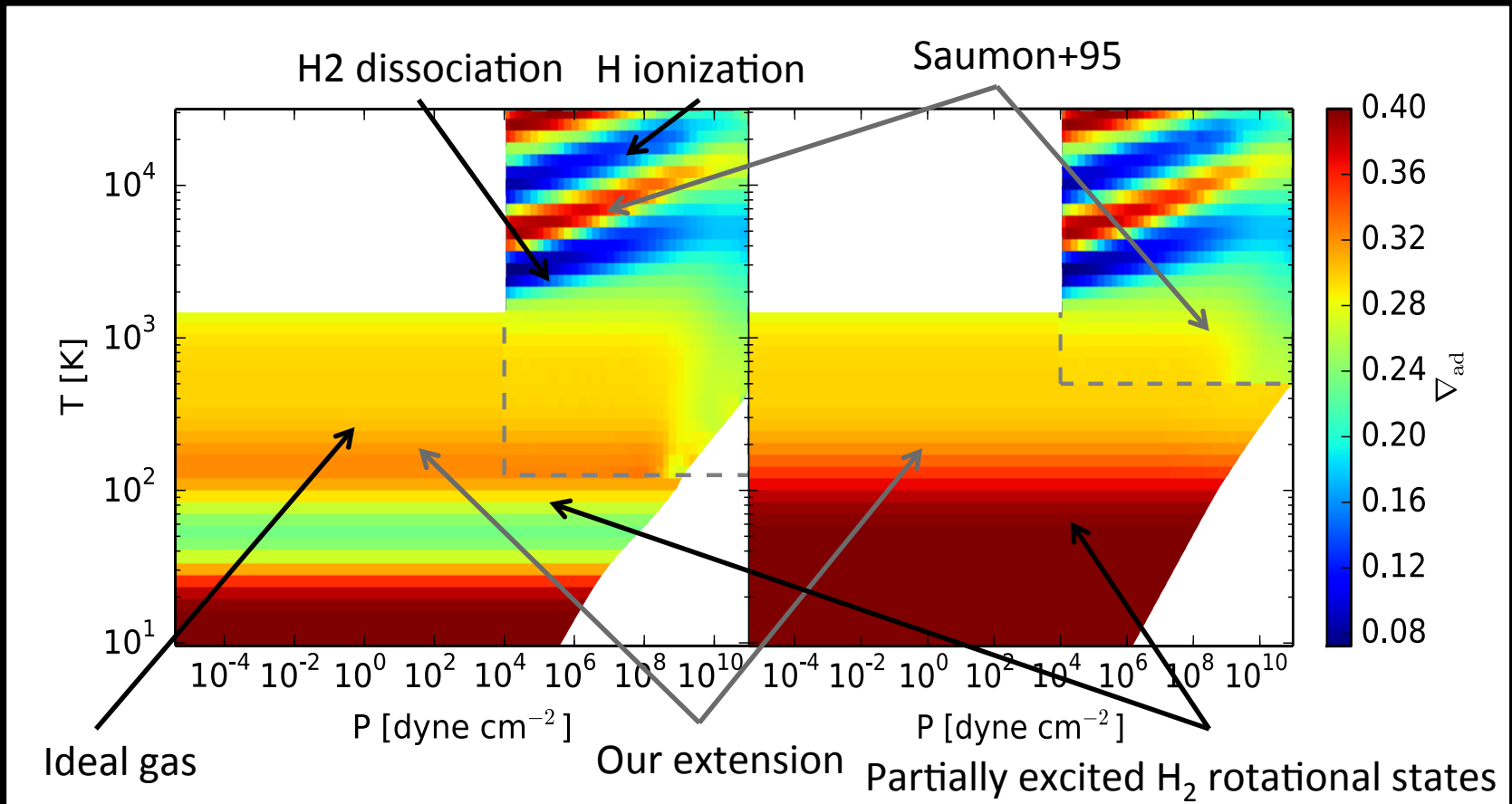
EQUATION OF STATE

DUST OPACITY

Adiabatic gradient  $\nabla_{ad} = \left( \frac{d \ln T}{d \ln P} \right)_{ad}$  is  
variable for realistic EOS

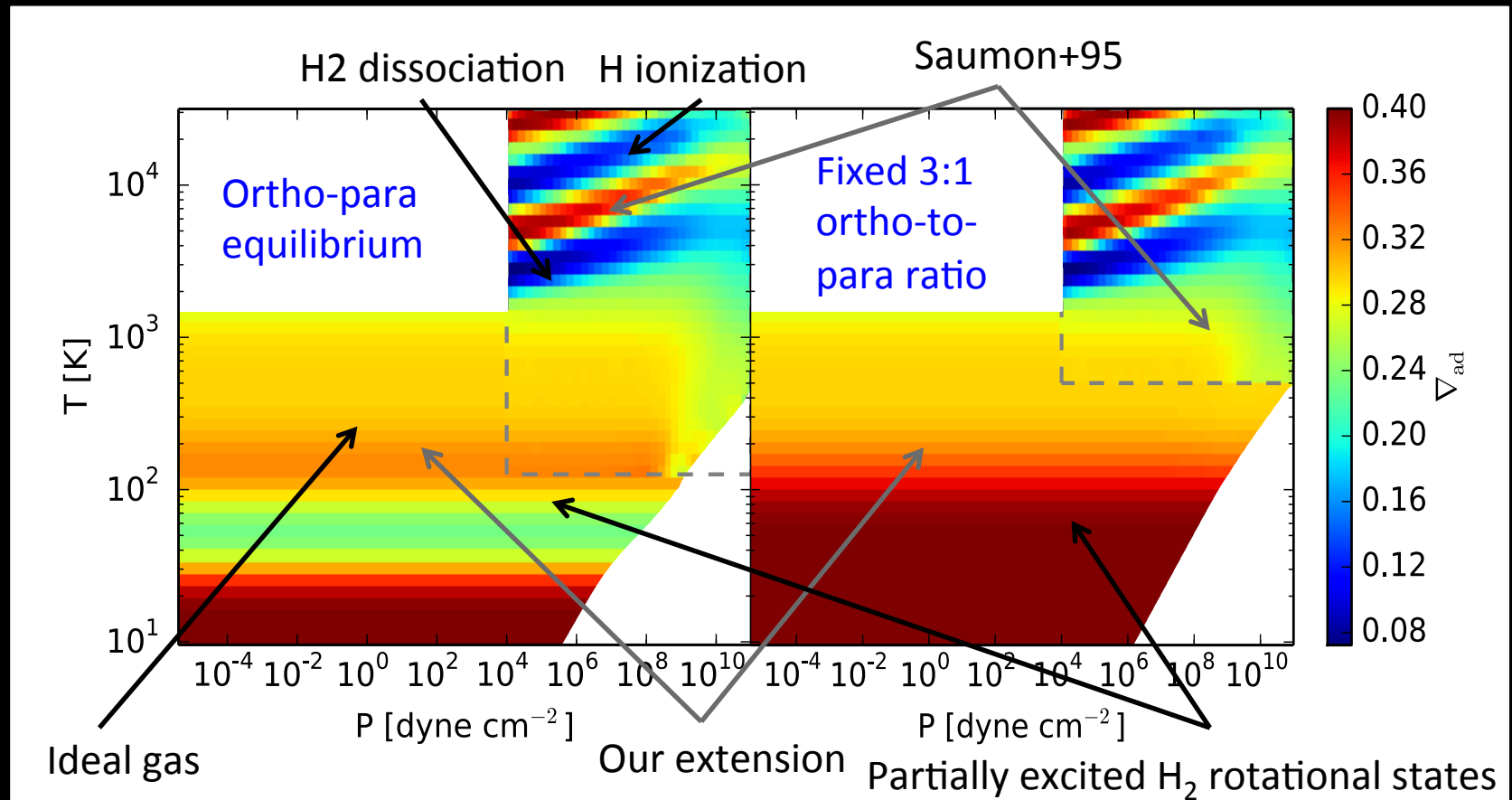


Adiabatic gradient  $\nabla_{ad} = \left( \frac{d \ln T}{d \ln P} \right)_{ad}$  is  
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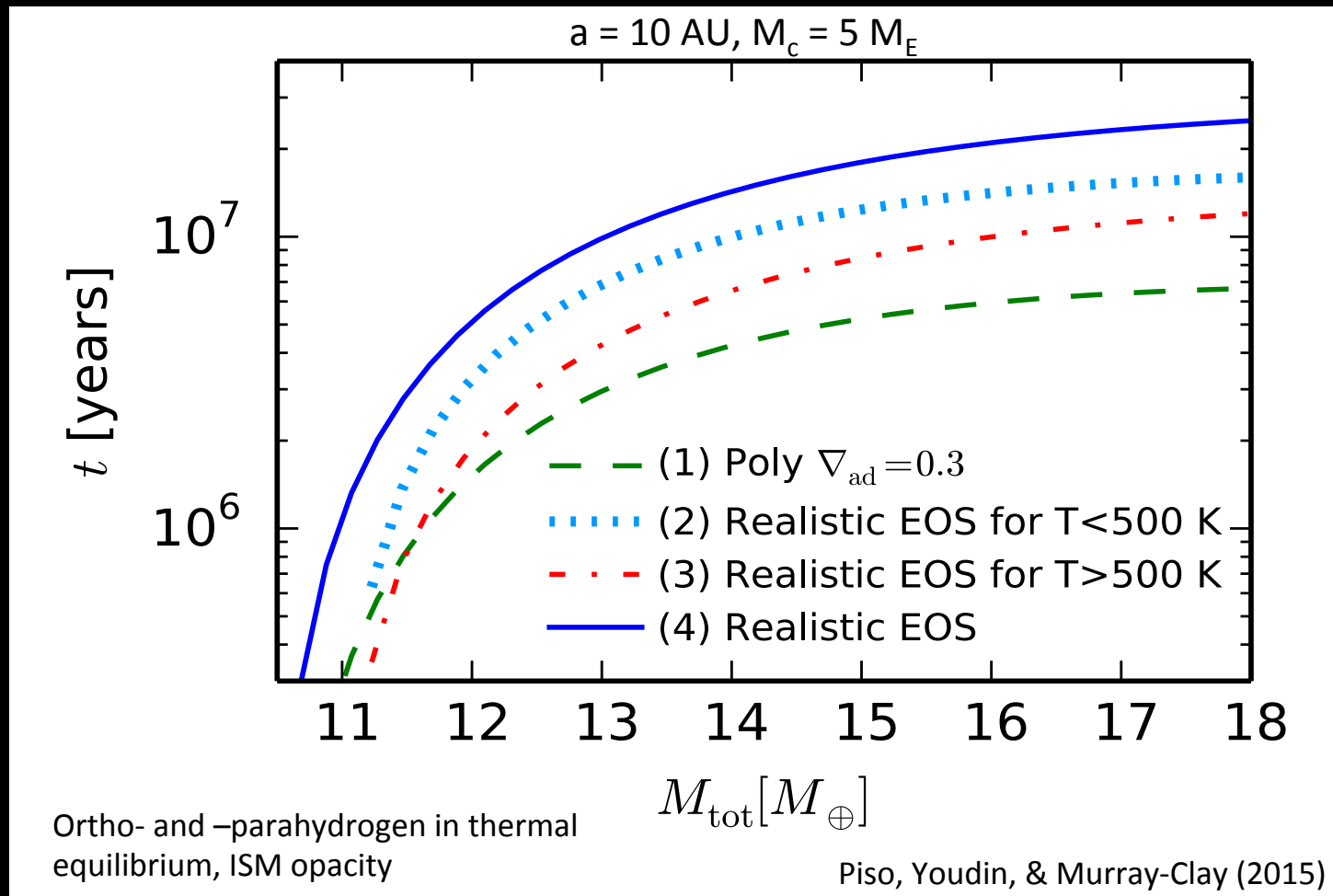


# Adiabatic gradient $\nabla_{ad} = \left( \frac{d \ln T}{d \ln P} \right)_{ad}$ is variable for realistic EOS

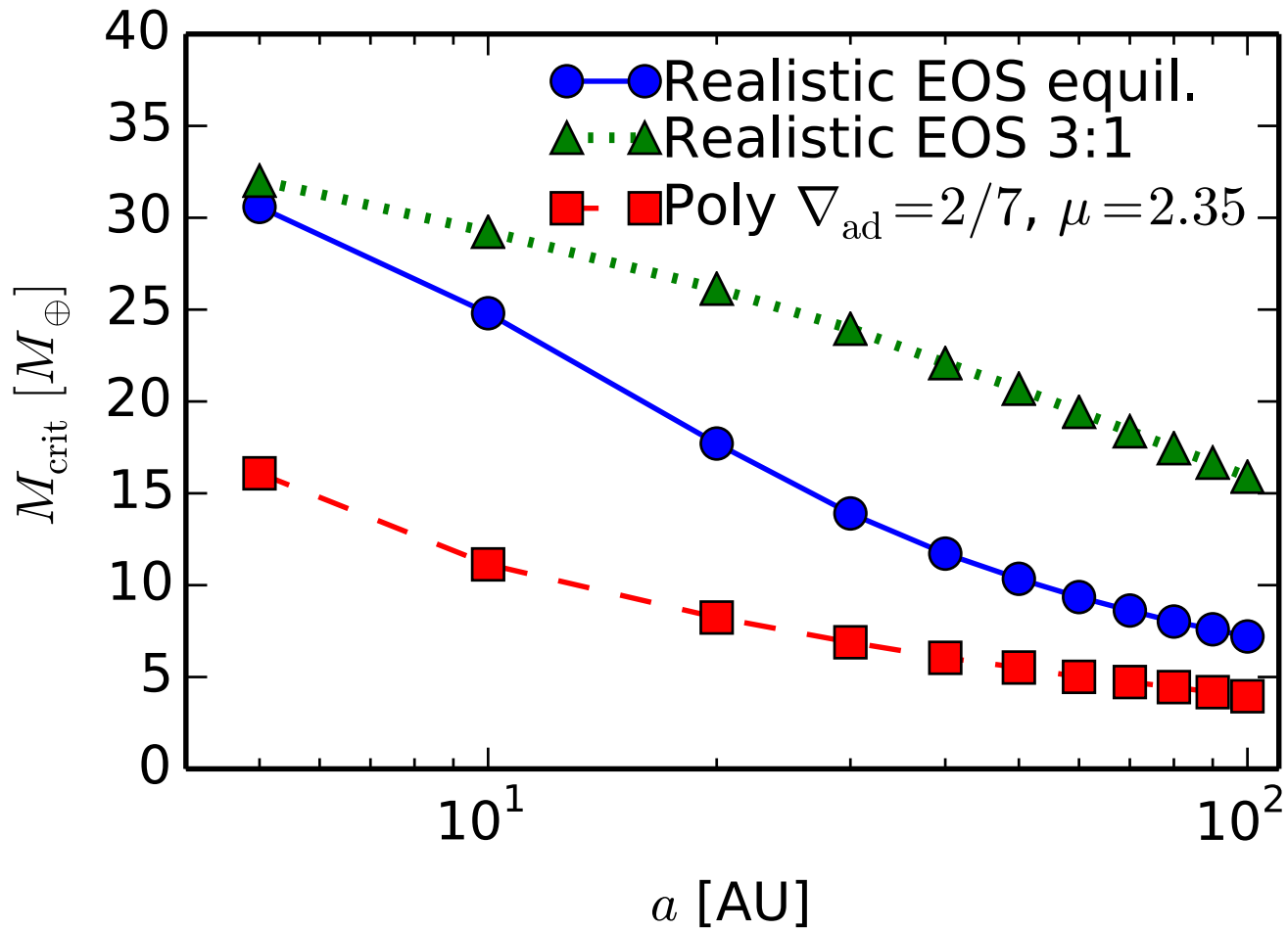
H<sub>2</sub> spin isomers  $\uparrow\uparrow$  ORTHOHYDROGEN and  $\uparrow\downarrow$  PARAHYDROGEN can be in **thermal equilibrium** or **fixed ratio**



Variations in  $\nabla_{\text{ad}}$  due to non-ideal EOS effects  
**INCREASE** the atmospheric evolutionary time



# Critical Core Mass

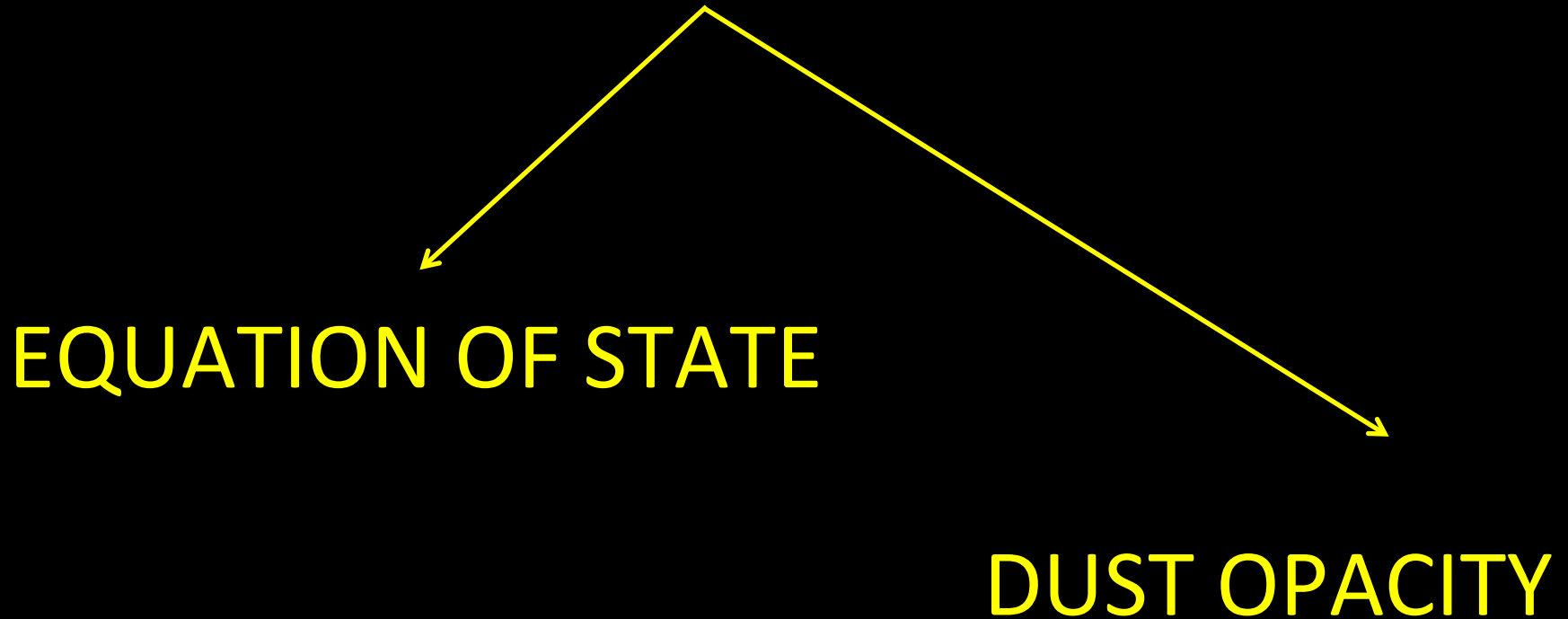


$t_{\text{disk}} \sim 3$  Myr, ISM opacity

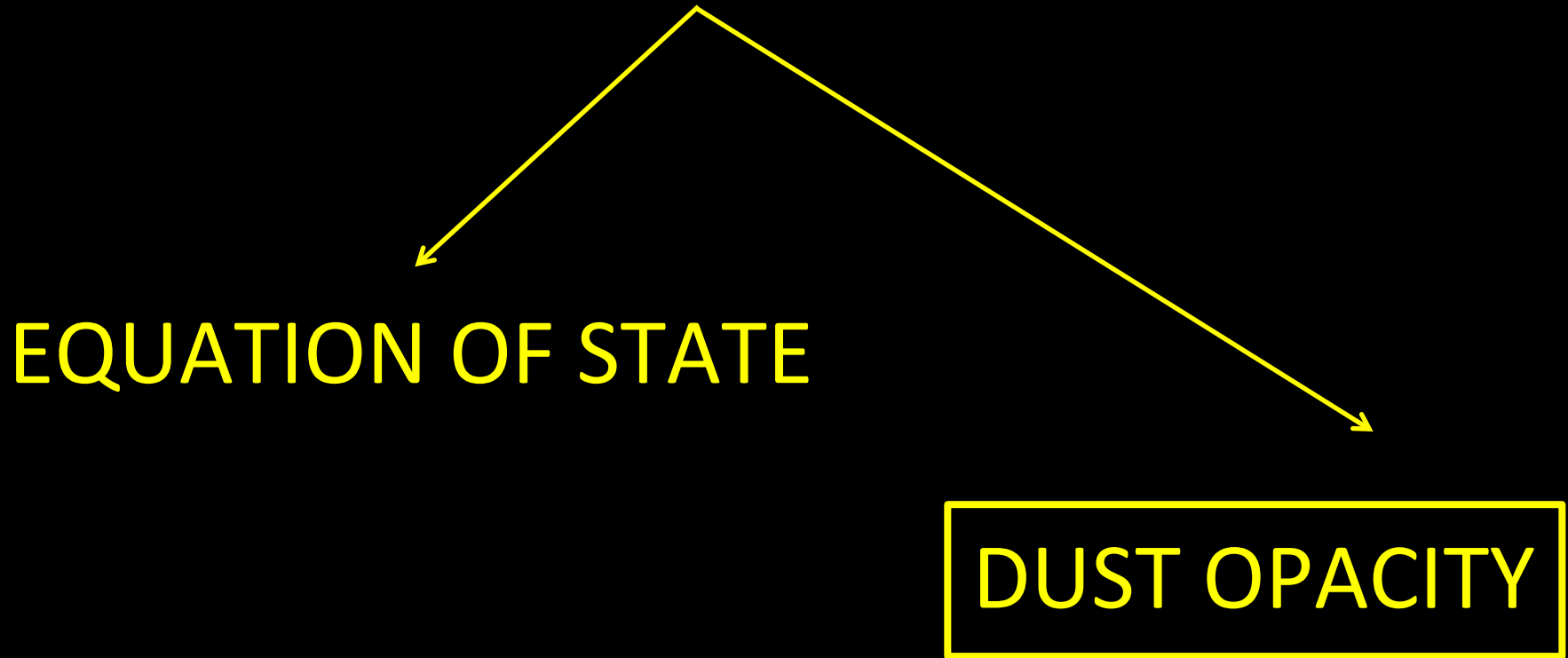
Piso, Youdin, & Murray-Clay (2015)



Atmospheric evolution and  $M_{\text{crit}}$  are  
highly dependent on



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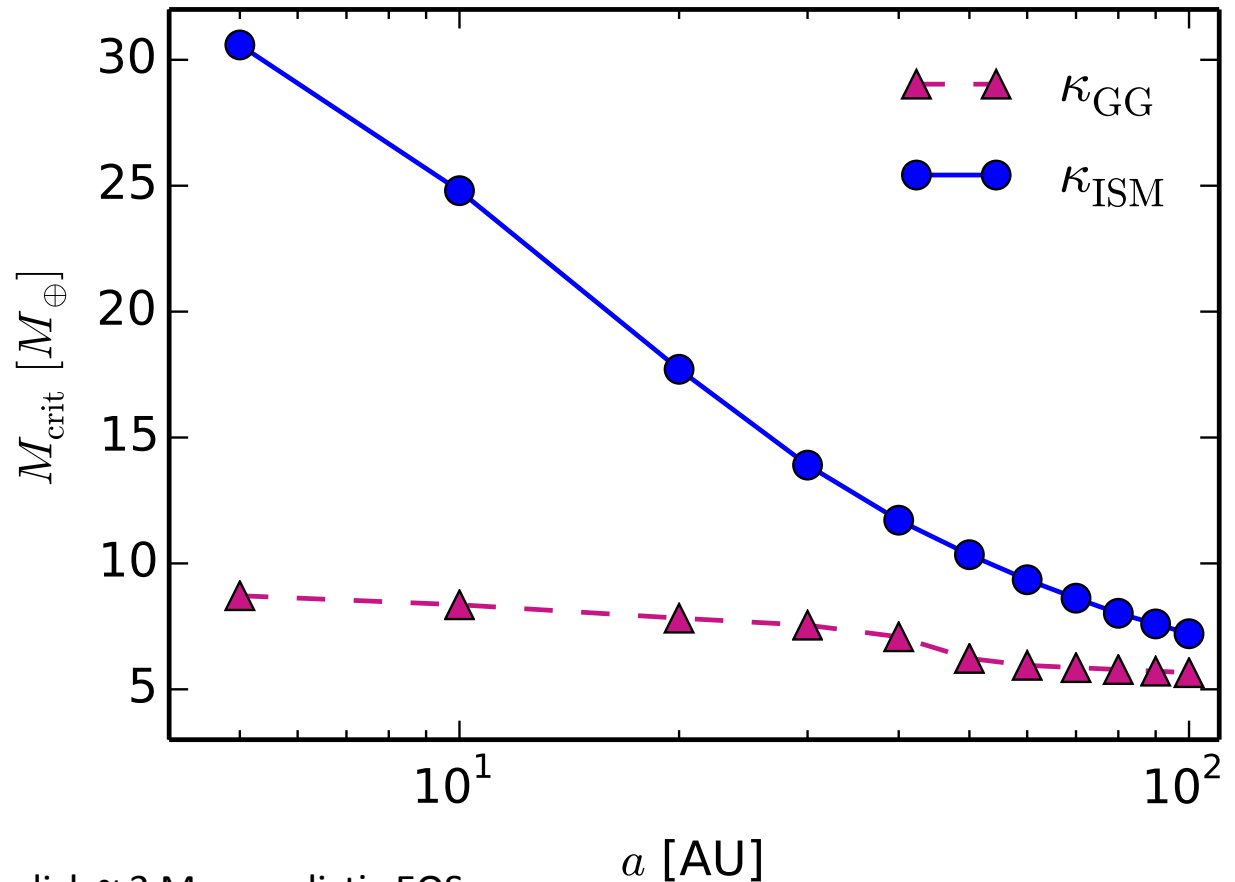


# Grain growth opacity **DECREASES** $M_{\text{crit}}$

$$dN/ds \sim s^{-p}$$

$$p = 3.5$$

$$s_{\text{max}} = 1 \text{ cm}$$



$t_{\text{disk}} \sim 3 \text{ Myr}$ , realistic EOS

Piso, Youdin, & Murray-Clay (2015)

# Grain growth opacity **DECREASES** $M_{\text{crit}}$

$$dN/ds \sim s^{-p}$$

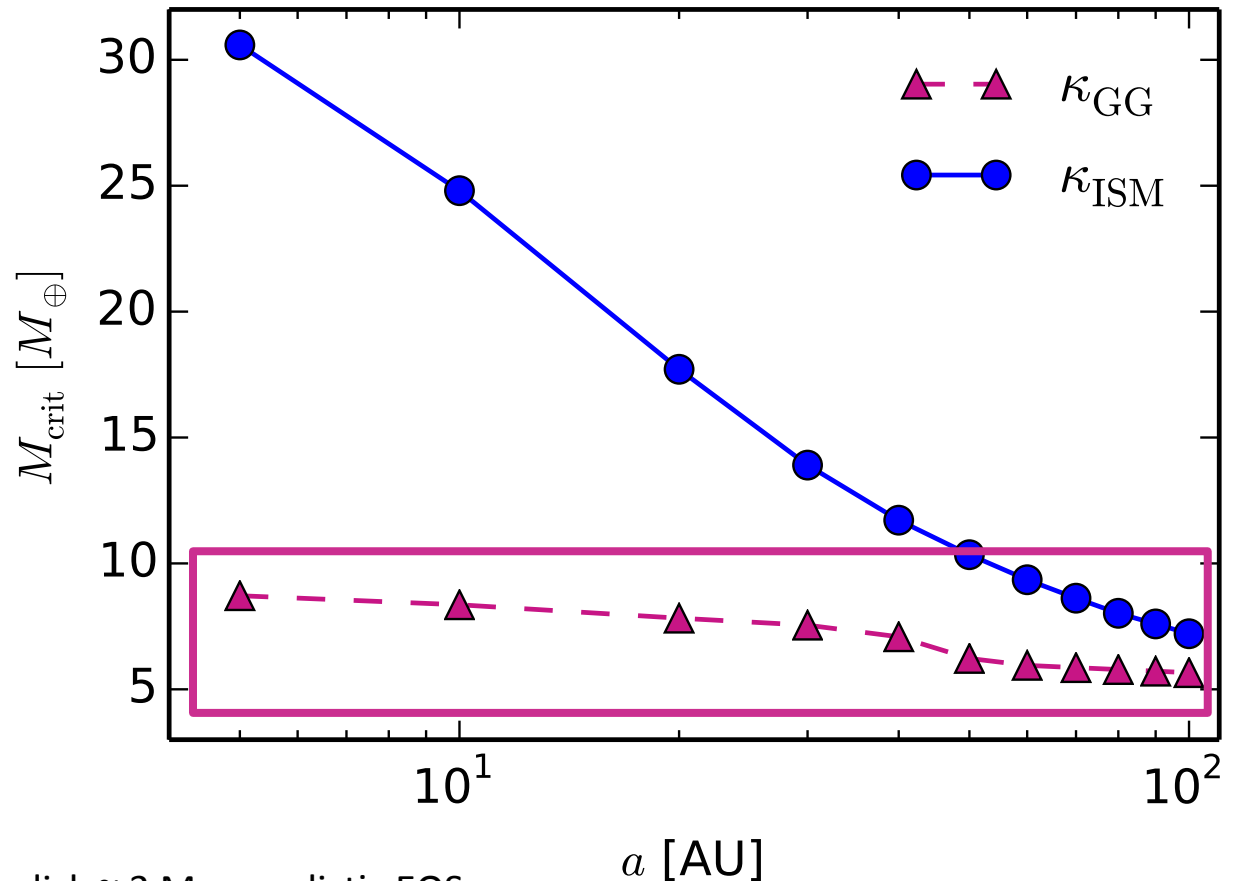
$$p = 3.5$$

$$s_{\text{max}} = 1 \text{ cm}$$

$M_{\text{crit}}:$

$\sim 8 M_{\text{E}} @ 5 \text{ AU}$

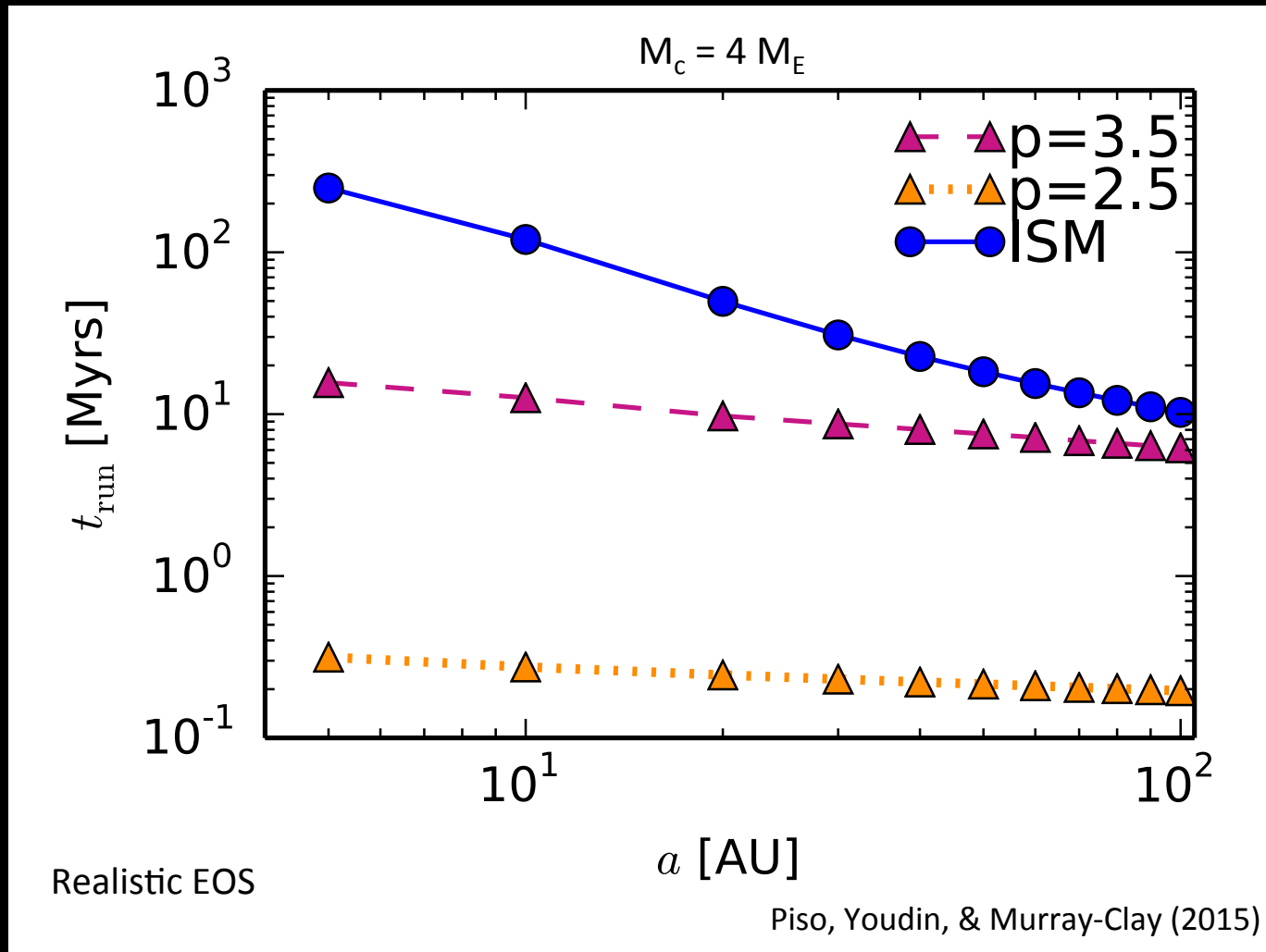
$\sim 5 M_{\text{E}} @ 100 \text{ AU}$



$t_{\text{disk}} \sim 3 \text{ Myr}$ , realistic EOS

Piso, Youdin, & Murray-Clay (2015)

Coagulation  $p=2.5$  may decrease  $M_{\text{crit}}$  by up to one order of magnitude!



# Summary

- H<sub>2</sub> dissociation and variable occupation of H<sub>2</sub> rotational states **INCREASE**  $M_{\text{crit}}$  when compared to an ideal gas polytrope
- Grain growth opacity **DECREASES**  $M_{\text{crit}}$  compared to ISM opacity
- $M_{\text{crit}} \sim 8 M_{\text{E}}$  at **5 AU** and  $\sim 5 M_{\text{E}}$  at **100 AU** for a **realistic EOS** with H<sub>2</sub> spin isomers in thermal equilibrium and grain growth opacity with standard collisional cascade ( **$p=3.5$** ) and  **$s_{\text{max}}=1 \text{ cm}$**
- $M_{\text{crit}}$  **may decrease by up to one order of magnitude** if coagulation is taken into account ( **$p=2.5$** )