1 Function Approximation Warmup

1.1 Exploring and downloading the data

```
rm(list=ls())           # Clear the workspace
set.seed(20866)
library(ggplot2)
library(sandwich)
library(car)
library(xtable)
library(aod)
library(systemfit)

## Loading required package:  Matrix
## Loading required package:  lmtest
## Loading required package:  zoo
##
## Attaching package:  'zoo'
##
## The following objects are masked from 'package:base':
##
##    as.Date, as.Date.numeric

library(MASS)
library(stargazer)

##
## Please cite as:
##
##  Hlavac, Marek (2014).  stargazer:  LaTeX code and ASCII text for
well-formatted regression and summary statistics tables.
##  R package version 5.1.  http://CRAN.R-project.org/package=stargazer

setwd("/Users/Tony/Downloads")

data <- read.csv("cps_00005.csv")
datamatrix <- as.matrix(read.csv("cps_00005.csv"))
datamatrix <- datamatrix[,-5:-8]
datamatrix <- datamatrix[,-2:-3]


datamatrix <- datamatrix[datamatrix[,9]!= 0,]
datamatrix <- datamatrix[datamatrix[,9]!= 9999999,]
```

```r
incomeadjust <- function(data.m = datamatrix, sampq = TRUE){

  AdjInc <- c(rep(NA, nrow(data.m)))
  data.m <- cbind(data.m, AdjInc)

  for (i in 1:nrow(datamatrix)){

    year <- as.numeric(data.m[i,1])
    income <- as.numeric(data.m[i,9])

    if (year == 2004){

      AdjustedIncome <- income * 1.25
      data.m[i,10] = round(AdjustedIncome)
    }

    if (year == 2014){

      AdjustedIncome <- income
      data.m[i,10] = round(AdjustedIncome)
    }


  }

 if (sampq == TRUE){
  top <- head(data.m, n=15)
  bottom<- tail(data.m, n=15)

  sample <- rbind(top,bottom)
  row.names(sample) <- NULL
  return(sample)

 }

 if (sampq == FALSE){
   return(data.m)
 }
}

incomeadjust(datamatrix, TRUE)
```

```
##       YEAR REGION AGE SEX RACE EDUC99 EMPSTAT HRSWORK INCWAGE AdjInc
##  [1,] 2004     11  59   2  100     13      10       2   60000  75000
##  [2,] 2004     11  49   1  100     10      10      20   32000  40000
```

```
##  [3,] 2004   11  42   2  100   15   10   40  30000  37500
##  [4,] 2004   11  68   2  100   15   10   20  18000  22500
##  [5,] 2004   11  42   2  100   10   10   24  30000  37500
##  [6,] 2004   11  45   1  100   13   10   33  50000  62500
##  [7,] 2004   11  20   1  100   10   30    0  15000  18750
##  [8,] 2004   11  19   1  100   10   10   44  18000  22500
##  [9,] 2004   11  18   2  100    8   10   20  10000  12500
## [10,] 2004   11  59   2  100    8   10   25  20285  25356
## [11,] 2004   11  74   1  100   15   10   26  19000  23750
## [12,] 2004   11  73   2  100   14   10   32  24250  30312
## [13,] 2004   11  71   2  802   11   32    0   5270   6588
## [14,] 2004   11  47   2  802   17   10   30  20900  26125
## [15,] 2004   11  36   1  100   10   10   19  26048  32560
## [16,] 2014   42  58   1  651   11   10   40  50000  50000
## [17,] 2014   42  30   2  652   16   10   40  25000  25000
## [18,] 2014   42  30   1  652   13   12    0   5000   5000
## [19,] 2014   42  48   1  651   10   10   50  43160  43160
## [20,] 2014   42  42   2  651   10   10   80  55120  55120
## [21,] 2014   42  35   1  802   10   10   40  24000  24000
## [22,] 2014   42  50   1  804   10   10   40  14000  14000
## [23,] 2014   42  39   1  651   15   10   40  27000  27000
## [24,] 2014   42  26   1  651   10   10   15  18000  18000
## [25,] 2014   42  24   2  651   17   10   40  60000  60000
## [26,] 2014   42  26   1  652   10   10   32  39000  39000
## [27,] 2014   42  20   1  652   10   30    0   3480   3480
## [28,] 2014   42  36   2  100   13   21    0  55300  55300
## [29,] 2014   42  47   1  807   10   32    0  35000  35000
## [30,] 2014   42  21   2  807   11   10   19  10300  10300
```

To find the CPI, I used the Bureau of Labor Statistics CPI Inflation Calculator, which told me that a dollar in 2004 has the same buying power as $1.25 in 2014. Therefore, to adjust 2004 income to its 2014 equivalent, I wrote a function that multiplied all 2004 incom

1.2 Make a new variable that is log wage income in your data

```
testdata <- incomeadjust(datamatrix, TRUE)

logVarf <- function(data.m = testdata){

  logInc <- c(rep(NA, nrow(data.m)))
  data.m <- cbind(data.m, logInc)

  for (i in 1:nrow(data.m)){
```

```
    rowIncomeLog <- log(data.m[i,10])
    data.m[i,11] <- rowIncomeLog

  }

  ## return(datamatrix) Commenting out so it doesn't actually return this
  return(data.m)

}

logVarf(testdata)
```

```
##        YEAR REGION AGE SEX RACE EDUC99 EMPSTAT HRSWORK INCWAGE AdjInc
##  [1,] 2004     11  59   2  100     13      10       2   60000  75000
##  [2,] 2004     11  49   1  100     10      10      20   32000  40000
##  [3,] 2004     11  42   2  100     15      10      40   30000  37500
##  [4,] 2004     11  68   2  100     15      10      20   18000  22500
##  [5,] 2004     11  42   2  100     10      10      24   30000  37500
##  [6,] 2004     11  45   1  100     13      10      33   50000  62500
##  [7,] 2004     11  20   1  100     10      30       0   15000  18750
##  [8,] 2004     11  19   1  100     10      10      44   18000  22500
##  [9,] 2004     11  18   2  100      8      10      20   10000  12500
## [10,] 2004     11  59   2  100      8      10      25   20285  25356
## [11,] 2004     11  74   1  100     15      10      26   19000  23750
## [12,] 2004     11  73   2  100     14      10      32   24250  30312
## [13,] 2004     11  71   2  802     11      32       0    5270   6588
## [14,] 2004     11  47   2  802     17      10      30   20900  26125
## [15,] 2004     11  36   1  100     10      10      19   26048  32560
## [16,] 2014     42  58   1  651     11      10      40   50000  50000
## [17,] 2014     42  30   2  652     16      10      40   25000  25000
## [18,] 2014     42  30   1  652     13      12       0    5000   5000
## [19,] 2014     42  48   1  651     10      10      50   43160  43160
## [20,] 2014     42  42   2  651     10      10      80   55120  55120
## [21,] 2014     42  35   1  802     10      10      40   24000  24000
## [22,] 2014     42  50   1  804     10      10      40   14000  14000
## [23,] 2014     42  39   1  651     15      10      40   27000  27000
## [24,] 2014     42  26   1  651     10      10      15   18000  18000
## [25,] 2014     42  24   2  651     17      10      40   60000  60000
## [26,] 2014     42  26   1  652     10      10      32   39000  39000
## [27,] 2014     42  20   1  652     10      30       0    3480   3480
## [28,] 2014     42  36   2  100     13      21       0   55300  55300
## [29,] 2014     42  47   1  807     10      32       0   35000  35000
## [30,] 2014     42  21   2  807     11      10      19   10300  10300
##          logInc
##  [1,] 11.225243
```

```
##  [2,] 10.596635
##  [3,] 10.532096
##  [4,] 10.021271
##  [5,] 10.532096
##  [6,] 11.042922
##  [7,]  9.838949
##  [8,] 10.021271
##  [9,]  9.433484
## [10,] 10.140771
## [11,] 10.075338
## [12,] 10.319299
## [13,]  8.793005
## [14,] 10.170648
## [15,] 10.390840
## [16,] 10.819778
## [17,] 10.126631
## [18,]  8.517193
## [19,] 10.672669
## [20,] 10.917268
## [21,] 10.085809
## [22,]  9.546813
## [23,] 10.203592
## [24,]  9.798127
## [25,] 11.002100
## [26,] 10.571317
## [27,]  8.154788
## [28,] 10.920528
## [29,] 10.463103
## [30,]  9.239899
```

1.3 Construct "potential experience", which will be "Age - years of schooling - 5"

```
sample <- logVarf(testdata)

potExpf <- function(data.m = testdata){

  potExp <- c(rep(NA, nrow(data.m)))
  YrsOfSch <- c(rep(NA, nrow(data.m)))
  data.m <- cbind(data.m, potExp, YrsOfSch)

  for (i in 1:nrow(data.m)){
```

```
    indAge = as.numeric(data.m[i,3])
    indEduCode = as.numeric(data.m[i,6])

    if (indEduCode < 6){
      indYrsOfSch = 9
      indPotExp = indAge - indYrsOfSch - 5
      data.m[i,12] = indPotExp
      data.m[i,13] = indYrsOfSch

    }

    if (indEduCode == 6){
      indYrsOfSch = 10
      indPotExp = indAge - indYrsOfSch - 5
      data.m[i,12] = indPotExp
      data.m[i,13] = indYrsOfSch

    }

    if (indEduCode == 7){
      indYrsOfSch = 11
      indPotExp = indAge - indYrsOfSch - 5
      data.m[i,12] = indPotExp
      data.m[i,13] = indYrsOfSch

    }

    if (indEduCode == 8){
      indYrsOfSch = 12
      indPotExp = indAge - indYrsOfSch - 5
      data.m[i,12] = indPotExp
      data.m[i,13] = indYrsOfSch

    }

    if (indEduCode == 9){
      indYrsOfSch = 13
      indPotExp = indAge - indYrsOfSch - 5
      data.m[i,12] = indPotExp
      data.m[i,13] = indYrsOfSch

    }

    if (indEduCode == 10){
      indYrsOfSch = 13
```

```
    indPotExp = indAge - indYrsOfSch - 5
    data.m[i,12] = indPotExp
    data.m[i,13] = indYrsOfSch

  }

  if (indEduCode == 11){
    indYrsOfSch = 14
    indPotExp = indAge - indYrsOfSch - 5
    data.m[i,12] = indPotExp
    data.m[i,13] = indYrsOfSch

  }

  if (indEduCode == 12){
    indYrsOfSch = 15
    indPotExp = indAge - indYrsOfSch - 5
    data.m[i,12] = indPotExp
    data.m[i,13] = indYrsOfSch

  }

  if (indEduCode == 13){
    indYrsOfSch = 15
    indPotExp = indAge - indYrsOfSch - 5
    data.m[i,12] = indPotExp
    data.m[i,13] = indYrsOfSch

  }

  if (indEduCode == 14){
    indYrsOfSch = 15
    indPotExp = indAge - indYrsOfSch - 5
    data.m[i,12] = indPotExp
    data.m[i,13] = indYrsOfSch

  }

  if (indEduCode == 15){
    indYrsOfSch = 17
    indPotExp = indAge - indYrsOfSch - 5
    data.m[i,12] = indPotExp
    data.m[i,13] = indYrsOfSch

  }
```

```
    if (indEduCode == 16){
      indYrsOfSch = 19
      indPotExp = indAge - indYrsOfSch - 5
      data.m[i,12] = indPotExp
      data.m[i,13] = indYrsOfSch

    }

    if (indEduCode == 17){
      indYrsOfSch = 19
      indPotExp = indAge - indYrsOfSch - 5
      data.m[i,12] = indPotExp
      data.m[i,13] = indYrsOfSch

    }

    if (indEduCode == 18){
      indYrsOfSch = 22
      indPotExp = indAge - indYrsOfSch - 5
      data.m[i,12] = indPotExp
      data.m[i,13] = indYrsOfSch

    }

  }

  ## return(datamatrix) Commenting out so it doesn't actually return this
  return(data.m)

}

potExpf(sample)
```

```
##       YEAR REGION AGE SEX RACE EDUC99 EMPSTAT HRSWORK INCWAGE AdjInc
##  [1,] 2004     11  59   2  100     13      10       2   60000  75000
##  [2,] 2004     11  49   1  100     10      10      20   32000  40000
##  [3,] 2004     11  42   2  100     15      10      40   30000  37500
##  [4,] 2004     11  68   2  100     15      10      20   18000  22500
##  [5,] 2004     11  42   2  100     10      10      24   30000  37500
##  [6,] 2004     11  45   1  100     13      10      33   50000  62500
##  [7,] 2004     11  20   1  100     10      30       0   15000  18750
##  [8,] 2004     11  19   1  100     10      10      44   18000  22500
##  [9,] 2004     11  18   2  100      8      10      20   10000  12500
## [10,] 2004     11  59   2  100      8      10      25   20285  25356
## [11,] 2004     11  74   1  100     15      10      26   19000  23750
```

```
## [12,] 2004    11  73   2  100    14    10    32   24250  30312
## [13,] 2004    11  71   2  802    11    32     0    5270   6588
## [14,] 2004    11  47   2  802    17    10    30   20900  26125
## [15,] 2004    11  36   1  100    10    10    19   26048  32560
## [16,] 2014    42  58   1  651    11    10    40   50000  50000
## [17,] 2014    42  30   2  652    16    10    40   25000  25000
## [18,] 2014    42  30   1  652    13    12     0    5000   5000
## [19,] 2014    42  48   1  651    10    10    50   43160  43160
## [20,] 2014    42  42   2  651    10    10    80   55120  55120
## [21,] 2014    42  35   1  802    10    10    40   24000  24000
## [22,] 2014    42  50   1  804    10    10    40   14000  14000
## [23,] 2014    42  39   1  651    15    10    40   27000  27000
## [24,] 2014    42  26   1  651    10    10    15   18000  18000
## [25,] 2014    42  24   2  651    17    10    40   60000  60000
## [26,] 2014    42  26   1  652    10    10    32   39000  39000
## [27,] 2014    42  20   1  652    10    30     0    3480   3480
## [28,] 2014    42  36   2  100    13    21     0   55300  55300
## [29,] 2014    42  47   1  807    10    32     0   35000  35000
## [30,] 2014    42  21   2  807    11    10    19   10300  10300
##          logInc potExp YrsOfSch
##  [1,] 11.225243     39       15
##  [2,] 10.596635     31       13
##  [3,] 10.532096     20       17
##  [4,] 10.021271     46       17
##  [5,] 10.532096     24       13
##  [6,] 11.042922     25       15
##  [7,]  9.838949      2       13
##  [8,] 10.021271      1       13
##  [9,]  9.433484      1       12
## [10,] 10.140771     42       12
## [11,] 10.075338     52       17
## [12,] 10.319299     53       15
## [13,]  8.793005     52       14
## [14,] 10.170648     23       19
## [15,] 10.390840     18       13
## [16,] 10.819778     39       14
## [17,] 10.126631      6       19
## [18,]  8.517193     10       15
## [19,] 10.672669     30       13
## [20,] 10.917268     24       13
## [21,] 10.085809     17       13
## [22,]  9.546813     32       13
## [23,] 10.203592     17       17
## [24,]  9.798127      8       13
## [25,] 11.002100      0       19
```

```
## [26,] 10.571317      8        13
## [27,]  8.154788      2        13
## [28,] 10.920528     16        15
## [29,] 10.463103     29        13
## [30,]  9.239899      2        14
```

1.4 Make a table comparing the following regressions for 2014 and 2014

```
library(stargazer)

regData <- incomeadjust(datamatrix, FALSE)
regData <- logVarf(regData)
regData <- potExpf(regData)

regData <- as.data.frame(regData)

data04 <- regData[regData[,1]== 2004,]
data14 <- regData[regData[,1]== 2014,]
data04m <- data04[data04[,4]== 1,]
data04f <- data04[data04[,4]== 2,]
data14m <- data14[data14[,4]== 1,]
data14f <- data14[data14[,4]== 2,]

fit04 <- lm(data04$logInc ~ data04$YrsOfSch + data04$potExp
          + I(data04$potExp^2), data=data04 )

fit04m <- lm(data04m$logInc ~ data04m$YrsOfSch + data04m$potExp
          + I(data04m$potExp^2), data=data04m )

fit04f <- lm(data04f$logInc ~ data04f$YrsOfSch + data04f$potExp
          + I(data04f$potExp^2), data=data04f )

fit14 <- lm(data14$logInc ~ data14$YrsOfSch + data14$potExp
          + I(data14$potExp^2), data=data14 )

fit14m <- lm(data14m$logInc ~ data14m$YrsOfSch + data14m$potExp
          + I(data14m$potExp^2), data=data14m )

fit14f <- lm(data14f$logInc ~ data14f$YrsOfSch + data14f$potExp
          + I(data14f$potExp^2), data=data14f)


stargazer(fit04, fit04m, fit04f)


##
## % Table created by stargazer v.5.1 by Marek Hlavac, Harvard University. E-mail: hlavac at fas.harvard.edu
## % Date and time: Thu, Apr 30, 2015 - 19:46:49
## \begin{table}[!htbp] \centering
##   \caption{}
##   \label{}
## \begin{tabular}{@{\extracolsep{5pt}}lccc}
## \\[-1.8ex]\hline
## \hline \\[-1.8ex]
##  & \multicolumn{3}{c}{\textit{Dependent variable:}} \\
## \cline{2-4}
## \\[-1.8ex] & logInc & logInc & logInc \\
## \\[-1.8ex] & (1) & (2) & (3)\\
## \hline \\[-1.8ex]
##  YrsOfSch & 0.163$^{***}$ &  &  \\
##   & (0.001) &  &  \\
##   & & & \\
##  potExp & 0.106$^{***}$ &  &  \\
##   & (0.001) &  &  \\
##   & & & \\
##  potExp$\hat{\mkern6mu}$2) & $-$0.002$^{***}$ &  &  \\
##   & (0.00002) &  &  \\
##   & & & \\
##  YrsOfSch &  & 0.160$^{***}$ &  \\
##   &  & (0.002) &  \\
##   & & & \\
##  potExp &  & 0.120$^{***}$ &  \\
##   &  & (0.001) &  \\
##   & & & \\
##  potExp$\hat{\mkern6mu}$2) &  & $-$0.002$^{***}$ &  \\
##   &  & (0.00002) &  \\
##   & & & \\
##  YrsOfSch &  &  & 0.171$^{***}$ \\
```

```
##   &  &  & (0.002) \\
##   & & & \\
##  potExp &  &  & 0.091$^{***}$ \\
##   &  &  & (0.001) \\
##   & & & \\
##  potExp$\hat{\mkern6mu}$2) &  &  & $-$0.002$^{***}$ \\
##   &  &  & (0.00002) \\
##   & & & \\
##  Constant & 6.719$^{***}$ & 6.869$^{***}$ & 6.501$^{***}$ \\
##   & (0.019) & (0.024) & (0.030) \\
##   & & & \\
## \hline \\[-1.8ex]
## Observations & 103,084 & 52,848 & 50,236 \\
## R$^{2}$ & 0.310 & 0.385 & 0.266 \\
## Adjusted R$^{2}$ & 0.310 & 0.385 & 0.266 \\
## Residual Std. Error & 1.026 (df = 103080) & 0.942 (df = 52844) & 1.045 (df = 50232) \\
## F Statistic & 15,448.400$^{***}$ (df = 3; 103080) & 11,041.710$^{***}$ (df = 3; 52844) & 6,081.976$^{***}$ (df = 3; 50232) \\
## \hline
## \hline \\[-1.8ex]
## \textit{Note:}  & \multicolumn{3}{r}{$^{*}$p$<$0.1; $^{**}$p$<$0.05; $^{***}$p$<$0.01} \\
## \end{tabular}
## \end{table}


stargazer(fit14, fit14m, fit14f)


##
## % Table created by stargazer v.5.1 by Marek Hlavac, Harvard University. E-mail: hlavac at fas.harvard.edu
## % Date and time: Thu, Apr 30, 2015 - 19:46:50
## \begin{table}[!htbp] \centering
##   \caption{}
##   \label{}
## \begin{tabular}{@{\extracolsep{5pt}}lccc}
## \\[-1.8ex]\hline
## \hline \\[-1.8ex]
##  & \multicolumn{3}{c}{\textit{Dependent variable:}} \\
## \cline{2-4}
## \\[-1.8ex] & logInc & logInc & logInc \\
## \\[-1.8ex] & (1) & (2) & (3)\\
## \hline \\[-1.8ex]
##  YrsOfSch & 0.166$^{***}$ &  &  \\
##   & (0.002) &  &  \\
##   & & & \\
##  potExp & 0.093$^{***}$ &  &  \\
##   & (0.001) &  &  \\
##   & & & \\
##  potExp$\hat{\mkern6mu}$2) & $-$0.002$^{***}$ &  &  \\
##   & (0.00002) &  &  \\
##   & & & \\
##  YrsOfSch &  & 0.164$^{***}$ &  \\
##   &  & (0.002) &  \\
##   & & & \\
##  potExp &  & 0.105$^{***}$ &  \\
##   &  & (0.001) &  \\
##   & & & \\
##  potExp$\hat{\mkern6mu}$2) &  & $-$0.002$^{***}$ &  \\
##   &  & (0.00002) &  \\
##   & & & \\
##  YrsOfSch &  &  & 0.179$^{***}$ \\
##   &  &  & (0.002) \\
##   & & & \\
##  potExp &  &  & 0.078$^{***}$ \\
##   &  &  & (0.001) \\
##   & & & \\
##  potExp$\hat{\mkern6mu}$2) &  &  & $-$0.001$^{***}$ \\
##   &  &  & (0.00003) \\
##   & & & \\
##  Constant & 6.752$^{***}$ & 6.864$^{***}$ & 6.474$^{***}$ \\
##   & (0.024) & (0.031) & (0.036) \\
##   & & & \\
## \hline \\[-1.8ex]
## Observations & 65,183 & 33,760 & 31,423 \\
## R$^{2}$ & 0.287 & 0.339 & 0.266 \\
## Adjusted R$^{2}$ & 0.287 & 0.339 & 0.266 \\
## Residual Std. Error & 1.001 (df = 65179) & 0.948 (df = 33756) & 1.005 (df = 31419) \\
## F Statistic & 8,759.542$^{***}$ (df = 3; 65179) & 5,763.025$^{***}$ (df = 3; 33756) & 3,794.622$^{***}$ (df = 3; 31419) \\
## \hline
## \hline \\[-1.8ex]
## \textit{Note:}  & \multicolumn{3}{r}{$^{*}$p$<$0.1; $^{**}$p$<$0.05; $^{***}$p$<$0.01} \\
## \end{tabular}
## \end{table}
```

Table 1:

	Dependent variable:		
	logInc	logInc	logInc
	(1)	(2)	(3)
YrsOfSch	0.163***	0.160***	0.171***
	(0.001)	(0.002)	(0.002)
potExp	0.106***	0.120***	0.091***
	(0.001)	(0.001)	(0.001)
potExpˆ2	−0.002***	−0.002***	−0.002***
	(0.00002)	(0.00002)	(0.00002)
Constant	6.719***	6.869***	6.501***
	(0.019)	(0.024)	(0.030)
Observations	103,084	52,848	50,236
R^2	0.310	0.385	0.266
Adjusted R^2	0.310	0.385	0.266
Residual Std. Error	1.026 (df = 103080)	0.942 (df = 52844)	1.045 (df = 50
F Statistic	15,448.400*** (df = 3; 103080)	11,041.710*** (df = 3; 52844)	6,081.976*** (df =
Note:			*p<0.1; **p<0.05;