Problem Set 2

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1 Machinery for the Schelling Model

1.1 Write a function that calculates distances between coordinate points

```
an_individual \leftarrow c(0,0)
neighbors = matrix(1:8, ncol = 2, byrow = T)
print(neighbors)
      [,1] [,2]
## [1,]
        1 2
## [2,]
         3
         5
## [3,]
                6
## [4,]
         7
colnames(neighbors) <- c("X","Y")</pre>
dstances = matrix(ncol = 3, byrow = T)
colnames(dstances) <- c("X","Y", "Pythgorean")</pre>
f1 <- function(an_individual, neighbors){</pre>
 for (i in 1:nrow(neighbors)){
   neighbor_longitude = neighbors[i,1]
    ## Find your neighbor's longitude
   neighbor_latitude = neighbors[i,2]
    ## Find your neighbor's latitude
   individual_longitude = an_individual[1]
    ## Find your own longitude
    individual_latitude = an_individual[2]
    ## Find your own latitude
   lftrghtdstance = abs(neighbor_longitude - individual_longitude)
```

```
## Find east/west distance between indiv. and neighbor
   updowndstance = abs(neighbor_latitude - individual_latitude)
    ## Find north/south distance between indiv. and neighbor
   pyth = sqrt(((lftrghtdstance)^2) + ((updowndstance)^2))
   ## Find Euclidian distance
   currentdistance = c(lftrghtdstance,updowndstance,pyth)
    ## Make vector with Manhattan and Euclidian distances
   dstances <- rbind(dstances, currentdistance)</pre>
    ## Add vector as row in matrix of distances
 return(dstances)
f1(an_individual, neighbors)
                  X Y Pythgorean
##
                 NA NA NA
## currentdistance 1 2 2.236068
## currentdistance 3 4 5.000000
## currentdistance 5 6 7.810250
## currentdistance 7 8 10.630146
```

1.2 Write a function that simulates Schelling's Segregation model

```
library(RANN)
library(ggplot2)
library(reshape2)

library(foreach)
library(doParallel)

## Loading required package: iterators
## Loading required package: parallel

library(parallel)

require(foreach)
require(doParallel)
require(parallel)
```

```
require(ggplot2)
numCores <- detectCores()</pre>
cl <- makeCluster(numCores)</pre>
registerDoParallel(cl)
testv = 100
testRacialPreferenceTable <- matrix(1:15, ncol = 5, nrow = 3)</pre>
testRacialPreferenceTable[1,] <- c("R",1, 50, 5, 2)</pre>
testRacialPreferenceTable[2,] <- c("G", 0, 50, 5, 2)
testRacialPreferenceTable[3,] <- c("B", -1, 50, 5, 2)
colnames(testRacialPreferenceTable) <- c("Color", "Value", "Pop.", "Test Pool Size", "Racial")</pre>
print(testRacialPreferenceTable)
        Color Value Pop. Test Pool Size Racial Threshold
## [1,] "R" "1" "50" "5"
                                          "2"
             "0" "50" "5"
                                          "2"
## [2,] "G"
## [3,] "B"
             "-1" "50" "5"
                                          "2"
nR <- as.numeric(testRacialPreferenceTable[1, "Pop."])</pre>
nG <- as.numeric(testRacialPreferenceTable[2, "Pop."])</pre>
nB <- as.numeric(testRacialPreferenceTable[3, "Pop."])</pre>
n \leftarrow sum(nR + nG + nB)
## Find total population from summing each racial population
inputs <- testRacialPreferenceTable</pre>
stop.val <- .8
happy_counter <- 0
Schelling <- function(racialPreferenceTable = testRacialPreferenceTable, cyclemax = testv){
  set.seed(20016)
  library(ggplot2)
  LocationTable <- matrix(ncol = 3)</pre>
  ## Initalizing table for initial neighborhood coordinates
  for (i in 1:nR){
    x <- runif(1, min=0, max=1)
    ## Generate random X coordinate between 0 and 1 for point
    y <- runif(1, min=0, max=1)</pre>
    ## Generate random Y coordinate between O and 1 for point
    R = c(1, x, y)
    ## Create vector with point coordinates, labeling point as red
```

```
LocationTable <- rbind(LocationTable, R)</pre>
  ## Add red point to table of all neighborhood coordinates
for (i in 1:nG){
  x <- runif(1, min=0, max=1)</pre>
  y <- runif(1, min=0, max=1)
  G = c(0,x,y)
  LocationTable <- rbind(LocationTable, G)</pre>
for (i in 1:nB){
 x <- runif(1, min=0, max=1)
  y <- runif(1, min=0, max=1)</pre>
  B = c(-1, x, y)
  LocationTable <- rbind(LocationTable, B)</pre>
LocationTable <- LocationTable[-1,]</pre>
Count <- c(1:nrow(LocationTable))</pre>
## Create column counting number of points or people
Happy <- c(rep(0, nrow(LocationTable)))</pre>
## Create column to keep track of if person is happy
Testpool <- c(rep(0, nrow(LocationTable)))</pre>
## Create column for indvidual's testpool
Threshold <- c(rep(0, nrow(LocationTable)))</pre>
## Create column for indvidual's threshold
LocationTable <- cbind(Count, LocationTable, Happy, Testpool, Threshold)
## Add columns to Location Table
p <- qplot(x = LocationTable[,3], y = LocationTable[,4], col = ifelse(LocationTable[,2] ·
print(p)
testpoolR <- as.numeric(racialPreferenceTable[1,4])</pre>
## Pull m value for given race
thresholdR <- as.numeric(racialPreferenceTable[1,5])</pre>
```

```
##Pull j value for given race
testpoolG <- as.numeric(racialPreferenceTable[2,4])</pre>
thresholdG <- as.numeric(racialPreferenceTable[2,5])</pre>
testpoolB <- as.numeric(racialPreferenceTable[3,4])</pre>
thresholdB <- as.numeric(racialPreferenceTable[3,5])</pre>
for (individual in 1:nrow(LocationTable)){
  own_race <- LocationTable[individual,2]</pre>
  if(own_race == 1){
  ##If the point is red...
      testpool <- testpoolR</pre>
      ## Pull m value for individual given race
      threshold <- thresholdR
      ##Pull j value for indvidual given race
      LocationTable[individual,6] <- testpool</pre>
      LocationTable[individual,7] <- threshold</pre>
    if(own_race == 0){
    ##If the point is green...
      testpool <- testpoolG
      threshold <- thresholdG
      LocationTable[individual,6] <- testpool</pre>
      LocationTable[individual,7] <- threshold</pre>
    if(own_race == -1)
    ##If the point is blue...
      testpool <- testpoolB
      threshold <- thresholdB
      LocationTable[individual,6] <- testpool</pre>
      LocationTable[individual,7] <- threshold</pre>
```

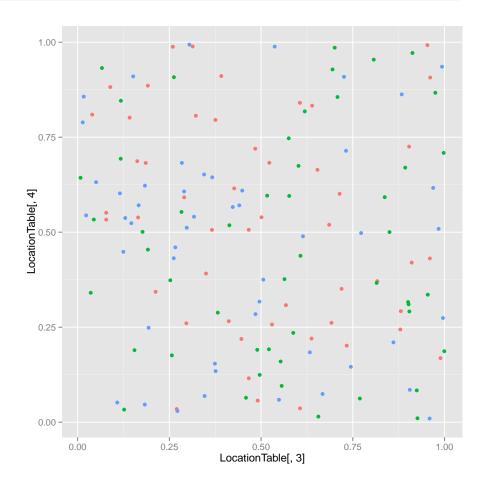
```
print(LocationTable)
 maxtestnumb <- max(testpoolR, testpoolG, testpoolB)</pre>
 #Finding max testpool value so we can create neighborlist outside loop
 LoopUnhappyLocationTable <- LocationTable
 justXYtable = LocationTable[,3:4]
  #Make seperate table with just X & Y coordinate for
  #nearest neighbor function
 neighborList <- get.knn(data = justXYtable, k = maxtestnumb)$nn.index</pre>
  ## Create matrix of m closest neighbors for each point
 print(neighborList)
 bad_neighbors <- 0</pre>
 good_neighbors <- 0</pre>
  ##Initialize value for total number of neighbors evaluate
 cycles <- 0
while (((happy_counter/n) < stop.val) & (cycles < cyclemax)){</pre>
     NumUnhappy <- nrow(LoopUnhappyLocationTable)</pre>
     cycles <- cycles + 1
     happy_counter<- sum((LocationTable[,5]), 1)</pre>
     for (individual in (1:NumUnhappy)){
     ##For a point in the location table...
       for (neighbor in 1:(LocationTable[individual,6])){
       ## For each closest neighbor of the given point
         neighborList <- neighborList[,1:LocationTable[individual,6]]</pre>
         ##Get rid of extraneous neighbors who are ranked lower than
         ## k closest
         a_neighbor <- neighborList[individual,neighbor]</pre>
```

```
## Find numerical value of neighboor in Location matrix
a_neighbors_race <- LocationTable[a_neighbor,1]</pre>
 ## Find neighbor's race
good_neighbors <- 0</pre>
##Initialize number of neighbors individual is happy with
bad_neighbors <- 0</pre>
## Initialize number of neighbors individual is unhappy with
   while ((bad_neighbors + good_neighbors) < (LocationTable[individual,6])){</pre>
     if (a_neighbors_race == own_race){
     good_neighbors <- goodneighbors + 1</pre>
       if ((good_neighbors + bad_neighbors) == (LocationTable[individual,6])){
         LocationTable[individual,5] = 1
         LoopUnhappyLocationTable = LoopUnhappyLocationTable[-individual,]
     if (a_neighbors_race != own_race){
       bad_neighbors <- bad_neighbors + 1</pre>
       ## If a neighbor's race is different from individual's,
       ## increase number of bad neighbors
         if (bad_neighbors > (LocationTable[individual,7])){
         ##If the number of bad neighbors exceeds threshold...
           new_x <- runif(1, min=0, max=1)</pre>
           new_y <- runif(1, min=0, max=1)</pre>
           LocationTable[individual,3] <- new_x</pre>
           LocationTable[individual,4] <- new_y
           LoopUnhappyLocationTable[individual,3] <- new_x
           LoopUnhappyLocationTable[individual,4] <- new_y</pre>
```

```
p <- qplot(x = LocationTable[,3], y = LocationTable [,4], col =
   if (cycles %% 5 == 0) {print(p)}
}

out <- c(cycles, happy_counter)
   return(out)
   print(p)
}

Schelling(testRacialPreferenceTable)</pre>
```



| ## | | Count | | | | Happy | Testpool | Threshold |
|----|----|-------|---|------------|-------------|-------|----------|-----------|
| ## | R. | 1 | 1 | 0.88087670 | 0.292274361 | 0 | 5 | 2 |
| ## | | 2 | | | 0.539329507 | 0 | 5 | 2 |
| ## | R. | 3 | | | 0.391174800 | 0 | 5 | 2 |
| | R | 4 | | | 0.350873383 | 0 | 5 | 2 |
| | R | 5 | | | 0.506259974 | 0 | 5 | 2 |
| | R | 6 | | | 0.795474492 | 0 | 5 | 2 |
| ## | | 7 | | | 0.719710088 | 0 | 5 | 2 |
| ## | | 8 | | | 0.686906370 | 0 | 5 | 2 |
| ## | | 9 | | | 0.885605896 | 0 | 5 | 2 |
| ## | | 10 | | | 0.600972072 | 0 | 5 | 2 |
| ## | R. | 11 | 1 | 0.60577097 | 0.840487010 | 0 | 5 | 2 |
| ## | R | 12 | 1 | 0.63742605 | 0.220050183 | 0 | 5 | 2 |
| ## | R | 13 | 1 | 0.03969718 | 0.809529376 | 0 | 5 | 2 |
| ## | R | 14 | 1 | 0.69181073 | 0.261534572 | 0 | 5 | 2 |
| ## | R | 15 | 1 | 0.65363839 | 0.664152477 | 0 | 5 | 2 |
| ## | R | 16 | 1 | 0.63901260 | 0.833021256 | 0 | 5 | 2 |
| ## | R | 17 | 1 | 0.52979992 | 0.257004289 | 0 | 5 | 2 |
| ## | R | 18 | 1 | 0.98889149 | 0.168652831 | 0 | 5 | 2 |
| ## | R | 19 | 1 | 0.42661108 | 0.615167781 | 0 | 5 | 2 |
| ## | R | 20 | 1 | 0.87949560 | 0.244099568 | 0 | 5 | 2 |
| ## | R | 21 | 1 | 0.31329813 | 0.988823090 | 0 | 5 | 2 |
| ## | R | 22 | 1 | 0.41195102 | 0.265774416 | 0 | 5 | 2 |
| ## | R | 23 | 1 | 0.25931412 | 0.987915983 | 0 | 5 | 2 |
| ## | R | 24 | 1 | 0.73325532 | 0.201447914 | 0 | 5 | 2 |
| ## | R | 25 | 1 | 0.07781230 | 0.533021456 | 0 | 5 | 2 |
| ## | R | 26 | 1 | 0.96087329 | 0.906998900 | 0 | 5 | 2 |
| ## | R | 27 | 1 | 0.56762140 | 0.308037600 | 0 | 5 | 2 |
| ## | R | 28 | 1 | 0.81676286 | 0.371100862 | 0 | 5 | 2 |
| ## | R | 29 | 1 | 0.46643300 | 0.115485445 | 0 | 5 | 2 |
| ## | R | 30 | 1 | 0.91045513 | 0.420044321 | 0 | 5 | 2 |
| ## | R | 31 | 1 | 0.95330606 | 0.992173342 | 0 | 5 | 2 |
| ## | R | 32 | 1 | 0.21233086 | 0.343192349 | 0 | 5 | 2 |
| ## | R | 33 | 1 | 0.60603245 | 0.036496113 | 0 | 5 | 2 |
| ## | R | 34 | 1 | 0.49077000 | 0.056881471 | 0 | 5 | 2 |
| ## | R | 35 | 1 | 0.07772721 | 0.551119528 | 0 | 5 | 2 |
| ## | R | 36 | _ | | 0.682729156 | 0 | 5 | 2 |
| ## | R | 37 | | | 0.219016305 | 0 | 5 | 2 |
| ## | | 38 | | | 0.034623944 | 0 | 5 | 2 |
| ## | | 39 | | | 0.538759632 | 0 | 5 | 2 |
| ## | | 40 | | | 0.591719521 | 0 | 5 | 2 |
| ## | | 41 | | | 0.506071298 | 0 | 5 | 2 |
| ## | | 42 | | | 0.430965685 | 0 | 5 | 2 |
| ## | | 43 | | | 0.682198081 | 0 | 5 | 2 |
| ## | R | 44 | 1 | 0.29617673 | 0.260350465 | 0 | 5 | 2 |
| | | | | | | | | |

| ## | R | 45 | 1 | 0.08887899 | 0.881948053 | 0 | 5 | 2 |
|----|----|----|---|------------|-------------|---|---|---|
| ## | R | 46 | | | 0.801370089 | 0 | 5 | 2 |
| ## | R. | 47 | _ | | 0.806377763 | 0 | 5 | 2 |
| ## | R. | 48 | | | 0.519523249 | 0 | 5 | 2 |
| ## | R. | 49 | | | 0.910894458 | 0 | 5 | 2 |
| ## | R. | 50 | | | 0.725260953 | 0 | 5 | 2 |
| ## | G | 51 | _ | | 0.288304984 | 0 | 5 | 2 |
| ## | G | 52 | | | 0.437951637 | 0 | 5 | 2 |
| ## | G | 53 | | | 0.553282319 | 0 | 5 | 2 |
| ## | G | 54 | - | | 0.335656283 | 0 | 5 | 2 |
| ## | G | 55 | | | 0.062349494 | 0 | 5 | 2 |
| ## | G | 56 | | | 0.985571126 | 0 | 5 | 2 |
| ## | G | 57 | | | 0.291436276 | 0 | 5 | 2 |
| ## | G | 58 | | | 0.866844861 | 0 | 5 | 2 |
| ## | G | 59 | | | 0.747099884 | 0 | 5 | 2 |
| ## | G | 60 | | | 0.376455617 | 0 | 5 | 2 |
| ## | G | 61 | | | 0.596139638 | 0 | 5 | 2 |
| ## | G | 62 | | | 0.175912370 | 0 | 5 | 2 |
| ## | G | 63 | - | | 0.500281350 | 0 | 5 | 2 |
| ## | G | 64 | | | 0.191887318 | 0 | 5 | 2 |
| ## | G | 65 | 0 | 0.99933825 | 0.186784270 | 0 | 5 | 2 |
| ## | G | 66 | 0 | 0.90205565 | 0.310173962 | 0 | 5 | 2 |
| ## | G | 67 | 0 | 0.11732077 | 0.693351585 | 0 | 5 | 2 |
| ## | G | 68 | 0 | 0.15488647 | 0.189495955 | 0 | 5 | 2 |
| ## | G | 69 | 0 | 0.90067305 | 0.316219866 | 0 | 5 | 2 |
| ## | G | 70 | 0 | 0.45880769 | 0.064337363 | 0 | 5 | 2 |
| ## | G | 71 | 0 | 0.92430297 | 0.083698585 | 0 | 5 | 2 |
| ## | G | 72 | 0 | 0.41358364 | 0.518244113 | 0 | 5 | 2 |
| ## | G | 73 | 0 | 0.81491619 | 0.366424271 | 0 | 5 | 2 |
| ## | G | 74 | 0 | 0.89288318 | 0.669900519 | 0 | 5 | 2 |
| ## | G | 75 | 0 | 0.83698380 | 0.592185493 | 0 | 5 | 2 |
| ## | G | 76 | 0 | 0.91252799 | 0.971544161 | 0 | 5 | 2 |
| ## | G | 77 | 0 | 0.49615943 | 0.124587787 | 0 | 5 | 2 |
| ## | G | 78 | 0 | 0.06626001 | 0.932025275 | 0 | 5 | 2 |
| ## | G | 79 | 0 | 0.19143956 | 0.454173630 | 0 | 5 | 2 |
| ## | G | 80 | 0 | 0.12666432 | 0.033178403 | 0 | 5 | 2 |
| ## | G | 81 | | | 0.159727750 | 0 | 5 | 2 |
| ## | G | 82 | | | 0.928274332 | 0 | 5 | 2 |
| ## | | 83 | | | 0.674556291 | 0 | 5 | 2 |
| ## | | 84 | | | 0.095542465 | 0 | 5 | 2 |
| ## | G | 85 | | | 0.500974125 | 0 | 5 | 2 |
| ## | | 86 | | | 0.235076410 | 0 | 5 | 2 |
| ## | | 87 | | | 0.595454185 | 0 | 5 | 2 |
| ## | | 88 | | | 0.373429720 | 0 | 5 | 2 |
| ## | G | 89 | 0 | 0.80710407 | 0.954102898 | 0 | 5 | 2 |

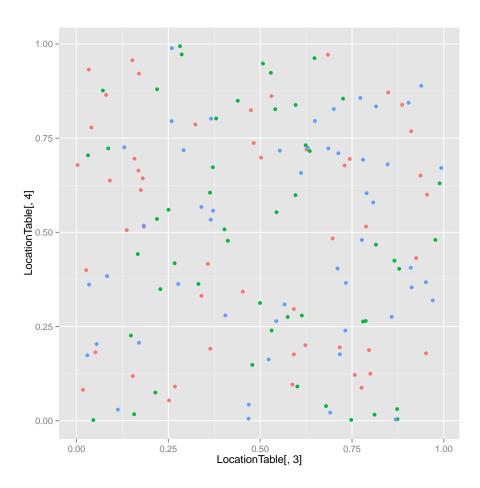
| ## | G | 90 | 0 | 0.11780056 | 0.845909939 | 0 | 5 | 2 |
|----|---|-----|----|------------|-------------|---|---|---|
| ## | G | 91 | 0 | 0.03558219 | 0.340554802 | 0 | 5 | 2 |
| ## | G | 92 | 0 | 0.92623339 | 0.010365395 | 0 | 5 | 2 |
| ## | G | 93 | 0 | 0.00783140 | 0.643187550 | 0 | 5 | 2 |
| ## | G | 94 | 0 | 0.48946651 | 0.190491560 | 0 | 5 | 2 |
| ## | G | 95 | 0 | 0.26242574 | 0.907880367 | 0 | 5 | 2 |
| ## | G | 96 | 0 | 0.61903045 | 0.817983840 | 0 | 5 | 2 |
| ## | G | 97 | 0 | 0.04407600 | 0.533258923 | 0 | 5 | 2 |
| ## | G | 98 | 0 | 0.65611025 | 0.014729884 | 0 | 5 | 2 |
| ## | G | 99 | 0 | 0.99759068 | 0.708671428 | 0 | 5 | 2 |
| ## | G | 100 | 0 | 0.70825015 | 0.855745154 | 0 | 5 | 2 |
| ## | В | 101 | -1 | 0.28403739 | 0.682381599 | 0 | 5 | 2 |
| ## | В | 102 | -1 | 0.49549380 | 0.317354294 | 0 | 5 | 2 |
| ## | В | 103 | -1 | 0.01665007 | 0.856748833 | 0 | 5 | 2 |
| ## | В | 104 | -1 | 0.36686837 | 0.644468423 | 0 | 5 | 2 |
| ## | В | 105 | -1 | 0.15136172 | 0.909936710 | 0 | 5 | 2 |
| ## | В | 106 | -1 | 0.99574788 | 0.274148161 | 0 | 5 | 2 |
| ## | В | 107 | -1 | 0.34591864 | 0.068874221 | 0 | 5 | 2 |
| ## | В | 108 | -1 | 0.73146704 | 0.714227306 | 0 | 5 | 2 |
| ## | В | 109 | -1 | 0.86064525 | 0.210119003 | 0 | 5 | 2 |
| ## | В | 110 | -1 | 0.96896713 | 0.616654244 | 0 | 5 | 2 |
| ## | В | 111 | -1 | 0.37609992 | 0.134423233 | 0 | 5 | 2 |
| ## | В | 112 | -1 | 0.53699035 | 0.988473766 | 0 | 5 | 2 |
| ## | В | 113 | -1 | 0.26198562 | 0.431435353 | 0 | 5 | 2 |
| ## | В | 114 | -1 | 0.44866089 | 0.609484812 | 0 | 5 | 2 |
| ## | В | 115 | -1 | 0.61410004 | 0.489205373 | 0 | 5 | 2 |
| ## | В | 116 | -1 | 0.48478954 | 0.284334196 | 0 | 5 | 2 |
| ## | В | 117 | -1 | 0.54874250 | 0.059020051 | 0 | 5 | 2 |
| ## | В | 118 | -1 | 0.12959936 | 0.537379685 | 0 | 5 | 2 |
| ## | В | 119 | -1 | 0.01384381 | 0.788933858 | 0 | 5 | 2 |
| ## | В | 120 | -1 | 0.14618622 | 0.523666771 | 0 | 5 | 2 |
| ## | В | 121 | -1 | 0.88337735 | 0.862787974 | 0 | 5 | 2 |
| ## | В | 122 | -1 | 0.26621716 | 0.459968218 | 0 | 5 | 2 |
| ## | В | 123 | -1 | 0.44061894 | 0.570699342 | 0 | 5 | 2 |
| ## | В | 124 | -1 | 0.77261437 | 0.497840131 | 0 | 5 | 2 |
| ## | В | 125 | -1 | 0.27200541 | 0.029366484 | 0 | 5 | 2 |
| ## | В | 126 | -1 | 0.34462786 | 0.651964305 | 0 | 5 | 2 |
| ## | В | 127 | -1 | 0.42271211 | 0.566269456 | 0 | 5 | 2 |
| ## | В | 128 | -1 | 0.11508901 | 0.602072069 | 0 | 5 | 2 |
| ## | В | 129 | -1 | 0.30451388 | 0.993687095 | 0 | 5 | 2 |
| ## | В | 130 | -1 | 0.16626382 | 0.570786456 | 0 | 5 | 2 |
| ## | В | 131 | -1 | 0.29007546 | 0.607338065 | 0 | 5 | 2 |
| ## | В | 132 | -1 | 0.37406760 | 0.154123175 | 0 | 5 | 2 |
| ## | | | | | 0.375157764 | 0 | 5 | 2 |
| ## | В | 134 | -1 | 0.18329200 | 0.622406428 | 0 | 5 | 2 |
| | | | | | | | | |

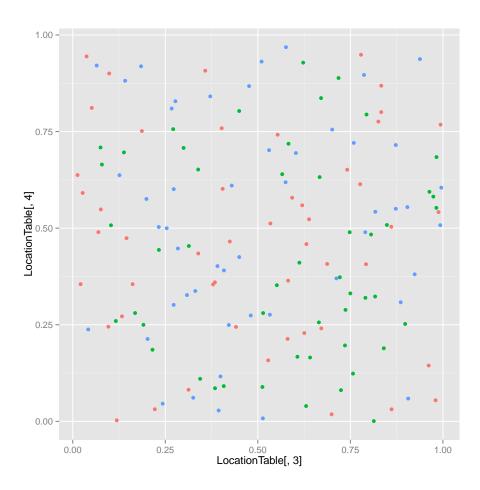
```
## B
        135 -1 0.12450300 0.448399968
                                               0
                                                         5
                                                                     2
## B
        136 -1 0.99320260 0.935470444
                                               0
                                                         5
                                                                     2
## B
        137 -1 0.90531437 0.085126241
                                               0
                                                         5
                                                                     2
                                                         5
                                                                     2
## B
        138 -1 0.10787591 0.051739027
                                               0
        139 -1 0.31719869 0.540758874
                                                         5
                                                                     2
## B
                                               0
## B
        140 -1 0.74466186 0.145718680
                                               0
                                                         5
                                                                     2
## B
        141 -1 0.95939913 0.009733661
                                                         5
                                                                     2
                                               0
                                                         5
                                                                     2
## B
        142 -1 0.98383691 0.508911631
                                               0
## B
        143 -1 0.19343030 0.248508668
                                               0
                                                         5
                                                                     2
                                                         5
                                                                     2
## B
        144 -1 0.02300792 0.544214905
                                               0
                                                                     2
## B
        145 -1 0.05023313 0.631581234
                                               0
                                                         5
## B
                                                         5
                                                                     2
        146 -1 0.18296334 0.046411481
                                               0
## B
        147 -1 0.29731931 0.511776394
                                                         5
                                                                     2
                                               0
## B
        148 -1 0.72596524 0.908810235
                                               0
                                                         5
                                                                     2
## B
        149 -1 0.66749887 0.074263743
                                                         5
                                                                     2
                                               0
## B
        150 -1 0.63282073 0.183889588
                                                         5
                                                                     2
##
           [,1] [,2] [,3] [,4] [,5]
##
      [1,]
             57
                   66
                         69
                               20
                                   109
##
      [2,]
              5
                   61
                        123
                             127
                                   114
      [3,]
            113
                   88
                         51
                              122
                                    41
##
      [4,]
                   73
                         28
                              52
                                    24
##
             14
##
      [5,]
              2
                   72
                        123
                             127
                                    41
##
      [6,]
             47
                   49
                          7
                              101
                                   126
##
      [7,]
             36
                   59
                        114
                              19
                                    83
##
      [8,]
             43
                   67
                        134
                              128
                                   130
##
      [9,]
            105
                   95
                         90
                              46
                                    45
##
    [10,]
             48
                   15
                        108
                              124
                                    75
##
    [11,]
             96
                         59
                              100
                                    82
                   16
    [12,]
                               24
##
            150
                   86
                         14
                                    81
##
    [13,]
            119
                  103
                         90
                               45
                                    46
##
    [14,]
             12
                   24
                          4
                              150
                                    86
##
    [15,]
             83
                   10
                        108
                               87
                                    59
##
    [16,]
             96
                   11
                        100
                               59
                                    82
##
    [17,]
            116
                   86
                         27
                                   102
                               64
    [18,]
                  106
                         71
                              137
##
             65
                                    20
##
    [19,]
                  123
                        127
                              104
            114
                                   126
##
    [20,]
            109
                    1
                         57
                               66
                                    69
##
    [21,]
            129
                   23
                         95
                               49
                                     9
    [22,]
                              102
                                    94
##
             51
                   37
                        116
##
    [23,]
            129
                   21
                         95
                                9
                                   105
##
    [24,]
            140
                   14
                         12
                             150
                                   109
##
    [25,]
             35
                   97
                        118
                              144
                                   120
##
    [26,]
             58
                  136
                         76
                               31
                                   121
##
    [27,]
                        102
             17
                   60
                               86
                                   116
##
    [28,]
             73
                    4
                         69
                                1
                                    66
```

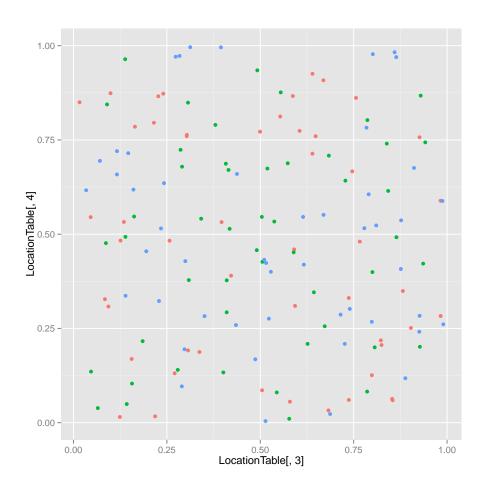
```
##
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              77
                    70
                           34
                                 94
                                       84
##
     [30,]
              42
                    54
                           63
                                 69
                                       28
     [31,]
              76
                   136
                           26
                                 58
                                      121
##
##
     [32,]
              88
                   143
                         113
                                 79
                                       44
##
     [33,]
              98
                   117
                         149
                                 84
                                       34
##
     [34,]
              70
                   117
                          29
                                77
                                       84
              25
                    97
                         118
##
     [35,]
                                144
                                      128
##
     [36,]
               7
                    83
                          59
                                 61
                                       87
                    22
     [37,]
                                       17
##
              94
                         116
                                 64
##
     [38,]
             125
                   107
                         146
                                 62
                                       80
                   130
##
     [39,]
             120
                         118
                                 85
                                      128
                         139
     [40,]
                                147
##
             131
                    53
                                      126
##
     [41,]
              72
                   139
                         147
                                127
                                       53
     [42,]
              30
                   142
                          54
                                 69
                                       63
##
                   134
                           67
                                101
##
     [43,]
               8
                                      128
##
     [44,]
              51
                    62
                         143
                                 22
                                       32
     [45,]
                    78
                         105
                                103
                                       13
##
              90
##
     [46,]
              90
                    45
                           9
                                 13
                                      105
##
     [47,]
                6
                    95
                          49
                                101
                                        9
     [48,]
                         124
                                 52
##
             115
                    10
                                       87
##
     [49,]
              21
                     6
                         129
                                47
                                       95
##
     [50,]
              74
                    99
                         110
                               121
                                       75
##
     [51,]
              22
                    44
                          37
                               116
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     [52,]
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                                       27
##
             115
                    60
                           48
##
     [53,]
             139
                    40
                         147
                               131
                                      122
##
     [54,]
              69
                    66
                           57
                               106
                                        1
     [55,]
             140
                   149
                           98
                               137
                                       24
##
                   148
##
     [56,]
              82
                           89
                                100
                                      112
     [57,]
                                 20
                                       54
##
              66
                      1
                           69
##
              26
                   136
                         121
                                 76
                                       31
     [58,]
##
                    96
                           36
                                  7
     [59,]
              83
                                       11
##
     [60,]
             133
                    27
                           52
                                102
                                      116
                2
##
     [61,]
                    87
                         114
                               123
                                       36
     [62,]
              44
                   143
                           68
                                132
                                      111
##
##
     [63,]
             124
                    75
                           30
                                 42
                                       28
##
     [64,]
              94
                    81
                           17
                                77
                                       86
##
     [65,]
              18
                   106
                           71
                                 20
                                      137
                    57
                                 54
                                       20
##
     [66,]
              69
                           1
     [67,]
               8
                    43
                               128
                                      134
##
                         145
##
     [68,]
             143
                    62
                         138
                                146
                                       44
     [69,]
              66
                    57
                                 54
                                       20
##
                           1
##
     [70,]
              34
                    29
                          77
                                117
                                       84
     [71,]
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                         141
                                 18
##
             137
                                       65
##
     [72,]
             127
                    41
                            5
                               123
                                        2
              28
                      4
                                 69
                                       66
##
     [73,]
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```

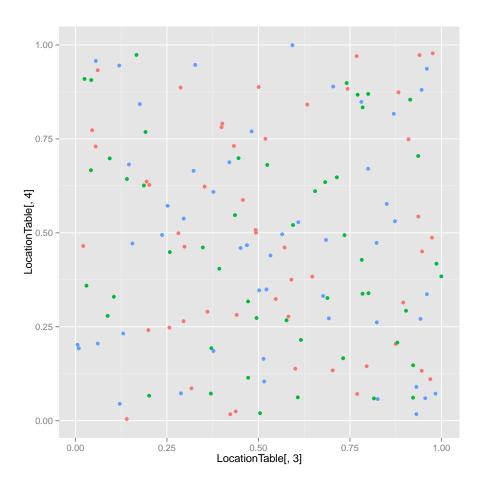
```
##
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                                     108
##
     [75,]
              63
                    74
                         124
                                10
                                     110
     [76,]
              31
                    26
                         136
                                     121
##
                                89
##
     [77,]
              29
                    94
                          84
                                81
                                      34
##
     [78,]
              45
                   105
                         103
                                90
                                       13
##
     [79,]
              85
                   135
                         113
                               122
                                     120
                   146
                          38
                               125
                                       68
##
     [80,]
             138
##
     [81,]
              64
                    84
                          77
                                94
                                       86
     [82,]
##
             148
                    56
                         100
                                16
                                      89
##
     [83,]
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                    59
                          36
                                87
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##
     [84,]
             117
                    81
                                34
                                       33
     [85,]
##
             120
                    39
                          79
                               118
                                     130
##
     [86,]
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                         150
                                27
                                       64
     [87,]
                    83
                           2
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                                       15
##
              61
                                  3
                                      79
##
     [88,]
              32
                   113
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##
     [89,]
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                    76
                          56
                                82
                                     121
              45
                                  9
                                       13
##
     [90,]
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                         105
##
     [91,]
             135
                    32
                         143
                                68
                                      79
##
     [92,]
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                                       18
     [93,]
                         128
##
             145
                   144
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##
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                          77
                                81
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##
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##
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                               100
                                      82
                    25
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                                     145
##
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                         117
                                55
                                      84
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##
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                                     121
   [100,]
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                                96
##
             148
                    16
                                       11
   [101,]
##
             126
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                               104
                                       43
   [102,]
                          17
                                27
                                       60
##
             116
                   133
                   119
                                      90
## [103,]
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                                78
## [104,]
             126
                    19
                         131
                               114
                                     101
##
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                                       46
## [106,]
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                                66
                                       69
## [107,]
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                         125
                                       70
             111
                               132
## [108,]
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                          83
                               100
              15
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## [109,]
              20
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                                66
                                       69
## [110,]
              74
                    99
                         142
                                50
                                       75
                          29
                                70
## [111,]
             132
                   107
                                       37
   [112,]
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                                82
##
              11
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                                       16
##
   [113,]
             122
                    88
                          79
                               147
                                        3
                                        2
              19
                   123
                                61
##
   [114,]
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## [115,]
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                    48
                          87
                                60
                                        2
## [116,]
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                          22
                                37
                                       27
             102
## [117,]
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                                       70
              84
                         130
                                       35
## [118,]
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                    39
                                25
```

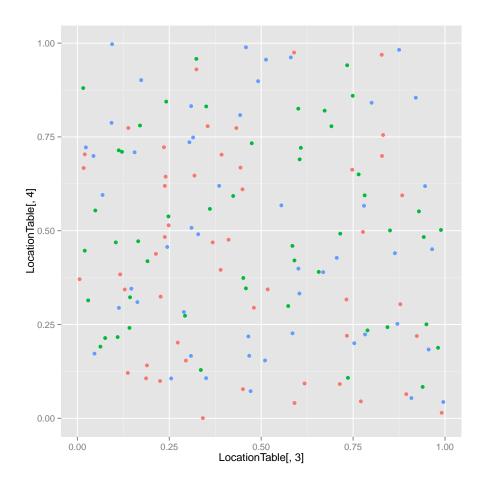
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## [120,]
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                              130
                                    25
## [121,]
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                   58
                         76
                               89
                                   136
## [122,]
            113
                  147
                         79
                               88
                                    53
## [123,]
            127
                  114
                         19
                               72
                                      2
## [124,]
             63
                   48
                         75
                               10
                                    28
## [125,]
             38
                               80
                                     62
                  107
                        146
## [126,]
            104
                  101
                        131
                               40
                                     19
## [127,]
            123
                   72
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                         19
                              114
## [128,]
            130
                   35
                        118
                              134
                                   145
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                         95
                                      9
## [129,]
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## [130,]
             39
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                  118
                              134
                                   128
## [131,]
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                   53
                        126
                              139
                                   101
## [132,]
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                  107
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                               29
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                  102
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                                     52
## [133,]
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                              116
## [134,]
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                              128
                                    39
## [135,]
             79
                                    25
                   85
                        120
                              118
## [136,]
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                               76
                                   121
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## [137,]
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                               18
                                   109
## [138,]
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                                   125
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## [139,]
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                               41
                                   131
## [140,]
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                              150
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## [141,]
             92
                   71
                        137
                               18
                                     65
## [142,]
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             42
                  110
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                               63
## [143,]
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                   62
                         32
                               44
                                    88
                   35
                         25
## [144,]
             97
                              145
                                    93
## [145,]
             93
                  128
                         35
                               67
                                   144
## [146,]
             80
                  138
                         38
                              125
                                    68
## [147,]
                        122
                               41
                                    40
            139
                   53
                  100
                         56
                                     16
## [148,]
             82
                               89
## [149,]
             98
                   33
                              140
                         55
                                    84
## [150,]
             12
                   86
                         81
                                     24
                               14
```

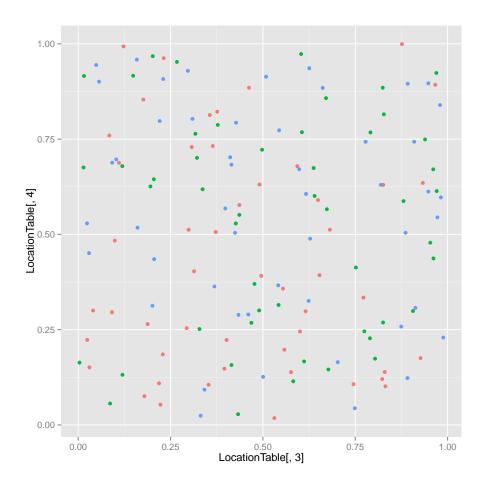


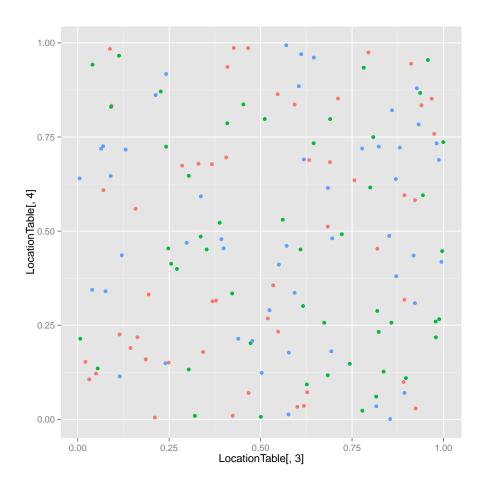


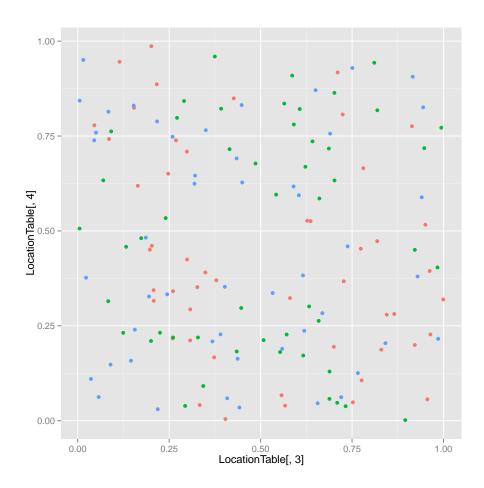


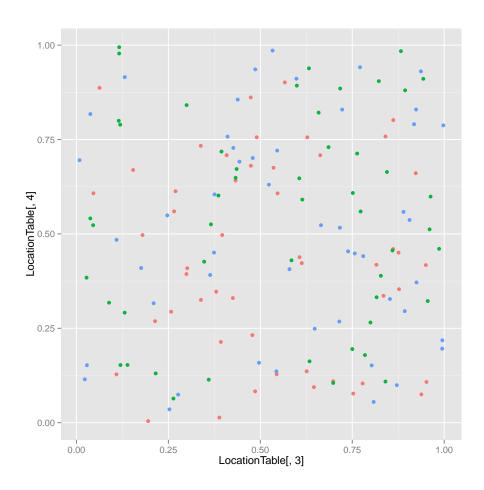


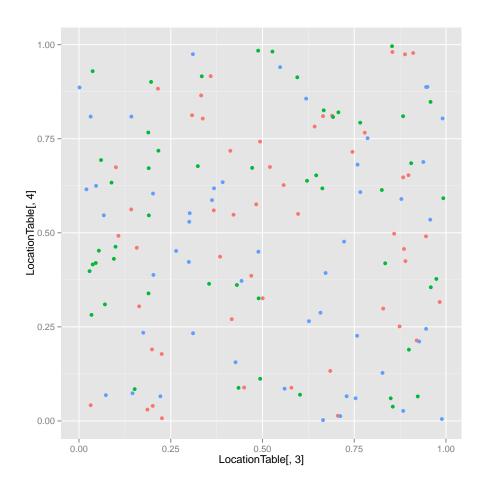


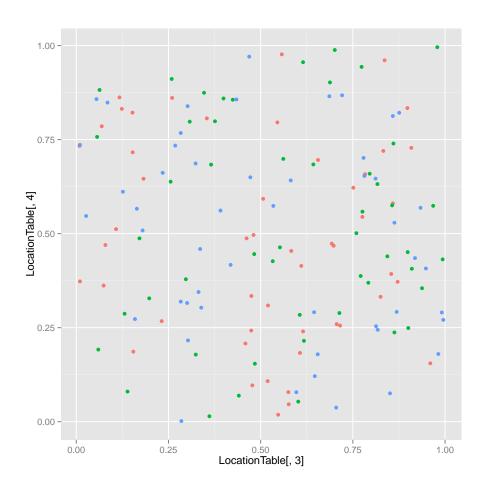


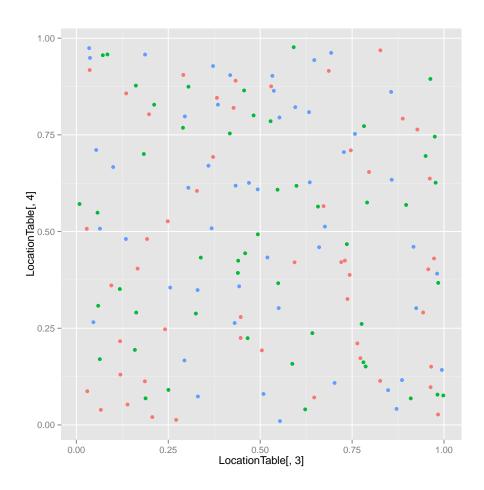


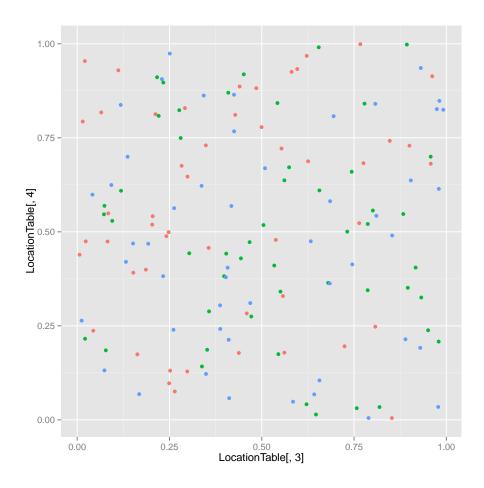


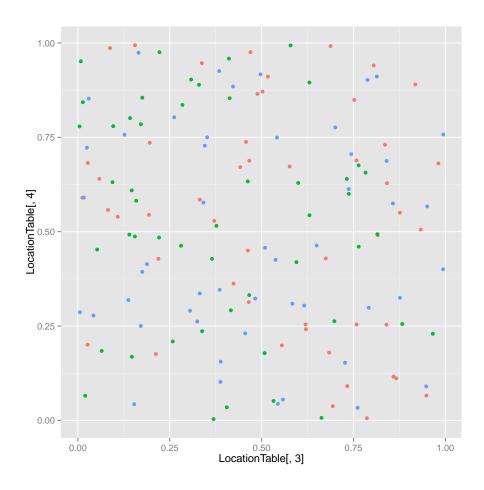


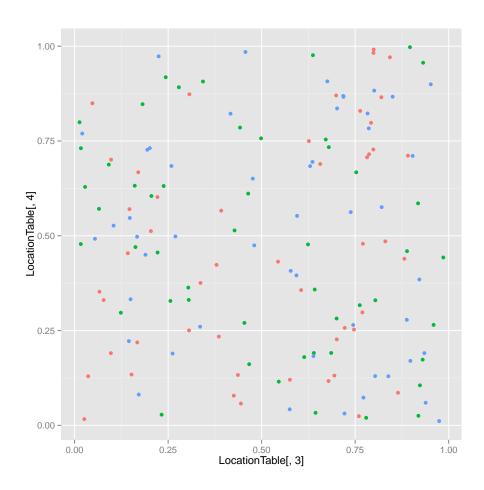


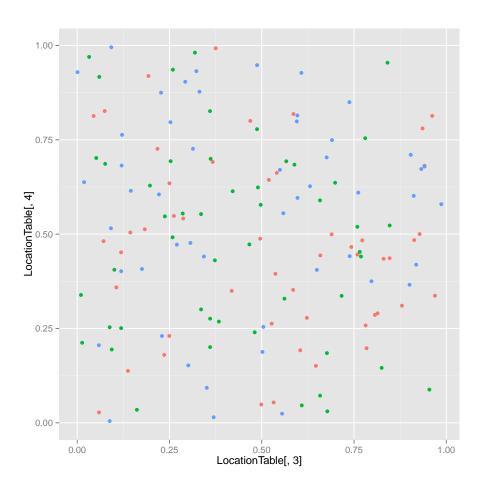


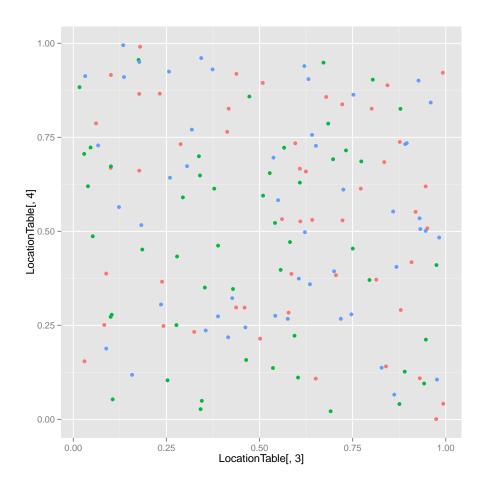


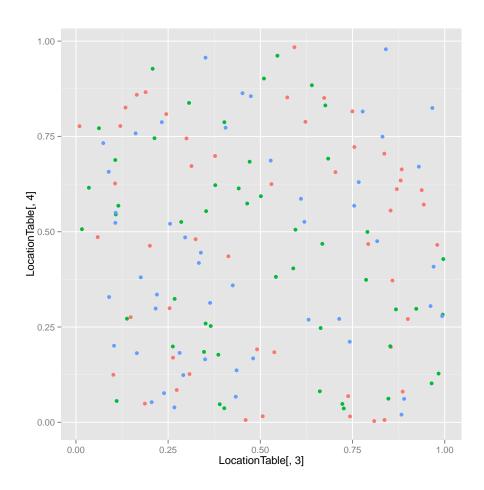


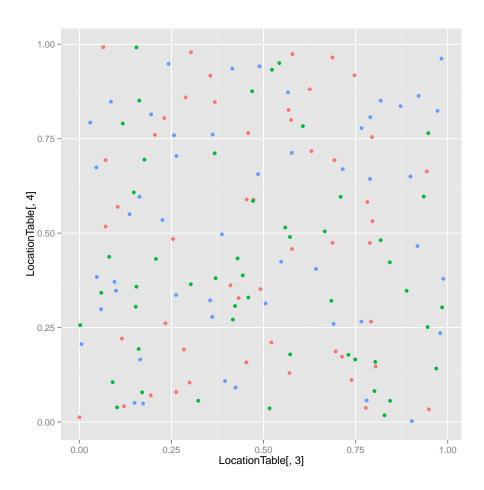


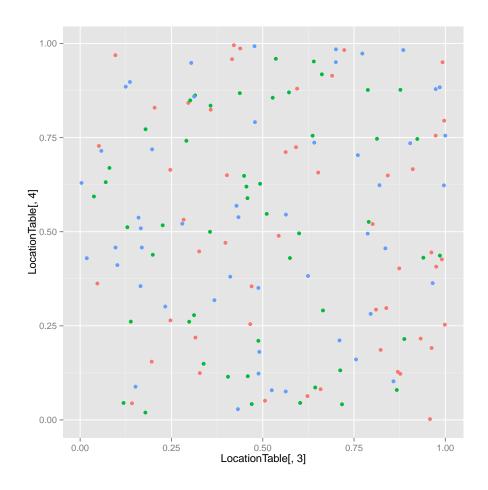












```
## [1] 100 1
# print(system.time(Schelling(testRacialPreferenceTable)))
```

2 Code Review

2.1 Sketch model that code is based on