

## Assignment 9

### Advanced Mathematical Techniques in Chemical Engineering (CH 61015)

Full Marks: 30

Solve the following PDEs using Green's function method

1.

$$\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial x^2} + t$$

$$\text{At } t=0, u=1, \text{ at } x=0, \frac{\partial u}{\partial x} = 1, \text{ at } x=1, u=0$$

2.

$$\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = xy$$

$$\text{At } x=0, \frac{\partial u}{\partial x} = 1, \text{ at } x=1, u=0; \text{ at } y=0, u=2 \text{ and at } y=1, \frac{\partial u}{\partial y} + y = 0$$

$$3. \frac{\partial^2 u}{\partial t^2} + \frac{\partial^2 u}{\partial x^2} = t$$

$$\text{At } t=0, \frac{\partial u}{\partial t} = 1 \text{ and } u=2, \text{ at } x=0, \frac{\partial u}{\partial x} = 0; \text{ at } x=1, u=0$$