

**Indian Institute of Technology Kharagpur**

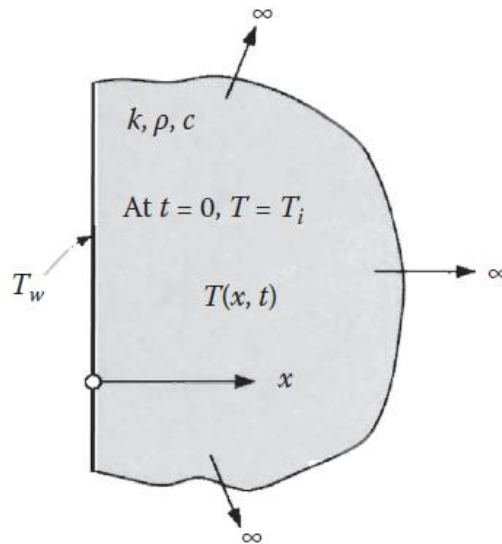
**Department of Chemical Engineering**

**Advanced Heat Transfer CH61014 (Spring 2025)**

**Assignment**

1. A slab, extending from  $x = 0$  to  $x = L$  and of infinite extent in the  $y$  and  $z$  directions, is initially at a uniform temperature  $T_i$ . For times  $t \geq 0$ , a constant heat flux  $q''$ , is applied to the surface at  $x = L$ , while the surface at  $x = 0$  is kept perfectly insulated. Assume that the thermo-physical properties of the slab are constant. Obtain an expression for the unsteady-state temperature distribution  $T(x, t)$  in the slab for  $t > 0$  using
  - a) Separation of Variables
  - b) Integral Transform Technique
  
2. A long solid cylinder of constant thermo-physical properties and radius  $r_0$  is initially at a uniform temperature  $T_i$ . For times  $t \geq 0$ , a constant heat flux  $q''$  is applied to the peripheral surface at  $r = r_0$ . Obtain an expression for the unsteady-state temperature distribution  $T(r, t)$  in the cylinder for  $t > 0$  using
  - a) Separation of Variables
  - b) Integral Transform Technique
  
3. A solid sphere,  $0 \leq r \leq r_0$ , of constant thermo-physical properties is initially at a uniform temperature  $T_i$ . For times  $t \geq 0$ , the sphere is heated by applying a constant heat flux  $q''$  to its surface at  $r = r_0$ . Obtain an expression for the unsteady-state temperature distribution  $T(r, t)$  in the sphere for  $t > 0$  using
  - a) Separation of Variables
  - b) Integral Transform Technique

4. Consider a semi-infinite solid,  $0 \leq x < \infty$ , initially at a uniform temperature  $T_i$ . The surface temperature at  $x = 0$  is changed to and kept at a constant temperature  $T_w$  for times  $t \geq 0$ . Assume constant thermo-physical properties ( $k, \rho, c$ ). Obtain an expression for the unsteady-state temperature distribution  $T(x, t)$  in the slab using
- Finite Fourier Transform
  - Similarity Method



5. A slab of thickness  $L$  is initially at zero temperature. For times  $t > 0$ , the boundary surface at  $x = 0$  is kept at zero temperature, while the surface at  $x = L$  is subjected to a time-varying temperature  $f(t)$  defined by

$$f(t) = \begin{cases} bt & \text{for } 0 < t < \tau_1 \\ 0 & \text{for } t > \tau_1 \end{cases}$$

Assume constant thermo-physical properties ( $k, \rho, c$ ). Obtain an expression for the unsteady-state temperature distribution  $T(x, t)$  in the slab using Duhamel's Method.

6. A slab of thickness  $L$  is initially at zero temperature. For times  $t > 0$ , the boundary surface at  $x = L$  is kept insulated, while the surface at  $x = 0$  is subjected to a time-dependent heat flux  $f(t)$  of the functional form:

$$-k \left. \frac{\partial T}{\partial x} \right|_{x=0} = f(t) \equiv \begin{cases} t & \text{for } 0 < t < \tau_1 \\ 0 & \text{for } t > \tau_1 \end{cases}$$

Assume constant thermo-physical properties ( $k, \rho, c$ ). Using Duhamel's theorem, develop an expression for the temperature distribution  $T(x, t)$  in the slab for times:

(i)  $t < \tau_1$  and for (ii)  $t > \tau_1$ .

7. Consider a large solid,  $x \geq 0$ , initially at the fusion temperature  $T_f$ . At  $t = 0$ , the temperature of the boundary surface at  $x = 0$  is raised to  $T_0 (> T_f)$  and maintained at that constant temperature for times  $t > 0$ . Assume constant thermo-physical properties for the liquid phase, and neglect any convective motion in the melt.

- (a) Derive the expressions for the solid-liquid interface location as a function of time (Stefan Condition).  
 (b) Obtain exact expressions for both the temperature distribution in the liquid phase by  
 (i) Stefan's exact method and (ii) Integral method.

8. A slab, which extends from  $x = 0$  to  $x = L$ , is initially at a uniform temperature  $T_\infty$  at  $t = 0$ . For times  $t \geq 0$ , a plane heat source, of strength  $q''(t)$  ( $\text{W/m}^2$ ) and located normal to the  $x$ -direction at  $x = a$  within the slab, releases heat continuously, while the surface at  $x = 0$  is kept perfectly insulated and the surface at  $x = L$  dissipates heat by convection with a constant heat transfer coefficient  $h$  into a fluid medium maintained at the constant temperature  $T_\infty$ . Assuming constant thermo-physical properties for the slab, obtain an expression for the temperature distribution  $T(x, t)$  in the slab for  $t > 0$ .