

(1.) Extraction (Liquid-Liquid extraction)

(2.) Leaching

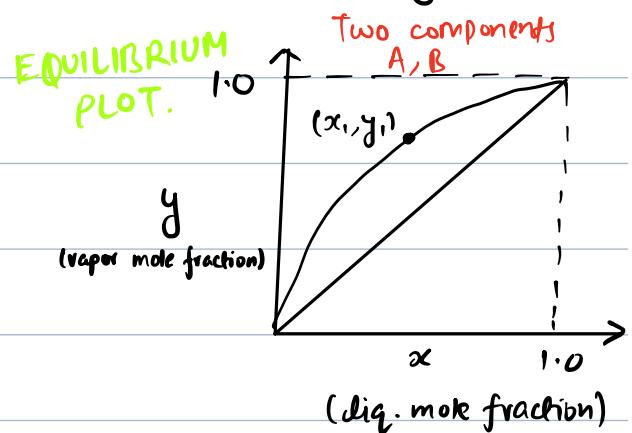
(3.) Adsorption

separation of 2 liquids \rightarrow for liquids that can't be separated by distillation.

Relative volatility (α)

= vapour pressure of the lower boiling (more volatile) comp.
vapour pressure of the higher boiling (less volatile) comp.

$$= \frac{y/x}{(1-y)/(1-x)} = \frac{y}{1-y} \times \frac{(1-x)}{x}$$



vapour pressure of a component = P_A / x_A

$$= \frac{P_1}{x_1} = \frac{y_1 P_T}{x_1}$$

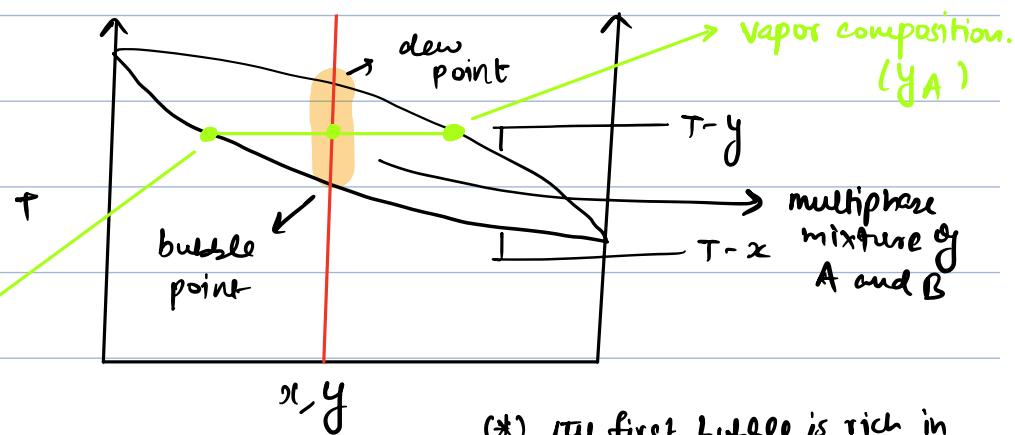
(*) Eq'n curve is drawn w.r.t the more volatile component.

(*)

A] Liquids - 60°C
B] Miscible - 100°C

50 : 50

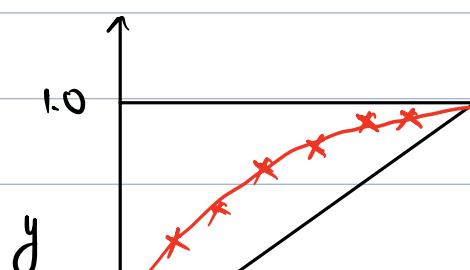
liquid composition (x_A)



(*) the first bubble is rich in more volatile component, but it is a mixture.

(*) (x_A, y_A) gives us a datapoint on the equilibrium plot.

(*)



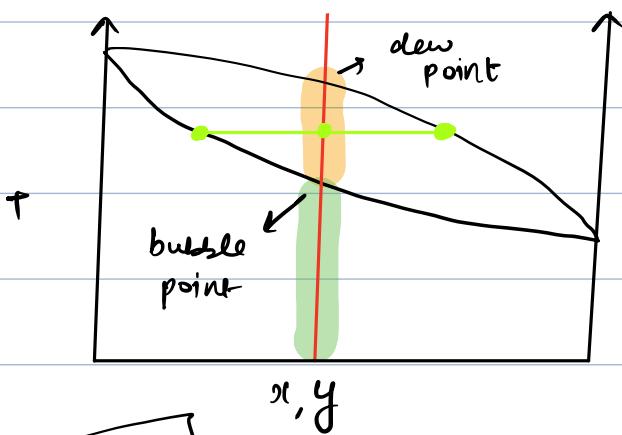
NOT AN ISOTHERMAL PLOT.



(*)

$$\text{liq. mix} \Rightarrow P = 1, C = 2 \quad (\text{phase}) \\ F = 3 \quad \text{Rule}$$

(temp., pressure, composition)

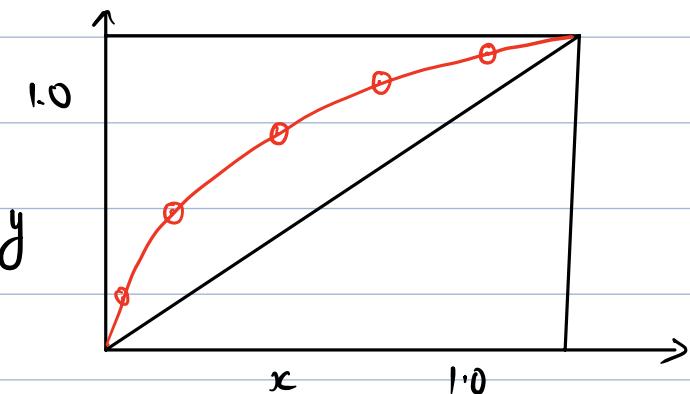


$$\text{Multiphase mix} \Rightarrow P = 2, C = 2 \\ F = 2$$

(temp., composition)

Pressure
constant

(*) What is an OPERATING LINE ?



Extraction

Distillation fails when $x \rightarrow 1.0$

Check:-

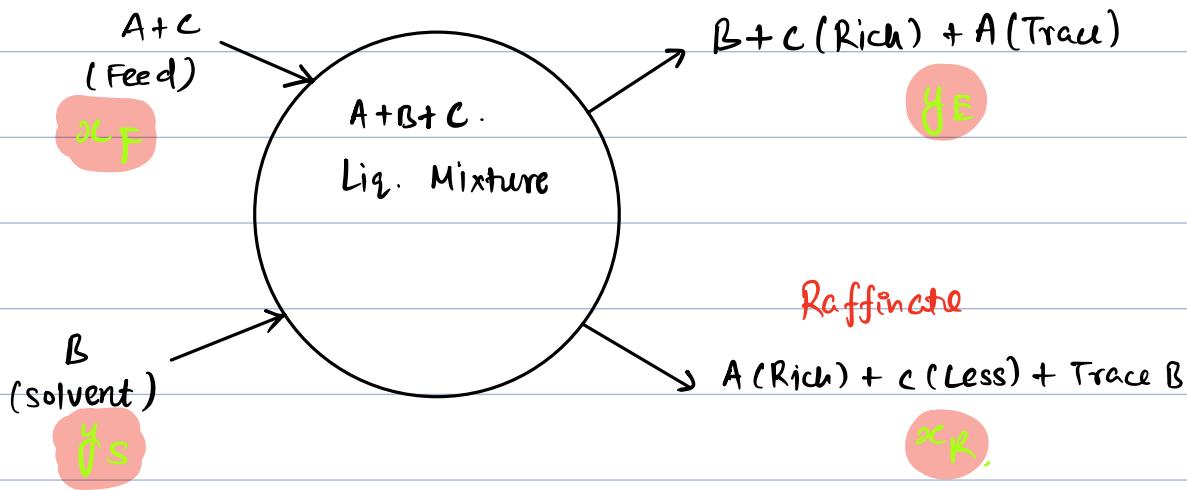
(ADU, VDU)

Atmospheric Distillation Unit
Vacuum Distillation Unit

Liq. mixture

A + e ; $C = \text{solute}$ (* This is the component you want to separate)

A = carrier



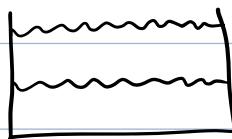
$A, C \rightarrow$ miscible ($C \downarrow$)

$B, C \rightarrow$ miscible ($C \uparrow$)

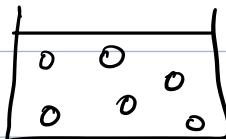
$A, B \rightarrow$ not miscible

Somehow B, C can be separated.

(*) Two immiscible liquids



$A + B$
(stratified layer)



$A + B$
(emulsification)

Whether A and B form a stratified layer OR

emulsification depends on 2 factors:-

① difference in density.

(dispersed phase)

② interfacial tension b/w 2 liquids.

↓
favoured when interfacial tension is HIGH.

Nomenclature:-

$x \rightarrow$ fraction of C in the Raffinate.

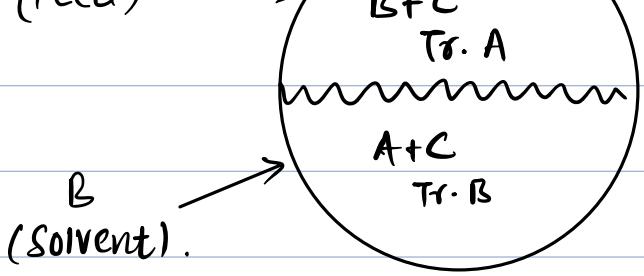
$y \rightarrow$ fraction of C in the Extract.

$$DOF = 4$$

$x, y \rightarrow$ liquid in the contact of extraction.

$A + C$
(Feed)

(*) After C gets mixed with B in

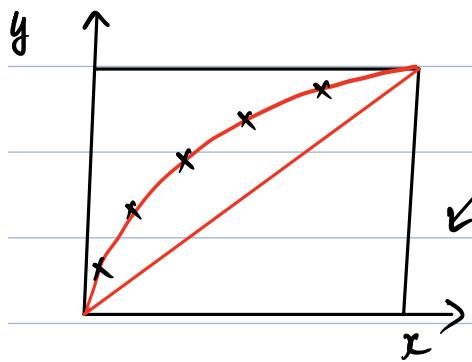


'B-C' mixture should also be immiscible with 'A-C' mixture.

(*) Relative density will decide which mixture is on top.

(*) we can separate using Decantation.

(#) $F = C - P + 2$ (GIBBS PHASE RULE).

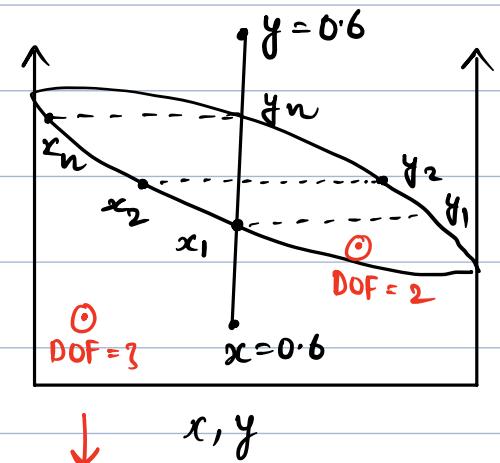


The ends of a tie-line

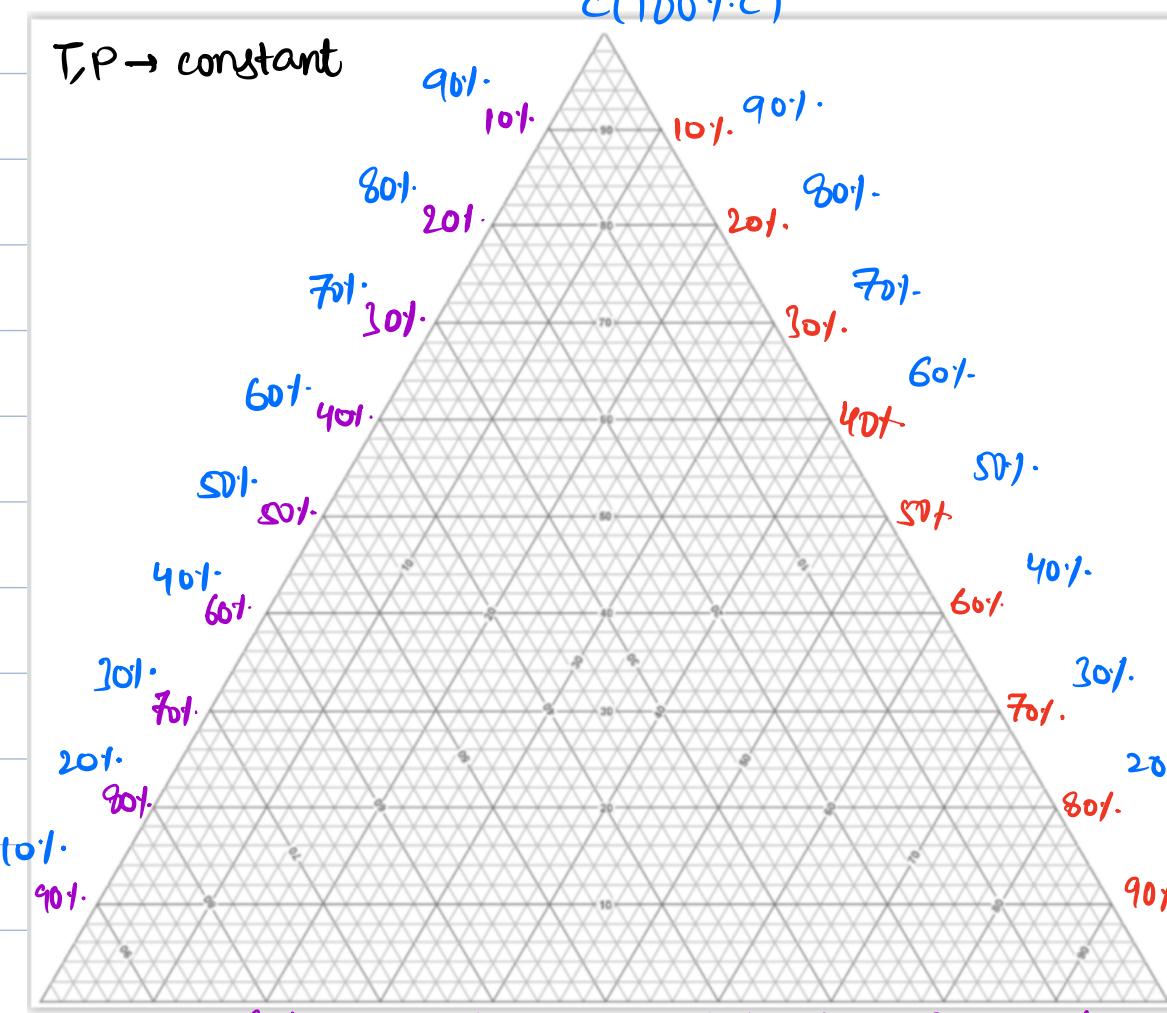
is translated
as a single point on
the x-y curve.

(All tie-lines are
at a different temp.)

Every (x,y) is at
a different temp.



This graph is at a
constant Pressure.



A(100%) A) 90% 80% 70% 60% 50% 40% 30% 20% 10%

10% 20% 30% 40% 50% 60% 70% 80% 90%

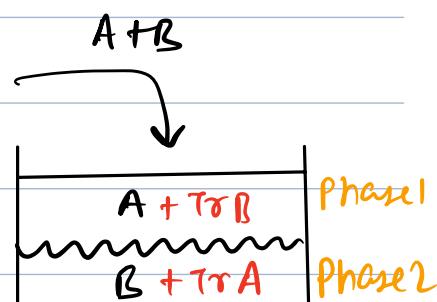
2 Immiscible Liquids :-

Assumption - (completely Immiscible)

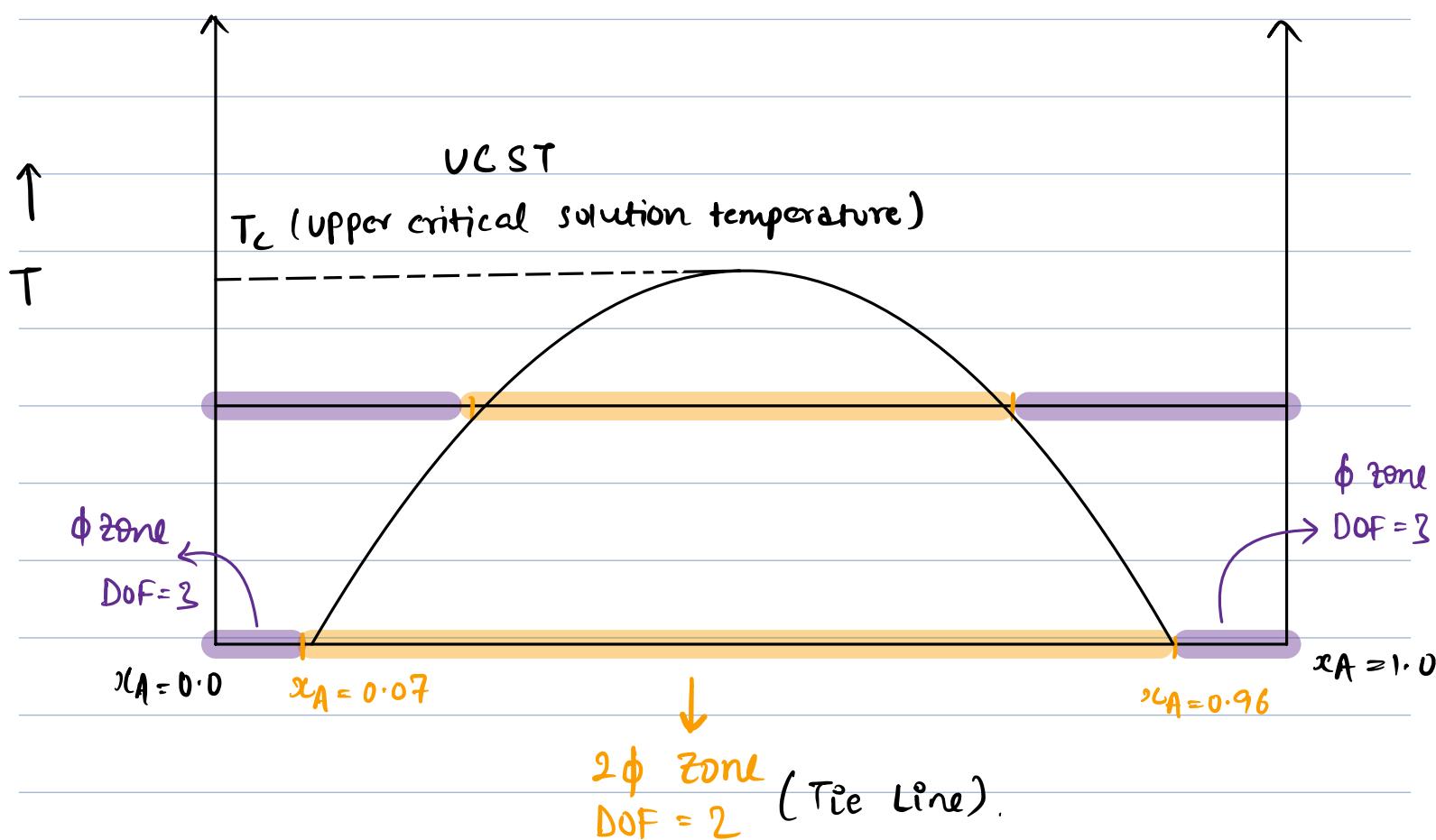
In reality 100% phase separation is impossible.

$$A \quad x_A \quad , \quad x_A + x_B = 1.0$$

$$B \quad x_B$$

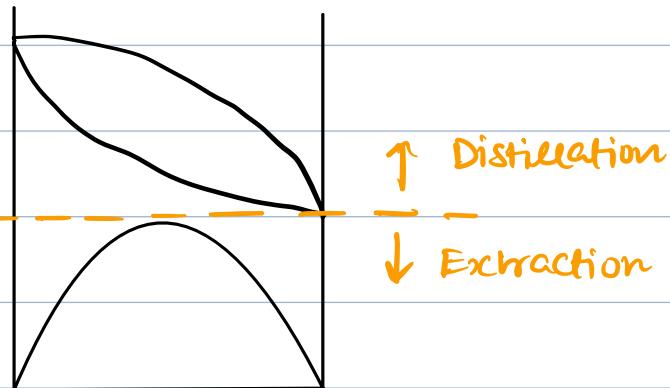


$$DOF = 2 + 2 - 2 = 2$$

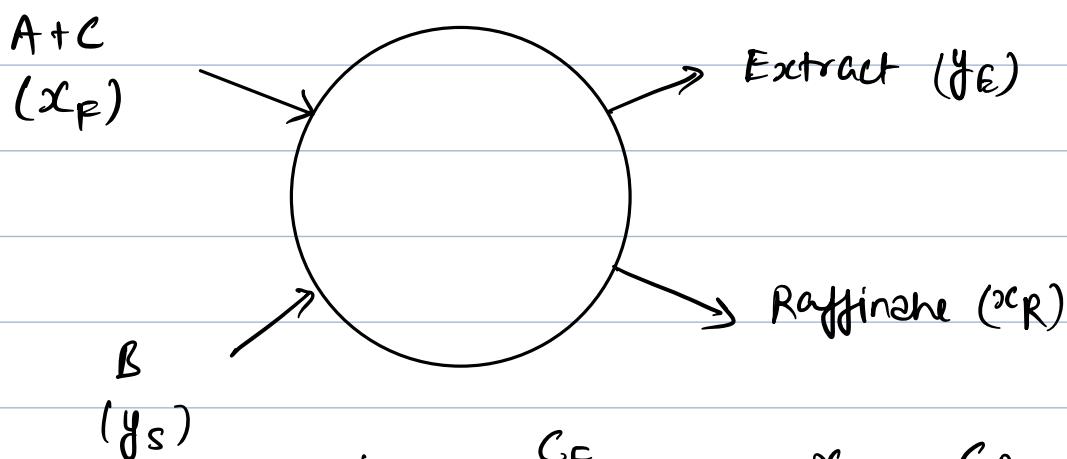


(*) With increase of temperature the region of insolubility decreases.
With $T \downarrow$, relative immiscibility increases.

complete picture



(*)



$$y_E = \frac{C_E}{A_E + B_E + C_E}, \quad x_R = \frac{C_R}{A_R + B_R + C_R}$$

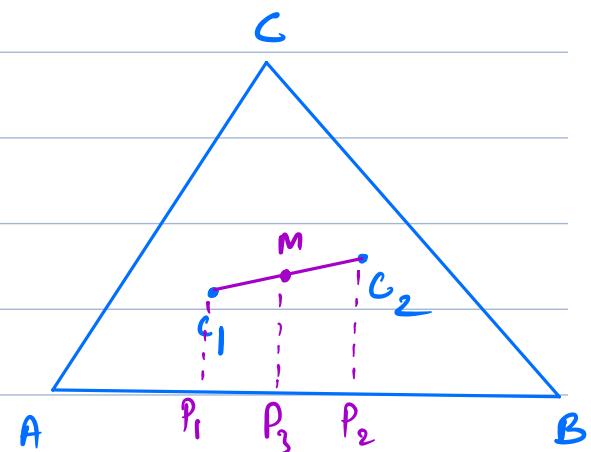
$y_E, x_R \rightarrow$ both fractions of C in liquid

(#)

$$\begin{aligned} c_1 &= x_1, L_1 \text{ kg} \\ c_2 &= x_2, L_2 \text{ kg} \end{aligned}$$

$$L_1 + L_2 = M$$

$$L_1 x_1 + L_2 x_2 = M x_M$$

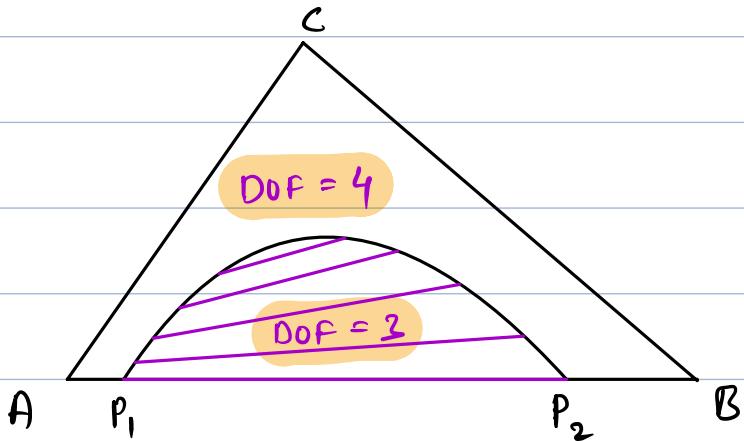


$$\Rightarrow M \cdot \overline{MP_3} = L_1 \overline{CP_1} + L_2 \overline{CP_2}$$

$$\Rightarrow (L_1 + L_2) \overline{MP_3} = L_1 \overline{CP_1} + L_2 \overline{CP_2}$$

$$\frac{L_1}{L_2} = \frac{\bar{M}_P_3 - \bar{C}_2 P_2}{\bar{C}_1 P_1 - \bar{M}_P_3} = \frac{x_2 - x_1}{x_M - x_1}$$

(#)



(#)

$$F \quad \left(\begin{array}{l} 70 \text{ kg} \\ x_F = 0.2 \end{array} \right)$$

$A + C$
 (x_F)

$F \quad (y_E)$

$R \quad (x_R)$

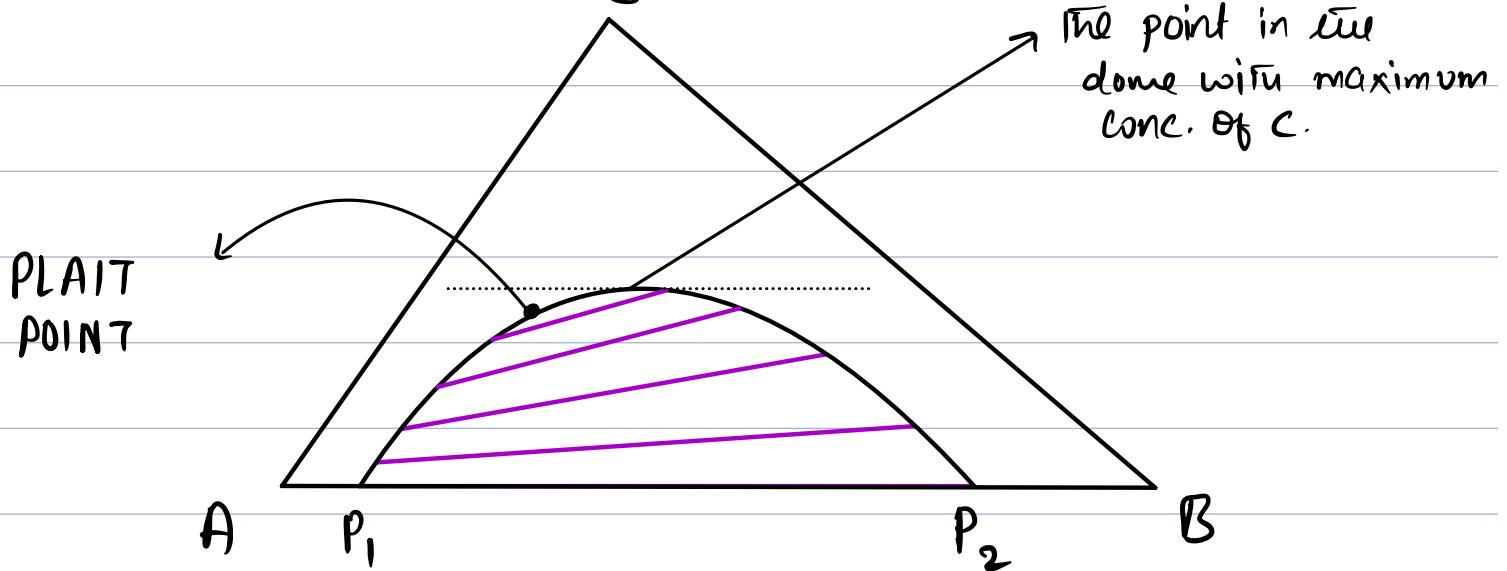
$$S = 40 \text{ kg} \quad S \quad y_S = 0 \quad (y_S)$$

$y_E > x_F \rightarrow \text{desired.}$

y_S should be ideally zero.
 x_R should be ideally zero.

y_E, x_R are in equilibrium.

(#)



As $C \uparrow$, region of immiscibility decreases.

(#)

$$M = F + S = 110 \text{ kg}$$

C Balance:

$$Mx_M = Fx_F + Sx_S \rightarrow 70 \times 0.2 = 110 x_M \Rightarrow x_M = \frac{14}{110}$$

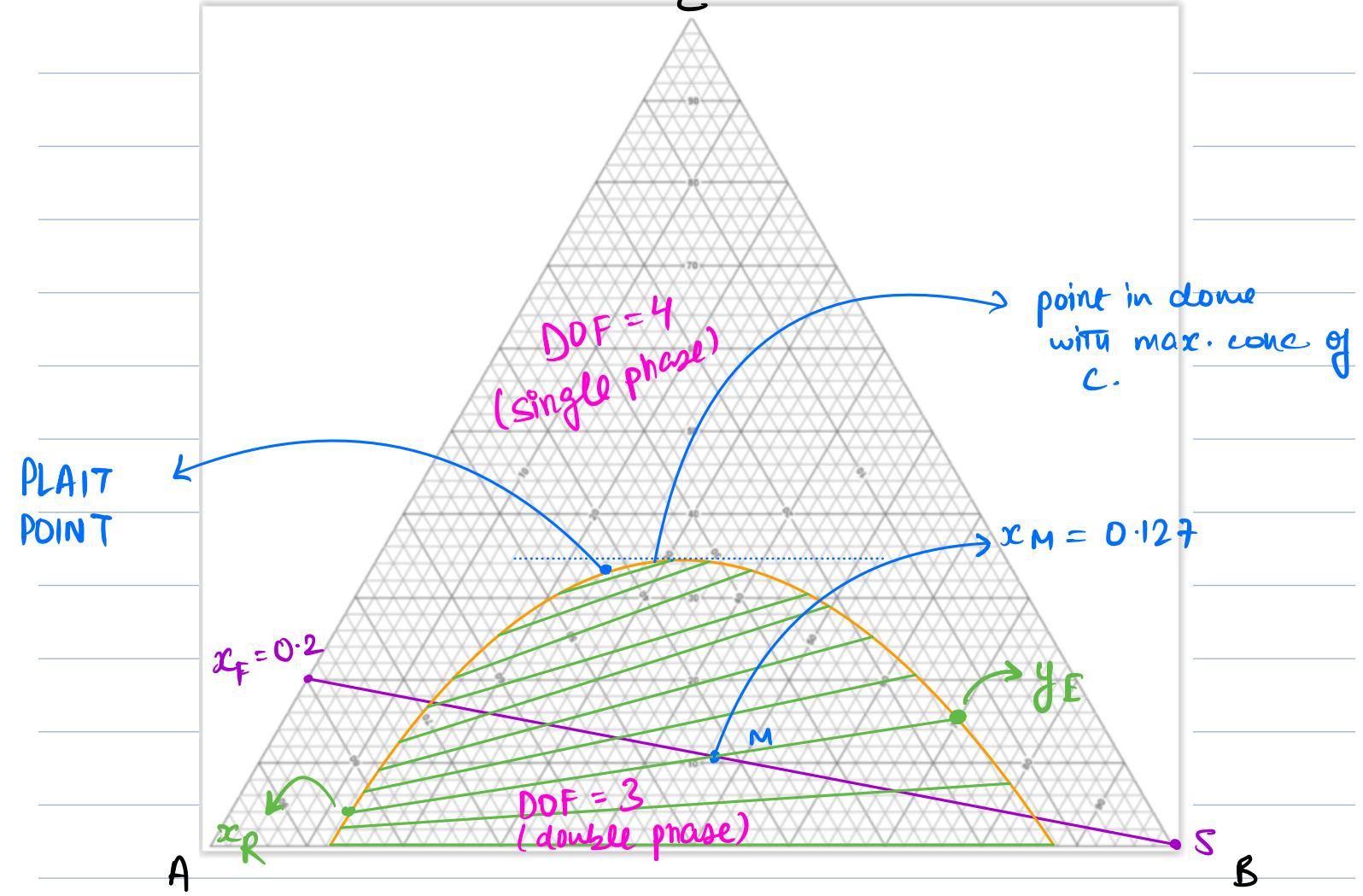
$x_M = 0.127$

(#)

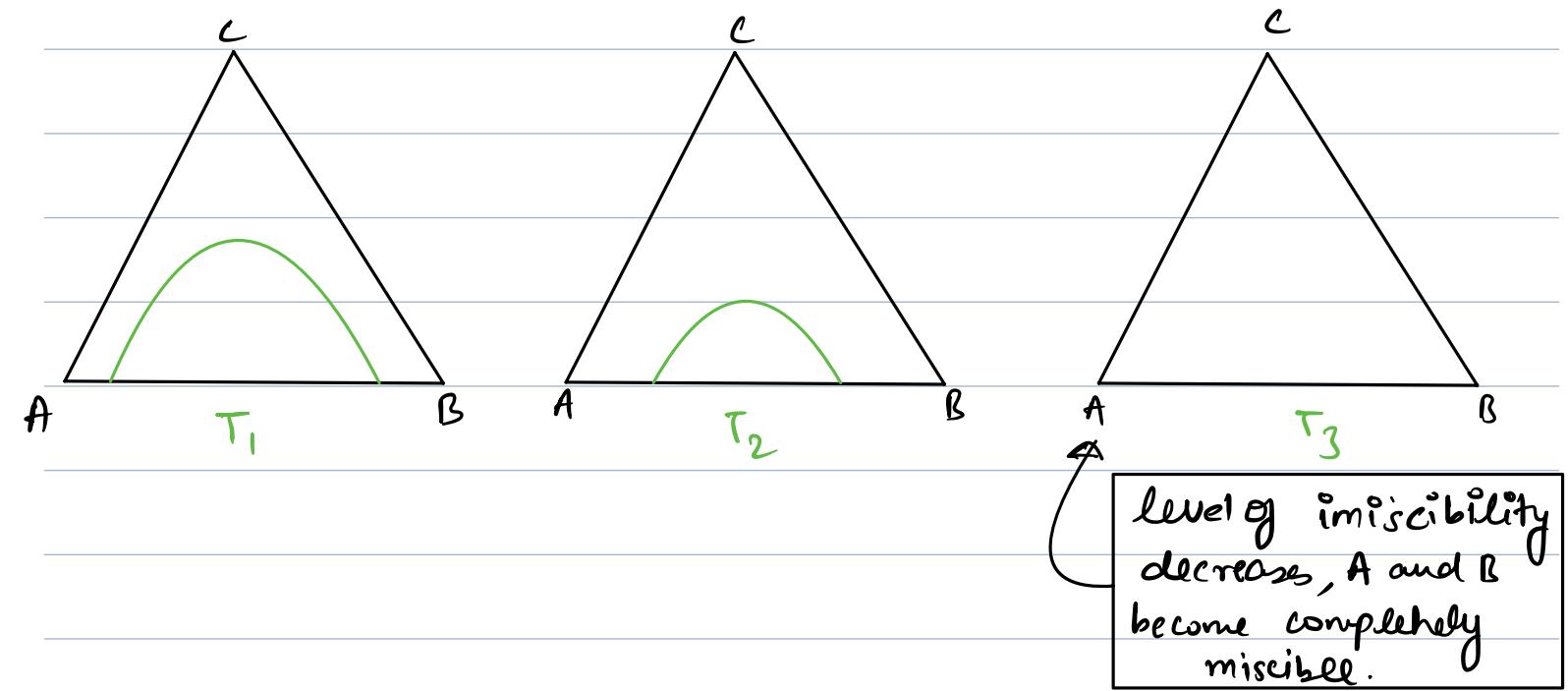
$\rightarrow M$ is inside the 2 phase region (dome of insolubility).

\rightarrow The two ends of the M-containing tie-line give the compositions of the two phases (A-rich) and (B-rich) in the 2-phase domain

\rightarrow Compositions INSIDE the dome are mathematical, the actual compositions of the two phases are given by the ends of the corresponding tie-line.

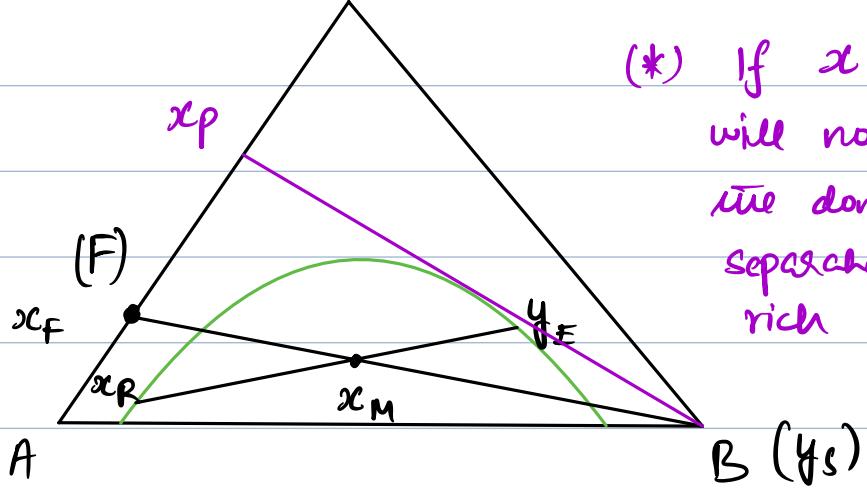


If T is increased



Conclusion \Rightarrow Extraction is preferred at lower temperature.

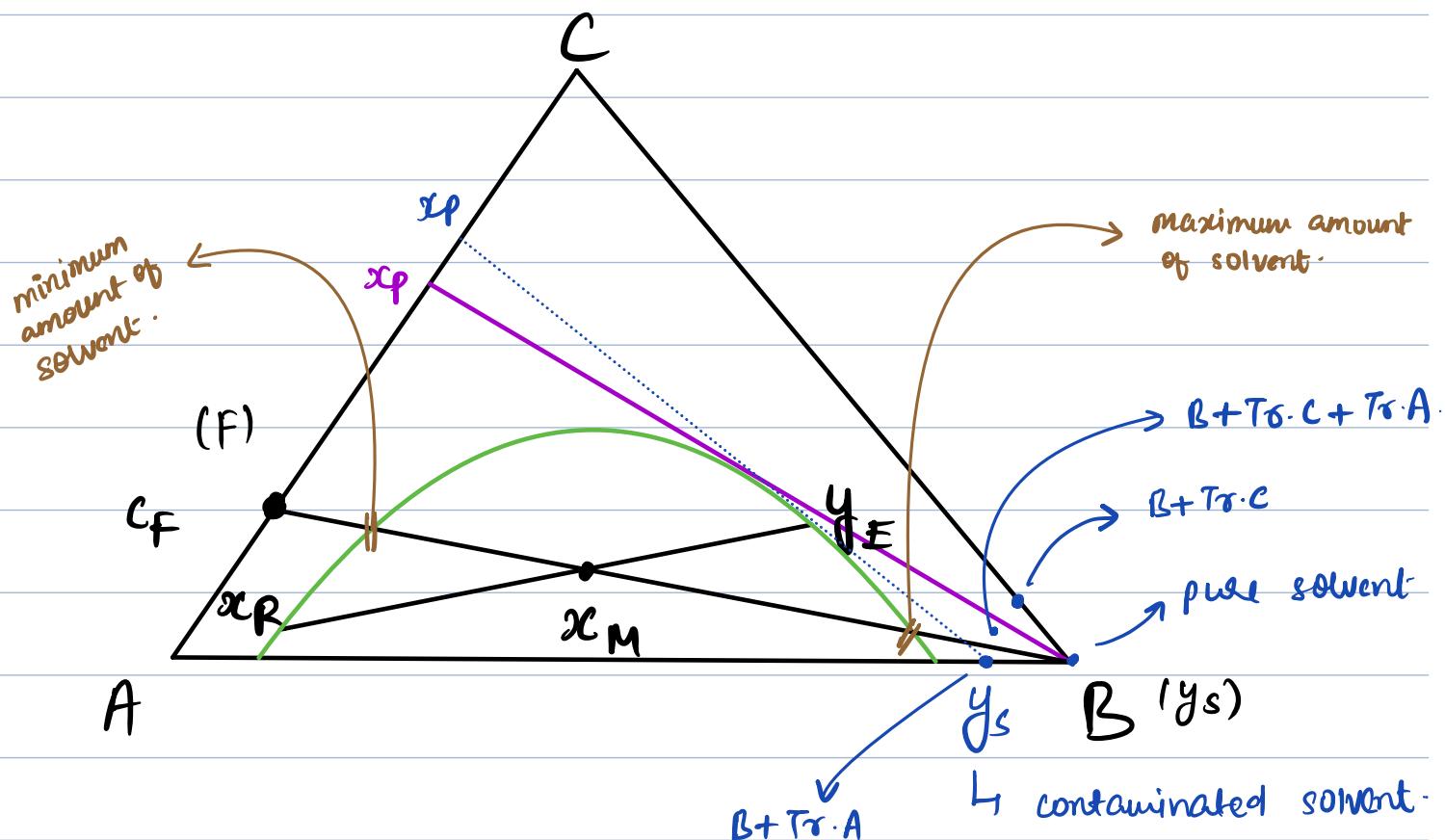
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(*) If $x_F > x_P$ then x_M will not be obtained inside the dome, and will not separate into A-rich and B-rich phase.

Therefore $x_F < x_P$, for the mixture to separate into A-rich and B-rich phase.

If $y_S \neq 0$, then



The value of x_P is maximum for $B+Tr.A$.

The value of x_P is minimum for $B+Tr.C$.

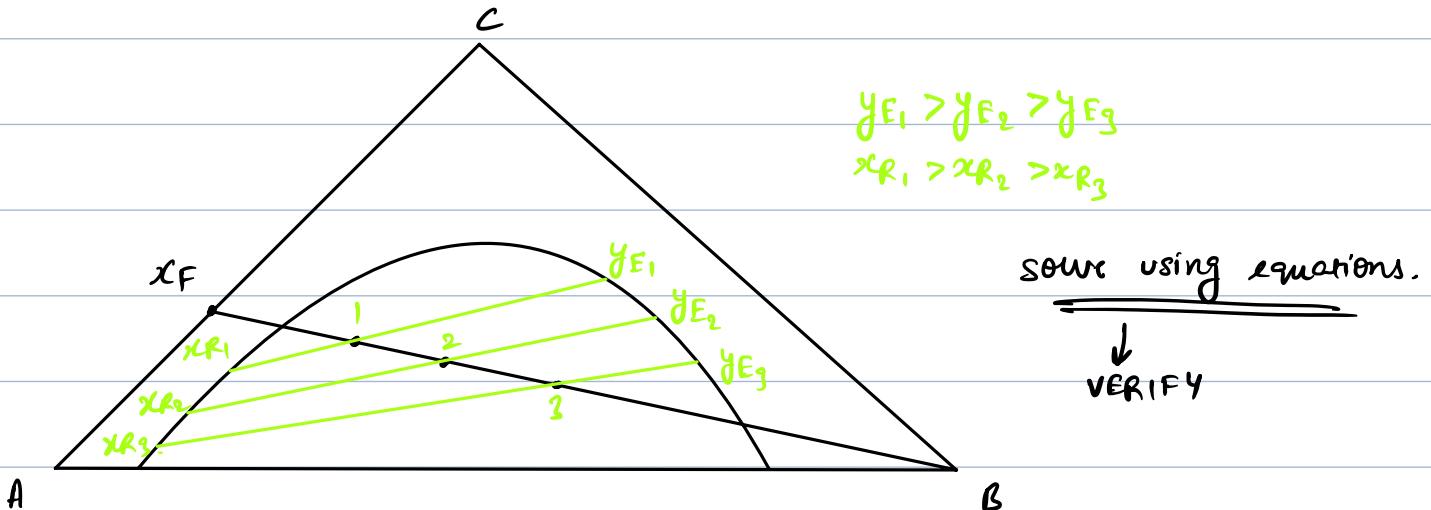
Even if $x_F < x_P$ it is possible that x_M lies outside the dome.

If we take F & S in extreme cases, then this may happen.

flow rate

(*) By changing the amount of S and F stream will translate along FB line.

(**) If solvent is low in amount then E will also drop. We will get a more pure product but in low quantities.



CHOICE OF SOLVENT

1.) Selectivity

$$\beta = \frac{(\text{wt. fraction of } C \text{ in } E) / (\text{wt. fraction of } A \text{ in } E)}{(\text{wt. fraction of } C \text{ in } R) / (\text{wt. fraction of } A \text{ in } R)}$$

partition coefficient.

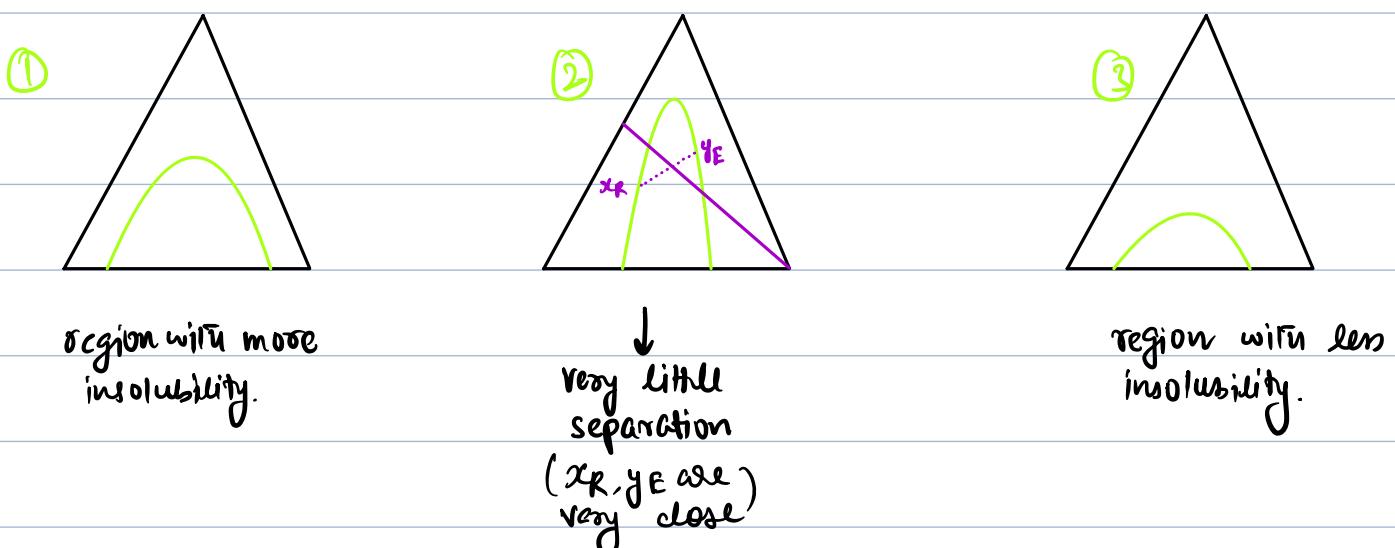
$$= \frac{y_E \times (\text{wt. fraction of } A \text{ in } R)}{x_R \times (\text{wt. fraction of } A \text{ in } E)}$$

Necessary condition for effective separation: $\beta > 1$

$\beta = 1 \rightarrow$ Tie line is horizontal. (x_R and y_E become equal, no separation possible.)

Azeotrope or not yet not !! → IMPORTANT

2.) Partition coefficient

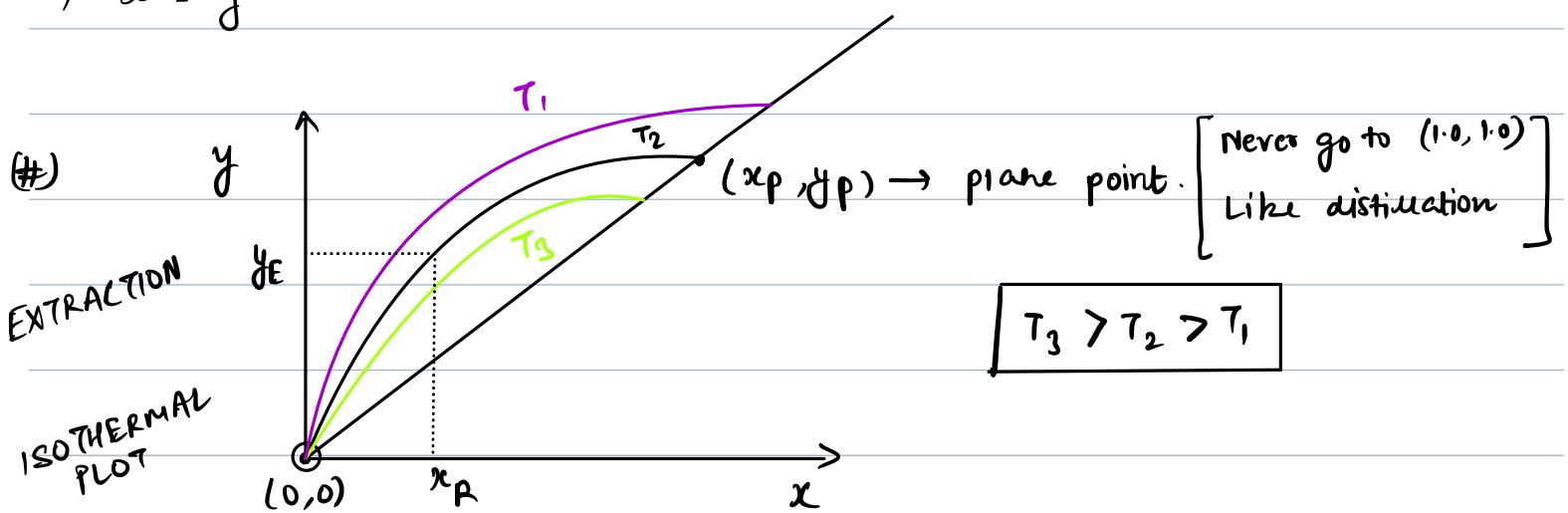


3.) Degree of Insolubility

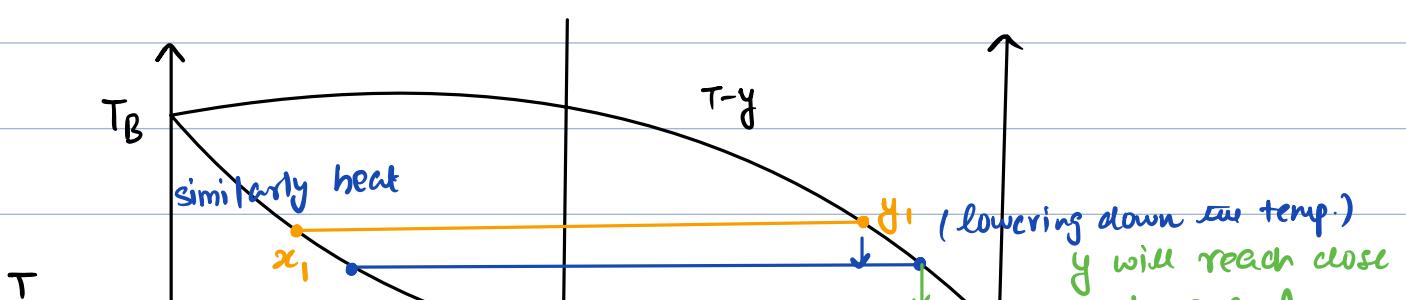
4.) Recyclability of the solvent

5.) Surface Tension

6.) Density



(*) why do we perform multistage in distillation?





TD pure A.

(*) McCabe-Thiell

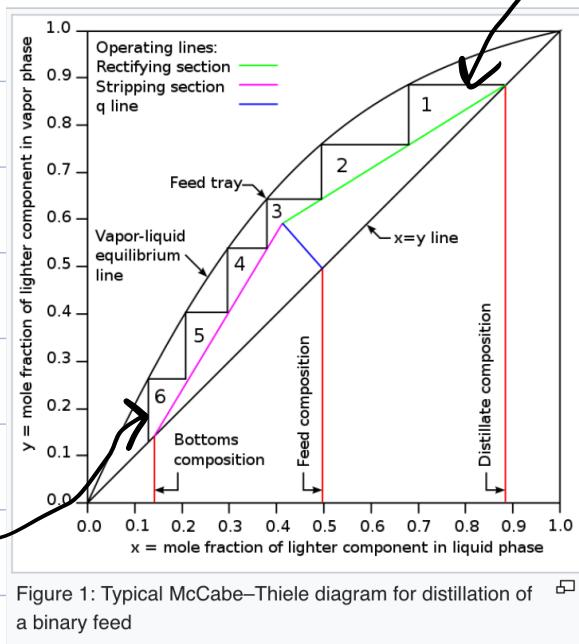
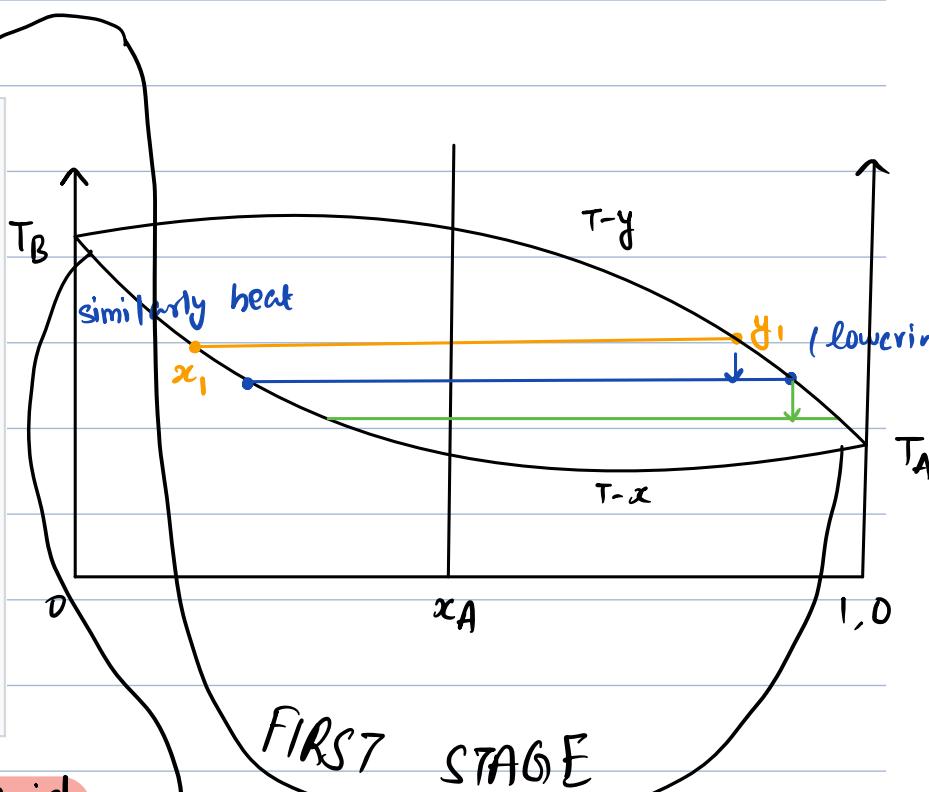


Figure 1: Typical McCabe-Thielle diagram for distillation of a binary feed

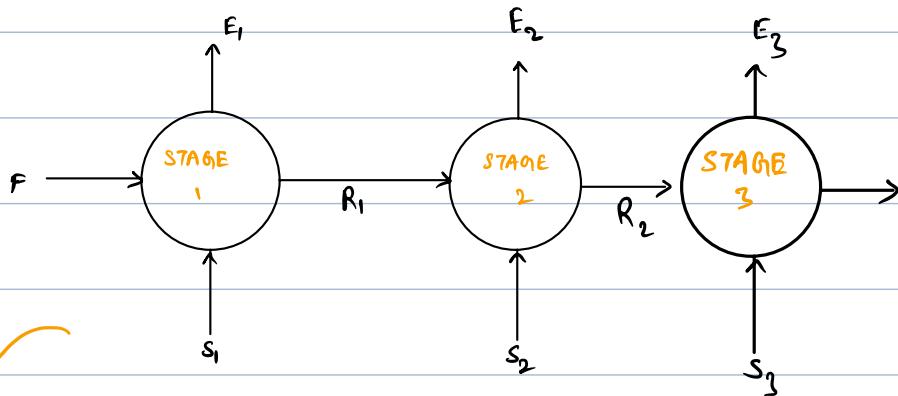
operating line relates ~~the~~ liquid and vapor streams b/w 2 trays.

LAST STAGE

FIRST STAGE



(#) Objective: To extract more C from the raffinate.



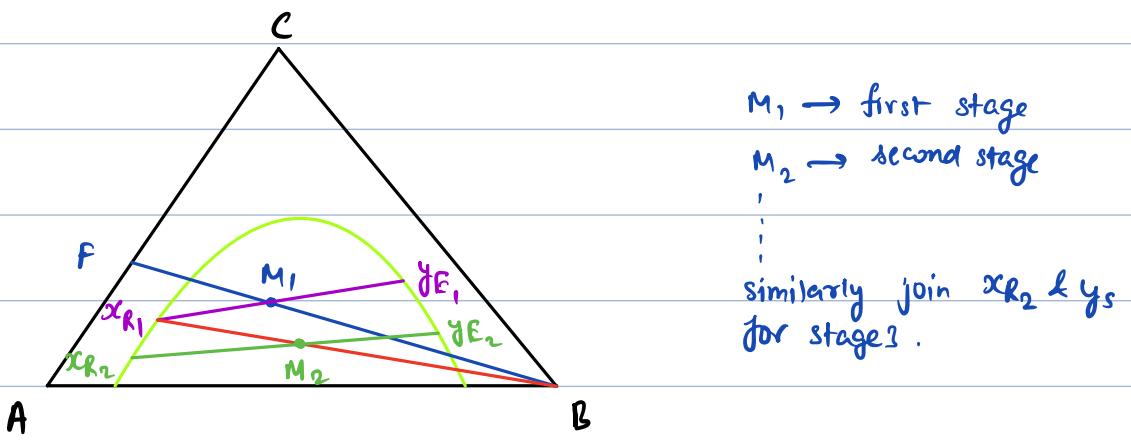
Balance for stage 2:

$$R_1 + S_2 = M_2$$

$$R_1 x_{R_1} + S_2 y_S = M_2 x_{M_2}$$

→ This is not similar to distillation column as this is CROSS FLOW.

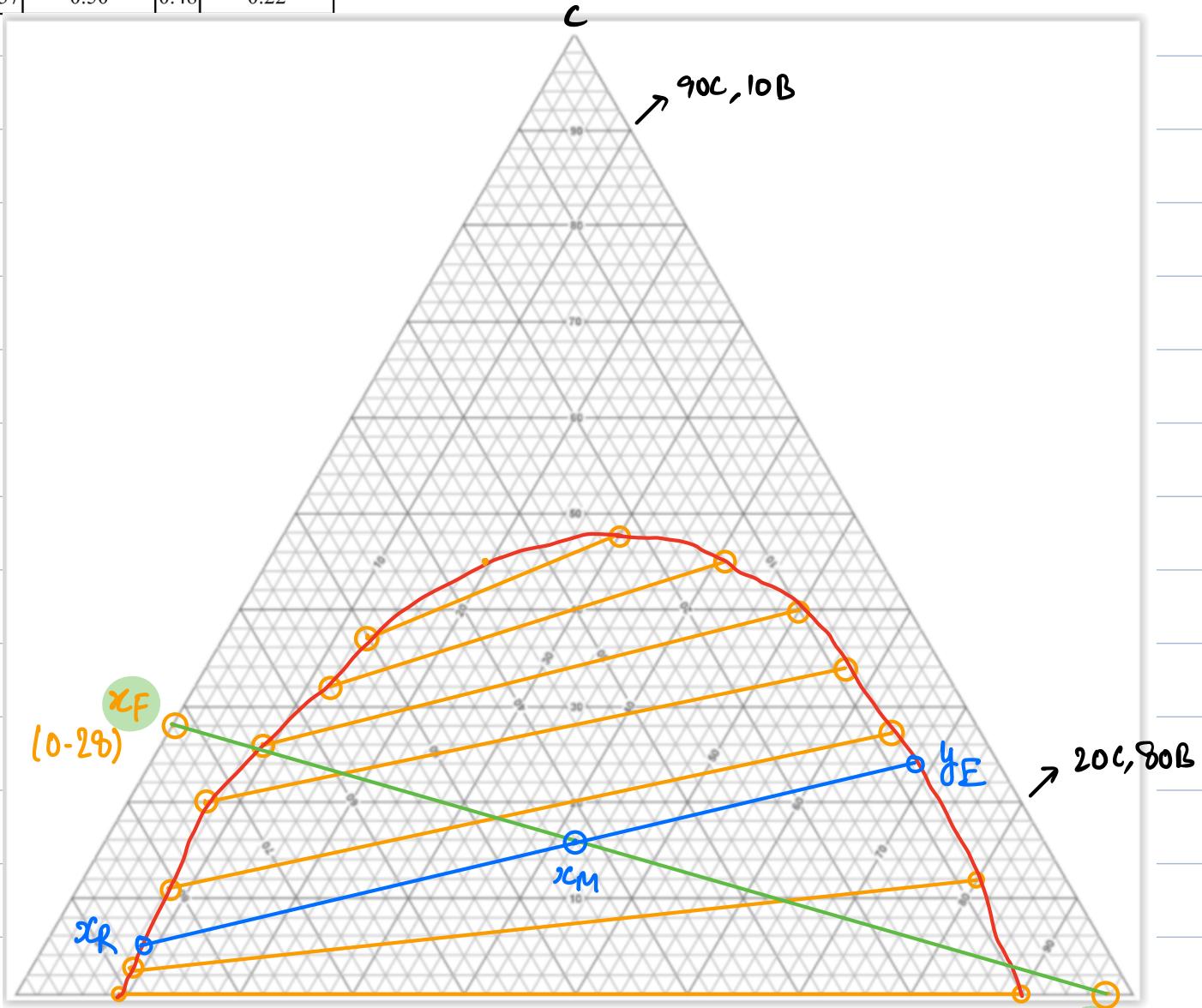
Representing stage-2 on the graph:-



(12 Sept, 2022)

x	Fraction of A	y	Fraction of A
0	0.91	0	0.10
0.05	0.87	0.12	0.08
0.12	0.81	0.27	0.08
0.20	0.73	0.34	0.09
0.26	0.65	0.40	0.10
0.32	0.58	0.45	0.14
0.37	0.50	0.48	0.22

40 kg of feed with 28% solute is mixed with 30 kg of solvent that has 2 % carrier in it, in a single stage batch extractor. Find the amount and composition of the extract and raffinate.



A
↓
90A
10B

B
↓
80B
20A
↓
90B
10A

$S \rightarrow$ Solvent has 2:1 carrier in it. (B and S not coincident).

MASS BALANCE

$$S + F = M = \tau_0$$

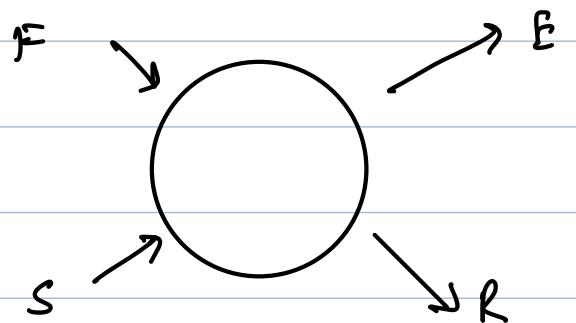
$$Sx_S + Fx_F = Mx_M$$

$$40 \times 0.28 = \tau_0 \times x_M$$

$$\Rightarrow x_M = \frac{40 \times 0.28}{\tau_0} = 0.16$$

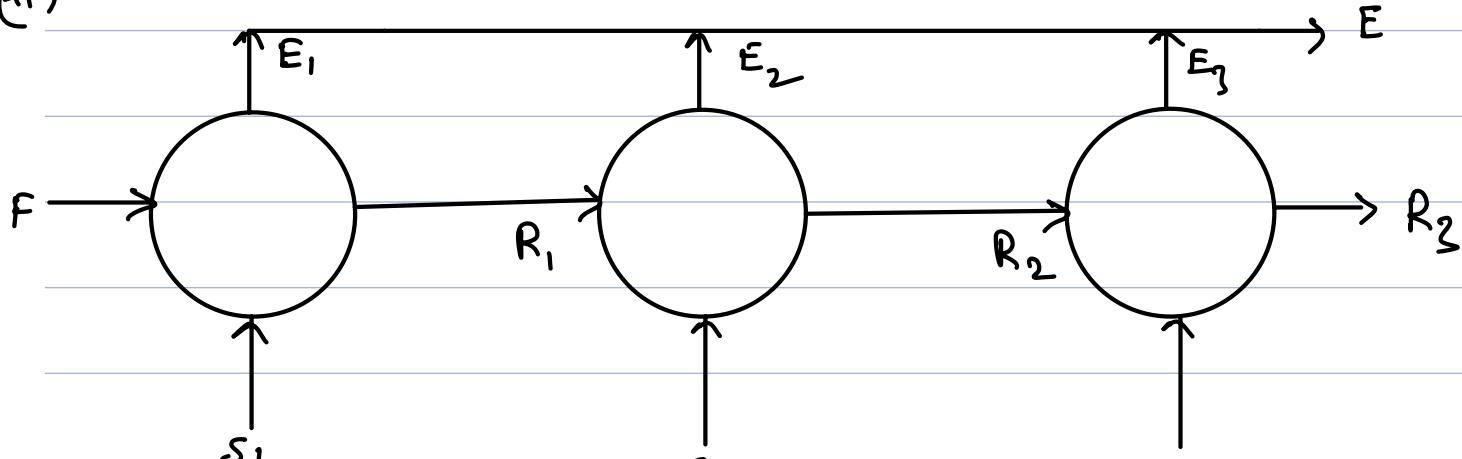
$$\text{from graph} \Rightarrow x_R = 0.06, y_E = 0.23$$

(#)



SINGLE STAGE
EXTRACTOR.

(#)

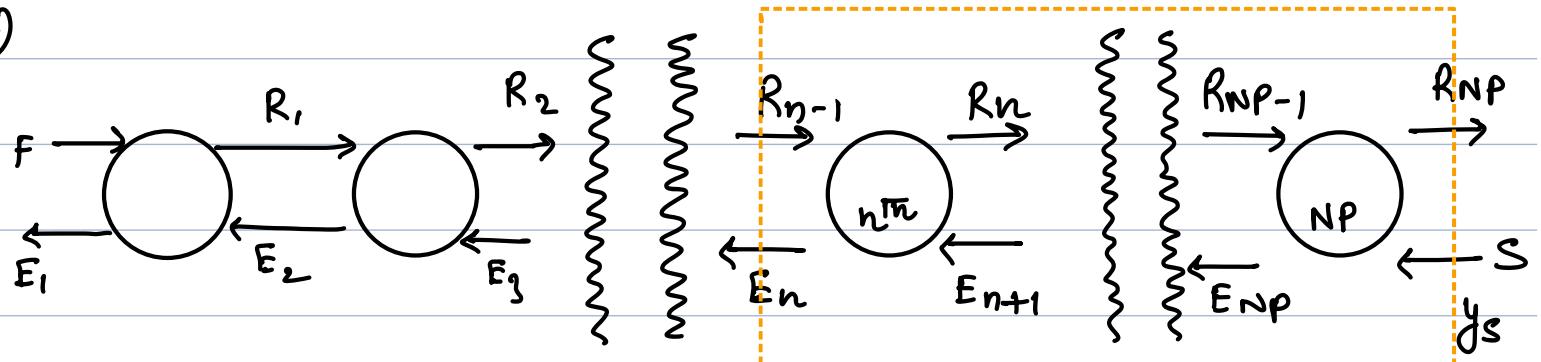


S_2

S_3

CROSS FLOW MULTISTAGE EXTRACTOR

(#)



$NP \rightarrow$ number of plates -

COUNTER FLOW MULTISTAGE EXTRACTOR.

(I)

Overall balance : $F + S = E_1 + R_{NP} = M$

$$F x_F + S y_S = E_1 y_1 + R_{NP} x_{NP} = M x_M$$

→ For this problem (E, y_E) or (R_{NP}, x_{NP}) must be specified.

→ Here M has no physical significance, but just a mathematical entity. F and S never come together OR $E_1 \neq R_{NP}$.

→ same for x_M .

⇒

$$R_{NP} - S = F - E_1 = \Delta R.$$

(II)

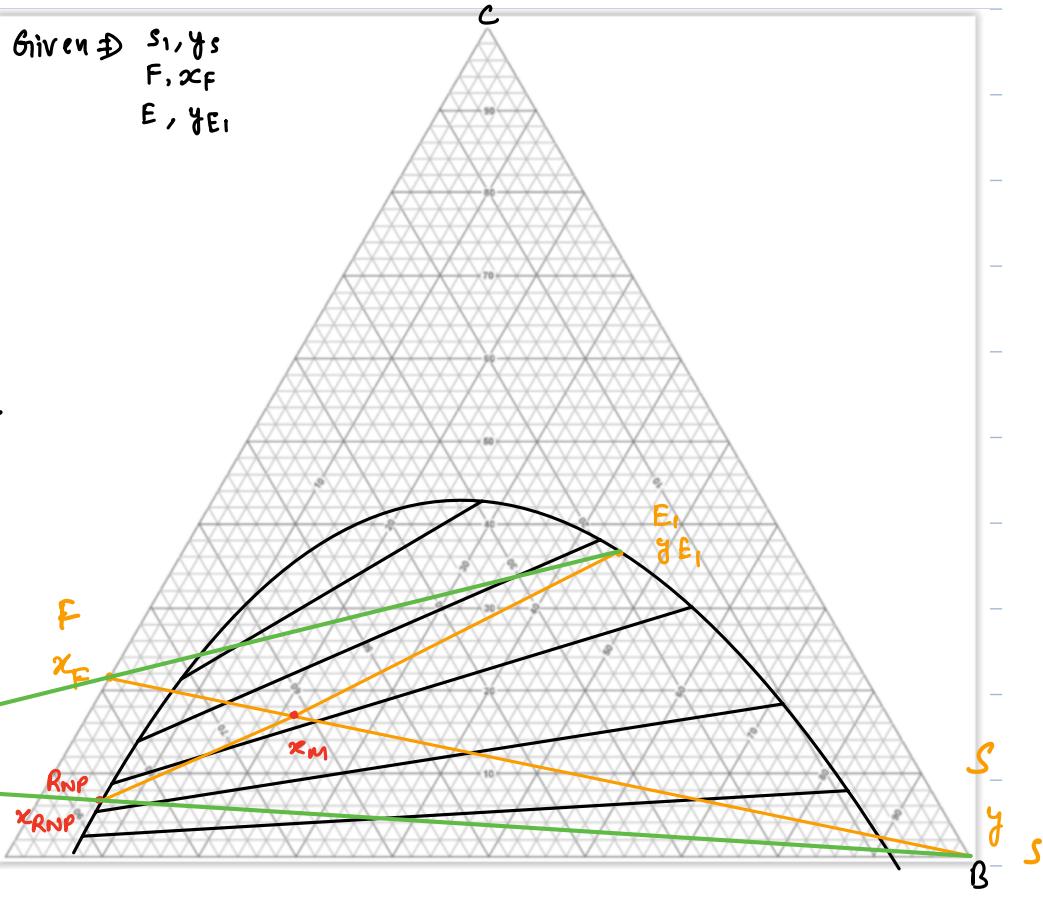
Overall balance for stage n gives

$$R_{n-1} + E_{n+1} = R_n + E_n \Rightarrow R_{n-1} - E_n = R_n - E_{n+1} = \Delta R.$$

III

Balance for whole plant from n^{th} to NP n^{th} stage.

$$R_{n-1} + S = E_n + R_{NP} \Rightarrow R_{NP} - S = R_{n-1} - E_n = \Delta R$$



R_1, E_1 in equilibrium.

15 $^{\text{th}}$ Sept

(Q.) CROSS FLOW CONFIGURATION IN 3 STAGES

40 kg, 28% C \rightarrow Feed

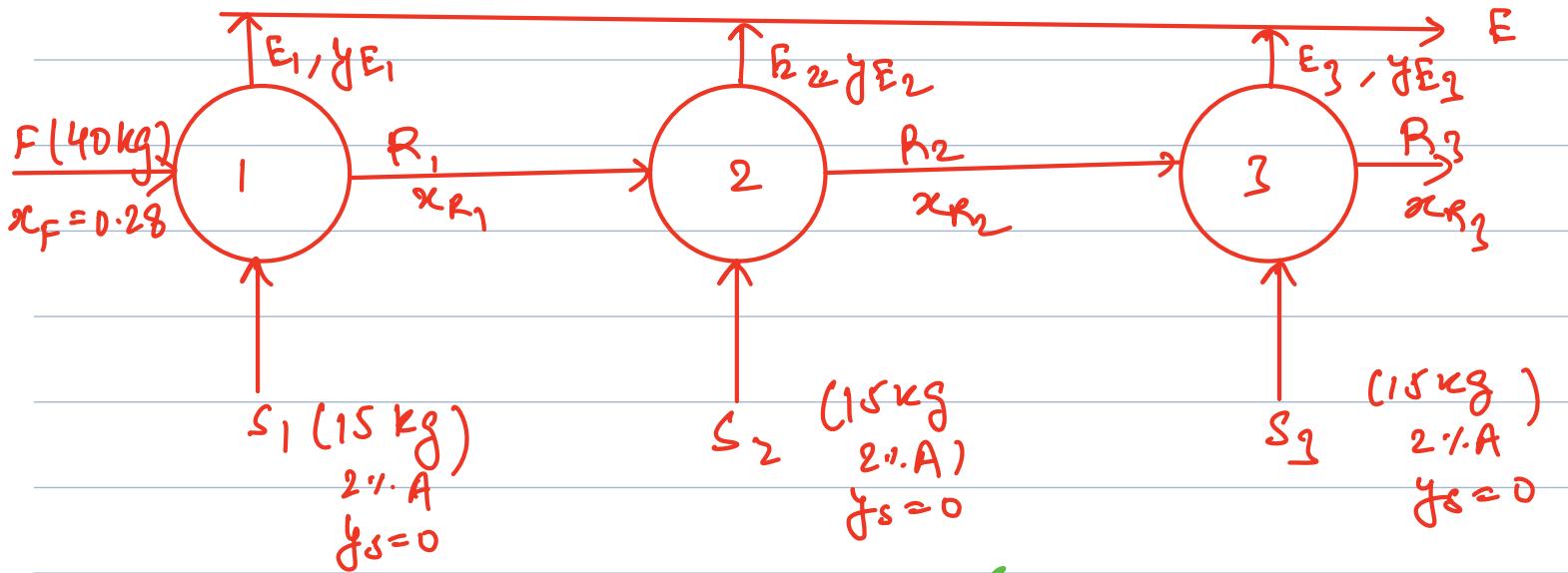
15 kg, 2% A \rightarrow Solvent

To Find \Rightarrow Extract $\xrightarrow[y]{\text{composition}}$ Amount

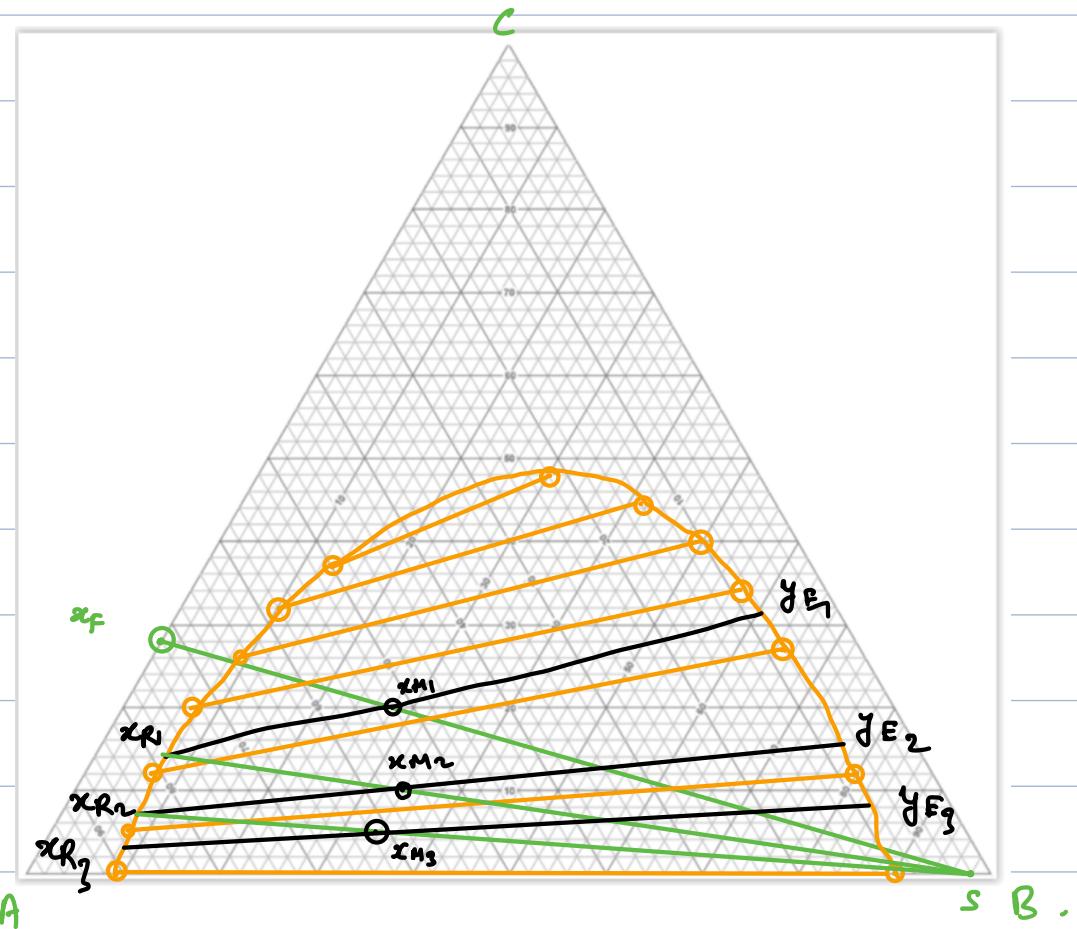
Raffinate $\xrightarrow[y]{\text{composition}}$ Amount

x	Fraction of A	y	Fraction of A
0	0.91	0	0.10
0.05	0.87	0.12	0.08
0.12	0.81	0.27	0.08
0.20	0.73	0.34	0.09
0.26	0.65	0.40	0.10
0.32	0.58	0.45	0.14
0.37	0.50	0.48	0.22

SOL'N (My attempt at the problem).



x	Fraction of A	y	Fraction of A
0	0.91	0	0.10 ✓
0.05	0.87	0.12	0.08 ✓
0.12	0.81	0.27	0.08 ✓
0.20	0.73	0.34	0.09 ✓
0.26	0.65	0.40	0.10 ✓
0.32	0.58	0.45	0.14 ✓
0.37	0.50	0.48	0.22 ✓



STAGE 1

$$F + S_1 = E_1 + R_1 \rightarrow \text{Total mass balance}$$

$$F x_F + S_1 y_{S_1} = y_{E_1} + R_1 x_{R_1} \rightarrow \text{C balance.}$$

$F = 40\text{kg}$, $x_F = 0.28$, To find y_{E_1} and x_{R_1} ,

$S_1 = 15\text{kg}$, $y_{S_1} = 0$, we need x_{M_1} .

From graph $x_{R_1} = 0.14$, $y_{E_1} = 0.31$

Mixture

$$F + S_1 = M_1$$

$$F x_F + S_1 y_{S_1} = M_1 x_{M_1}$$

$$E_1(0.31) + R_1(0.14) = 11.2$$

$$\Rightarrow E_1 = 20.6, R_1 = 34.4$$

$$r_{MF} + s_1 y_{S_1} = M_1 x_M$$

$$\Rightarrow M_1 = 55 \text{ kg}$$

$$\Rightarrow x_M = 0.2036$$

$y_{E_1} = 0.31$	$x_{R_1} = 0.14$
$E_1 = 20.6$	$R_1 = 34.4$

STAGE 2

$$\begin{cases} R_1 + S_2 = M_2 \\ R_1 x_{R_1} + S_2 y_{S_2} = M_2 x_{M_2} \end{cases}$$

$$34.4(0.14) + 15(0) = 49.4 x_{M_2}$$

$$x_{M_2} = 0.1$$

$$E_2 + R_2 = M_2$$

$$R_2 y_{R_2} + E_2 y_{E_2} = M_2 x_{M_2}$$

$$\text{From graph } x_{R_2} = 0.07 \\ y_{E_2} = 0.15$$

$$F_2 + R_2 = 49.4$$

$$E_2(0.15) + (49.4 - E_2)(0.07) = 49.4 \times 0.1$$

$$0.08E_2 + 3.458 = 4.94$$

$$E_2 = 18.525 \Rightarrow R_2 = 30.875$$

$y_{E_2} = 0.15$	$x_{R_2} = 0.07$
$E_2 = 18.525$	$R_2 = 30.875$

STAGE 3

$$R_2 + S_3 = M_3$$

$$\Rightarrow M_3 = 45.875$$

$$R_2 x_{R_2} + S_3 y_{S_3} = M_3 x_{M_3} \Rightarrow x_{M_3} = 0.05$$

$$E_2 + R_2 = 45.875$$

$$E_2(0.09) + (45.875 - E_2)0.03 = 45.875 \times 0.05$$

$$E_2(0.06) + 1.37625 = 2.29375$$

$$E_2 = 15.3 \Rightarrow R_2 = 30.6$$

$$y_{E_3} = 0.09$$

$$x_{R_3} = 0.03$$

$$E_3 + R_3 = M_3$$

$$E_3 y_{E_3} + R_3 x_{R_3} = M_3 x_{M_3}$$

$y_{E_3} = 0.09$	$x_{R_3} = 0.03$
$E_3 = 15.3$	$R_3 = 30.6$

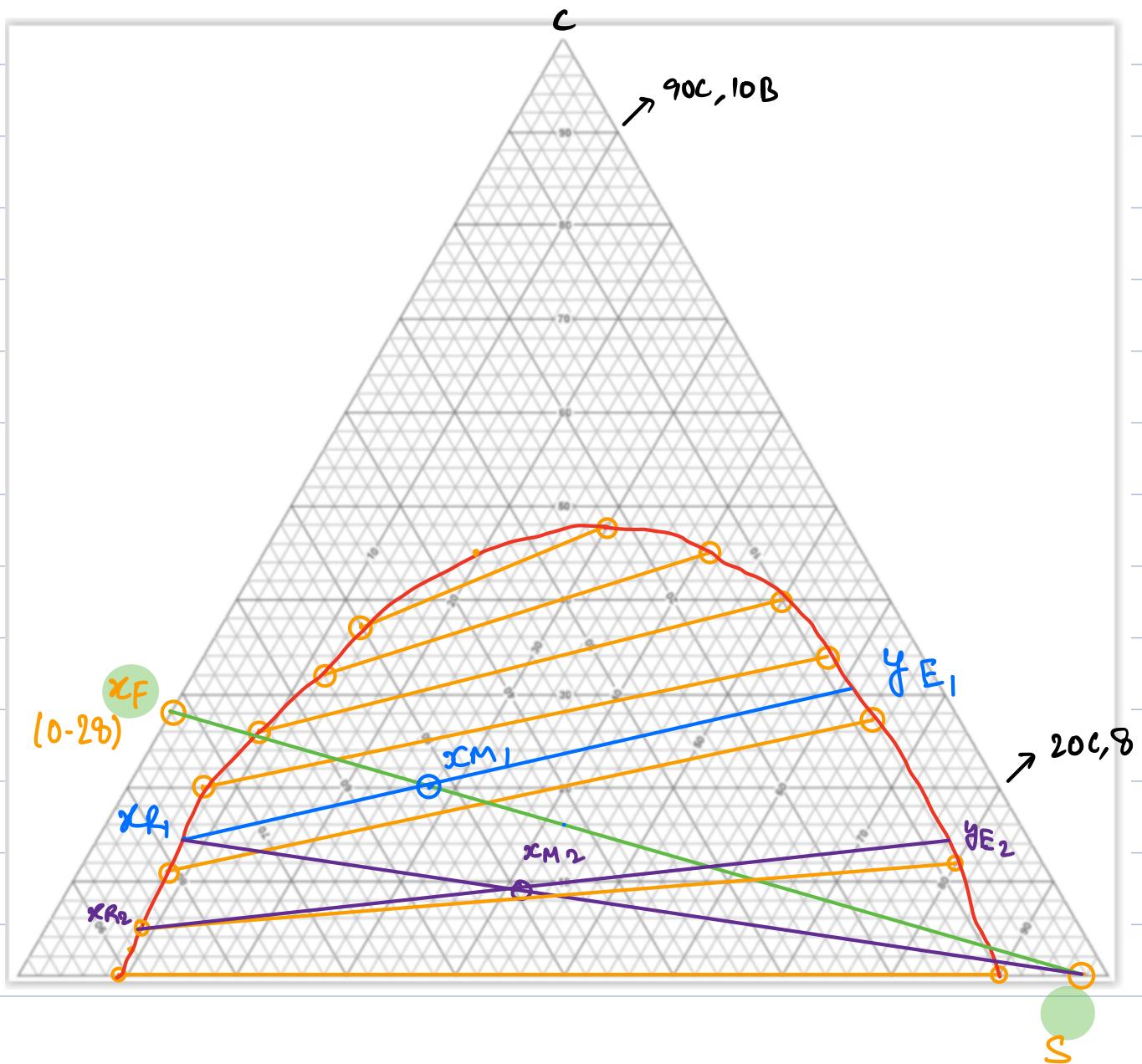
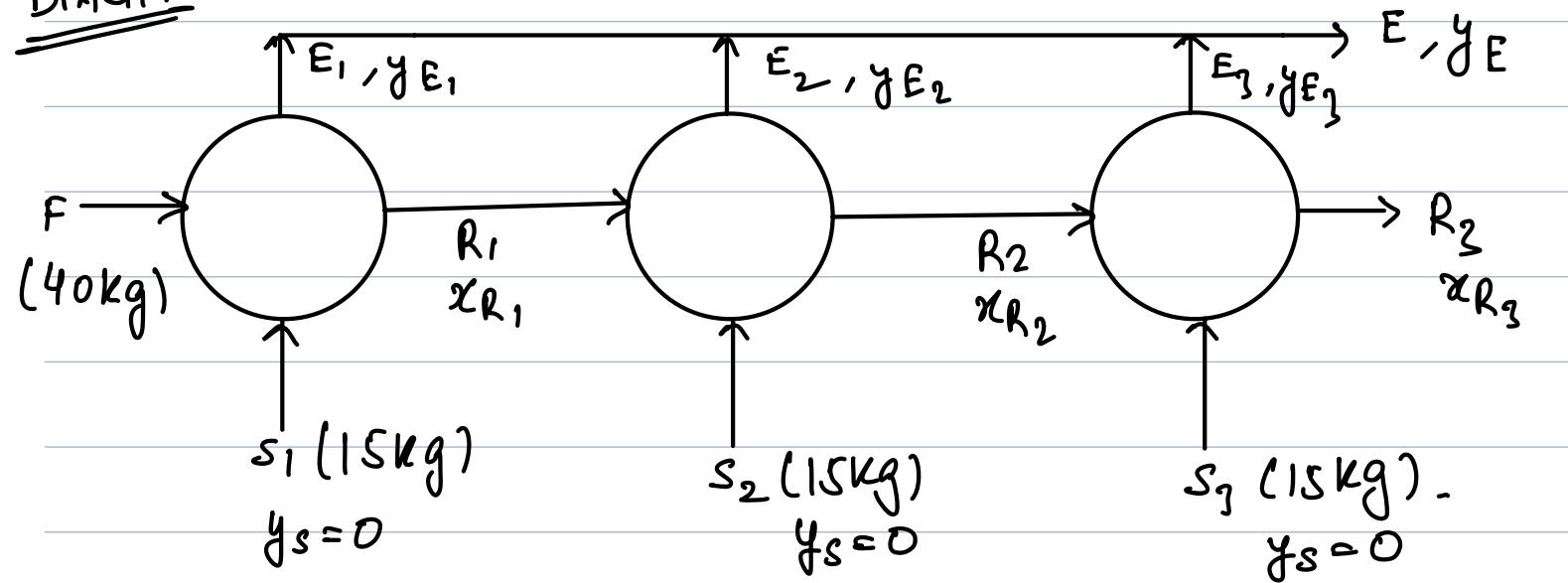
FINAL \Rightarrow

Raffinate = 30.6 kg, $x_{R_3} = 0.03$

Extract $\Rightarrow E, y_E$, $E = E_1 + E_2 + E_3 = 54.425$

$$y_E = \frac{\sum y_i E_i}{E} = 0.1916.$$

DIAGRAM



MASS BALANCE

$$S + F = M_1 = 15 + 40 = 55$$

$$Sx_S + Fx_F = Mx_M$$

$$40 \times 0.28 = 55 x_M$$

$$x_{M_1} = 0.2036$$

From graph $\Rightarrow x_{R_1} = 0.14, y_{E_1} = 0.31$

$$E_1 + R_1 = M_1 = 55 \rightarrow ①$$

$$y_{E_1} E_1 + x_{R_1} R_1 = 0.2036 \times 55 \rightarrow ②$$

$$(0.31)(E_1) + (0.14)(R_1) = 11.198$$

$$(0.31)(55 - R_1) + 0.14 R_1 = 11.198$$

$$17.05 - 0.17 R_1 = 11.198$$

$$R_1 = 34.4235 \Rightarrow E_1 = 20.5764$$

$$\begin{aligned} R_1 &= 34.4235 & E_1 &= 20.5764 \\ x_{R_1} &= 0.14 & y_{E_1} &= 0.31 \end{aligned} \quad] \quad \text{STAGE 1}$$

$$R_1 + S_2 = M_2 \Rightarrow M_2 = 15 + 34.4235 = 49.4235$$

$$R_1 x_{R_1} + S_2 y_{S_2} = M_2 x_{M_2} \Rightarrow (34.4235)(0.14) + (15)(0) = 49.4235 x_{M_2}$$

$$x_{M_2} = 0.0975$$

$$\text{From graph } x_{R_2} = 0.06 \quad y_{E_2} = 0.14$$

$$E_2 y_{E_2} + R_2 x_{R_2} = 49.4235 \times 0.0975 \rightarrow ①$$

$$E_2 + R_2 = 49.4235 \rightarrow ②$$

$$0.14 E_2 + 0.06 R_2 = 4.8188$$

$$0.14(49.4235 - R_2) + 0.06 R_2 = 4.8188$$

$$6.919 - 0.14R_2 + 0.06R_2 = 4.8188$$

$$2.10049 = 0.08R_2$$

$$R_2 = 26.2561 \Rightarrow E_2 = 23.167375$$

$$R_2 = 26.2561$$

$$x_{R_2} = 0.06$$

$$E_2 = 23.1674$$

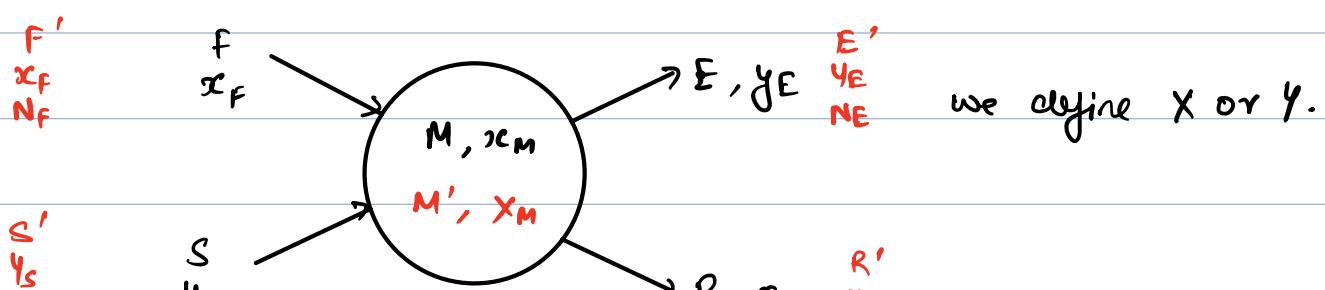
$$y_{E_2} = 0.14$$

STAGE 2.

POST MIDSEM



B - Free Calculation



N_s y_s $\rightarrow K, x_R \quad \frac{x_R}{N_R}$

$$y_E = \frac{c_E}{A_E + R_E + c_E} \quad , \quad x_R = \frac{c_R}{A_R + R_R + c_R}$$

\downarrow
(E)

 x or y

\hookrightarrow B free fraction of C.

$$y_E = \frac{c_E}{A_E + c_E} = \frac{c_E}{E'} \quad (E' - B \text{ free extract flow rate})$$

$$x_R = \frac{c_R}{A_R + c_R} = \frac{c_R}{R'} \quad (R' - B \text{ free raffinate flow rate})$$

$$N_R = \frac{B_R}{(A_R + c_R)}$$

N : B fraction on a B-free basis.

For a pure solvent $s' = 0$, $N_s = \infty$, $y_s = \infty$

$\hookrightarrow \left(\frac{0}{0}\right)$

$$N_s = \frac{B_s}{(A_s + c_s)} \rightarrow s'$$

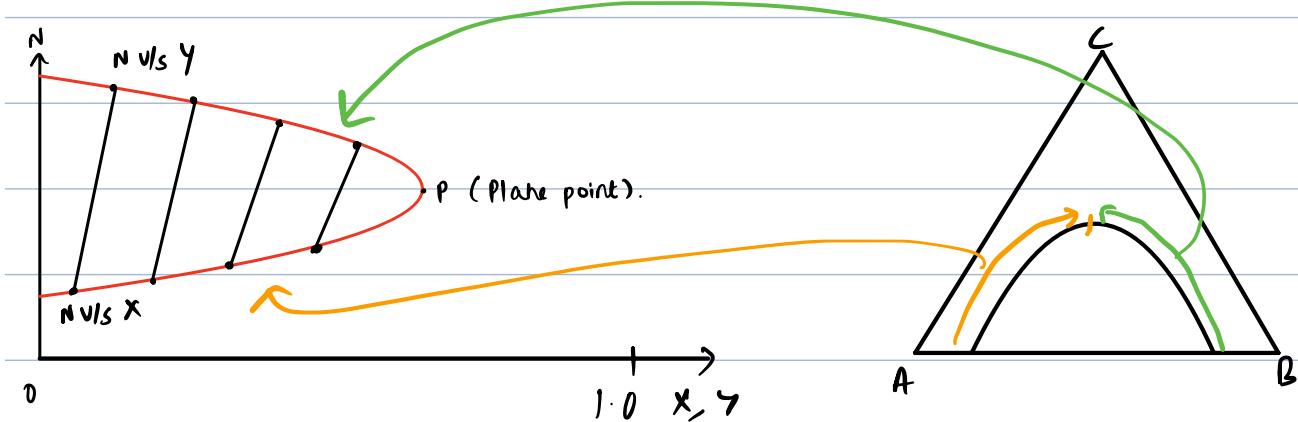
NOTE \rightarrow physically E', R', F', s' do not exist.

x	Fraction of A	y	Fraction of A
0	0.91	0	0.10
0.05	0.87	0.12	0.08
0.12	0.81	0.27	0.08
0.20	0.73	0.34	0.09
0.26	0.65	0.40	0.10
0.32	0.58	0.45	0.14
0.37	0.50	0.48	0.22

converting into
B-free basis

x	A	B	x	N_x
0	0.91	0.09	$\frac{0}{0.91}$	$\frac{0.09}{0.91} = 0.099$
0.05	0.87	0.08	$\frac{0.05}{0.92}$	$\frac{0.08}{0.92} = 0.087$
⋮	⋮	⋮	⋮	⋮
0.32	0.58	0.10	$\frac{0.32}{0.90}$	$\frac{0.10}{0.90} = 0.111$
0.12	0.81	0.07	$\frac{0.12}{0.93}$	$\frac{0.07}{0.93} = 0.075$
0.26	0.65	0.09	$\frac{0.26}{0.91}$	$\frac{0.09}{0.91}$

y	A	B	y	N_y
0.40	0.10	0.5	$\frac{0.4}{0.5}$	$\frac{0.5}{0.5}$



Advantage: We can plot using cartesian coordinates.

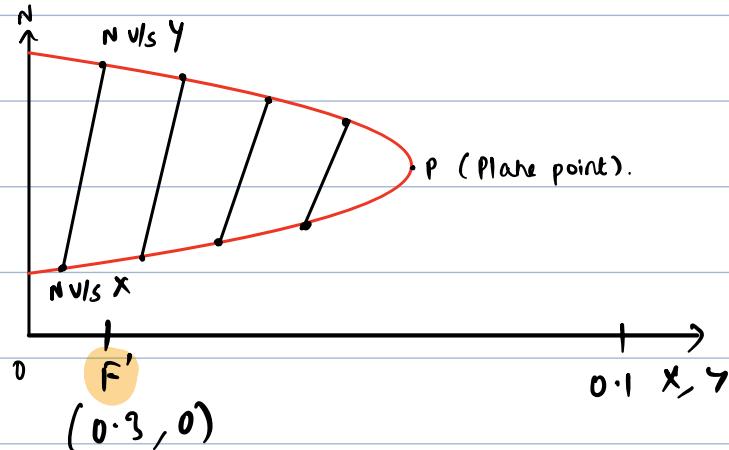
Ex:- Feed = 30% C

$$x_F = 0.3$$

$$x_F = 0.3$$

\nwarrow
 (∴ B_F is 0 in feed)

∴ Feed point $\rightarrow (0.3, 0)$



Overall Mass Balance:

$$S + F = M = E + R$$

B-Free Mass Balance:

$$F' + S' = M' = E' + R' \longrightarrow ①$$

what is the relation b/w F and F'? $\Rightarrow F = F'$ → no B_F in feed.

Pure solvent case

$$S' = 0$$

Using ①

$$F' + S' = M'$$

$$F' = M'$$

$$\Rightarrow F' = M' = F$$

$$F' = A_F + C_F$$

$$x_F = \frac{C_F}{A_F + C_F}$$

$$S' = A_S + C_S$$

$$y_S = \frac{C_S}{A_S + C_S}$$

$$N' = A_M + C_M$$

$$x_M = \frac{C_M}{A_M + C_M}$$

B free C balance:

$$F' x_F + S' y_S = N' x_M \quad \text{where, } \Rightarrow$$

For a pure solvent $\Rightarrow S' y_S = 0$ (1st approximation)

$$\Rightarrow F' x_F = N' x_M$$

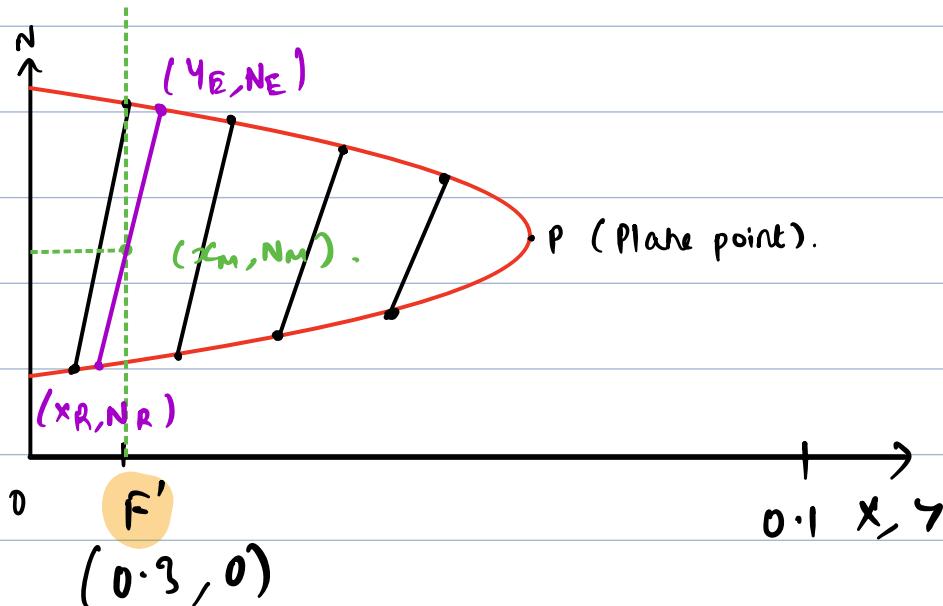
$$\Rightarrow x_F = x_M$$

B free B balance:

$$N_F' + N_S S' = N_M M'$$

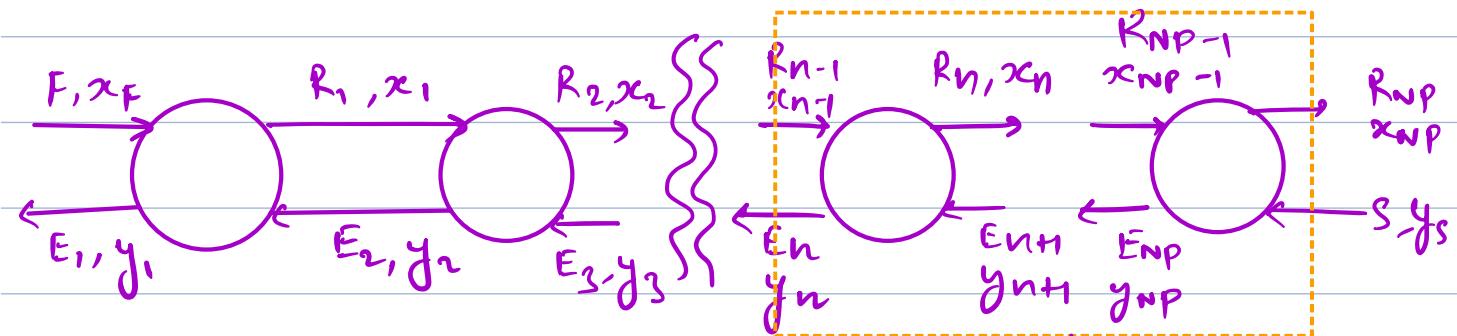
$$N_S S' = \frac{B_S}{(A_S + C_S)} \times (A_S + C_S) = B_S = S$$

$$\Rightarrow N_M M' = S \Rightarrow N_M = S/F$$



(*) All main equations are valid in case of pure and impure solvent but the approximations are valid only in case of pure solvent.

Continuous Counter-current multistage Extractor



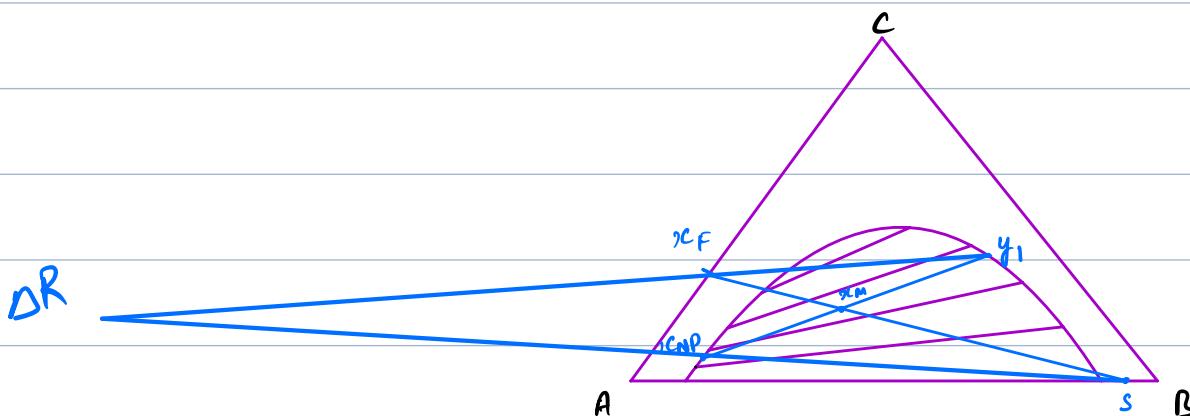
Overall balance :-

$$F + S = E_1 + R_{NP}$$

$$E_1 - F = S - R_{NP} = \Delta R$$

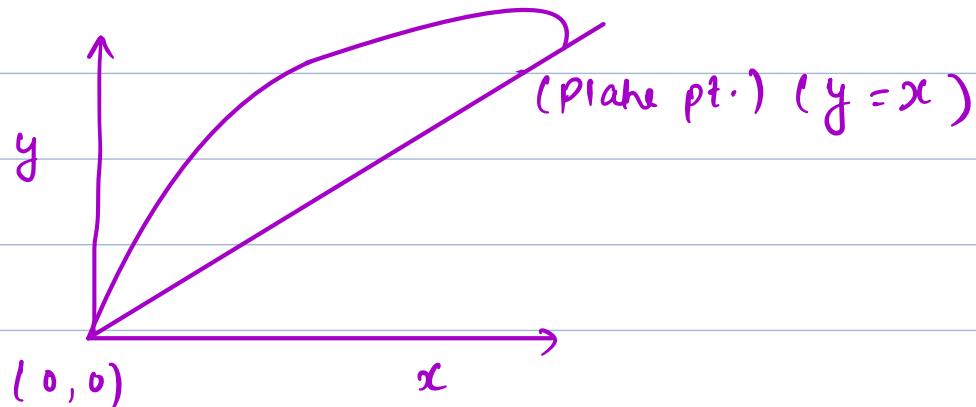
$$R_{n+1} + S = E_n + R_{NP}$$

$$E_n - R_{n-1} = S - R_{NP} = \Delta R$$



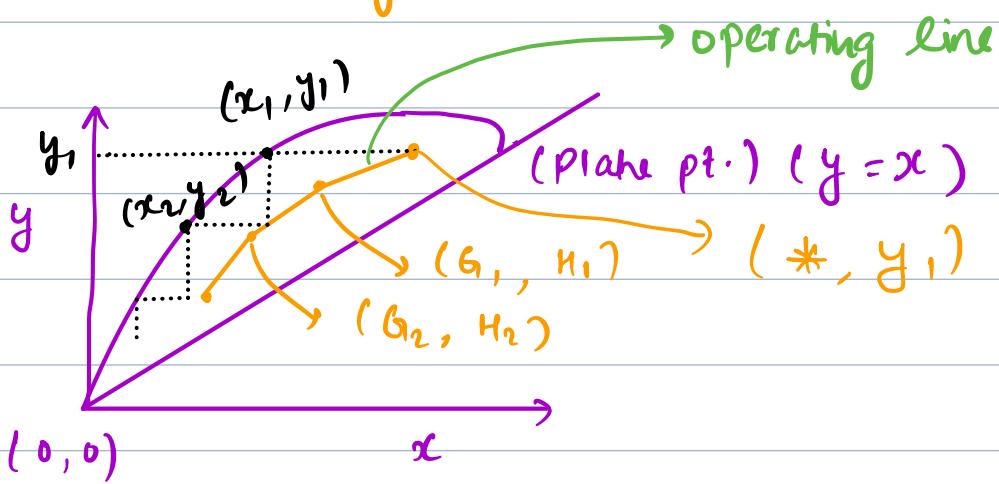
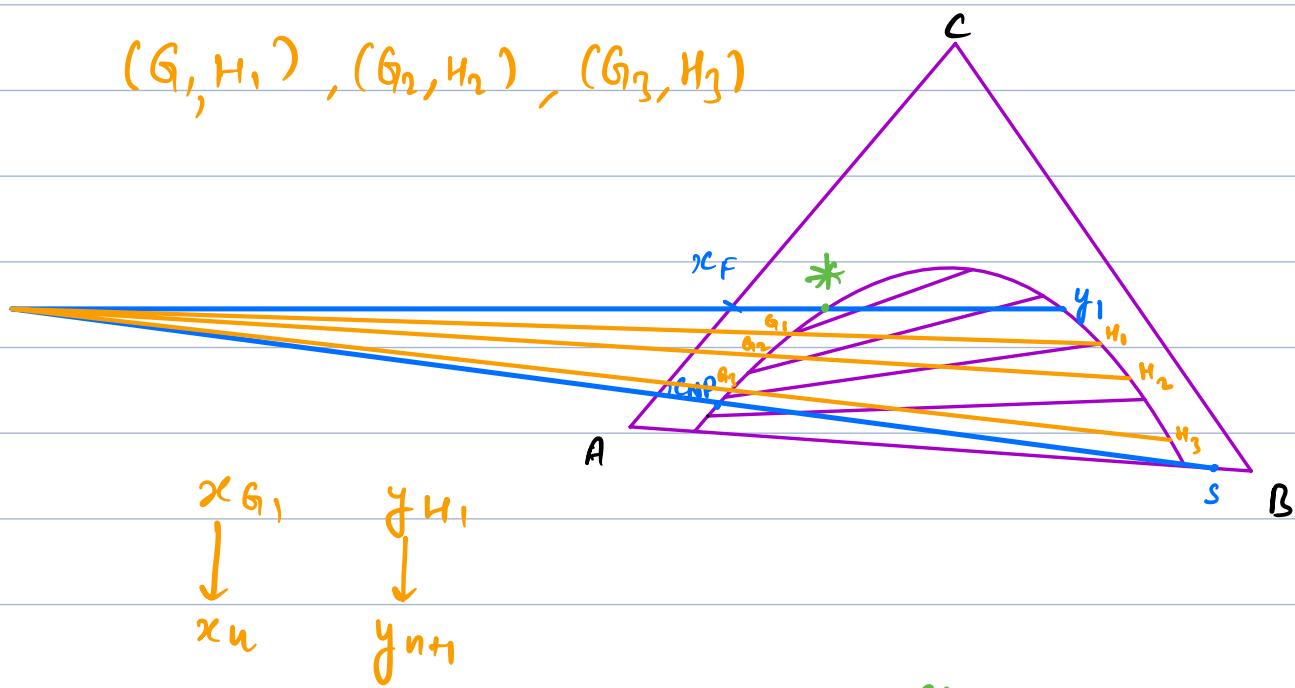
(*) y_{n+1} v/s x_n \rightarrow OPERATING LINE
Plot

x_n v/s y_n (equilibrium plot).



$(G_1, H_1), (G_2, H_2), (G_3, H_3)$

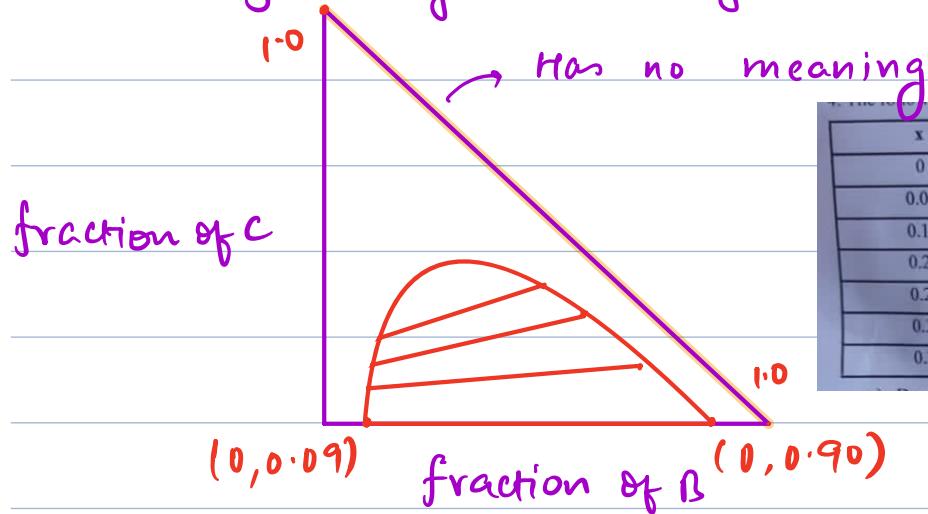
DR



Unlike Raoult-Thiele method we don't have an

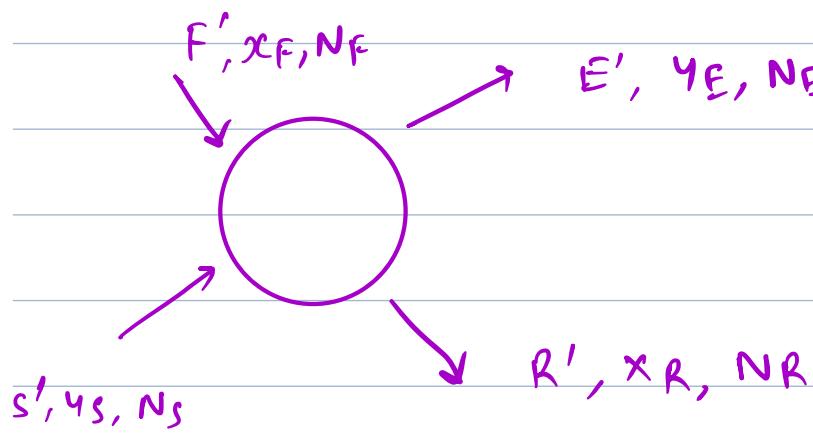
analytical eq'n for the operating line and that is why we have to generate the operating line from the DR plot.

⇒ Right Angular Triangular Plot.



x	Fraction of B	y	Fraction of B
0	0.09	0	0.90
0.06	0.07	0.12	0.80
0.12	0.07	0.27	0.65
0.20	0.08	0.34	0.57
0.26	0.10	0.40	0.50
0.32	0.11	0.45	0.41
0.37	0.13	0.48	0.31

B-Free calculations for multi-stage



$$x_F = c_F / (A_F + B_F + C_F)$$

$$y_E = c_E / (A_E + B_E + C_E)$$

$$X_F = C_F / (A_F + C_F)$$

$$N_F = B_F / (A_F + C_F) = 0$$

$$X_S = \frac{c_S}{A_S + C_S} = \frac{0}{0}$$

$$N_S = \frac{B_S}{A_S + C_S} = \frac{B_S}{0}$$

Pure Solvent.

$$Y_E = c_E / (A_E + C_E)$$

$$N_E = B_E / (A_E + C_E)$$

B-Free overall balance ⇒

$$F' + S' = M' = E' + R'$$

For pure solvent, $S' = 0$, $F' = M'$

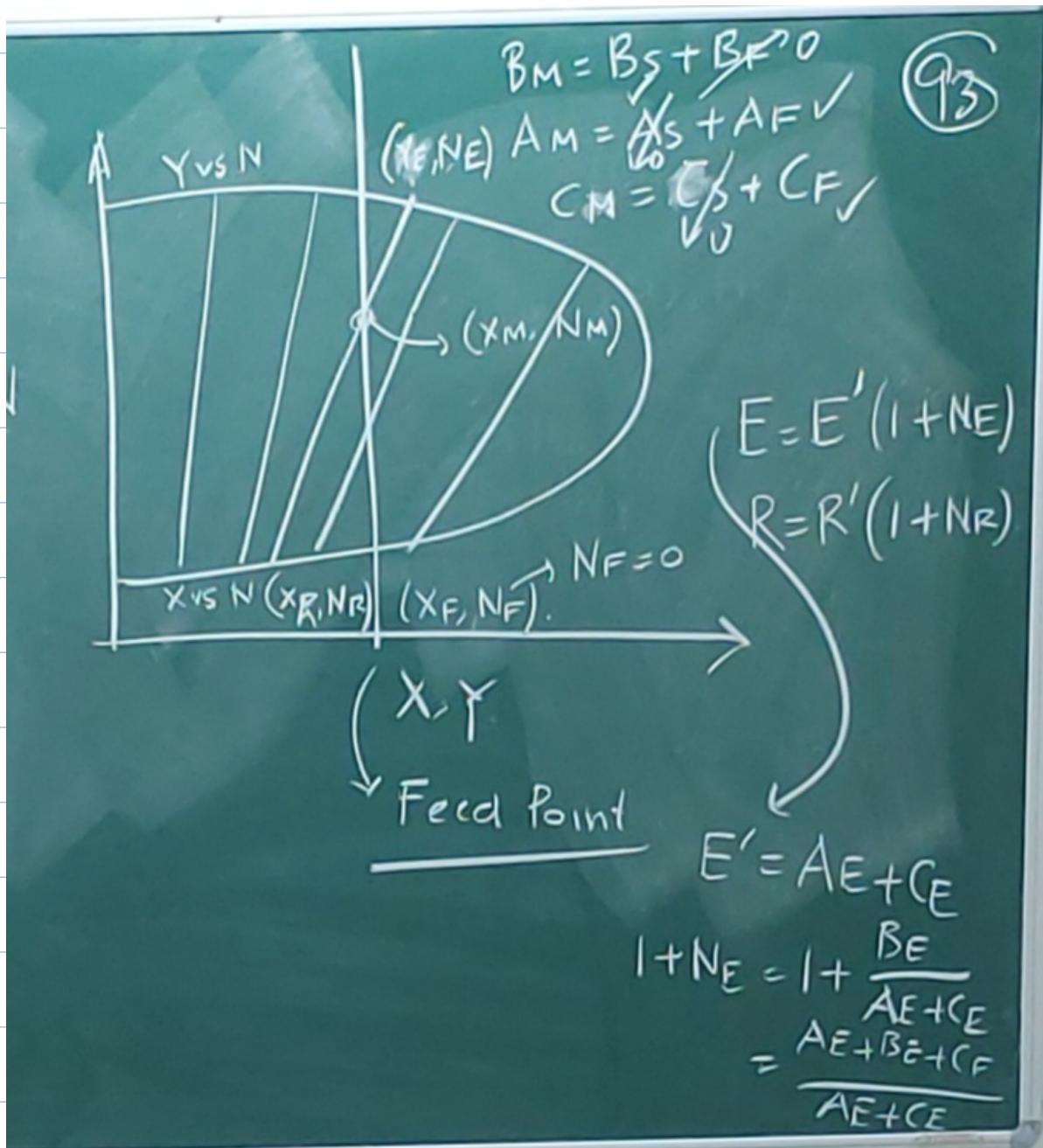
$$\text{Also } F = F' \Rightarrow \therefore B_F = 0$$

B-Free C balance \Rightarrow

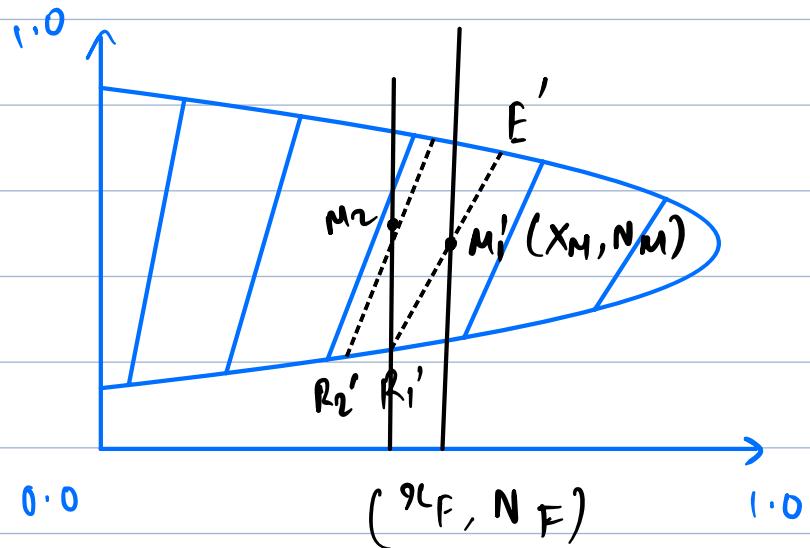
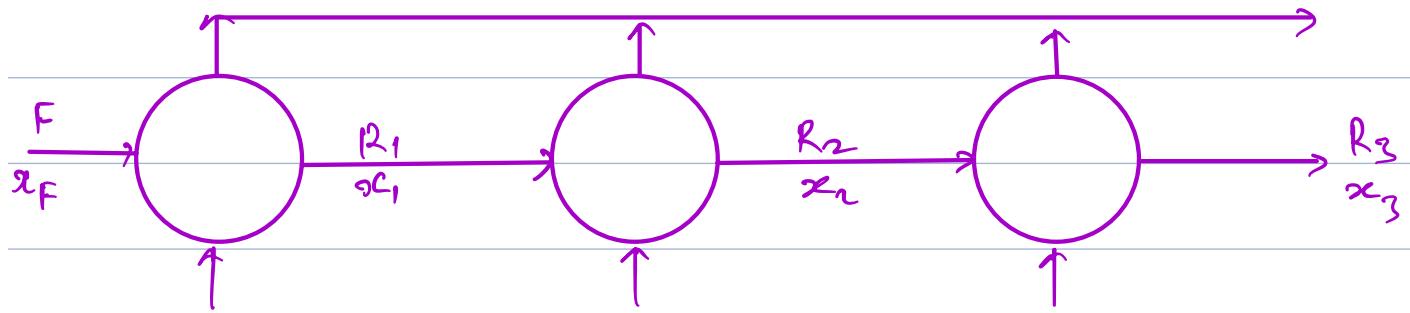
$$F' X_F + S' Y_S = M' X_M$$

$$F' X_F = M' X_M$$

$$X_F = X_M$$



Cross Flow by B-Free Basis (Pure Solvent)



Counter Flow on B Free basis

Overall balance: $F + S = M = E_i + R_{NP}$

Overall B-Free balance: $F' + S' = M = E' + R_{NP'}$

$$F' = M'$$

$F = F'$ (for pure solvent)

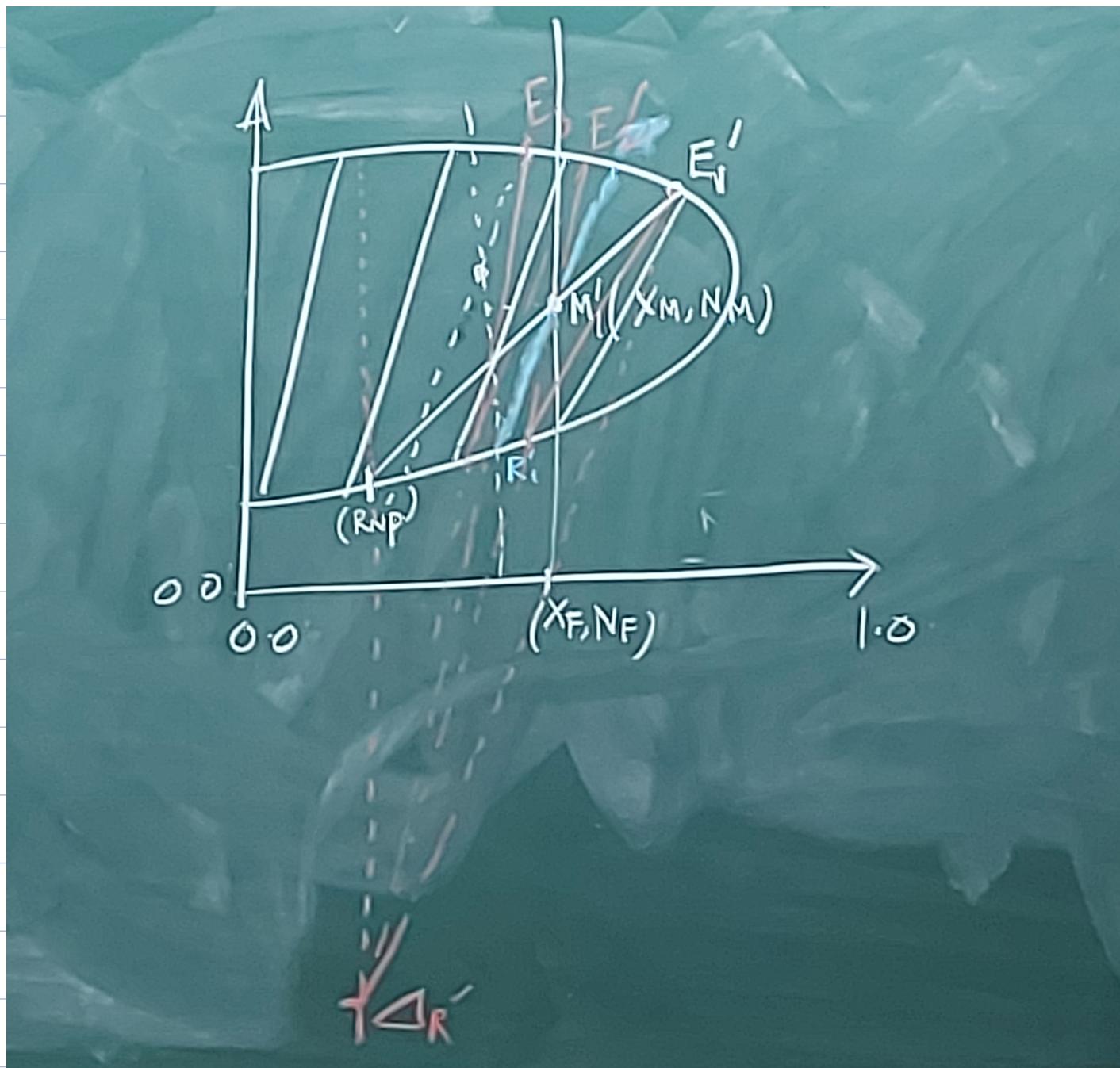
B-Free C balance:

$$F' x_F + S' y_S = M' x_M = E' y_{E_i} + R_{NP'} x_{NP}$$

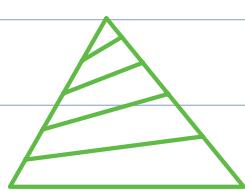
$$(x_F = x_M)$$

B-Free B balance:

$$F'N_F + S'N_S = M'N_M$$



When A, B, C are completely immiscible, the phase diagram is as follows:-



When A and B are completely immiscible we can use "c-free" notation.

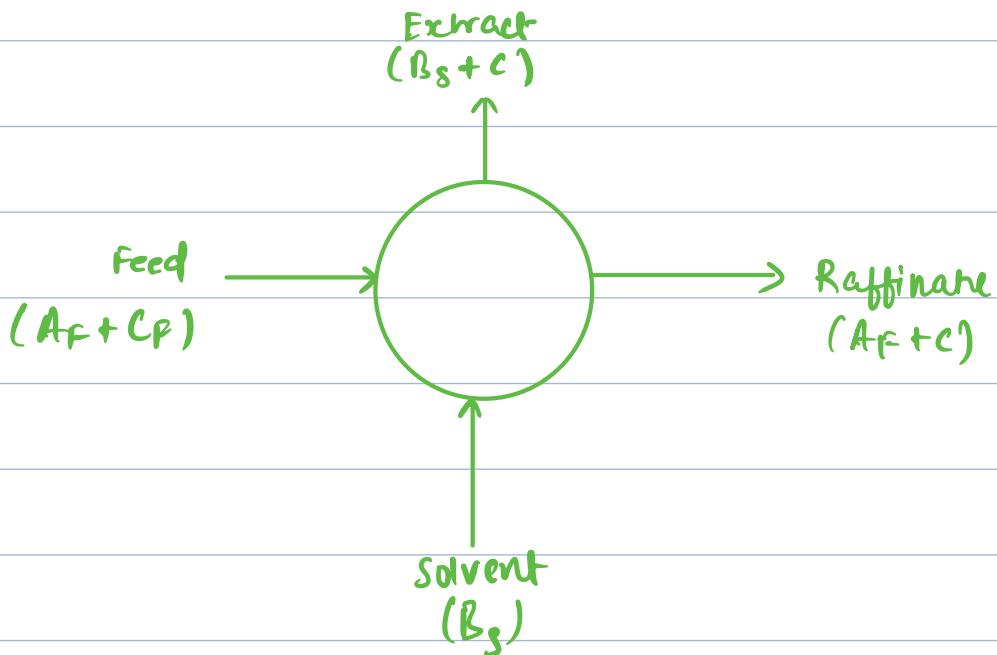
$$x' = \frac{x}{1-x}$$

x' : stream of raffinate (including feed)

$$y' = \frac{y}{1-y}$$

y' : stream of extract (including solvent).

SINCE A and B are COMPLETELY IMMISCIBLE



solute balance (c balance)

$$A_F x_F' + B_S y_S' = A_R x_R' + B_E y_E'$$

$$\frac{A_F \cdot c_F}{(A_F + B_F)} + \frac{B_S \cdot c_S}{(A_S + B_S)} = \frac{A_R \cdot c_R}{(A_R + B_R)} + \frac{B_E \cdot c_E}{(A_E + B_E)}$$

$$\begin{aligned} A_R &= A_F \\ B_S &= B_E \end{aligned}$$

\Rightarrow because of complete immiscibility of A and B.

$$A x_{F'} + B y_{S'} = A x_{R'} + B y_{E'}$$

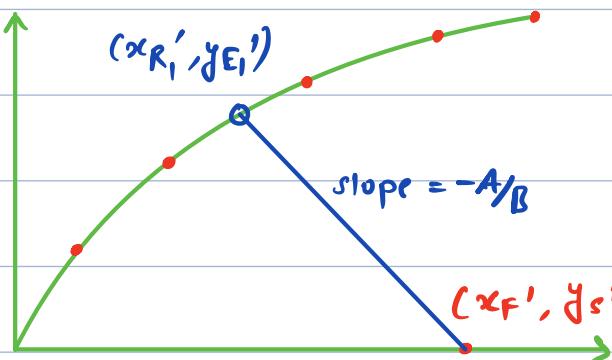
$$B(y_{S'} - y_{E'}) = -A(x_{P'} - x_{R'})$$

$$\frac{y_{S'} - y_{E'}}{x_{P'} - x_{R'}} = -\frac{A}{B}$$

\Rightarrow Need the equilibrium data in x' vs y' form.



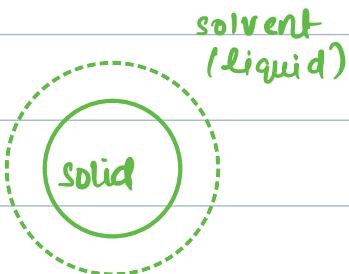
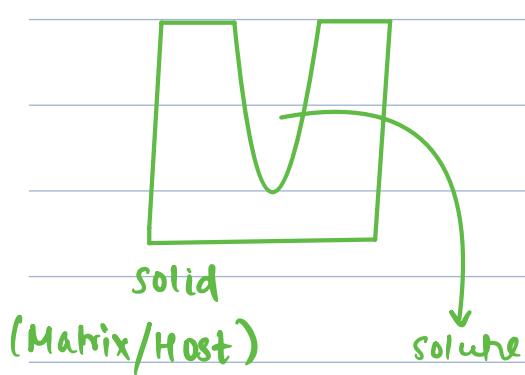
$x_{F'}$ is known
Pure solvent
A, B known



$(x_{F'}, y_{S'}) \rightarrow$ does not have any physical significance.

The line joining $(x_{R'}, y_{E'})$ and $(x_{F'}, y_{S'})$ has slope $-\frac{A}{B}$.

LEACHING



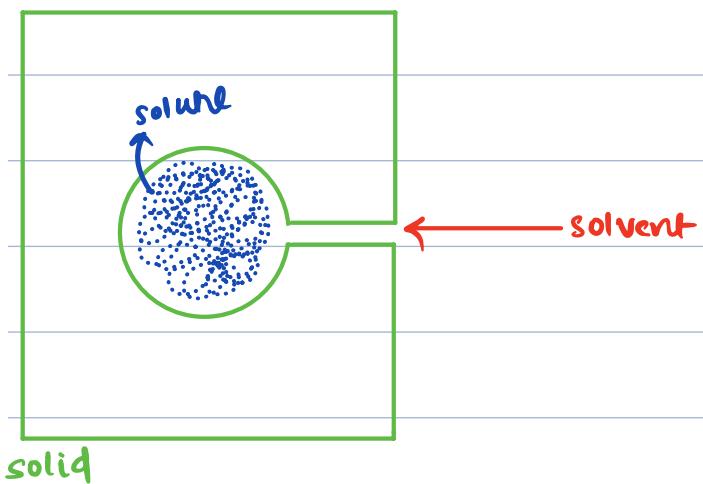
Lixivation :-

Decoction :- It is a special case of leaching when solvent is at boiling point.

Elutriation :- when the solute is mostly on the surface of the solid.

Solution Mining :-

steps



- ① Diffusion of the solvent to the pores.
- ② Dissolution of the solute inside the pores.
- ③ Outward diffusion

Problem Solving

$$x_F = 0.01 \Rightarrow x_F' = \frac{0.01}{0.99} = 0.010101$$

1. Nicotine (C) in water (A) solution containing 1.0 % nicotine is to be extracted with kerosene (B). Water and Kerosene are completely insoluble. Determine the percentage extraction of nicotine if 100 kg of feed solution is extracted in (a) One single stage with 150 Kg solvent; (b) three stages in cross flow configuration. All the stages use 50 Kg of kerosene.

(C) Same feed is now extracted in a counter current system. The target is to reduce the Nicotene content to 0.1%. Determine the number of stages if 115 KG of kerosene is used.

Equilibrium data:

x' (kg nicotine / kg water)	0	0.001011	0.00246	0.00502	0.00751	0.00998	0.0204
y'^* (kg nicotine / kg kerosene)	0	0.000807	0.001961	0.00456	0.00686	0.00913	0.0187



C-free balances

(a)

$$x_F = 0.01$$

$$x_{F'} = 0.010101$$

$$F = 100 \text{ kg}$$

$$A = A_F = 99 \text{ kg}$$

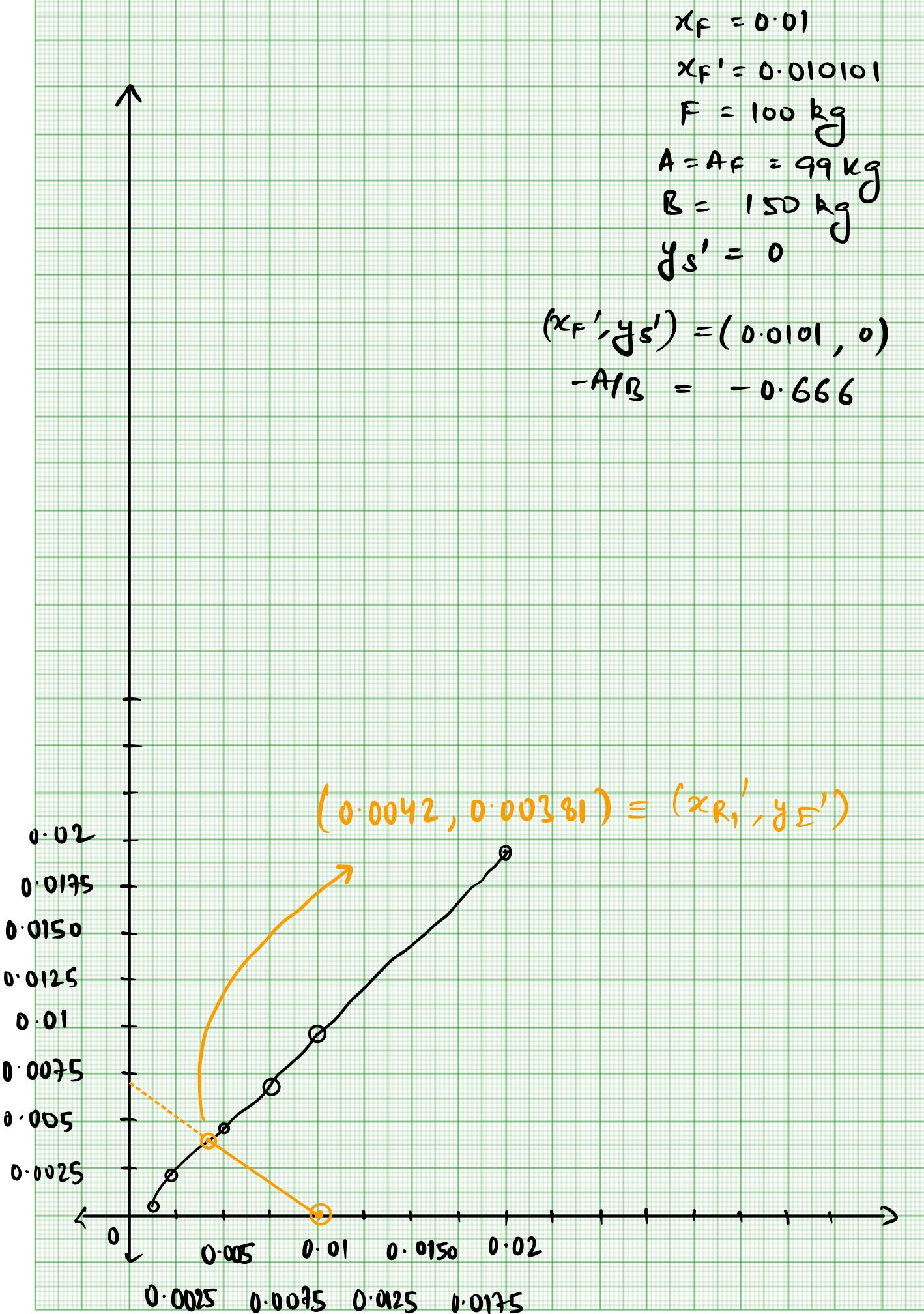
$$B = 150 \text{ kg}$$

$$y_s' = 0$$

$$(x_{F'}, y_{s'}) = (0.0101, 0)$$

$$-A/B = -0.666$$

$$(0.0042, 0.00381) \equiv (x_{R_1'}, y_{E'})$$

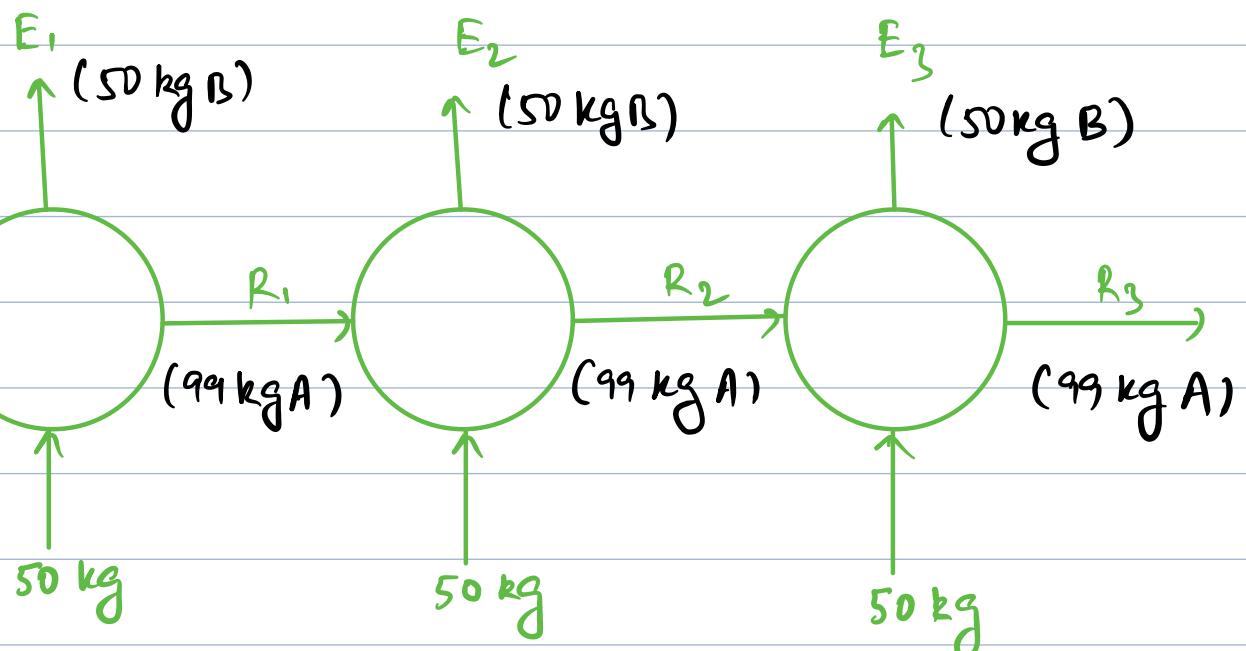


$A_F (x_F' - x_R')$ \Rightarrow Amount of C extracted

$$x_F' = \frac{C \text{ in } F}{A \text{ in } F} \quad x_R' = \frac{C \text{ in } R}{A \text{ in } R}$$

$$99(0.010101 - 0.0042) = 0.584199 \text{ kg}$$

$$\text{Ans} = \frac{0.584199}{1} \times 100\% = 58.42\%$$



For stage 1

$$x_F = 0.01 \Rightarrow x_F' = 0.010101$$

$$-A/B = -\frac{99}{50} = -1.98$$

Final Answer = 67%.

$$x_{R_1}' = 0.006875$$

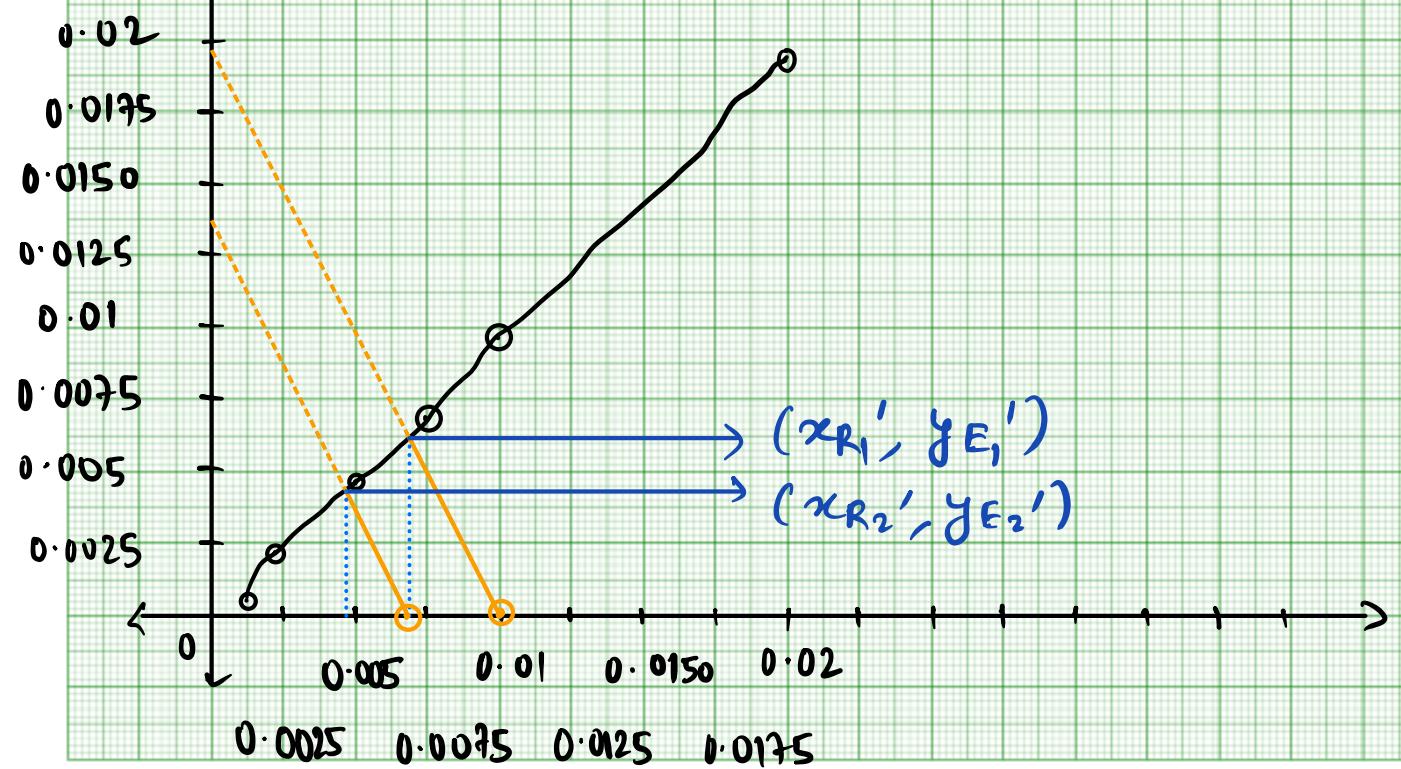
$$y_{E_1}' = 0.00625$$

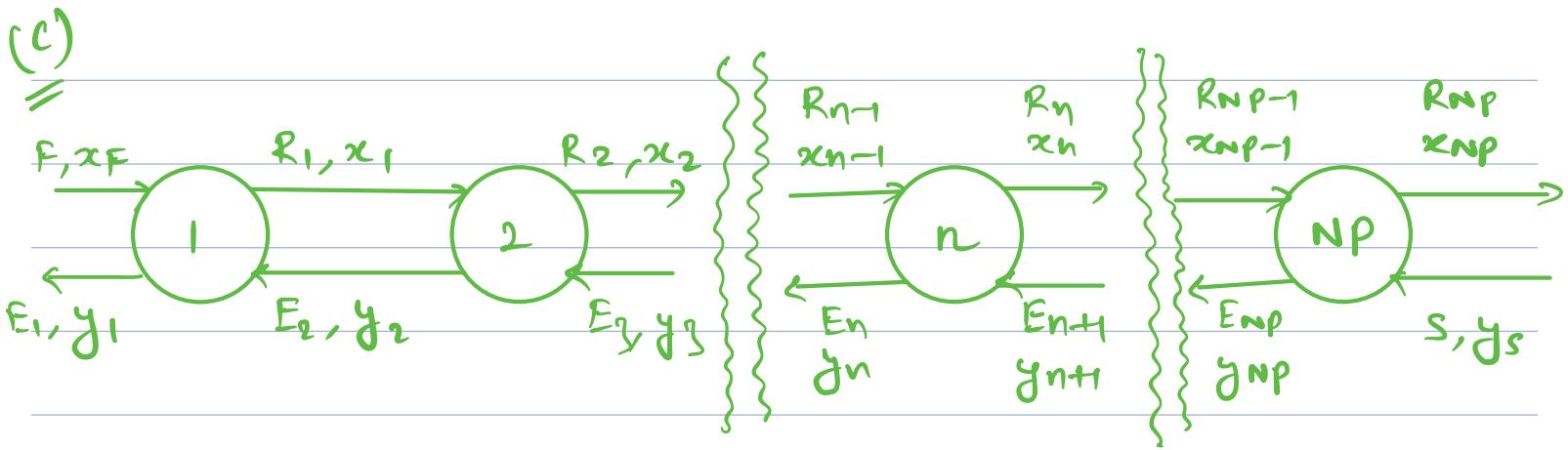
$$x_{R_2}' = 0.004175$$

$$y_{E_2}' = 0.004175$$

|
|
|

and so on.





Overall balance: $Fx_F + Sy_S = E_1y_1 + R_{NP}x_{NP}$

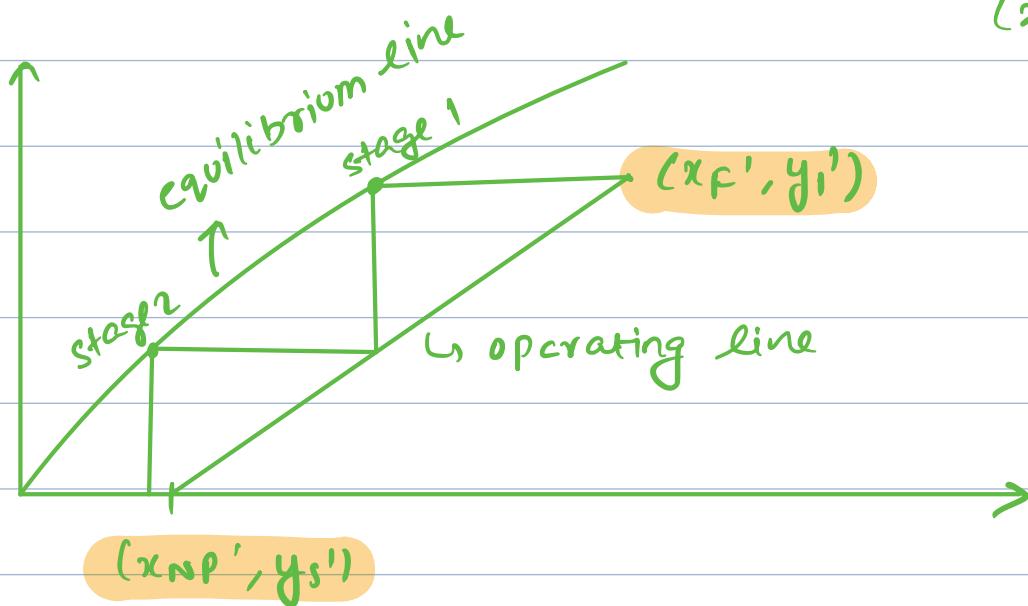
c-balance

$$By_S' + Ax_F' = Ax_{NP}' + By_1'$$

c-balance on c-free basis

$$\Rightarrow \frac{A}{B} = \frac{y_1' - y_S'}{x_F' - x_{NP}'} \Rightarrow \text{Find } y_1'$$

Locate (x_{NP}', y_S')
 (x_F', y_1')



$$y_1' = 0.0078$$

11 November

B → Insoluble (Inside which the solute is present),
C → Solute

A → Solvent

B Free coordinate

N, (x-y)

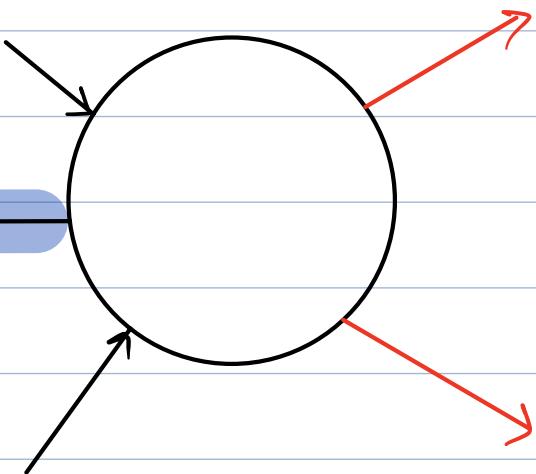
Feed

$$F = (A + C)_{\text{Feed}} = C_{\text{Feed}}$$

B = Insoluble

$$N_F = B_F / C_F$$

$$y_F = \frac{C_F}{A_F + C_F} = 1.0$$

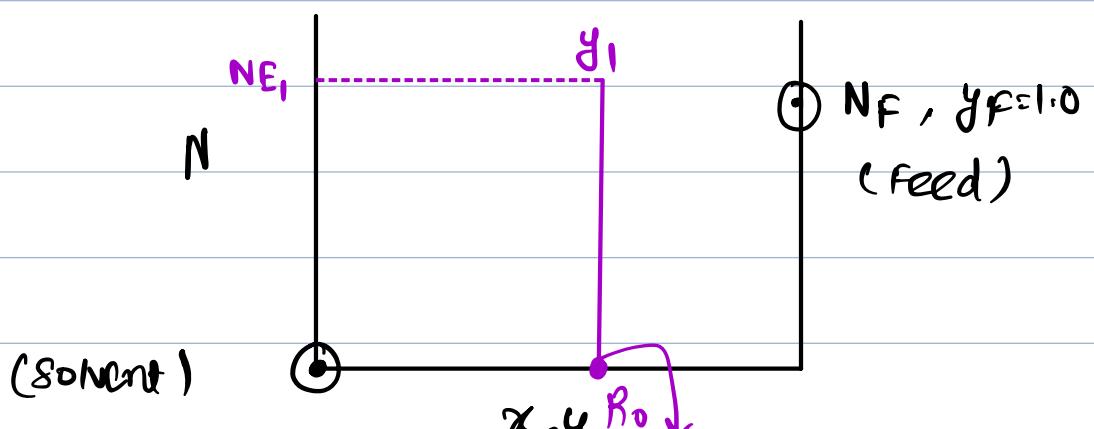


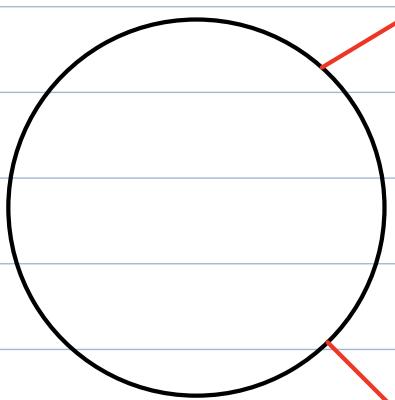
R_0 = Mass of the solvent

Solvent $C_S + A_S \approx A_S$ ($C_S = 0$)

$$x_0 = \frac{C_S}{A_S + C_S} = 0$$

$$N_0 = \frac{B_S}{A_S + C_S} = 0$$





leached solid (E_1)

$$E_1 = A + C$$

$$N_{E_1} = B/E_1$$

$$y_1 = \frac{C \text{ in } E}{(A+C) \text{ in } A}$$

Assumption
⇒ No C, A in
 E_1

leached solution (R_1)

$$R_1 = \text{mass of solution}$$

$$x_1 = \frac{\text{mass of } C}{(A+C) \text{ in } R}$$

$$N_{R_1} = \frac{\text{mass of } B}{(A+C) \text{ in } R}$$

Assumption
⇒ No B
in R_1

In practical situation

$$y_1 = x_1$$

