

Q1 A stack in an urban area is emitting 80 g/sec of NO_x. It has an effective stack height of 200m. The wind speed is 4 m/sec. at 10m. It is a clear summer day with the sun nearly overhead. Estimate the ground level concentration at
 a) 2 km downwind on the centreline and
 b) 2 km downwind, 100m off the centreline.

SOLN:- Given

$$x = 2000 \text{ m} (\text{downwind})$$

$$\text{Emission Rate} = 80 \text{ gm/sec.}$$

$$\text{Effective stack height (h)} = h + 4\Delta h = 200 \text{ m.}$$

$$\text{Wind speed at } 10 \text{ m } (u_1) = 4 \text{ m/sec.}$$

The wind speed at 200m can be calculated using formula

$$u_2 = u_1 \left(\frac{z_2}{z_1} \right)^p$$

It is mentioned in question that it is a clear summer day with the sun nearly overhead means it's belong to Neutral class (D).

From the dispersion coefficient graph for stability class D for $x = 2 \text{ km}$ the value of

$$P_z = 50 \text{ m.}$$

$$P_y = 130 \text{ m}$$

And the table,

Stability class	A	B	C	D	E	F
Rural	0.07	0.08	0.10	0.15	0.35	0.55
Urban	0.15	0.17	0.20	0.25	0.30	0.35

The value of p from here is 0.25

$$\begin{aligned} \text{So the wind speed at } 200 \text{ m } (u_2) &= u_1 \times \left(\frac{z_2}{z_1} \right)^p \\ &= 4 \times \left(\frac{200}{10} \right)^{0.25} \\ &= 4 \times 2.11 \\ &= 8.45 \text{ m.} \end{aligned}$$

The formula for calculating ground level concentration at centreline of plume ($y=0$) at height H .

$$c_{x,0} = \frac{Q}{\pi u \sigma_y \sigma_z} e^{-k_z (H^2/\sigma_z^2)}$$

$$X = 2000 \text{ m}$$

$$c_{2000,0} = \frac{80}{3.14 \times 8.45 \times 130 \times 50} e^{-k_z \left(\frac{200}{50}\right)^2}$$

$$= 0.000000155 \text{ gm/m}^3$$

$$= 0.155 \mu\text{gm/m}^3 (\text{Ans})$$

b) 2 km downwind and 100 m off the centreline

$$\text{means here } X = 2000 \text{ m}$$

$$Y = 100 \text{ m}$$

$$c_{x,y} = \frac{Q}{\pi u \sigma_y \sigma_z} e^{-k_z (Y^2/\sigma_y^2)} \cdot e^{-k_z (H^2/\sigma_z^2)}$$

$$c_{2000,100} = \frac{80}{3.14 \times 8.45 \times 130 \times 50} e^{-k_z \left(\frac{100}{130}\right)^2} \cdot e^{-k_z \left(\frac{200}{50}\right)^2}$$

$$=$$

$$= 1.15 \times 10^{-7} \text{ } \cancel{\text{gm}} / \text{m}^3$$

$$= 0.11564 \mu\text{gm/m}^3.$$

Q2 An industrial boiler is burning at 10 tons of 2.5% sulphur coal with an emission rate 151 gm/sec. the following exits: $H = 220 \text{ m}$ $U = 2 \text{ m/s}$ $\gamma = 0$. It is one hour before sunrise and the sky is clear. Find the downwind ground level SO_2 concentration at $x = 2 \text{ km}$ $y = 0$ $z = 0$.

$$\underline{\text{Sol}}) \text{ Emission rate } (Q) = 151 \text{ gm/sec.}$$

$$\text{Stack Height } (H) = 220 \text{ m}$$

$$\text{Wind speed } (U) = 2 \text{ m/s.}$$

$$\text{down wind distance for stack } x = 2 \text{ km} = 2000 \text{ m}$$

$$\text{cross wind distance } (y) = 0 \\ z = 0$$

It is given in the question that it is one hour before sunrise and the sky is clear so it belong to stability class F. (stable)

From the dispersion coefficient graph for stability class F the r_y & r_z are:

$$r_y = 70$$

$$r_z = 20$$

The ground level concentration can be calculated from

$$C_{x,y,z} = \frac{Q}{\pi r_y r_z U} e^{-y^2/2r_y^2} \left[e^{-(z-H)^2/2r_z^2} + e^{-(z+H)^2/2r_z^2} \right]$$

But here $y = 0$ and $z = 0$ so.

$$C_{x,0,0} = \frac{Q}{\pi r_y r_z U} e^{-y_2 (H^2/r_z^2)} \\ = \frac{151}{3.14 \times 70 \times 20 \times 2} e^{-1/2 (220/20)^2}$$

$$= 9.13 \times 10^{-29} \text{ gm/m}^3$$

$$= 9.13 \times 10^{-23} \mu\text{gm/m}^3 \text{ Ans}$$

Q3 A 500 MW thermal power plant burns 18000 tons of coal per day containing 0.58% sulphur. The plant emits the flue gasses into the atmosphere through a stack of inside diameter 1.5 m and height of 60 m. The velocity and the temperature of the plume at the exit are 5 m/sec and 155°C respectively. The ambient air temperature is 28°C and the wind speed at the stack altitude is 7 m/s. The barometric pressure is 825 milibar at the top of the stack. Assume a moderately stable plume.

- Calculate the effective height of stack.
- What is the downwind SO₂ concentration in the plume centreline at a distance of 2 km in the day time?
- Calculate the maximum concentration of SO₂ along the centreline of the plume and at what downwind distance it will occur.
- Show a concentration profile of SO₂ up to 10 km downwind distance and 800 m along the crosswind distance.

Sol) Stack diameter = 1.5 m

Stack height (h) = 60 m

Velocity of stack (v_s) = 5 m/sec.

Stack temperature (T_s) = 155°C + 273 = 428 K.

Ambient air Temperature (T_a) = 28°C + 273 = 301 K

Pressure = 825 milibar.

Wind speed at stack altitude (u) = 7 m/sec.

a) Now we have to calculate effective stack Height

$$H = h + \Delta h_v$$

Δh_v can be calculated using formula:-

$$\Delta h_v = \frac{v_s D}{u} \left[1.5 + 2.68 \times 10^{-3} \cdot P \cdot D \left(\frac{T_s - T_a}{T_s} \right) \right]$$

$$= \frac{5 \times 1.5}{7} \left[1.5 + 2.68 \times 10^{-3} \times 825 \times 1.5 \left(\frac{428 - 301}{428} \right) \right]$$

$$\begin{aligned}
 &= \frac{5 \times 1.5}{7} \left[1.5 + 2.68 + 10^{-3} \times 825 \times 1.5 \times \frac{0.296}{0.447} \right] \\
 &= 1.07 \times \left[1.5 + \frac{0.984}{1.396} \right] \\
 &= 1.07 \times 2.484 \\
 &= 2.657 \text{ m}
 \end{aligned}$$

Effective stack height $H = h + 1.5 \text{ m}$

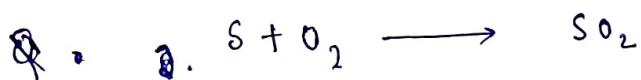
$$\begin{aligned}
 &= 60 + \frac{2.657}{1.396} \text{ m} \quad 2.657 \text{ m} \\
 &= 62.098 \text{ m}. \quad (Aprox) \quad 62.657 \text{ m} (A \text{ m})
 \end{aligned}$$

(b) The downwind SO_2 concentration in the plume centerline at a distance of 2 km in the day time.

For this we have to calculate emission rate of $\text{SO}_2 (\dot{Q})$
this power plant burns 18000 tons / day of coal containing
0.58% sulphur content SO

$$\dot{Q} = 18000 \text{ tons/day} = \frac{18000 \times 10^3}{24 \times 60 \times 60} \text{ kg/sec.} = 208 \text{ kg/sec.}$$

$$\begin{aligned}
 \text{Sulphur content} &= 0.58\% \\
 &= 208.33 \times 0.0058 \\
 &= 1.208 \text{ kg/sec.}
 \end{aligned}$$



$$\text{Sulphur per second} = 208.33 \times 0.0058 = 1.208 \text{ kg/sec.}$$

1 mol of sulphur produces 2 kg of SO_2

$$\text{SO}_2 = 2 \times 1.208$$

$$\text{SO}_2 = 2.416 \text{ kg/sec.}$$

$$\dot{Q} = 2416 \text{ gm/sec.}$$

From the dispersion coefficient graph at 2 km at
stable (F) class

$$C_y = 70 \quad C_z = 20$$

For the concentration of SO_2 at centreline, $y = 0$

$$\begin{aligned}
 C_{x,0} &= \frac{\rho}{\pi u r_y r_z} \cdot e^{-V_2 \cdot h^2 / r_z^2} \\
 &= \frac{2416}{3.14 \times \underbrace{7 \times 70 \times 20}_{0.0785}} e^{-V_2 \left(\frac{62.657}{20} \right)^2} \\
 &\sim 0.00740 \\
 &= 0.000580 \text{ g/m}^3 \\
 &= 580 \text{ mg/m}^3 (\text{Am})
 \end{aligned}$$

- ③ The maximum concentration of SO_2 along the centrelne of the plume & at what downwind distance it will occur.

For maximum concentration of SO_2 , $F_2 = 0.7074$

$$F_2 = 0.707 \times 62.657 \\ = 44.298 \text{ m}$$

From the dispersion coefficient graph for $r_2 = 44.298$

the down wind distance $x = 10.3$ km

= 10300 meter.

From this graph $r_y = 300\text{m}$

The maximum concentration of SO_2

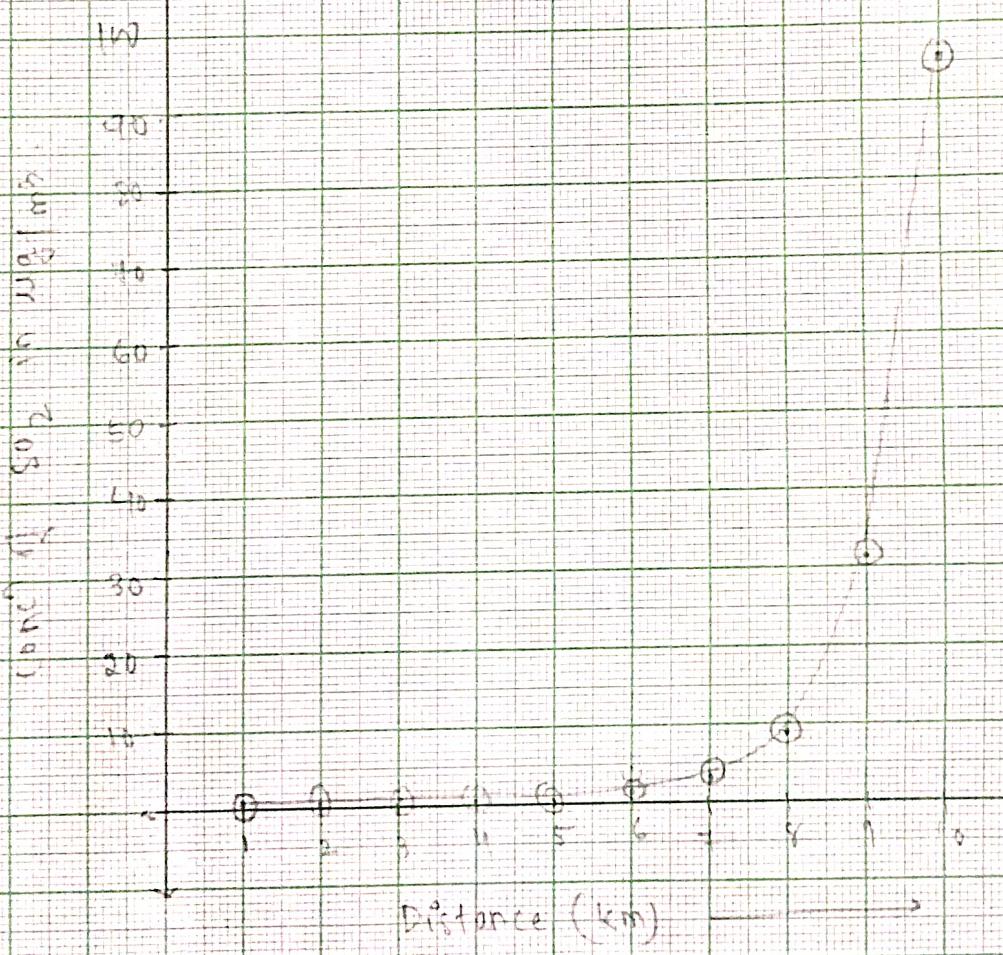
$$\begin{aligned}
 C_{\max} &= \frac{\rho}{\pi u r y R_2} e^{-V_2 H^2 / R_2^2} \\
 &= \frac{2416}{3.14 \times 7 \times 300 \times 44.298} e^{-V_2 (62.657 / 44.298)^2} \\
 &= \frac{0.00827}{0.003678} \\
 &= 0.003042 \text{ gm/m}^3 \\
 &= 3042 \text{ mg/m}^3 \text{ Ans.}
 \end{aligned}$$

d) Concentration profile of SO_2 up to 10 km downwind and 800m along the cross wind distance.

$$C_{x,y} = \frac{q}{\pi u r_y r_2} e^{-r_2 (h/r_2)^2} \cdot e^{-\frac{1}{2} (\frac{y}{r_y})^2}$$

$$y = 800 \text{ m.} = 0.8 \text{ km}$$

S. No	Distance (km)	r_y (m)	r_2 (m)	C_{SO_2} $\mu\text{g}/\text{m}^3$
1	1	35	16	0
2	2	71	22	0
3	3	93	26	0
4	4	130	30	0
5	5	150	35	0
6	6	190	38	0.5
7	7	200	42	1.44
8	8	230	43	9.07
9	9	260	46	31.95
10	10	300	50	95.43



Q4/ A stack gas from a cement clinkers emit dust at the rate of 115.0 gm/sec. at a temperature of 175°C , velocity 8 m/sec and barometric pressure of 977 milibars. A slightly unstable plume is found at the exit of the chimney. The ambient air temperature is 30°C and wind velocity is 4 m/sec. A chimney of 96 cm diameter may be used for dispersion. Under slightly unstable condition calculate:-

- Effective stack height?
- The concentration of dust at a distance of 6km downwind along the centralline of the plume
- Maximum ground level concentration of dust and at which it will occur?

Sol? :- Given:-

Emission rate of stack gas (Q) = 115 gm/sec.

Stack gas temperature (T_s) = 175°C

$$175 + 273 = 448\text{K}$$

Stack gas velocity (V_s) = 8 m/sec

Barometric Pressure (P) = 977 milibar

Ambient Temperature (T_a) = 30°C

$$30 + 273 = 303\text{K}$$

Wind velocity (U) = 4 m/sec.

Chimney diameter (D) = 96 cm = 0.96 m.

It is given that the condition is for slightly unstable condition so belong to class 'c'.

(a) Effective stack height $H = h + 4hD$

We have to calculate for physical stack height

$$h = 74 (Q_p)^{0.27}.$$

δ_p = Particulate Emission Rate in Ton/hr.

Emission rate $\delta = 115 \text{ gm/sec.}$

$$\begin{aligned} \text{convert it to ton/hr} &= 115 \times 10^{-6} \text{ ton} \times 3600 \\ &= 414000 \times 10^{-6} \\ &= 0.414 \text{ ton/hr} \end{aligned}$$

$$\begin{aligned} h &= 74 (\delta_p)^{0.27} \\ &= 74 \times (0.414)^{0.27} \\ &= 58.32 \text{ m.} \end{aligned}$$

Now we have to calculate Δh_v

$$\begin{aligned} \Delta h_v &= \frac{V_s D}{u} \left[1.5 + 2.68 \times 10^{-3} \rho \cdot D \times \frac{T_s - T_a}{T_b} \right] \\ &= \frac{8 \times 0.96}{4} \left[1.5 + 2.68 \times 10^{-3} \times 977 \times 0.96 \times \left(\frac{448 - 303}{448} \right) \right] \\ &= 1.92 \times 2.313 \\ &= 1.92 \times 2.313 \\ &= 4.44 \text{ m} \end{aligned}$$

Now the effective stack height $H = h + \Delta h_v$

$$\begin{aligned} &= 58.32 + 4.44 \\ &= 62.760 \text{ m.} \end{aligned}$$

b) conc' of dust at a distance 6 km downwind along the centreline of the plume.

conc' of dust at centreline of the plume can be calculated using formula ($y = 0$)

$$C_{x,0} = \frac{\delta}{\pi u \sigma_y \sigma_z} \cdot e^{-V_2 (H^2 / \sigma_z^2)}$$

Here x downwind distance = 6 km

And it belongs to stability class 'c'

so from the dispersion coefficient graph

the value of $r_z = 300 \text{ m}$
 $r_y = 550 \text{ m}$.

$$C_{6\text{Km}, 0} = \frac{115}{3.14 \times 4 \times 300 \times 550} e^{-r_z \left(\frac{62.760}{300} \right)^2}$$

$$= 5.54 \times 10^{-5} \quad 0.978$$

$$= 5.42 \times 10^{-5} \text{ gm/m}^3$$

$$= 54.2 \text{ ug/m}^3 \text{ (A.m)}$$

(c) max^m ground level concentration and at which it will occur.

for max^m concentration the value of $r_z = 0.7074$

$$r_z = 44.37 \text{ m}$$

The downwind distance at which it will occur is

corresponds to r_z from dispersion coefficient graph

the down wind distance

$$n = 0.7 \text{ Km} = 700 \text{ m}$$

$$\sigma_y = 80 \text{ m}$$

$$C_{\max} = \frac{a}{\pi u \sigma_y r_z} e^{-r_z (H/r_z)^2}$$

$$= \frac{115}{3.14 \times 4 \times 80 \times 44.37} e^{-r_z \left(\frac{62.76}{44.37} \right)^2}$$

$$= 0.000946 \text{ gm/m}^3 \quad 0.367$$

$$= 946 \text{ ug/m}^3 \text{ A.m.}$$

Q5 A coal burning plant burns 24000 tons of coal / day. The coal has a sulphur content 1.7%. The physical stack height h is 200 ft. Inside diameter of stack at exit is 0.8 m, stack gas velocity is 18.3 m/sec. which leaves the chimney at a temperature of 140°C . Ambient air temperature is 28°C . The atmospheric pressure is 1000mbar and prevailing wind speed is 4.5 m/sec.

- Calculate the effective stack height.
- What is the maximum concentration of SO_2 at the ground level? Use moderately unstable condition of plume.
- Calculate the concentration of SO_2 at a distance of 5km away from the plant. Also how the concentration profile of SO_2 up to 3km from the chimney.

Sol: Given data: capacity of plant = 24000 TPD.

sulphur content = 1.7%.

physical stack height, $h = 200\text{ ft}$

Inside diameter of stack $D = 0.8\text{ m}$

Stack gas velocity $V_s = 18.3\text{ m/sec.}$

Temperature of gas (T_g) = $140^{\circ}\text{C} = 413\text{ K}$

Ambient air temperature $T_a = 28^{\circ}\text{C} = 301\text{ K}$

pressure $P = 1000\text{ mbar}$

Wind speed $u = 4.5\text{ m/s.}$

a) Effective stack height $H = h + Ahv$

$$Ahv = \frac{V_s D}{u} \left[1.5 + 2.68 \times 10^{-3} \times P \times D \times \left(\frac{T_g - T_a}{T_g} \right) \right]$$

$$= \frac{18.3 \times 0.8}{4.5} \left[1.5 + 2.68 \times 10^{-3} \times 1000 \times 0.8 \times \frac{413 - 301}{413} \right]$$

$$= 6.771 \text{ m.}$$

$$\text{Given } h = 200 \text{ ft} = 60.96 \text{ m.}$$

$$Y = h + \Delta h v = 60.96 + 6.771 \text{ m} = 67.731 \text{ m.} \\ = 222.2 \text{ ft.}$$

b) Maximum ground level concentration of SO_2

$$C_{\max} = \frac{Q}{\pi u \sigma_y \sigma_z} e^{-Y_2 H^2 / \sigma_z^2}$$

$$\text{For } C_{\max}, \sigma_z = 0.707 \text{ m}$$

$$\sigma_z = 0.707 \times 67.731$$

$$= 47.885 \text{ m.}$$

It was given that stability class is (B) [moderately unstable]
From dispersion coefficient graph corresponding σ_y

value is

$$\sigma_y = 77 \text{ m}$$

$$\text{corresponding downwind distance } X = 0.43 K m \\ = 430 \text{ m.}$$

Now we have to calculate Emission rate (Q) of SO_2

$$\text{Sulphur content} = \frac{24000 \times 10^3}{86400} \times 0.017$$

$$= 4.722 \text{ kg/s}$$

$$= 4722.22 \text{ gm/sec.}$$



4.722 kg s gives 9.44 kg SO_2

$$Q_{\text{SO}_2} = 9444 \text{ gm/sec.}$$

$$C_{\max} = \frac{9444}{3.14 \times 4.5 \times 77 \times \underbrace{47.885}_{0.1812}}$$

$$e^{-1/2 \left(\frac{67.731}{47.885} \right)^2}$$

$$\approx 0.367$$

$$= 0.0666 \text{ g/m}^3$$

$$= 66.66 \text{ mg/m}^3 (\text{Nm})$$

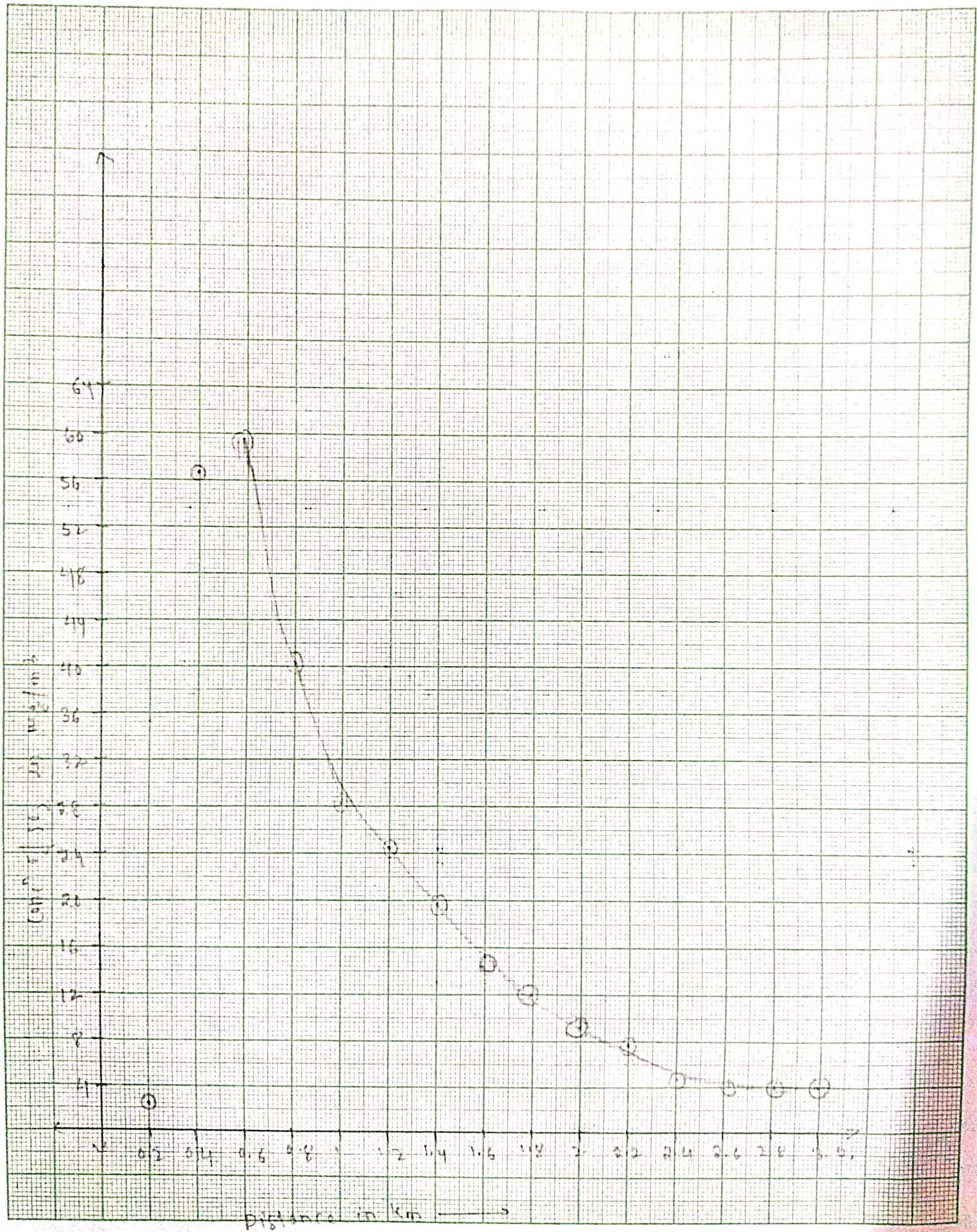
c) Concentration of SO_2 at 5km distance.

downward distance = 5 Km $r_z = 620 \text{ m}$
for class (B) $r_y = 680 \text{ m}$

$$\begin{aligned} C_{\text{SO}_2} &= \frac{Q_{\text{SO}_2}}{\pi u r_y r_z} e^{-V_2 (H^2 / r_z^2)} \\ &= \frac{9444}{3.14 \times 4.5 \times 680 \times 620} \times e^{-V_2 \left(\frac{67.731}{620} \right)^2} \\ &\quad \text{~~~~~} 0.9940 \\ &= 0.00157 = 1.5 \text{ mg/m}^3 \\ &\quad \underline{1.5 \text{ mg/m}^3}. \end{aligned}$$

c) Show the concentration profile of SO_2 up to 3km from
Given stability (Max B)

S. No	Distance km	$r_y(\text{m})$	$r_z(\text{m})$	$C_{\text{SO}_2} (\text{mg/m}^3)$
1.	0.2	38	20	2.8417
2.	0.4	70	40	56.8899
3.	0.6	100	65	59.717
4.	0.8	140	85	40.8667
5.	1.0	165	120	28.7707
6.	1.2	180	140	23.5813
7.	1.4	210	150	19.1517
8.	1.6	235	180	14.7132
9.	1.8	270	200	11.6814
10.	2.0	300	230	9.2707
11.	2.2	320	250	8.0494
12.	2.4	350	270	6.85
13.	2.6	380	300	5.7124
14.	2.8	420	320	4.86
15.	3	440	350	4.2573



Q6 A 100 MW power plant burns 10000 tones of 1.5% S containing coal/day. The flue gases are emitted into the atmosphere through a stack of height 200m. and the diameter of stack at the plume exit is 0.5m. The velocity and temperature of the plume is 10 m/s and 120°C respectively at the exit. What is the downwind concentration of SO₂ in the plume centralline at a distance of 5Km for class D plume (neutral)? Assume the ambient temperature is 15°C and wind velocity is 6m/sec.

Sol Given:-

$$\text{Coal burned} = 10000 \text{ tones per day}$$

$$\text{Stack Height (h)} = 200 \text{ m}$$

$$\text{Diameter of the stack} = 0.5 \text{ m}$$

$$\text{Stack velocity (V_s)} = 10 \text{ m/s}$$

$$\text{Stack exit temperature (T_s)} = 120^\circ\text{C} + 273 = \\ = 393 \text{ K}$$

$$\text{Ambient temperature (T_a)} = 15^\circ\text{C} + 273 \\ = 288 \text{ K}$$

$$\text{Wind velocity (u)} = 6 \text{ m/sec}$$

It is given in the question that the plume is class D(Neutral) plume.

lets assume pressure (P) = 100 millibar

so calculate the effective stack height (H)

$$H = h + \Delta h_{nv}$$

$$\Delta h_{nv} = \frac{V_s \cdot D}{u} \left[1.5 + 2.68 \times 10^{-3} P \cdot D \left(\frac{T_s - T_a}{T_s} \right) \right]$$

$$= \frac{10 \times 0.5}{6} \left[1.5 + 2.68 \times 10^{-3} \times 100 \times 0.5 \times \left(\frac{393 - 288}{393} \right) \right]$$

$$= 0.833 \times 1.535$$

$$= 1.27 \text{ m}$$

$$\text{Effective stack Height (H)} = h + \Delta h v$$

$$= 200 + 1.27$$

$$= 201.27 \text{ m.}$$

For calculating the downwind concentration of SO_2 in the plume centreline at a distance of 5 km ($y=0$)

$$C_{x,0} = \frac{Q}{\pi u \sigma_y \sigma_z} e^{-\frac{x}{2} \left(\frac{H^2}{\sigma_z^2} \right)}$$

we have to first calculate the emission rate $Q (\text{kg}/\text{s})$

~~Given~~ Sulphur content = 1000 ton per day of 1.5 yrs

$$= \frac{100000 \times 10^3}{24 \times 60 \times 60} \times 0.015$$

$$= 1.736 \text{ kg/sec.}$$



1.736 kgs gives 3.472 kg/s

$$Q_{\text{SO}_2} = 3.472$$

~~Given~~ For stability class D at $x = 5 \text{ km}$, from the dispersion coefficient graph the value of $\sigma_y \& \sigma_z$ is

$$\sigma_y = 300 \text{ m}$$

$$\sigma_z = 90 \text{ m.}$$

$$C_{(5000,0)} = \frac{3472}{3.14 \times 6 \times 300 \times 90} \cdot e^{-\frac{x}{2} \left(\frac{H^2}{\sigma_z^2} \right)}$$

$$= 0.000565 \text{ gm/m}^3$$

$$= 565 \text{ ug/m}^3 (\text{Nm})$$

Q7 SO_2 is emitted through a stack 50m Height and 2m diameter at the exit at a temperature of 120°C , with a velocity of 10 m/sec. the SO_2 emission rate is 200 g/sec. show how the ground level concentration at a down level distance of 1km varies with wind speed for stability category D when the Pressure is 100 milibar and ambient temperature is 25°C .

Soln:- Given stack Height (h) = 50 m

stack Diameter (D) = 2 m

$$\begin{aligned}\text{Stack exit temperature } (T_s) &= 120^\circ\text{C} + 273 \\ &= 393 \text{ K}\end{aligned}$$

stack gas velocity (V_s) = 10 m/sec.

Emission rate of SO_2 $Q(\text{SO}_2)$ = 200 g/sec.

Pressure is (P) = 100 milibar

$$\begin{aligned}\text{Ambient temperature } (T_a) &= 25^\circ\text{C} + 273 \\ &= 298 \text{ K}\end{aligned}$$

first we have to calculate effective stack height (H)

$$H = h + \Delta h_V$$

$$\Delta h_V = \frac{V_s D}{u} \left[1.5 + 2.68 \times 10^{-3} P \cdot D \left(\frac{T_s - T_a}{T_s} \right) \right]$$

How the ground level concentration at a down level distance of 1km varies with wind speed so we are taking wind speed of 1, 2, 4, 6, 8

$$\text{If } u = 1 \text{ m}$$

$$\begin{aligned}\Delta h_V &= \frac{10 \times 2}{1} \left[1.5 + 2.68 \times 10^{-3} \cdot 100 \times 2 \times \left(\frac{393 - 298}{393} \right) \right] \\ &= 20 \times 1.629 \\ &= 32.58 \text{ m.}\end{aligned}$$

$$\text{Effective stack height (H)} = h + \Delta h_v \\ = 50 + 32.58 \\ = 82.58 \text{ m.}$$

Concentration of SO_2 at a downwind distance 1km.

$$C_{1000,0} = \frac{Q}{\pi u \sigma_y \sigma_z} e^{-V_2 \frac{H^2}{\sigma_z^2}}$$

σ_y and σ_z at 1km distance
dispersion coefficient graph is

$$\sigma_y = 70 \text{ m} \quad \sigma_z = 30 \text{ m}$$

$$C_{1000,0} \quad Q = 200 \text{ g/sec.}$$

$$C_{1000,0} = \frac{200}{3.14 \times 1 \times 70 \times 30} e^{-V_2 \left(\frac{82.58}{30}\right)^2}$$

$$= 0.000691 \text{ gm/m}^3$$

$$= 691 \text{ ug/m}^3$$

If wind speed $u = 2 \text{ m/sec}$

$$\Delta h_v = \frac{V_s D}{u} \left[1.5 + 2.68 \times 10^{-3} P.D. \left(\frac{T_s - T_a}{T_s} \right) \right]$$

$$= \frac{10 \times 2}{2} \left[1.5 + 2.68 \times 10^{-3} \times 100 \times 2 \left(\frac{393 - 298}{393} \right) \right]$$

$$= 16.29 \text{ m}$$

$$H = h + \Delta h_v \\ = 50 + 16.29 \\ = 66.29 \text{ m.}$$

$$C_{1000,0} = \frac{200}{3.14 \times 2 \times 70 \times 30} e^{-V_2 \left(\frac{66.29}{30}\right)^2}$$

$$= 0.001334 \text{ gm/m}^3$$

$$= 1334 \text{ ug/m}^3 \text{ Ans.}$$

If wind speed (u) = 4 m/sec.

$$\Delta h_{vr} = \frac{10 \times 2}{4} \left[1.5 + 2.68 \times 10^{-3} \times 100 \times 2 \times \left(\frac{393 - 298}{393} \right) \right] \\ = 8.145 \text{ m}$$

$$H = 50 + 8.145$$

$$= 58.145$$

$$C_{1000,0} = \frac{200}{3.14 \times 4 \times 70 \times 30} e^{-\gamma_2 (58.145/30)^2} \\ = 0.001167 \text{ gm/m}^3 \\ = 116.7 \text{ ug/m}^3.$$

If wind speed u = 6 m/sec.

$$\Delta h_{vr} = \frac{10 \times 2}{6} \left[1.5 + 2.68 \times 10^{-3} \times 100 \times 2 \times \left(\frac{393 - 298}{393} \right) \right] \\ = 5.43 \text{ m}$$

$$H = 50 + 5.43 = 55.43$$

$$C_{1000,0} = \frac{200}{3.14 \times 6 \times 70 \times 30} e^{-\gamma_2 (55.43/30)^2} \\ = 0.000914 \text{ gm/m}^3 \\ = 914 \text{ ug/m}^3$$

If wind speed is 8 m/sec.

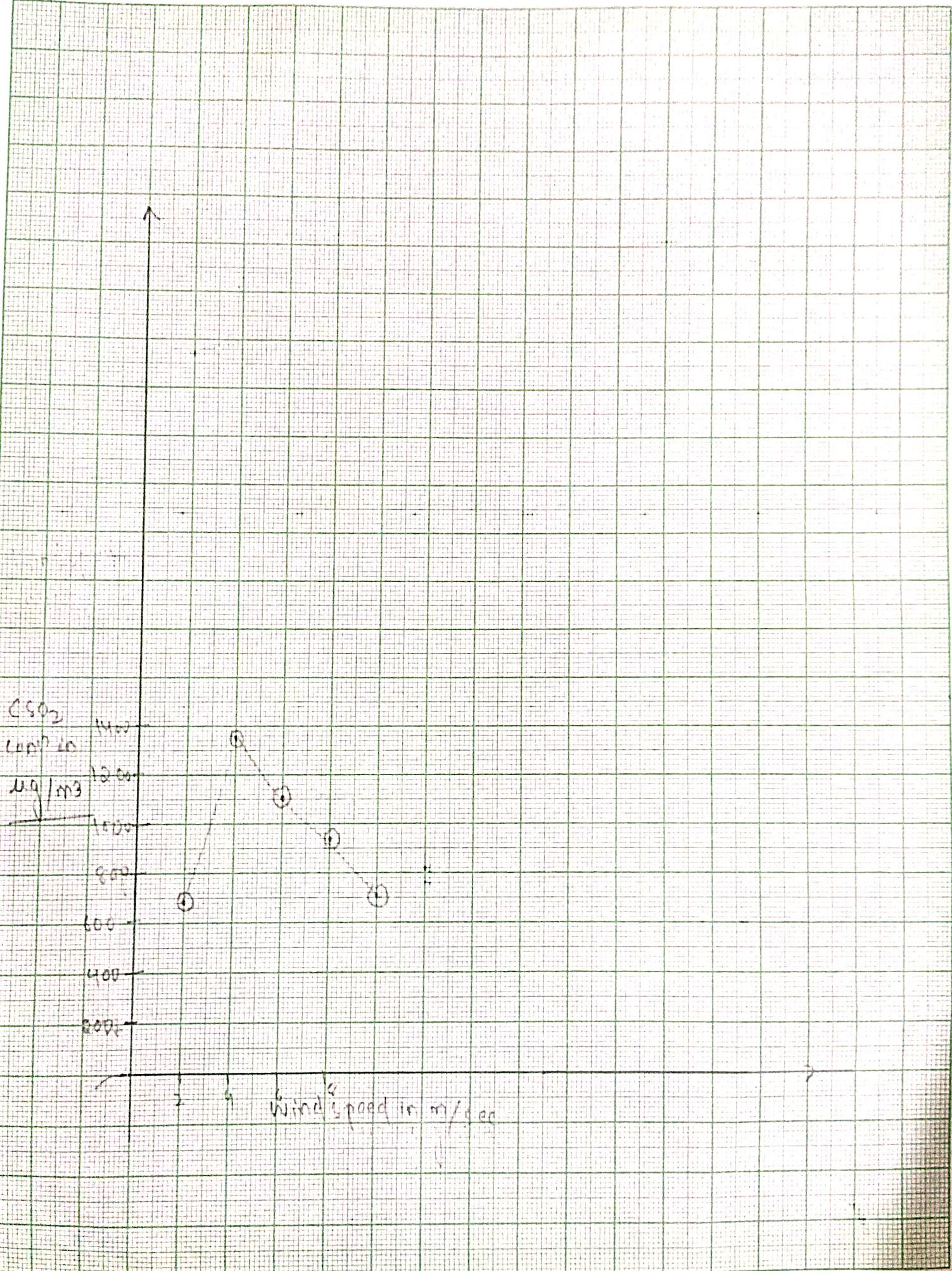
$$\Delta h_{vr} = \frac{10 \times 2}{8} \left[1.5 + 2.68 \times 10^{-3} \times 100 \times 2 \times \left(\frac{393 - 298}{393} \right) \right] \\ = 4.07 \text{ m}$$

$$H = 50 + 4.07 \text{ m} = 54.07$$

$$C_{1000,0} = \frac{200}{3.14 \times 8 \times 70 \times 30} e^{-\gamma_2 (54.07/30)^2} \\ = 0.000746 \text{ gm/m}^3 = 746 \text{ ug/m}^3.$$

The concentration of SO_2 at downwind distance of 1km varies with wind speed.

SL.NO	Wind speed m/sec.	Δh_r (m)	H (m)	$c(\text{SO}_2)$ $\mu\text{g}/\text{m}^3$
1	1	32.58	82.58	691
2	2	16.29	66.29	1334
3	4	8.145	58.145	1167
4	6	5.43	55.43	914
5	8	4.07	54.07	746.



Q8. If smelting plant emit SO_2 at the rate of 100 kg/s and as per stringent central control board norms the maximum permissible concentration at a distance of 500 m from the stack is 80 ug/m^3 . Wind velocity at the top of chimney is 7.5 m/sec and the stability coefficient (downwind and cross wind) $r_y = 35 \text{ m}$ $r_2 = 20 \text{ m}$ respectively.

a) Calculate the effective stack height if a particulate emission from the smelter plant is at the rate of $3 \times 10^{-3} \text{ tons/hr}$.

Calculate the minimum stack height?

Given:-

$$\text{SO}_2 \text{ emission rate } Q = 100 \text{ kg/s} = 1 \times 10^5 \text{ g/sec.}$$

$$\text{Down wind distance } x = 500 \text{ m}$$

$$\begin{aligned} \text{Maximum permissible ground level conc}^n c &= 80 \text{ ug/m}^3 \\ &= 80 \times 10^{-5} \text{ gm/m}^3 \end{aligned}$$

$$\text{Wind speed (u)} = 7.5 \text{ m/s.}$$

$$\begin{aligned} \text{dispersion coefficient } r_y &= 35 \text{ m} \\ r_2 &= 20 \text{ m} \end{aligned}$$

effective stack height:-

$$C_{x,0} = \frac{Q}{\pi u r_y \times r_2} e^{-r_2 [H/r_2]^2}$$

$$C_{5000,0} = \frac{1.0 \times 10^5}{3.14 \times 7.5 \times 3.5 \times 20} \times e^{-r_2 [H/20]^2}$$

$$\Rightarrow 8 \times 10^{-5} = \frac{1.0 \times 10^5}{3.14 \times 7.5 \times 3.5 \times 20} \times e^{-r_2 [H/20]^2}$$

$$\boxed{H = 94.81 \text{ m}} \text{ am.}$$

If the emission rate is 3×10^3 tons/hr. = 34.72 kg/s

$$C_{\frac{5000}{8 \times 10^{-5}}, 0} = \frac{\cancel{40 \times 10^5} \ 34.72}{3.14 \times 7.5 \times 35 \times 20} e^{-\gamma_2 \left(\frac{H}{20}\right)^2}$$

$$\Rightarrow H =$$

b) minimum stack height

$$h = 74 (\alpha_p)^{0.27}$$

$$= 74 (3 \times 10^{-3})^{0.27}$$

$$h = 15.41 \text{ m}$$