

Simple case of Ternary Liquid-Liquid System ... could.

when extract and raffinate both are dilute in the solute, man fraction instead of mags ratio can be used.

X = Mans or mole ratio  $\begin{cases} X_i = \frac{\chi_i}{1-\chi_i} \\ \chi = Mans \text{ or mole fraction} \end{cases}$ =)  $K_{D_{i}} = \frac{\chi_{i} / (1 - \chi_{i}^{(1)})}{\chi_{i} / (1 - \chi_{i}^{(2)})}$ when z; is small, KD;  $= K_{D_{i}} \left[ \frac{1 - x_{i}^{(2)}}{1 - x_{i}^{(1)}} \right]$ approaches Ko

Further interpretation of Distribution Coefficient

For each phase in a multiphase, multicomponent system, the total Gibbs Free energy is

G = G (T, P, N<sub>1</sub>, N<sub>2</sub>, ..., N<sub>i</sub>, ..., N<sub>c</sub>)

Where Ni is number of moles of species i.

At equilibrium, the total G for all

phases is a minimum.

=> The total differential of G is zero.

The total differential of G is given by

dG = - Sdf + VdP + \( \frac{\text{L}}{1=1} \)

(4)

for constant temperature for constant pressure

this is the partial molar Gibbs free energy of species i's and is referred as chemical potential.

Simple case of Ternary Liquid-Liquid System - - · · · contd. Conservation of moles of each species across all phases in the system requires  $\Rightarrow$   $dN_{i}^{(1)} + \sum_{p=2}^{N} dN_{i}^{(p)} = 0$ = dn; (P) = 0 Following Egn. 4 and Egn. 5  $dG_{\text{system}} = \sum_{i=1}^{C} \mu_{i} dN_{i}^{(i)} + \sum_{p=2}^{N} (\sum_{i=1}^{C} \mu_{i} dN_{i}^{(p)})$  $= \sum_{i=1}^{c} \mu_{i} \left\{ -\sum_{p=2}^{N} dn_{i}^{(p)} \right\} + \sum_{p=2}^{N} \left( \sum_{i=1}^{c} \mu_{i}^{(p)} dn_{i}^{(p)} \right)$ = \\ \left\{ \teft\{ \left\{ \left\{ \left\{ \left\{ \teft\{ \left\{ \teft\{ \teft\{ \left\{ \left\{ \teft\{ \left\{ \teft\{ \teft\{ \left\{ \teft\{ \left\{ \left\{ \left\{ \left\{ \teft\{ \teft\{ \teft\{ \teft\{ \left\{ \teft\{ \ at equilibrium => jui = jui Since

dggstem

0 Each dN; (P) term can be varied independently of any other This requires that each coefficient of dN; (P) is Zero.

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(N)

Hi = Mi = Mi = --- = Mi Chemical potential is related to fugacity, and in turn to activity coefficient. f; = c e light = fil = fil

there of y reo Further  $f_{i_L} = g_{i_L} \times g_{i_L}$ and fic is fugacity of component "i" as pure species at the same presure and phase condition that remains same for each phase. 一つるにからいか。  $= \frac{\chi_{i}^{(2)}}{\chi_{i}^{(2)}} = \frac{\chi_{i}^{(2)}}{\chi_{i}^{(2)}} = \frac{\chi_{i}^{(2)}}{\chi_{i}^{(2)}} = \frac{\chi_{i}^{(2)}}{\chi_{i}^{(2)}} = \chi_{i}^{(2)}$   $= \frac{\chi_{i}^{(2)}}{\chi_{i}^{(2)}} = \chi_{i}^{(2)}$  Thumb Rule: Choose a solvent that lowers the activity coefficient of the solute in comparison with the feed. Hen KDB will be higher and XB will be higher that is desired.

When the solute concentrations in extract and raffinate are small, the activity coefficients can be approximated by the values at infinite ditution.

 $\Longrightarrow$   $K_D = f(T)$  only

In typical calculations, the extraction process can be considered isothermal, which allows use of constant KD

Example Problem

-> Solute B to be reduced to 1%. FA = (1-0.08) 13,500 = 12,420 kg/h (F) 13500-12420

Feed: 13,500 Kg/h containing 8 wt. y. solute (B) and rest carrier (A)

Raffinate to contain I wt. Y. B  $= \times X_{B}^{(R)} = 0.01 = 0.0101$ 1-0.01

Extraction Factor (As per Egn. 3)

 $E_B = \frac{X_B^{(F)}}{X_B^{(R)}} - 1 = \frac{0.087}{0.0101} - 1 = 7.61$ 

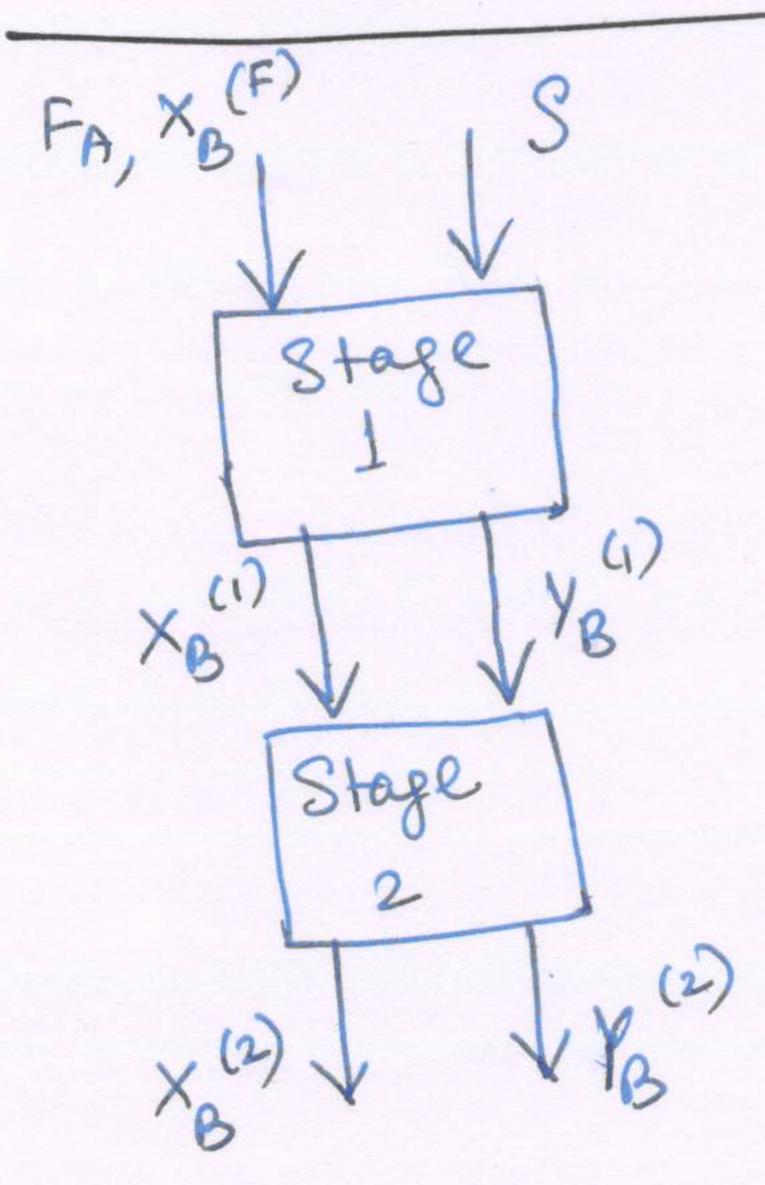
=  $S = \frac{E_B F_A}{K_D} = \frac{7.61 \times 12,420}{0.657}$  $E_B = \frac{SK_D}{F_A}$ = 1,44,000 Kg/h

Feed Stream: 13,500 kg/h
Solvent Stream: 1,44,000 kg/h
(Required): 1,44,000 kg/h 4 Feasibility ?

A collection of contacting stages Separation Cascade:

## Co-current cascade

Extract stream Man Ratio is referred as YB, Since the superscript will now be used to mark the Stage Number.



At the end of 1st stage, material balance for B gives
$$X_{B}^{(F)} F_{A} + 0 = X_{B}^{(I)} F_{A} + Y_{B}^{(I)} S - \dots Eq. 6$$

$$= X_{B}^{(I)} F_{A} + K_{D_{B}}^{(I)} S$$

$$= X_{B}^{(I)} F_{A} + K_{D_{B}}^{(I)} S$$

$$=)\frac{\left[\begin{array}{c} Y_{B}^{(1)} \\ X_{B}^{(F)} \end{array}\right]}{\left[\begin{array}{c} Y_{B}^{(1)} \\ X_{B}^{(F)} \end{array}\right]} = \frac{\left[\begin{array}{c} X_{B}^{(1)} \\ X_{B}^{(1)} \end{array}\right]}{\left[\begin{array}{c} F_{A} + K_{D_{B}} \\ Y_{B}^{(1)} \end{array}\right]}$$

For the second stage, material balance for B gives

From 2qn.6,  $L.H.S. = \chi_B^{(F)}F_A$ and  $KD_B = \frac{\gamma_B^{(2)}}{\chi_B^{(2)}} = \chi_B^{(2)}F_A$ 

= xB(2)FA+ KD3 xB(2)S = xB(2) [FA+ KDB'S]

Equating (L. H.S) with (R. H.S.)

 $\frac{X_{B}^{(2)}}{X_{B}^{(F)}} = \frac{1}{1+E} = \frac{By \text{ induction}}{X_{B}^{(N)}} = \frac{X_{B}^{(N)}}{X_{B}^{(F)}} \text{ after N Stages}.$ 

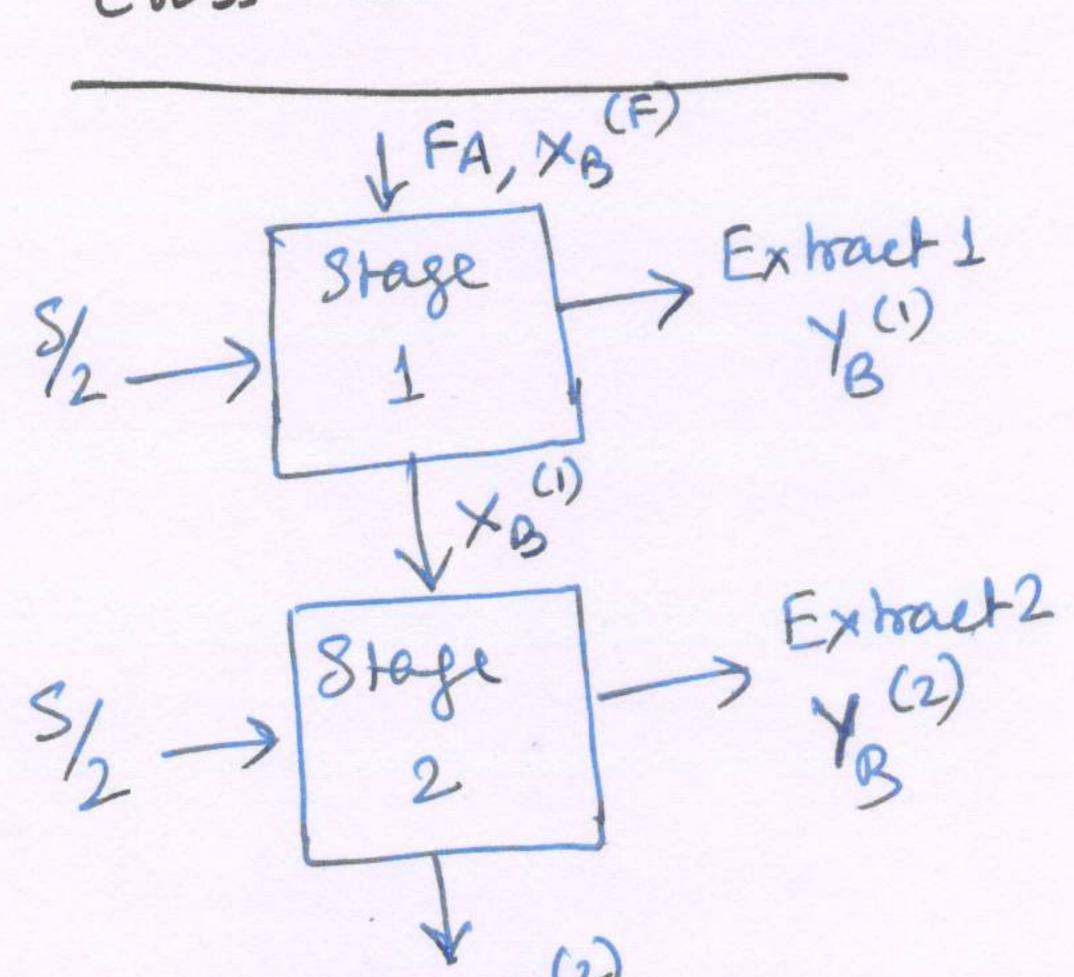
 $\Rightarrow \times_{B}^{(2)} = \times_{B}^{(1)}$ 

(No additional extraction due to addition of second stage).

Note the superscript

The stream leaving a stage bears the stage No, as superscript.

## Cross-current cascade



First Stage can be treated as isolated single stage

Similarly, 
$$\frac{X_{B}}{X_{B}} = \frac{1}{1 + \frac{K_{0B}(S_{A})}{F_{A}}} = \frac{1}{1 + \frac{F}{2}}$$

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Since 
$$\frac{\chi_{B}^{(N)}}{\chi_{B}^{(F)}} = \frac{\chi_{B}^{(N)}}{\chi_{B}^{(N+1)}} \frac{\chi_{B}^{(N+1)}}{\chi_{B}^{(N-2)}} \frac{\chi_{B}^{(1)}}{\chi_{B}^{(F)}}$$

$$= \frac{1}{(1+\frac{E}{N})^{N}}$$

$$\frac{XB}{XB}(N-1) = \frac{1}{1+EN}$$

She as
the solvent
mass flow rate
to each stage

Lt 
$$\frac{x_{B}}{x_{B}^{(F)}} = \frac{1}{e^{E}}$$
 complete extraction not possible,

Counter current cascade

Feed FA A Extract

XB Stage

1

XB Stage

2

XB Stage

X

For Stage 1  $\times_{B}^{(F)}F_{A} + Y_{B}^{(2)}S = \times_{B}^{(1)}F_{A} + Y_{B}^{(1)}S$   $\times_{B}^{(F)}F_{A} + Y_{B}^{(2)}S = \times_{B}^{(1)}F_{A} + Y_{B}^{(2)}S$ and  $K_{D6} = \frac{Y_{B}}{\times_{B}^{(1)}}$   $\times_{B}^{(1)}F_{A} = \times_{B}^{(2)}F_{A} + Y_{B}^{(2)}S$   $\times_{B}^{(1)}F_{A} = \times_{B}^{(2)}F_{A} + Y_{B}^{(2)}S$   $\times_{B}^{(1)}F_{A} = \times_{B}^{(2)}F_{A} + X_{B}^{(2)}S$   $\times_{B}^{(2)}F_{A} = \times_{B}^{(2)}F_{A} + X_{B}^{(2)}S$   $\times_{B}^{(2)}F_{A} + X_{B}^{(2)}S$ 

For N-counter current =  $\frac{\times_{B}}{\times_{B}} = \frac{1}{1 + E + E^{2}}$  where  $\frac{\times_{B}}{\times_{B}} = \frac{1}{1 + E + E^{2}}$  where  $\frac{\times_{B}}{\times_{B}} = \frac{1}{1 + E + E^{2}}$   $\frac{\times_{B}}{\times_{B}} = \frac{1}{1 + E + E^{2}}$ 

Interstage values of XB in counter current cascade

cross current flow Cocument flow = Single Stage Extraction

Counter current extraction is most efficient.

Equilibrium Stages