UH. EDU | 2006 | BC EXAM |
SOLUTIONS TO F.R. # 3,4,6
SHUBLEKA | CALCULUS QUESTIONS, ORG

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$$J: \begin{cases} x = t+1 \\ y = t^2 - 1 \end{cases}$$
 $J: \begin{cases} x = 6t+3 \\ y = -2t \end{cases}$

a):
I:
$$V(4) = \langle x'|+1, y'|+1 \rangle / T: V(4) = \langle 6, -2 \rangle$$

 $= \langle 1, 2+7 \rangle / T: V(4) = \langle 6, -2 \rangle$
 $= \langle 1, 8 \rangle$

b) Distance =
$$\int (x'(t))^2 + (y'(t))^2 dt$$

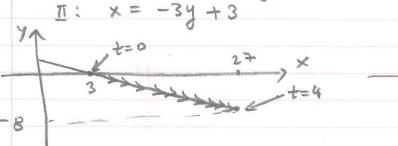
 $t=1$
 $= \int \sqrt{36 + 4} dt = \int \sqrt{40} dt$

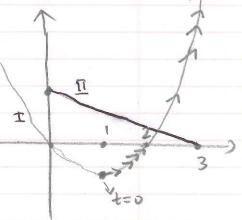
c) Collision
$$\int x_1(t) = x_2(t)$$
 (=) $\begin{cases} t+1 = 6t + 3 \\ y_1(t) = y_2(t) \end{cases}$

No solution, hance no collision!

d) I:
$$t = x - 1 \longrightarrow y = (x - 1)^2 - 1$$

II: $x = -3y + 3$





a)
$$f(x) = x \cdot e^{x} = x \left[1 + x + \frac{x^{2}}{2!} + \frac{x^{3}}{3!} + 111 + \frac{x^{h}}{n!} + 111 \right]$$

$$= x + x^{2} + \frac{x^{3}}{3!} + \frac{x^{4}}{3!} + 111 + \frac{x^{h+1}}{n!} + 111 = \frac{x^{h}}{n=0} + \frac{x^{h+1}}{n!}$$

b)
$$f(x) = x + \frac{x^2}{1!} + \frac{x^3}{2!} + \frac{x^4}{3!} + \frac{x^{h+1}}{n!} + \frac{x^{h+1}}{n!}$$

$$f(x) = 1 + 2x + 3\frac{x^{2}}{3!} + 4\frac{x^{3}}{3!} + 1n + (n+1)\frac{x}{n!} + 111$$

$$= 1 + (x+x) + (2\frac{x^{2}}{2!} + \frac{x^{2}}{2!}) + (3\frac{x^{3}}{3!} + \frac{x^{3}}{3!}) + 1n + (n+1)\frac{x}{n!} + \frac{x^{n}}{n!} + \frac{x^{n}}$$

$$= \left(\frac{x^2 + \frac{x^3}{3} + \frac{x^4}{4 \cdot 2!} + \frac{x^5}{5 \cdot 3!} + \frac{x^4}{11!} + \frac{x^{n+1}}{2!} + \frac{x^{n+1}}{4!} + \frac{x^{n+1}}{4!} + \frac{x^{n+2}}{5!} + \frac{x^{n+2}}{4!} + \frac{x^{n+2}}{5!} +$$



solution through (0,1)

$$\frac{dy}{dx} = 2xy \quad y(0) = 2 \quad \triangle x = 0.2$$

×	y	04/dx	Computations
0	2	0	7 = 2
0.2	2	0.8	y-2 = 0.8 (x-0.2) → y (0.4)
0.4	2.16	1.728	y-2.16 = 1.728 (x-0.4)
0.6 2.5056		6	b y = 2.16 +1.7228.0.2
*			4(0.6) =
	f(0.6)	≈ 2.5056.	

d)
$$\frac{d^2y}{dx^2} = \frac{d}{dx} \left(\frac{dy}{dx} \right) = \frac{d}{dx} \left(2xy \right) = 2 \left(1y + x \cdot dy \right)$$
$$= 2y + 2x \cdot \left[2xy \right] = 2y \left[1 + 2x^2 \right]$$