

ARE YOU READY 4 CALCULUS

TEACHER NAME: _____

STUDENT NAME: _____

PERIOD: _____

50 Problems - Calculator allowed for some problems

SCORE SHEET**STUDENT NAME:** _____

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Problem: 1

One solution of $x^3 - 5x^2 + 5x - 1 = 0$ is 1. Find the other two solutions.

- | | |
|---------------------------------------|---------------------------------------|
| A) $\{4 + \sqrt{3}, 4 - \sqrt{3}\}$ | B) $\{2 + \sqrt{3}, 2 - \sqrt{3}\}$ |
| C) $\{4 + 2\sqrt{3}, 4 - 2\sqrt{3}\}$ | D) $\{2 + 2\sqrt{3}, 2 - 2\sqrt{3}\}$ |
-

Problem 2

A twenty-five foot ladder just reaches the top of a house and forms an angle of 41.5 degrees with the wall of the house. How tall is the house? Round your answer to the nearest 0.1 foot.

- | | | | |
|------------|----------|------------|------------|
| A) 18.6 ft | B) 19 ft | C) 18.7 ft | D) 18.8 ft |
|------------|----------|------------|------------|
-

Problem: 3

What principal invested at 8%, compounded continuously for 4 years, will yield \$1190? Round the answer to two decimal places.

- | | | | |
|--------------|-------------|-------------|--------------|
| A) \$1188.62 | B) \$864.12 | C) \$627.48 | D) \$1638.78 |
|--------------|-------------|-------------|--------------|

Problem: 4

The logistic growth model $P(t) = \frac{1240}{1 + 30e^{-0.333t}}$ represents the population of a bacterium in a culture tube after t hours. What was the initial amount of bacteria in the population?

- A) 45 B) 40 C) 39 D) 41
-

Problem: 5

If $\sin \theta = 0.3$, find $\sin(\theta + \pi)$.

- A) -0.7 B) 0.3 C) -0.3 D) 0.7
-

Problem: 6

Find all the zeros of the function and write the polynomial as a product of linear factors.

$$f(x) = x^3 - x^2 + 36x - 36$$

- A) $f(x) = (x - 1)(x + 1)(x + 36)$ B) $f(x) = (x - 1)(x + 6i)(x - 6i)$
C) $f(x) = (x - 1)(x + 6)(x - 6)$ D) $f(x) = (x - 25)(x + i)(x - i)$
-

Problem: 7

Information is given about a polynomial $f(x)$ whose coefficients are real numbers. Find the remaining zeros of f .

Degree 3; zeros: $2, 3 - i$

A) $3 + i$

B) $-3 + i$

C) -2

D) no other zeros

Problem: 8

Without graphing the function, determine its amplitude or period as requested.

$y = \sin 5x$ Find the period.

A) 2π

B) 5

C) $\frac{2\pi}{5}$

D) 1

Problem: 9

Without graphing the function, determine its amplitude or period as requested.

$y = -4 \sin x$ Find the amplitude.

A) 2π

B) 4

C) $\frac{\pi}{4}$

D) -4π

Problem: 10

Write as the sum and/or difference of logarithms. Express powers as factors.

$$\log_3 \left(\frac{x-2}{x^8} \right)$$

- A) $\log_3 (x-2) - \log_3 x$ B) $8 \log_3 x - \log_3 (x-2)$
C) $\log_3 (x-2) + 8 \log_3 x$ D) $\log_3 (x-2) - 8 \log_3 x$
-

Problem: 11

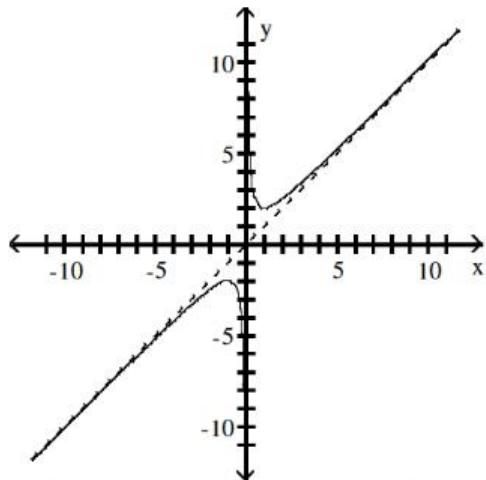
Write as the sum and/or difference of logarithms. Express powers as factors.

$$\log_9 \frac{11}{4}$$

- A) $\log_9 11 + \log_9 4$ B) $\log_9 4 - \log_9 11$
C) $\log_9 11 - \log_9 4$ D) $\log_9 11 + \log_9 11$
-

Problem: 12

Use the graph to find the oblique asymptote, if any, of the function.



A) $y = -x$

B) $y = 2x$

C) $y = x$

D) none

Problem: 13

Find the exact solution of the equation.

$$\sin^{-1} x = \frac{\pi}{2}$$

A) $x = 1$

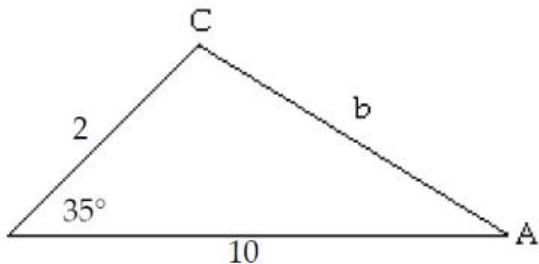
B) $x = -1$

C) $x = 0$

D) $x = \pi$

Problem: 14

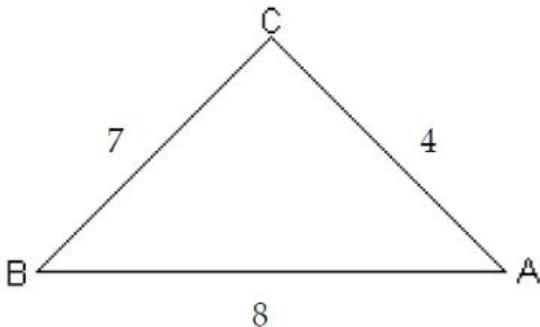
Solve the triangle.



- A) $b = 9.44$, $A = 7.8^\circ$, $C = 137.2^\circ$
B) $b = 7.44$, $A = 137.2^\circ$, $C = 7.8^\circ$
C) $b = 8.44$, $A = 137.2^\circ$, $C = 7.8^\circ$
D) $b = 8.44$, $A = 7.8^\circ$, $C = 137.2^\circ$
-

Problem: 15

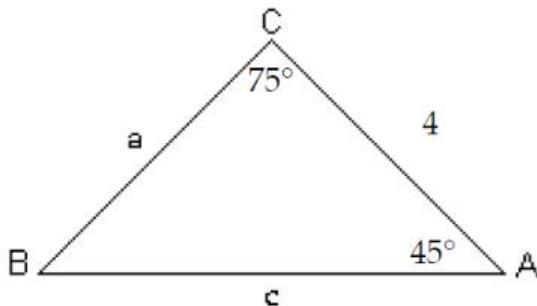
Solve the triangle.



- A) $A = 61^\circ$, $B = 89^\circ$, $C = 30^\circ$
B) $A = 30^\circ$, $B = 89^\circ$, $C = 61^\circ$
C) $A = 30^\circ$, $B = 61^\circ$, $C = 89^\circ$
D) $A = 61^\circ$, $B = 30^\circ$, $C = 89^\circ$
-

Problem: 16

Solve the triangle.



- A) $B = 60^\circ$, $a = 3.27$, $c = 4.46$
C) $B = 60^\circ$, $a = 4.46$, $c = 3.27$

- B) $B = 55^\circ$, $a = 4.46$, $c = 3.27$
D) $B = 65^\circ$, $a = 3.27$, $c = 4.46$

Problem: 17

Find the vertical asymptotes of the rational function.

$$H(x) = \frac{x - 4}{16x - x^3}$$

- A) $x = 0, x = -4$
C) $x = 0, x = 4$

- B) $x = -4, x = 4$
D) $x = 0, x = -4, x = 4$
-

Problem: 18

Find the exact value of the expression.

$$\sin \frac{\pi}{12}$$

- A) $-\sqrt{2}(\sqrt{3} - 1)$ B) $\sqrt{2}(\sqrt{3} - 1)$ C) $-\frac{\sqrt{2}(\sqrt{3} - 1)}{4}$ D) $\frac{\sqrt{2}(\sqrt{3} - 1)}{4}$
-

Problem: 19

Find the exact value of the expression.

$$\sin^{-1} \frac{\sqrt{2}}{2}$$

- A) $\frac{3\pi}{4}$ B) $\frac{\pi}{4}$ C) $\frac{\pi}{3}$ D) $\frac{2\pi}{3}$
-

Problem: 20

Express the product as a sum containing only sines or cosines.

$$\sin(6\theta) \sin(3\theta)$$

- A) $\frac{1}{2}[\cos(3\theta) - \cos(9\theta)]$ B) $\frac{1}{2}[\sin(9\theta) + \cos(3\theta)]$
C) $\sin^2(18\theta^2)$ D) $\frac{1}{2}[\cos(9\theta) - \cos(3\theta)]$

Problem: 21

Use the given zero to find the remaining zeros of the function.

$$f(x) = x^3 + 3x^2 - 8x + 10; \text{ zero: } 1 + i$$

A) $1 - i, 5$

B) $-5, 5$

C) $1 - i, 5i$

D) $1 - i, -5$

Problem: 22

Use the Change of Base formula and a calculator to evaluate the logarithm. Round your answer to three decimal places.

$$\log_2 60.29$$

A) 0.169

B) 1.780

C) 5.914

D) 30.145

Problem: 23

Use the properties of logarithms to evaluate the expression. Do not use a calculator.

$$\log_3 3^{10}$$

Problem: 24

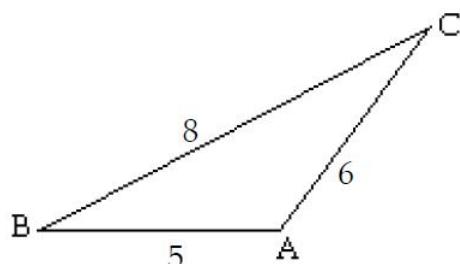
Use the properties of logarithms to evaluate the expression. Do not use a calculator.

$$\ln e^{\sqrt{7}}$$

- A) 49 B) 7 C) $\sqrt{7}$ D) e

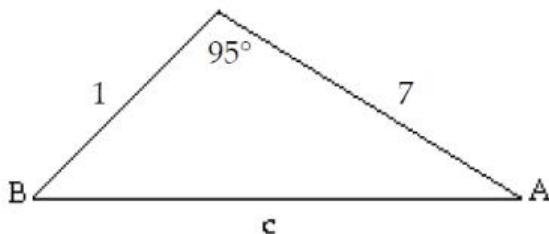
Problem: 25

Find the area of the triangle. If necessary, round the answer to two decimal places.



Problem: 26

Find the area of the triangle. If necessary, round the answer to two decimal places.



A) 3.49

B) 13.95

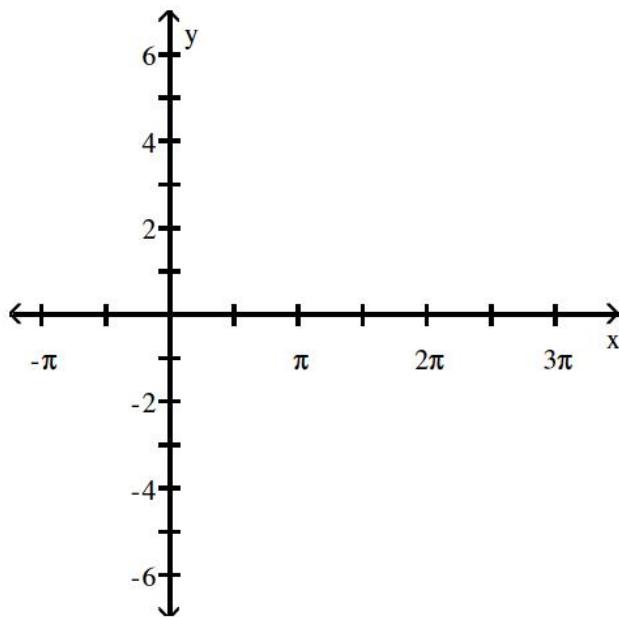
C) 4.29

D) 0.31

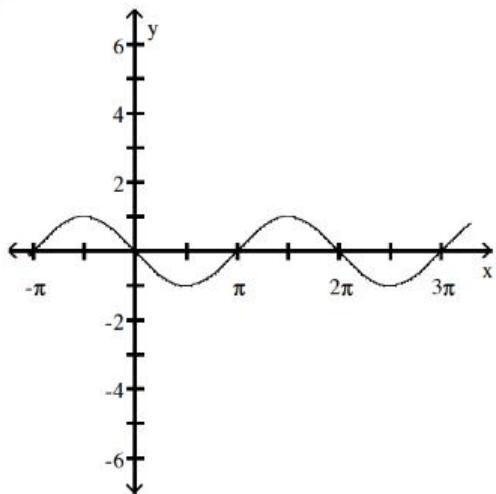
Problem: 27

Use transformations to graph the function.

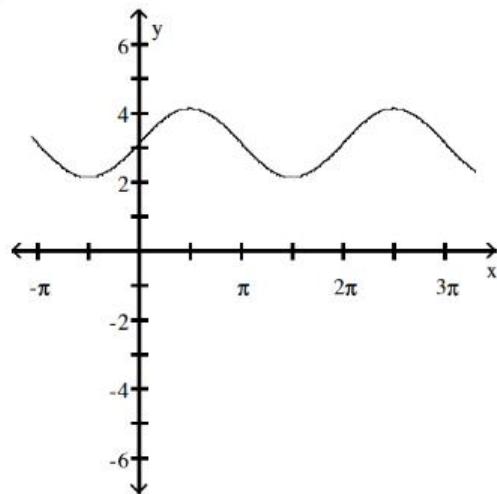
$$y = \sin(\pi x)$$



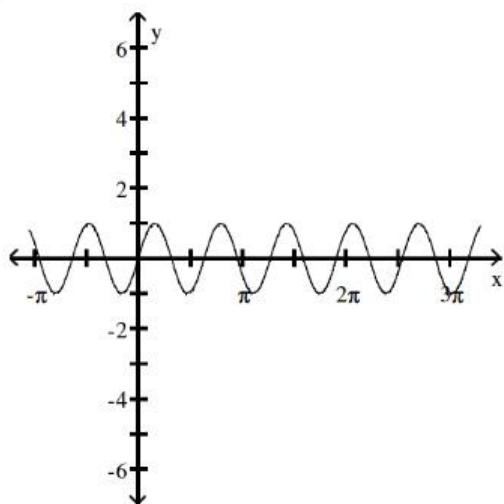
A)



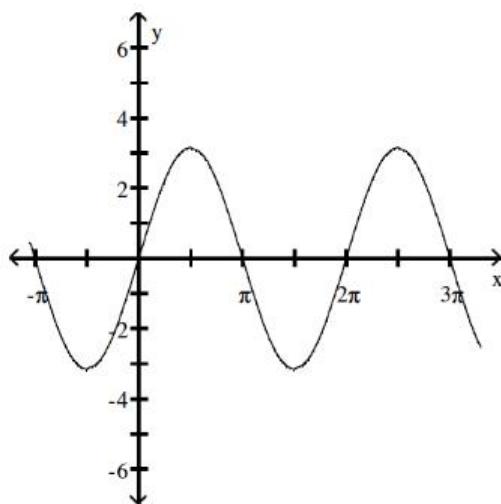
B)



C)



D)



Problem: 28

Express the sum or difference as a product of sines and/or cosines.

$$\cos(10\theta) - \cos(4\theta)$$

- A) $-2 \cos(7\theta) \sin(3\theta)$ B) $2 \cos(3\theta)$
C) $2 \cos(7\theta) \cos(3\theta)$ D) $-2 \sin(7\theta) \sin(3\theta)$
-

Problem: 29

Two sides of a triangle are given. Determine whether the given information results in one triangle, two triangles, or no triangles at all. Solve any triangle(s) that results.

$$a = 7, b = 9, B = 49^\circ$$

- A) one triangle B) two triangles
 $A = 35.94^\circ, C = 95.06^\circ, c = 11.88$
 $A_1 = 76.01^\circ, C_1 = 54.99^\circ, c_1 = 7.60$ or
 $A_2 = 103.99^\circ, C_2 = 27.01, c_2 = 12.14$
C) one triangle D) no triangle
 $A = 76.01^\circ, C = 54.99^\circ, c = 7.60$
-

Problem: 30

Simplify the expression.

$$\frac{\cos \theta}{1 + \sin \theta} + \tan \theta$$

- A) 1 B) $\sin^2 \theta$ C) $\cos \theta + \sin \theta$ D) $\sec \theta$

Problem: 31

Use the Change of Base formula and a calculator to evaluate the logarithm. Round your answer to two decimal places.

$$\log_3 25$$

- A) 1.10 B) 3.22 C) 0.34 D) 2.93

Problem: 32

Find the center (h, k) and radius r of the circle with the given equation.

$$(x - 1)^2 + (y + 1)^2 = 25$$

- A) $(h, k) = (-1, 1); r = 5$ B) $(h, k) = (1, -1); r = 25$
C) $(h, k) = (1, -1); r = 5$ D) $(h, k) = (-1, 1); r = 25$

Problem: 33

Solve the equation on the interval $0 \leq \theta \leq 2\pi$.

$$2 \sin^2 \theta = \sin \theta$$

A) $0, \pi, \frac{\pi}{6}, \frac{5\pi}{6}$

B) $\frac{\pi}{3}, \frac{2\pi}{3}$

C) $\frac{\pi}{2}, \frac{3\pi}{2}, \frac{\pi}{3}, \frac{2\pi}{3}$

D) $\frac{\pi}{6}, \frac{5\pi}{6}$

Problem: 34

Solve the equation on the interval $0 \leq \theta \leq 2\pi$.

$$2 \cos \theta + 3 = 2$$

A) $\frac{5\pi}{6}, \frac{7\pi}{6}$

B) $\frac{2\pi}{3}, \frac{5\pi}{3}$

C) $\frac{2\pi}{3}, \frac{4\pi}{3}$

D) $\frac{5\pi}{6}, \frac{11\pi}{6}$

Problem: 35

Find the domain of the function.

$$f(x) = \sqrt{21 - x}$$

A) $\{x | x \neq \sqrt{21}\}$

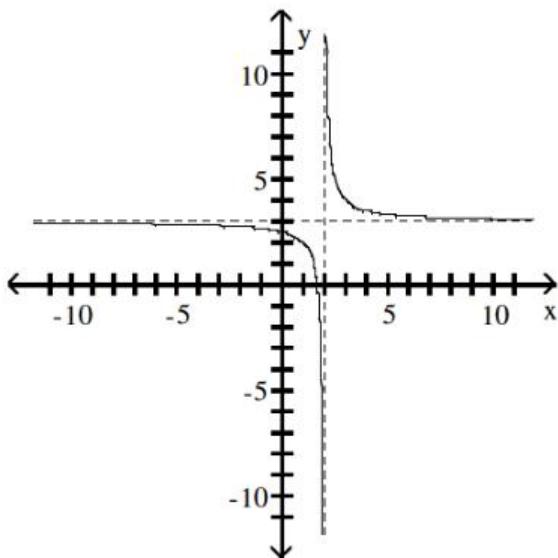
B) $\{x | x \leq 21\}$

C) $\{x | x \neq 21\}$

D) $\{x | x \leq \sqrt{21}\}$

Problem: 36

Use the graph to determine the domain and range of the function.



A) domain: $\{x \mid x \neq 3\}$
range: $\{y \mid y \neq -2\}$

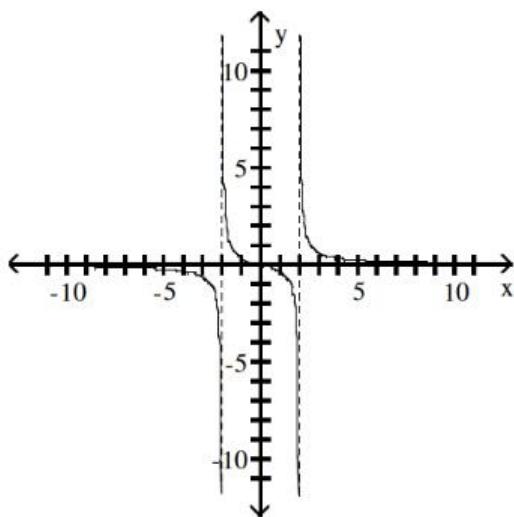
C) domain: $\{x \mid x \neq 3\}$
range: $\{y \mid y \neq 2\}$

B) domain: $\{x \mid x \neq 2\}$
range: $\{y \mid y \neq 3\}$

D) domain: $\{x \mid x \neq -2\}$
range: $\{y \mid y \neq 3\}$

Problem: 37

Use the graph to determine the domain and range of the function.



- A) domain: $\{x \mid x \neq -2, x \neq 2\}$
range: all real numbers

C) domain: $\{x \mid x \neq -2, x \neq 2\}$
range: $\{y \mid y \neq 0\}$

B) domain: all real numbers
range: all real numbers

D) domain: all real numbers
range: $\{y \mid y \neq -2, y \neq 2\}$

Problem: 38

Solve the equation

$$\log_2 x = 3$$

- A) {9} B) {1.58} C) {6} D) {8}

Problem: 39

Solve the equation

$$\log(3x) = \log 4 + \log(x - 1)$$

A) $\left\{-\frac{4}{7}\right\}$

B) $\{-4\}$

C) $\{4\}$

D) $\left\{\frac{3}{2}\right\}$

Problem: 40

A point on the terminal side of the angle θ is given. Find the exact value of the indicated trigonometric function of θ .

(-3, -4)

Find $\sin \theta$.

A) $\frac{3}{5}$

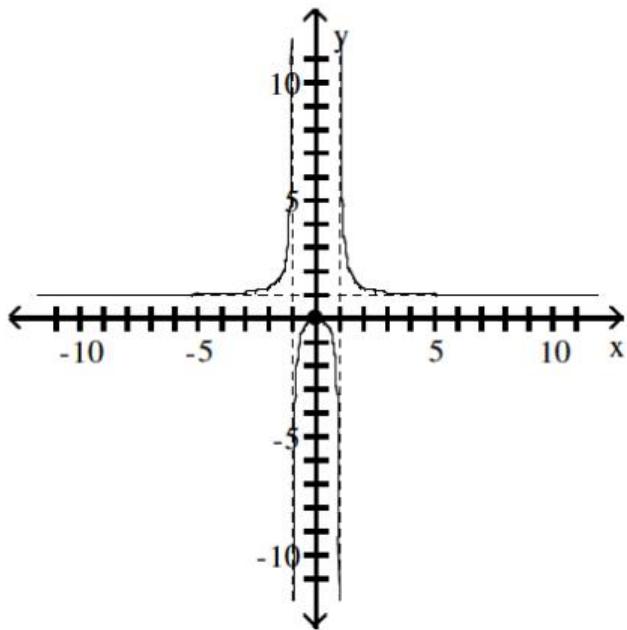
B) $-\frac{3}{5}$

C) $-\frac{4}{5}$

D) $\frac{4}{5}$

Problem: 41

Use the graph to find the horizontal asymptote, if any, of the function.

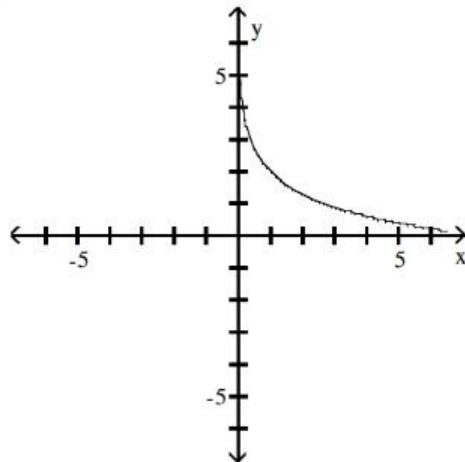


- A) $y = -1, y = 1$ B) $y = 1$
C) $x = -1, x = 1, y = 1$ D) $y = 0, y = 1$
-

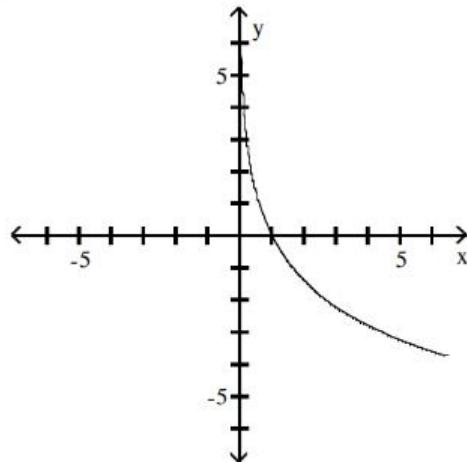
Problem: 42

Identify the graph the function $f(x) = 2 \ln x$, without a calculator.

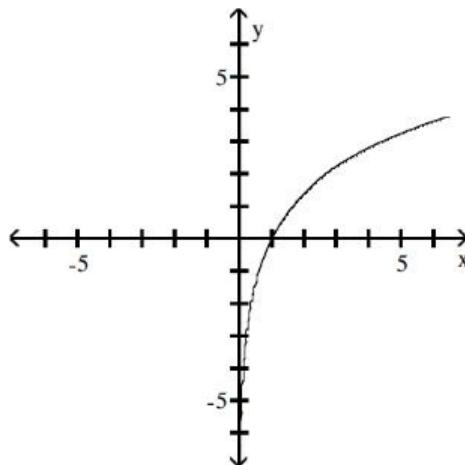
A)



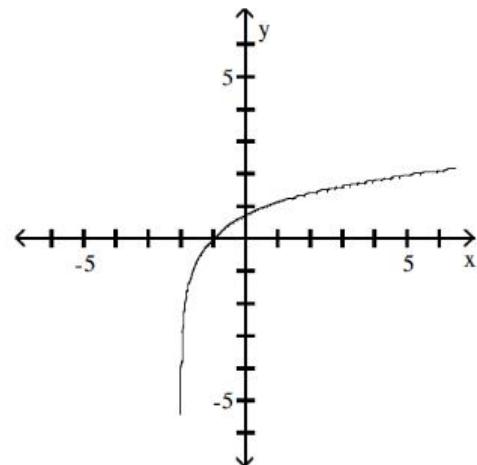
B)



C)



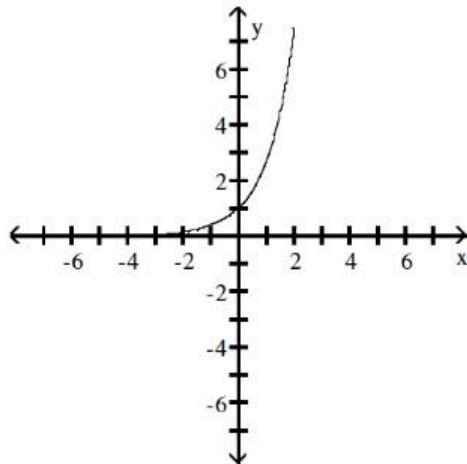
D)



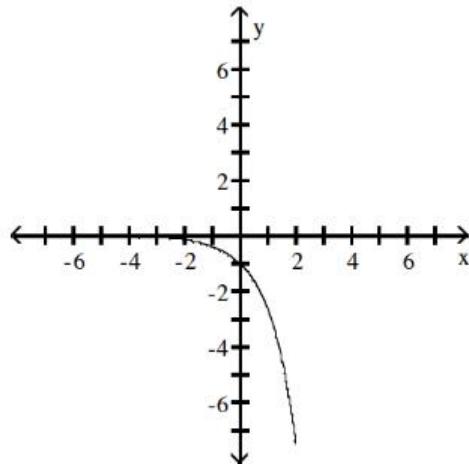
Problem: 43

Identify the graph of $f(x) = e^x$, without a calculator.

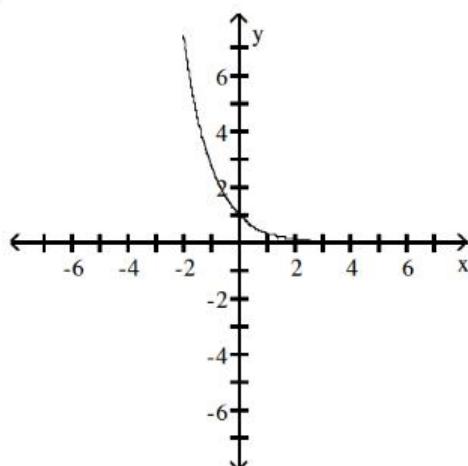
A)



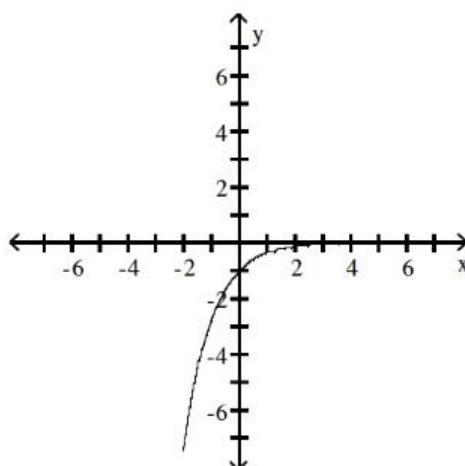
B)



C)

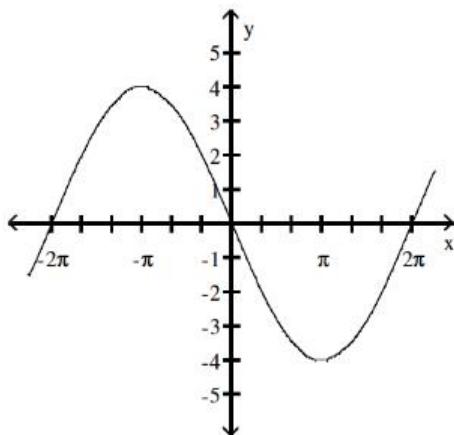


D)



Problem: 44

Find an equation for the given graph.



- A) $y = -4 \cos(2x)$ B) $y = -4 \sin\left(\frac{1}{2}x\right)$ C) $y = -4 \cos\left(\frac{1}{2}x\right)$ D) $y = -4 \sin(2x)$

Problem: 45

Find the domain of the rational function.

$$G(x) = \frac{x+4}{x^2 + 1}$$

- A) $\{x | x \neq -1, x \neq 1\}$ B) $\{x | x \neq 0, x \neq -1\}$
C) $\{x | x \neq -1, x \neq 1, x \neq -4\}$ D) all real numbers

Problem: 46

Find the intercepts of the function $f(x)$.

$$f(x) = x^3 + 2x^2 - 9x - 18$$

- A) x-intercept: -3; y-intercept: -18
B) x-intercepts: -3, -2, 3; y-intercept: -18
C) x-intercepts: -3, 2, 3; y-intercept: -18
D) x-intercept: -2; y-intercept: -18
-

Problem: 47

Give the equation of the horizontal asymptote, if any, of the function.

$$G(x) = \frac{x^2 + 1x - 9}{x - 9}$$

- A) $y = 0$ B) $y = 1$ C) $y = 9$ D) none
-

Problem: 48

Find the amount that results from the investment.

\$12,000 invested at 7% compounded quarterly after a period of 4 years

- A) \$3839.15 B) \$15,729.55 C) \$15,566.73 D) \$15,839.15
-

Problem: 49

Solve the equation in the real number system

$$x^3 + 9x^2 + 26x + 24 = 0$$

- A) {3, 4} B) {2, 3, 4} C) {-4, -3, -2} D) {-4, -3}
-

Problem: 50

Use the information given about the angle θ , for $0 \leq \theta \leq 2\pi$, to find the exact value of the indicated trigonometric function of θ .

$$\sin \theta = \frac{5}{13}, \quad 0 < \theta < \frac{\pi}{2} \quad \text{Find } \cos(2\theta).$$

- A) $\frac{119}{169}$ B) $\frac{118}{169}$ C) $\frac{120}{169}$ D) $-\frac{119}{169}$

ANSWER KEY

Problem	Answer	Problem	Answer
1	B	26	A
2	C	27	C
3	B	28	D
4	B	29	A
5	C	30	D
6	B	31	D
7	A	32	C
8	C	33	A
9	B	34	C
10	D	35	B
11	C	36	B
12	C	37	A
13	A	38	D
14	D	39	C
15	D	40	C
16	A	41	B
17	A	42	C
18	D	43	A
19	B	44	B
20	A	45	D
21	D	46	B
22	C	47	D
23	C	48	D
24	C	49	C
25	C	50	A