ALGEBRA II: MISCELLANEOUS PROBLEMS (1 – 40)

- 1. The average of the numbers 5, 9, 10, 13, and a equals 11. Find the value of a.
- a. 16
- b. 17
- c. 18
- d. 20
- 2. A shirt is on sale for \$34.40, which is 20% off the original price. Find the original price of the shirt.
- a. \$36.40
- b. \$41.28
- c. \$43.00
- d. \$54.40
- 3. How many quarts of water does one add to 6 quarts of a 60% alcohol solution to create a 40% alcohol solution?
- a. 2 qt.
- b. 3 qt.
- c. 6 qt.
- d. 9 qt.
- 4. Express (7+3i)-(2-3i) in the form a+bi where a and b are real numbers.
- a. 5 6i
- b. 5 + 6i
- c. 9
- d. 9 + 5i
- 5. Find the value of k that completes the square for $x^2 + 10x + k$.
- a. 5
- b. 10
- c. 25
- d. 100
- 6. Find the solutions to the equation: |2x 14| = 6.
- a. x = -4, 10
- b. x = 4, 10
- c. x = 11, 17
- d. x = 12, 14

- 7. Solve the inequality $7 < 4x + 3 \le 21$, and express the solution as an interval.
- a. (1, 4.5]
- b. [1.75, 7)
- c. (7/3, 17)
- d. [4.5, 5.25]
- 8. Solve the inequality $\frac{-18}{6x-42} > 0$, and express the solution as an interval
- a. $(-3, \infty)$
- b. $(7, \infty)$
- c. $(-\infty, -3)$
- $d.(-\infty,7)$
- 9. Solve the inequality $2|x-10| \le 3$, and express the solution as an interval.
- a. (7, 8.5)
- b. (8.5, 10)
- c. (8.5, 11.5)
- d. (11.5, 13)
- 10. An object is shot upward with an initial velocity of 240 feet per second so that its height s (in feet) above the ground after t seconds is given by $s(t) = -16t^2 + 240t$. For what values of t will the object be at least 416 feet above the ground?
- a. [2, 5]
- b. [2, 13]
- c. [3, 5]
- d. [3, 13]
- 11. Find the distance d(A, B) between the points A(-1, 0) and B(4, 3).
- a. $3\sqrt{2}$
- b. 5
- c. $\sqrt{34}$
- d. 8
- 12. Determine the point A(x, y) so that the points A(x, y), B(0, 3), C(1, 0), D(7, 2) will be the vertices of a parallelogram.
- a. A(-6, 1)
- b. A((3, 7))
- c. A(5, 6)

d. A(6, 5)

- 13. Find the midpoint of the line segment from A(-2, 9) to B(4, 5).
- a. C(1, 7)
- b. D(3, 7)
- c. P(4, 9)
- d. Q(5, 9)
- 14. Find the point on the positive y-axis that is a distance 5 from the point P(3, 4).
- a. A(0, 6)
- b. B(0,8)
- c. C(6,0)
- d. D(8,0)
- 15. Find the x-intercept and y-intercept of the equation 5x 3y = 30.
- a. 6 and 10 respectively
- b. 10 and 6 respectively
- c. 6 and -10 respectively
- d. 6 and 2 respectively
- 16. Give the equation for the circle with center C(3, -2) and radius 4.
- a. $x^2 + y^2 = 52$
- b. $(x-3)^2 + (y-2)^2 = 16$
- c. $(x+3)^2 + (y-2)^2 = 42$
- d. $(x-3)^2 + (y+2)^2 = 16$
- 17. Give the center of the circle with equation $x^2 + 2x + y^2 10y + 22 = 0$.
- a. A(2, 4)
- b. B(1, 5)
- c. C(-1, 5)
- d. D(-2, 4)
- 18. Find an equation for the line with slope 1/2 and *y*-intercept 3.
- a. x/2 y = 3
- b. -x + 2y = 6
- c. x + 2y = 6
- d. 2x y = 3

19. Find the slope of the line through the points A(-1, 6) and B(5, 2)

- $a_1 1$
- b. -2/3
- c. 2/3
- d. 1

20. Find an equation for the line with y-intercept 3 that is perpendicular to the line 3y = 2x - 4.

- a. 2y = 6 3x
- b. 2y = 3x + 6
- c. 3y = 9 2x
- d. 3y = 2x + 9

21. Fahrenheit and Celsius temperatures are related by the equation F = 9 C + 32, where F is the temperature in degrees Fahrenheit and C is the temperature on the Celsius scale. If the temperature is a balmy 77° Fahrenheit, what is the temperature on the Celsius scale?

- a. 25°
- b. 33.8°
- c. 43°
- d. 45°

22. If $f(x) = x^2 + 5$, find f(a+h) - f(a).

- a. $2ah + h^2 + 10$
- b. $2ah + h^2 + 5$
- c. $2ah + h^2$
- $d. h^2$

23. From a square piece of cardboard with width x inches, a square of width x - 3 inches is removed from the center. Write the area of the remaining piece as a function of x.

- a. f(x) = 6x 9
- b. f(x) = 6x + 9
- c. $f(x) = 2x^2 9$
- d. $f(x) = 2x^2 6x 9$

24. If P(4, -5) is a point on the graph of the function y = f(x), find the corresponding point on the graph of y = 2f(x - 6).

- a. A(1, 8)
- b. B(2, -5)
- c. C(6, 8)
- d. *D*(10,–10)

25. Explain how the graph of $y-5=(x-3)^2$ can be obtained from the graph of $y=x^2$.

- a. Shift the graph of $y = x^2$ left 3 units and down 5 units
- b. Shift the graph of $y = x^2$ left 3 units and up 5 units
- c. Shift the graph of $y = x^2$ right 3 units and down 5 units
- d. Shift the graph of $y = x^2$ right 3 units and up 5 units

26. Determine e the vertex of $y = x^2 - 8x + 22$.

- a. A(-4, 11)
- b . *B*(-4, 18)
- c. C(4, 6)
- d.D(4, 8)

27. An object is projected upward from the top of a tower. Its distance in feet above the ground after *t* seconds is given by

 $s(t) = -16t^2 + 64t + 80$. How many seconds will it take to reach ground level?

- a. 1 second
- b. 4 seconds
- c . 5 seconds
- d. 8 seconds

28. Find the maximum value of $y = -x^2 + 6x$.

- a. 8
- b.9
- c.10
- d.11

29. Several values of the two function f and g are listed in the following tables:

| ***** | |
|-------|------|
| X | 4567 |
| f(x) | 7654 |
| | |

| X | 4567 |
|------|------|
| g(x) | 6745 |

Find $(f \circ g)(6)$.

- a. 4
- b.5
- $c\;.\;6$
- d.7

30. Given f(x) = 5x + 7 and $g(x) = x^2 + 7$, find $(g \circ f)(x)$.

- a. $(g \circ f)(x) = 5x^2 + 7$
- b. $(g \circ f)(x) = 5x^2 + 42$
- c. $(g \circ f)(x) = (5x)^2 + 14$
- d. $(g \circ f)(x) = 25x^2 + 70x + 56$

31.

Find x:

$$\begin{bmatrix} 1 & 3x & 2 \\ 3 & 0 & 5 \end{bmatrix} \begin{bmatrix} 4 & 1 \\ 2 & 0 \\ 0 & 1 \end{bmatrix} - \begin{bmatrix} 16 & 3 \\ 6 & 2 \end{bmatrix} = 3 \begin{bmatrix} x - 2 & 0 \\ 2 & 2 \end{bmatrix}$$

- a) 3
- b) 2
- c) 1
- d) 1/4

32.

Which of the following is a factor of $2x^4 - 6x^3 - 20x^2 + 48x$

- a) x 3
- b) x + 3
- c) x 1
- d) x + 1

33.

Solve for x:
$$\frac{2x+3}{x-1} - \frac{2x-3}{x+1} = \frac{10}{x^2-1}$$

- a) No solution
- b) x = 1
- c) x = 2
- d) $x = \frac{3}{4}$

34.

When photographing a lighted object, the exposure time (t) is inversely proportional to the square of the object's distance (d) from the light source. Which equation best represents this relationship?

a)
$$t^2 = kd$$

$$b) \quad t = \frac{k}{d^2}$$

c)
$$t = \frac{k}{d}$$

d)
$$t = kd$$

35.

Express as a single log $2\log_3 5 - \log_3 10 + 3\log_3 4$

a)
$$\log_3 \frac{5}{128}$$

c)
$$\log_3 160$$

36.

If $\log_7(x+1) + \log_7(x-5) = 1$, then x =

- a) 6
- b) -2
- d) 7

37.

Find the fifth term in the expansion of $(x + y)^{10}$

- a) 252x⁵y⁵
- b) $210x^4y^6$
- c) 210x⁶y⁴ d) 252x⁶y⁴

38.

Solve the equation $3x^2 = 57x$ using the method of your choice. You might want to try graphing or the quadratic formula. The value(s) of x that solve the equation are:

- **a.** x = 19 **b.** x = -19 **c.** x = 19 and x = 0 **d.** x = -19 and x = 0 **e.** x = 0

39.

Find g(-1) if $g(x) = -\left(\frac{1}{2}\right)^x$.

- **a.** $-\frac{1}{2}$ **b.** $\frac{1}{2}$ **c.** 0 **d.** -2 **e.** 2

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40.

Find the length of side x of the triangle below.

- **a.** 13.6
- **b.** 16.6
- **c.** 6.3
- **d.** 15.0
- **e.** 7.5

