# Image Clustering Using Local Discriminant Models and Global Integration

Yi Yang, Dong Xu, Member, IEEE, Feiping Nie, Shuicheng Yan, Senior Member, IEEE, and Yueting Zhuang

Abstract—In this paper, we propose a new image clustering algorithm, referred to as clustering using local discriminant models and global integration (LDMGI). To deal with the data points sampled from a nonlinear manifold, for each data point, we construct a local clique comprising this data point and its neighboring data points. Inspired by the Fisher criterion, we use a local discriminant model for each local clique to evaluate the clustering performance of samples within the local clique. To obtain the clustering result, we further propose a unified objective function to globally integrate the local models of all the local cliques. With the unified objective function, spectral relaxation and spectral rotation are used to obtain the binary cluster indicator matrix for all the samples. We show that LDMGI shares a similar objective function with the spectral clustering (SC) algorithms, e.g., normalized cut (NCut). In contrast to NCut in which the Laplacian matrix is directly calculated based upon a Gaussian function, a new Laplacian matrix is learnt in LDMGI by exploiting both manifold structure and local discriminant information. We also prove that K-means and discriminative K-means (DisKmeans) are both special cases of LDMGI. Extensive experiments on several benchmark image datasets demonstrate the effectiveness of LDMGI. We observe in the experiments that LDMGI is more robust to algorithmic parameter, when compared with NCut. Thus, LDMGI is more appealing for the real image clustering applications in which the ground truth is generally not available for tuning algorithmic parameters.

*Index Terms*—Clustering, K-means clustering, local discriminant model, spectral clustering.

#### I. INTRODUCTION

N the past decades, a large family of clustering methods were proposed to partition data points into clusters such that the data points within the same group are similar to each other, while the data points in different groups are dissimilar. Many clustering methods have been successfully used for image clustering to better organize, represent and browse images as well

Manuscript received July 21, 2009; revised December 25, 2009; accepted March 16, 2010. Date of publication April 26, 2010; date of current version September 17, 2010. This work was supported in part by the Singapore National Research Foundation Interactive Digital Media R&D Program under Grant No. NRF2008IDM-IDM004-018, in part by MOE AcRF Tier-1 Grant No. RG63/07, in part by the National Natural Science Foundation of China under Grant No. 90920303, and in part by the 973 Program under Grant No. 2010CB327905. The associate editor coordinating the review of this manuscript and approving it for publication was Dr. Patrick J. Flynn.

- Y. Yang and Y. Zhuang are with College of Computer Science, Zhejiang University, Hangzhou, Zhejiang Province 310027, P. R. China.
- D. Xu and F. Nie are with the School of Computer Engineering, Nanyang Technological University, 639798, Singapore (e-mail: dongxu@ntu.edu.sg).
- S. Yan is with Department of Electrical and Computer Engineering, National University of Singapore, 117576, Singapore.

Color versions of one or more of the figures in this paper are available online at http://ieeexplore.ieee.org.

Digital Object Identifier 10.1109/TIP.2010.2049235

as to improve the performances of related applications, such as content based image retrieval (CBIR), image annotation, and image indexing [6].

Many works [4], [10], [18] have demonstrated that the performances of CBIR systems can be improved by adopting image clustering methods. For example, to improve the performance of CBIR, images are grouped into clusters in [11] by using the classical clustering algorithm K-means as a preprocessing technique. Clustering algorithms were successfully applied in automatic image annotation systems [15], [19] as well. In [15], the personal album images were first clustered and then a web-based annotation method was developed to obtain the conceptual labels for image clusters, followed by a graph-based semisupervised learning method to propagate the conceptual labels to the whole photo album. In [16] and [28], the image clustering algorithms were utilized to extract a small subset of representative images for representing the diverse views of the landmarks. It has also been reported that image clustering is helpful for efficient indexing of high-dimensional images [36].

K-means has been frequently used for image clustering because of its simplicity. The traditional K-means clustering algorithm iteratively assigns each data point to the cluster with the closest centroid and updates the centroid of the samples in each cluster. However, the performance of K-means may drop significantly when the dimension of the image feature vector is high [5]. To address this problem, a straightforward way is to project the high-dimensional data into a low-dimensional subspace through subspace learning algorithms, e.g., principal components analysis (PCA) and then perform K-means in the lower-dimensional subspace. In recent years, some researchers have shown that linear discriminant analysis (LDA) [5], [31], [38] is a better choice than PCA for data clustering because discriminant information is utilized in LDA. Those researchers suggested simultaneously perform clustering and subspace learning by integrating K-means and LDA into a joint framework [5], [31], [38]. The initial works [5], [31] iteratively employed K-means to generate the cluster labels for LDA and exploited LDA to select the most discriminative subspace for K-means clustering. More recently, Ye et al. proposed a new discriminative K-means (DisKmeans) algorithm to simplify the iterative procedures as a trace maximization problem [38], which can be directly solved. It has been experimentally demonstrated that K-means with LDA outperforms traditional K-means and K-means with PCA for data clustering, because of the utilization of the discriminant information [5], [31], [38]. However, manifold information is not considered in K-means and DisKmeans. Consequently, K-means and DisKmeans can not effectively partition the data points sampled from nonlinear manifolds.

Besides discriminant information, the manifold structure of data is another crucial property to be considered in data clustering. The well-known spectral clustering (SC) algorithm normalized cut (NCut) [27] and its extension k-way NCut [39] have achieved promising clustering performances in image segmentation and many other applications, in which the similarities among neighboring points are considered to construct a graph for data clustering. However, the Gaussian function is directly adopted to compute a Laplacian matrix in NCut for data clustering, which may be sensitive to the bandwidth parameter in many applications, as reported in [32]. Recently, local learning based clustering (LLC) [33] was proposed to learn a Laplacian matrix for data clustering, which is based upon the assumption that the cluster label of each data point can be well predicted by its neighboring data points with a kernel rigid regression function. LLC can be regarded as an SC algorithm [33] as well. While the manifold information is utilized in NCut and LLC, the discriminant information is not sufficiently exploited.

To utilize both manifold information and discriminant information, we propose a new clustering method, namely clustering using local discriminant models and global integration (LDMGI), for image clustering. Similarly to [26], [27], and [33], for each data point, we consider a local clique. We construct a local discriminant model for each local clique and evaluate the clustering performance of samples in the clique with a variant of the Fisher criterion (referred to as the local discriminant score). A larger local discriminant score indicates that the samples in the local clique from different clusters are better separated. We further propose a unified objective function to maximize the sum of local discriminant scores from all the local cliques. We observe that LDMGI shares an objective function similar to other spectral clustering algorithms (e.g., NCut). Eigenvalue decomposition method is then used to obtain the relaxed continuous valued solution of the scaled cluster assignment matrix, which is further discretized to obtain the binary cluster assignment matrix for all the samples. LDMGI learns a new Laplacian matrix by using both manifold structure and local discriminant information, making it more robust for data clustering. When compared with NCut which is sensitive to the bandwidth parameter of the Gaussian function, LDMGI is robust to the algorithmic parameter. The ground truth is generally not available for tuning the parameters of clustering algorithms. Thus, LDMGI is more suitable for real clustering applications.

We theoretically prove that K-means and DisKmeans are both special cases of LDMGI. When compared with K-means and DisKmeans, LDMGI can effectively deal with the data points sampled from a nonlinear manifold. It is worth mentioning that K-means clustering and the spectral clustering algorithms are traditionally regarded as two different types of clustering techniques. However, an interesting observation in this paper is that K-means, DisKmeans and the spectral clustering algorithms are connected via LDMGI. That is K-means and DisKmeans are special cases of LDMGI, while LDMGI is a spectral clustering algorithm. While the connection between K-means and NCut has been discovered in [7] in terms of a kernel view, this work presents another new perspective to understand and explain the relationships between K-means (or DisKmeans) and spectral clustering algorithms.

It is worthwhile to highlight the following aspects of this paper:

- We propose a new clustering algorithm LDMGI, which utilizes both manifold information and discriminant information for data clustering.
- We theoretically prove that K-means and DisKmeans are both special cases of LDMGI. We also show that LDMGI is a type of spectral clustering algorithm. Thus, our work provides a new perspective to discover and understand the relationships between K-means (or DisKmeans) and other spectral clustering algorithms (e.g., NCut).
- Our work outperforms several existing data clustering methods and it is more robust to the algorithmic parameter.
   The rest of this paper is organized as follows. In Section II, we introduce the details of the proposed LDMGI algorithm.
   The connections between LDMGI and other existing clustering algorithms are discussed in Section III. Experimental results are reported in Section IV. Finally, we conclude this paper in Section V.

### II. CLUSTERING USING LOCAL DISCRIMINANT MODELS AND GLOBAL INTEGRATION

#### A. Local Discriminant Models

Let us define  $\mathcal{X}=\{x_1,x_2,\ldots,x_n\}$  as the image data set to be clustered, where  $x_i\in\mathbb{R}^m(1\leq i\leq n)$  is the ith data point and n is the total number of images. Clustering is to partition  $\mathcal{X}$  into c clusters  $\{C_j\}_{j=1}^c$ . Denote the cluster assignment matrix by  $Y=[y_1,y_2,\ldots,y_n]^T\in\{0,1\}^{n\times c}$ , where  $y_i\in\{0,1\}^{c\times 1}(1\leq i\leq n)$  is the cluster assignment vector for the image  $x_i$ . The jth element of  $y_i$  is 1 if  $x_i\in C_j$ , and 0 otherwise. We also denote  $X=[x_1,x_2,\ldots,x_n]$  as the data matrix. For any d, we define  $\mathbf{1}_d\in\mathbb{R}^d$  as a column vector with all its elements equal to  $1,H_d=I-(1)/(d)\mathbf{1}_d\mathbf{1}_d^T\in\mathbb{R}^{d\times d}$  as a matrix for centering the data by subtracting the mean of the data. It follows that  $H_d=H_d^T=H_dH_d$ . Following [39], instead of directly solving the cluster assignment matrix Y, we first define the scaled cluster assignment matrix G as follows:

$$G = [g_1, g_2, \dots, g_n]^T = Y(Y^T Y)^{-1/2}$$
 (1)

in which  $g_i$  is the scaled cluster assignment vector for the image  $x_i$ . It is obvious that the jth column of G is given by

$$G_{j} = \underbrace{[0, \dots, 0, \underbrace{1, \dots 1}_{n_{j}}, \underbrace{0, \dots, 0}_{n_{j}}]^{T} / \sqrt{n_{j}}}_{\sum_{i=j+1}^{c} n_{i}}$$
(2)

where  $n_j$  is the number of samples in the jth cluster  $C_j$ . Since  $Y^TY$  is a diagonal matrix, it is easy to verify that

$$G^TG = (Y^TY)^{-1/2}Y^TY(Y^TY)^{-1/2} = I.$$
 (3)

As shown in [8], the total scatter matrix  $S_t$  and the betweencluster scatter matrix  $S_b$  can be defined as

$$S_t = \sum_{i=1}^{n} (x_i - \mu)(x_i - \mu)^T = \tilde{X}\tilde{X}^T$$
 (4)

$$S_b = \sum_{i=1}^{c} n_i (\mu_i - \mu) (\mu_i - \mu)^T = \tilde{X} G G^T \tilde{X}^T$$
 (5)

where  $\mu_i$  is the mean of samples in the *i*th cluster  $C_i$ ,  $\mu$  is the mean of all samples and  $\tilde{X} = XH_n$  is the data matrix after subtracting the mean  $\mu$ . Intuitively, to better cluster the data, the distance between data from different clusters should be as large as possible while the distance between data from the same cluster should be as small as possible. Inspired by the Fisher criterion [8], the optimal scaled cluster assignment matrix  $G^*$  can be obtained by maximizing the following objective function:

$$G^* = \arg \max_{G} Tr[(S_t + \lambda I)^{-1}S_b]$$

$$= \arg \max_{G} Tr[(\tilde{X}\tilde{X}^T + \lambda I)^{-1}\tilde{X}GG^T\tilde{X}^T]$$

$$= \arg \max_{G} Tr[G^T\tilde{X}^T(\tilde{X}\tilde{X}^T + \lambda I)^{-1}\tilde{X}G] \qquad (6)$$

where the identity matrix I is added to make the matrix  $(\tilde{X}\tilde{X}^T +$  $\lambda I$ ) nonsingular with the regularization parameter  $\lambda > 0$ . Considering that  $G^TG = I$ , we can also minimize the following objective function to obtain  $G^*$ :

$$G^* = \arg\min_{G} Tr[G^T G - G^T \tilde{X}^T (\tilde{X}\tilde{X}^T + \lambda I)^{-1} \tilde{X}G].$$
(7)

Note that both the total scatter matrix  $S_t$  and the between-cluster scatter matrix  $S_b$  in (6) are defined according to Euclidean distances among the data. Thus, it is not easy to partition the data sampled from the nonlinear manifold into the correct clusters with such a criterion. Previous manifold learning algorithms [1], [26] and clustering algorithms [27], [33] have demonstrated that it is beneficial to exploit local geometric properties for recovering the intrinsic manifold structure of data. Considering that local manifold structure is approximately linear [26], for each data point  $x_i$ , we consider a local clique  $\mathcal{N}_k(x_i)$  comprising k data points including  $x_i$  and its k-1 nearest neighbors, and employ a local linear discriminant model to evaluate the clustering results for the data points in  $\mathcal{N}_k(x_i)$ . The overall clustering results can then be obtained by globally optimizing the local discriminant models of all the local cliques.

Let  $F_i = \{i_0, i_1, i_2, \dots, i_{k-1}\}$  be the index set of the samples in  $\mathcal{N}_k(x_i)$ , where we set  $i_0 = i$ . We define  $X_i = [x_{i_0}, x_{i_1}, \dots, x_{i_{k-1}}]$  as the local data matrix comprising all the data points in  $\mathcal{N}_k(x_i)$ . Given the scaled cluster assignment matrix G, we define  $G_{(i)} = [g_{i_0}, g_{i_1}, \dots, g_{i_{k-1}}]^T \in \mathbb{R}^{k \times c}$   $A(A^TA + \lambda I)^{-1} = (AA^T + \lambda I)^{-1}(AA^T + \lambda I)A(A^TA + \lambda I)^{-1}$ as the local scaled cluster assignment matrix for the ith clique, in which  $g_{i_j}$  is the scaled cluster assignment vector of  $x_{i,j} \in \mathcal{N}_k(x_i)$   $(\bar{j} = 0, \dots, k-1)$ . More specifically,  $G_{(i)}$  is selected from the scaled cluster assignment matrix G, namely

$$G_{(i)} = S_i^T G \tag{8}$$

where  $S_i \in \mathbb{B}^{n \times k}$  is the selection matrix with its element  $(S_i)_{pq} = 1$ , if  $p = F_i\{q\}$ ;  $(S_i)_{pq} = 0$ , otherwise. Let  $m_{i_p}|_{p=1}^c$ be the number of samples from the pth cluster in the local clique  $\mathcal{N}_k(x_i)$ . Without loss of generality, we assume that the samples in the local clique are reorganized such that the samples from the same cluster are put together. The jth column of  $G_{(i)}$  can

$$G_{(i)}^{j} = \left[\underbrace{0, \dots, 0}_{\sum_{j=1}^{j-1} m_{i_p}}, \underbrace{1, \dots, 1}_{m_{i_j}}, \underbrace{0, \dots, 0}_{\sum_{p=j+1}^{c} m_{i_p}}\right]^{T} / \sqrt{n_j}.$$
 (9)

Thus, we have

$$G_{(i)}G_{(i)}^{T} = [G_{(i)}^{1}, G_{(i)}^{2}, \dots, G_{(i)}^{c}] \begin{bmatrix} G_{(i)}^{1}, G_{(i)}^{2}, \dots, G_{(i)}^{c} \end{bmatrix}^{T}$$

$$= \begin{bmatrix} K_{1} & 0 & 0 \\ 0 & \ddots & 0 \\ 0 & 0 & K_{c} \end{bmatrix}$$
(10)

where  $K_p \in R^{m_{i_p} \times m_{i_p}}$  is a square matrix with all its elements equaling to  $1/n_p(1 \le p \le c)$ . We define the local discriminant score for the ith clique as follows:

$$\arg\max_{G_{(i)}} Tr \left[ G_{(i)}^T \tilde{X}_i^T (\tilde{X}_i \tilde{X}_i^T + \lambda I)^{-1} \tilde{X}_i G_{(i)} \right]$$
 (11)

where  $\tilde{X}_i = X_i H_k$ . As shown in (10),  $G_{(i)} G_{(i)}^T$  is a block diagonal matrix. Similar to (5),  $\tilde{X}_i G_{(i)} G_{(i)}^T \tilde{X}_i^T$  still measures the intercluster separability of samples within the local clique. Thus, a larger local discriminant score indicates that the samples in the local clique from different clusters are better separated. Considering that the number of samples in each local clique is small, we impose a regularization term  $Tr(G_{(i)}^T H_k G_{(i)})$  to control the capacity of the local discriminant model. Similar to (7), we have the following objective function for the ith local clique:

$$\arg\min_{G_{(i)}} Tr \left\{ G_{(i)}^T H_k G_{(i)} - G_{(i)}^T \tilde{X}_i^T \left( \tilde{X}_i \tilde{X}_i^T + \lambda I \right)^{-1} \tilde{X}_i G_{(i)} \right\}. \quad (12)$$

In the following, we show that the objective function in (12) with the regularization term can be rewritten to (13) by using lemma-1 and Theorem-1, which can be more efficiently solved when compared with (11).

Lemma 1: For any matrix A, we have  $A(A^TA + \lambda I)^{-1} =$  $(AA^T + \lambda I)^{-1}A$ .

*Proof:* It is obvious that  $(AA^T + \lambda I)A = A(A^TA + \lambda I)$ . Then, we have

$$A(A^{T}A + \lambda I)^{-1} = (AA^{T} + \lambda I)^{-1}(AA^{T} + \lambda I)A(A^{T}A + \lambda I)^{-1}$$
$$= (AA^{T} + \lambda I)^{-1}A(A^{T}A + \lambda I)(A^{T}A + \lambda I)^{-1}$$
$$= (AA^{T} + \lambda I)^{-1}A.$$

Theorem 1: The optimization problem of (12) is equivalent to the following optimization problem:

$$\arg\min_{G_{(i)}} Tr \left\{ G_{(i)}^T \left[ H_k \left( \tilde{X}_i^T \tilde{X}_i + \lambda I \right)^{-1} H_k \right] G_{(i)} \right\}. \tag{13}$$

*Proof:* According to *lemma-1* and  $\tilde{X}_i H_k = \tilde{X}_i$ , we have

$$\begin{split} G_{(i)}^T \left[ \tilde{X}_i^T \left( \tilde{X}_i \tilde{X}_i^T + \lambda I \right)^{-1} \tilde{X}_i \right] G_{(i)} \\ &= G_{(i)}^T \left[ H_k \tilde{X}_i^T \left( \tilde{X}_i \tilde{X}_i^T + \lambda I \right)^{-1} \tilde{X}_i H_k \right] G_{(i)} \\ &= G_{(i)}^T \left[ H_k \left( \tilde{X}_i^T \tilde{X}_i + \lambda I \right)^{-1} \tilde{X}_i^T \tilde{X}_i H_k \right] G_{(i)} \\ &= G_{(i)}^T \left[ H_k \left( \tilde{X}_i^T \tilde{X}_i + \lambda I \right)^{-1} \left( \tilde{X}_i^T \tilde{X}_i + \lambda I - \lambda I \right) H_k \right] G_{(i)} \\ &= G_{(i)}^T [H_k - \lambda H_k \left( \tilde{X}_i^T \tilde{X}_i + \lambda I \right)^{-1} H_k] G_{(i)}. \end{split}$$

Therefore, the optimization problem of (12) is equivalent to the problem of (13).

Since k is the number of samples in each local clique, it is usually much smaller than the dimension of data points.  $\tilde{X}_i^T \tilde{X}_i$  is of size  $k \times k$ , so it is much faster to calculate the inverse of  $\tilde{X}_i^T \tilde{X}_i + \lambda I$  in (13) in comparison to the inverse of  $\tilde{X}_i \tilde{X}_i^T + \lambda I$  in (12). Additionally, with (13), the proposed clustering algorithm LDMGI can be easily extended to its kernel version, which will be studied in the future. The objective function of (13) can be also rewritten as

$$\arg\min_{G_{(i)}} Tr \left[ G_{(i)}^T L_i G_{(i)} \right] \tag{14}$$

where

$$L_i = H_k (\tilde{X}_i^T \tilde{X}_i + \lambda I)^{-1} H_k. \tag{15}$$

#### B. Global Integration

To obtain the optimal G, we expect that the data points are well separated in all the local cliques. Thus, we propose the following objective function to globally integrate the local discriminant models by summing (14) over all the local cliques, which can be formulated as

$$\arg\min_{G} \sum_{i=1}^{n} Tr\left[G_{(i)}^{T} L_{i} G_{(i)}\right]. \tag{16}$$

Note that the local scaled cluster assignment matrix  $G_{(i)}$  is selected from the scaled assignment matrix G, i.e.,  $G_{(i)} = S_i^T G$ . Then, the objective function in (16) can be rewritten as

$$\arg\min_{G} \sum_{i=1}^{n} Tr \left[ G^{T} S_{i} L_{i} S_{i}^{T} G \right]$$

$$= \arg\min_{G} Tr \left[ G^{T} \left( \sum_{i=1}^{n} S_{i} L_{i} S_{i}^{T} \right) G \right]. \quad (17)$$

Let us define

$$L = \sum_{i=1}^{n} S_i L_i S_i^T$$

$$= [S_1, S_2, \dots, S_n] \begin{bmatrix} L_1 & & \\ & \cdots & \\ & & L_n \end{bmatrix} [S_1, S_2, \dots, S_n]^T.$$

The objective function of LDMGI becomes

$$\arg\min_{G} Tr(G^{T}LG). \tag{19}$$

As shown in (1) and (3), we have two constraints for G, namely, G is a scaled cluster assignment matrix, i.e.,  $G = Y(Y^TY)^{-1/2}$ , and  $G^TG = I$ . Then the objective function of LDMGI can be written as

$$\arg\min_{G} Tr(G^TLG)$$
 s.t.  $G^TG = I$  and  $G = Y(Y^TY)^{-1/2}$ . (20)

In the following *Theorem*-2, we prove that the matrix L defined in (18) is a Laplacian matrix. Therefore, the objective function of LDMGI in (20) has a similar form to NCut [27]. Ncut directly adopts the Gaussian function to compute a Laplacian matrix for clustering, which is sensitive to the bandwidth parameter of the Gaussian function [32]. In contrast, we learn a new Laplacian matrix by employing discriminant information and manifold structure, which is more robust for data clustering.

Lemma 2: Given a positive semidefinite matrix C,  $DCD^T$  is a positive semidefinite matrix for any matrix D.

*Proof:* C is a positive semidefinite matrix, so we can write C as  $C = M^TM$ . Then, we have  $DCD^T = DM^TMD^T = (MD^T)^T(MD^T)$ . Therefore,  $DCD^T$  is a positive semidefinite matrix.

Theorem 2: The matrix L defined in (18) is a Laplacian matrix

*Proof:*  $L_i = H_k(\tilde{X}_i^T\tilde{X}_i + \lambda I)^{-1}H_k$ . It is obvious  $(\tilde{X}_i^T\tilde{X}_i + \lambda I)^{-1}$  is a positive semidefinite matrix. According to lemma-2,  $L_i$  is a positive semidefinite matrix. In addition, we have  $H_k\mathbf{1}_k = (I-(1)/(k)\mathbf{1}_k\mathbf{1}_k^T)\mathbf{1}_k = \mathbf{0}$ . Then, it can be shown that  $L_i\mathbf{1}_k = \mathbf{0}$ . Therefore, we conclude that  $L_i$  is a Laplacian matrix.

Laplacian matrix.  $L_1$  Let us define  $A=\begin{bmatrix}L_1\\ \dots\end{bmatrix}$  and  $L_n$   $S=[S_1,S_2,\dots,S_n]$ , then  $L=SAS^T$ .  $L_i$  is a positive semidefinite matrix, so  $q_i^TL_iq_i\geqslant 0, \ \forall\ q_i\in\mathbb{R}^k$ . Let us denote z=nk. We have  $q^TAq=\sum_i q_i^TL_iq_i\geqslant 0, \ \forall\ q=[q_1^T,q_2^T,\dots,q_n^T]^T\in\mathbb{R}^z$ . Thus, A is a positive semidefinite matrix. According to lemma-2,  $L=SAS^T$  is a positive semidefinite matrix. In addition, we have  $A\mathbf{1}_z=\mathbf{0}$  and  $S^T\mathbf{1}_n=\mathbf{1}_z$ . Then,  $L\mathbf{1}_n=SAS^T\mathbf{1}_n=SA\mathbf{1}_z=\mathbf{0}$ . Thus, we can conclude that L is a Laplacian matrix.

#### C. Relaxation and Discretization

As shown in [27], the objective function in (20) is NP hard, because the scaled cluster assignment matrix G is constrained as  $G = Y(Y^TY)^{-1/2}$ . Following [27], we first remove this constraint and relax G to the continuous-valued domain. That is, the objective function is simplified as  $\min_{G^TG=I} Tr(G^TLG)$ . Then eigenvalue decomposition method can be used to solve the optimization problem

$$Lu_i = \lambda_i u_i \tag{21}$$

 $^{1}$ The Laplacian matrix L can be also obtained by globally aligning a set of local linear regression models. For more details, please refer to [37].

where  $\lambda_0 < \lambda_1 <, \ldots, < \lambda_{n-1}$  are the eigenvalues and  $u_i|_{i=0}^{n-1}$  are the corresponding eigenvectors. It is obvious that there is a trivial solution with  $\lambda_0 = 0$  and  $u_0 = \mathbf{1}_n$ . After removing this trivial solution, we have the optimal solution  $G^*$ 

$$G^* = [u_1, u_2, \dots, u_{c-1}, u_c]. \tag{22}$$

To obtain the cluster assignment matrix  $Y \in \mathbb{B}^{n \times c}$ , we then discretize  $G^*$  using spectral rotation [39]. For any orthogonal matrix (referred to as a rotation matrix)  $R \in \mathbb{R}^{c \times c}$ , it is easy to show that  $\hat{G}^* = G^*R$  is the solution of the optimization problem  $\min_{G^TG=I} Tr(G^TLG)$  as well. Thus, the global optimal solution  $G^*$  is not unique. We therefore compute the optimal binary valued cluster assignment matrix Y which is closest to  $G^*R$ . Following [39], we define a mapping function for  $G^*$  as:

$$Y^* = f^{-1}(G^*) = \text{Diag}(G^*G^{*T})^{-1/2}G^*$$
 (23)

where  $\operatorname{Diag}(G^*G^{*T})$  is the diagonal matrix with the same size and the same diagonal elements of  $G^*G^{*T}$ . In [39], it has been proven that  $f^{-1}(G^*R) = Y^*R$  and  $Y^*R$  is the optimal solution to the optimization problem in (20). Then, the optimal binary valued solution Y and the rotation matrix R can be simultaneously obtained by solving the following optimization problem:

$$\arg\min_{Y\in\mathbb{B}^{n\times c},R\in\mathbb{R}^{c\times c}} \quad ||Y-Y^*R||^2$$
 s.t. 
$$Y\mathbf{1}_c=\mathbf{1}_n,R^TR=I. \tag{24}$$

We iteratively optimize Y and R until convergence. For more details, please refer to [39]. We summarize our proposed LDMGI algorithm in the following Procedure-1.

#### Procedure-1: The LDMGI Clustering Algorithm.

- 1) For each data point  $x_i$ , construct its local clique  $\mathcal{N}_k(x_i), i = 1, \dots, n$ ;
- 2) compute  $L_i|_{i=1}^n$  according to (15);
- 3) compute L using (18);
- 4) solve the eigenvalue decomposition problem in (21) to obtain the optimal  $G^* = [u_1, u_2, \dots, u_c]$ . The trivial solution  $u_0 = \mathbf{1}_n$  corresponding to the eigenvalue  $\lambda_0 = 0$  is removed;
- 5) compute  $Y^*$  according to (23) and solve the optimization problem shown in (24) using spectral rotation [39].

#### III. CONNECTIONS WITH PREVIOUS CLUSTERING ALGORITHMS

The most well-known and widely-used clustering algorithms are K-means clustering and spectral clustering. In this section, we discuss the connections between our LDMGI and some representative clustering techniques including K-means, DisKmeans, and spectral clustering.

#### A. Connection With K-Means

K-means is a simple and frequently used clustering algorithm. The K-means clustering algorithm partitions n data

points into c clusters  $\{C_j\}_{j=1}^c$  by minimizing the following objective function:

$$\arg\min_{C_{j}|_{j=1}^{c}} \sum_{j=1}^{c} \sum_{x_{i} \in C_{j}} \|x_{i} - \mu_{j}\|^{2}$$
 (25)

where  $\mu_j$  is the mean of samples in the jth cluster  $C_j$ . The traditional K-means clustering algorithm uses an EM-like approach to iteratively assign each data point to the cluster with the closest centroid and update the centroid of the samples in each cluster. In [40], it is proven that the objective function of K-means can be rewritten as

$$\arg\max_{G^T G = I} Tr(G^T \tilde{X}^T \tilde{X} G) \tag{26}$$

where  $\tilde{X} = XH_n$  and G is the scaled cluster assignment matrix. The connection between K-means and LDMGI is discovered as follows.

*Proposition 1:* K-means is a special case of the proposed LDMGI clustering algorithm, when k = n and  $\lambda \to \infty$ .

*Proof:* When k = n, we have  $G_{(i)} = G$  and  $\tilde{X}_i = \tilde{X}$ . First, we prove  $Tr(G^TH_nG) = c - 1$ 

$$Tr(G^{T}H_{n}G)$$

$$= Tr\left[G^{T}\left(I - \frac{1}{n}\mathbf{1}_{n}\mathbf{1}_{n}^{T}\right)G\right]$$

$$= Tr(G^{T}G) - \frac{1}{n}Tr\left(\mathbf{1}_{n}^{T}GG^{T}\mathbf{1}_{n}\right)$$

$$= c - \frac{1}{n}Tr\left[\mathbf{1}_{n}^{T}Y(Y^{T}Y)^{-1}Y^{T}\mathbf{1}_{n}\right]$$

$$= c - \frac{1}{n}Tr$$

$$\left\{ \begin{bmatrix} n_{1}, \dots, n_{c} \end{bmatrix} \begin{bmatrix} \frac{1}{n_{1}} & \cdots & \\ & \frac{1}{n_{c}} \end{bmatrix} \begin{bmatrix} n_{1} \\ \cdots \\ & n_{c} \end{bmatrix} \right\}$$

$$= c - 1.$$

Therefore, the objective function in (12) is equivalent to the objective function in (11), when k=n. When  $\lambda\to\infty$ , the objective function in LDMGI can be rewritten as

$$\begin{split} & \arg\max_{G^TG=I} \sum_{i=1}^n Tr[G^T\tilde{X}^T(\tilde{X}\tilde{X}^T+\lambda I)^{-1}\tilde{X}G] \\ & = \arg\max_{G^TG=I} Tr(G^T\tilde{X}^T\tilde{X}G). \end{split}$$

Thus, K-means is a special case of LDMGI, when k=n and  $\lambda \to \infty$ .

#### B. Connection With Discriminative K-Means (DiskMeans)

Recently, some researchers suggested to simultaneously perform K-means clustering and LDA by optimizing the following objective function [5], [31] [38]:

$$\arg \max_{W,G} Tr[(W^T(S_t + \gamma I)W)^{-1}W^TS_bW]$$

$$= \arg \max_{W,G} Tr[(W^T(\tilde{X}\tilde{X}^T + \gamma I)W)^{-1}W^T\tilde{X}GG^T\tilde{X}^TW]$$
(27)

where W is the projection matrix, and G is the scaled cluster assignment matrix. The initial works [5] [31] iteratively optimize G and W by employing K-means to generate the cluster labels for LDA and using LDA to select the most discriminative subspace for K-means clustering. In [38], Ye *et al.* have proven that the objective function shown in (27) can be simplified to the following trace maximization problem:

$$\arg\max_{G^TG=I} Tr\left\{G^T \left[I - \left(I + \frac{1}{\gamma}\tilde{X}^T\tilde{X}\right)^{-1}\right]G\right\}. \quad (28)$$

Instead of using the iterative procedure, Ye *et al.* proposed the DisKmeans clustering algorithm in which only G needs to be solved [5]. The connection between DisKmeans and LDMGI is as follows.

Proposition 2: DisKmeans [38] is a special case of LDMGI, when k=n.

*Proof:* Again, when k=n, we have  $G_{(i)}=G$  and  $\tilde{X}_i=\tilde{X}$ . As shown in the proof of *Proposition*-1, we have  $Tr(G^TH_nG)=c-1$ . Therefore, when k=n-1, the objective function of LDMGI can be rewritten as

$$\arg \max_{G^T G = I} Tr \left[ G^T \tilde{X}^T (\tilde{X} \tilde{X}^T + \lambda I)^{-1} \tilde{X} G \right]$$

$$= \arg \max_{G^T G = I} Tr \left[ G^T \tilde{X}^T \left( I + \frac{1}{\gamma} \tilde{X} \tilde{X}^T \right)^{-1} \tilde{X} G \right]$$

$$= \arg \max_{G^T G = I} Tr \left\{ G^T \left[ \left( I + \frac{1}{\gamma} \tilde{X}^T \tilde{X} \right)^{-1} \tilde{X}^T \tilde{X} \right] G \right\}$$

$$= \arg \max_{G^T G = I} Tr \left\{ G^T \left[ \gamma \left( I + \frac{1}{\gamma} \tilde{X}^T \tilde{X} \right)^{-1} \left( \frac{1}{\gamma} \tilde{X}^T \tilde{X} + I - I \right) \right] G \right\}$$

$$= \arg \max_{G^T G = I} Tr \left\{ G^T \left[ I - \left( I + \frac{1}{\gamma} \tilde{X}^T \tilde{X} \right)^{-1} \right] G \right\}.$$
(29)

In the first step, we set  $\lambda = \gamma$ , and *lemma-1* is used in the second step. Therefore, DisKmeans [38] is a special case of LDMGI.

Both DisKmeans and LDMGI make use of discriminant information. However, manifold information is not utilized in DisKmeans. Thus, DisKmeans cannot effectively cope with data points sampled from a nonlinear manifold. LDMGI employs both discriminant information and manifold structure, and it is more robust.

#### C. Connection With Spectral Clustering

In recent years, several spectral clustering algorithms have been proposed [22], [27], [33]. These algorithms can be generally formulated as the following optimization problem:

$$\arg\min_{G^TG=I} Tr(G^T\hat{L}G) \tag{30}$$

where  $\hat{L}$  is a Laplacian matrix. Different spectral clustering algorithms use different Laplacian matrices, which play key roles

in spectral clustering. In NCut [27] and its extension k-way NCut [39], the Laplacian matrix is defined as

$$\tilde{L} = I - D^{-1/2} A D^{-1/2} \tag{31}$$

where D is a diagonal matrix with its diagonal elements defined as  $D_{ii} = \sum_{j=1}^{n} A_{ij}$  for  $i=1,\ldots,n$  and the graph affinity matrix A is computed by using Gaussian function

$$A_{ij} = \begin{cases} \exp\left(-\frac{||x_i - x_j||^2}{\sigma^2}\right), & x_i \text{ and } x_j \text{ are k-nearest neighbors;} \\ 0, & \text{otherwise} \end{cases}$$
(32)

where  $\sigma$  is the bandwidth parameter.

More recently, Wu and Schölkopf proposed a local learning approach for data clustering (referred to as LLC here) [33]. Denote  $\mathcal{N}_i = \{x_{i_1}, x_{i_2}, \ldots, x_{i_k}\}$  as the k-nearest neighbor set of  $x_i$  excluding  $x_i$  and  $G = [g^1, g^2, \ldots, g^c] \in \mathbb{R}^{n \times c}$  as the scaled cluster assignment matrix, in which  $g^l = [g^l_1, \ldots, g^l_n]^T \in \mathbb{R}^n (1 \leq l \leq c)$  is the lth column of G. LLC is based upon the assumption that the cluster label  $g^l_i$  of each data point  $x_i (1 \leq i \leq n)$  can be well predicted by a local model  $o^l(x_i) = \sum_{x_j \in \mathcal{N}_i} \beta^l_{ij} K(x_i, x_j)$ , where K is a kernel matrix,  $\beta^l_{ij}$  are the linear combination coefficients. LLC adopted a two-step approach to learn a Laplacian matrix for data clustering. In the first step of LLC, a local model is trained for each data point  $x_i$  using the following kernel ridge regression function:

$$\arg\min_{\beta_i^l \in \mathbb{R}^k} \eta(\beta_i^l)^T \mathbf{K}_i \beta_i^l + \left\| \mathbf{K}_i \beta_i^l - g_{(i)}^l \right\|^2$$
 (33)

where  $\eta > 0$  is a regularization parameter,  $\beta_i^l = [\beta_{ii_1}^l, \dots \beta_{ii_k}^l]^T, g_{(i)}^l = [g_{i_1}^l, \dots g_{i_k}^l]^T$ , and  $\mathbf{K}_i \in \mathbb{R}^{k \times k}$  denotes the subkernel matrix, i.e.,  $\mathbf{K}_i = [K(x_u, x_v)]$  for  $x_u, x_v \in \mathcal{N}_i$ . In the second step, each locally trained model is used to predict the cluster labels of one data point only. Then the clustering results can be obtained by minimizing the sum of prediction errors of all the local models

$$\sum_{l=1}^{c} \sum_{i=1}^{n} (g_i^l - o^l(x_i))^2.$$
 (34)

Let us define  $\alpha_i^T = k_i^T (\mathbf{K}_i + \eta I)^{-1}$  where  $k_i = [K(x_i, x_{i_1}), \dots, K(x_i, x_{i_k})]^T$  and  $A = [a_{ij}] \in \mathbb{R}^{N \times N}$  which is constructed as follows:  $\forall x_i, x_j$ , if  $x_j \in \mathcal{N}_i$ , then  $a_{ij}$  is equal to the corresponding element of  $\alpha_i$ ; otherwise,  $a_{ij}$  equals zero. It has been proven in [33] that the optimization problem shown in (34) is equivalent to the following optimization function:

$$\arg\min_{G^TG=I} Tr(G^T L_l G) \tag{35}$$

where  $L_l$  is a Laplacian matrix which is defined as  $L_l = (I - A)^T (I - A)$ . With (35), it is obvious that LLC has a form similar to (30), thus, it is a spectral clustering method [33]. Considering that the matrix L defined in (18) is also a Laplacian matrix (see *Theorem 2*), we have the following proposition.

*Proposition 3:* LDMGI is a spectral clustering algorithm, which learns a Laplacian matrix for data clustering by explicitly employing discriminant information and manifold structure.

Discussions: NCut, LLC, and our LDMGI are all spectral clustering algorithms. They are different because they use different Laplacian matrices. Neut directly adopts a Gaussian function to compute the Laplacian matrix for data clustering. As reported in [32], a major disadvantage of using Gaussian function to compute a Laplacian matrix is that it is sensitive to the bandwidth parameter  $\sigma$ . On the other hand, LDMGI learns a Laplacian matrix for clustering by using discriminant information and manifold structure, making it more effective and robust. Traditionally, K-means clustering and spectral clustering are regarded as different families of clustering algorithms. While the connection between K-means and NCut has been discussed in [7] in terms of a kernel view, this work presents another new perspective to understand and explain the relationships between K-means (or DisKmeans) and spectral clustering algorithms via LDMGI. That is, K-means and DisKmeans are both special cases of LDMGI, and LDMGI is a type of spectral clustering algorithm.

#### IV. EXPERIMENTS

We compare the proposed LDMGI with K-means, DisKmeans [38] and two spectral clustering algorithms NCut [27] and LLC [33]. For LDMGI, NCut, and LLC, spectral rotation [39] is used to obtain the clustering results. For LLC, both a Gaussian kernel (denoted as LLC-G) and a linear kernel (denoted as LLC-L) are used as the kernel function  $K(x_i,x_j)$  in (33).

#### A. Image Dataset

In our experiments, over 30 000 samples from 10 benchmark databases were used to test the image clustering performance. The COIL-20 [21] database has 1440 images of 20 objects, with each object containing 72 images captured from different views. The USPS database contains 9298 gray-scale handwritten digit images scanned from envelopes by the U.S. Postal Service. The image size is  $16 \times 16$ . The MNIST database [17] has a training set of 60 000 examples, and a test set of 10 000 examples with an image size of  $28 \times 28$  and two subdatabases are chosen from the MNIST database. Following [34], we use the first part of the test set of the MNIST database (referred to as MNIST-T) which is cleaner than the second part [17]. MNIST-T consists of 5000 images of handwritten numbers with each digital number having 500 images. In the second subdatabase (referred to as MNIST-S), for each class we randomly sample one handwritten digit image per ten images. Thus, we totally have 6996 handwritten images in MNIST-S. The USF HumanID database constructed by Sarkar et al. [25] consists of people walking in elliptical paths in front of the camera. We resize each average silhouette image [14], [35] to  $32 \times 22$  and then represent it as a 704-dimensional feature vector. 2190 sampled images are used in this experiment. The UMIST face image database [13] has 575 multiview face images of 20 people, covering a broad range of poses from profile to frontal views. The images are resized to  $28 \times 23$ 

TABLE I DATABASE DESCRIPTIONS

Dataset	Sample Size	Feature Dim	Classes Number
COIL-20	1440	1024	20
USPS	9298	256	10
MNIST-T	5000	784	10
MNIST-S	6996	784	10
USF HumanID	2190	704	122
UMIST	575	644	20
YALE-B	2414	1024	38
JAFFE	213	676	10
Pointing04	2790	1120	15
MPEG7	600	200	30

pixels. The YALE-B database [9] contains 2414 near frontal images from 38 persons under different illuminations. Each image is resized to  $32 \times 32$ . The Japanese Female Facial Expression (JAFFE) database consists of 213 images of different facial expressions from 10 Japanese female models [20]. The images are resized to  $26 \times 26$ . The Pointing 04 face database consists of 15 sets of images [12]. Each set contains two series of 93 images of the same person. In our experiment, each face is resized to  $40 \times 28$ , and then represented by a 1120-dimensional normalized feature vector. The first 600 images from MPEG7 shape image database [3], [30] were first aligned by employing the Hungarian method, and the pair-wise distances among images were computed based upon the shape context algorithm [2]. After that, multidimensional scaling (MDS) is used to obtain a 200 dimensional normalized feature vector for each shape image. Table I summarizes the detailed information in terms of the total number of data, the total number of clusters and the feature dimension.

#### B. Evaluation Metrics

We use clustering accuracy (ACC) and normalized mutual information (NMI) for performance evaluation in this work.

Clustering Accuracy (ACC): For the ith image, let us denote  $q_i$  as the clustering result from the clustering algorithm and  $p_i$  as the ground truth label. The ACC is defined as

$$ACC = \frac{\sum_{i=1}^{n} \delta(p_i, \text{map}(q_i))}{n}$$
 (36)

where n is the total number of images,  $\delta(x,y)=1$  if x=y ( $\delta(x,y)=0$  otherwise), and  $\mathrm{map}(q_i)$  is the optimal mapping function that permutes clustering labels to match the ground truth labels. The optimal mapping can be obtained by using the Kuhn-Munkres algorithm [23]. A larger ACC indicates better performance.

Normalized Mutual Information (NMI): NMI is another widely used measure for evaluating the clustering results. For two arbitrary variables P and Q, NMI is defined as follows [29]:

$$NMI(P,Q) = \frac{I(P,Q)}{\sqrt{H(P)H(Q)}}$$
(37)

where I(P,Q) is the mutual information between P and Q and H(P) and H(Q) denote the entropies of P and Q, respectively [29]. It is obvious that  $\mathrm{NMI}(P,Q)$  equals 1 if P is identical with Q, and it becomes 0 if P is independent from Q. Let  $t_l$  be

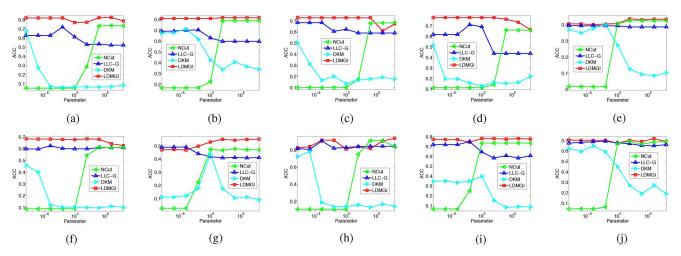


Fig. 1. Performance variations (ACC) of NCut [39], LLC-G [33], DisKmeans (DKM) [38] and our LDMGI with different parameters. (a) COIL-20, (b) USPS, (c) MNIST-T, (d) MNIST-S, (e) USF HumanID, (f) UMIST, (g) YALE-B, (h) JAFFE, (i) Pointing04, and (h) MPEG7.

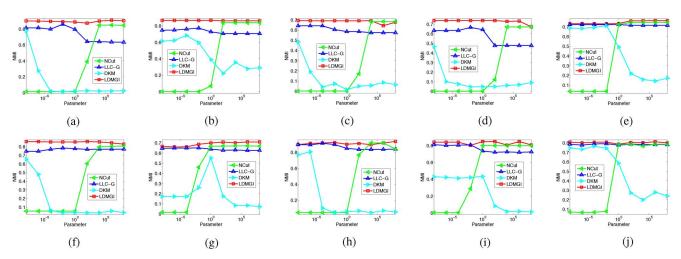


Fig. 2. Performance variations (NMI) of NCut [39], LLC-G [33], DisKmeans (DKM) [38] and our LDMGI with different parameters. (a) COIL-20, (b) USPS, (c) MNIST-T, (d) MNIST-S, (e) USF HumanID, (f) UMIST, (g) Yale-B, (h) JAFFE (i) Pointing04, (h) MPEG7.

the number of samples in the cluster  $C_l$   $(1 \le l \le c)$  obtained by using the clustering algorithms and  $\tilde{t}_h$  be the number of samples in the hth ground truth class  $(1 \le h \le c)$ . NMI is defined as [29]

$$NMI = \frac{\sum_{l=1}^{c} \sum_{h=1}^{c} t_{l,h} \log \left( \frac{n \cdot t_{l,h}}{t_{l} \tilde{t}_{h}} \right)}{\sqrt{\left(\sum_{l=1}^{c} t_{l} \log \frac{t_{l}}{n}\right) \left(\sum_{h=1}^{c} \tilde{t}_{h} \log \frac{\tilde{t}_{h}}{n}\right)}}$$
(38)

where  $t_{l,h}$  is the number of samples that are in the intersection between the cluster  $C_l$  and the hth ground truth class. Again, a larger NMI indicates a better clustering result.

#### C. Performance Comparison

Several parameters need to be set beforehand for these clustering techniques. The total number of clusters c is provided for all the clustering algorithms. For LDMGI, NCut and LLC, we also need to determine the parameter k which specifies the number of nearest neighbors. The clustering performance can be different if k changes. Generally speaking, k should be set as a small number to preserve the local manifold structure. To

fairly compare performance of LDMGI, NCut and LLC, we fix k as 5 for all the three algorithms on all the databases. We need to determine the optimal parameter  $\gamma$  in (28) for DisKmeans,  $\eta$  in (33) for LLC,  $\sigma$  in (32) for NCut, and  $\lambda$  in (15) for our LDMGI. For fair comparison, we set these parameters as  $\{10^{-8}, 10^{-6}, 10^{-4}, 10^{-2}, 10^{0}, 10^{2}, 10^{4}, 10^{6}, 10^{8}\}$  and then report the best clustering results from the optimal parameters. Different parameters may be used for different databases (see Figs. 1 and 2).

The results of all clustering algorithms depend upon the initialization [39]. For all the clustering algorithms, we independently repeat the experiments 20 times with random initializations to reduce the statistical variation. For clustering algorithms DisKmeans, LLC, NCut, and LDMGI, we also need to search for the best parameters in the set  $\{10^{-8}, 10^{-6}, 10^{-4}, 10^{-2}, 10^{0}, 10^{2}, 10^{4}, 10^{6}, 10^{8}\}$ . Thus, on each database 20 rounds of clustering are performed for K-means, and 180 rounds of clustering are performed for other clustering algorithms. In Tables II and III, we report the best results from these 20 or 180 rounds of clustering corresponding to the best objective values in terms of ACC and NMI, respectively. For NCut, LLC-G, DisKmeans

TABLE II

PERFORMANCE COMPARISON (ACC%) OF K-MEANS, DISKMEANS [38], NCUT [39], LLC (LLC-L AND LLC-G) [33] AND OUR LDMGI. IN THIS TABLE,
WE REPORT THE BEST ACC CORRESPONDING TO THE BEST OBJECTIVE VALUE FROM MULTIPLE RANDOM INITIALIZATIONS AND PARAMETERS

	K-means	DisKmeans	NCut	LLC-L	LLC-G	LDMGI
COIL-20	67.9	68.1	73.6	68.9	72.0	82.4
USPS	67.4	71.5	78.7	70.1	71.6	81.5
MNIST-T	56.6	50.4	68.2	66.1	68.5	72.8
MNIST-S	53.2	51.8	66.2	71.0	71.2	77.9
USF HumanID	36.9	40.8	42.9	42.6	40.3	43.5
UMIST	42.9	45.3	60.8	61.3	62.4	69.1
YALE-B	12.3	43.9	47.7	48.9	49.0	55.1
JAFFE	84.0	78.4	91.1	89.7	90.6	93.9
Pointing04	35.8	39.9	73.5	76.1	75.0	77.9
MPEG7	57.0	64.8	69.2	66.7	69.3	71.8

TABLE III

PERFORMANCE COMPARISON (NMI %) OF K-MEANS, DISKMEANS [38], NCUT [39], LLC (LLC-L AND LLC-G) [33] AND OUR LDMGI. IN THIS TABLE,
WE REPORT THE BEST NMI CORRESPONDING TO THE BEST OBJECTIVE VALUE FROM MULTIPLE RANDOM INITIALIZATIONS AND PARAMETERS

	K-means	DisKmeans	NCut	LLC-L	LLC-G	LDMGI
COIL-20	77.3	77.5	85.0	85.1	86.0	91.1
USPS	61.2	68.4	83.6	77.6	78.2	86.5
MNIST-T	50.3	48.4	68.4	61.3	64.2	69.2
MNIST-S	49.5	46.8	67.3	68.6	66.8	73.9
USF HumanID	68.9	72.6	75.2	74.8	72.6	76.1
UMIST	64.5	66.1	79.2	78.2	78.6	86.6
YALE-B	18.3	55.2	67.1	65.1	64.9	71.1
JAFFE	88.1	80.7	91.8	89.5	91.3	93.6
Pointing04	42.8	43.4	79.9	81.3	80.8	84.7
MPEG7	73.9	76.4	78.7	77.8	79.2	81.2

TABLE IV Performance Comparison (Mean ACC  $\pm$  Standard Deviation%) of K-Means, Diskmeans [38], NCut [39], LLC (LLC-L and LLC-G) [33] and our LDMGI. The Results Shown in Boldface Are Significantly Better Than the Others, With a Significance Level of 0.05

	K-means	DisKmeans	NCut	LLC-L	LLC-G	LDMGI
COIL-20	$59.2 \pm 3.8$	$53.5 \pm 6.1$	$68.3 \pm 5.3$	$63.1 \pm 3.3$	$67.5 \pm 5.3$	<b>75.3</b> ± 4.9
USPS	$64.9 \pm 3.6$	$69.4 \pm 3.7$	$73.4 \pm 6.3$	$66.6 \pm 3.1$	$70.1 \pm 3.9$	<b>80.5</b> ± 5.6
MNIST-T	$55.3 \pm 2.6$	$48.8 \pm 3.4$	$66.2 \pm 3.4$	$66.1 \pm 2.3$	$64.7 \pm 3.6$	<b>71.5</b> ± 3.5
MNIST-S	$53.0 \pm 4.1$	$48.6 \pm 5.6$	$64.5 \pm 2.0$	$66.7 \pm 3.4$	$68.2 \pm 4.5$	<b>76.3</b> ± 3.4
USF HumanID	$35.9 \pm 1.0$	$39.7 \pm 1.1$	<b>42.6</b> ± 0.4	$42.3 \pm 0.3$	$40.1 \pm 0.2$	<b>42.9</b> ± 0.5
UMIST	$42.7 \pm 2.5$	$43.0 \pm 3.2$	$60.1 \pm 0.7$	$59.6 \pm 1.7$	$59.4 \pm 3.2$	<b>67.0</b> ± 1.7
YALE-B	$11.3 \pm 0.7$	$41.1 \pm 3.1$	$46.2 \pm 1.5$	$48.5 \pm 0.6$	$46.7 \pm 0.6$	<b>55.0</b> ± 1.2
JAFFE	$71.3 \pm 10.7$	$75.6 \pm 9.4$	$83.9 \pm 6.5$	$82.8 \pm 6.8$	$79.7 \pm 5.6$	<b>90.4</b> ± 6.0
Pointing04	$35.2 \pm 1.5$	$36.3 \pm 4.2$	$70.6 \pm 3.2$	$72.9 \pm 3.3$	$70.2 \pm 2.9$	<b>77.2</b> ± 1.9
MPEG7	$56.5 \pm 4.1$	$58.4 \pm 3.9$	$66.9 \pm 1.8$	$64.0 \pm 2.2$	$65.9 \pm 2.0$	<b>68.0</b> $\pm$ 3.2

and our LDMGI, we also find the best results for each parameter corresponding to the best objective values from twenty rounds of random initializations. To compare the parameter sensitivity of different algorithms, we plot the performance variations of these algorithms with different parameters in Fig. 1 (*resp.* Fig. 2) in terms of ACC (*resp.* NMI). For each clustering algorithm, we also calculate the the mean ACC (*resp.* NMI) from twenty rounds of random initializations for each parameter and then we additionally report the best mean ACC (*resp.* NMI) together with the standard deviation corresponding to the optimal parameter in Table IV (*resp.* Table V). A significance test is conducted with the significance level of 0.05 and the results are also re-

ported in Tables IV and V. From these results, we have the following observations.

- 1) When comparing two global clustering approaches (i.e., Kmeans and DisKmeans), we find that DisKmeans is generally better than K-means, which demonstrates that the utilization of discriminant information is useful to improve the image clustering performance. We also observe that ACC (resp. NMI) on Yale-B database is significantly improved from 12.3 (resp. 18.3) to 43.9 (resp. 55.2) by using DisKmeans instead of Kmeans.
- 2) Three local clustering approaches (i.e., NCut [39], LLC (LLC-L and LLC-G) [33] and our LDMGI) are gener-

Authorized licensed use limited to: University of Melbourne. Downloaded on November 29,2023 at 10:09:31 UTC from IEEE Xplore. Restrictions apply.

TABLE V
Performance Comparison (Mean NMI ± Standard Deviation%) of K-Means, Diskmeans [38], NCut [39], LLC (LLC-L and LLC-G) [33] and
OUR LDMGI. THE RESULTS SHOWN IN BOLDFACE ARE SIGNIFICANTLY BETTER THAN THE OTHERS, WITH A SIGNIFICANCE LEVEL OF 0.05

	K-means	DisKmeans	NCut	LLC-L	LLC-G	LDMGI
COIL-20	$74.5 \pm 2.1$	$70.5 \pm 3.2$	$82.3 \pm 2.4$	$83.5 \pm 0.8$	$85.3 \pm 0.5$	<b>90.0</b> ± 0.7
USPS	$60.6 \pm 1.2$	$67.6 \pm 1.6$	$82.4 \pm 1.9$	$76.4 \pm 1.5$	$76.8 \pm 1.5$	<b>86.1</b> ± 2.3
MNIST-T	$49.3 \pm 1.0$	$45.7 \pm 2.0$	$67.4 \pm 1.4$	$61.2 \pm 1.3$	$62.4 \pm 1.6$	<b>68.9</b> ± 1.5
MNIST-S	$48.5 \pm 2.0$	$44.8 \pm 4.0$	$66.6 \pm 1.0$	$67.9 \pm 1.4$	$65.1 \pm 2.8$	<b>73.9</b> ± 1.5
USF HumanID	$67.8 \pm 0.6$	$70.5 \pm 0.7$	<b>75.1</b> $\pm$ 0.1	<b>74.6</b> ± 0.1	$72.5 \pm 0.1$	<b>75.9</b> $\pm$ 0.2
UMIST	$63.5 \pm 2.5$	$63.6 \pm 2.6$	$79.1 \pm 0.6$	$76.2 \pm 1.1$	$76.2 \pm 1.3$	<b>84.5</b> ± 1.0
YALE-B	$17.8 \pm 0.1$	$52.0 \pm 3.1$	$66.6 \pm 0.6$	$64.6 \pm 0.5$	$65.8 \pm 0.1$	<b>70.8</b> $\pm$ 0.5
JAFFE	$79.2 \pm 6.7$	$79.7 \pm 6.2$	$90.6 \pm 1.0$	$88.7 \pm 0.7$	$89.6 \pm 0.6$	<b>92.6</b> ± 1.4
Pointing04	$41.9 \pm 1.0$	$40.0 \pm 4.4$	$79.2 \pm 1.2$	$79.6 \pm 1.7$	$78.6 \pm 1.5$	<b>84.2</b> ± 0.1
MPEG7	$72.7 \pm 1.9$	$73.7 \pm 2.0$	$78.5 \pm 0.3$	$77.1 \pm 0.6$	$78.0 \pm 0.7$	<b>80.3</b> ± 0.4

ally better than K-means and DisKmeans. It demonstrates that NCut, LLC and LDMGI can effectively make use of the essential manifold structure of the images which is not considered in the global clustering methods K-means and DisKmeans. This observation confirms that local data structural information is crucial for image clustering.

- 3) NCut outperforms LLC-G (or LLC-L) on some databases and NCut is worse than LLC-G (or LLC-L) on other databases. In other words, there is no consistent winner. We also observe that LLC-G is generally better than LLC-L, possibly owing to the utilization of nonlinear kernel function in the local regression model.
- 4) From Tables II and III, we observe that our method LDMGI achieves the best results over all the 10 datasets in terms of ACC and NMI. As shown in Tables IV and V, LDMGI also outperforms K-means, DisKmeans, NCut [39], LLC (LLC-L and LLC-G) in terms of mean ACC and NMI over all the 10 databases. Judged by the t-test (with a significance level of 0.05), LDMGI is significantly better than K-means, DisKmeans, NCut, LLC (LLC-L and LLC-G) in 9 out of the 10 databases. These results demonstrate that LDMGI can effectively utilize local manifold structure as well as the discriminant information for image clustering.
- 5) Except for the simplest clustering algorithm K-means, one parameter needs to be set beforehand for other clustering algorithms (i.e.,  $\gamma$  in (28) for DisKmeans,  $\eta$  in (33) for LLC,  $\sigma$  in (32) for NCut, and  $\lambda$  in (15) for our LDMGI). From Figs. 1 and 2, we observe that DisKmeans and NCut are more sensitive to their parameters. Our observation that NCut is sensitive to the bandwidth parameter is consistent with the prior work [32].
- 6) From Figs. 1 and 2, we also observe that LDMGI is more robust to the algorithmic parameter λ, when compared with NCut [27], LLC-G [33] and DisKmeans [38]. A possible reason is that our LDMGI learns a Laplacian matrix for data clustering during which both local data structural information and discriminant information are used. In real applications, ground truth is generally not available for tuning the parameters of clustering algorithms. Thus, LDMGI is more suitable for real image clustering applications because LDMGI is not only more accurate but also more stable to the algorithmic parameter.

7) For all the clustering algorithms, we also observe that the ACCs in Table II (*resp.* NMIs in Table III) corresponding to the best objective values are generally higher than the mean ACCs in Table IV (*resp.* the mean NMIs in Table V). Since it is still a nontrivial task to obtain the globally optimal solutions for the clustering algorithms, it is reasonable to choose the clustering results from the optimal initialization corresponding to the best objective values in practical clustering applications.

Discussions About Features: Pose, illumination and expression are three major challenges in face recognition. Therefore, the clustering performances on the UMINST database [13] (with strong pose variation) and Yale-B database [9] (with significant illumination variation) using the low-level gray-scale intensity features are relatively poor, when compared with the results on other databases. The explanation is the extracted gray-scale intensity features are not discriminant enough to effectively group face images into different subjects in these cases. Similarly, it has been reported that human identification performance on the USF HumanID database [25] is also poor using the gray-scale intensity features extracted from average silhouette images when the images are captured from different types of surfaces (e.g., grass and concrete) [25]. One can employ more discriminant features to improve the clustering performance.

Here, we take the UMIST face database as an example to test the clustering performance using Gabor features [34]. We extracted 40 Gabor features with five different scales and eight different orientations [34], so each image is then represented as a 25760-dimensional feature vector. We additionally take the MPEG7 shape image database as another example to test the clustering performance by directly using the gray-scale intensity values as features. Specifically, the size of each shape image is  $60 \times 100$ . Again, we independently perform all the clustering algorithms 20 times with random initializations. We report the clustering results corresponding to the best objective values in Table VI and report the mean ACC and NMI together with the standard deviation in Table VII. The performance variations of NCut, LLC-G, DisKmeans and our LDMGI with different parameters are shown in Fig. 3. In Table VI, Table VII and Fig. 3, we refer to the results on UMIST and MPEG7 shape image databases as UMIST-Gabor and MPEG7-Gray in order

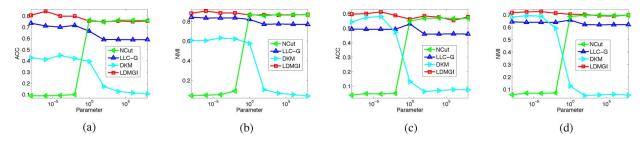


Fig. 3. ACC and NMI variations of NCut [39], LLC-G [33], DisKmeans (DKM) [38] and our LDMGI with different parameters. (a) UMIST-Gabor (ACC), (b) UMIST-Gabor (NMI), (c) MPEG7-Gray (ACC), (d) MPEG7-Gray (NMI).

## TABLE VI PERFORMANCE COMPARISON (ACC AND NMI %) OF K-MEANS, DISKMEANS [38], NCUT [39], LLC (LLC-L AND LLC-G) [33] AND LDMGI. IN THIS TABLE, WE REPORT THE BEST ACC AND NMI CORRESPONDING TO THE BEST OBJECTIVE VALUE FROM MULTIPLE RANDOM INITIALIZATIONS AND PARAMETERS

	K-means	DisKmeans	NCut	LLC-L	LLC-G	LDMGI
UMIST-Gabor (ACC)	41.7	44.9	76.4	68.5	73.6	84.0
UMIST-Gabor (NMI)	61.2	63.2	87.1	77.7	84.4	90.4
MPEG7-Gray (ACC)	55.5	58.2	57.2	57.3	53.6	61.2
MPEG7-Gray (NMI)	68.7	68.9	69.7	69.8	65.9	72.6

#### TABLE VII

PERFORMANCE COMPARISON (MEAN ACC AND NMI  $\pm$  STANDARD DEVIATION %) OF K-MEANS, DISKMEANS [38], NCUT [39], LLC (LLC-L AND LLC-G) [33] AND LDMGI. THE RESULTS IN BOLDFACE ARE SIGNIFICANTLY BETTER THAN THE OTHERS, WITH A SIGNIFICANCE LEVEL OF 0.05

	K-means	DisKmeans	NCut	LLC-L	LLC-G	LDMGI
UMIST-Gabor (ACC)	$41.2 \pm 2.7$	$41.6 \pm 2.4$	$73.3 \pm 1.9$	$68.2 \pm 1.9$	$72.1 \pm 2.7$	<b>78.7</b> ± 3.1
UMIST-Gabor (NMI)	$57.9 \pm 2.6$	$58.4 \pm 2.4$	$85.6 \pm 0.8$	$77.6 \pm 1.0$	$84.1 \pm 0.6$	<b>87.5</b> ± 1.4
MPEG7-Gray (ACC)	$49.7 \pm 4.2$	$51.3 \pm 3.6$	$56.5 \pm 1.3$	$55.9 \pm 1.2$	$56.5 \pm 1.3$	<b>58.1</b> ± 1.9
MPEG7-Gray (NMI)	$64.5 \pm 2.8$	$65.6 \pm 2.1$	$69.5 \pm 0.2$	$69.4 \pm 0.5$	$69.5 \pm 0.2$	<b>71.6</b> ± 0.9

to distinguish the new results and the previous results shown in Tables II –V, and Figs. 1 and 2.

The clustering performances of most of the algorithms on the UMIST database are improved by using Gabor features. Similarly, we also observe the clustering performances of most of the methods degrade on the MPEG7 shape image database by using the gray-scale intensity features, when compared with the features obtained by using MDS method based upon the pairwise distances calculated with shape context algorithm [2]. Therefore, features are another important factor for image clustering and it is crucial to use discriminant features in real image clustering applications. However, the design of discriminant features is data-dependent and, thus, it is out of the scope of this work. It is worth mentioning again that our method LDMGI still achieves the best results using alternative features and it is also more stable to the algorithmic parameter  $\lambda$ . Moreover, judged by the t-test (with a significance level of 0.05), LDMGI is also significantly better than other methods (see Table VII).

a new clustering algorithm, referred to as Clustering with Local Discriminant Models and Global Integrations (LDMGI). For each data point, we consider a local clique comprising this data point and its neighboring data points. A local discriminant model is used to measure the clustering performance of samples in each local clique. To globally integrate the local models from all the cliques, we further propose a unified objective function. We observe that LDMGI shares a similar objective function as SC algorithms (e.g., NCut). Thus, the optimal cluster assignment matrix can be obtained by employing spectral relaxation and spectral rotation. Moreover, the connections between LDMGI and other existing clustering algorithms are theoretically discussed. Our experiments demonstrate that LDMGI outperforms other existing clustering methods and LDMGI is also more robust to algorithmic parameter, when compared with NCut. In the future, we will investigate how to extract more discriminant image features to further improve the clustering performance as well as study how to automatically determine the optimal parameters for LDMGI.

#### V. CONCLUSION

#### ACKNOWLEDGMENT

Observing that discriminant information and manifold information are both crucial for image clustering, we have proposed

The authors would like to thank Dr. M. Wu for his helpful discussions.

#### REFERENCES

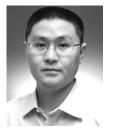
- M. Belkin and P. Niyogi, "Laplacian eigenmaps for dimensionality reduction and data representation," *Neural Comput.*, vol. 15, no. 6, pp. 1373–1396, 2002.
- [2] S. Belongie, J. Malik, and J. Puzicha, "Shape matching and object recognition using shape contexts," *IEEE Trans. Pattern Anal. Mach. Intell.*, vol. 24, no. 4, pp. 509–522, Apr. 2002.
- [3] M. Bicego and V. Murino, "Similarity-based classification of sequences using hidden Markov models," *Pattern Recognit.*, vol. 37, no. 12, pp. 2281–2291, 2004.
- [4] Y. Chen, J. Wang, and R. Krovetz, "Clue: Cluster-based retrieval of images by unsupervised learning," *IEEE Trans. Image Process.*, vol. 14, no. 8, pp. 1187–1201, Aug. 2005.
- [5] H. Chris, Q. Ding, and T. Li, "Adaptive dimension reduction using discriminant analysis and k-means clustering," in *Proc. Int. Conf. Machine Learning*, 2007, pp. 521–528.
- [6] R. Datta, D. Joshi, J. Li, and J. Wang, "Image retrieval: Ideas, influences, and trends of the new age," ACM Comput. Surv., vol. 40, no. 2, 2008.
- [7] I. Dhillon, Y. Guan, and B. Kulis, "Kernel kmeans, spectral clustering and normalized cuts," in *Proc. ACM SIGKDD Conf. Knowledge Dis*covery Data Mining, 2004, pp. 551–556.
- [8] K. Fukunaga, Introduction to Statistical Pattern Recognition, 2nd ed. San Diego, CA: Academic, 1990.
- [9] A. Georghiades, P. Belhumeur, and D. Kriegman, "From few to many: Illumination cone models for face recognition under variable lighting and pose," *IEEE Trans. Pattern Anal. Mach. Intell.*, vol. 23, no. 6, pp. 643–660, Jun. 2001.
- [10] J. Goldberger, S. Gordon, and H. Greenspan, "Unsupervised image-set clustering using an information theoretic framework," *IEEE Trans. Image Process.*, vol. 15, no. 2, pp. 449–458, Feb. 2006.
- [11] S. Gordon, H. Greenspan, and J. Goldberger, "Applying the information bottleneck principle to unsupervised clustering of discrete and continuous image representations," in *Proc. IEEE Int. Conf. Computer Vision*, 2003, pp. 370–377.
- [12] N. Gourier, D. Hall, and J. Crowley, "Estimating face orientation from robust detection of salient facial features," in *Proc. ICPR Workshop on Visual Observation of Deictic Gestures*, 2004.
- [13] D. Graham and N. Allinson, Web Site of Umist Multi-View Face Database [Online]. Available: http://images.ee.umist.ac.uk/danny/database. html image engineering and neural computing lab, umist, uk.
- [14] Y. Huang, D. Xu, and T. J. Cham, "Face and human gait recognition using image-to-class distance," *IEEE Trans. Circuits Syst. Video Technol.*, vol. 20, no. 3, pp. 431–438, Mar. 2010.
- [15] J. Jia, N. Yu, and X. Hua, "Annotating personal albums via web mining," ACM Multimedia, pp. 459–468, 2008.
- [16] L. Kennedy and M. Naaman, "Generating diverse and representative image search results for landmarks," in *Proc. Int. World Wide Web Conf.*, 2008, pp. 297–306.
- [17] Y. LeCun, L. Bottou, Y. Bengio, and P. Haffner, "Gradient-based learning applied to document recognition," *Proc. IEEE*, vol. 86, no. 11, pp. 2278–2324, Nov. 1998.
- [18] J. Li, "Two-scale image retrieval with significant meta-information feedback," ACM Multimedia, pp. 499–502, 2005.
- [19] J. Li and J. Z. Wang, "Real-time computerized annotation of pictures," ACM Multimedia, pp. 911–920, 2006.
- [20] M. Lyons, J. Budynek, and S. Akamatsu, "Automatic classification of single facial images," *IEEE Trans. Pattern Anal. Mach. Intell.*, vol. 21, no. 12, pp. 1357–1362, Dec. 1999.
- [21] S. Nene, S. Nayar, and H. Murase, Columbia Object Image Library (Coil-20) Tech. Rep. CUCS-005-96, 1996.
- [22] A. Ng, M. Jordan, and Y. Weiss, "On spectral clustering: Analysis and an algorithm," in *Proc. NIPS*, 2001, pp. 849–856.
- [23] C. Papadimitriou and K. Steiglitz, Combinatorial Optimization: Algorithms and Complexity. New York: Dover, 1998.
- [24] F. Samaria and A. Harter, "Parameterisation of a stochastic model for human face identification," in *Proc. IEEE Workshop on Applications of Computer Vision*, 1994, pp. 138–142.
- [25] S. Sarkar, P. Phillips, Z. Liu, I. Vega, P. Grother, and K. Bowyer, "The humanid gait challenge problem: Data sets, performance, and analysis," *IEEE Trans. Pattern Anal. Mach. Intell.*, vol. 27, no. 2, pp. 162–177, Feb. 2005.

- [26] L. Saul and S. Roweis, "Think globally, fit locally: Unsupervised learning of low dimensional manifolds," J. Mach. Learn. Res., vol. 4, pp. 119–155, 2003.
- [27] J. Shi and J. Malik, "Normalized cuts and image segmentation," *IEEE Trans. Pattern Anal. Mach. Intell.*, vol. 22, no. 8, pp. 888–905, Aug. 2000
- [28] I. Simon, N. Snavely, and S. Seitz, "Scene summarization for online image collections," in *Proc. IEEE Int. Conf. Computer Vision*, 2007, vol. 1–8.
- [29] A. Strehl and J. Ghosh, "Cluster ensembles—A knowledge reuse framework for combining multiple partitions," J. Mach. Learn. Res., vol. 3, pp. 583–617, 2002.
- [30] N. Thakoor, J. Gao, and S. Jung, "Hidden Markov model-based weighted likelihood discriminant for 2-D shape classification," *IEEE Trans. Image Process.*, vol. 16, no. 11, pp. 2707–2719, Nov. 2007.
- [31] F. D. Torre and T. Kanade, "Discriminative cluster analysis," in *Proc. Int. Conf. Machine Learning*, 2006, pp. 241–248.
- [32] F. Wang and C. Zhang, "Label propagation through linear neighbor-hoods," *IEEE Trans. Knowl. Data Eng.*, vol. 20, no. 1, pp. 55–67, Jan. 2008.
- [33] M. Wu and B. Schölkopf, "A local learning approach for clustering," in *Proc. NIPS*, 2006, pp. 1529–1536.
- [34] D. Xu, S. Yan, L. Zhang, S. Lin, H. Zhang, and T. Huang, "Reconstruction and recognition of tensor-based objects with concurrent subspaces analysis," *IEEE Trans. Circuits Syst. Video Technol.*, vol. 18, no. 1, pp. 36–47, 2008.
- [35] D. Xu, S. Yan, D. Tao, S. Lin, and H. Zhang, "Marginal fisher analysis and its variants for human gait recognition and content based image retrieval," *IEEE Trans. Image Process.*, vol. 16, no. 11, pp. 2811–2821, Nov. 2007.
- [36] H. Xu, D. Yu, D. Xu, and A. Zhang, "Ss-clustertree: A subspace clustering based indexing algorithm over high-dimensional image features," in *Proc. Int. Conf. Image and Video Retrieval*, 2008, pp. 95–104.
- [37] Y. Yang, D. Xu, F. Nie, J. Luo, and Y. Zhuang, "Ranking with local regression and global alignment for cross media retrieval," ACM Multimedia, 2009.
- [38] J. Ye, Z. Zhao, and M. Wu, "Discriminative k-means for clustering," Neural Inf. Process. Syst., pp. 1649–1656, 2008.
- [39] S. X. Yu and J. Shi, "Multiclass spectral clustering," in *Proc. Int. Conf. Computer Vision*, 2003, pp. 313–319.
- [40] H. Zha, X. He, C. Ding, M. Gu, and H. Simon, "Spectral relaxation for k-means clustering," in *Proc. NIPS*, 2001, pp. 1057–1064.



Yi Yang received the B.S. degree from Zhejiang University, Hangzhou, China in 2003 and is currently pursuing the Ph.D. degree from the College of Computer Science, Zhejiang University.

His research interests include data mining, machine learning and their applications to multimedia content analysis, information retrieval, and computer vision.



**Dong Xu** (M'07) received the B.Eng. and Ph.D. degrees from the Electronic Engineering and Information Science Department, University of Science and Technology of China, Hefei, China, in 2001 and 2005, respectively.

He is currently an Assistant Professor with Nanyang Technological University, Singapore. During his Ph.D. studies, he worked with Microsoft Research Asia and The Chinese University of Hong Kong. He also spent one year at Columbia University, New York, as a Postdoctoral Research Scientist.

He was co-author (with his Ph.D. student Lixin Duan) of a paper that won the Best Student Paper Award in the IEEE International Conference on Computer Vision and Pattern Recognition 2010. His research interests include computer vision, machine learning, and multimedia content analysis.



**Feiping Nie** received the B.S. degree in computer science from North China University of Water Conservancy and Electric Power, China, in 2000, the M.S. degree in computer science from Lanzhou University, Lanzhou, China in 2003, and the Ph.D. degree in computer science from Tsinghua University, Beijing, China, in 2009.

His research interests include machine learning, pattern recognition, data mining, and image processing.



Yueting Zhuang received the B.S., M.S., and Ph.D. degrees from Zhejiang University, Hangzhou, China. He is now a professor at College of Computer Science, Zhejiang University. His research interests include multimedia database, artificial intelligence, and

video based animation.



**Shuicheng Yan** (M'06–SM'09) received the Ph.D. degree from the School of Mathematical Sciences, Peking University, in 2004.

He spent three years as Postdoctoral Fellow at the Chinese University of Hong Kong and then at the University of Illinois at Urbana-Champaign, Urbana, and he is currently an Assistant Professor in the Department of Electrical and Computer Engineering at National University of Singapore. In recent years, his research interests have focused on computer vision (biometrics, surveillance, and internet vision), mul-

timedia (video event analysis, image annotation, and media search), machine learning (feature extraction, sparsity/non-negativity analysis, large-scale machine learning), and medical image analysis. He has authored or coauthored over 140 technical papers over a wide range of research topics.

Dr. Yan has served on the editorial board of the *International Journal of Computer Mathematics*, as guest editor of a special issue of *Pattern Recognition Letters*, and as a guest editor of a special issue of *Computer Vision and Image Understanding*. He has served as Co-Chair of the IEEE International Workshop on Video-oriented Object and Event Classification (VOEC'09) held in conjunction with ICCV'09. He is the special session chair of the Pacific-Rim Symposium on Image and Video Technology 2010. He is an Associate Editor of IEEE TRANSACTIONS ON CIRCUITS AND SYSTEMS FOR VIDEO TECHNOLOGY.