Свойства регулярных выражений

1.
$$a ... a = a^n$$

$$n$$
 раз

2.
$$a \cdot a^n = aa^n = a^n a = a^{n+1}$$

3.
$$a^n a^m = a^{n+m}$$

4.
$$a + a = a$$

5.
$$aa^* = a^*a = a^+$$

6.
$$a + a^* = a^*$$

7.
$$a + a^+ = a^+$$

8.
$$a^n + a^+ = a^+$$

9.
$$a^n + a^* = a^*$$

10.
$$a^+ + a^* = a^*$$

11.
$$a^+ + \varepsilon = a^*$$

12.
$$a^n a^* = a^{n-1} a a^* = a^{n-1} a^+ = (a^+)^n$$

13.
$$a^n a^+ = (a^+)^{n+1}$$

14.
$$a^*a^+ = a^+a^* = a^*$$

15.
$$a\varepsilon = \varepsilon a = a$$

16.
$$(a^+)^* = (a^*)^* = a^*$$

17.
$$ab c = a bc = abc$$

18.
$$a + b + c = a + b + c = a + b + c$$

19.
$$a + b c = ac + bc$$

20.
$$a + c^* = a + \varepsilon + c^+ = a + \varepsilon + c^*$$

21.
$$a^+ + b^* = a^* + b^+ = a^* + b^*$$

22.
$$a(ba)*b = (ab)*$$

23.
$$a(ba)^*b + \varepsilon = (ab)^*$$

24.
$$a(ba)^+b = ab \ ab \ ^+ = ((ab)^+)^2$$

25.
$$a + b*a = b*a$$

26.
$$a + ab^* = ab^*$$

27.
$$(a+b)^* = (a^*b^*)^* = (a^*b)^*a^* = (a^++b)^* = (a+b^+)^* = (a^*+b^*)^* = (a^*+b)^* = (a^*+b)^* = (a^*+b)^* = (a^*+b)^* = (a^*+b)^*b^* = a^*(a+b)^*b^*$$

28.
$$a(a+b)^* = (ab^*)^+ = (a^+b^*)^+$$

29.
$$(a + b)*b = (a*b)* = (a*b*)*$$

30.
$$(a+b)^+ = (a^+b^*)^+ + (a^*b^+)^+ = (ab^*)^+ + (a^*b)^+$$