## Financial Engineering MA374 Lab – 03

Submitted by –

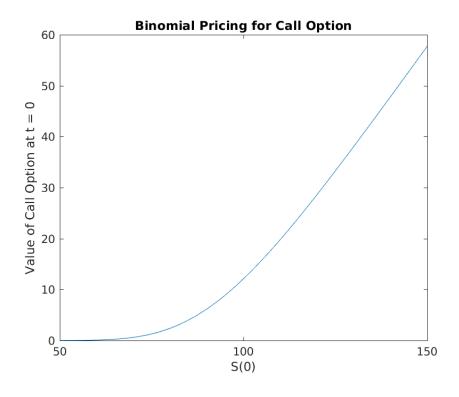
Ashish Kumar Poddar

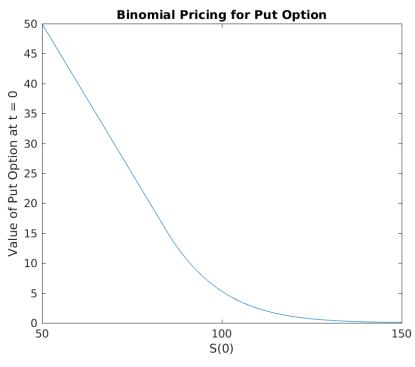
Roll No. – 150123049

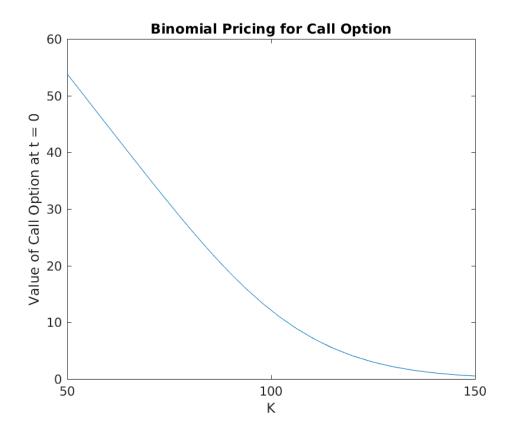
Date – 5<sup>th</sup> February, 2018

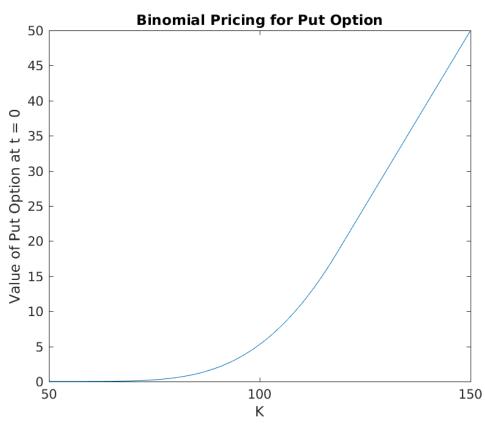
## Question 1

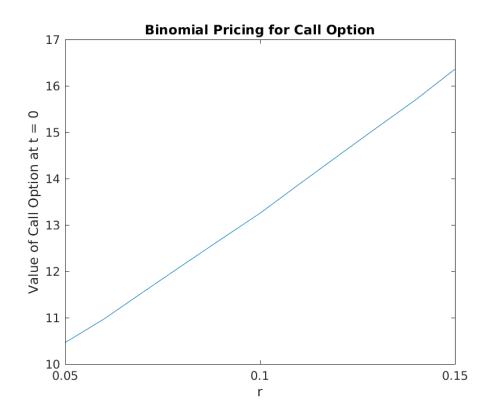
We needed to find the initial values of the American Call and Put options for different values of the variables and here are the results.

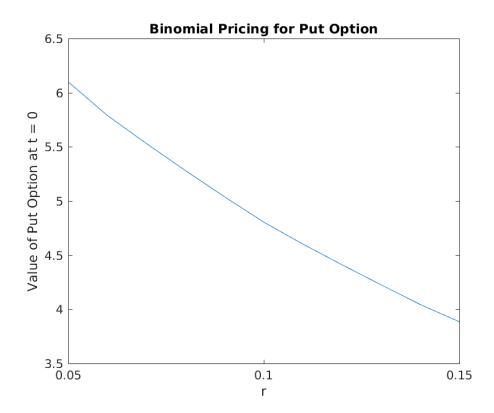


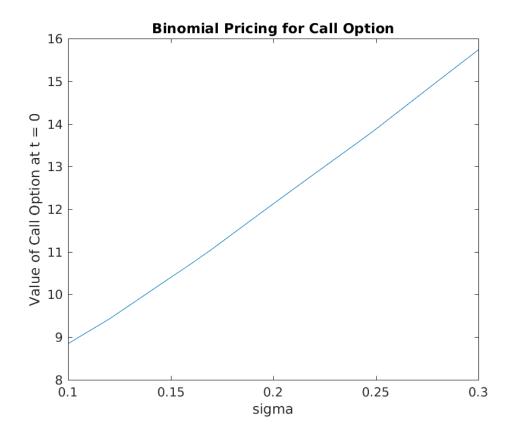


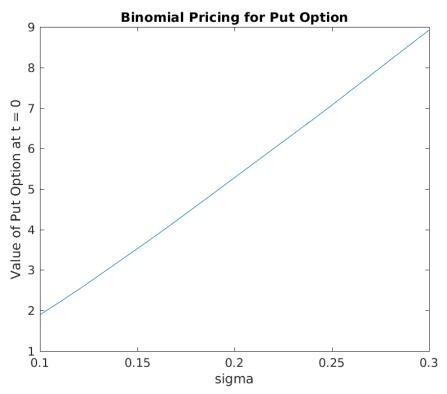


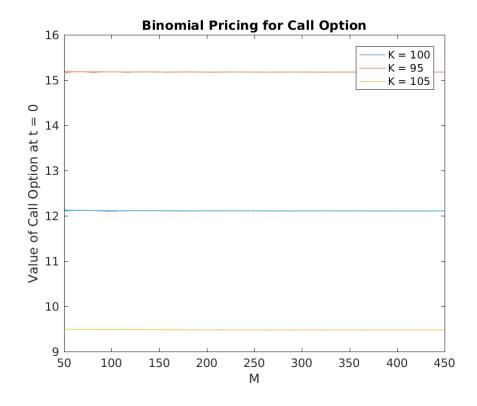


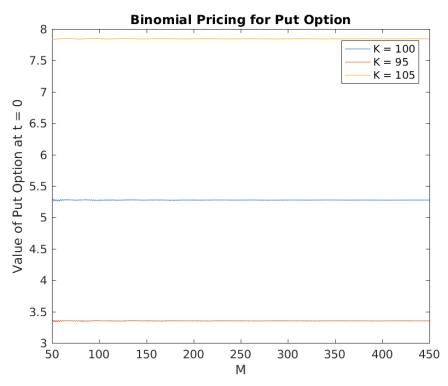












## Question 2

The initial value of the lookback option for M = 5 and M = 10 are 9.1193 and 10.0806 respectively. For M = 25 and M = 50, we are unable to run the program using this method due to computational time problems.

The initial value is increasing with increasing value of M here based on the two values obtained.

9.119299	9.027951	8.548076	7.416771	5.501639	0
0	9.50484	9.799119	9.955271	9.571392	11.18141
0	0	7.147916	6.201916	4.60048	0
0	0	12.16866	13.71286	15.63185	19.45269
0	0	0	6.201916	4.60048	0
0	0	0	8.324615	8.003614	9.349917
0	0	0	7.148418	6.680843	6.374517
0	0	0	17.58206	21.18809	25.39456
0	0	0	0	4.60048	0
0	0	0	0	8.003614	9.349917
0	0	0	0	3.846929	0
0	0	0	0	13.07138	16.26637
0	0	0	0	3.846929	0
0	0	0	0	10.6809	13.578
0	0	0	0	10.6809	13.578
0	0	0	0	25.05123	29.4826
0	0	0	0	0	0
0	0	0	0	0	9.349917
0	0	0	0	0	0
0	0	0	0	0	16.26637
0	0	0	0	0	0
0	0	0	0	0	7.818416
0	0	0	0	0	5.330382
0	0	0	0	0	21.23498
0	0	0	0	0	0
0	0	0	0	0	7.818416
0	0	0	0	0	2.90135
0	0	0	0	0	18.80595
0	0	0	0	0	2.90135
0	0	0	0	0	18.80595
0	0	0	0	0	18.80595
0	0	0	0	0	32.10539

## Question 3

The initial value of the lookback option for M = 5, 10, 25 and 50 are 9.1193, 10.0806, 11.0035 and 11.5109 respectively.

The initial value is increasing with increasing value of M.

For M = 5, the values are -

166.06574787682462, 166.06574787682462) :0.0 150.04587225655362, 138.86445913876912) 11.181413117784501 150.04587225655362, 150.04587225655362) 5.501638813873981 138.8644591387691, 138.8644591387691) :0.0 135.57138705044142, 116.118695507311) :19.452691543130413 135.57138705044142, 125.46861206060268) :9.57139153170023 135.57138705044142, 135.57138705044142) 7.416771005131012 125.46861206060268, 116.118695507311) :9.349916553291678 125.46861206060268, 125.46861206060268) 4.600479677676438 122.49321297792528, 116.11869550731102) 6.374517470614265 122.49321297792528, 97.09864950286031) :25.39456347506497 122.49321297792528, 113.3650230595177) :9.95527127295782 122.49321297792528, 122.49321297792528) 8.548076183576446 116.11869550731102, 116.11869550731102) :0.0 113.3650230595177, 97.09864950286031) :16.266373556657385 113.3650230595177, 104.91706553244704) :8.003613780975444 113.3650230595177, 113.3650230595177) :6.201916453882752 110.676651999383, 97.09864950286031) :13.578002496522686 110.676651999383, 104.91706553244704) :6.680842999256647
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