## Bayesian Networks for Recommender Systems:

Going Beyond Ratings Prediction with "Most Relevant Explanation"

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COLLEGE OF BUSINESS

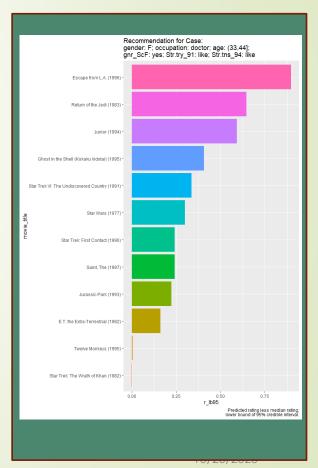
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## Background

### **Case Profile**



### Recommendation

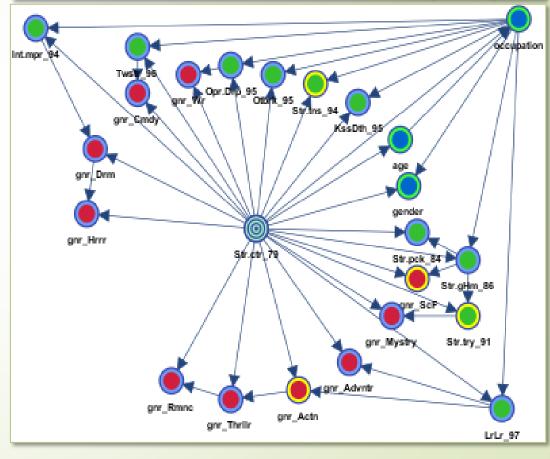


### Approach: Build Ensemble of Bayesian Networks

- $\blacksquare$  Build BBN for each movie,  $m_i$ 
  - Tree-Augmented Naïve Bayes (TANB): Highly confirming/refuting other movies, Viewer & Movie Features
    - Avoids giant BBN containing all movies with either
       (a) limited connection to Viewer & Movie features –
       limiting their predictive value or
       (b) excessive connections to Viewer & Movie features –
       resulting in intractable inference
  - All movie nodes, including target, have states equal to Viewer Ratings (5-star scale)

    centered on each Viewer's median rating
- Exploit parallel processing

## Bayesian Belief Network (BBN) for "Star Trek: The Motion Picture (1979)"



# Approach: Selecting Nodes for Each BBN Generalized Bayes Factor & Weight of Evidence

Generalized Bayes Factor, GBF(H:E)
Rank order candidate movies as Evidence E given Hypotheses H\*=Like Target Movie

Find F to Maximize:  $GBF(H^* : E) = \frac{Odds(H = Like Target Movie | E = Like Candidate Movie)}{Odds(H = Like Target Movie)}$   $= \frac{P(E = Like Candidate Movie | H = Like Target Movie)}{P(E = Like Candidate Movie | H = Like Target Movie)}$ 

 $P(E=Like\ Candidate\ Movie\ |\ H'\ \neq Like\ Target\ Movie)$ 

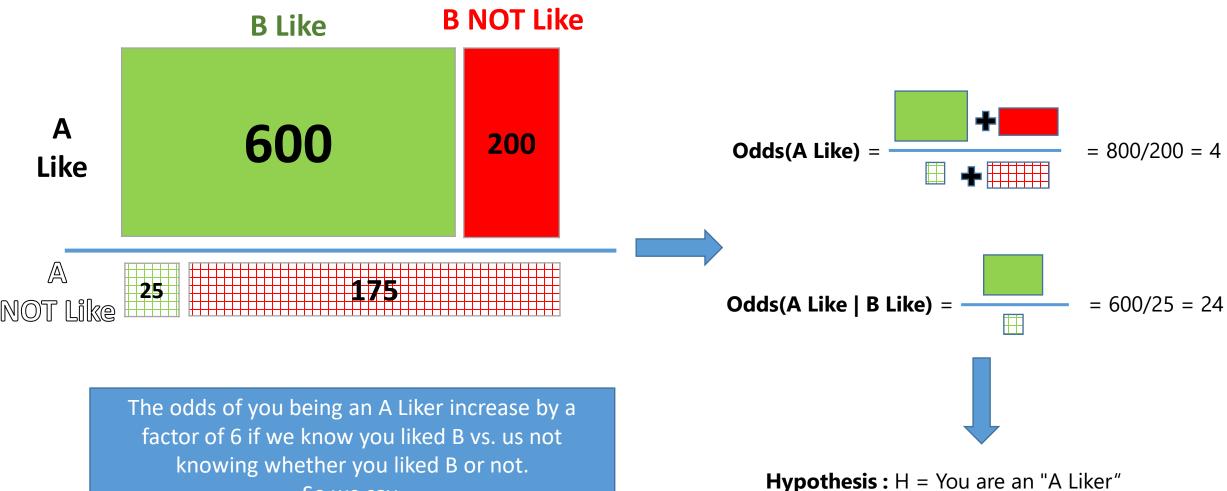
Weight of Evidence is the logarithm of GBF

W(H\*: E) =  $\log_2 GBF(H^*: E)$ ; in decibans: W(H\*: E) =  $\mathbf{10} \times \log_{10} GBF(H^*: E)$ 

- ► Kass & Raftery: evidence provides substantial support if W(H:E) > 5 decibans = 1.66 bits
- ■I.J. Good: a person can only discern  $\Delta W > 1$  deciban = 0.33 bits
- Build TANB: nodes for candidate movies w/top 10 | W(H:E) |

Finds movies either disproportionately liked or disliked

#### Example: Total = 1000 viewers, Movie A (pattern), Movie B (color)



"The observation 'Like B' is strong confirmatory evidence for the hypothesis 'Like A'."

Evidence: E = You are a "B Liker"

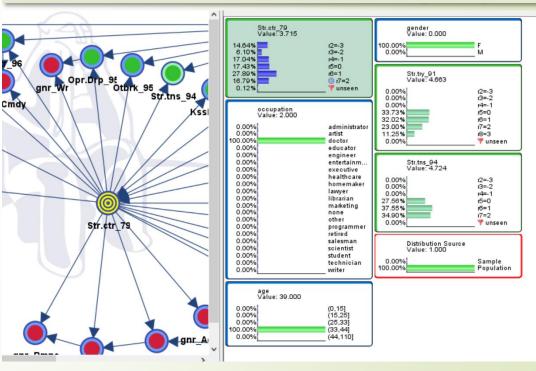
GBF(H:E) = Odds(H | E) / Odds(H) = 24/4 = 6

W(H:E) = 2.6 bits = 7.8 decibans.

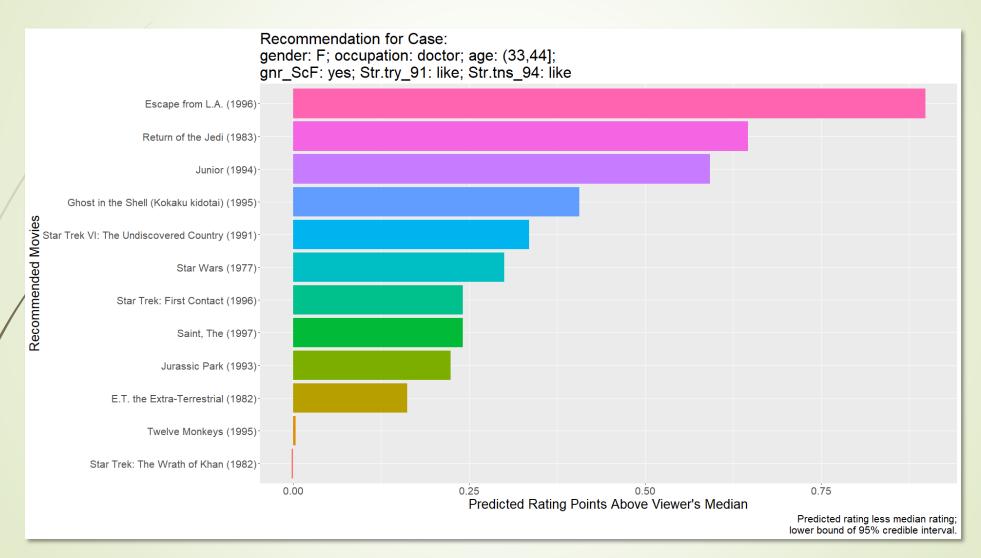
### Approach: Recommend Movies

- Apply Bayesian Inference
  - Compute posterior: P(Rating  $m_i$  | Case Profile,  $m_i$  Seen)  $\forall m_i$
  - Rank movies by largest to smallest  $\frac{Score(m_i) = Lower-Bound-of-95\%-Credible-Interval}{Score(m_i)}$
- Exploit parallel processing

## Bayesian Belief Network (BBN) for "Star Trek: The Motion Picture (1979)"

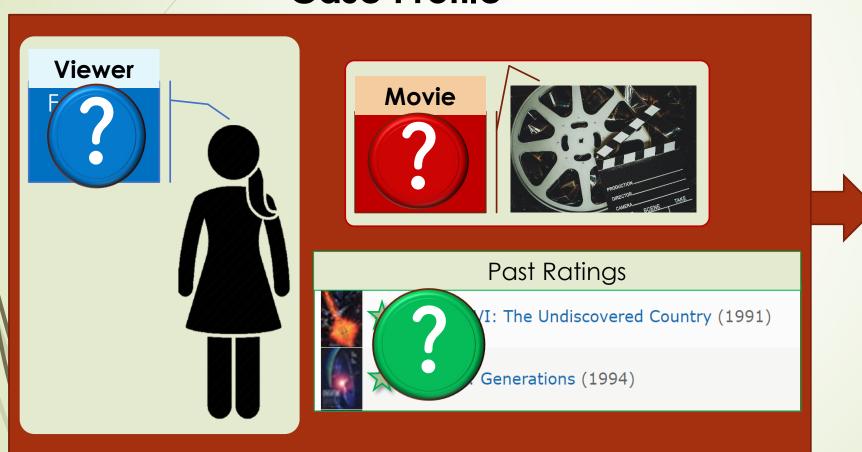


## Approach: Recommend Movies



## Ratings Prediction under Incomplete Information

### **Case Profile**



### Recommendation

#### **CAVEATS:**

Database sample is sparse & biased

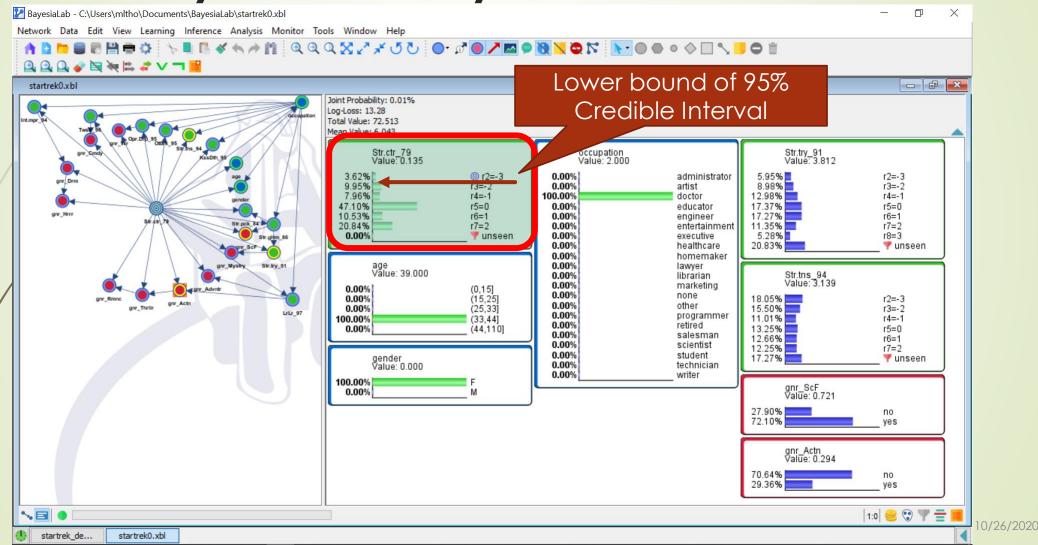
it is not representative of the US population w.r.t. gender, age, occupation.

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## **Issues: Sparsity & Bias**

- Sparsity Sample does not capture enough people within many of the gender-age-occupation cohorts
  - Account for uncertainty by leveraging posterior distribution in forming recommendation rankings ->
     Use Lower-Bound-of-95%-Credible-Interval as metric for ranking movies
  - Also: Aggregation of states; Prior distributions on conditional probability tables (CPTs)
- Bias Sample proportions of gender-age-occupation cohorts differ greatly from those in the target population to which we wish to apply our models
  - Account for non-representativeness by applying post-stratification to aggregate predictions marginalized over the user features → Use Evidence Instantiation to transfer learned preferences within each gender-age-occupation cohort and marginalize over the joint distribution of gender, age, and occupation

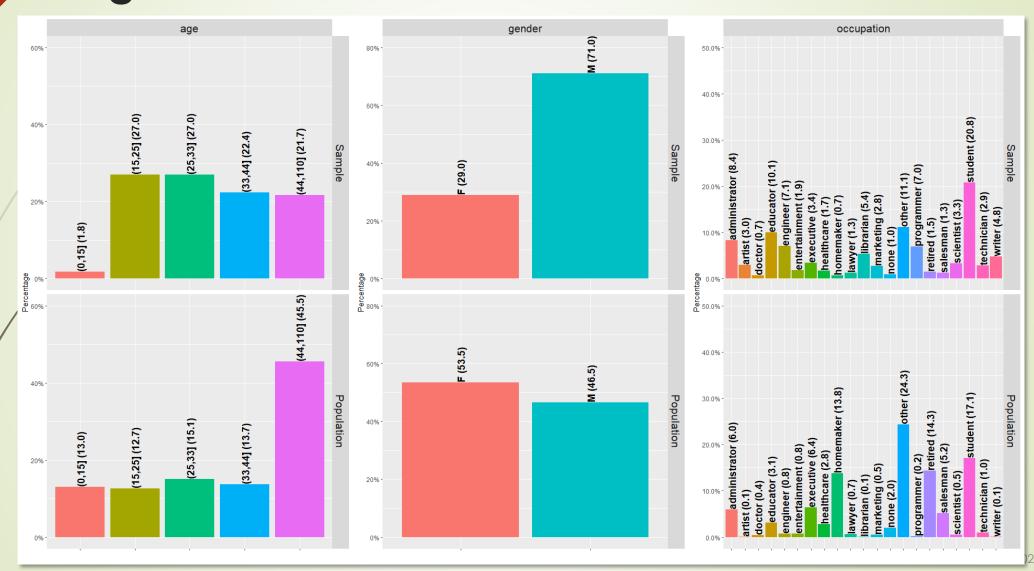
# Mitigating Issue of Sparsity: Quantify Uncertainty with Full Posterior



# Mitigating Issue of Bias: Post-Stratify Outcomes with Population Distn.

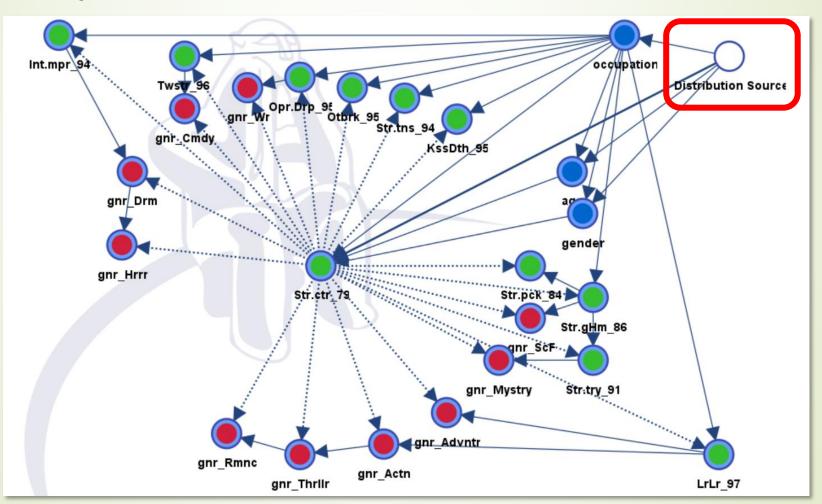
- Each TANB BBN captures the joint distribution  $P(Rating m_i, \{Other Movie Ratings\}, \{Movie features\}, \{Viewer features\})$
- Factors into conditional & marginal P(Rating  $m_i$ , {Other Movie Ratings }, {Movie features} | {Viewer features}) X P({Viewer features}) Captures Viewer Feature Distribution: Biased
- Impose Representative Viewer-Feature Distribution P({Viewer features}\*)
  - Supply distribution on Gender-Age-Occupation cohorts from U.S. Bureau of Labor Statistics
  - Augment TANB with node "Distribution Source" ∈ {Sample, Population} and arcs P({Viewer features} | Distribution Source)
  - Assert evidence "Distribution Source" = Population
  - Use BayesiaLab's "Evidence Instantiation" to create new TANB conditional probability tables consistent with  $P(Rating m_i, \{Other Movie Ratings\}, \{Movie features\}, \{Viewer features\}^*)$

### Marginal Distributions of Viewer Features



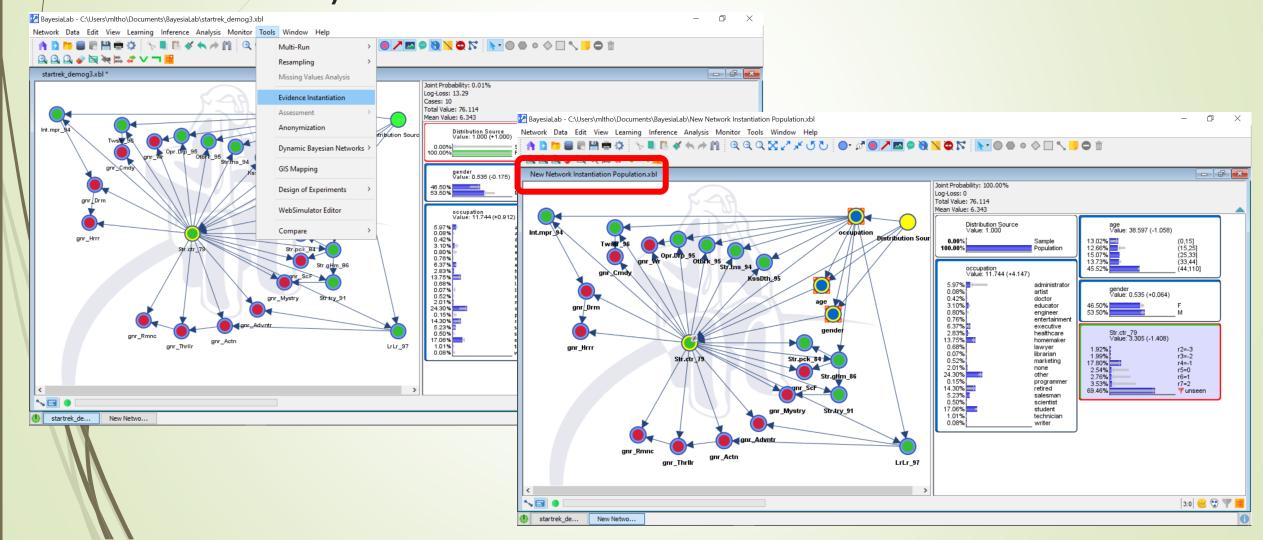
### Post-Stratification:

BayesiaLab's "Evidence Instantiation"



### Post-Stratification:

BayesiaLab's "Evidence Instantiation"



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## **Audience Analysis**

### Finding Folks who are Likely to Love the Film

Most Relevant Explanation (MRE)
Fix Evidence E=E\*, search over candidate Hypotheses H

Find H to Maximize:

GBF(H:E\*) =  $\frac{P(E = E^* = Like Target Movie | H = \{Viewer Features\})}{P(E = E^* = Like Target Movie | H \neq \{Viewer Features\})} = \frac{Odds(H|E^*)}{Odds(H)}$ 

**Example:** Observing someone likes "Star Trek: The Motion Picture (1979)" strongly confirms that person is an engineer if Likers are far more prevalent among engineers than they are among Non-engineers.

Gives same

order for E as does P(H\* | E).

Which type of Viewers
have a higher
prevalence of people
who Like the movie than
exists among people
different than that type
of Viewer?

■ Most Confirmatory Clues (MCC)

Fix Hypothesis H=H\*, search over candidate Evidence sets E

Find E to Maximize:

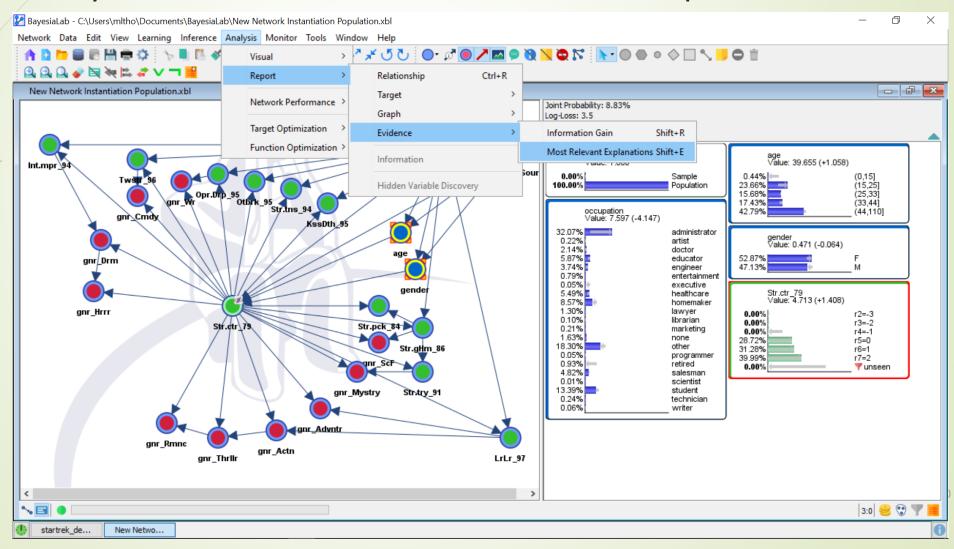
GBF(H\*: E) =  $\frac{P(E = \{Viewer Features\} \mid H = H^* = Like Target Movie)}{P(E = \{Viewer Features\} \mid H \neq Like Target Movie)} = \frac{Odds(H^*|E)}{Odds(H^*)}$ 

**Example:** Observing someone is an engineer strongly confirms that person will like "Star Trek: The Motion Picture (1979)" **if engineers are far more prevalent among Likers than they are among Non-Likers.** 

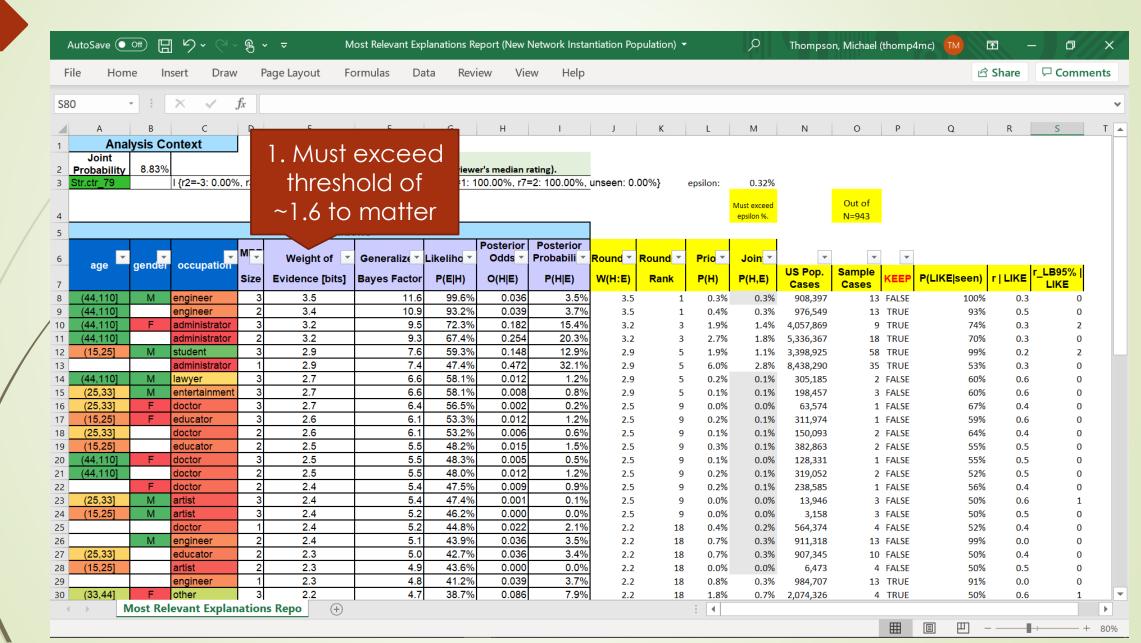
Which type of Viewers are far more prevalent among the people who Like the movie than they are among the people who dislike or didn't see the movie?

### **Audience Analysis:**

BayesiaLab's "Most Relevant Explanation"

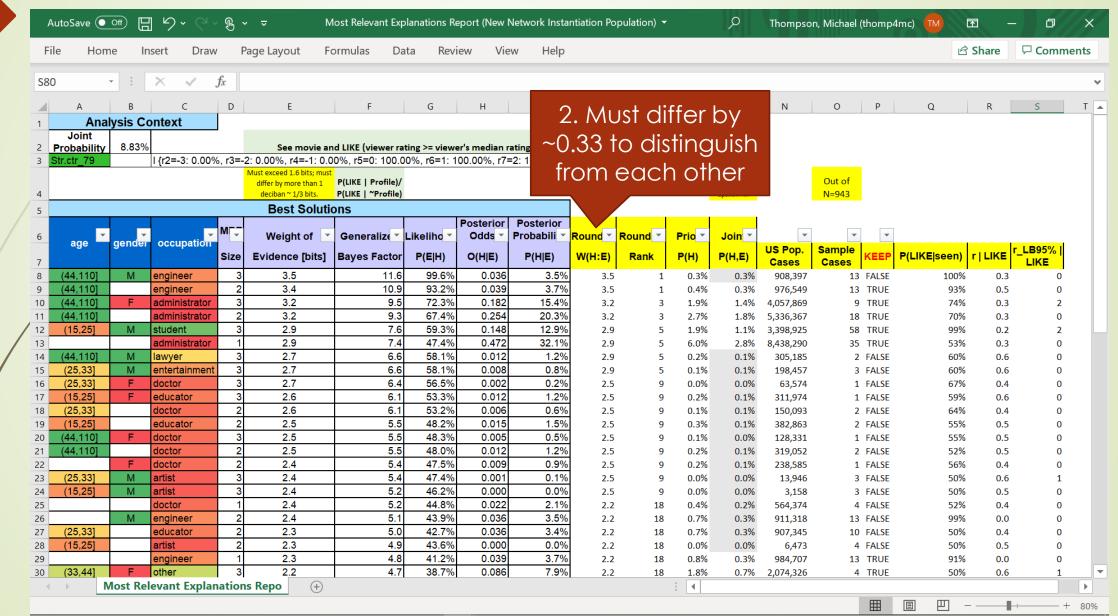


## Most Relevant Explanation: Three Key Issues



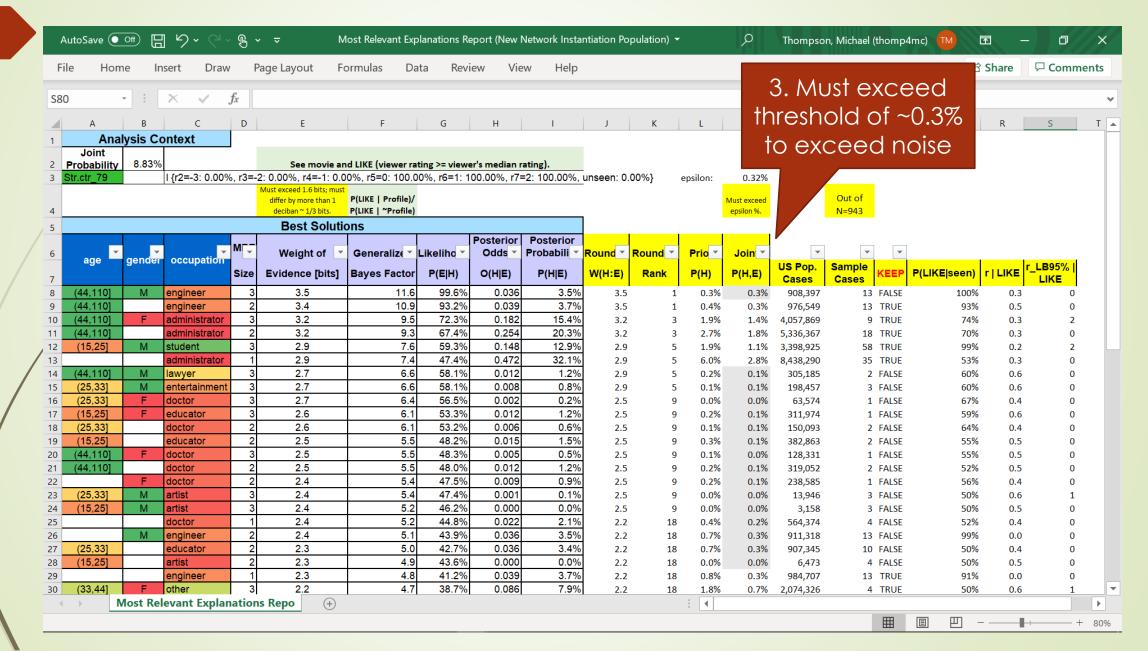
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## Most Relevant Explanation: Three Key Issues

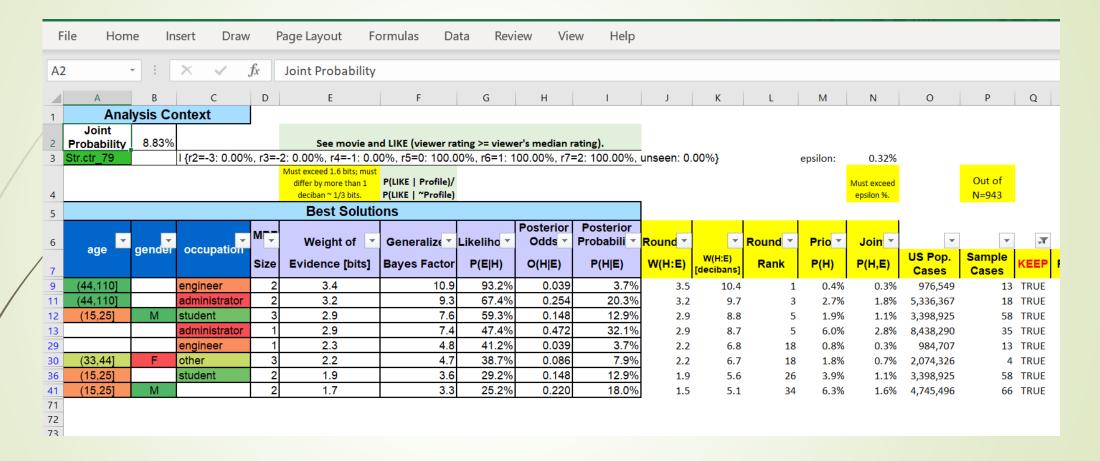


## Most Relevant Explanation: Three Key Issues

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### **Modified MRE**



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## Potential Extensions for BayesiaLab: Generalize MRE feature

- Allow "Most Confirmatory Clues", MCC
  - argmax E: GBF(H\*: E) currently, "Most Relevant Explanation", MRE, is argmax H: GBF(H: E\*); generalizes Target Optimization P(H\*|E): H\* can involve multiple nodes (compound hypothesis)
  - Checkbox to signal fixing Hypothesis and searching over Evidence combos
- Allow threshold on solutions as well as number of solutions
  - Entry field to accept minimum acceptable GBF (or W)
- Allow threshold on joint P(E,H) to avoid returning solutions that are just noise
  - Entry field to accept minimum acceptable P(E,H) for a solution, whether MRE or MCC; default equal 0, thus no imposition of threshold
- Allow tolerance in comparing GBF to account for human discernibility & noise
  - ► Entry field to accept minimum acceptable difference in GBF for two solutions to be considered different; default equal to 1 deciban per I.J. Good W(H:E) in decibans is 10 X log10(GBF(H:E)).
- Allow minimization of GBF for "LRE", Least Relevant Explanation, & "LCC", Least Confirmatory Clues
  - Checkbox to signal searching for strongest Refutation rather than Confirmation

### **Lessons Learned**

- Analysis over entire Joint Probability Distribution is a powerful feature of BBN
  - Caveat: Be wary of chasing noise analysis in the tails is much less robust than analysis of conditional expectations in the body of the distribution
- Bayesian methods allow principled post-stratification & uncertainty quantification
  - Caveat: "Garbage In, Garbage Out" No amount of reweighting can compensate for extreme sparsity and/or selection bias, esp. if unobserved context changes behavior of sample cohorts relative to the same population cohorts
- BayesiaLab offers state-of-the-art capabilities for Bayesian Analysis
  - Caveat: Even BayesiaLab can be made more powerful!

# Questions?