Indian Institute of Technology Delhi

Department of Physics

Numerical Methods

Assisgment II

1. Suppose we have a vector $\mathbf{v} = (2xz + 3y^2)\hat{j} + 4yz^2\hat{k}$. Check the Stokes theorem

$$\iint (\nabla \times \mathbf{v}) \cdot d\mathbf{a} = \oint \mathbf{v} \cdot d\mathbf{l}$$

using Simpsons method by assuming $h = 10^{-4}$ for the surface between (0,0,0)(0,1,1). (See Introduction to Electrodynamics 3^{rd} edition David J Griffith Example 1.11)

2. Suppose a body of mass m is traveling vertically upward starting at the surface of the earth. If all resistance except gravity is neglected, the escape velocity v is given by

$$v^2 = 2gR \int_1^\infty z^{-2} dz$$

and R = 3960 miles is the radius of the earth, and $g = 0.00609mi/s^2$ is the force of gravity at the surface. Approximate the escape velocity by assuming $h = 10^{-3}$?