

Q-1)

$$\pi_{\theta}(s, a) = p(a|s, \theta) = \frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{(a - \mu(s, \theta))^2}{2\sigma^2}\right)$$

$$\text{where } \mu(s, \theta) = \phi(s)^T \theta$$

$$\nabla_{\theta} \log \pi_{\theta}(s, a) = \nabla_{\theta} \log \frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{(a - \mu(s, \theta))^2}{2\sigma^2}\right)$$

$$= \nabla_{\theta} \log\left(\frac{1}{\sigma\sqrt{2\pi}}\right) + \nabla_{\theta} \left(-\frac{(a - \mu(s, \theta))^2}{2\sigma^2}\right)$$

$$= 0 - \nabla_{\theta} \left[\frac{(a - \phi(s)^T \theta)^2}{2\sigma^2} \right]$$

$$= \frac{1}{2\sigma^2} \left\{ 2(a - \phi(s)^T \theta) \cdot \phi(s) \right\}$$

$$= \frac{(a - \phi(s)^T \theta) \cdot \phi(s)}{\sigma^2}$$