

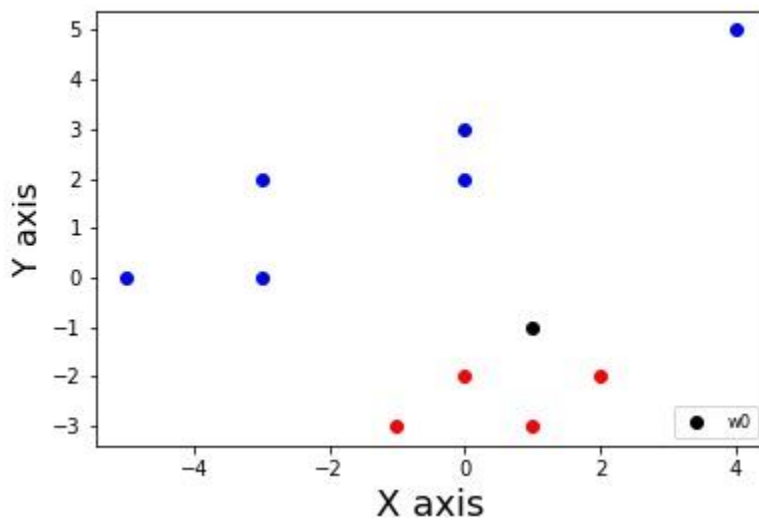
Assignment 4

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Note : I have only does those parts here that require plots. The rest have been done as handwritten solutions

Q1.

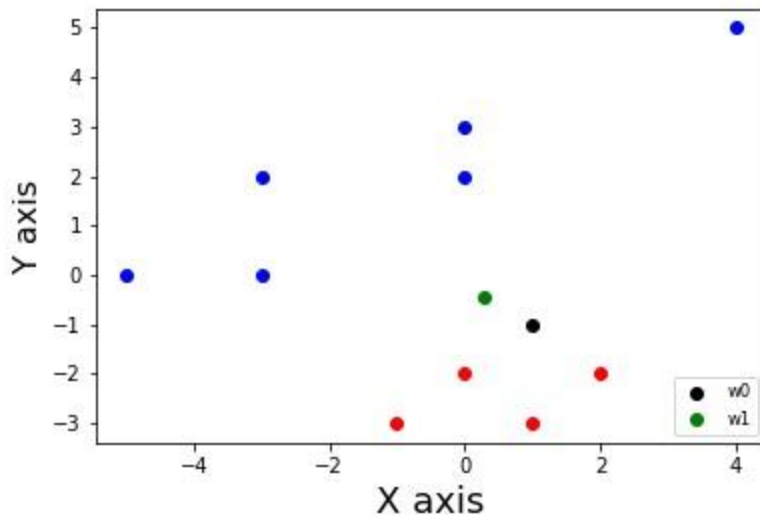
A) The initial working set is $W_0 = \{4\}$. Given below is the plot of data points



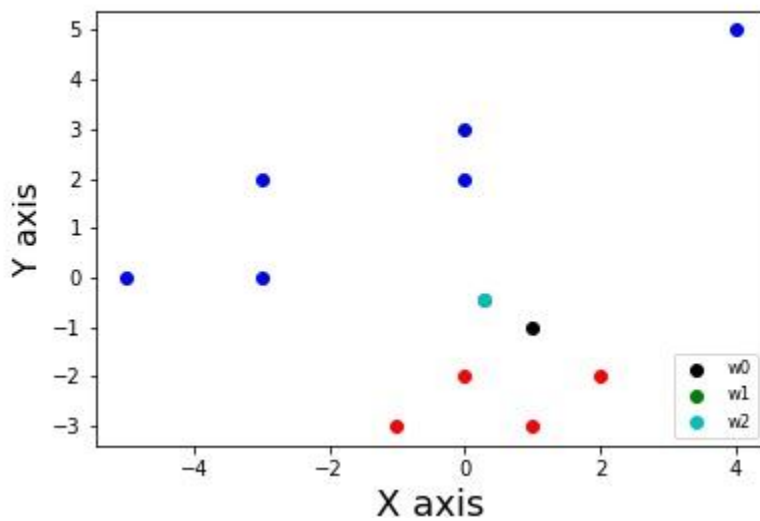
b) The working set after 1st iteration is $W_1 = \{1, 4\}$. The next iterate after 1st iteration is $w_1 =$

$[0.28571, -0.42857]$. The feasible direction obtained after minimization with respect to d is $[-1.09756, 0.87805]$

The corresponding Lagrange multiplier is $= -0.02439$



c)



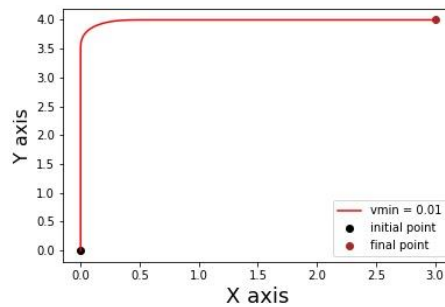
The working set after 2nd iteration is $W2 = \{1, 4\}$. The next iterate after 2nd iteration is $w1 = [0.28571, -0.42857]$. The feasible direction obtained after minimization with respect to d is $[-1.09756, 0.87805]$

The corresponding Lagrange multiplier is $= -0.02439$. Since $w1$ is the same as $w0$ therefore they only $w2$ is visible on the plot.

3 a)

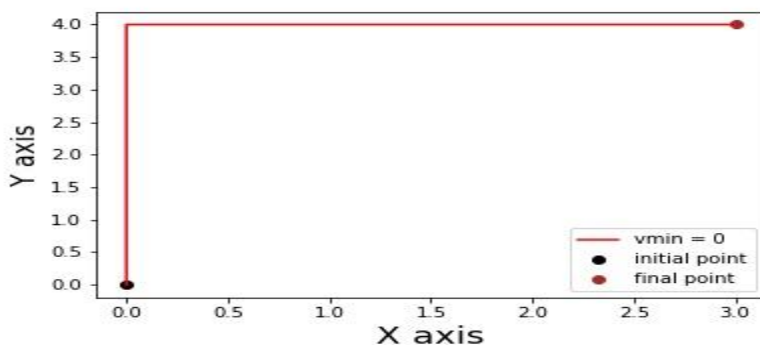
Case 1) $\theta_f = 0$, $v_{\min} = 0.01$

$v[1], v[2] = 1.716$, $v[100] = 2.422$ and the rest $v[i] = 0.01$ for $i \neq \{1, 2, 100\}$. The plot of trajectory is given below.



Case 2) $\theta_f = 0$, $v_{\min} = 0$

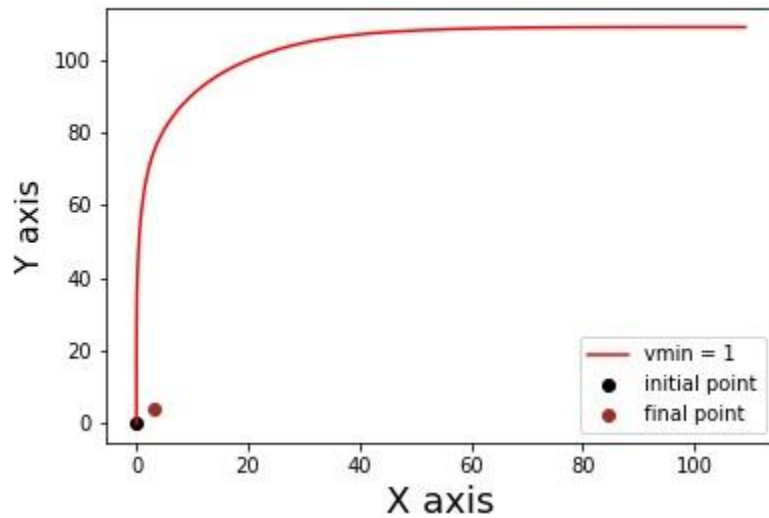
$v[1], v[2] = 2$, $v[100] = 3$ and the rest $v[i] = 0$ for $i \neq \{1, 2, 100\}$. The plot of trajectory is given below.



Case 3) $\theta_f = 0$, $v_{min} = 1$

The plot of trajectory is given below.

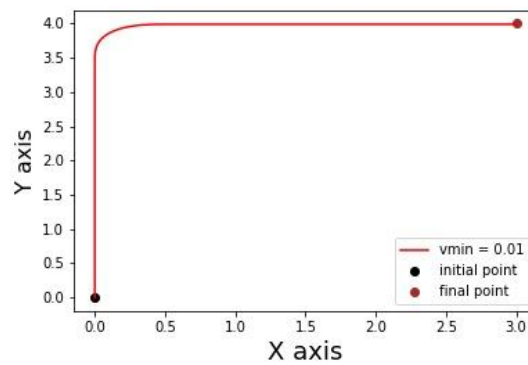
The solution does not converge hence trajectory goes beyond final point



3 a)

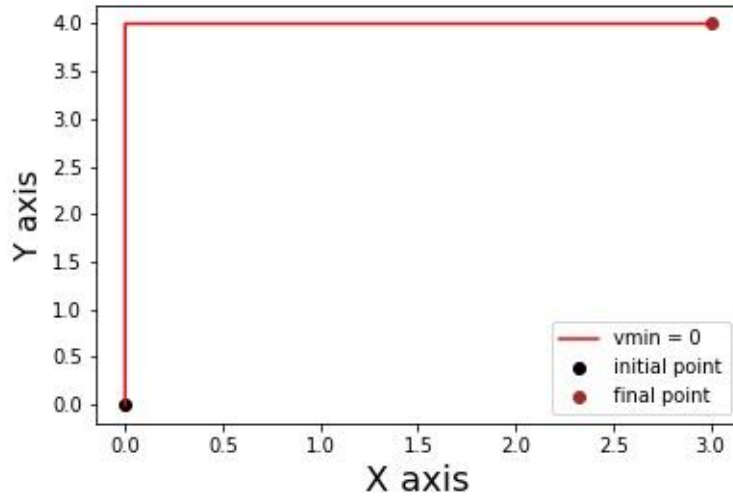
Case 1) $\theta_f = 90$ degree, $v_{min} = 0.01$

$v[1], v[2] = 1.711$, $v[99] = 2.432$ and the rest $v[i] = 0.01$ for $i \in \{1, 2, 99\}$. The plot of trajectory is given below.



Case 2) $\theta_f = 90^\circ$, $v_{min} = 0$

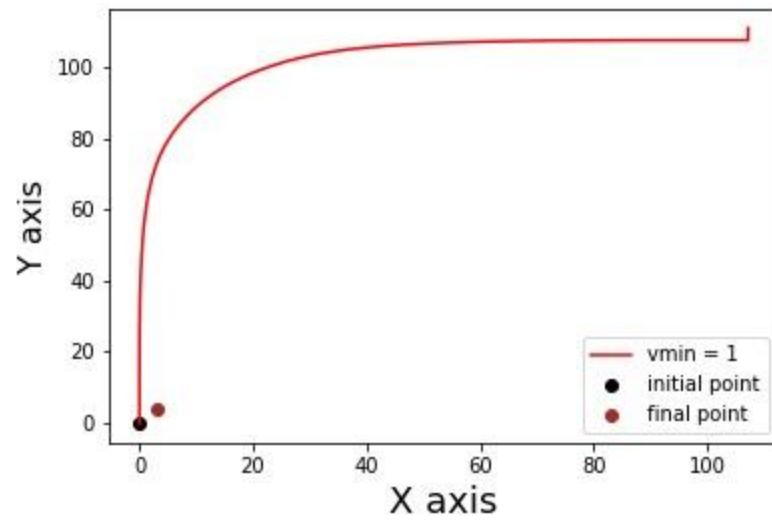
$v[1], v[2] = 2$, $v[99] = 3$ and the rest $v[i] = 0$ for $i \neq \{1, 2, 99\}$. The plot of trajectory is given below.



Case 3) $\theta_f = 90^\circ$, $v_{min} = 1$

The plot of trajectory is given below.

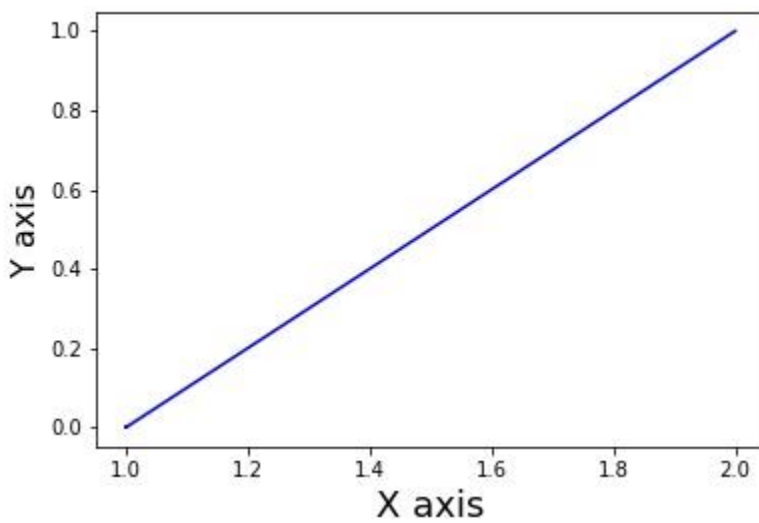
The solution does not converge hence trajectory goes beyond final point



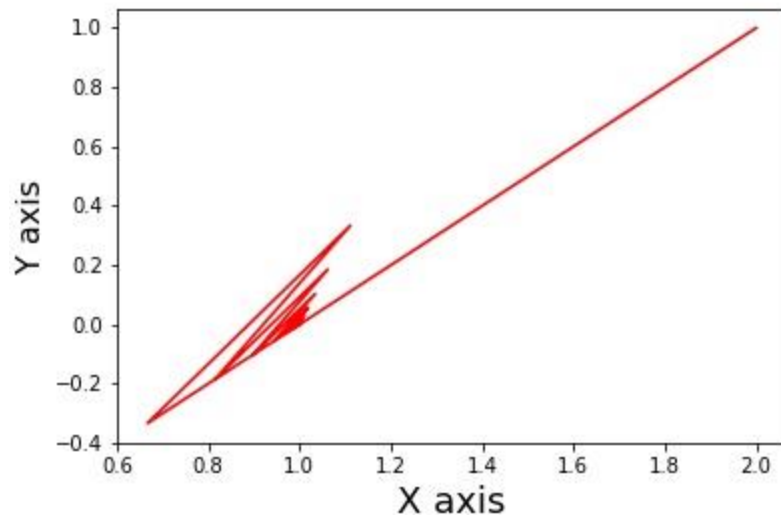
5 c) The optimal projection point obtained after 100 iterations is $[3, 0.5, 0.5]$

d) The final projected point obtained is $[1, 0]$. This is the trajectory obtained. The red trajectory is for step size $= 2/L$ and the blue trajectory is

For step size $= 1/L$



For step size $= 2/L$ trajectory is -



From the plots we can see that with step size $= 2/L$ the trajectory follows a zig zag path hence takes more iterations to converge. Therefore stepsize $1/L$ is better.