

# Finding Plans with Branches, Loops, and Preconditions

Siddharth Srivastava

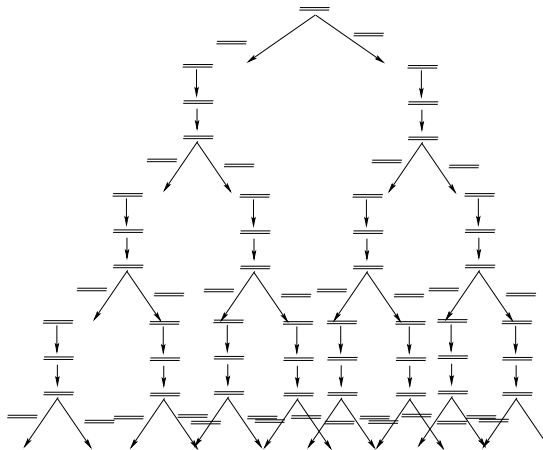
Joint work with Neil Immerman and Shlomo Zilberstein  
University of Massachusetts, Amherst

ICAPS 2009 Workshop on  
Verification and Validation of Planning and Scheduling  
Systems  
September 20<sup>th</sup>, 2009

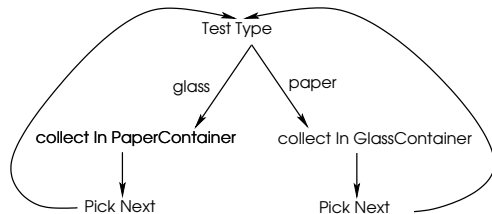
# Overview

- Introduction
- Our Framework
- Planning Algorithms
- Results

# Conditional Planning



# Conditional Planning



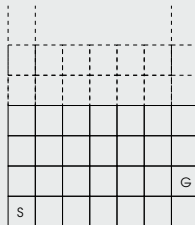
- Serious problems with applicability test, instantiation:
  - Loop termination, progress

# Plan Preconditions

- One approach: simulated execution.
- Will be wasted if  $G$  cannot solve a problem.

NavigateGrids /\*Start at bottom left\*/

```
repeat
  while  $\neg$ rightmost do
    | mvR()
  end
  mvU()
  while  $\neg$ leftmost do
    | mvL()
  end
  mvU()
until atgoal
```

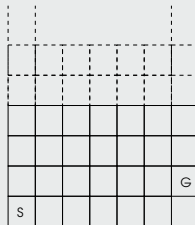


# Plan Preconditions

- One approach: simulated execution.
- Will be wasted if  $G$  cannot solve a problem.

NavigateGrids /\*Start at bottom left\*/

```
repeat
  while  $\neg$ rightmost do
    | mvR()
  end
  mvU()
  while  $\neg$ leftmost do
    | mvL()
  end
  mvU()
until atgoal
```



# Plan Preconditions (ctd.)

- Historically not common: not required for simple plans  $(a_1, \dots, a_n)$ .
- Computed plans with loops etc. will typically have a limited applicability.
  - Simulated execution may not even terminate!!

Ideal applicability test: linear in the size of the problem

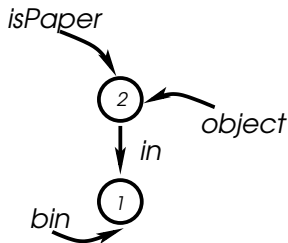
# Our Objective

- Compute algorithm-like “generalized” plans.
  - Efficient applicability tests
  - Efficient generation of generalized plans
- Need to determine progress and termination.



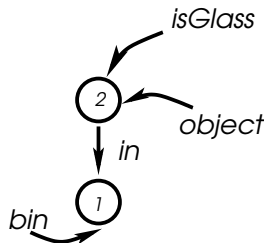
# Concrete States as Logical Structures

$$\mathcal{V} = \{object^1, bin^1, isGlass^1, isPaper^1, in^2, empty^1, collected^1, forGlass^1, forPaper^1\}$$



$((object(2))) = 1$   
 $((isPaper(2))) = 1$   
 $((bin(1))) = 1$   
 $((in(2,1))) = 1$

$S_1$



$((object(2))) = 1$   
 $((isGlass(2))) = 1$   
 $((bin(1))) = 1$   
 $((in(2,1))) = 1$

$S_2$

# Example: The Collect Action

## Collect(o,c)

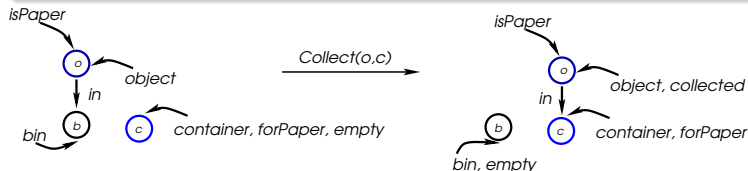
$\text{object}(o) \wedge \text{container}(c) \wedge (\text{isGlass}(o) \leftrightarrow \text{forGlass}(c)) \wedge$   
 $\exists b(\text{bin}(b) \wedge \text{in}(o, b) \wedge \text{robotAt}(b))$

$$\text{in}'(u, v) := (\text{in}(u, v) \wedge u \neq o) \vee$$

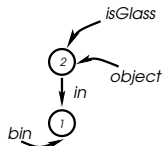
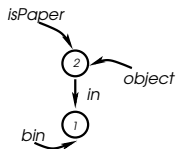
$$(\neg \text{in}(u, v) \wedge u = o \wedge v = c)$$

$$\text{empty}'(u) := (\text{empty}(u) \wedge u \neq c) \vee \text{in}(o, u)$$

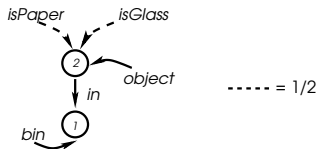
$$\text{collected}'(u) := \text{collected}(u) \vee o = u$$



# Abstraction Using 3-Valued Logic

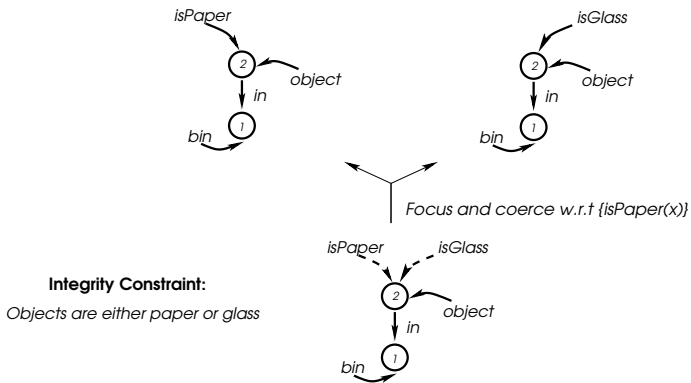


Use 3-Valued logic to abstract as:



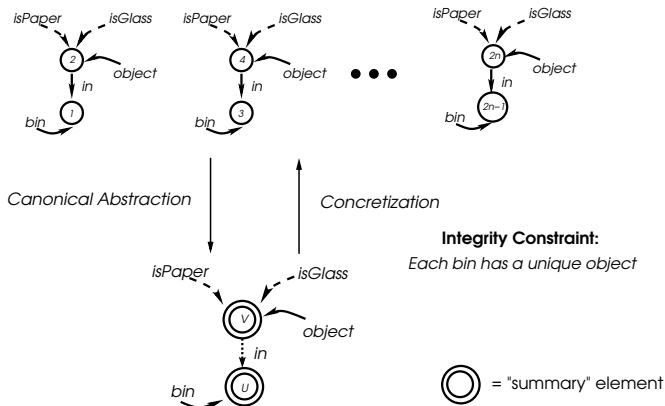
TVLA: [Sagiv et al., 2002]

# Abstraction Using 3-Valued Logic



Implementation of “sensing” actions

# Abstraction Using 3-Valued Logic



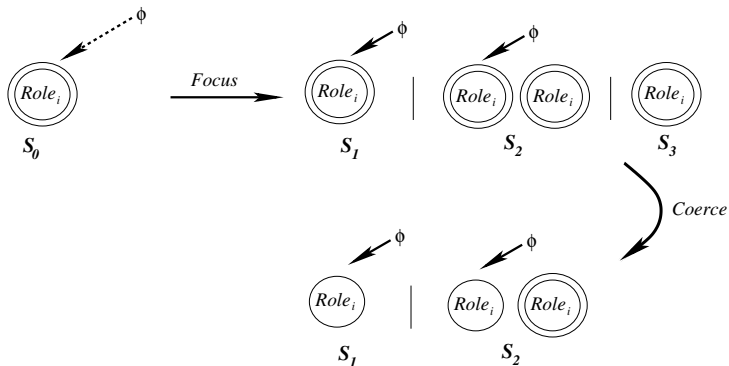
# Abstraction Using 3-Valued Logic: Summary

TVLA [Sagiv et al., 2002]: Three Valued Logic Analysis

- **Abstraction predicates**: unary predicates.
- Element's **role** = set of abstraction predicates satisfied
- Collapse elements of a role into **summary elements**.
- Use **integrity constraints** to retrieve concrete states.

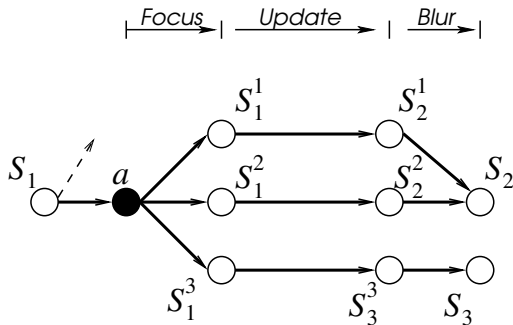
# Action Application on Belief States

- Make structures precise by creating possible cases: focus (automatic)
- Apply action



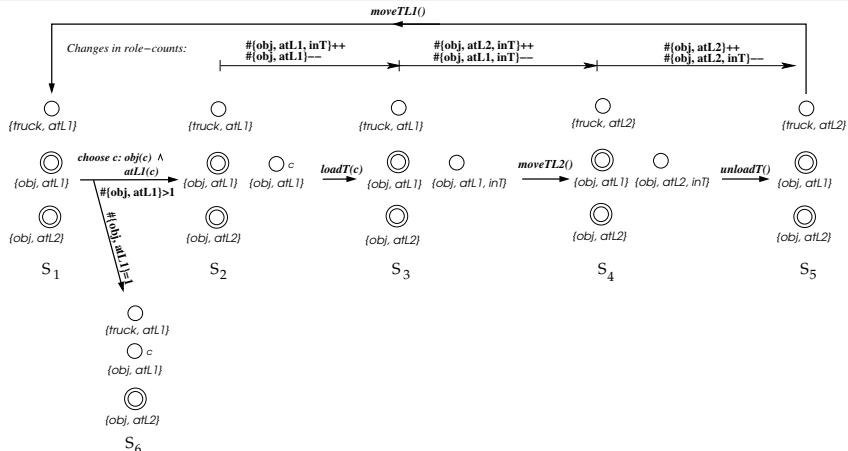
# Action Application on Belief States

- Make structures precise by creating possible cases: focus (automatic)
- Apply action

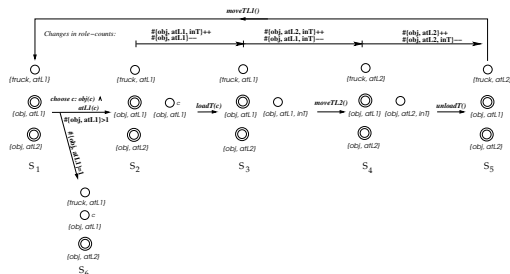




# Role-counts, Branches and Plan Preconditions



# Role-counts, Branches and Plan Preconditions

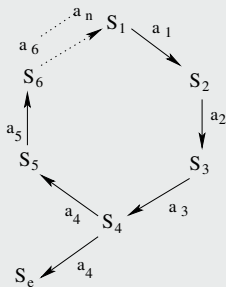


- Goal is provably reachable from the infinitely many structures represented by  $S_1$ .
- $\forall s \in S_1$ , can compute number of steps required to reach the goal.

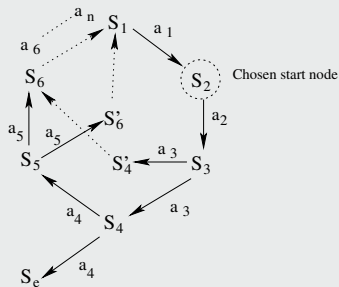
Generalized to *extended-LL* domains.

## Extension to Complex Loops with Shortcuts

## Shortcuts due to sensing actions



(a) A simple loop



(b) A simple loop with (non-composable) shortcuts

# Extension to Nested Loops?

```

for i = 1 to n {
  for j = 1 to k {
    .
  }
  .
}

```

```

for i = 1 to n {
  .
  if (...) {
    .
  }
  if (...) {
    .
  }
}

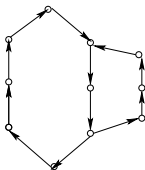
```

# Extension to Nested Loops?

```

for i = 1 to n {
  for j = 1 to k {
    .
  }
}

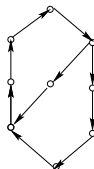
```



```

for i = 1 to n {
  .
  if (...) {
    .
  }
  if (...) {
    .
  }
}

```



# Extension to Nested Loops?

```

for i = 1 to n {
  a1
  for j = 1 to k {
    a2
  }
  a3
}

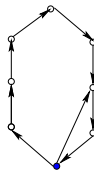
```



```

i = 1; j = 1
if (i < n+1) { a1 }
for i = 1 to n {
  if (j > k) {
    a3
    i++
    a1
    j = 1
  }
  if (j < k+1) {
    a2
    j++
  }
}

```



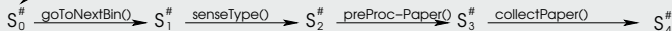
- Execution sequences match.
- Translation of the loop entry point  $\implies$  complex loop with a shortcut!
- Methods applicable to many so-called “nested” loops.

# Plan Generalization

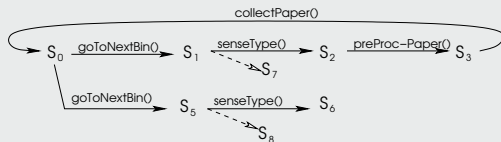
Use **abstract structures** to recognize **loop invariants** in example concrete plans.

## Example Execution

2 objects of each type collected;  
2 bins remaining



## Find Loops



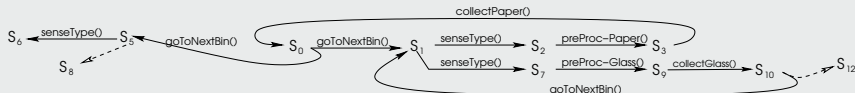
Developed for completely observable settings [Srivastava et al., 2008]

# Merging Generalized Plans

## Plan for Unhandled Structure

$S_7 \xrightarrow{\text{preProc-Glass()}} S_9 \xrightarrow{\text{collectGlass()}} S_{10} \xrightarrow{\text{goToNextBin()}} S_{11} \text{ ---}$

## Generalize and Merge



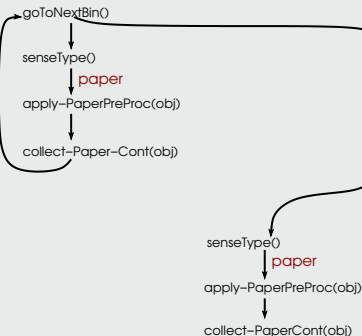
- A single plan may not explore all possibilities.
- Construct problem instances from unsolved belief states.
- Solve them using classical planners.



# Example Results

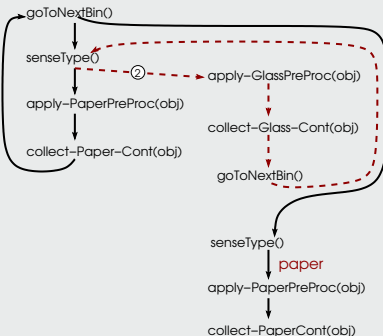
$p_0 = \|\{\text{paper, collected}\}\|$ ;  $pc_0 = \|\{\text{empty, container, forPaper}\}\|$ ;  
 $g_0, gc_0$  : similar for glass;  $b_0 = \|\{\text{bin}\}\|$

## Loop 1



- Precons:  $pc_0 = l_1$ ;  $b_0 = l_1$
- Solves 1 out of  $2^n$

## Loops 1 & 2



- Precons:  
 $pc_0 = l_1$ ;  $gc_0 = l_2$ ;  $b_0 = l_1 + l_2$
- $2^{n-1} + 1$  out of every  $2^n$

# Merging Generalized Plans: Algorithm

**Input:** Existing plan  $\Pi$ , eg trace  $\text{trace}_i$

**Output:** Extension of  $\Pi$

```

1  if  $\Pi = \emptyset$  then
2       $\Pi \leftarrow \text{trace}_i$ 
3      return  $\Pi$ 
  end
4   $\text{mp}_{\Pi}, \text{mp}_t \leftarrow \text{findMergePoint}(\Pi, \text{trace}_i, \text{bp}_{\Pi}, \text{bp}_t)$ 
5  repeat
6      if  $\text{mp}_{\Pi}$  found then
7           $\text{bp}_{\Pi}, \text{bp}_t \leftarrow \text{findBranchPoint}(\Pi, \text{trace}_i, \text{mp}_{\Pi}, \text{mp}_t)$ 
      end
8      if  $\text{bp}_{\Pi}$  found then
9           $\text{mp}_{\Pi}, \text{mp}_t \leftarrow \text{findMergePoint}(\Pi, \text{trace}_i, \text{bp}_{\Pi}, \text{bp}_t)$ 
10          $\text{addEdges}(\Pi, \text{trace}_i, \text{bp}_t, \text{mp}_t, \text{mp}_{\Pi}, \text{bp}_{\Pi})$ 
      end
  until new  $\text{bp}_{\Pi}$  or  $\text{mp}_{\Pi}$  not found
11 return  $\Pi$ 

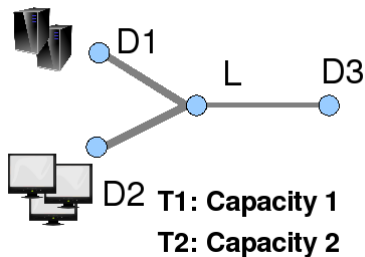
```

## Algorithm 1: ARANDA-Merge

# Conclusions

- Approach addressing plan/algorithm synthesis and verification.
  - Advantage of automated synthesis: can choose to keep control structure verifiable.
- Close to program synthesis, but free of associated intractability.
- Efficient precondition tests and measures of progress.

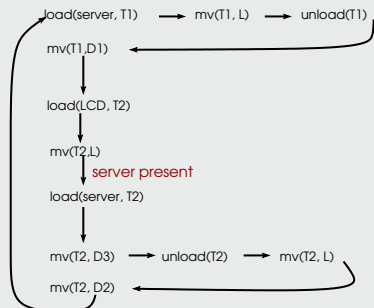
# Transport Domain



# Transport Domain: Results

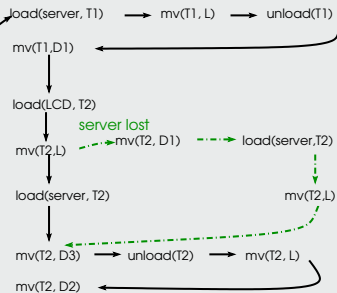
$$m_0 = \|\{\text{monitor, atD2}\}\|; s_0 = \|\{\text{server, atD1}\}\|$$

## Loop 1



- Precons:  $m_o = l_1; s_o = l_1$

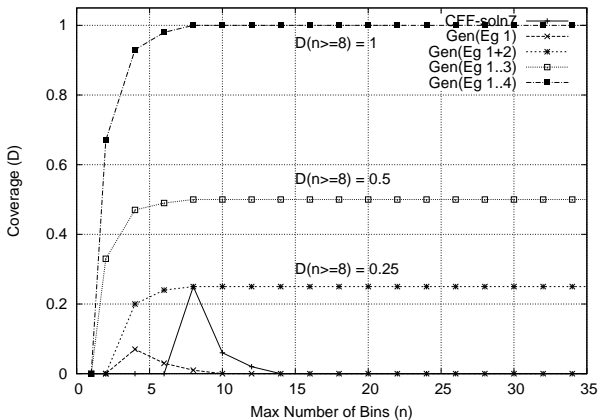
## Loops 1 & 2



- Precons:

$$m_o = l_1; s_o = l_1 + k_1$$

# Example Results: Domain Coverage






$$D_{\pi}(n) = |\mathcal{S}_{\pi}(n)|/|\mathcal{T}(n)|$$

# Related Work

- Plans with Loops
  - [Winner and Veloso, 2007]: no preconditions or sensing actions, but use partial ordering.
  - [Levesque, 2005]: single planning parameter, limited preconditions.
  - [Cimatti et al., 2003]: “hard” loops.
- Planning with unknown quantities:
  - [Milch et al., 2005]: action operators not provided.

# References I

-  Cimatti, A., Pistore, M., Roveri, M., and Traverso, P. (2003).  
Weak, strong, and strong cyclic planning via symbolic model  
checking.  
*Artif. Intell.*, 147(1-2):35–84.
-  Levesque, H. J. (2005).  
Planning with loops.  
In *Proc. of IJCAI*, pages 509–515.
-  Milch, B., Marthi, B., Russell, S. J., Sontag, D., Ong, D. L.,  
and Kolobov, A. (2005).  
Blog: Probabilistic models with unknown objects.  
In *Proc. of IJCAI*, pages 1352–1359.



# References II



Sagiv, M., Reps, T., and Wilhelm, R. (2002).

Parametric shape analysis via 3-valued logic.

*ACM Transactions on Programming Languages and Systems*,  
24(3):217–298.



Srivastava, S., Immerman, N., and Zilberstein, S. (2008).

Learning generalized plans using abstract counting.

In *Proc. of AAAI*, pages 991–997.



Winner, E. and Veloso, M. (2007).

LoopDISTILL: Learning domain-specific planners from  
example plans.

In *Workshop on AI Planning and Learning, ICAPS*.