

Challenges in Finding Generalized Plans

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Generalized Planning

Plans or planning structures that “work in many situations”

- Triangle Tables [Fikes et al., 1972]
- Case Based Planning [Hammond, 1986]
- Explanation Based Planning
[Minton et al., 1989, Shavlik, 1990]
- Contingent Planning
- Learning domain specific planners from examples
[Winner and Veloso, 2003]; Planning with loops
[Levesque, 2005];

Overview

- Universal Challenges
- Our Framework
- Generalized Planning with Sensing Actions
- Results

Examples of Generalized Plans

Classical Plans

$\text{mvToTable}(b_3), \text{mvToTable}(b_2), \text{mvToTable}(b_1)$

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“Unstack”:

$\text{while}(\exists b: \text{topmost}(b) \wedge \neg \text{onTable}(b)) \{ \text{mvToTable}(b) \}$

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FF, SATPLAN, SGPLAN, ...

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Common fundamental problem (*Generalized Planning*):

Find a function G (a *generalized plan*):

$G : \text{Problem instance} \rightarrow \text{sequence of actions}$

What makes us prefer one over another?

Challenges for Any Approach to Generalized Planning

- ① Applicability Test
- ② Cost of Instantiation
- ③ Domain Coverage
- ④ Quality of instantiated plans
- ⑤ Complexity of creating generalized plans

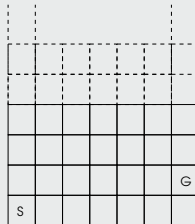
Applicability Test

G : Problem instance $\xrightarrow{\text{plan instantiation}} a_1, \dots, a_n$

- One approach: simulated execution.
- Cost of instantiation will be wasted if G cannot solve it.

NavigateGrids /*Start at bottom left*/

```
repeat
  while  $\neg$ rightmost do
    | mvR()
  end
  mvU()
  while  $\neg$ leftmost do
    | mvL()
  end
  mvU()
until atgoal
```



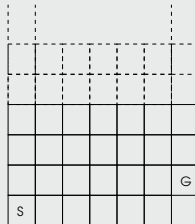
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Applicability Test (ctd.)

- Historically not common: not required for very general (FF) or very simple plans ($a_1, \dots a_n$).
- Computed generalized plans typically have a limited applicability.
- More of a problem with compact representations (loops).
 - Simulated execution may not even terminate!!

Ideal applicability test: linear in the size of the problem

Cost of Plan Instantiation

$$G : \text{Problem instance} \xrightarrow{\text{plan instantiation}} a_1, \dots, a_n$$

- Makes generalized plans like “unstack” ($O(n)$) more desirable than classical planners ($O(\exp(n))$).
- In hindsight: low COI = one of the main motivations behind this field.

Domain Coverage

The set/fraction of solvable problems solved by a generalized plan.

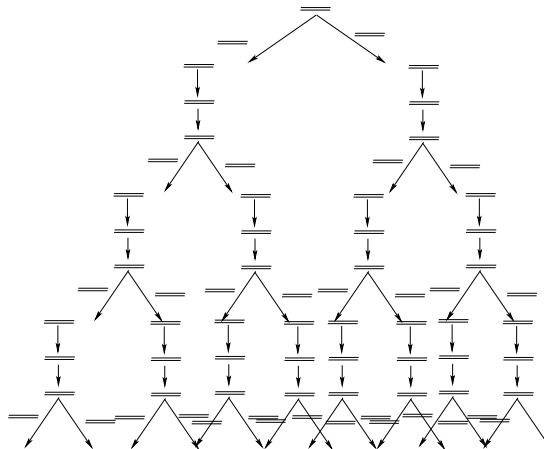
- Historically one of the most measured attributes.
- Trade-offs with cost of instantiation.

Quality of Instantiated Plans

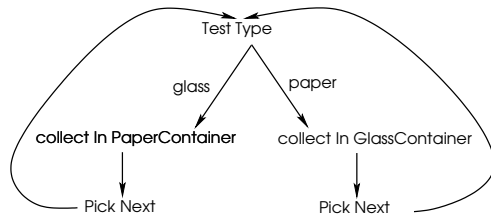
The computational cost (makespan/number of actions/time etc.) of executing the instantiated plan.

- Satisficing, optimal generalized plans.
- Trade-offs with domain coverage and cost of instantiation.

Complexity of Creating Generalized Plans



Complexity of Creating Generalized Plans



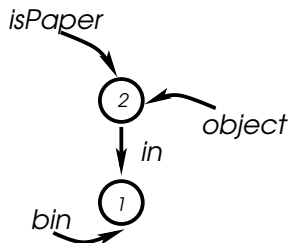
- Serious problems with applicability test, instantiation:
 - Loop termination, progress

Our Objective

- Compute algorithm-like “generalized” plans.
 - Low cost of instantiation
 - Efficient applicability tests
 - Efficient generation of generalized plans
- Need to determine progress and termination.

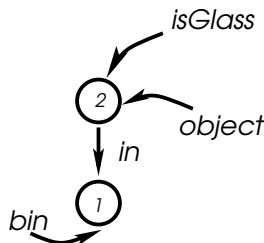
Concrete States as Logical Structures

$$\mathcal{V} = \{object^1, bin^1, isGlass^1, isPaper^1, in^2, empty^1, collected^1, forGlass^1, forPaper^1\}$$



$((object(2))) = 1$
 $((isPaper(2))) = 1$
 $((bin(1))) = 1$
 $((in(2,1))) = 1$

S_1



$((object(2))) = 1$
 $((isGlass(2))) = 1$
 $((bin(1))) = 1$
 $((in(2,1))) = 1$

S_2

Example: The Collect Action

Collect(o,c)

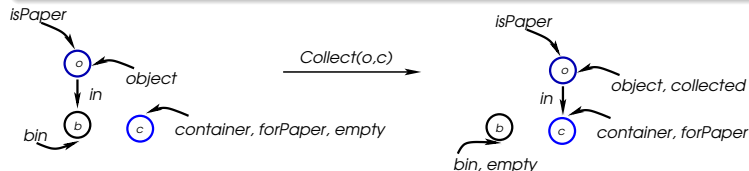
$\text{object}(o) \wedge \text{container}(c) \wedge (\text{isGlass}(o) \leftrightarrow \text{forGlass}(c)) \wedge$
 $\exists b(\text{bin}(b) \wedge \text{in}(o, b) \wedge \text{robotAt}(b))$

$$\text{in}'(u, v) := (\text{in}(u, v) \wedge u \neq o) \vee$$

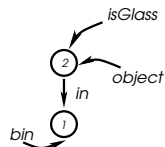
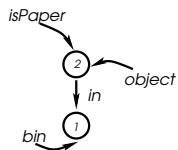
$$(\neg \text{in}(u, v) \wedge u = o \wedge v = c)$$

$$\text{empty}'(u) := (\text{empty}(u) \wedge u \neq c) \vee \text{in}(o, u)$$

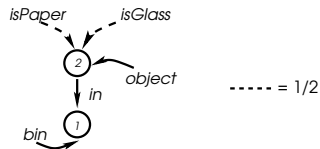
$$\text{collected}'(u) := \text{collected}(u) \vee o = u$$



Abstraction Using 3-Valued Logic

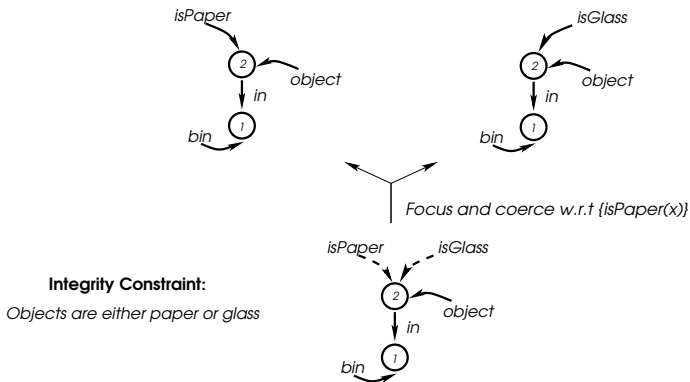


Use 3-Valued logic to abstract as:



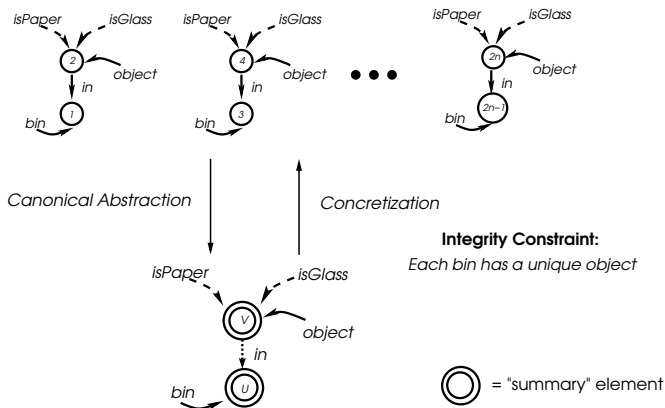
TVLA: [Sagiv et al., 2002]

Abstraction Using 3-Valued Logic



Implementation of “sensing” actions

Abstraction Using 3-Valued Logic



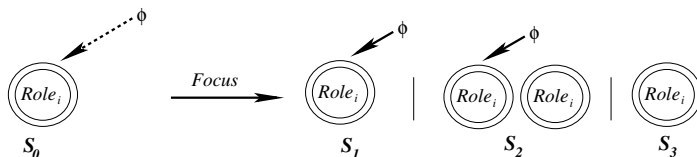
Abstraction Using 3-Valued Logic: Summary

TVLA [Sagiv et al., 2002]: Three Valued Logic Analysis

- **Abstraction predicates**: unary predicates.
- Element's **role** = set of abstraction predicates satisfied
- Collapse elements of a role into **summary elements**.
- Use **integrity constraints** to retrieve concrete states.

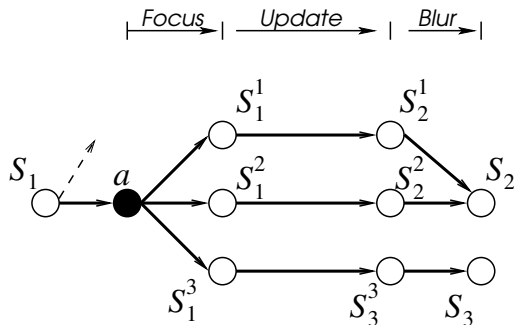
Action Application on Belief States

- Make structures precise by creating possible cases: focus (automatic)
- Apply action



Action Application on Belief States

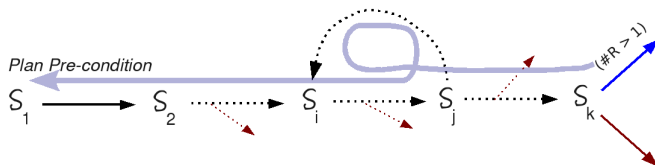
- Make structures precise by creating possible cases: focus (automatic)
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Action Branches and Plan Preconditions

Branches solve only *some* members of abstract structures

- May be classifiable, e.g. $\#_R\{S\} > 1$
 - Extended-LL domains: all branches are classifiable
- Subtract role-count changes to obtain preconditions at start.
- Generalize to simple loops, nested loops due to shortcuts and sensing actions.

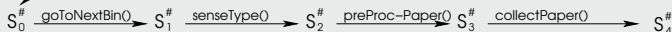


Plan Generalization

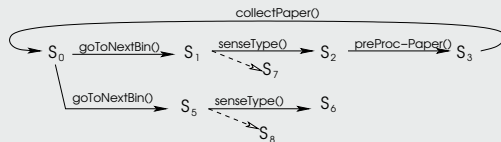
Use **abstract structures** to recognize **loop invariants** in example concrete plans.

Example Execution

2 objects of each type collected;
2 bins remaining



Find Loops



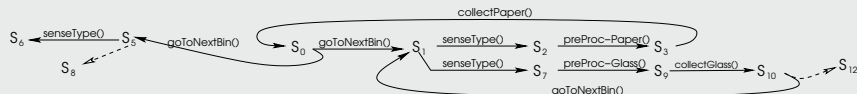
Developed for completely observable settings [Srivastava et al., 2008]

Merging Generalized Plans

Plan for Unhandled Structure

$S_7 \xrightarrow{\text{preProc-Glass()}} S_9 \xrightarrow{\text{collectGlass()}} S_{10} \xrightarrow{\text{goToNextBin()}} S_{11} \text{ ---}$

Generalize and Merge

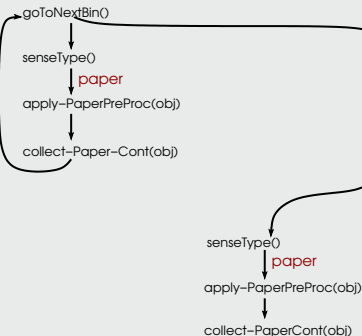


- A single plan may not explore all possibilities.
- Construct problem instances from unsolved belief states.
- Solve them using classical planners.

Example Results

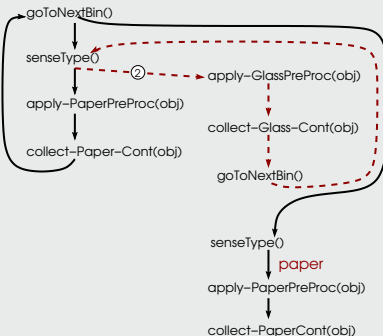
$p_0 = \|\{\text{paper, collected}\}\|$; $pc_0 = \|\{\text{empty, container, forPaper}\}\|$;
 g_0, gc_0 : similar for glass; $b_0 = \|\{\text{bin}\}\|$

Loop 1



- Precons: $pc_0 = l_1$; $b_0 = l_1$
- Solves 1 out of 2^n

Loops 1 & 2



- Precons:
 $pc_0 = l_1$; $gc_0 = l_2$; $b_0 = l_1 + l_2$
- $2^{n-1} + 1$ out of every 2^n

Merging Generalized Plans: Algorithm

Input: Existing plan Π , eg trace trace_i

Output: Extension of Π

```

1  if  $\Pi = \emptyset$  then
2       $\Pi \leftarrow \text{trace}_i$ 
3      return  $\Pi$ 
  end
4   $\text{mp}_{\Pi}, \text{mp}_t \leftarrow \text{findMergePoint}(\Pi, \text{trace}_i, \text{bp}_{\Pi}, \text{bp}_t)$ 
5  repeat
6      if  $\text{mp}_{\Pi}$  found then
7           $\text{bp}_{\Pi}, \text{bp}_t \leftarrow \text{findBranchPoint}(\Pi, \text{trace}_i, \text{mp}_{\Pi}, \text{mp}_t)$ 
      end
8      if  $\text{bp}_{\Pi}$  found then
9           $\text{mp}_{\Pi}, \text{mp}_t \leftarrow \text{findMergePoint}(\Pi, \text{trace}_i, \text{bp}_{\Pi}, \text{bp}_t)$ 
10          $\text{addEdges}(\Pi, \text{trace}_i, \text{bp}_t, \text{mp}_t, \text{mp}_{\Pi}, \text{bp}_{\Pi})$ 
      end
  until new  $\text{bp}_{\Pi}$  or  $\text{mp}_{\Pi}$  not found
11 return  $\Pi$ 

```

Algorithm 1: ARANDA-Merge

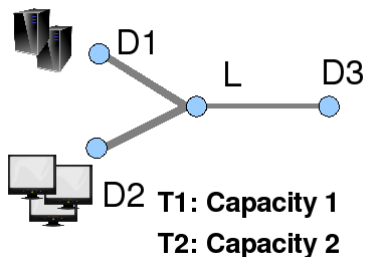
Addressing the Challenges

- Cost of testing applicability: independent of the size of the problem.
- Cost of instantiation: linear, or better with role-lists
- Domain Coverage can increase exponentially with new examples
- Complexity of creating generalized plan: $O(s \cdot n_{eg}^2)$ to find loops, $O(s \cdot n_{eg})$ for preconditions.

Conclusions

- Clear formal framework for algorithmic plans, avoiding intractability of automated program synthesis.
- Approach for learning generalized conditional plans with nested loops by composition of simple linear plans.
- Efficient methods for computation of measures of progress and preconditions.

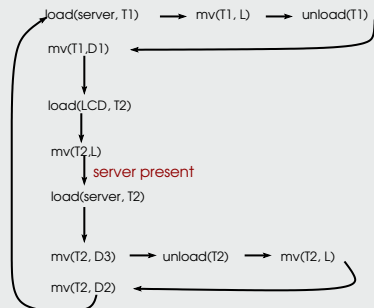
Transport Domain



Transport Domain: Results

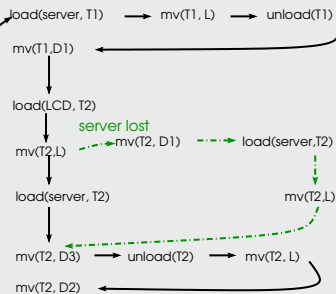
$$m_0 = \|\{\text{monitor, atD2}\}\|; s_0 = \|\{\text{server, atD1}\}\|$$

Loop 1



- Precons: $m_o = l_1; s_o = l_1$

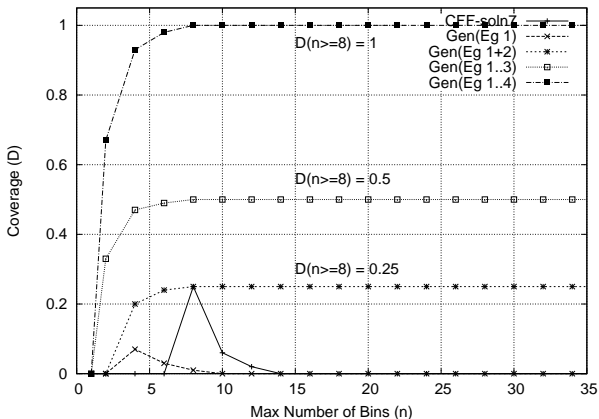
Loops 1 & 2



- Precons:

$$m_0 = l_1; s_o = l_1 + k_1$$

Example Results: Domain Coverage







$$D_{\pi}(n) = |\mathcal{S}_{\pi}(n)|/|\mathcal{T}(n)|$$

Related Work

- Plans with Loops
 - [Winner and Veloso, 2007]: no preconditions or sensing actions, but use partial ordering.
 - [Levesque, 2005]: single planning parameter, limited preconditions.
 - [Cimatti et al., 2003]: “hard” loops.
- Planning with unknown quantities:
 - [Milch et al., 2005]: action operators not provided.

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