



To use per-unit calculations, first define our nominal or base quantities

$$\begin{aligned} S_n &= S_b \text{ [VA]} \\ V_n &= V_b \text{ [V]} \\ I_n &= I_b \text{ [A]} \\ Z_b &= \frac{V_n^2}{S_n} \text{ (\Omega)} \end{aligned}$$

Per unit impedances are defined normalized to the base impedance

$$\begin{aligned} Z_{pu} \text{ [%]} &= \frac{Z \text{ (\Omega)}}{Z_b \text{ (\Omega)}} \\ X_{pu} \text{ [%]} &= \frac{X \text{ (\Omega)}}{Z_b \text{ (\Omega)}} \\ R_{pu} \text{ [%]} &= \frac{R \text{ (\Omega)}}{Z_b \text{ (\Omega)}} \end{aligned}$$

Impedance is defined as usual in the cartesian plane with resistance (real axis) and reactance (imaginary axis)

$$\begin{aligned} Z &= R + jX \\ Z_{pu} &= R_{pu} + jX_{pu} \end{aligned}$$

X over R (**XoR**) is a commonly defined parameter that defines the ratio of **X** to **R**, either in absolute or per unit

$$XoR = \frac{X_{pu}}{R_{pu}}, X_{pu} = XoR \cdot R_{pu}$$

XoR and per unit impedance can be used to work out per unit resistance and reactance

$$\begin{aligned} |Z_{pu}|^2 &= |R_{pu}|^2 + |X_{pu}|^2 \\ |Z_{pu}|^2 &= |R_{pu}|^2 + (|R_{pu}| \cdot XoR)^2 \\ |Z_{pu}|^2 &= |R_{pu}|^2 (1 + XoR^2) \\ R_{pu} &= \frac{Z_{pu}}{\sqrt{1 + XoR^2}} \end{aligned}$$

A baseline loss can be found from an efficiency at an operating point **S**

$$\begin{aligned} \eta &= \frac{P_o}{P_i} \\ P_i &= P_o + P_{loss} \\ P_{loss} &= P_i - P_o \\ P_{loss} &= \frac{P_o}{\eta} - P_o \\ P_{loss} &= P_o \left(\frac{1}{\eta} - 1 \right) \end{aligned}$$

Loss due to current can be determined using per unit values

$$P_{loadloss} = I^2 R$$





$$R = R_{pu} Z_b$$

$$Z_b = \frac{V_n^2}{S_n}$$

$$I = \frac{S}{V}$$

$$P_{loadloss} = \frac{S^2}{V^2} R_{pu} \frac{V_n^2}{S_n}$$

$$P_{loadloss} = \frac{V_n^2 S^2}{V^2 S_n} R_{pu}$$

This general equation is used when calculating load-based loss later, but given a nominal operating point $V = V_n$.

$$P_{loadloss}|_{V=V_n} = \frac{S^2}{S_n} R_{pu}$$

And since S is typically given as a percentage of S_n , load factor F , the equation simplifies further to

$$P_{loadloss} = F^2 S_n R_{pu}$$

We then find ***P_{noloadloss}*** to use for future loss calculations

$$P_{noloadloss} = P_{loss} - P_{loadloss}$$

