

```
%matplotlib inline
import matplotlib
import seaborn as sns
matplotlib.rcParams['savefig.dpi'] = 144

from static_grader import grader
```

Object-oriented exercises

Introduction

The objective of these exercises is to develop your familiarity with Python's `class` syntax and object-oriented programming. By deepening our understanding of Python objects, we will be better prepared to work with complex data structures and machine learning models. We will develop a `Point` class capable of handling some simple linear algebra operations in 2D.

Exercise 1: `point_repr`

The first step in defining most classes is to define their `__init__` and `__repr__` methods so that we can construct and represent distinct objects of that class. Our `Point` class should accept two arguments, `x` and `y`, and be represented by a string `'Point(x, y)'` with appropriate values for `x` and `y`.

When you've written a `Point` class capable of this, execute the cell with `grader.score` for this question (do not edit that cell; you only need to modify the `Point` class).

```
class Point(object):

    def __init__(self, x, y):
        self.x = x
        self.y = y

    def __repr__(self):
        return 'Point(%s, %s)'%(self.x, self.y)

grader.score.vc__point_repr(lambda points: [str(Point(*point)) for
point in points])
```

```
=====
Your score: 1.0
=====
```

Exercise 2: `add_subtract`

The most basic vector operations we want our `Point` object to handle are addition and subtraction. For two points $(x_1, y_1) + (x_2, y_2) = (x_1 + x_2, y_1 + y_2)$ and similarly for subtraction. Implement a method within `Point` that allows two `Point` objects to be added together using the `+` operator, and likewise for subtraction. Once this is done, execute the

grader.score cell for this question (do not edit that cell; you only need to modify the Point class.)

(Remember that `__add__` and `__sub__` methods will allow us to use the + and - operators.)

```
class Point(object):

    def __init__(self, x, y):
        self.x = x
        self.y = y

    def __repr__(self):
        return 'Point(%s, %s)'%(self.x, self.y)

    def __add__(self1, self2):
        return Point(self1.x + self2.x, self1.y + self2.y)

    def __sub__(self1, self2):
        return Point(self1.x - self2.x, self1.y - self2.y)
```

```
from functools import reduce
def add_sub_results(points):
    points = [Point(*point) for point in points]
    return [str(reduce(lambda x, y: x + y, points)),
            str(reduce(lambda x, y: x - y, points))]
```

```
grader.score.vc__add_subtract(add_sub_results)
```

```
=====
Your score:  1.0
=====
```

Exercise 3: multiplication

Within linear algebra there's many different kinds of multiplication: scalar multiplication, inner product, cross product, and matrix product. We're going to implement scalar multiplication and the inner product.

We can define scalar multiplication given a point P and a scalar a as

$$aP = a(x, y) = (ax, ay)$$

and we can define the inner product for points P, Q as

$$P \cdot Q = (x_1, y_1) \cdot (x_2, y_2) = x_1 x_2 + y_1 y_2$$

To test that you've implemented this correctly, compute $2(x, y) \cdot (x, y)$ for a `Point` object. Once this is done, execute the `grader.score` cell for this question (do not edit that cell; you only need to modify the `Point` class.)

(Remember that `__mul__` method will allow us to use the `*` operator. Also don't forget that the ordering of operands matters when implementing these operators.)

```
class Point(object):

    def __init__(self, x, y):
        self.x = x
        self.y = y

    def __repr__(self):
        return 'Point(%s, %s)'%(self.x, self.y)

    def __add__(self, other):
        return Point(self.x + other.x, self.y + other.y)

    def __sub__(self, other):
        return Point(self.x - other.x, self.y - other.y)

    def __mul__(self, a):
        return Point(a*self.x, a*self.y)

    def __mul__(self, other):
        return self.x*other.x+self.y*other.y
```

```
def mult_result(points):
    points = [Point(*point) for point in points]
    return [point*point*2 for point in points]
```

```
grader.score.vc__multiplication(mult_result)
```

```
=====
Your score:  1.0
=====
```

Exercise 4: Distance

Another quantity we might want to compute is the distance between two points. This is generally given for points $P_1 = (x_1, y_1)$ and $P_2 = (x_2, y_2)$ as

$$D = |P_2 - P_1| = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}.$$

Implement a method called `distance` which finds the distance from a point to another point.

Once this is done, execute the `grader.score` cell for this question (do not edit that cell; you only need to modify the `Point` class.)

Hint

- You can use the `sqrt` function from the `math` package.

```
from math import sqrt
```

```
class Point(object):
```

```
    def __init__(self, x, y):
        self.x = x
        self.y = y
```

```
    def distance(self, other):
        return sqrt((self.x-other.x)**2 + (self.y-other.y)**2)
```

```
    def __repr__(self):
        return 'Point(%s, %s)'%(self.x, self.y)
```

```
    def __add__(self, other):
        return Point(self.x + other.x, self.y + other.y)
```

```
    def __sub__(self, other):
        return Point(self.x - other.x, self.y - other.y)
```

```
    def __mul__(self, a):
        return Point(a*self.x, a*self.y)
```

```
    def __mul__(self, other):
        return self.x*other.x+self.y*other.y
```

```
    def __truediv__(self, p):
        self.x = self.x / p
        self.y = self.y / p
        return self
```

```
def dist_result(points):
    points = [Point(*point) for point in points]
    return [points[0].distance(point) for point in points]
```

```
grader.score.vc__distance(dist_result)
```

```
=====
Your score: 1.0
=====
```

Exercise 5: Algorithm

Now we will use these points to solve a real world problem! We can use our Point objects to represent measurements of two different quantities (e.g. a company's stock price and volume). One thing we might want to do with a data set is to separate the points into groups of similar points. Here we will implement an iterative algorithm to do this which will be a specific case of the very general k -means clustering algorithm. The algorithm will require us to keep track of two clusters, each of which have a list of points and a center (which is another point, not necessarily one of the points we are clustering). After making an initial guess at the center of the two clusters, C_1 and C_2 , the steps proceed as follows

1. Assign each point to C_1 or C_2 based on whether the point is closer to the center of C_1 or C_2 .
2. Recalculate the center of C_1 and C_2 based on the contained points.

See [reference](#) for more information.

This algorithm will terminate in general when the assignments no longer change. For this question, we would like you to initialize one cluster at $(1, 0)$ and the other at $(-1, 0)$.

The returned values should be the two centers of the clusters ordered by greatest x value. Please return these as a list of numeric tuples $[(x_1, y_1), (x_2, y_2)]$

In order to accomplish this we will create a class called cluster which has two methods besides `__init__` which you will need to write. The first method `update` will update the center of the Cluster given the points contained in the attribute `points`. Remember, you after updating the center of the cluster, you will want to reassign the points and thus remove previous assignments. The other method `add_point` will add a point to the `points` attribute.

Once this is done, execute the `grader.score` cell for this question (do not edit that cell; you only need to modify the `Cluster` class and `compute_result` function.)

```
class Cluster(object):
    def __init__(self, x, y):
        self.center = Point(x, y)
        self.points = []

    def update(self):
        center_point = Point(0,0)
        count=0
        for point in self.points:
            count+=1
            center_point = center_point + point
        print(len(self.points))
        self.center = center_point/count
        #self.points = []
```

```

def add_point(self, point):
    self.points.append(point)

def compute_result(points):
    points = [Point(*point) for point in points]
    a = Cluster(1,0)
    b = Cluster(-1,0)
    a_old = []

    for _ in range(10000): # max iterations
        a.points = []
        b.points = []
        for point in points:
            if point.distance(a.center) < point.distance(b.center):
                # add the right point (AP: append the recent point to
the list)
                a.add_point(point)
            else:
                # add the right point
                b.add_point(point)
        if a_old == a.points:
            break

        a_old = a.points
        a.update()
        b.update()

    #return [(x, y)] * 2

```

```
grader.score.vc__k_means(compute_result)
```

24

26

24

26

23

27

None is not of type 'array'

Failed validating 'type' in schema:

```

{'items': {'items': [{'type': 'number'}, {'type': 'number'}],
  'maxItems': 2,
  'minItems': 2,
  'type': 'array'},
  'maxItems': 2,
  'minItems': 2,
  'type': 'array'}

```

On instance:

None

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