# Astronomy from 4 perspectives: the Dark Universe

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## questions: Dark matter and the virial theorem

#### 1. theory behind the virial theorem

- (a) What's the idea of the virial theorem?
- (b) What's the difference to energy conservation?
- (c) For what kind of system can you use the virial theorem?

#### 2. mechanical similarity

- (a) Why is mechanical similarity restricted to potentials of the shape  $\Phi \propto r^{\alpha}$ ?
- (b) Does  $\alpha$  have to be integer?
- (c) What's the generalisation of the Kepler-law for a potential of the form  $\Phi \propto r^{\alpha}$ ?

#### 3. harmonic oscillator

(a) What can you say about different energy types in the harmonic oscillator on average?

### 4. Kepler-problem and planetary motion

- (a) Can you show that Kepler's third law implies that potential and kinetic energy are proportional to each other?
- (b) Is this true in general?

#### 5. virial theorem in galaxies

(a) Could one explain the rotation curves by assuming a different gravitational law?