timeseries-by-decade-plots-and-lms.R

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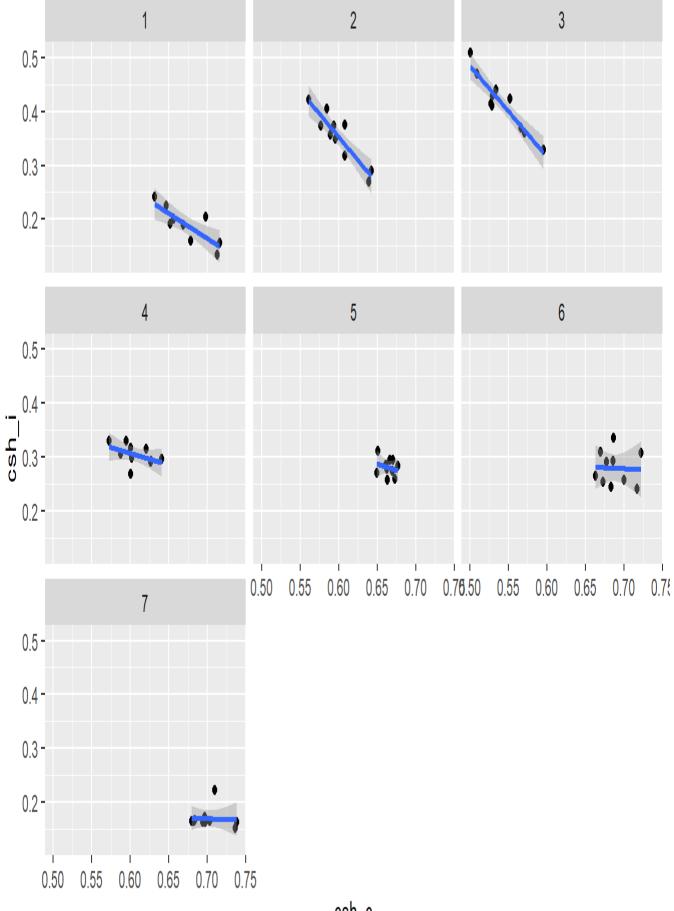
```
library(ggplot2)
## Warning: package 'ggplot2' was built under R version 4.1.3
library(tidyverse)
## Warning: package 'tidyverse' was built under R version 4.1.2
## -- Attaching packages ------------------ tidyverse 1.3.1 --
## v tibble 3.1.2 v dplyr 1.0.7
## v tidyr 1.1.3 v stringr 1.4.0
## v readr 1.4.0 v forcats 0.5.1
## v purrr 0.3.4
## -- Conflicts ------ tidyverse conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag() masks stats::lag()
library(readxl)
## Warning: package 'readxl' was built under R version 4.1.2
pwt100=read excel("C:\\Users\\Alexandros\\Desktop\\STAN\\pwt100.xlsx", sheet="Data")
data=pwt100
numerics=data %>% select if(is.numeric)
df=cbind(data[1:3], numerics) %>% as tibble
rep(1:7, times=1, each=10) %>% as.factor
## Levels: 1 2 3 4 5 6 7
#make decade as factor
df=df %>% group by(country) %>% mutate(decade=as.factor(rep(1:7,times=1,each=10)))
euro=df %>% filter(currency unit=="Euro")
```

```
GR=euro %>% filter(country=="Greece")
##plot scatter by decade
ggplot(GR, aes(csh_c, csh_i)) +
   geom_point() +
   geom_smooth(method=lm)+
   facet_wrap(vars(decade))

## `geom_smooth()` using formula 'y ~ x'

## Warning: Removed 1 rows containing non-finite values (stat_smooth).

## Warning: Removed 1 rows containing missing values (geom_point).
```

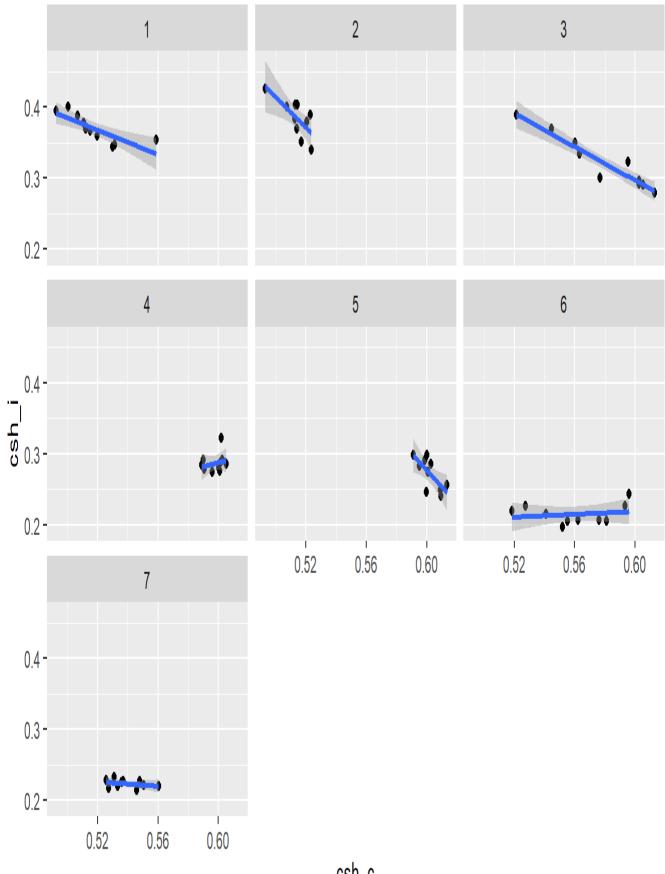


 csh_c

```
## starting httpd help server ...
## done
GR %>% split(.$decade) %>%
                            #split dataframe into 3 based on species
 map(~lm(csh c~csh i,data=.x)) %>%
                                    # run an lm regression on each split dataframe
 map(summary) %>% #Get summary for every model
 map(coef) #get coef
## $`1`
##
                Estimate Std. Error t value
                                                 Pr(>|t|)
## (Intercept) 0.8100461 0.03655589 22.159112 9.633418e-08
## csh i
             -0.7219423 0.19040198 -3.791674 6.788060e-03
##
## $`2`
##
                Estimate Std. Error t value
                                                 Pr(>|t|)
## (Intercept) 0.7700509 0.02748705 28.015045 2.845969e-09
         -0.4814513 0.07718150 -6.237911 2.489515e-04
##
## $`3`
##
                Estimate Std. Error t value
                                                  Pr(>|t|)
## (Intercept) 0.7579739 0.02809703 26.977012 3.838600e-09
## csh i -0.5212690 0.06712635 -7.765491 5.406275e-05
##
## $`4`
##
                Estimate Std. Error t value
                                                 Pr(>|t.|)
## (Intercept) 0.7663516 0.1043811 7.341863 8.056727e-05
            -0.5241465 0.3431524 -1.527445 1.651695e-01
## csh i
##
## $`5`
##
                Estimate Std. Error t value
                                                   Pr(>|t|)
## (Intercept) 0.7018296 0.05163546 13.5920091 8.253666e-07
             -0.1333642 0.18390570 -0.7251773 4.890093e-01
## csh i
##
## $`6`
##
                Estimate Std. Error t value
                                                 Pr(>|t|)
## (Intercept) 0.6950211 0.06114092 11.367526 3.235398e-06
## csh i -0.0258483 0.21767905 -0.118745 9.084049e-01
##
## $`7`
                 Estimate Std. Error
##
                                       t value
                                                    Pr(>|t|)
## (Intercept) 0.70932998 0.06518045 10.8825567 4.499002e-06
              -0.04261789 0.38247232 -0.1114274 9.140224e-01
## csh i
GR %>% split(.$decade) %>% #split dataframe into 3 based on species
 map(~lm(csh c~csh i,data=.x)) %>%
                                    # run an lm regression on each split dataframe
 map(summary) %>% #Get summary for every model
 map("r.squared") #get rsquared
## $`1`
## [1] 0.6725421
##
## $`2`
## [1] 0.8294663
##
## $`3`
## [1] 0.8828746
##
## $`4`
## [1] 0.2257881
##
```

```
## $`5`
## [1] 0.06168066
##
## $`6`
## [1] 0.001759446
##
## $`7`
## [1] 0.001549603
#### correlations for each decade
GR %>% split(.$decade) %>% #split dataframe into 3 based on species
 map(~cor(.x$csh c, .x$csh i))
## $`1`
## [1] NA
##
## $`2`
## [1] -0.9107504
##
## $`3`
## [1] -0.9396141
##
## $`4`
## [1] -0.4751716
##
## $`5`
## [1] -0.2483559
##
## $`6`
## [1] -0.04194575
##
## $`7`
## [1] -0.039365
ggplot(df %>% filter(country=="Germany"), aes(csh_c, csh_i)) +
 geom point() +
 geom smooth(method=lm)+
 facet wrap(vars(decade))+
 ggtitle("Germany")
\#\# `geom smooth()` using formula 'y ~ x'
```

Germany

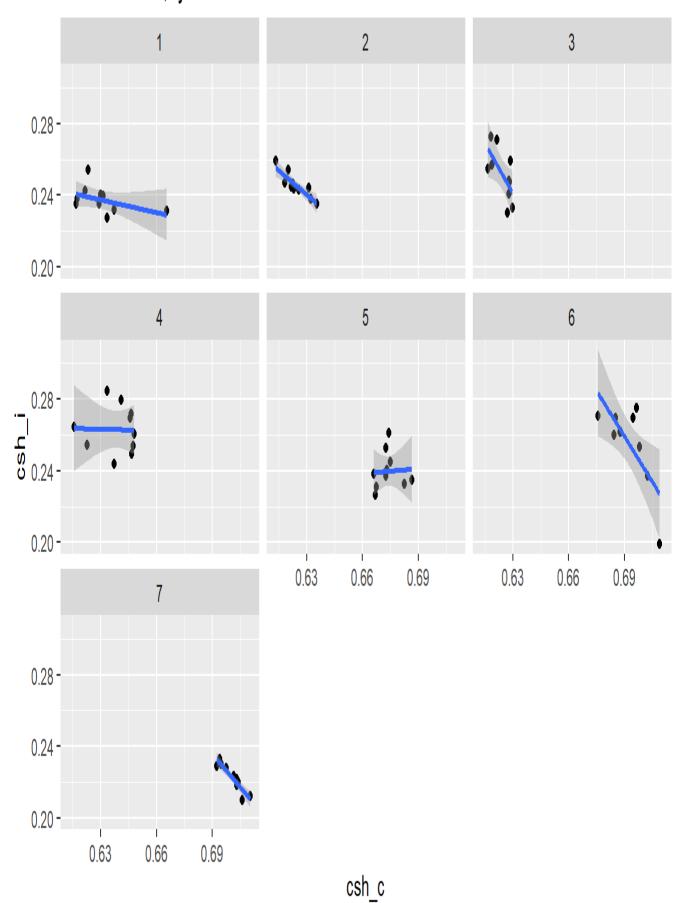


 csh_c

```
ggplot(df %>% filter(country=="United States"), aes(csh_c, csh_i)) +
  geom_point() +
  geom_smooth(method=lm)+
  facet_wrap(vars(decade))+
  ggtitle("United States,by decade 1950-2019")

## `geom_smooth()` using formula 'y ~ x'
```

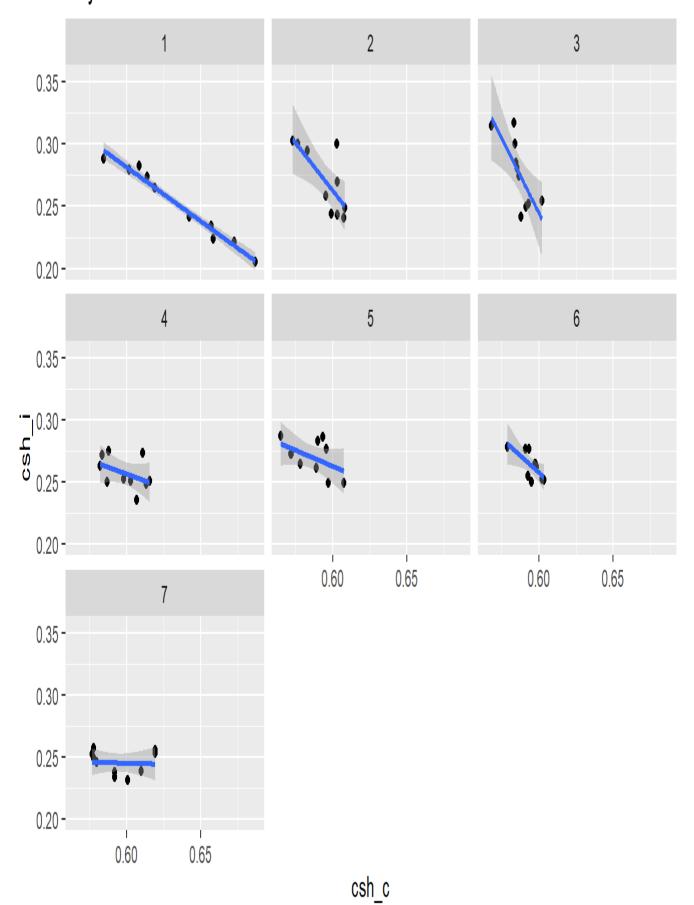
United States, by decade 1950-2019



```
ggplot(df %>% filter(country=="Italy"), aes(csh_c, csh_i)) +
  geom_point() +
  geom_smooth(method=lm)+
  facet_wrap(vars(decade))+
  ggtitle("Italy")

## `geom_smooth()` using formula 'y ~ x'
```

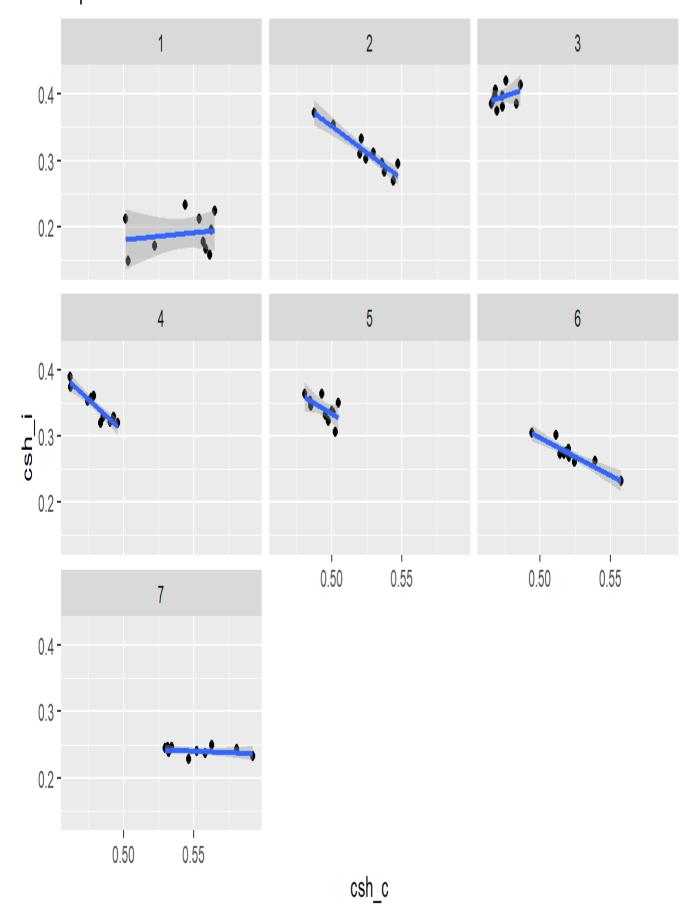
Italy



```
ggplot(df %>% filter(country=="Japan"), aes(csh_c, csh_i)) +
  geom_point() +
  geom_smooth(method=lm)+
  facet_wrap(vars(decade))+
  ggtitle("Japan")

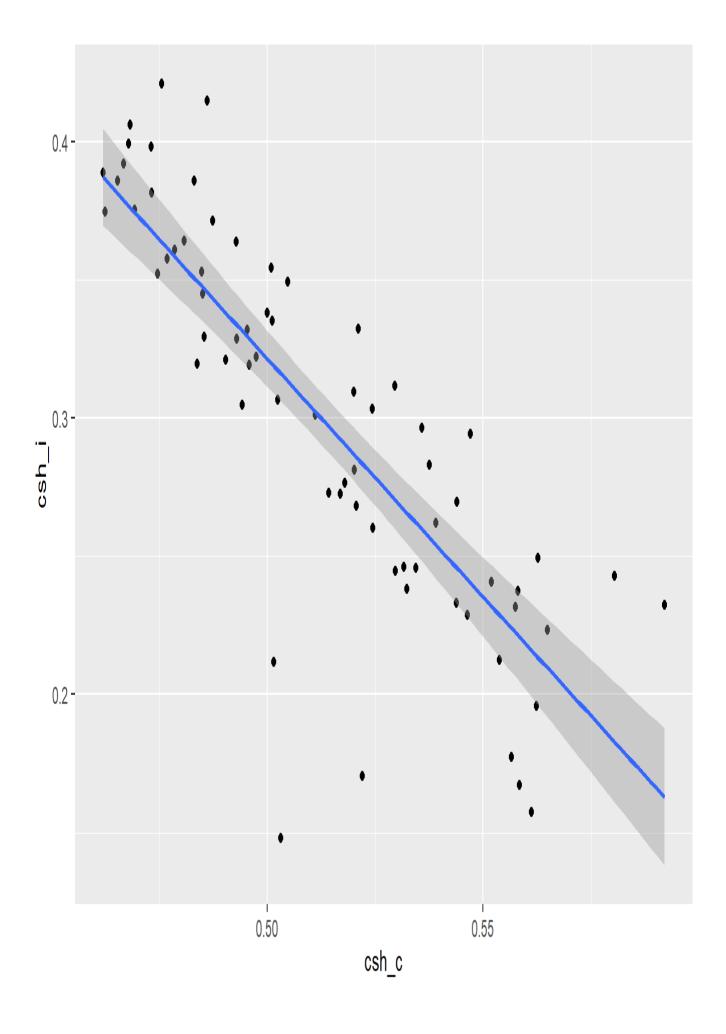
## `geom_smooth()` using formula 'y ~ x'
```

Japan



```
ggplot(df %>% filter(country=="Japan"), aes(csh_c, csh_i)) +
  geom_point() +
  geom_smooth(method=lm)

## `geom_smooth()` using formula 'y ~ x'
```

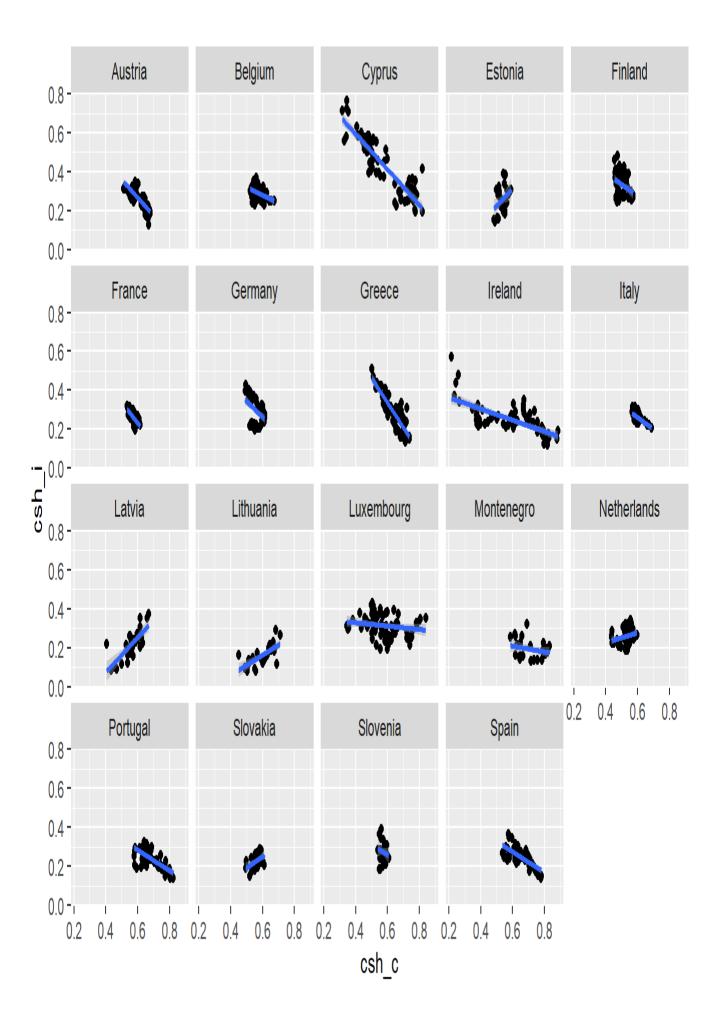


```
ggplot(euro %>% filter(country!="Malta"), aes(csh_c, csh_i)) +
   geom_point() +
   geom_smooth(method=lm)+
   facet_wrap(vars(country))

## `geom_smooth()` using formula 'y ~ x'

## Warning: Removed 241 rows containing non-finite values (stat_smooth).

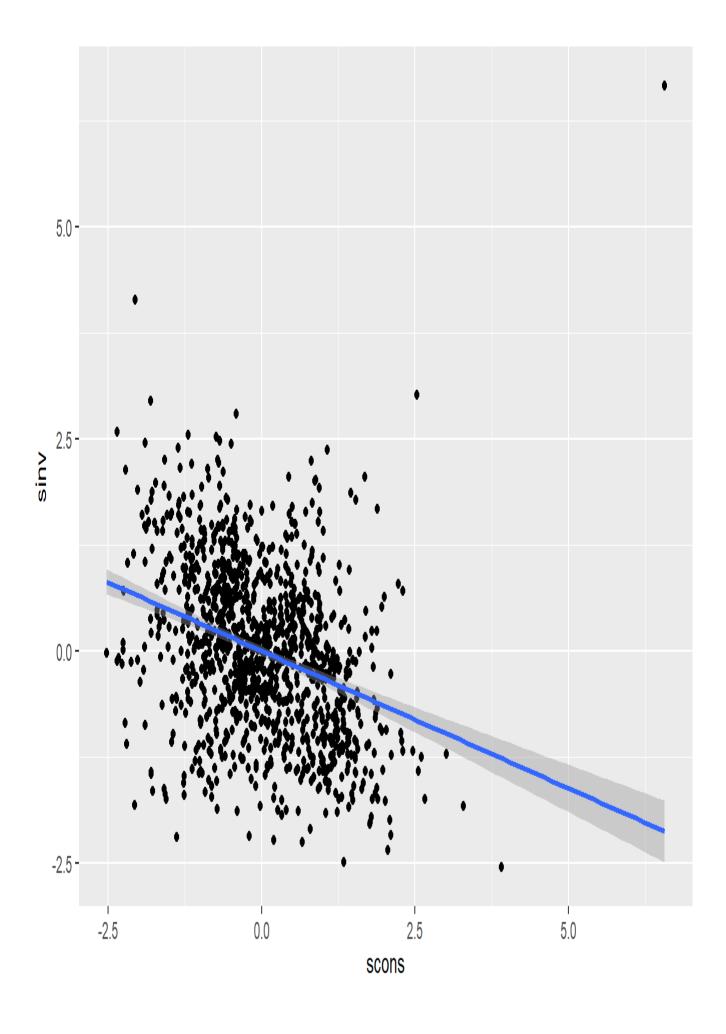
## Warning: Removed 241 rows containing missing values (geom_point).
```



```
seuro
## # A tibble: 1,400 x 50
     countrycode country currency_unit year rgdpe rgdpo pop
                                                                   emp avh
              <chr> <chr> <dbl>
                                              <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
##
     <chr>
## 1 AUT
                 Austria Euro
                                        1950 40357. 41605. 6.98 2.93 2086. 2.55
## 2 AUT
                Austria Euro
                                        1951 41846. 43706. 6.98 2.99 2083. 2.54
## 3 AUT
                                       1952 43858. 44922. 6.97 2.92 2080. 2.52
                Austria Euro
                                       1953 46027. 47309. 6.98 2.89 2078. 2.51
## 4 AUT
                Austria Euro
## 5 AUT
                                       1954 49078. 50658. 6.99 2.98 2075. 2.49
                Austria Euro
## 6 AUT
                                       1955 53920. 55542. 6.99 3.13 2072. 2.48
                Austria Euro
                                       1956 58296. 59630.7.003.22 2070.2.461957 61308. 62760.7.013.30 2067.2.45
## 7 AUT
                 Austria Euro
                 Austria Euro
## 8 AUT
                Austria Euro
## 9 AUT
                                       1958 64192. 65324. 7.03 3.32 2065. 2.43
                 Austria Euro
## 10 AUT
                                       1959 66692. 67548. 7.06 3.37 2062. 2.42
## # ... with 1,390 more rows, and 40 more variables: ccon <dbl>, cda <dbl>,
     cgdpe <dbl>, cgdpo <dbl>, cn <dbl>, ck <dbl>, ctfp <dbl>, cwtfp <dbl>,
      rgdpna <dbl>, rconna <dbl>, rdana <dbl>, rnna <dbl>, rkna <dbl>,
####
###
      rtfpna <dbl>, rwtfpna <dbl>, labsh <dbl>, irr <dbl>, delta <dbl>, xr <dbl>,
      pl_con <dbl>, pl_da <dbl>, pl_gdpo <dbl>, cor_exp <dbl>, statcap <dbl>,
####
      csh_c <dbl>, csh_i <dbl>, csh_g <dbl>, csh_x <dbl>, csh m <dbl>,
####
       csh r <dbl>, pl c <dbl>, pl i <dbl>, pl g <dbl>, pl x <dbl>, pl m <dbl>,
###
      pl n \langle dbl \rangle, pl k \langle dbl \rangle, decade \langle fct \rangle, scons \langle dbl[,1] \rangle, sinv \langle dbl[,1] \rangle
####
#scaled total scatterplot
ggplot(data=seuro, aes(scons, sinv)) +
 geom point()+
 geom smooth (method = lm)
## `geom smooth()` using formula 'y ~ x'
## Warning: Removed 245 rows containing non-finite values (stat smooth).
## Warning: Removed 245 rows containing missing values (geom point).
```

seuro=euro %>% group by(country) %>% mutate(scons=scale(csh c),sinv=scale(csh i)) %>%

ungroup



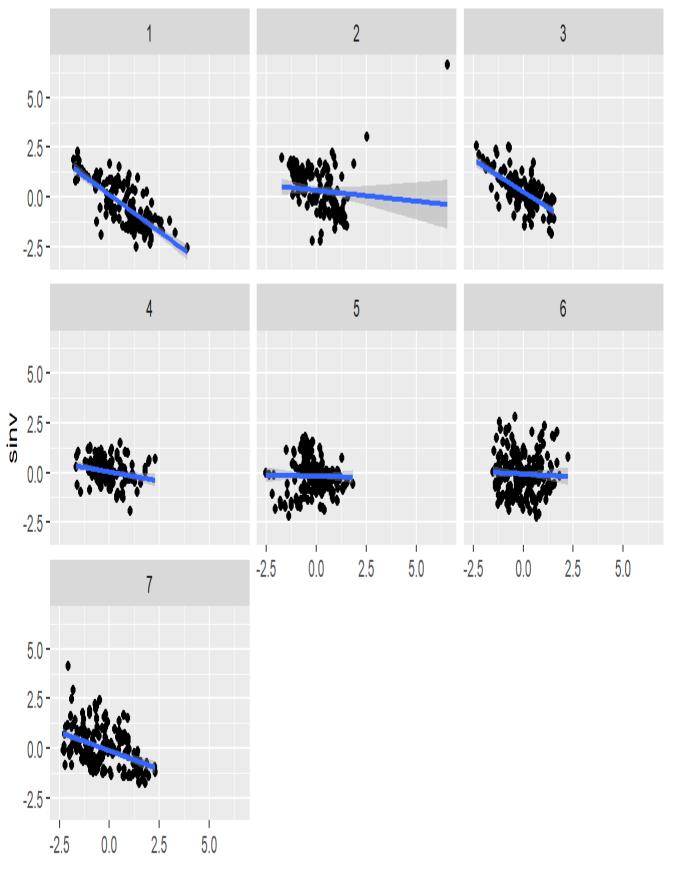
```
ggplot(data=seuro, aes(scons, sinv)) +
  geom_point()+
  geom_smooth(method = lm)+
  facet_wrap(~decade)+
  ggtitle("total scaled")

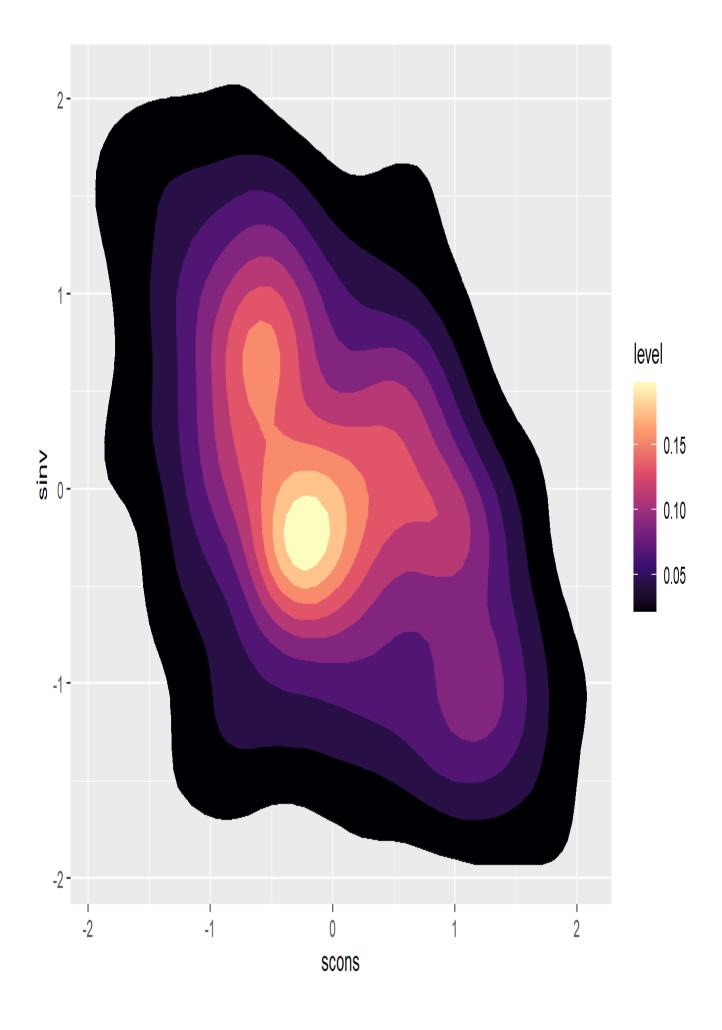
## `geom_smooth()` using formula 'y ~ x'

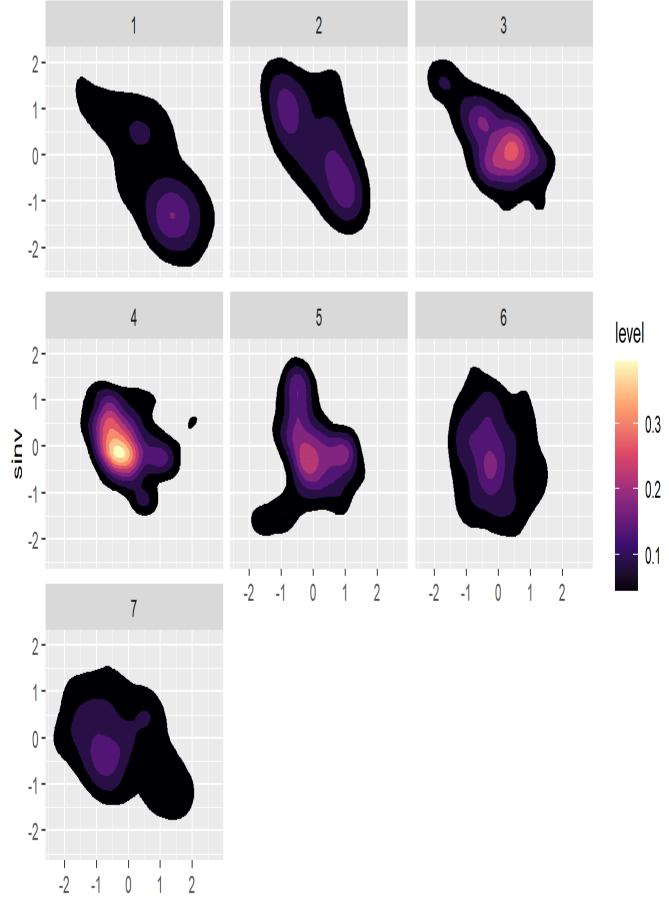
## Warning: Removed 245 rows containing non-finite values (stat_smooth).

## Warning: Removed 245 rows containing missing values (geom_point).
```

total scaled





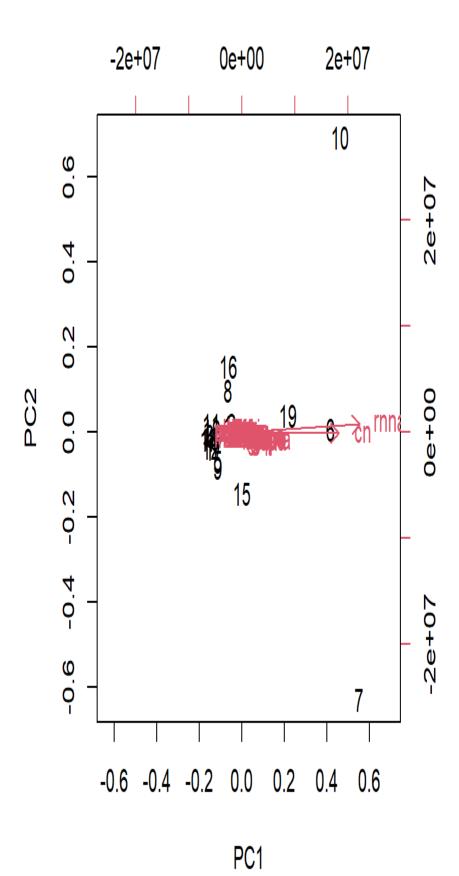


scons

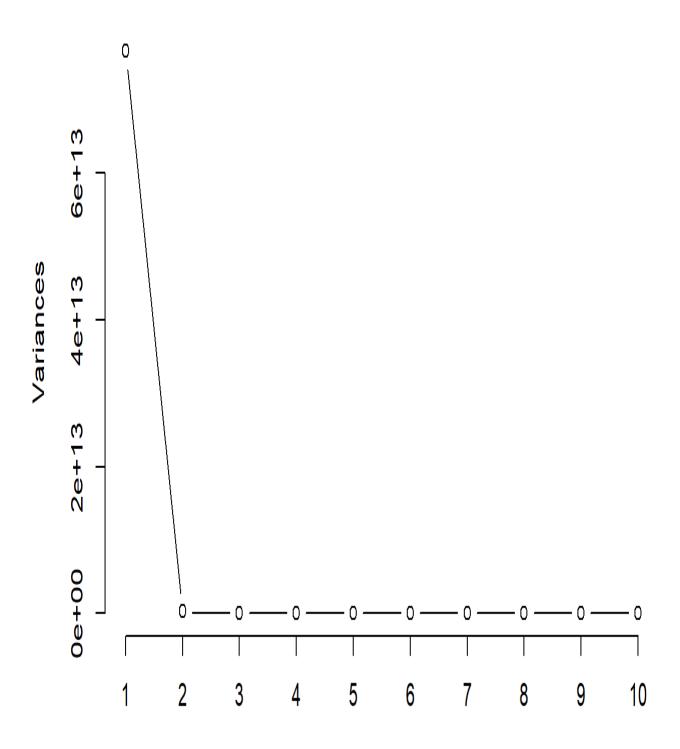
```
###3d print
seuro2=seuro %>%select(scons,sinv) %>% na.omit
den3d <- MASS::kde2d(seuro2$scons, seuro2$sinv)</pre>
# the new part:
library(plotly)
## Warning: package 'plotly' was built under R version 4.1.2
##
## Attaching package: 'plotly'
## The following object is masked from 'package:ggplot2':
##
##
      last plot
## The following object is masked from 'package:stats':
##
##
      filter
## The following object is masked from 'package:graphics':
##
##
      layout
#plot ly(x=den3d$x, y=den3d$y, z=den3d$z) %>% add surface()
df2000=euro %>% filter(year>=2000)
df2000=df2000 %>% select if(is.numeric) %>% summarize all(mean)
### Remove columns and rows with more than 50% NA
\#df2000[which(rowMeans(!is.na(dat)) > 0.5), which(colMeans(!is.na(dat)) > 0.5)]
## Remove rows with more than 50% NA
df2000[which(rowMeans(!is.na(df2000)) > 0.5), ]
## # A tibble: 20 x 45
                                                      hc ccon
##
     country year rgdpe
                           rgdpo pop
                                          emp
                                                avh
                                                                  cda cqdpe
                   <dbl> <</pre>
             <dbl>
##
     <chr>
## 1 Austria 2010. 3.95e5 3.86e5 8.44
                                        4.09 1691. 3.26 2.75e5 3.84e5 3.97e5
                                         4.48 1584. 3.08 3.26e5 4.65e5 4.75e5
   2 Belgium 2010. 4.73e5 4.49e5 10.9
##
##
   3 Cyprus
             2010. 2.74e4 2.36e4 0.797 0.321 1856. 2.72 2.13e4 2.80e4 2.76e4
##
   4 Estonia 2010. 3.37e4 3.21e4 1.34 0.625 1913. 3.47 2.43e4 3.34e4 3.35e4
   5 Finland 2010. 2.25e5 2.22e5 5.36 2.49 1641. 3.32 1.59e5 2.19e5 2.24e5
                                        27.0 1526. 3.05 1.93e6 2.56e6 2.55e6
   6 France
             2010. 2.56e6 2.54e6 64.6
##
   7 Germany 2010. 3.56e6 3.66e6 81.6 41.0 1424.
                                                     3.63 2.57e6 3.37e6 3.56e6
##
             2010. 3.22e5 3.05e5 10.9
                                         4.43 2071.
   8 Greece
##
                                                     2.93 2.73e5 3.42e5 3.19e5
   9 Ireland 2010. 2.57e5 2.73e5 4.40 1.95 1818. 3.02 1.24e5 2.16e5 2.60e5
##
             2010. 2.27e6 2.24e6 59.1 24.7
## 10 Italy
                                               1774. 2.97 1.68e6 2.26e6 2.28e6
## 11 Latvia
            2010. 4.36e4 4.26e4 2.14 0.933 1925. 3.01 3.53e4 4.61e4 4.32e4
## 12 Lithuan~ 2010. 7.26e4 6.75e4 3.15
                                        1.37 1876. 3.13 6.05e4 7.35e4 7.18e4
## 13 Luxembo~ 2010. 4.84e4 3.66e4 0.511 0.354 1538. 3.19 2.11e4 3.34e4 4.88e4
             2010. 1.38e4 1.19e4 0.416 0.171 2073. 2.99 9.79e3 1.28e4 1.38e4
## 14 Malta
## 15 Montene~ 2010. 8.46e3 9.40e3 0.622 0.204 NA NA
                                                          8.63e3 1.05e4 8.30e3
## 16 Netherl~ 2010. 8.13e5 8.33e5 16.6
                                        8.74 1432. 3.27 5.49e5 7.39e5 8.09e5
## 17 Portugal 2010. 3.03e5 2.89e5 10.4
                                         4.92 1885. 2.35 2.42e5 3.16e5 3.03e5
## 18 Slovakia 2010. 1.39e5 1.29e5 5.42 2.22 1762. 3.59 1.06e5 1.36e5 1.37e5
```

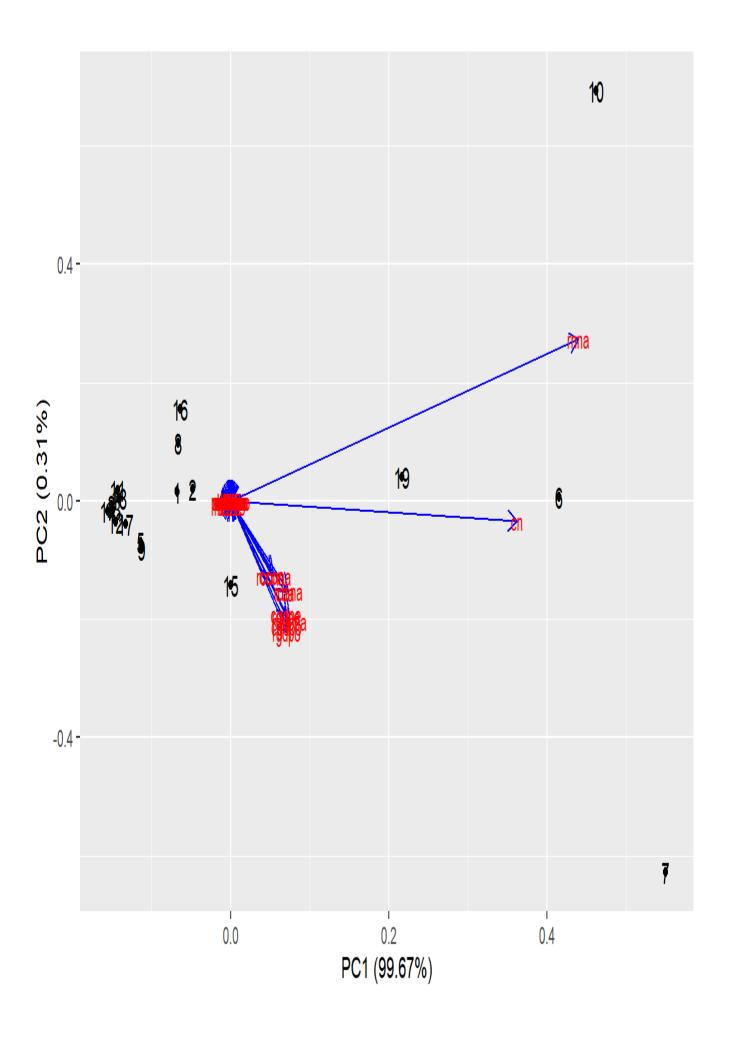
```
## 19 Slovenia 2010. 6.39e4 5.92e4 2.03 0.960 1672. 3.39 4.48e4 6.19e4 6.38e4
            2010. 1.59e6 1.55e6 45.2 18.9 1715. 2.80 1.16e6 1.60e6 1.59e6
## # ... with 34 more variables: cgdpo <dbl>, cn <dbl>, ck <dbl>, ctfp <dbl>,
      cwtfp <dbl>, rgdpna <dbl>, rconna <dbl>, rdana <dbl>, rnna <dbl>,
       rkna <dbl>, rtfpna <dbl>, rwtfpna <dbl>, labsh <dbl>, irr <dbl>,
####
       delta <dbl>, xr <dbl>, pl con <dbl>, pl da <dbl>, pl gdpo <dbl>,
####
       cor exp <dbl>, statcap <dbl>, csh c <dbl>, csh i <dbl>, csh g <dbl>,
       csh x <dbl>, csh m <dbl>, csh r <dbl>, pl c <dbl>, pl i <dbl>, pl g <dbl>,
       pl x <dbl>, pl m <dbl>, pl n <dbl>, pl k <dbl>
####
df2000[which(rowMeans(is.na(df2000)) > 0.5), ] #the rows that are dropped
## # A tibble: 0 x 45
## # ... with 45 variables: country <chr>, year <dbl>, rgdpe <dbl>, rgdpo <dbl>,
       pop <dbl>, emp <dbl>, avh <dbl>, hc <dbl>, ccon <dbl>, cda <dbl>,
       cgdpe <dbl>, cgdpo <dbl>, cn <dbl>, ck <dbl>, ctfp <dbl>, cwtfp <dbl>,
       rgdpna <dbl>, rconna <dbl>, rdana <dbl>, rnna <dbl>, rkna <dbl>,
####
      rtfpna <dbl>, rwtfpna <dbl>, labsh <dbl>, irr <dbl>, delta <dbl>, xr <dbl>,
     pl con <dbl>, pl da <dbl>, pl gdpo <dbl>, cor exp <dbl>, statcap <dbl>,
####
###
     csh c < dbl>, csh i < dbl>, csh g < dbl>, csh x < dbl>, csh m < dbl>,
       csh r <dbl>, pl c <dbl>, pl i <dbl>, pl g <dbl>, pl x <dbl>, pl m <dbl>,
## #
      pl n <dbl>, pl k <dbl>
####PCA
#we want to drop columns for pca, lets say columns with more than 80% nas
df2000=df2000[, which(colMeans(!is.na(df2000)) > 0.8)]
df2000[, which(colMeans(is.na(df2000)) > 0.8)] #columns that are dropped
## # A tibble: 20 x 0
pc=prcomp(df2000 %>% ungroup %>% select(-country) %>% na.omit)
biplot(pc)
## Warning in arrows(0, 0, y[, 1L] * 0.8, y[, 2L] * 0.8, col = col[2L], length =
## arrow.len): zero-length arrow is of indeterminate angle and so skipped
## Warning in arrows(0, 0, y[, 1L] * 0.8, y[, 2L] * 0.8, col = col[2L], length =
## arrow.len): zero-length arrow is of indeterminate angle and so skipped
## Warning in arrows(0, 0, y[, 1L] * 0.8, y[, 2L] * 0.8, col = col[2L], length =
## arrow.len): zero-length arrow is of indeterminate angle and so skipped
## Warning in arrows(0, 0, y[, 1L] * 0.8, y[, 2L] * 0.8, col = col[2L], length =
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## arrow.len): zero-length arrow is of indeterminate angle and so skipped
## Warning in arrows(0, 0, y[, 1L] * 0.8, y[, 2L] * 0.8, col = col[2L], length =
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## Warning in arrows(0, 0, y[, 1L] * 0.8, y[, 2L] * 0.8, col = col[2L], length =
## arrow.len): zero-length arrow is of indeterminate angle and so skipped
## Warning in arrows(0, 0, y[, 1L] * 0.8, y[, 2L] * 0.8, col = col[2L], length =
## arrow.len): zero-length arrow is of indeterminate angle and so skipped
## Warning in arrows(0, 0, y[, 1L] * 0.8, y[, 2L] * 0.8, col = col[2L], length =
## arrow.len): zero-length arrow is of indeterminate angle and so skipped
## Warning in arrows(0, 0, y[, 1L] * 0.8, y[, 2L] * 0.8, col = col[2L], length =
```

```
## arrow.len): zero-length arrow is of indeterminate angle and so skipped
## Warning in arrows(0, 0, y[, 1L] * 0.8, y[, 2L] * 0.8, col = col[2L], length =
## arrow.len): zero-length arrow is of indeterminate angle and so skipped
## Warning in arrows(0, 0, y[, 1L] * 0.8, y[, 2L] * 0.8, col = col[2L], length =
## arrow.len): zero-length arrow is of indeterminate angle and so skipped
## Warning in arrows(0, 0, y[, 1L] * 0.8, y[, 2L] * 0.8, col = col[2L], length =
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## Warning in arrows(0, 0, y[, 1L] * 0.8, y[, 2L] * 0.8, col = col[2L], length =
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## arrow.len): zero-length arrow is of indeterminate angle and so skipped
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## arrow.len): zero-length arrow is of indeterminate angle and so skipped
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## arrow.len): zero-length arrow is of indeterminate angle and so skipped
## Warning in arrows(0, 0, y[, 1L] * 0.8, y[, 2L] * 0.8, col = col[2L], length =
## arrow.len): zero-length arrow is of indeterminate angle and so skipped
## Warning in arrows(0, 0, y[, 1L] * 0.8, y[, 2L] * 0.8, col = col[2L], length =
## arrow.len): zero-length arrow is of indeterminate angle and so skipped
## Warning in arrows(0, 0, y[, 1L] * 0.8, y[, 2L] * 0.8, col = col[2L], length =
## arrow.len): zero-length arrow is of indeterminate angle and so skipped
## Warning in arrows(0, 0, y[, 1L] * 0.8, y[, 2L] * 0.8, col = col[2L], length =
## arrow.len): zero-length arrow is of indeterminate angle and so skipped
## Warning in arrows(0, 0, y[, 1L] * 0.8, y[, 2L] * 0.8, col = col[2L], length =
## arrow.len): zero-length arrow is of indeterminate angle and so skipped
## Warning in arrows(0, 0, y[, 1L] * 0.8, y[, 2L] * 0.8, col = col[2L], length =
## arrow.len): zero-length arrow is of indeterminate angle and so skipped
## Warning in arrows(0, 0, y[, 1L] * 0.8, y[, 2L] * 0.8, col = col[2L], length =
## arrow.len): zero-length arrow is of indeterminate angle and so skipped
## Warning in arrows(0, 0, y[, 1L] * 0.8, y[, 2L] * 0.8, col = col[2L], length =
## arrow.len): zero-length arrow is of indeterminate angle and so skipped
```



screeplot(pc,type="lines") ### See explained variance of PCs





```
PC1
                                                   PC2
                                                                       PC3
                                                                                           PC4
                                                                                                                PC5
## year
                -4.366476e-16 -1.727275e-15 -2.008419e-15 -2.726751e-15 -3.899719e-14
## rgdpe
                 1.163471e-01 -3.211434e-01 1.163559e-01 -1.328551e-02 1.477255e-01
                 1.172742 {\texttt{e}} - 01 \quad -3.671515 {\texttt{e}} - 01 \quad 1.693539 {\texttt{e}} - 01 \quad -2.770090 {\texttt{e}} - 01 \quad -1.714075 {\texttt{e}} - 01
## rgdpo
                 2.848176e-06 -4.167688e-06 -8.327364e-06 2.629758e-05 -4.712103e-06
## pop
                 1.290503 e - 06 - 4.006313 e - 06 - 3.029337 e - 06 - 7.246312 e - 07 - 2.277668 e - 05 - 2.277668 e
## emp
## avh
               -1.038479e-05 1.512420e-04 -2.337976e-04 2.727525e-04 -3.273535e-03
                 2.540704e-09 -3.072211e-07 6.990711e-07 -8.804097e-07 -2.877806e-07
## hc
## ccon
                 8.573486e-02 -2.070590e-01 1.021339e-01 4.129845e-01 -4.800375e-01
                 1.135044e-01 -2.559503e-01 7.243866e-02 4.975738e-01 3.289821e-01
## cda
                 1.164014e-01 -3.176451e-01 1.057651e-01 -4.318799e-02 1.836200e-01
## cgdpe
                 1.165930e-01 -3.510540e-01 1.613542e-01 -3.272559e-01 -1.148388e-01
## cgdpo
                 5.983041e-01 -5.675991e-02 -7.927930e-01 -5.895581e-02 -4.537497e-02
## cn
## ck
                 8.030604e-09 -8.466063e-09 1.138016e-08 -2.068293e-09 1.742033e-08
## ctfp
                 7.066625e-09 -8.106208e-08 9.608801e-08 -8.178140e-07 5.544703e-06
                 4.814915e-09 -3.164508e-08 -2.366525e-08 2.216038e-07 2.839497e-06
## cwtfp
                 1.234594e-01 -3.362229e-01 9.970518e-02 -3.999526e-01 6.846581e-02
## rgdpna
                 8.979034e-02 -2.090417e-01 4.448265e-02
                                                                             3.227053e-01 -5.756507e-01
## rconna
                 1.206294e-01 -2.530717e-01
                                                        2.220571e-02
                                                                             3.583378e-01
                                                                                                 4.741596e-01
## rdana
## rnna
                 7.276740e-01 4.533587e-01
                                                        5.137575e-01 -3.050613e-03 1.639550e-02
## rkna
                 3.039258e-09 3.313567e-08 -7.180455e-08 3.003133e-07 -1.823751e-06
## rtfpna
                 1.902326e-09 4.359484e-08 -1.243772e-07 9.172260e-08 -4.131477e-07
## rwtfpna 8.736138e-10 4.644850e-08 -1.750151e-07 1.809155e-08 -7.014178e-07
                 1.737037e-09 -2.884885e-08 -4.493147e-08 3.742622e-07 -3.016770e-07
## labsh
               -1.095137e-09 2.677633e-09 1.840896e-08 -2.403879e-07 4.687056e-07
## irr
## delta
               -1.801489e-10 -1.588803e-09 6.007999e-09 -3.150416e-08 1.145213e-07
## xr
               -2.022422e - 10 \quad -2.799871e - 09 \quad 1.492465e - 08 \quad 8.516969e - 08 \quad -2.033255e - 08
## pl con
                 7.267624e-09 -3.171664e-08 6.090944e-08 -9.994184e-07 4.838259e-06
## pl da
                7.134561e-09 -4.168964e-08 8.313953e-08 -6.580461e-07 3.717463e-06
## pl gdpo 3.632534e-09 -2.896277e-08 6.522654e-08 -3.981774e-07 2.843473e-06
                                                                             7.376179e-07 -2.780023e-06
## csh c
               -2.267930e-10 4.328989e-08 -1.088801e-07
               -1.265942e-09 1.057156e-08 -3.844380e-08 -7.085273e-08 8.809432e-07
## csh i
               -1.786176e-09 -3.878947e-09 3.956719e-08 3.846073e-07 -9.005556e-07
## csh g
              -6.505380e-09 -1.622521e-07 4.413130e-07 -1.572436e-06 5.620327e-06
## csh_x
## csh m
               1.397178e-08 1.085533e-07 -3.216351e-07 4.138747e-07 -1.738624e-06
## csh r
               -4.187494e-09 3.716290e-09 -1.192122e-08 1.071893e-07 -1.082068e-06
## pl c
               5.731766e-09 -2.895578e-08 2.421739e-08 -8.087134e-07 3.929812e-06
                 5.117599e-09 -8.319329e-08 2.028472e-07 -1.026226e-07 2.208050e-06
## pl i
## pl_g
                 1.162451e-08 -2.993816e-08 1.906994e-07 -1.601432e-06 7.271829e-06
## pl x
                 1.117738e-09 -2.953413e-09 -2.668170e-09 4.834186e-09 1.295574e-07
## pl m
                 3.239846e-09 -1.211877e-08 1.792696e-08 -5.072617e-08 5.394507e-07
## pl n
                 7.208685e-09 -1.170217e-07 2.699284e-07 -2.356048e-07 3.063502e-06
## pl k
                -2.064915e-09 -7.982573e-08 3.758692e-07 -2.322160e-06 6.911738e-06
                                                  PC7
                                                                                           PC9
##
                              PC6
                                                                       PC8
                                                                                                              PC10
## year
                 1.478393e-14 5.801333e-14 -1.014168e-13 4.191867e-13
                                                                                                  7.947580e-13
## rqdpe
               -3.104311e-01
                                     3.795978e-01 -3.323682e-01 -1.445455e-02
                                                                                                 5.312382e-02
## rgdpo
               -2.197147e-01 \quad 1.165772e-02 \quad 4.024816e-01 \quad 5.613985e-01 \quad -4.334429e-01
## pop
               -2.285704e-06 -7.574614e-05 -1.538805e-05 3.635880e-04 4.493174e-04
## emp
                1.116407e-06 -6.637296e-07 -5.193817e-06 2.886894e-04 -1.115458e-05
## avh
                 3.844990e-03 -1.417488e-02 1.248841e-02 4.916988e-02 2.679044e-02
                4.230837e-06 1.571281e-05 2.051514e-06 -1.956271e-05 1.638152e-04
## hc
                                                                             3.362153e-01 4.325317e-01
## ccon
               -2.006999e-01 -3.160898e-01 -2.952356e-01
               -2.245448e - 01 \quad -4.607704e - 01 \quad 3.861856e - 02 \quad -3.153807e - 01 \quad -4.429475e - 01
## cda
               -2.070605e-01 4.572847e-01 -2.752752e-01 -1.483276e-01 5.056309e-02
## cgdpe
## cgdpo
               -9.839852e-02 -2.073715e-01 4.507419e-01 -4.949384e-01 4.622847e-01
## cn
               -6.531931e-02 -1.835673e-02 9.301633e-03 6.169073e-03 5.118780e-03
               -1.360741e-08 9.120535e-08 1.063213e-07 -4.784720e-07 -3.696601e-07
## ck
               -3.616409e-06 7.330663e-07 -7.795766e-06 -6.189053e-05 -3.116637e-06
## ctfp
               -2.204402e-06 3.482849e-06 -5.130768e-06 -3.949264e-05 -3.707357e-06
## cwtfp
## rqdpna
               5.525731e-01 -3.660373e-01 -4.920411e-01 3.157368e-02 -1.210721e-01
               4.320642e-01 3.653716e-01 9.695658e-02 -3.076079e-01 -2.862780e-01
## rconna
## rdana
                 4.640093e-01 1.524353e-01 3.289209e-01 3.272174e-01 3.351928e-01
```

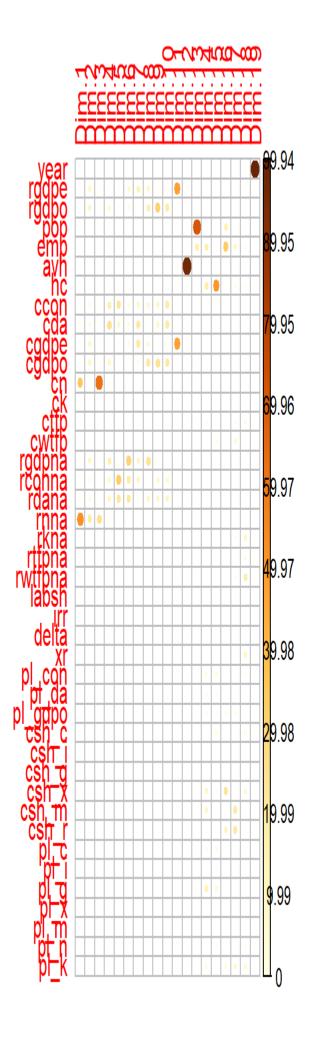
```
2.232495e-02 1.346090e-02 -1.806144e-03 -2.271001e-03 -6.574925e-03
## rnna
          -1.549769e-06 3.530859e-06 2.751946e-06 1.470154e-05 -1.231007e-05
## rkna
## rtfpna -1.761111e-06 1.031309e-06 -5.760995e-06 -1.501540e-05 -1.429555e-05
## rwtfpna -1.767165e-06 -1.767078e-07 -6.486281e-06 -2.677903e-06 -1.148192e-06
         -1.051763e-06 3.657174e-06 1.445844e-07 2.833355e-06 -3.249632e-05
## labsh
## irr
           3.971185e-07 -1.927078e-06 -2.043561e-06 -1.217217e-05 1.767122e-05
## delta
           3.942977e-08 8.512322e-08 4.408314e-08 -1.036601e-06 2.840903e-06
## xr
          -3.660563e-07 1.586986e-06 6.841866e-07 2.583312e-06 3.420782e-05
## pl con -3.705036e-06 5.396334e-06 -1.095341e-05 -1.194103e-04 -7.224782e-05
          -3.282417e-06 5.064697e-06 -6.742625e-06 -9.260731e-05 -6.242691e-05
## pl da
## pl qdpo -2.446467e-06 9.207358e-06 -2.947344e-05 -1.331784e-04 -7.471416e-05
         8.437801e-07 3.766326e-07 2.853300e-06 2.559398e-05 8.662035e-06
## csh c
         5.081183e-07 9.256502e-07 -2.338592e-06 -1.420131e-05 -1.963636e-05
## csh i
         1.481632e-08 1.961010e-07 3.007615e-06 1.439922e-05 1.427318e-05
## csh g
          -3.754657e-06 2.548007e-05 8.754555e-06 -2.769745e-05 6.353788e-06
## csh x
         1.427819e-06 -2.731608e-05 1.611695e-05 4.057127e-05 1.521558e-05
## csh m
          9.601227e-07 3.376312e-07 -2.839383e-05 -3.866572e-05 -2.486821e-05
## csh r
          -2.733546e-06 2.583878e-06 -3.707053e-06 -9.446302e-05 -5.381836e-05
## pl c
## pl_i
          -1.752322e-06 3.109072e-06 -1.104501e-06 -4.428359e-05 -2.795571e-05
## pl_g
          -5.242987e-06 1.390815e-05 -3.391663e-05 -1.901431e-04 -1.209187e-04
          1.457665e-07 7.494887e-07 2.725898e-07 -4.877600e-06 3.318434e-06
## pl x
          -3.999620e-07 5.741779e-07 6.835328e-07 -4.401839e-06 -4.863967e-06
## pl m
         -2.015864e-06 4.704517e-06 -4.938414e-06 -5.109968e-05 -3.731133e-05
## pl n
          5.900560e-07 -1.098865e-05 -2.542690e-05 -1.559986e-04 7.820883e-05
## pl k
##
                  PC11
                               PC12
                                      PC13
                                                      PC14
## year
          -2.232416e-13 -7.245130e-13 -7.378692e-10 -6.784694e-10 -9.109630e-10
          6.914139e-01 -1.256064e-01 -6.285693e-04 2.300326e-04 -1.159978e-04
## rgdpe
## rgdpo
          -4.876413e-02 2.881405e-02 2.076456e-04 -5.243844e-05 9.945479e-05
## pop
          -3.620326e-04 2.492405e-03 -8.436345e-01 3.395855e-02 1.392686e-01
          -1.952475e-04 1.550505e-03 -4.268275e-01 4.160720e-01 8.319510e-02
## emp
          -1.635986e-01 -9.847366e-01 -2.575011e-03 5.914603e-04 8.985917e-04
## avh
           3.993676e-04 5.207200e-04 2.630743e-02 -4.237564e-01 7.087923e-01
## hc
## ccon
          -9.366804e-02 4.579042e-02 5.632214e-04 1.256959e-05 -1.871440e-05
## cda
          -1.634844e-02 -1.984911e-02 -3.655185e-04 -7.928015e-05 3.342533e-05
         -6.906749e-01 9.713335e-02 4.454962e-04 -2.114332e-04 9.090783e-05
## cadpe
          4.682852e-02 -1.140110e-02 -1.050973e-04 6.917415e-05 -9.212269e-05
## cgdpo
          5.276315e-05 8.733395e-04 1.716524e-05 -1.998995e-06 -9.972313e-07
## cn
           5.804710e-07 -2.245071e-06 7.237647e-04 -3.746515e-04 1.966801e-04
## ck
## ctfp
          -3.732539e-05 -3.498496e-04 2.899498e-02 1.484696e-01 -3.500528e-02
## cwtfp
         -5.760499e-05 -3.589816e-04 4.042854e-02 1.176802e-01 -2.039134e-01
## rgdpna
         6.099375e-03 -1.959091e-03 -2.641547e-05 -3.371396e-05 1.068677e-05
           5.901296e-02 -3.333411e-02 -4.054518e-04 -1.341284e-05 7.494143e-06
## rconna
           3.191352e-02 2.242129e-02 3.565511e-04 7.527740e-05 -2.430485e-05
## rdana
           2.224741e-04 -5.740667e-04 -1.142674e-05 9.475977e-07 1.143710e-06
## rnna
           3.958581e-05 2.838619e-04 2.264576e-02 4.351822e-02 2.177331e-02
## rkna
## rtfpna -1.651041e-05 4.631779e-05 4.760935e-02 6.544778e-02 6.312474e-02
## rwtfpna -4.615896e-05 -9.562252e-05 4.054568e-02 5.596635e-02 3.634506e-02
## labsh 1.326228e-05 2.921181e-04 1.057138e-02 -1.630270e-02 -1.188181e-02
          -3.171449e-05 -2.273526e-04 -2.427475e-03 9.273838e-03 -1.578590e-02
## irr
         -1.306064e-06 -3.298122e-05 -2.262036e-04 -4.236057e-03 4.344536e-03
## delta
          -1.235782e-05 4.993837e-05 -1.736895e-02 1.098440e-02 4.604245e-02
## xr
          7.689371e-08 8.825154e-05 1.170899e-01 2.303789e-01 2.222203e-01
## pl con
          4.831007e-05 3.946739e-05 1.039564e-01 1.929503e-01 1.835103e-01
## pl da
## pl gdpo -2.449873e-05 1.275889e-04 1.171847e-01 1.808561e-01 1.723421e-01
## csh c -4.544404e-05 -4.852222e-05 2.513911e-02 4.486934e-02 -2.312690e-01
## csh i
          -4.473434e-05 1.546941e-04 1.277376e-02 -1.355996e-02 4.916351e-02
         4.804300e-05 -1.321817e-04 -2.579880e-02 -6.264517e-02 -7.172860e-03
## csh g
          -1.927262e-05 -4.537570e-04 -5.979722e-02 -3.403505e-01 1.867406e-01
## csh x
          1.680863e-04 5.915110e-04 5.175213e-03 3.449309e-01 1.170857e-01
\#\# csh m
## csh r
          -1.066783e-04 -1.117441e-04 4.250794e-02 2.675548e-02 -1.145480e-01
## pl c
          1.210312e-05 2.790742e-05 9.138913e-02 1.819135e-01 2.062766e-01
          1.409502e-04 -8.999546e-05 4.719394e-02 9.240432e-02 1.470197e-01
## pl i
          -6.068491e-05 3.152113e-04 1.919089e-01 3.716733e-01 2.708595e-01
## pl g
          -7.976438e-06 1.732729e-05 1.627613e-03 1.322731e-02 8.431212e-03
## pl x
```

```
1.183799e-05 1.009929e-06 7.515154e-03 2.462417e-02 4.831505e-02
## pl m
## pl n
          1.842410e-04 -1.033199e-04 6.022870e-02 1.140738e-01 1.743864e-01
## pl k
          -6.808875e-05 -1.468698e-03 4.320021e-02 2.055153e-01 1.393512e-01
                                PC17
##
                   PC16
                                              PC18
                                                           PC19
           1.636274e-09 2.014296e-09 -2.350880e-09 9.997090e-01
## year
           1.003535e-05 -3.089894e-06 1.406466e-05 -2.040236e-06
## rgdpe
          1.484178e-04 -4.329194e-05 -6.607787e-05 -1.140832e-06
## rgdpo
## pop
          3.765376e-01 1.311890e-01 -7.795455e-02 -3.374239e-03
## emp
          -5.828870e-01 -3.464330e-01 1.735264e-01 4.191066e-03
## avh
         -8.875190e-05 6.373594e-04 6.800332e-04 1.222372e-05
           4.713694e-02 -2.088742e-01 1.588355e-01 1.174005e-02
## hc
          -6.724879e-05 -3.578122e-05 -2.613854e-05 -1.810036e-06
## ccon
          2.276642e-05 2.278641e-05 2.716004e-05 2.108911e-06
## cda
## cgdpe -2.912817e-05 6.345539e-05 1.651838e-05 3.278218e-06
         -1.203793e-04 2.178988e-06 4.853305e-05 1.997160e-07
## cgdpo
## cn
          -9.047980e-07 -1.443779e-06 -7.709613e-07 -3.876259e-08
          -3.452713e-04 4.160996e-04 4.567109e-04 -2.117623e-05
## ck
## ctfp
          -1.018331e-01 -1.876476e-01 -2.444449e-01 3.063934e-03
         -4.501327e-02 -2.681237e-01 1.415862e-01 3.407149e-03
## cwtfp
## rgdpna -7.410202e-07 1.100951e-05 -2.089597e-06 1.701581e-07
## rconna 4.318605e-05 3.810590e-05 1.688909e-05 1.339926e-06
## rdana -2.129868e-05 -5.005181e-05 -2.767619e-05 -2.078496e-06
          1.424200e-06 6.466405e-07 3.227674e-07 2.599490e-08
## rnna
         -4.523427e-02 1.473750e-01 -3.528336e-01 4.374945e-03
## rkna
## rtfpna -9.365752e-02 1.364784e-01 2.540609e-01 -2.170661e-03
## rwtfpna -5.162775e-02 -1.645420e-01 -4.199859e-01 8.637628e-04
## labsh -1.298695e-01 -1.814097e-01 4.749321e-02 -3.095176e-03
## irr
          1.672077e-02 -1.041785e-01 -6.460188e-02 8.814544e-05
          -6.187551e-03 -4.821907e-02 1.096313e-03 -8.037652e-04
## delta
## xr 4.154493e-02 -4.821118e-02 3.512889e-01 -4.301650e-03
## pl con -1.276120e-03 1.567839e-02 -1.453142e-01 -2.354362e-03
## pl da 2.867735e-03 -8.638830e-03 -9.579640e-04 -3.242954e-03
## pl gdpo 1.744884e-01 -1.715693e-01 1.277775e-01 -5.628840e-03
## csh c -1.296662e-02 4.159611e-02 2.264090e-01 6.003198e-03
        4.507514e-02 -5.458544e-02 1.501292e-01 -3.626314e-03
## csh i
## csh g
         5.350314e-02 -8.586889e-03 2.732941e-02 -7.950494e-04
         -4.852659e-01 3.796824e-02 -2.796943e-01 -1.041469e-02
## csh x
           3.205558e-02 4.468180e-01 -8.236526e-02 9.071973e-03
## csh m
## csh r
          3.675986e-01 -4.632100e-01 -4.180813e-02 -2.447369e-04
          1.465809e-02 -1.417191e-02 -1.129571e-01 -3.039920e-03
## pl c
## pl i
          3.333309e-02 5.766974e-02 1.354596e-01 -3.624924e-03
          1.799504e-02 1.325385e-01 4.268035e-02 -2.200002e-03
## pl g
          1.812344e-02 -1.050287e-01 1.095261e-01 -2.091920e-03
## pl x
          -1.104390e-02 -2.041071e-02 6.207389e-02 -1.877953e-03
## pl m
         1.268052e-02 1.241190e-01 1.947861e-01 -4.012248e-03
## pl n
           2.490620e-01 -3.131662e-01 -2.793722e-01 -1.102114e-03
## pl k
pc$scale
## [1] FALSE
####### to see variable importance
varpc=factoextra::get pca var(pc)
varpc
```

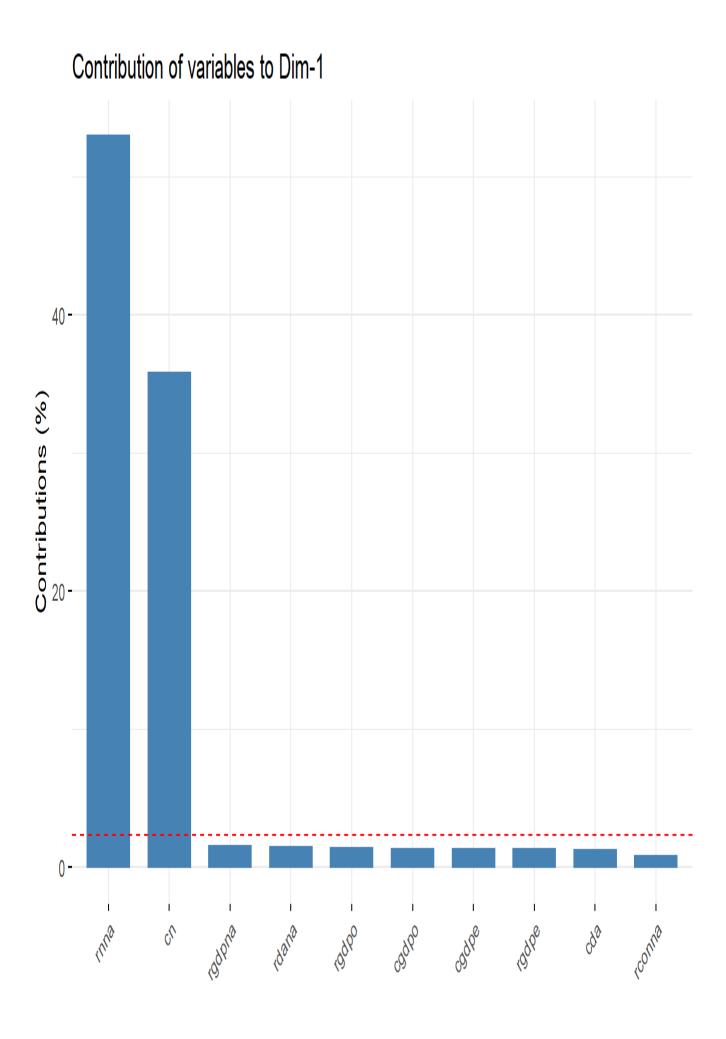
```
Dim.1
                               Dim.2
                                            Dim.3
                                                         Dim.4
                                                                      Dim.5
## year
          1.906611e-29 2.983481e-28 4.033747e-28 7.435170e-28 1.520781e-25
## rqdpe
         1.353664e+00 1.031331e+01 1.353870e+00 1.765046e-02 2.182283e+00
## rgdpo 1.375324e+00 1.348002e+01 2.868075e+00 7.673396e+00 2.938054e+00
          8.112105e-10 1.736962e-09 6.934500e-09 6.915628e-08 2.220392e-09
## pop
          1.665399e-10 1.605054e-09 9.176885e-10 5.250903e-11 5.187770e-08
## emp
## avh
          1.078438e-08 2.287415e-06 5.466133e-06 7.439395e-06 1.071603e-03
## hc
          6.455176e-16 9.438480e-12 4.887004e-11 7.751212e-11 8.281766e-12
          7.350467e-01 4.287343e+00 1.043133e+00 1.705562e+01 2.304360e+01
## ccon
         1.288326e+00 6.551055e+00 5.247360e-01 2.475797e+01 1.082292e+01
## cda
## cgdpe 1.354928e+00 1.008984e+01 1.118626e+00 1.865202e-01 3.371632e+00
          1.359394e+00 1.232389e+01 2.603519e+00 1.070964e+01 1.318795e+00
## cgdpo
## cn
           3.579678e+01 3.221688e-01 6.285207e+01 3.475788e-01 2.058888e-01
## ck
          6.449060e-15 7.167422e-15 1.295080e-14 4.277837e-16 3.034679e-14
## ctfp
          4.993719e-15 6.571061e-13 9.232906e-13 6.688197e-11 3.074373e-09
## cwtfp
         2.318341e-15 1.001411e-13 5.600441e-14 4.910825e-12 8.062742e-10
## rgdpna 1.524222e+00 1.130459e+01 9.941123e-01 1.599621e+01 4.687567e-01
## rconna 8.062305e-01 4.369844e+00 1.978706e-01 1.041387e+01 3.313738e+01
          1.455146e+00 6.404526e+00 4.930936e-02 1.284060e+01 2.248274e+01
## rdana
           5.295094e+01 2.055341e+01 2.639468e+01 9.306240e-04 2.688123e-02
## rnna
          9.237087e-16 1.097973e-13 5.155893e-13 9.018807e-12 3.326069e-10
## rkna
## rtfpna 3.618845e-16 1.900510e-13 1.546968e-12 8.413036e-13 1.706910e-11
## rwtfpna 7.632010e-17 2.157464e-13 3.063030e-12 3.273043e-14 4.919869e-11
## labsh
         3.017297e-16 8.322560e-14 2.018837e-13 1.400722e-11 9.100900e-12
          1.199325e-16 7.169720e-16 3.388897e-14 5.778635e-12 2.196850e-11
## irr
           3.245364e-18 2.524295e-16 3.609605e-15 9.925121e-14 1.311512e-12
## delta
## xr
           4.090191e-18 7.839276e-16 2.227452e-14 7.253876e-13 4.134125e-14
## pl con 5.281836e-15 1.005945e-13 3.709959e-13 9.988371e-11 2.340875e-09
## pl da 5.090196e-15 1.738026e-13 6.912181e-13 4.330247e-11 1.381953e-09
## pl gdpo 1.319531e-15 8.388423e-14 4.254502e-13 1.585453e-11 8.085337e-10
## csh c 5.143504e-18 1.874014e-13 1.185487e-12 5.440802e-11 7.728529e-10
## csh i
         1.602610e-16 1.117578e-14 1.477926e-13 5.020109e-13 7.760609e-11
## csh g
         3.190424e-16 1.504623e-15 1.565563e-13 1.479227e-11 8.110003e-11
## csh_x
         4.231996e-15 2.632575e-12 1.947572e-11 2.472556e-10 3.158808e-09
\#\# csh m
         1.952107e-14 1.178382e-12 1.034492e-11 1.712922e-11 3.022813e-10
## csh r
         1.753510e-15 1.381081e-15 1.421155e-14 1.148955e-12 1.170871e-10
          3.285314e-15 8.384375e-14 5.864818e-14 6.540174e-11 1.544342e-09
## pl c
          2.618982e-15 6.921124e-13 4.114699e-12 1.053140e-12 4.875483e-10
## pl i
          1.351293e-14 8.962934e-14 3.636628e-12 2.564583e-10 5.287949e-09
## pl g
## pl x
          1.249339e-16 8.722647e-16 7.119129e-16 2.336935e-15 1.678513e-12
## pl_m
          1.049660e-15 1.468647e-14 3.213760e-14 2.573144e-13 2.910071e-11
## pl n
          5.196515e-15 1.369407e-12 7.286132e-12 5.550963e-12 9.385042e-10
## pl k
           4.263875e-16 6.372148e-13 1.412777e-11 5.392429e-10 4.777213e-09
                              Dim.7
                                           Dim.8
                                                        Dim.9
##
                 Dim.6
           2.185644e-26 3.365547e-25 1.028537e-24 1.757175e-23 6.316403e-23
## year
## rqdpe
          9.636745e+00 1.440945e+01 1.104686e+01 2.089341e-02 2.822140e-01
          4.827457e+00 1.359024e-02 1.619914e+01 3.151683e+01 1.878728e+01
## rgdpo
## pop
          5.224442e-10 5.737477e-07 2.367921e-08 1.321962e-05 2.018861e-05
## emp
          1.246365e-10 4.405370e-11 2.697574e-09 8.334159e-06 1.244247e-08
          1.478394e-03 2.009274e-02 1.559604e-02 2.417677e-01 7.177274e-02
## avh
## hc
          1.789998e-09 2.468923e-08 4.208709e-10 3.826995e-08 2.683543e-06
          4.028045e+00 9.991278e+00 8.716407e+00 1.130407e+01 1.870837e+01
## ccon
## cda
           5.042036e+00 2.123093e+01 1.491393e-01 9.946496e+00 1.962025e+01
          4.287405e+00 2.091093e+01 7.577644e+00 2.200108e+00 2.556626e-01
## cgdpe
         9.682268e-01 4.300292e+00 2.031683e+01 2.449640e+01 2.137072e+01
## cgdpo
## cn
          4.266612e-01 3.369694e-02 8.652038e-03 3.805746e-03 2.620191e-03
## ck
          1.851616e-14 8.318416e-13 1.130422e-12 2.289354e-11 1.366486e-11
          1.307841e-09 5.373863e-11 6.077396e-09 3.830438e-07 9.713425e-10
## ctfp
         4.859388e-10 1.213024e-09 2.632478e-09 1.559668e-07 1.374449e-09
## cwtfp
## rgdpna 3.053370e+01 1.339833e+01 2.421044e+01 9.968972e-02 1.465845e+00
## rconna 1.866795e+01 1.334964e+01 9.400578e-01 9.462263e+00 8.195511e+00
## rdana 2.153046e+01 2.323652e+00 1.081890e+01 1.070712e+01 1.123542e+01
```

```
4.984033e-02 1.811958e-02 3.262158e-04 5.157446e-04 4.322964e-03
## rnna
          2.401784e-10 1.246697e-09 7.573208e-10 2.161353e-08 1.515378e-08
## rtfpna 3.101513e-10 1.063598e-10 3.318906e-09 2.254621e-08 2.043627e-08
## rwtfpna 3.122872e-10 3.122564e-12 4.207184e-09 7.171167e-10 1.318346e-10
         1.106204e-10 1.337492e-09 2.090464e-12 8.027903e-10 1.056011e-07
## labsh
          1.577031e-11 3.713631e-10 4.176143e-10 1.481617e-08 3.122720e-08
## irr
## delta
         1.554707e-13 7.245963e-13 1.943323e-13 1.074542e-10 8.070729e-10
          1.339972e-11 2.518525e-10 4.681113e-11 6.673502e-10 1.170175e-07
## xr
## pl con 1.372729e-09 2.912042e-09 1.199771e-08 1.425882e-06 5.219748e-07
## pl da 1.077426e-09 2.565116e-09 4.546299e-09 8.576114e-07 3.897119e-07
## pl qdpo 5.985200e-10 8.477545e-09 8.686837e-08 1.773649e-06 5.582205e-07
## csh c 7.119649e-11 1.418521e-11 8.141319e-10 6.550517e-08 7.503085e-09
         2.581842e-11 8.568283e-11 5.469013e-10 2.016771e-08 3.855868e-08
## csh i
## csh g
         2.195235e-14 3.845561e-12 9.045746e-10 2.073376e-08 2.037236e-08
## csh x
         1.409745e-09 6.492339e-08 7.664223e-09 7.671489e-08 4.037062e-09
         2.038667e-10 7.461684e-08 2.597562e-08 1.646028e-07 2.315139e-08
## csh m
         9.218356e-11 1.139948e-11 8.062096e-08 1.495038e-07 6.184281e-08
## csh r
          7.472275e-10 6.676423e-10 1.374224e-09 8.923263e-07 2.896416e-07
## pl c
          3.070632e-10 9.666330e-10 1.219923e-10 1.961036e-07 7.815219e-08
## pl i
## pl_g
          2.748891e-09 1.934366e-08 1.150338e-07 3.615440e-06 1.462132e-06
## pl x
         2.124787e-12 5.617333e-11 7.430521e-12 2.379098e-09 1.101200e-09
## pl m 1.599696e-11 3.296803e-11 4.672171e-11 1.937618e-09 2.365818e-09
## pl n
         4.063709e-10 2.213248e-09 2.438793e-09 2.611178e-07 1.392135e-07
         3.481661e-11 1.207504e-08 6.465272e-08 2.433556e-06 6.116621e-07
## pl k
##
                Dim.11
                          Dim.12 Dim.13 Dim.14
## year
          4.983680e-24 5.249191e-23 5.444509e-17 4.603207e-17 8.298536e-17
         4.780531e+01 1.577696e+00 3.950994e-05 5.291497e-06 1.345550e-06
## rgdpe
         2.377940e-01 8.302496e-02 4.311668e-06 2.749790e-07 9.891255e-07
## rgdpo
         1.310676e-05 6.212082e-04 7.117192e+01 1.153183e-01 1.939574e+00
## pop
          3.812159e-06 2.404067e-04 1.821817e+01 1.731159e+01 6.921425e-01
## emp
          2.676451e+00 9.697061e+01 6.630680e-04 3.498253e-05 8.074670e-05
## avh
## hc
          1.594945e-05 2.711494e-05 6.920810e-02 1.795695e+01 5.023866e+01
          8.773701e-01 2.096763e-01 3.172183e-05 1.579946e-08 3.502288e-08
## ccon
## cda
         2.672714e-02 3.939872e-02 1.336038e-05 6.285343e-07 1.117253e-07
         4.770318e+01 9.434887e-01 1.984669e-05 4.470400e-06 8.264233e-07
## cgdpo
        2.192910e-01 1.299850e-02 1.104545e-06 4.785063e-07 8.486591e-07
## cn
          2.783950e-07 7.627219e-05 2.946454e-08 3.995981e-10 9.944702e-11
          3.369466e-11 5.040346e-10 5.238353e-05 1.403637e-05 3.868306e-06
## ck
          1.393185e-07 1.223947e-05 8.407089e-02 2.204322e+00 1.225370e-01
## ctfp
         3.318335e-07 1.288678e-05 1.634466e-01 1.384864e+00 4.158066e+00
## cwtfp
## rgdpna 3.720238e-03 3.838038e-04 6.977769e-08 1.136631e-07 1.142071e-08
## rconna 3.482529e-01 1.111163e-01 1.643912e-05 1.799042e-08 5.616219e-09
## rdana
         1.018473e-01 5.027143e-02 1.271287e-05 5.666687e-07 5.907255e-08
          4.949472e-06 3.295526e-05 1.305705e-08 8.979414e-11 1.308072e-10
## rnna
## rkna
          1.567036e-07 8.057757e-06 5.128307e-02 1.893835e-01 4.740769e-02
## rtfpna 2.725936e-08 2.145338e-07 2.266650e-01 4.283412e-01 3.984733e-01
## rwtfpna 2.130650e-07 9.143666e-07 1.643952e-01 3.132233e-01 1.320963e-01
## labsh 1.758881e-08 8.533300e-06 1.117541e-02 2.657779e-02 1.411773e-02
          1.005809e-07 5.168921e-06 5.892634e-04 8.600408e-03 2.491947e-02
## irr
## delta
         1.705804e-10 1.087761e-07 5.116807e-06 1.794418e-03 1.887500e-03
          1.527158e-08 2.493841e-07 3.016805e-02 1.206570e-02 2.119907e-01
## xr
## pl con 5.912643e-13 7.788335e-07 1.371004e+00 5.307442e+00 4.938184e+00
## pl da
         2.333863e-07 1.557675e-07 1.080693e+00 3.722983e+00 3.367605e+00
## pl gdpo 6.001879e-08 1.627893e-06 1.373226e+00 3.270893e+00 2.970181e+00
## csh c 2.065161e-07 2.354406e-07 6.319749e-02 2.013258e-01 5.348534e+00
## csh i
         2.001161e-07 2.393027e-06 1.631689e-02 1.838726e-02 2.417051e-01
         2.308130e-07 1.747201e-06 6.655780e-02 3.924417e-01 5.144992e-03
## csh q
          3.714340e-08 2.058955e-05 3.575708e-01 1.158385e+01 3.487207e+00
## csh x
          2.825301e-06 3.498853e-05 2.678283e-03 1.189773e+01 1.370905e+00
## csh m
         1.138027e-06 1.248675e-06 1.806925e-01 7.158554e-02 1.312124e+00
## csh r
          1.464855e-08 7.788242e-08 8.351972e-01 3.309252e+00 4.255004e+00
## pl c
## pl i
          1.986696e-06 8.099183e-07 2.227268e-01 8.538559e-01 2.161481e+00
## pl g
          3.682658e-07 9.935817e-06 3.682903e+00 1.381410e+01 7.336487e+00
         6.362356e-09 3.002349e-08 2.649125e-04 1.749618e-02 7.108534e-03
## pl x
```

```
1.401381e-08 1.019957e-10 5.647754e-03 6.063496e-02 2.334344e-01
## pl m
## pl n
          3.394474e-06\ 1.067500e-06\ 3.627497e-01\ 1.301283e+00\ 3.041061e+00
## pl k
          4.636078e-07 2.157075e-04 1.866258e-01 4.223652e+00 1.941876e+00
##
                 Dim.16
                              Dim.17
                                           Dim.18
                                                        Dim.19
          2.677391e-16 4.057387e-16 5.526635e-16 9.994181e+01
## year
          1.007083e-08 9.547445e-10 1.978148e-08 4.162564e-10
## rgdpe
          2.202783e-06 1.874192e-07 4.366285e-07 1.301497e-10
## rgdpo
## pop
          1.417806e+01 1.721056e+00 6.076912e-01 1.138549e-03
## emp
          3.397572e+01 1.200158e+01 3.011140e+00 1.756504e-03
## avh
          7.876900e-07 4.062271e-05 4.624451e-05 1.494193e-08
          2.221891e-01 4.362845e+00 2.522871e+00 1.378287e-02
## hc
          4.522400e-07 1.280296e-07 6.832235e-08 3.276230e-10
## ccon
          5.183099e-08 5.192203e-08 7.376676e-08 4.447504e-10
## cda
## cgdpe 8.484502e-08 4.026586e-07 2.728568e-08 1.074671e-09
         1.449118e-06 4.747990e-10 2.355457e-07 3.988648e-12
## cgdpo
## cn
          8.186594e-11 2.084499e-10 5.943813e-11 1.502539e-13
## ck
          1.192123e-05 1.731389e-05 2.085848e-05 4.484328e-08
## ctfp
          1.036999e+00 3.521161e+00 5.975331e+00 9.387689e-04
## cwtfp
          2.026194e-01 7.189033e+00 2.004666e+00 1.160866e-03
## rgdpna 5.491110e-11 1.212092e-08 4.366416e-10 2.895379e-12
## rconna 1.865035e-07 1.452060e-07 2.852414e-08 1.795400e-10
          4.536338e-08 2.505184e-07 7.659714e-08 4.320144e-10
## rdana
          2.028345e-10 4.181440e-11 1.041788e-11 6.757350e-14
## rnna
          2.046139e-01 2.171939e+00 1.244915e+01 1.914015e-03
## rkna
## rtfpna 8.771732e-01 1.862637e+00 6.454695e+00 4.711770e-04
## rwtfpna 2.665425e-01 2.707406e+00 1.763882e+01 7.460861e-05
         1.686609e+00 3.290949e+00 2.255605e-01 9.580115e-04
## labsh
## irr
          2.795842e-02 1.085315e+00 4.173403e-01 7.769619e-07
         3.828579e-03 2.325079e-01 1.201901e-04 6.460386e-05
## delta
          1.725981e-01 2.324318e-01 1.234039e+01 1.850419e-03
## xr
## pl con 1.628481e-04 2.458118e-02 2.111620e+00 5.543019e-04
## pl da
          8.223905e-04 7.462939e-03 9.176951e-05 1.051675e-03
## pl gdpo 3.044619e+00 2.943601e+00 1.632710e+00 3.168384e-03
## csh c
         1.681331e-02 1.730236e-01 5.126106e+00 3.603838e-03
         2.031768e-01 2.979570e-01 2.253877e+00 1.315015e-03
## csh i
## csh g
         2.862586e-01 7.373466e-03 7.468968e-02 6.321036e-05
         2.354830e+01 1.441587e-01 7.822890e+00 1.084657e-02
## csh x
## csh m
         1.027560e-01 1.996463e+01 6.784036e-01 8.230070e-03
          1.351288e+01 2.145635e+01 1.747920e-01 5.989613e-06
## csh r
          2.148596e-02 2.008431e-02 1.275931e+00 9.241113e-04
## pl c
## pl i
          1.111095e-01 3.325799e-01 1.834931e+00 1.314007e-03
## pl g
          3.238215e-02 1.756647e+00 1.821612e-01 4.840008e-04
          3.284591e-02 1.103103e+00 1.199597e+00 4.376130e-04
## pl x
          1.219677e-02 4.165969e-02 3.853167e-01 3.526708e-04
## pl m
          1.607957e-02 1.540553e+00 3.794162e+00 1.609813e-03
## pl n
          6.203187e+00 9.807307e+00 7.804882e+00 1.214655e-04
## pl k
library("corrplot")
## Warning: package 'corrplot' was built under R version 4.1.2
## corrplot 0.92 loaded
corrplot(varpc$contrib, is.corr=FALSE)
```



Contributions of variables to PC1
factoextra::fviz_contrib(pc, choice = "var", axes = 1, top = 10)



Contributions of variables to PC2
factoextra::fviz_contrib(pc, choice = "var", axes = 2, top = 10)

Contribution of variables to Dim-2

