

General Expression:-

$$ax^2 + bx + c = 0 \quad [a \neq 0]$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

(1) *If the two roots of a quadratic equation be α & β , then*

$$(a) \alpha + \beta = -\frac{b}{a}$$

$$(b) \alpha\beta = \frac{c}{a}$$

(2) **General structure of a quadratic equation:-**

$$x^2 - (\text{Sum of the roots})x + (\text{Product of the roots}) = 0$$

(3) *Discriminant, $D = b^2 - 4ac$*

Case I:- (When $D > 0$ & a square no.)

The roots will be real, rational & unequal

Case II:- (When $D > 0$ but not a square no.)

The roots will be real, irrational & unequal

Case III:- (When $D = 0$)

The roots will be real & equal

Case IV:- (When $D < 0$)

The roots will be imaginary

(4) *If a, b, c are real & a root of equation (i) be $\alpha + i\beta$, then the other root will be $\alpha - i\beta$ and vice versa (where α, β real).*

(5) *If a, b, c are rational & a root of equation (i) be $p + \sqrt{q}$, then the other root will be $p - \sqrt{q}$ & vice versa (where p, q real).*

(6) *The two roots will be common of two quadratic equation $ax^2 + bx + c = 0$ & $a_1x^2 + b_1x + c_1 = 0$*

$$\text{iff } \frac{a}{a_1} = \frac{b}{b_1} = \frac{c}{c_1}.$$

(7) *The two quadratic equations $ax^2 + bx + c = 0$ & $a_1x^2 + b_1x + c_1 = 0$ will have exactly one common root iff*

$$(a_1c - ac_1)^2 = (ab_1 - a_1b)(bc_1 - b_1c) \text{ \& } \frac{b}{a} \neq \frac{b_1}{a_1} \text{ or } \frac{c}{a} \neq \frac{c_1}{a_1}.$$

Permutation

(1) $n! = n(n-1)(n-2)(n-3) \dots \dots \dots 3.2.1$

(2) $0! = 1$

(3) ${}_nP_r = \frac{n!}{(n-r)!} = \text{No. of permutations of } n \text{ dissimilar things taken } r \text{ at a time}$

(4) $\frac{n!}{p!q!r!} = \text{The permutation of } n \text{ things in which } p \text{ of them to be } a, q \text{ of them to be } b, r \text{ of them to be } c, \text{ and the rest to be unlike.}$

(5) $n^r = \text{The no. of permutations of } n \text{ different things taken } r \text{ at a time, each thing may be repeated once, twice, } \dots \dots \text{ upto } r \text{ times in any arrangement.}$