## Algorithm to Create the PLTS for Memory-Related Deadlocks

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The pseudo-code to create a PLTS  $L = \langle \mathcal{Q}, q_{start}, \mathcal{A}, \mathcal{L} \rangle$  of a mapped workload  $\langle \mathcal{T}, \mathcal{B}, \mathcal{D} \rangle$  is given in Algorithm 1.

Algorithm 1 visits all states that have not been visited yet and, for each of them, adds to  $\mathcal{L}$  new transitions corresponding to valid task start (lines 11 to 27) or end (lines 28 to 40) actions.

If the arrival state of a new transition is new (lines 13 and 30) its memories occupancy is computed (lines 14 to 18 and 31 to 35).

Of course, in a state q, a task can be started only if was a future task in state q, all its immediate predecessor tasks ended (line 11) and all its output buffers can be allocated without overflowing any memory (lines 19 and 24). Similarly a task t can be ended only if it was running (line 28).

For  $\mathbf{start}(t)$  actions the new memories occupancy is computed by considering all output buffers of task t (line 15) and adding their size to the occupancy of their memory (line 17). For  $\mathbf{end}(t)$  actions the new memories occupancy is computed by identifying the input buffers of task t that can be deallocated because all their consumer tasks ended (line 32) and subtracting their size from the occupancy of their memory (line 34).

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1 Function buildPLTS(D = \langle \mathcal{T}, \mathcal{B}, \mathcal{D} \rangle) is
           q_{start} \leftarrow (\emptyset, \emptyset, \mathcal{T}) \, ; \boldsymbol{O_{q_{start}}} \leftarrow 0^n;
 2
                                                                                                     // initial state
           q_{end} \leftarrow (\mathcal{T}, \emptyset, \emptyset); \mathbf{O}_{q_{end}} \leftarrow 0^n;
                                                                                                       // final state
 3
           Q \leftarrow \{q_{start}, q_{end}\};
                                                                                     // initialize set of states
 4
           \mathcal{A} \leftarrow \{\mathbf{start}(t), \mathbf{end}(t) | t \in \mathcal{T}\};
                                                                                                 // set of actions
 5
           \mathcal{L} \leftarrow \emptyset;
                                                                               // initialize set of transitions
 6
          \mathcal{V} \leftarrow \{q_{start}\};
                                                                         // initialize set of states to visit
 7
           while \mathcal{V} \neq \emptyset do
                                                                         // while there are states to visit
 8
 9
                select q \in \mathcal{V};
                                                                                        // pick state q to visit
                \mathcal{V} \leftarrow \mathcal{V} \setminus \{q\};
                                                                                            // mark q as visited
10
                 // for future tasks which predecessors all ended
                 foreach t \in \mathcal{F}_q such that \mathcal{P}_t \subset \mathcal{E}_q do
11
                      // build state r from q by starting task t
                      r \leftarrow (\mathcal{E}_q, \mathcal{R}_q \cup \{t\}, \mathcal{F}_q \setminus \{t\});
12
                      if r \notin \mathcal{Q} then
                                                                                                          // if r new
13
                            // compute memories occupancy
                            O_r \leftarrow O_q;
                                                                                                   // initialization
14
                            foreach b \in \mathcal{O}_t do
                                                                                    // for output buffers of t
15
                                                                                              //\ b memory index
                                 i \leftarrow \mathrm{idx}(b);
16
                                 O_r[i] \leftarrow O_r[i] + \text{size}(b);
                                                                                                // allocate buffer
17
                            end
18
                            if O_r \leq X then
                                                                                   // if no memory overflow
19
                                  Q \leftarrow Q \cup \{r\};
                                                                                                // add new state
20
                                 \mathcal{V} \leftarrow \mathcal{V} \cup \{r\};
                                                                                       // must visit new state
21
                            end
22
                      end
23
                                                                                   // if no memory overflow
                      if O_r \leq X then
24
                           \mathcal{L} \leftarrow \mathcal{L} \cup \{q \xrightarrow{\mathbf{start}(t)} r\};
                                                                                         // add new transition
25
                      end
26
                 \mathbf{end}
27
                 foreach t \in \mathcal{R}_q do
                                                                                            // for running tasks
28
                      // build state r from q by ending task t
                      r \leftarrow (\mathcal{E}_q \cup \{t\}, \mathcal{R}_q \setminus \{t\}, \mathcal{F}_q);
29
                      if r \notin \mathcal{Q} then
                                                                                                          // if r new
30
                            // compute memories occupancy
                            O_r \leftarrow O_q;
                                                                                                    // initialization
31
                            // for input buffers which consumers all ended
                            foreach b \in \mathcal{I}_t such that \mathcal{C}_b \subset \mathcal{E}_r do
32
                                                                                              // b memory index
                                 i \leftarrow \mathrm{idx}(b);
33
                                  O_r[i] \leftarrow O_r[i] - \text{size}(b);
                                                                                             // deallocate buffer
34
                            end
35
                            Q \leftarrow Q \cup \{r\};
                                                                                                // add new state
36
                            \mathcal{V} \leftarrow \mathcal{V} \cup \{r\};
                                                                                       // must visit new state
37
                      end
38
                      \mathcal{L} \leftarrow \mathcal{L} \cup \{q \xrightarrow{\mathbf{end}(t)} r\};
                                                                                         // add new transition
39
40
                end
41
          end
                                                                                                   // return PLTS
          return L = \langle \mathcal{Q}, q_{start}, \mathcal{A}, \mathcal{L} \rangle;
42
43 end
```

**Algorithm 1:** Algorithm to construct the PLTS