otherwise in [c, b].

This is a consequence of the Intermediate Value Theorem, which states that a continuous function on an interval is taking all its intermediate values.

If f(c) < f(d), then f must take a local minimum within [a, d],