The function $f$ is differentiable and the set

$$X_1 := \{x \in \mathbb{R} : f(x) \le f(x_1^{(1)})\}$$

is bounded. Moreover we require the problem

$$\min_\tau f(x + \tau e_i)$$

to have for each $i$ and $x$ a unique solution.