

Let us look at Taylor's theorem as it is valid for a real valued C^2 -function (two time continuous differentiable):

$$f(x+h) = f(x) + h^T f'(x) + \frac{1}{2!} h^T D^2 f(x + \theta h) h$$

with θ being a suitable real in $(0, 1)$.