Definition 1. Functor

A functor F between to categories C and D consists of two functions. One which maps objects from C to objects in D and one which maps morphisms from C to morphisms in D. Moreover, the following must hold:

- (1) for $f \in Hom(A, B)$, $F(f) \in Hom(F(A), F(B))$
- (2) $F(id_A) = id_{F(A)}$
- (3) $F(g \circ f) = F(g) \circ F(f)$