

Restoration in the presence of Noise only- Spatial filtering:

When the only degradation present in an image is noise, i.e.

$$g(x,y)=f(x,y)+\eta(x,y) \text{ or}$$

$$G(u,v)= F(u,v)+ N(u,v)$$

The noise terms are unknown so subtracting them from $g(x,y)$ or $G(u,v)$ is not a realistic approach. In the case of periodic noise it is possible to estimate $N(u,v)$ from the spectrum $G(u,v)$.

So $N(u,v)$ can be subtracted from $G(u,v)$ to obtain an estimate of original image.

Spatial filtering can be done when only additive noise is present. The following techniques can be used to reduce the noise effect:

i) Mean Filter:**ii) (a) Arithmetic Mean filter:**

It is the simplest mean filter. Let S_{xy} represents the set of coordinates in the sub image of size $m*n$ centered at point (x,y) . The arithmetic mean filter computes the average value of the corrupted image $g(x,y)$ in the area defined by S_{xy} . The value of the restored image f at any point (x,y) is the arithmetic mean computed

$$\hat{f}(x,y) = \frac{1}{mn} \sum_{(s,t) \in S_{xy}} g(s,t)$$

using the pixels in the region defined by S_{xy} .

This operation can be using a convolution mask in which all coefficients have value $1/mn$. A mean filter smoothes local variations in image Noise is reduced as a result of blurring. For every pixel in the image, the pixel value is replaced by the mean value of its neighboring pixels with a weight. This will result in a smoothing effect in the image.

(b) Geometric Mean filter:

An image restored using a geometric mean filter is given by the expression

$$\hat{f}(x, y) = \left(\prod_{(s, t) \in S_{xy}} g(s, t) \right)^{1/mn}$$

This filter is useful for finding the darkest point in image. Also, it reduces salt noise of the min operation.

(c) Midpoint filter:

The midpoint filter simply computes the midpoint between the maximum and minimum values in the area encompassed by

$$\hat{f}(x, y) = \left(\max_{(s, t) \in S_{xy}} \{g(s, t)\} + \min_{(s, t) \in S_{xy}} \{g(s, t)\} \right) / 2$$

It combines the order statistics and averaging. This filter works best for randomly distributed noise like Gaussian or uniform noise.

(d) Harmonic Mean filter:

The harmonic mean filtering operation is given by the expression

$$\hat{f}(x, y) = \sum_{(s, t) \in S_{xy}} g(s, t)^{Q+1} / \sum_{(s, t) \in S_{xy}} g(s, t)^Q$$

The harmonic mean filter works well for salt noise but fails for pepper noise. It does well with Gaussian noise also.

(e) Order statistics filter:

Order statistics filters are spatial filters whose response is based on ordering the pixel contained in the image area encompassed by the filter. The response of the filter at any point is determined by the ranking result.

Median filter:

It is the best order statistic filter; it replaces the value of a pixel by the median of gray levels in the Neighborhood of the pixel.

$$\hat{f}(x, y) = \underset{(s,t) \in Sxy}{\text{median}} \{g(s, t)\}$$

The original of the pixel is included in the computation of the median of the filter are quite possible because for certain types of random noise, the provide excellent noise reduction capabilities with considerably less blurring then smoothing filters of similar size. These are effective for bipolar and unipolar impulse noise.

Max and Min filter:

Using the 100th percentile of ranked set of numbers is called the max filter and is given by the equation

$$\hat{f}(x, y) = \underset{(s,t) \in Sxy}{\max} \{g(s, t)\}$$

It is used for finding the brightest point in an image. Pepper noise in the image has very low values, it is reduced by max filter using the max selection process in the sublimated area sky. The 0th percentile filter is min filter.

$$\hat{f}(x, y) = \underset{(s,t) \in Sxy}{\min} \{g(s, t)\}$$

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