(a) For each protein p, we define a set S_p consisting of all proteins similar to it; we do this by simply enumerating all proteins q for which $d(p,q) \leq \Delta$. With respect to these sets, a representative set $R \subseteq P$ is simply a set for which $\{S_p : p \in R\}$ if a set cover for P.

Thus, to approximate the size of the smallest representative set, we can use the approximation algorithm for Set Cover from this chapter, obtaining an approximation guarantee of $O(\log n)$.

(b) The problem with using the approximation algorithm for Center Selection is that we'd obtain a set R of proteins for which every protein is within distance 2Δ of some element of R. But this doesn't satisfy the requirements for a representative, which stipulated that every protein had to be within distance Δ of some element of R.

 $^{^{1}}$ ex815.903.104