

Supermarket Sweep

Adam Profili, Brynn Schneberger

4/25/2021

Project Overview

A contestant in a gameshow has a default of 90 seconds to make their way around a grocery store, collect up to a default of 15 items in their cart, and return to the start. Their score is the total cost of the items in their cart. Items are spread around the following aisles, and each have specific prices and locations.

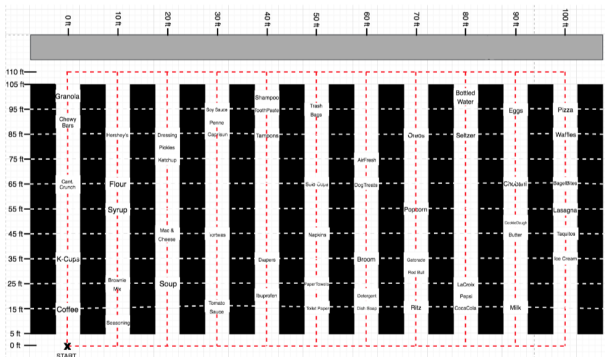


Figure 1: Grocery Store Layout

(a) asks:

For each pair of items $i, j \in \llbracket 1, 56 \rrbracket$, compute the shortest time d_{ij} to go from item i to item j , and store these values. You may not use any optimization software to answer this question. Compute also the shortest time to travel between the start/end location and any item.

(a) solution:

(b) asks:

Formulate the Supermarket Sweep problem as a Mixed-Integer Program.

(b) Data Placeholders:

n represents the number of nodes, with node 1 being the start node, nodes 2,3,..., n being item nodes, and $n+1$ being the end node which shares the attributes of the start node.

T represents the maximum time the contestant is given to shop.

C represents the maximum amount of items the contestant can put in their cart.

v_i represents the value of node i . $\forall i = 1, 2, \dots, n$

d_{ij} represents the minimum time it takes to move from node i to node j . If node j represents an item and not a start/end point, it will include the 2 seconds to add that item to the cart.

$\forall i = 1, 2, \dots, n \quad \forall j = 2, 3, \dots, n + 1$

(c) asks:

Code and solve your optimization model. What is the optimal path? Which items are picked? What is the total value of these items?

(c) solution:

Path Taken:

Node 1: Start Node (0,0)

Node 2: Coffee Beans: \$6.99 at (0,15)

Node 3: K-Cups: \$10.99 at (0,35)

Node 6: Granola: \$5.49 at (0,100)

Node 26: Shampoo: \$8.99 at (40,100)

Node 31: Trash Bags: \$8.99 at (50,95)

Node 36: Air Freshner: \$6.99 at (60,75)

Node 35: Dog Treats: \$3.99 at (60,65)

Node 34: Broom: \$13.99 at (60,35)

Node 33: Detergent: \$12.99 at (60,20)

Node 40: Redbull (4): \$7.99 at (70,30)

Node 39: Gatorade (12): \$6.99 at (70,35)

Node 28: Paper Towels: \$9.99 at (50,25)

(d) asks:

How does the optimal value of the problem vary with respect to the total amount of time allowed (initially set to 90 sec)? Answer this question by plotting and analyzing the optimal value of the problem with different values of the total amount of time that is allowed.

(d) solution:

(e) asks:

How does the optimal value of the problem vary with respect to the capacity of the cart (initially set to 15)? Answer this question by plotting and analyzing the optimal value of the problem with different values of the cart capacity.

(e) solution:

(f) asks:

Consider the initial parameters of the problem (cart of size 15, time allowed of 90 seconds). Gurobi has a parameter called MIPGap. Its default value is 0.0001. This means that Gurobi will output a solution, as soon as its objective value is within 0.01% of the optimal value of the problem. Changing this parameter will influence the time it takes Gurobi to output a solution. What happens if you change this Gurobi parameter for the Supermarket Sweep problem? Answer this question by plotting and analyzing the time Gurobi takes to output a solution with respect to the optimality gap that is allowed.