

List Vs Array

There are two basic ways of storing the sequence of values:

List	Array
Flexible Length	Fixed Size
Easy to modify the structure	Support <code>random access</code>
Values scattered in memory	Allocates <code>contiguous</code> block of memory
<code>Sequence of nodes</code>	
Each node contains value and points to next node in sequence <code>linked list</code>	<code>index-value</code> storage thus random access
Access: takes time proportional to index the elem is located <code>O(n)</code>	Access: <code>constant</code> time independent of index
Insert/Delete: <code>Constant</code>	Insert/Delete: <code>O(n)</code>
Swap: <code>O(n)</code>	Swap: <code>Constant</code>
Good for <code>Insertion Sort</code>	Good for <code>Binary Search</code>
	List in Python are arrays

Implementing Lists in python:

```
class Node:
    def __init__(self, v=None):
        self.value = v    #self.value: None-> empty list
        self.next = None #points to next node
        return

    def isempty(self):
        if self.value == None:
            return(True)
        else:
            return(False)
```

```
# create lists
l1 = Node() # empty list
l2 = Node(5) # Singleton list
```

appending to the list

```
def append(self, v):
    if self.isempty():
        self.value = v
    elif self.next == None:
        self.next = Node(v)
    else:
        self.next.append(v)
    return
```

```
def appendi(self, v):
    # append, iterate
    if self.isempty():
        self.value = v
        return

    temp = self
    while temp.next != None:
        temp = temp.next

    temp.next = Node(v)
    return
```

insert at start of list

```
def insert(self, v):
    if self.isempty():
        self.value = v
        return

    newnode = Node(v)

    # Exchange values in self and newnode
    (self.value, newnode.value) = (newnode.value, self.value)
```

```
# switch the links:
(self.next, newnode.next) = (newnode, self.next)

return
```

Remove first occurrence of v

- Scan for first v- look ahead at next node
- If next node is v: Bypass it!

```
def delete(self, v):
    if self.isempty():
        return

    if self.value == v:
        self.value = None
        if self.next != None:
            self.value = self.next.value
            self.next = self.next.next
        return
    else:
        if self.next != None:
            self.next.delete(v)
            if self.next.value == None:
                self.next = None
```

summary

- Use linked list of nodes to implement a flexible list
- Append is easy
- Insert requires some care, cannot change where the head points to
- When deleting, look one step ahead to bypass the node to be deleted.

List in Python

- **Arrays** - **double space** as and when needed
- Keep track of last position of list in the array
 - `l.append()` and `l.pop()` are **constant time**, amortised **$O(1)$** CHEAP
 - Insertion and deletion requires **$O(n)$** EXPENSIVE
- Useful for representing the matrices
- Need to be careful when initialising multidimensional list:
 - `zero_list = [0,0,0]`
 - `zero_matrix = [zero_list, zero_list, zero_list]`
 - `zero_matrix[1][1] = 1`
 - `[[0,1,0],[0,1,0],[0,1,0]]` Mutability
 - Solution:
 - list comprehension
 - `[[0 for i in range(3)]for j in range(3)]`
 - numpy library

```
import numpy as np
zeromatrix = np.zeros(shape =(3,3))
```

Dictionary in Python

Array/List	Dictionary
Access: Positional Indices	Access: Arbitrary Keys
	Random Access
	Implemented as hash tables

- Underlying storage is `array`
- Keys have to be mapped to $\{0,1,\dots,n-1\}$
 - **Hash Function** : `h: S → X` maps a set of values S to a small range of integers X = $\{0,1,2,\dots,n-1\}$
 - Typically `|X| << |S|` so there will be collisions, `h(s) = h(s') , s ≠ s'`
 - A good hash function will minimise collisions
 - **SHA-256** is an industry standard for the Hashing function whose range is 256 bits
 - lets say `d = dict()`
 - `d[k] = v`
 - hash: `k → h(k)`
 - put v at h(k) position
- How to avoid the collisions:

Open Addressing[Closed Hashing]	open Hashing
Probe a <code>sequence</code> of alternate slots in <code>same array</code>	Each slot in the array points to a list of values
Example: Parking lot: Look for the open slot of parking.	Each position in array store the values in list
	<code>List</code> for each position