

# Search Problem

## Searching in List

```
L = [1,2,3,4,5,6,7,8]

# NAIVE SOLUTION:

# We will scan the list and if element is preset return true

def naivesearch(elem, L):
    for c in L:
        if c == elem:
            return True
    return false
```

Worst Case Scenario:  $O(n)$

## Searching a Sorted List: BINARY SEARCH

What if **L** is sorted in ascending order?

```
def binarysearch(v, l):
    if l == []:
        return False

    m = len(l)/2

    # if v = m then its a midpoint
    if v == l[m]:
        return True

    # search first half as v < m
    if v < l[m]:
        return binarysearch(v, l[:m])

    # search second half if v > m
```

```
else:  
    return binarysearch(v, l[m+1:])
```

How long does this take?

$\log(n)$  : number of times divide  $n$  by 2 to reach 1.

Another approach to this:

$T(n)$  : time to search the list of length  $n$ :

- If  $n == 0$ :  $T(0) = 1$
- If  $n > 0$ :  $T(n//2) + 1$

If we Unwind this:

- $T(n) = T(n//2) + 1$
- $T(n) = (T(n//4) + 1) + 1$
- $T(n) = (T(n//4)) + 1 + 1$
- $T(n) = (T(n//2^k)) + k$
- $T(n) = T(1) + k$  for  $k = \log(n)$
- $T(n) = T(0) + 1 + \log(n) = 2 + \log(n)$