Foundations of Machine Learning for Physicists

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* With (mostly unknowing) help from: Mel Abler, Julie Barnum, Stuart Mumford, James Mason, Monica Bobra, Aurélien Géron, François Chollet, Brandon Rohrer, Theo Wolf and xkcd-font.





Outline

1. The Fundamental Building Blocks

2. Convolutions, Encodering/Decoding and Autoencoders

3. Physics-Informed Neural Networks

Outline

I. The Fundamental Building Blocks
Tutorial!

2. Convolutions, Encodering/Decoding and Autoencoders

Tutorial!

3. Physics-Informed Neural Networks
Tutorial!

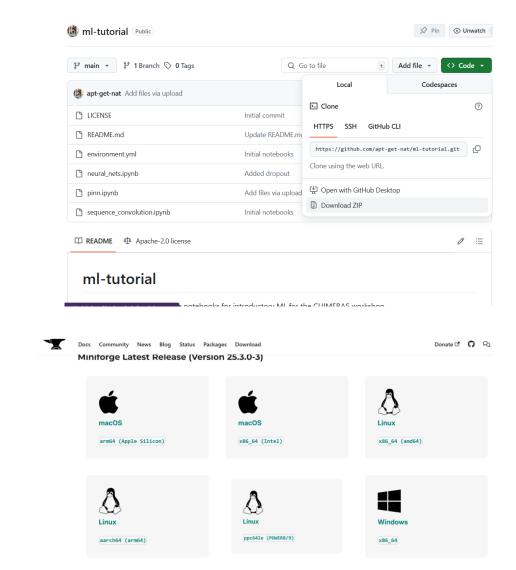
Outline

- I. The Fundamental Building Blocks
 Tutorial!
- 2. Convolutions, Encodering/Decoding and Autoencoders

 Tutorial!
- 3. Panic because we're running out of time (you go home tonight run the) Tutorial!

Instructions to follow along

- This is not a workshop; I don't have time to debug everything. But if you want to follow along, you can!
- https://github.com/apt-get-nat/ml-tutorial
- I recommend you download mini-forge if you haven't, and set up the environment.
 That can take a little while so it's good to do it right away!

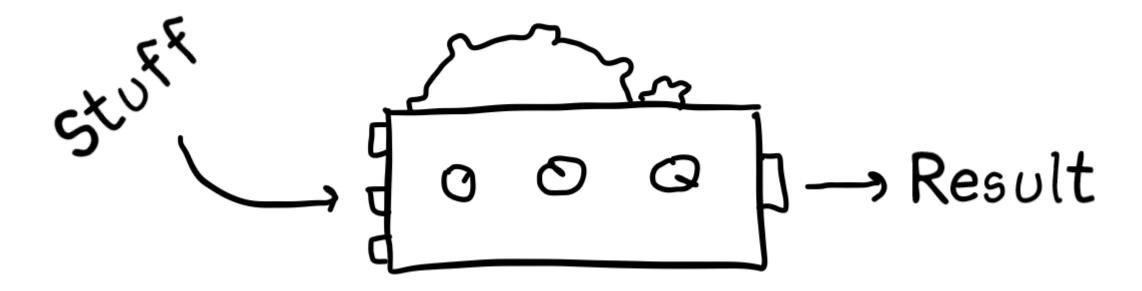


What is Al?

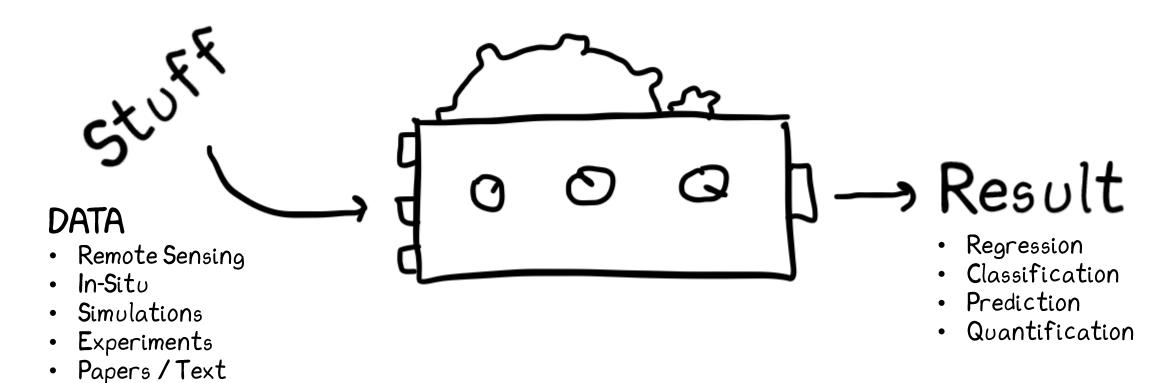
What is Machine Learning?

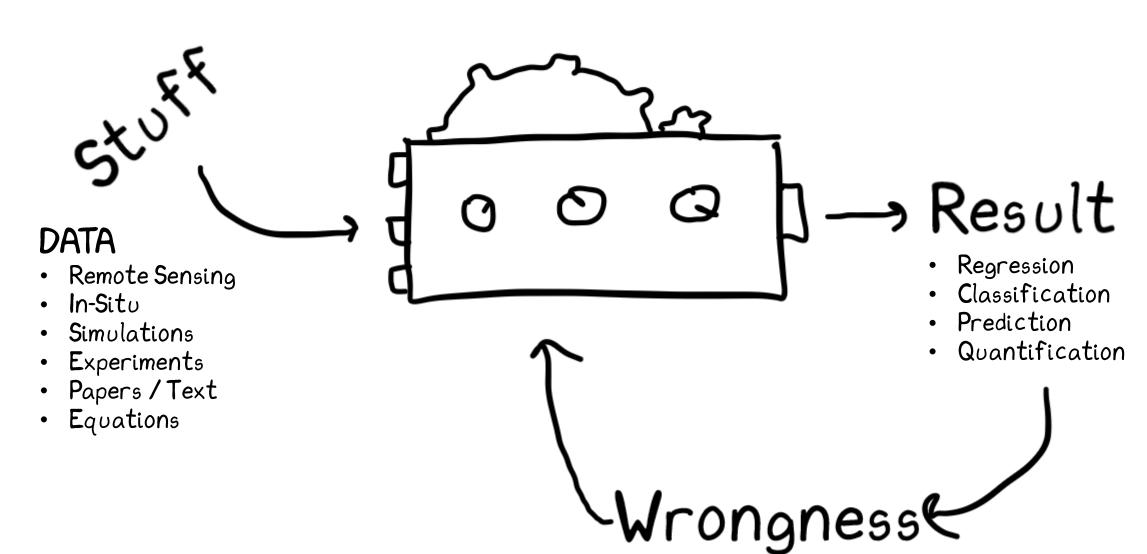
What is a Neural Network?

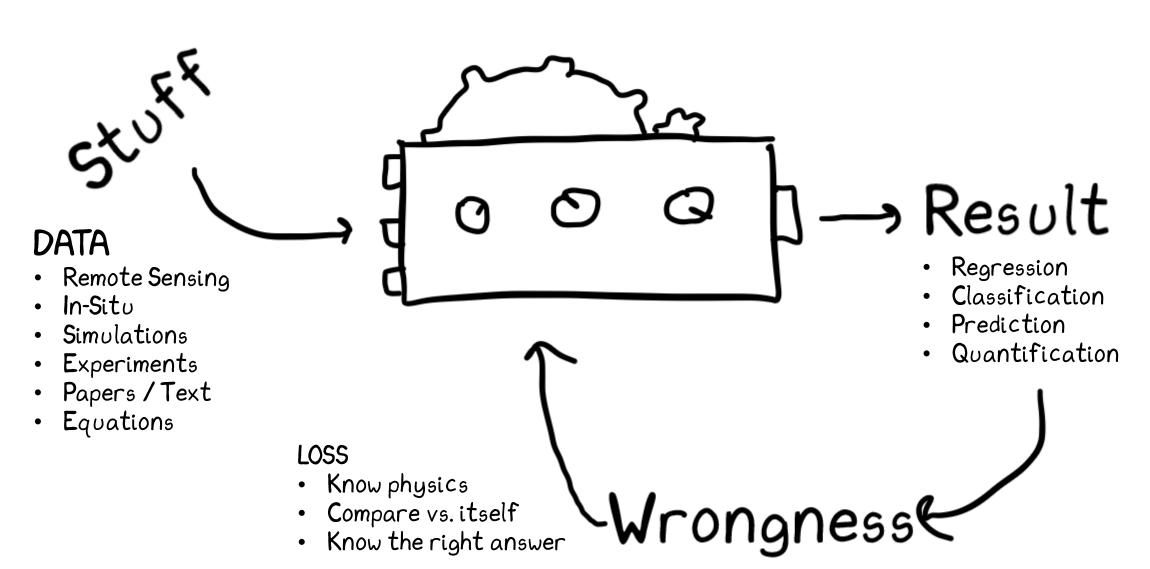
What is this talk even about?

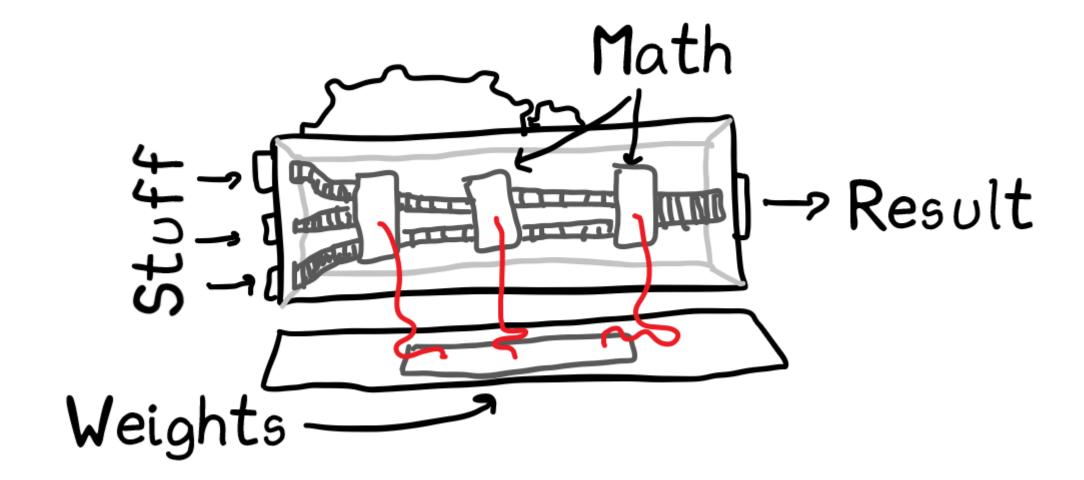


Equations







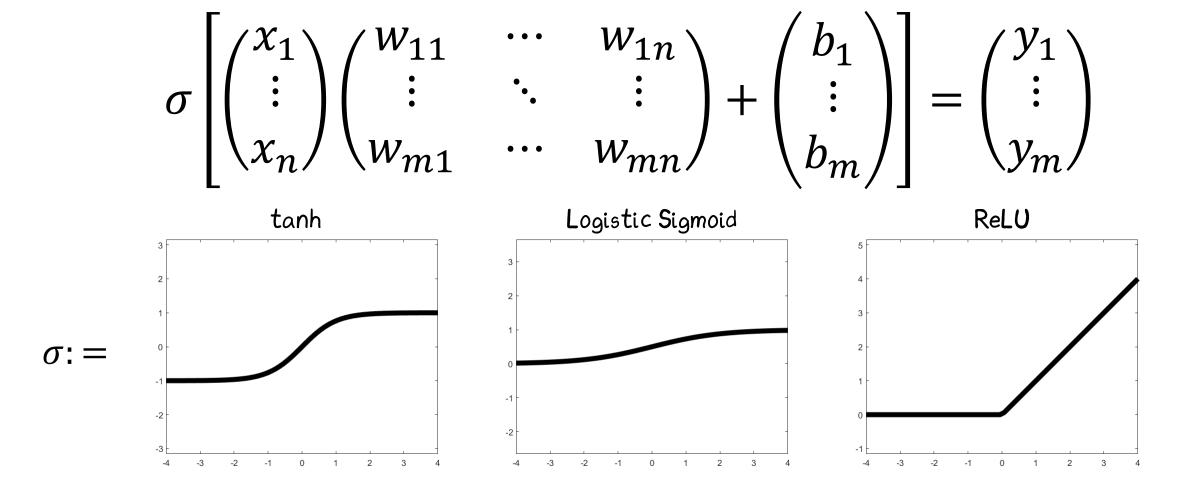


What is a Neural Network?

$$\begin{pmatrix} x_1 \\ \vdots \\ x_n \end{pmatrix} \begin{pmatrix} w_{11} & \cdots & w_{1n} \\ \vdots & \ddots & \vdots \\ w_{m1} & \cdots & w_{mn} \end{pmatrix} + \begin{pmatrix} b_1 \\ \vdots \\ b_m \end{pmatrix}$$

$$\sigma \begin{bmatrix} \begin{pmatrix} x_1 \\ \vdots \\ x_n \end{pmatrix} \begin{pmatrix} w_{11} & \cdots & w_{1n} \\ \vdots & \ddots & \vdots \\ w_{m1} & \cdots & w_{mn} \end{pmatrix} + \begin{pmatrix} b_1 \\ \vdots \\ b_m \end{pmatrix} \end{bmatrix}$$

$$\sigma \begin{bmatrix} \begin{pmatrix} x_1 \\ \vdots \\ x_n \end{pmatrix} \begin{pmatrix} w_{11} & \cdots & w_{1n} \\ \vdots & \ddots & \vdots \\ w_{m1} & \cdots & w_{mn} \end{pmatrix} + \begin{pmatrix} b_1 \\ \vdots \\ b_m \end{pmatrix} \end{bmatrix} = \begin{pmatrix} y_1 \\ \vdots \\ y_m \end{pmatrix}$$



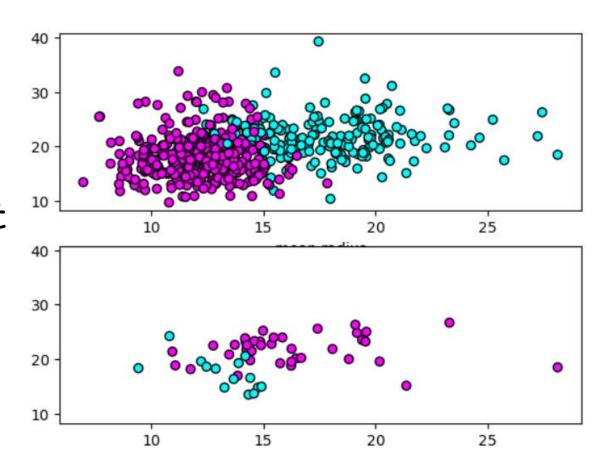
Deep Neural Networks

$$\sigma \begin{bmatrix} \begin{pmatrix} x_{11} \\ \vdots \\ x_{1n} \end{pmatrix} \begin{pmatrix} w_{111} & \cdots & w_{11n} \\ \vdots & \ddots & \vdots \\ w_{1m1} & \cdots & w_{1mn} \end{pmatrix} + \begin{pmatrix} b_{11} \\ \vdots \\ b_{1m} \end{pmatrix} \end{bmatrix} = \begin{pmatrix} x_{21} \\ \vdots \\ x_{2m} \end{pmatrix}$$

$$\sigma \begin{bmatrix} \begin{pmatrix} x_{21} \\ \vdots \\ x_{2m} \end{pmatrix} \begin{pmatrix} w_{211} & \cdots & w_{21m} \\ \vdots & \ddots & \vdots \\ w_{2\ell m} & \cdots & w_{2\ell \ell} \end{pmatrix} + \begin{pmatrix} b_{21} \\ \vdots \\ b_{2m} \end{pmatrix} \end{bmatrix} \xrightarrow{\text{many layers!}} \begin{pmatrix} y_1 \\ \vdots \\ y_q \end{pmatrix}$$

Deep Neural Networks: example!

- · Classification
 - We'll start with an example, nonphysics dataset (cw cancer)
 - Two classes, 30-dimensional input
 - Walk through how to actually set up and train a model
 - Output a scalar [O,I] and convert it back to a class at the end



Deep Neural Networks: example!

First we'll grab the data

```
import matplotlib.pyplot as plt
import numpy as np
from tqdm.notebook import tqdm
from sklearn.datasets import load_breast_cancer

import os
os.environ['KERAS_BACKEND'] = 'torch'
import torch
import keras
from keras import layers
```

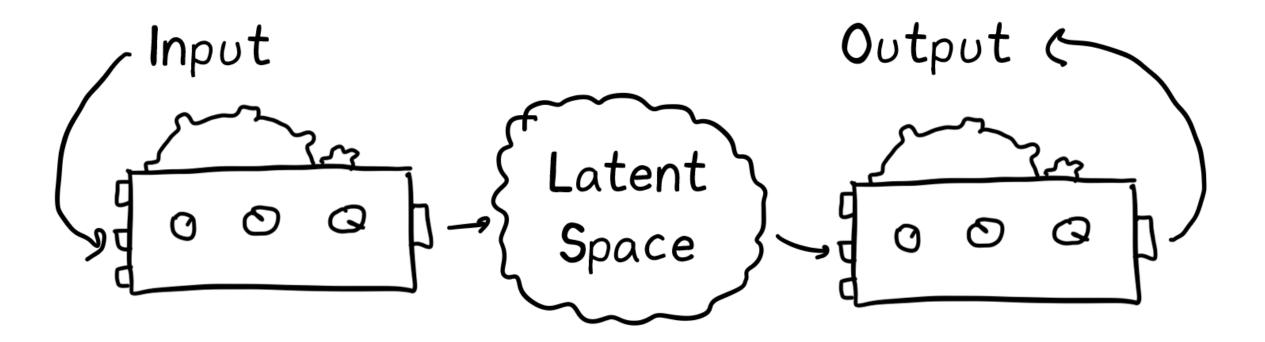
```
# Load the data and split off some for testing
data = load_breast_cancer()
x = data['data'][:-10]
y = data['target'][:-10]
```

Then we'll build our model

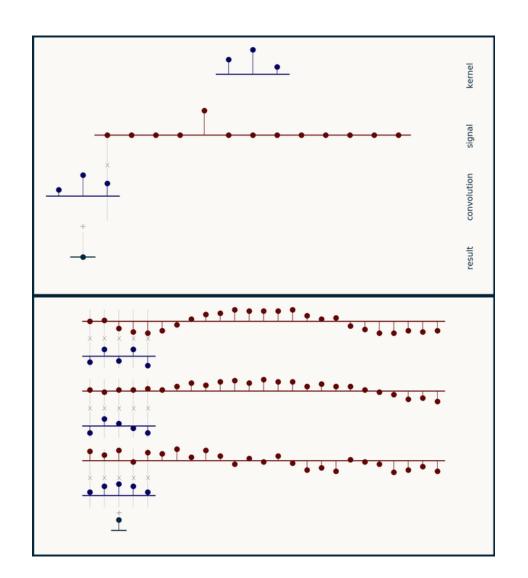
Then we'll train and run it

What is an autoencoder?

Encoding

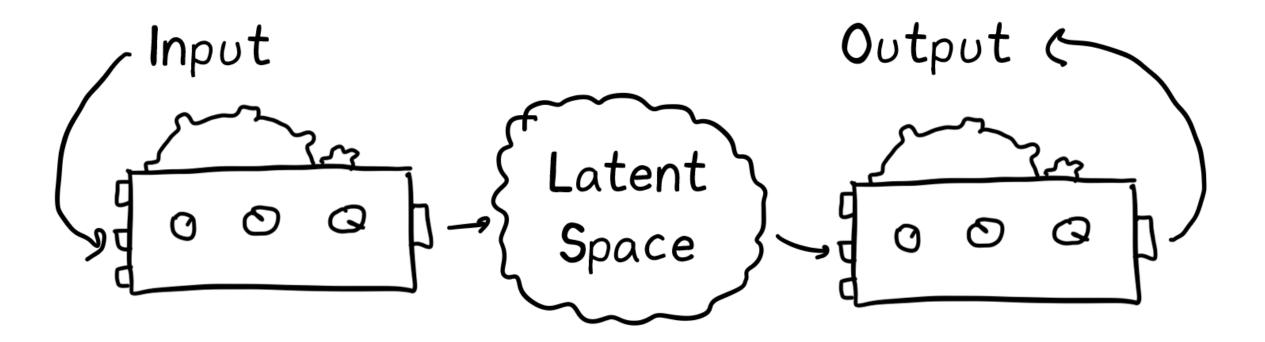


Encoding: Convolutional Layers

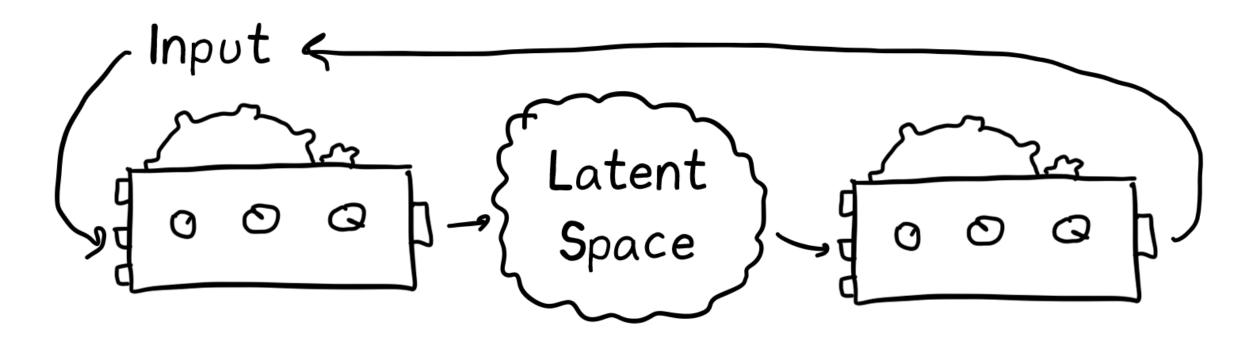


- A Convolution Layer passes a moving window over the input (or previous output from the last layer)
- For simple filters, this is a "smoothing" operation
- Convolutions are a good way to create an abstract representation of data when things are continuous, spatial or in time-series
- · Think of the Fourier transform!

Encoding



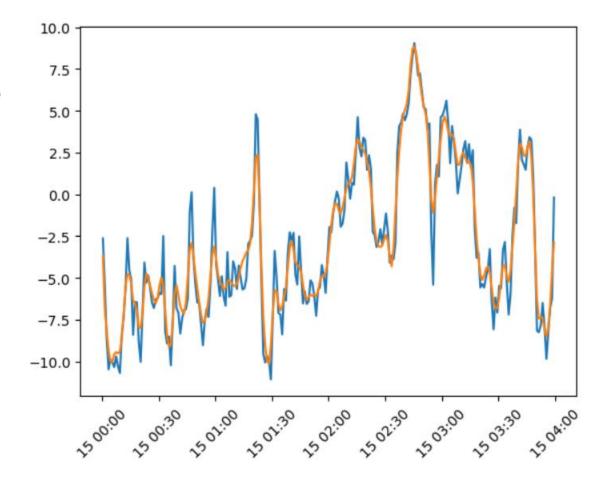
Autoencoders



Autoencoding: example!

· Feature Detection

- We'll train an autoencoder on a bunch of solar wind data from Parker Solar Probe
- Then we'll test on other data from the next year
- Look for where the trained autoencoder does badly
- Hopefully interesting things are happening there!



Autoencoding: example!

This time we need to decide how long our windows will be, and slice up the data

And we'll use convolutional layers to encode the time series

```
model = keras.Sequential([
   layers.Input(shape=(TIME_STEPS, FEATURES)),
   layers.Conv1D(
       filters=32,
       kernel size=10,
       padding="same",
       activation="relu",
   layers.Dropout(rate=0.2),
   layers.Conv1D(
       filters=8,
       kernel size=10,
       padding="same",
       activation="relu",
   layers.Dropout(rate=0.2),
   layers.Conv1D(
       filters=4,
       kernel size=10,
       padding="same",
       activation="relu",
   layers.Conv1D(filters=FEATURES, kernel_size=4, padding="same"),
model.compile(optimizer=keras.optimizers.Adam(learning rate=0.001), loss="mse")
model.summary()
```

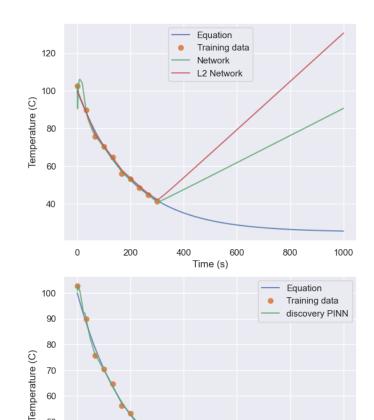
Physics-Informed Neural Networks

Physics-Informed Neural Networks: PINNs

- · We've talked about training to labeled data (supervised)
- We've talked about training to reproduce the input (unsupervised autoregression)
- Let's talk about training if you know the RULES (Physics-Informed Neural Networks)
 - Developed by Maziar Raissi

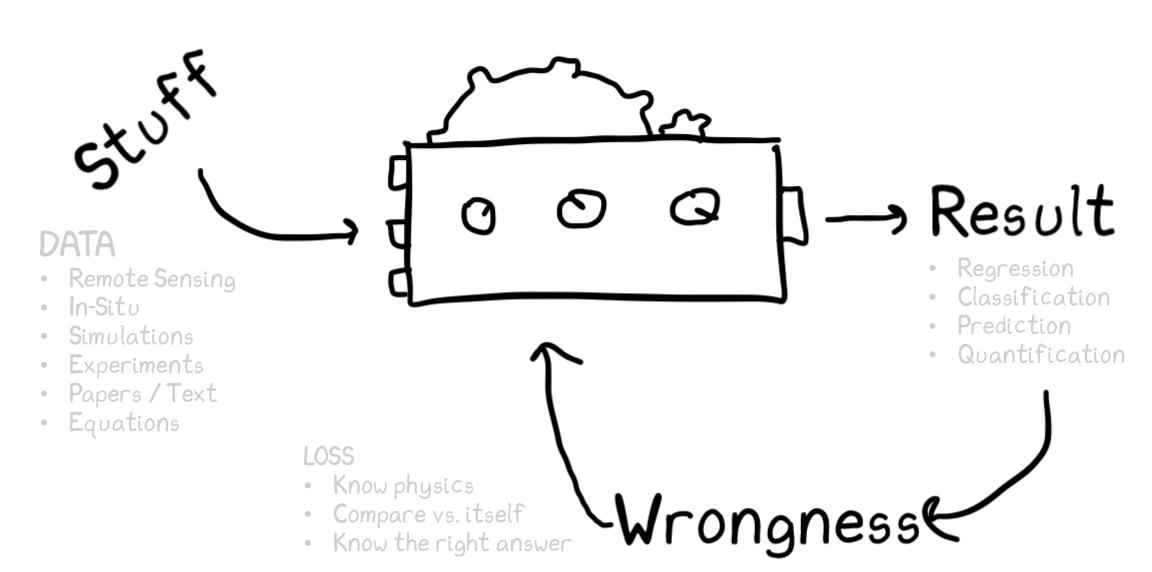
Physics-Informed Neural Networks

- Normally, neural networks for physics can be very expensive because making training data is hard
 - Often experiments or simulation
- · Plus, we need to carpet the full parameter space
 - (Unregularized) Neural Networks are bad at extrapolating
- We can solve both problems by putting the physical equations into the loss function

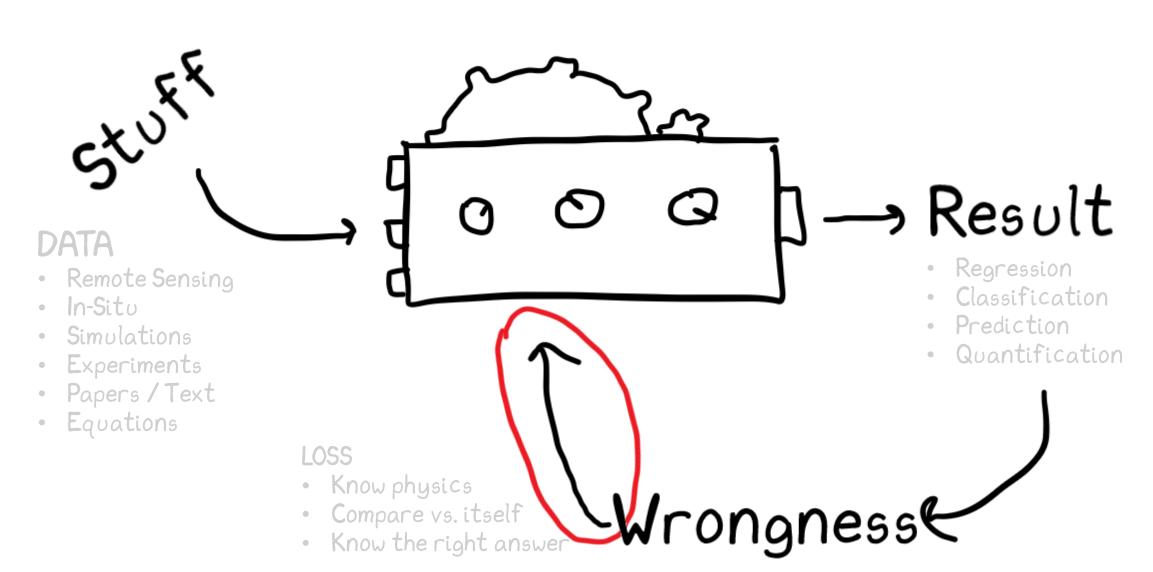


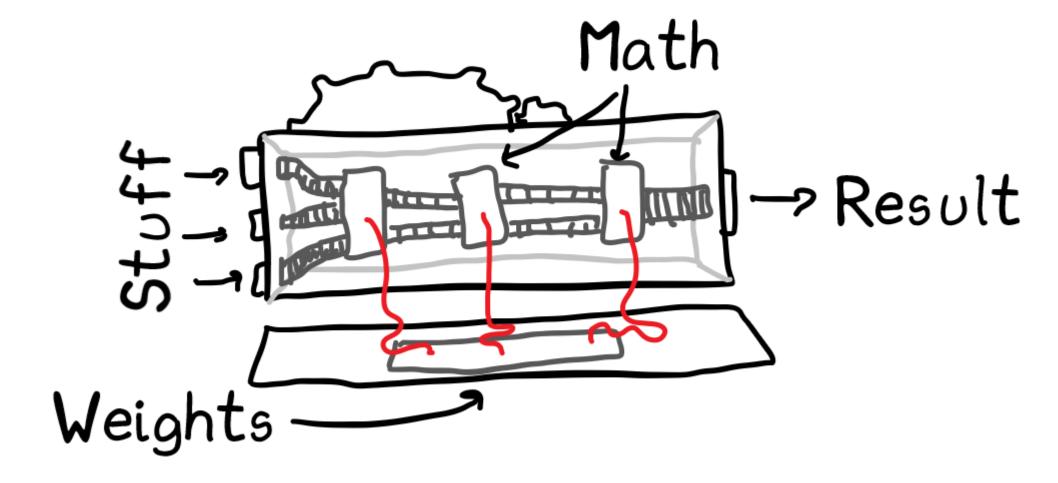
Wolf's models of a cooling coffee cup: two standard networks and a PINN

Machine Learning (remember this?)

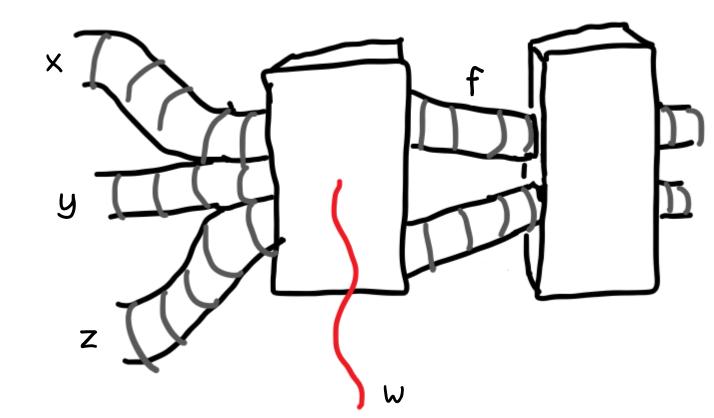


Machine Learning (remember this?)

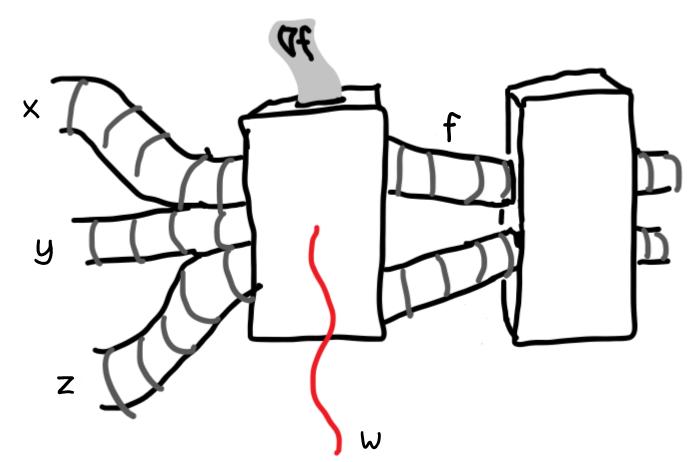




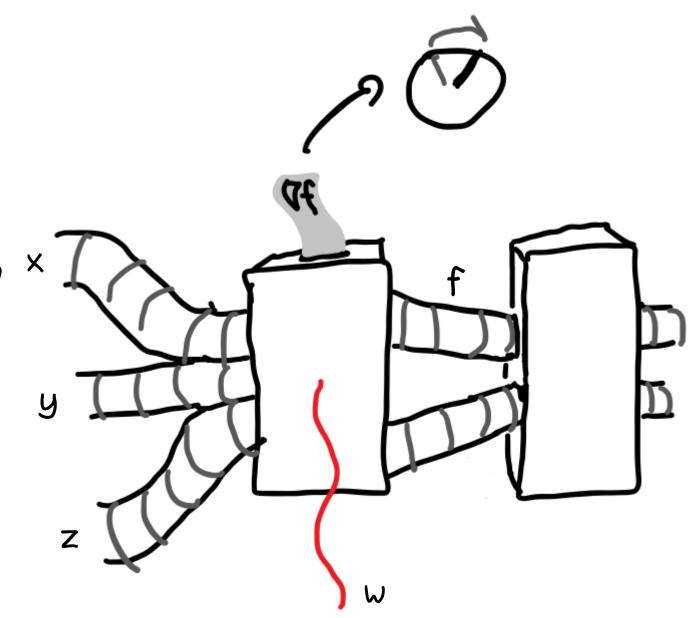
 Inside the box is a pipeline that combines inputs to each layer with weights



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- The derivatives at each step get logged

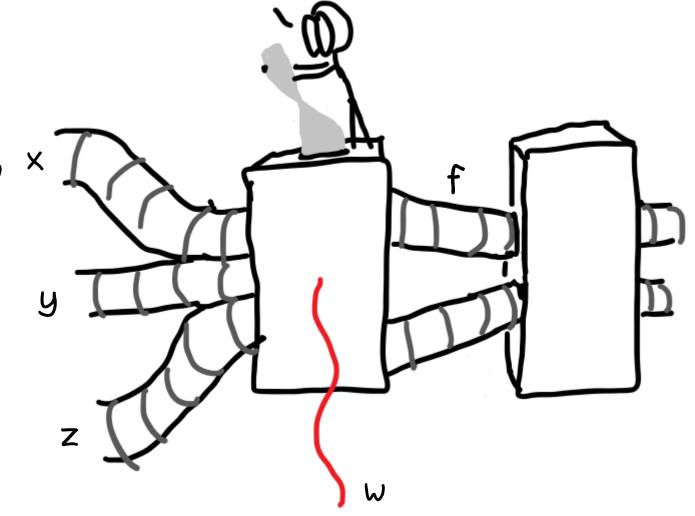


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- This log is how we know how to tune the weights



- Inside the box is a pipeline that combines inputs to each layer with weights
- The derivatives at each step get logged
- This log is how we know how to tune the weights
- But we can take advantage of this to take physical derivatives we care about!

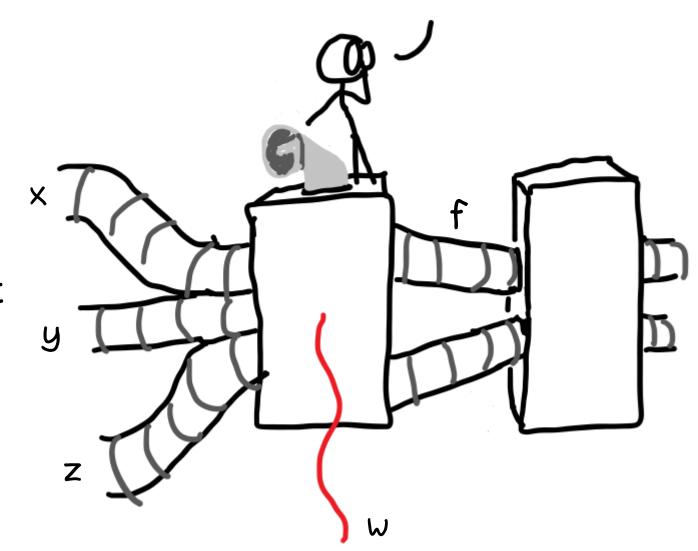
Oh.... oh that's not right.



Physics-Informed Neural Networks

- We can use these physical derivatives to build our differential equation's residual
- Put that residual in the loss function wherever we don't have known data
- Physics will 'supervise' our training FOR us!

I should probably call someone about this...



PINNs: example!

• ID Burger's Equation

$$u_{t} + uu_{x} - \left(\frac{v}{\pi}\right)u_{xx} = 0, x \in [-1,1], t \in [0,1]$$
$$u(0,x) = -\sin(\pi x)$$
$$u(t,-1) = u(t,1) = 0$$

- We'll use torch's autodifferentiation abilities, but in a way that makes keras unhappy
 - · We'll have to write our own training loop.
 - We won't do any of the fancy validation and batch-shuffling keras was doing, just to keep things simple

PINNs: example!

First we set up some data points

 Want boundaries, and some randomly sampled interior points

```
Nbd = 100
N = 5000
xt bd = np.vstack((
    np.vstack((np.linspace(-1,1,Nbd),np.zeros(Nbd))).transpose(),
    np.vstack((-np.ones(Nbd),np.linspace(1/Nbd,1,Nbd))).transpose(),
    np.vstack((np.ones(Nbd),np.linspace(1/Nbd,1,Nbd))).transpose()
),dtype=np.float32)
u bd = np.hstack((
    -np.sin(np.pi*np.linspace(-1,1,Nbd)),
    np.zeros(2*Nbd)
),dtype=np.float32)
v = 0.01
sampler = LatinHypercube(2)
xt = sampler.random(n=N)
xt[:,0] = 2*xt[:,0]-1
xt = np.vstack((xt bd,xt),dtype=np.float32)
```

We define a custom loss function

 We use physics to put Burger's equation in, and look at boundary errors

```
def lossfn(y_true,y_pred):
    bd loss = torch.sum(keras.losses.mean squared error(y true,y pred))/(3*Nbd)
    xt_tensor = torch.tensor(xt,requires grad=True, device=y pred.device)
    xt tensor.grad = None
    u = model(xt_tensor).squeeze()
    xt grad = torch.autograd.grad(
        u,xt tensor,grad outputs=torch.ones(u.shape,device=u.device),
        retain graph=True, create graph=True
   )[0]
    du dx = xt grad[:,0]
    du dt = xt grad[:,1]
   xt_grad2 = torch.autograd.grad(
        du dx,xt tensor,grad outputs=torch.ones(u.shape,device=u.device),
        retain graph=True
    )[0]
    d2u_dx2 = xt_grad2[:,0]
    residual = du dt + u * du dx - (v / np.pi) * d2u dx2
    phys loss = torch.sum(torch.pow(residual,2))/N
    return 5*bd loss + phys loss
```

PINNs: example!

We'll use a very simple neural network - our simplest yet!

```
nnlayers = [20,20,20,20,20,20,20]

model = keras.Sequential([])
model.add(keras.Input(shape=(2,)))
for L in nnlayers:
    model.add(layers.Dense(L, activation='tanh'))
model.add(layers.Dense(1))

model.compile(loss=lossfn)
```

Then comes our custom training loop - this is real pytorch



```
def run_epoch(model, input, target):
    def closure():
        optimizer.zero_grad()
        output = model(input)
        loss = lossfn(target,output)
        loss.backward()
        return loss

loss = optimizer.step(closure)

return loss.item()
```

```
epochs = 10000
patience = 10
threshold = 1e-4
losses = np.array([0.]*epochs)
optimizer = torch.optim.Adam(model.parameters(), lr=1e-4)
bar = tqdm(range(epochs))
for e in bar:
    model.train(True)
    loss = run_epoch(model,xt_bd,u_bd)
    losses[e] = loss
    bar.set_description(f'epoch {e+1}, loss: {loss:.3e}')
    if e > patience and np.max(
        np.abs(losses[e-patience:e]-loss)
    )<threshold*loss:
        print('Model converged.')
        break
```

Conclusion

- Machine Learning uses very simple components that we strap together in new ways
- · It can be useful in a variety of contexts
 - Classifying populations with lots of parameters (we didn't even talk about the right way to do this, kd-clustering)
 - · Prediction and regression
 - · Solving equations
 - Finding rare events in the noise
 - · Anything you want to be FAST and DIRTY
- The best way to learn is by doing!

Thanks!

