

Consider \mathbb{Z}_7 .

$$1^{-1} = 1$$

$$\because 1 \cdot 1 = 1 \quad (1)$$

by Existence of a Multiplicative Identity

$$2^{-1} = 4$$

$$\because 2 \cdot 4 \equiv 1 \pmod{7} \quad (2)$$

$$3^{-1} = 5$$

$$\because 3 \cdot 5 \equiv 1 \pmod{7} \quad (3)$$

$$4^{-1} = 2$$

$$\because 4 \cdot 2 \equiv 1 \pmod{7} \quad (4)$$

$$5^{-1} = 3$$

$$\because 5 \cdot 3 \equiv 1 \pmod{7} \quad (5)$$

$$6^{-1} = 6$$

$$\because 6 \cdot 6 \equiv 1 \pmod{7} \quad (6)$$