

# Uncertainties in estimating winter balance from direct measurements on glaciers

Alexandra PULWICKI,<sup>1</sup> Gwenn E. FLOWERS,<sup>1</sup> Valentina RADIĆ,<sup>2</sup>

<sup>1</sup> *Simon Fraser University, Burnaby, BC, Canada*

<sup>2</sup> *University of British Columbia, Vancouver, BC, Canada*

*Correspondence: Alexandra Pulwicks <apulwick@sfu.ca>*

**ABSTRACT.** Accurately estimating winter surface mass balance for a glacier is central to quantifying overall mass balance and melt runoff. However, measuring and modelling snow distribution and variability is inherently difficult in alpine terrain, resulting in high winter balance uncertainty. The goal of this paper is to examine methods and sources of error when converting snow measurements to estimates of winter balance and to gain a more comprehensive understanding of uncertainties inherent in this process. We extensively measure snow depth and density, at various spatial scales, on three glaciers in the St. Elias Mountains, Yukon. Elevation is found to be the dominant driver of accumulation variability but the relationship varies between glaciers. Our results also suggest that wind redistribution and preferential deposition affect snow distribution but that more complex parametrization is needed to fully capture wind effects. By using a Monte Carlo method to quantify the effects of various sources of uncertainty, we find that interpolation of SWE measurements is the largest source of winter balance uncertainty. Snow distribution patterns differed considerably between glaciers, highlighting strong inter- and intra-basin variability. Accurately and precisely estimating winter balance therefore continues to be a difficult and elusive problem.

## INTRODUCTION

Accurate estimation of winter surface mass balance is critical for correctly simulating the summer and overall mass balance of a glacier (e.g. Réveillet and others, 2016). Effectively representing spatial distribution of snow is also important for simulating snow and ice melt as well as energy and mass exchange between the land and atmosphere to better monitor surface runoff and its downstream effects (e.g. Clark and others, 2011). Snow distribution is sensitive to a number of complex processes that partially depend on glacier location, topography, and orientation (e.g. Blöschl and others, 1991; Mott and others, 2008; Clark and others, 2011; Sold and others, 2013). Current models are not able to fully represent these processes so the distribution of snow in remote, mountainous locations is not well known. There is, therefore, a significant source of uncertainty that undermines the ability of models to represent current glacier conditions and make predictions of glacier response to a warming climate (Réveillet and others, 2016).

Winter surface mass balance is the net accumulation and ablation of snow over the winter season (Cogley and others, 2011), which constitutes glacier mass input. We refer to this quantity as winter balance throughout the paper. Accurate estimates of winter balance are critical for calculating glacier mass balance, not only because winter balance constitutes half of the glacier mass balance but also because the distribution of snow on a glacier initializes the summer balance and high snow albedo contributes to

reduced summer melt (e.g. Hock, 2005; Réveillet and others, 2016).

Winter balance is notoriously difficult to estimate. Snow distribution in alpine regions is highly variable and influenced by dynamic interactions between the atmosphere and complex topography, operating on multiple spatial and temporal scales (e.g. Barry, 1992; Liston and Elder, 2006; Clark and others, 2011). Extensive, high resolution and accurate accumulation measurements on glaciers are almost impossible to achieve due to cost benefits of the various methods used to quantify snow water equivalent (e.g. Cogley and others, 2011; McGrath and others, 2015). For example, snow probes obtain accurate point observations but have negligible spatial coverage. Conversely, gravimetric methods obtain extensive measurements of mass change but cannot capture relevant spatial variability of snow (Cogley and others, 2011). Glacierized regions are also generally remote and challenging to access during the winter due to poor travelling conditions.

Most glacier mass balance programs estimate winter balance in a similar way to summer balance. Measurements of the amount of snow at the end of the winter season are taken at a few stake locations and then basic interpolation methods are used to estimate winter balance (e.g. Hock and Jensen, 1999; Thibert and others, 2008; MacDougall and Flowers, 2011; Cullen and others, 2017). However, equivalence between summer and winter balance estimation methods is likely inappropriate. Melt is strongly affected by air temperature and solar radiation (e.g. Hock, 2005), both

of which are consistent across large spatial domains (e.g. Barry, 1992). Conversely, snow distribution is largely driven by precipitation (e.g. Lehning and others, 2008) and wind patterns (e.g. Bernhardt and others, 2009; Musselman and others, 2015), which are known to be highly heterogeneous in alpine environments (e.g. Barry, 1992). Snow distribution is therefore highly variable and has short correlation length scales (e.g. Anderton and others, 2004; Egli and others, 2011; Grunewald and others, 2010; Helbig and van Herwijnen, 2017; López-Moreno and others, 2011, 2013; Machguth and others, 2006; Marshall and others, 2006).

Detailed studies of winter balance are far less common than those of summer balance and uncertainty in winter mass balance currently overshadows differences between summer balance models (e.g. Réveillet and others, 2016). Studies that focus on estimating winter balance employ a wide range of snow measurement techniques (Sold and others, 2013), including direct measurement (e.g. Cullen and others, 2017), lidar/photogrammetry (e.g. Sold and others, 2013) and ground penetrating radar (e.g. Machguth and others, 2006; Gusmeroli and others, 2014; McGrath and others, 2015). Spatial coverage of measurements is often limited for winter balance studies and typically consists of an elevation transect along the glacier centreline (e.g. Kaser and others, 2003; Machguth and others, 2006). Interpolation of these measurements is primarily done by computing a linear regression that includes only a few topographic parameters (e.g. MacDougall and Flowers, 2011), with elevation being the most common. Other applied techniques include hand contouring (e.g. Tangborn and others, 1975), kriging (e.g. Hock and Jensen, 1999) and attributing measured accumulation values to elevation bands (e.g. Thibert and others, 2008). Physical snow models have been applied on a few glaciers (e.g. Mott and others, 2008; Dadić and others, 2010) but a lack of detailed meteorological data generally prohibits their wide-spread application. Error analysis is rarely considered and to our knowledge, no studies have investigated uncertainty in winter balance estimates.

There is a disparity in snow survey sophistication within glacier winter balance studies when compared to snow science studies. Winter mass balance surveys employ similar techniques and methods as snow science surveys (e.g. Elder and others, 1991; Deems and Painter, 2006; Nolan and others, 2015; Godio and Rege, 2016) but favour more simple approaches (e.g. Kaser and others, 2003; Sold and others, 2013). Snow science surveys are generally extensive and designed to measure snow throughout the basin and ensure that all terrain types are sampled. A wide array of measurement interpolation methods are used, including linear (e.g. López-Moreno and others, 2010) and non-linear regressions (e.g. Molotch and others, 2005) and geospatial interpolation (e.g. Erxleben and others, 2002) such as kriging, and methods are often combined to yield improved fit (e.g. Balk and Elder, 2000). Physical snow models, such as Alpine3D (Lehning and others, 2006) and SnowDrift3D (Schneiderbauer and Prokop, 2011), are continuously being improved and tested within the snow science literature. Snow survey error has been considered from both a theoretical (e.g. Trujillo and Lehning, 2015)

and applied perspective (e.g. Turcan and Loijens, 1975; Woo and Marsh, 1978; Deems and Painter, 2006).

The precision and accuracy of winter balance estimates can likely be improved by incorporating snow science tools and interpolation methodologies and by gaining a more comprehensive understanding of uncertainties inherent when estimating winter balance on glaciers. Ultimately, we need a thorough knowledge of the processes that affect spatial and temporal snow variability and an effective method to predict snow accumulation. The contribution of our work toward these goals is to (1) examine methods and uncertainties when moving from direct snow depth and density measurements to estimating winter balance and (2) show how snow variability, data error and our methodological choices interact to create uncertainty in our estimate of winter balance. We focus on commonly applied low-complexity methods of measuring and predicting winter balance with the hope of making our results broadly applicable to current and future winter mass balance programs.

## STUDY SITE

Winter balance surveys were conducted on three glaciers in the Donjek Range of the St. Elias Mountains, located in the south western Yukon, Canada. The Donjek Range is approximately  $30 \times 30$  km and Glacier 4, Glacier 2, and Glacier 13 (labelling adopted from Crompton and Flowers (2016)) are located along a SW-NE transect through the range. There is a local topographic divide in the Donjek Range that follows an “L” shape, with one glacier located in each of the south, north, and east regions (Figure 1). These mid-sized alpine glaciers are generally oriented SE-NW, with Glacier 4 dominantly south facing and Glaciers 2 and 13 generally north facing. The glaciers are low angled with steep head walls and steep valley walls. The St. Elias mountains boarder the Pacific Ocean and rise sharply, creating a significant climatic winter gradient between coastal maritime conditions, generated by Aleutian–Gulf of Alaska low-pressure systems, and interior continental conditions, determined by Yukon–Mackenzie high-pressure system (Taylor-Barge, 1969). The average dividing line between the two climatic zones shifts between Divide Station and the head of the Kaskawalsh Glacier based on synoptic conditions. The Donjek Range is located approximately 40 km to the east of the head of the Kaskawalsh Glacier. Research on snow distribution and glacier mass balance in the St. Elias is limited. A series of research programs were operational in the 1960s (Wood, 1948; Danby and others, 2003) and long-term studies on a few alpine glaciers have arisen in the last 30 years (e.g. Clarke and others, 1984; Paoli and Flowers, 2009).

## METHODS

Estimating winter balance involves transforming snow depth and density measurements to distributed estimates of snow water equivalent (SWE). We use four main processing steps. First, we obtain measurements of snow depth and density. Since density is measured more sparsely than depth,

**Table 1.** Physical details of study glaciers as well as details of snow survey conducted in May 2016 at Glacier 4 (G4), Glacier 2 (G2), and Glacier 13 (G13). Values shown include number of snow depth measurement locations along transects ( $n_T$ ), total length of transects ( $d_T$  [km]), number of combined SP and FS density measurement locations ( $n_\rho$ ) and number of zigzag ( $n_{zz}$ ).

	Location	Elevation (m a.s.l.)		Slope (°)	Area (km)	Date	Survey Details			
		Mean	Range				$n_T$	$d_T$ (km)	$n_\rho$	$n_{zz}$
<b>G4</b>	595470 E 6740730 N	2344	1958–2809	12.8	3.8	May 4–7	649	13.1	7	3
<b>G2</b>	601160 E 6753785 N	2495	1899–3103	13.0	7.0	May 8–11	762	13.6	7	3
<b>G13</b>	604602 E 6763400 N	2428	1923–3067	13.4	12.6	May 12–15	941	18.1	19	4

the second step is to interpolate density measurements to all depth measurement locations and to calculate the SWE at each measurement location. Third, we average all SWE values within one grid cell of a digital elevation model (DEM) with given spatial resolution to produce a single value of SWE for each grid cell. Fourth, we interpolate SWE values to obtain a distributed estimate of SWE across the surface of the glacier. We choose to use a linear regression between SWE and topographic parameters as well as simple kriging to interpolation grid cell SWE. To estimate the specific winter balance we then calculate aeri-ally-averaged integrated SWE. For brevity, we refer to these four steps as (1) field measurements, (2) distributed snow density, (3) grid cell average SWE and (4) distributed SWE. Detailed methodology for each step is outlined below.

## Field measurements

### Sampling design

The sampling design attempted to capture depth variability at multiple spatial scales. We measured winter balance at three glaciers along the precipitation gradient in the St. Elias Mountains, Yukon (Taylor-Barge, 1969) in an attempt to account for range-scale variability (Clark and others, 2011). We measured winter balance on Glaciers 4, 2, and 13, which are located increasingly far from the head of the Kaskawalsh Glacier (Figure 1b). Snow depth was measured along linear and curvilinear transects to account for basin-scale variability. At each measurement location, three values of snow depth were recorded to account for point-scale variability (Clark and others, 2011). We selected centreline and transverse transects with sample spacing of 10 – 60 m (Figure 1d) to capture previously established correlations between elevation and accumulation (e.g. Machguth and others, 2006; Walmsley, 2015) as well as accumulation differences between ice-marginal and centre accumulation. We also implemented an hourglass and circle design (Figure 1), which allows for sampling in all directions and easy travel (Parr, C., 2016 personal communication). At each measurement location, we took 3 – 4 depth measurements within  $\sim 1$  m of each other (Figure 1e), resulting in more than 9,000 snow depth measurements throughout the study area.

### Snow depth

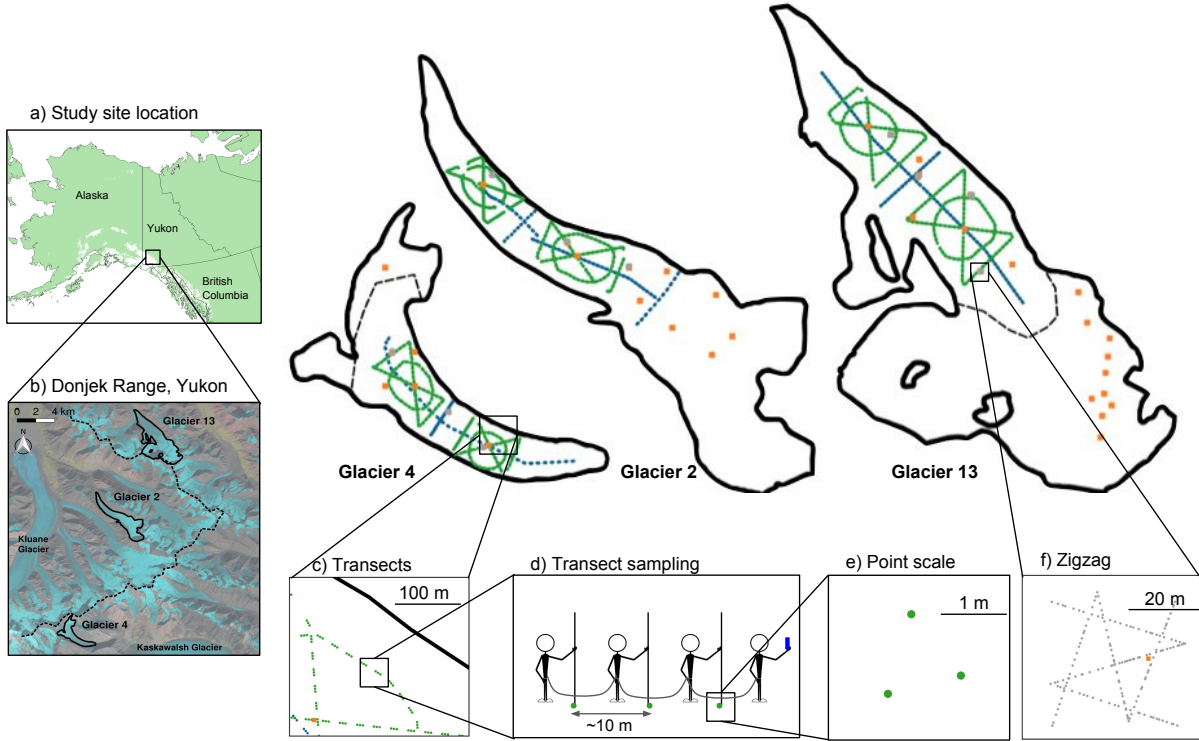
The estimated SWE is the product of the snow depth and depth-averaged density. Snow depth is generally accepted

to be more variable than density (Elder and others, 1991; Clark and others, 2011; López-Moreno and others, 2013) so we chose a sampling design with relatively small measurement spacing along transects that resulted in a ratio of approximately 55:1 snow depth to snow density measurements. Our sampling campaign involved four people and occurred between May 5 and 15, 2015, which corresponds to the historical peak accumulation in the Yukon (Yukon Snow Survey Bulletin and Water Supply Forecast, May 1, 2016). While roped-up for glacier travel at fixed distances between observers, the lead person used a single frequency GPS (Garmin GPSMAP 64s) to navigate as close to the predefined transect measurement locations as possible (Figure 1). The remaining three people used 3.2 m aluminium avalanche probes to take snow depth measurements. The location of each set of depth measurements, taken by the second, third and fourth observers, was approximated based on the recorded location of the first person.

Snow depth sampling was primarily done in the ablation area to ensure that only snow from the current accumulation season was measured. Determining the boundary between snow and firn in the accumulation area, especially when using an avalanche probe, is difficult and often incorrect (Grunewald and others, 2010; Sold and others, 2013). We intended to use a firn corer to extract snow cores in the accumulation area but due to environmental conditions we were unable to obtain cohesive cores. Successful measurements within the accumulation area were done either in a snow pit or using a Federal Sampler with shovel validation so that we could identify the snow-firn transition based on a change in snow crystal size and density.

### Zigzags

To capture variability at spatial scales smaller than a DEM grid cell, we implemented a linear-random sampling design, termed ‘zigzag’ (Shea and Jamieson, 2010). We measured depth at random intervals (0.3 – 3.0 m) along two ‘Z’-shaped transects within three to four  $40 \times 40$  m squares (Figure 1c) resulting in 135 – 191 measurement points for each zigzag. Zigzag locations were randomly chosen within the upper ( $\sim 2350$  m a.s.l.), middle ( $\sim 2250$  m a.s.l.), and lower portions ( $\sim 2150$  m a.s.l.) of the ablation area of each glacier. We were able to measure a fourth zigzag on Glacier 13 that was located in the middle ablation area ( $\sim 2200$  m a.s.l.).



**Fig. 1.** Sampling design for Glaciers 4, 2 and 13, located in the Donjek Range, Yukon (a,b). Centreline and transverse transects are shown in blue dots, hourglass and circle design are shown in green dots. (c) Linear and curvilinear transects typically consist of sets of three measurement locations, spaced  $\sim 10$  m apart (d). (e) At each measurement location, three snow depth observations are made. (f) Linear-random snow depth measurements in ‘zigzag’ design are shown as grey dots. Orange squares are locations of snow density measurements.

### Snow density

Snow density was measured using a wedge cutter in three snowpits on each glacier. We measured a vertical density profile by inserting a  $5 \times 10 \times 10$  cm wedge-shaped cutter ( $250 \text{ cm}^3$ ) in 5 cm increments to extract snow samples and then weighed the samples with a spring scale (e.g. Gray and Male, 1981; Fierz and others, 2009). Uncertainty in estimating density from snow pits stems from measurement errors and incorrect assignment of density to layers that could not be sampled (i.e. ice lenses and ‘hard’ layers).

While snow pits provide the most accurate measure of snow density, digging and sampling a snow pit is time and labour intensive. Therefore, a Federal Snow Sampler (FS) (Clyde, 1932), which measures bulk SWE, was used to augment the spatial extent of density measurements. A minimum of three measurements were taken at each of 7 – 19 locations on each glacier and an additional eight FS measurements were co-located with each snow pit profile. Measurements where the snow core length inside the FS was less than 90% of the snow depth were assumed to be an incorrect sample and were excluded. Density values were then averaged for each location.

During the field campaign there were two small accumulation events. The first, on May 6, also involved high winds so accumulation could not be determined. The second, on May 10, resulted in 0.01 m w.e accumulation at one location on Glacier 2. Warm temperatures and clear skies occurred

between May 11 and 16, which we believed resulted in significant melt occurring on Glacier 13. The snow in the lower part of the ablation area was isothermal and showed clear signs of melt and snow metamorphosis. The total amount of accumulation and melt during the study period could not be estimated so no corrections were made.

### Distributed snow density

Measured density is interpolated to estimate SWE at each depth sampling location. We chose four separate methods that are commonly applied to interpolate density: (1) mean density over an entire range (e.g. Cullen and others, 2017), (2) mean density for each glacier (e.g. Elder and others, 1991; McGrath and others, 2015), (3) linear regression of density with elevation (e.g. Elder and others, 1998; Molotch and others, 2005) and (4) inverse-distance weighted density (e.g. Molotch and others, 2005). SP and FS densities are treated separately, for reasons explained below, which results in eight density interpolation options (Table 2).

### Grid cell average SWE

We average SWE values within each DEM-aligned grid cell ( $40 \times 40$  m). The locations of measurements have considerable uncertainty both from the error of the GPS unit (2.7 – 4.6 m) and the estimation of observer location based on the GPS unit. These errors could easily result in the incorrect assignment of a SWE measurement to a certain grid cell but this source of variability was not further

**Table 2.** Description of density interpolation methods used to calculate SWE used in the topographic regression. Abbreviations with ‘S’ used snowpit-derived densities and abbreviations with an ‘F’ used Federal Sampler-derived densities.

	Snow density source		Estimation method
	<i>Snowpit</i>	<i>Federal Sampler</i>	
S1 F1	■	■	Mean of all glaciers
S2 F2	■	■	Glacier mean
S3 F3	■	■	Linear regression of elevation and density for each glacier
S4 F4	■	■	Inverse distance weighted mean

investigated because we assume that SWE variability is captured in the zigzag measurements described below. There are no significant differences between observers ( $p > 0.05$ ), with the exception of the first transect on Glacier 4. No corrections to the data based on observer differences are applied.

## Distributed SWE

### Linear regression

SWE are interpolated and extrapolated for each glacier using linear regression (LR) as well as simple kriging (SK). Linear regressions relate observed SWE to grid cell values of DEM-derived topographic parameters (Davis and Sampson, 1986). We choose to include elevation, distance from centreline, slope, aspect, curvature, “northness” and a wind redistribution parameter in the LR. Our sampling design ensured that the ranges of topographic parameters covered by the measurements represent more than 70% of the total area of each glacier (except for the elevation range on Glacier 2, which is 50%). For details on data and methods used to estimate the topographic parameters see the Supplementary Material. Topographic parameters are weighted by a set of fitted regression coefficients ( $\beta_i$ ). Regression coefficients are calculated by minimizing the sum of squares of the vertical deviations of each data point from the regression line (Davis and Sampson, 1986). Snow depth data are highly variable so there is a possibility for the LR to fit to this data noise, a process known as overfitting. To prevent overfitting, cross-validation and model averaging are implemented (see Supplementary Material). The distributed estimate of SWE is found by using regression coefficients to estimate SWE at each grid cell. Specific winter balance is calculated as the aerally-averaged, integrated SWE for each glacier ([m w.e.]).

### Simple kriging

Simple kriging (SK) estimates SWE values at unsampled locations by using the isotropic spatial correlation (covariance) of measured SWE to find a set of optimal weights (Davis and Sampson, 1986; Li and Heap, 2008). SK assumes that if sampling points are distributed throughout a surface, the degree of spatial correlation of the observed surface can

be determined and the surface can then be interpolated between sampling points. We used the `DiceKriging` R package (Roustant and others, 2012) to calculate the maximum likelihood covariance matrix, as well as range distance ( $\theta$ ) and nugget. The range distance is a measure of data correlation length and the nugget is the residual that encompasses sampling-error variance as well as the spatial variance at distances less than the minimum sample spacing (Li and Heap, 2008).

## Uncertainty analysis

To quantify effects of uncertainty on the winter balance estimate, we conduct a Monte Carlo experiment, which uses repeated random sampling to calculate a numerical solution (Metropolis and Ulam, 1949). This random sampling process is done 1000 times, which results in a distribution of possible winter balance values based on uncertainty within the data processing steps. We quantify the effect of uncertainty as the standard deviation of the distribution. Three sources of uncertainty, which encompass error and uncertainty within each processing step, are considered: (1) density uncertainty, (2) SWE uncertainty and (3) interpolation uncertainty. Individual sources of uncertainty are propagated through the process of converting snow measurements to winter balance. Then, all three uncertainty sources are considered together and their combined effect on winter balance uncertainty is quantified.

### SWE uncertainty ( $\sigma_{\text{SWE}}$ )

To estimate winter balance, we must represent SWE within a grid cell with a single value despite the fact that each grid cell contains a distribution of SWE values. The resulting uncertainty from this SWE representation is characterized by generating a normal distribution, with a standard deviation equal to the mean standard deviation of all zigzags on each glacier. For each iteration of the Monte Carlo, a set of random values is generated from the distribution and added to the observed SWE values. These perturbed SWE values are then used to estimate winter balance. The winter balance uncertainty due to SWE uncertainty ( $\sigma_{\text{SWE}}$ ) is calculated as the standard deviation of the resulting distribution of winter balance estimates.

### Density uncertainty ( $\sigma_\rho$ )

We incorporate uncertainty in interpolating density measurements by carrying forward all eight density interpolation options when estimating winter balance. The density measurement and interpolation methods used in our study encompass a broad spectrum of possible density values. The winter balance uncertainty due to density uncertainty ( $\sigma_\rho$ ) is calculated as the standard deviation of winter balance estimates calculated using each density interpolation option.

### Interpolation uncertainty ( $\sigma_{\text{INT}}$ )

We represent the uncertainty in fitting an interpolation model to observed data in different ways for LR and SK. LR uncertainty is represented by obtaining a multivariate normal distribution of possible  $\beta_i$  values. The standard deviation of each distribution is calculated using the

covariance of regression coefficients as outlined in Bago and Adam (2015). The  $\beta_i$  distributions are randomly sampled and the new  $\beta_i$  values are used to estimate winter balance. SK uncertainty is derived from the 95% confidence interval SWE surfaces generated within the *DiceKriging* package. The standard deviation of each grid cell is then calculated from the confidence interval surfaces and the glacier wide standard deviation is found by taking the square root of the average variance. The distribution of winter balance values is centred at the SK winter balance estimate and has a standard deviation equal to the glacier wide standard deviation. For consistency, the standard deviation of winter balance values that result from either LR or SK interpolation uncertainty is referred to as  $\sigma_{\text{INT}}$ .

## RESULTS AND DISCUSSION

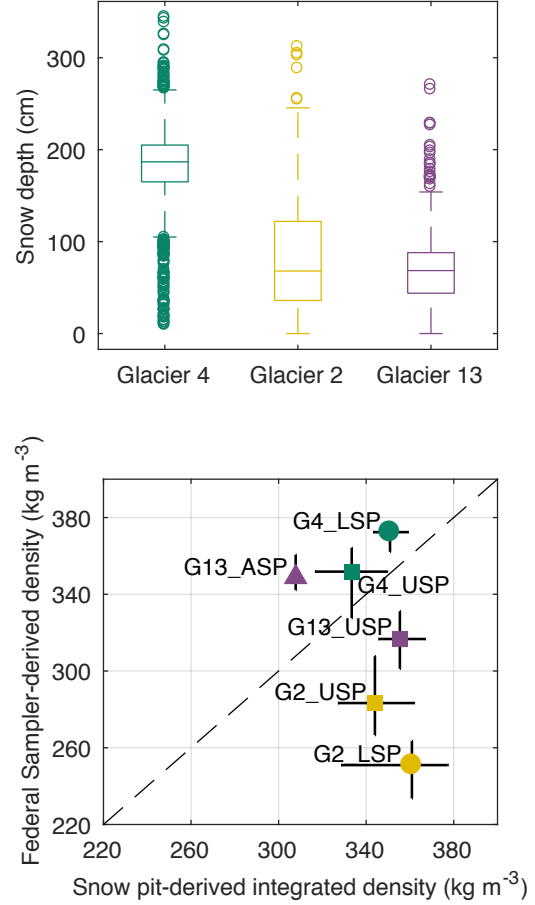
### Field measurements

Despite the lack of measurements in the accumulation area, especially along steep head walls, we observed a wide range of snow depth on all three study glaciers (Figure 2). Glacier 4 has the highest mean snow depth and a high proportion of outliers, indicating a more variable snow depth overall. Glacier 13 has the lowest mean snow depth and a narrower distribution of observed values. At each measurement location, the median range of measured depths (3 – 4 points) as a percent of the mean depth at that location is 2%, 11%, and 12%, for Glaciers 4, 2 and 13, respectively.

Mean snow pit (SP) and Federal Sampler (FS) density values are within one standard deviation of each other for each glacier and over all three glaciers. The standard deviation of glacier-wide mean density is less than 10% of the mean density. However, FS densities have a larger range of values (227 – 431 kg m<sup>-3</sup>) when compared to SP densities (299 – 381 kg m<sup>-3</sup>). The mean SP densities are within one standard deviation between glaciers, whereas mean FS densities are not.

Co-located FS and SP measurements are not correlated and we find that FS density values are positively correlated with snow depth ( $R^2 = 0.59$ ,  $p < 0.01$ ). This positive relationship could be a result of physical processes, such as compaction, but is more likely a result of measurement artefacts for a number of reasons. First, the range of densities measured by the Federal sampler is large and the extreme values seem unlikely to exist in our study region, which experiences a continental snow pack with minimal mid-winter melt events. Second, compaction effects would likely be small at these study glaciers because of the relatively shallow snow pack (deepest measurement was 340 cm). Third, no linear relationship exists between depth and SP density ( $R^2 = 0.05$ ). Together, these findings indicate that the FS measurements have a bias which is challenging to correct for.

The FS appears to oversample in deep snow and undersample in shallow snow. Oversampling by small diameter (area of 10–12 cm<sup>2</sup>) sampling tubes has been observed in previous studies, with a percent error between +6.8% and 11.8% (e.g. Work and others, 1965; Fames and others, 1982; Conger and McClung, 2009). Studies



**Fig. 2.** (Left) Boxplot of measured snow depth on Glaciers 4, 2 and 13. The box shows first quartiles, the line within the box indicates data median, bars indicate minimum and maximum values (excluding outliers), and circles show outliers, which are defined as being outside of the range of 1.5 times the quartiles (approximately  $\pm 2.7\sigma$ ). (Right) Comparison of integrated density estimated using wedge cutters in a snow pit and density estimated using Federal Sampler measurements for Glacier 4 (G04), Glacier 2 (G02) and Glacier 13 (G13). Snow pits were distributed in the accumulation area (ASP), upper ablation area (USP) and lower ablation area (LSP). Error bars are minimum and maximum values.

that use Federal Samplers often apply a 10% correction to all measurements (e.g. Molotch and others, 2005). Oversampling has been attributed to slots “shaving” snow into the tube as it is rotated (e.g. Dixon and Boon, 2012) and to snow falling into the slots, particularly when snow samples had densities greater than 400 kg m<sup>-3</sup> and snow depth greater than 1 m (e.g. Beaumont and Work, 1963). Undersampling is likely to occur due to snow falling out of the bottom of the sampler (Turcan and Loijens, 1975), which likely occurred in our study since a large portion of the lower elevation snow on both Glaciers 2 and 13 was melt affected and weak, allowing for easier lateral displacement of the snow as the sampler was extracted. Relatively poor FS spring scale sensitivity also made it difficult to obtain accurate measurements of small snow quantities.

Uncertainty in SP density is largely due to sampling error of exceptionally dense snow layers. We quantify this uncertainty by varying three values. Ice layer density is varied between 700 and 900 kg m<sup>-3</sup>, ice layer thickness is varied by  $\pm 1$  cm of the recorded thickness, and the density of layers identified as being too hard to sample (but not ice) is varied between 600 and 700 kg m<sup>-3</sup>. The range of integrated density values is always less than 15% of the reference density, with the largest ranges present on Glacier 2. Density values for shallow pits that contain ice lenses are particularly sensitive to changes in prescribed density and ice lens thickness.

### Distributed density

Since we find no correlation between co-located SP and FS densities (Figure 2), each set of density values is used for all four density interpolation options. Regional and glacier mean densities are higher when SP densities are used (see Supplementary Material Table 6). Density gradient with elevation differs between SP and FS densities (see Supplementary Material Table 6). At Glaciers 2 and 13, SP density decreases with elevation, likely indicating melt and/or compaction at lower elevations. SP density is independent of elevation on Glacier 4. FS density increases with elevation on Glacier 2 and there is no relationship with elevation on Glaciers 4 and 13. There is a positive linear relation between measured snow density and depth for all FS measurements but no correlation exists between SP density and elevation. Considering these results, of the four interpolation methods used our preferred method is a glacier-wide mean of SP densities. Many winter balance studies assume uniform density (e.g. Elder and others, 1991; McGrath and others, 2015; Cullen and others, 2017) and it is realistic for future studies to measure snow density profiles at a few locations in the study basin.

### Grid cell average

In an attempt to capture the spatial variability of SWE in a grid cell, we use a zigzag sampling scheme, which offers a relatively easy way to take a large number of probe measurements. The average standard deviation of all zigzags on Glacier 4 is  $\sigma_{G4ZZ} = 0.027$  m w.e., on Glacier 2 is  $\sigma_{G2ZZ} = 0.035$  m w.e. and on Glacier 13 is  $\sigma_{G13ZZ} = 0.040$  m w.e. SWE measurements for each zigzag are not normally distributed about the mean SWE (Figure 3). For simplicity, we assume uniform SWE uncertainty within grid cells across each glacier and represent this uncertainty by a normal distribution with the mean zigzag standard deviation for each glacier.

Each measured grid cell contains one to six measurements which are then averaged to give SWE grid cell average values. The distribution of grid-cell SWE values for each glacier is similar to that of Figure 2 but with fewer outliers. The zigzag standard deviation is almost two times larger than the mean standard deviation within grid cells measured along transects. However, a small number of grid cells sampled along transects have standard deviations that exceed 0.25 m w.e. We deem these values to be outliers but further work on the distribution of grid cell variability is needed. Therefore, we assume that the grid cell variability is

**Table 3.** Specific winter balance (WB [m w.e.]) estimated using linear regression and simple kriging interpolation for study glaciers. Average root mean squared error (RMSE [m w.e.]) between estimated and observed grid cells for all points, which were randomly selected and excluded from interpolation, is also shown. RMSE as a percent of the WB is shown in brackets.

	Linear Regression		Simple Kriging	
	WB	RMSE	WB	RMSE
<b>G4</b>	0.582	0.153 (26%)	0.616	0.134 (22%)
<b>G2</b>	0.577	0.102 (18%)	0.367	0.073 (20%)
<b>G13</b>	0.381	0.080 (21%)	0.271	0.068 (25%)

captured with dense sampling in zigzag grid cells. Since grid cell variability is relatively easy to quantify using zigzags, there is little need to take multiple measurements within a grid cell along a transect. Instead, transect spacing can be decreased to allow for greater spatial extent of sampling, which would better capture basin-scale variability.

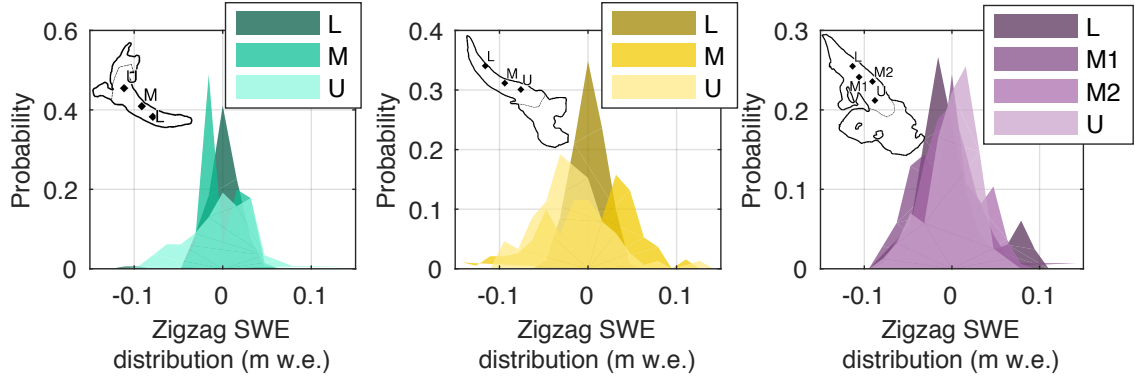
### Interpolated SWE

The choice of interpolation method affects the specific winter balance (Table 3). When using LR, the winter balance on Glaciers 4 and 2 are similar in magnitude. SK produces the highest winter balance on Glacier 4 and the lowest winter balance on Glacier 13. Winter balance estimated by SK is  $\sim 30\%$  lower than winter balance estimated by LR on Glaciers 2 and 13. However, when only the ablation area is considered, LR and SK produce winter balance estimates that differ by less than 7% for all glaciers. Extrapolation of observed SWE into the accumulation area appears to have a large effect on winter balance estimates. SWE estimated with LR and SK differ considerably in the upper accumulation areas of Glaciers 2 and 13 (Figure 4). The significant influence of elevation in the LR results in substantially higher SWE values at high elevation, whereas the accumulation area of the SK estimates approximate the mean observed SWE.

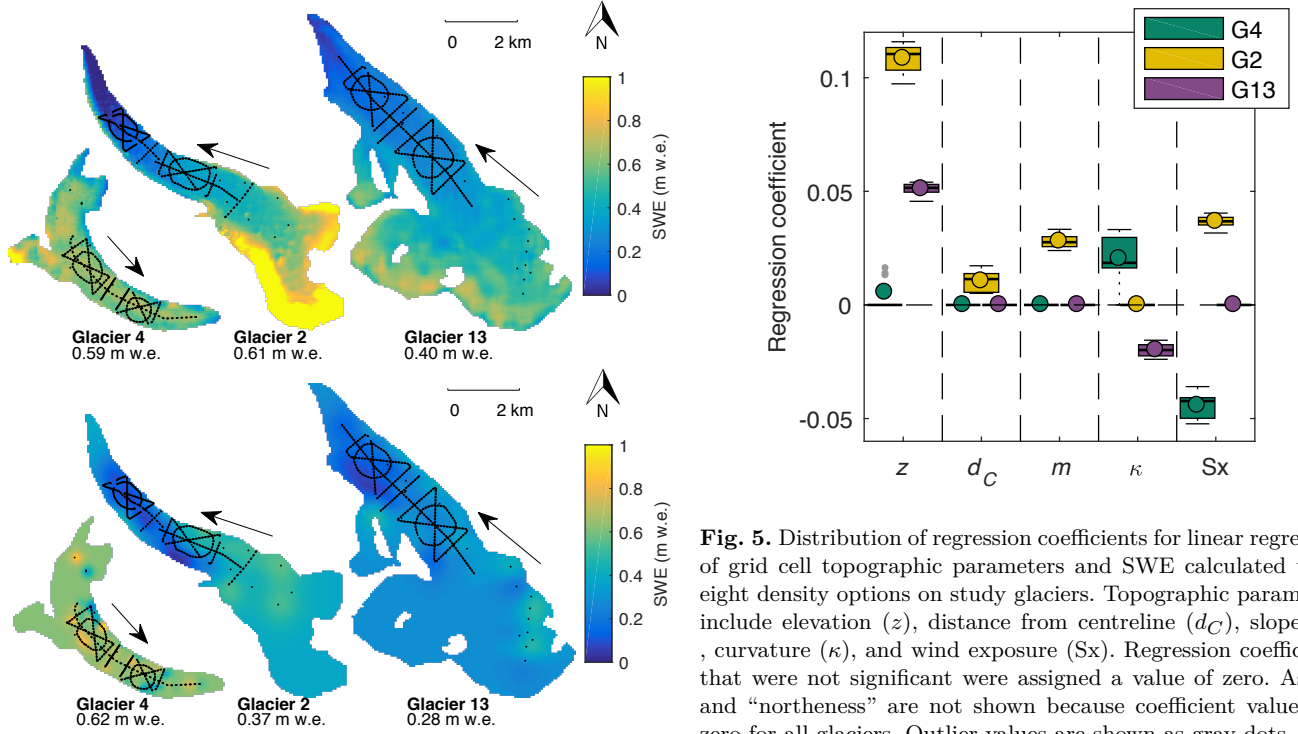
#### Linear Regression

Analysis of topographic parameters reveals that elevation is the most significant predictor for Glacier 2 and 13, while wind distribution is the most significant predictor for Glacier 4 (Figure 5). Elevation, as the predictor, is positively correlated with SWE, meaning that grid cells at higher elevation show higher SWE. While on Glacier 4 wind distribution parameter is negative (i.e. negative correlation with SWE), which indicates less snow in ‘sheltered’ areas, on the other two glaciers wind distribution is positive. Similarly, curvature is positively correlated for Glacier 4 and negatively correlated for the other two glaciers. It is possible that the elevation correlation was accentuated, especially on Glacier 13, during the field campaign due to warmer than normal temperatures and an early (1–2 weeks) start to the melt season (Yukon Snow Survey Bulletin and Water Supply Forecast, May 1, 2016). The southwestern Yukon winter snow pack in 2015 was also well below average, possibly emphasizing effects of early melt onset.





**Fig. 3.** Distribution of zigzag SWE values with the local mean subtracted on Glacier 4 (upper panel), Glacier 2 (middle panel) and Glacier 13 (lower panel). Zigzags are distributed throughout the ablation area of each glacier, with one located in the lower portion (L), one in the middle portion (M), and one in the upper portion (U). There were two zigzags in the middle ablation area of Glacier 13.



**Fig. 4.** Spatial distribution of SWE estimated using linear regression (upper) and simple kriging (lower). Grid-cell SWE observations are found using glacier wide mean snow pit density and are shown as black dots. Glacier flow directions are indicated by arrows. Specific winter balance values are also shown.

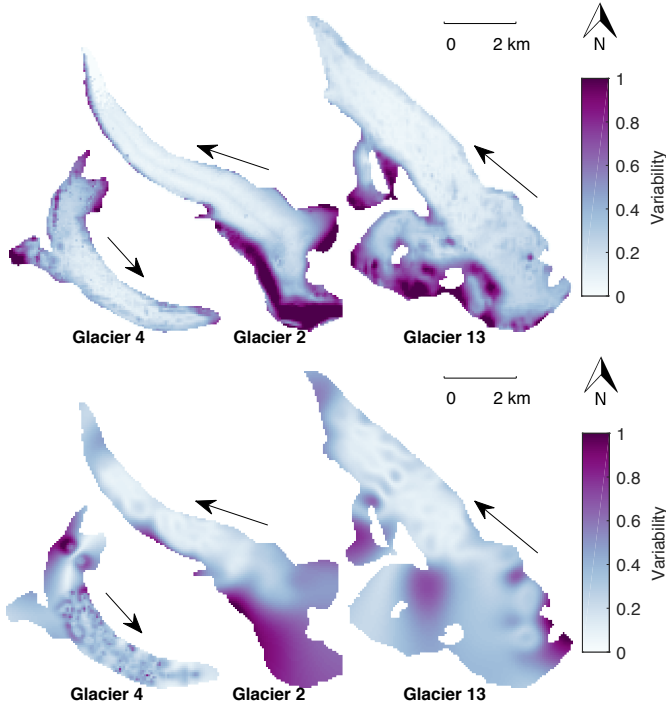
Our mixed insights into dominant predictors of accumulation are consistent with the conflicting results present in the literature. Many winter balance studies have found elevation to be the most significant predictor of SWE (e.g. Machguth and others, 2006; McGrath and others, 2015). However, accumulation elevation gradients vary considerably between glaciers (e.g. Winther and others, 1998) and other factors, such as orientation relative to dominant wind direction

**Fig. 5.** Distribution of regression coefficients for linear regression of grid cell topographic parameters and SWE calculated using eight density options on study glaciers. Topographic parameters include elevation ( $z$ ), distance from centreline ( $d_C$ ), slope ( $m$ ), curvature ( $\kappa$ ), and wind exposure ( $S_x$ ). Regression coefficients that were not significant were assigned a value of zero. Aspect and “northernness” are not shown because coefficient values are zero for all glaciers. Outlier values are shown as gray dots.

and glacier shape, have been noted to affect accumulation distribution (Machguth and others, 2006; Grabiec and others, 2011). There are also a number of accumulation studies on glaciers that found no significant correlation between accumulation and topographic parameters and the highly variable snow distribution was attributed to complex local conditions (e.g. Grabiec and others, 2011; López-Moreno and others, 2011).

Wind redistribution and preferential deposition of snow is known to have a large influence on accumulation at sub-basin scales (e.g. Dadic and others, 2010; Winstral and others, 2013; ?). Our results indicate that wind likely has an impact on snow distribution but that the wind redistribution parameter may not adequately represent this





**Fig. 6.** Uncertainty of SWE estimated using linear regression (top) and simple kriging (bottom). Uncertainty is a relative quantity measured by taking the sum of differences between one hundred estimates of distributed winter balance that include SWE uncertainty and, in the case of linear regression, regression uncertainty. The sum is then normalized for each glacier. Glacier flow directions are indicated by arrows.

impact. For example, Glacier 4 is located in a curved valley with steep side walls so having a single cardinal direction for wind may be inappropriate. Further, the scale of deposition may be smaller than the resolution of the  $S_x$  parameter estimated from our DEM. Our results corroborate McGrath and others (2015), who completed a winter balance study on six Alaskan glaciers (DEM resolutions of 5 m) and found that  $S_x$  was the only other significant parameter, besides elevation, for all glaciers. Regression coefficients were small ( $< 0.3$ ) and in some cases, negative. Sublimation from blowing snow has also been shown to be an important mass loss from ridges (e.g. Musselman and others, 2015). Incorporating snow loss as well as redistribution and preferential deposition may be needed for accurate representations of seasonal accumulation.

Since we are unable to measure SWE in grid cells that have high topographic parameter values, we must linearly extrapolate relationships. The accumulation area, where there are few observations, is most susceptible to extrapolation errors (Figure 6). This area typically also has the highest SWE values (Figure 4), affecting the specific winter balance estimated for the glacier. In our study, the dependence of SWE on elevation, especially on Glacier 2, means that LR extrapolation results in almost 2 m w.e. estimated in the parts of the accumulation area. This exceptionally large estimate of SWE is unlikely for a

continental snow pack. Extrapolating a LR that is fitted to predominantly ablation area SWE values is likely erroneous.

While a LR can be used to predict distributed SWE in other basins, we found that transfer of LR coefficients between glaciers results in large estimation error. The lowest overall root mean squared error (0.2051 m w.e.) results from calculating a LR using all available observations. Our results are consistent with Grünwald and others (2013), who found that local statistical models are able to perform well but they cannot be transferred to different regions and that regional-scale models are not able to explain the majority of variance. The inter-basin variability in our study range is greater than the intra-basin variability.

### Simple kriging

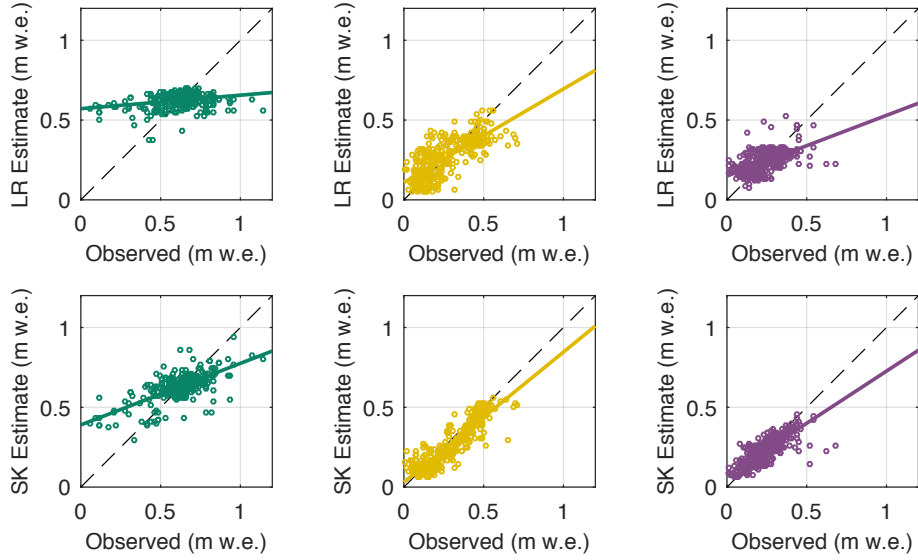
For all study glaciers, simple kriging (SK) is a better predictor of observed SWE than LR (Figure 7 and Table 3). However, the winter balance uncertainty that arises from using SK is large, and unrealistic values of 0 m w.e. winter balance can be estimated. Our observations are generally limited to the ablation area so SK estimates an almost uniform distribution of SWE in the accumulation areas of the study glaciers, which is inconsistent with observations described in the literature (e.g. Machguth and others, 2006; Grabiec and others, 2011). Extrapolation using SK leads to large uncertainty (Figure 6) in estimating winter balance, which further emphasizes the need for spatially distributed SWE observations in a glacierized basin.

SK cannot be used to understand physical processes that may be controlling snow distribution and cannot be used to estimate accumulation beyond the study area. However, fitted kriging parameters, including the nugget and spatial correlation length, can provide insight into important scales of variability. Glaciers 2 and 13 have longer correlation lengths and smaller nuggets indicating variability at large scales (see Supplementary Material Table 7). Conversely, Glacier 4 has a short correlation length and large nugget, indicating that accumulation variability occurs at small scales.

### Uncertainty analysis

Specific winter balance is affected by uncertainty introduced when interpolating density ( $\sigma_\rho$ ), when calculating grid cell SWE values ( $\sigma_{SWE}$ ), and when interpolating observations ( $\sigma_{INT}$ ). We find that when using LR and SK, interpolation uncertainty has a larger effect on winter balance uncertainty than density uncertainty or SWE uncertainty. The distribution of winter balance values that arises from SWE uncertainty is much narrower than the distribution that arises from interpolation uncertainty (Figure 8 and Table 4).

A large contributor to uncertainty arises from extrapolation beyond the sampled region, which results in high uncertainty in estimated SWE in the accumulation area (Figure 6). The winter balance distributions obtained using LR and SK overlap for each glacier but the distribution modes differ. SK generally estimating lower winter balance in the accumulation area, which lowers the overall winter balance estimate. It is important to note that although the distributions from LR are narrower than those from



**Fig. 7.** Estimated grid cell SWE found using linear regression (LR) and simple kriging (SK) plotted against observed values of SWE on Glacier 4 (left), Glacier 2 (middle) and Glacier 13 (right). Line of best fit between estimated and observed SWE is also plotted.

**Table 4.** Standard deviation ( $[ \times 10^{-2}$  m w.e.]) of winter balance distributions arising from SWE ( $\sigma_{\text{SWE}}$ ), density ( $\sigma_{\rho}$ ) and interpolation ( $\sigma_{\text{INT}}$ ) uncertainty. Result for Glacier 4 (G4), Glacier 2 (G2) and Glacier 13 (G13) are shown.

	Linear Regression			Simple Kriging		
	$\sigma_{\rho}$	$\sigma_{\text{SWE}}$	$\sigma_{\text{INT}}$	$\sigma_{\rho}$	$\sigma_{\text{SWE}}$	$\sigma_{\text{INT}}$
<b>G4</b>	1.90	0.86	2.13	2.15	0.85	14.05
<b>G2</b>	3.37	1.80	3.09	2.03	2.53	13.78
<b>G13</b>	1.68	1.12	2.80	1.27	1.15	9.65

SK, that does not necessitate that LR is a more accurate method of estimating winter balance. Based on the sources of uncertainty chosen, LR appears to be more precise than SK but the methods of calculating interpolation uncertainty are different so the distributions should not be directly compared.

SWE uncertainty is the smallest contributor to winter balance uncertainty. Therefore, obtaining the most accurate value of SWE to represent a grid cell, even a relatively large grid cell, does not need to be a priority when designing a snow survey. Many parts of a glacier are characterized by a relatively smooth surface, with roughness lengths on the order of centimetres (e.g. Hock, 2005), resulting in low SWE uncertainty. However, we assume that the sampled grid cells are representative of the uncertainty across the entire glacier, which is likely not true for areas with debris cover, crevasses and steep slopes.

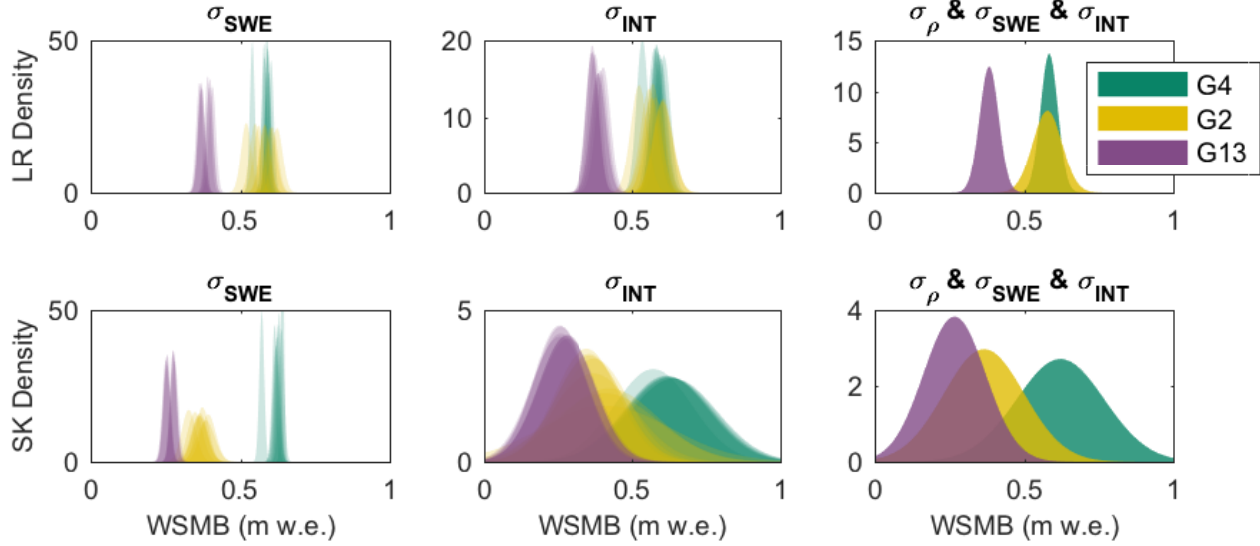
Density, SWE, and interpolation uncertainty all contribute to spatial patterns of winter balance uncertainty (Figure 6). For both LR and SK, the greatest uncertainty in estimated SWE occurs in the accumulation area. When LR is used, estimated SWE is highly sensitive to the elevation regression parameter. In the case of SK, uncertainty is greatest in areas far from observed SWE, which consist of the upper accumulation area on Glaciers 2 and 13.

Uncertainty is greatest on Glacier 4 when LR interpolation is used at the upper edges of the accumulation area, which correspond to the locations with extreme values of the wind redistribution parameter. When SK is used for interpolation on Glacier 4, uncertainty is greatest at the measured grid cells, which highlights the short correlation length and the significant effect of density interpolation on the SK SWE estimate.

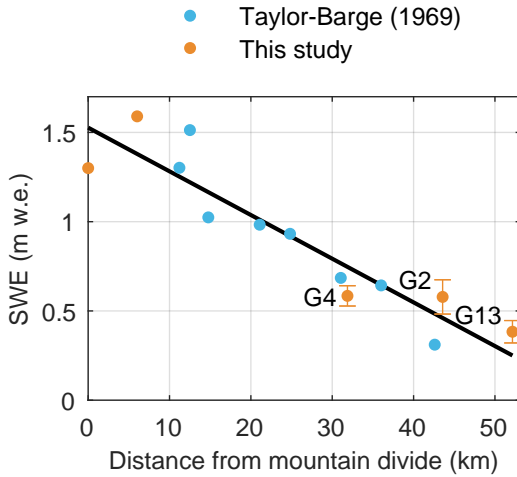
Using a Monte Carlo experiment to propagate uncertainty allowed us to quantify effects of uncertainty on estimates of winter balance. However, our analysis did not include uncertainty arising from a number of data sources, which we assumed to contribute negligibly to the uncertainty in winter balance or to be encompassed by investigated sources of uncertainty. These sources of uncertainty include error associated with SP and FS density measurement, DEM vertical and horizontal error and error associated with estimating measurement locations.

## Mountain range accumulation gradient

An accumulation gradient is observed for the continental side of the St. Elias Mountains (Figure 9). Accumulation data are compiled from Taylor-Barge (1969), the three glaciers presented in this paper, as well as two snow pits we dug near the head of the Kaskawalsh Glacier in May 2016. The data show a linear decrease in observed SWE as distance from the main mountain divide (identified by Taylor-Barge (1969)) increases, with a gradient of  $-0.024$  m w.e.  $\text{km}^{-1}$ . While the three study glaciers fit the regional relationship, the same relationship would not apply when just the Donjek Range is considered. Therefore, glacier location within a mountain range also affects glacier-wide winter balance. Interaction between meso-scale weather patterns and mountain topography is a major driver of glacier-wide accumulation. Further insight into mountain-scale accumulation trends can be achieved by investigating



**Fig. 8.** Distributions of winter balance values that arise from (left) SWE uncertainty ( $\sigma_{SWE}$ ), (middle) interpolation uncertainty ( $\sigma_{INT}$ ) and (right) all three sources of uncertainty. Results from a linear regression interpolation (top panels) and simple kriging (bottom panels) are shown. Each distribution is calculated using one of eight density interpolation methods for Glacier 4 (G4), Glacier 2 (G2) and Glacier 13 (G13).



**Fig. 9.** Relation between SWE and linear distance from St. Elias mountain divide, located at the head of the Kaskawalsh Glacier. Blue dots are snow pit derived SWE values from Taylor-Barge (1969). Orange dots furthest from the divide are mean winter balance from Glaciers 4, 2 and 13, with 95% confidence interval using a linear regression interpolation. Orange dots close to the divide are snow pit derived SWE value at two locations in the accumulation area of the Kaskawalsh Glacier collect in May 2016. Black line indicates line of best fit ( $R^2 = 0.85$ ).

moisture source trajectories and orographic precipitation contribution to accumulation.

### Limitations and future work

Extensions to this work could include an investigation of experimental design, examining the effects of DEM grid size on winter balance and resolving temporal variability. Our sampling design was chosen to extensively sample the ablation area and is likely too finely resolved for many future mass balance surveys to replicate. Determining a sampling design that minimizes error and reduces the number of measurements, known as data efficiency thresholds, would contribute to optimizing snow surveys in mountainous regions. For example, López-Moreno and others (2010) concluded that 200 – 400 observations are needed to obtain accurate and robust snow distribution models.

DEM grid cell size is known to significantly affect computed topographic parameters and the ability for a DEM to resolve important hydrological features (i.e. drainage pathways) in the landscape (Zhang and Montgomery, 1994; Garbrecht and Martz, 1994; Guo-an and others, 2001; López-Moreno and others, 2010), which can have implications for calculating a LR that uses topographic parameters. Zhang and Montgomery (1994) found that a 10 m grid cell size is an optimal compromise between increasing resolution and large data volumes. Further, the importance of topographic parameters in predicting SWE is correlated with DEM grid size (e.g. Kienzie, 2004; López-Moreno and others, 2010). A decrease in spatial resolution of the DEM results in a decrease in the importance of curvature and an increase in the importance of elevation. A detailed and ground controlled DEM is therefore needed to identify the features that drive accumulation variability. Even with a high resolution DEM, microtopography that creates small scale snow variability cannot be resolved. For example, the lower part of Glacier 2 has an undulating ice surface (on the

order of 5 m horizontal and 0.5 m vertical) that results in large variability in snow depth.

Temporal variability in accumulation is not considered in our study. While this limits the extent of our conclusions, a number of studies have found temporal stability in spatial patterns of snow accumulation and that terrain-based model could be applied reliable between years (e.g. Grünwald and others, 2013). For example, Walmsley (2015) analyzed more than 40 years of accumulation recorded on two Norwegian glaciers and found that snow accumulation is spatially heterogeneous yet exhibits robust time stability in its distribution.

## CONCLUSION

We estimate spatial accumulation patterns and specific winter balance for three glaciers (labelled as Glacier 2, Glacier 4 and Glacier 13) in the St. Elias mountains from extensive snow depth and density sampling. Our objectives are to (1) examine methods and uncertainties when moving from snow measurements to estimating winter balance and (2) show how snow variability, data error and our methodological choices interact to create uncertainty in our estimate of winter balance.

We find that the method used to interpolate observations has a large effect on winter balance estimates and its associated uncertainty. On Glacier 4, winter balance estimates are consistent between linear regression (LR) and simple kriging (SK) but both explain only a small portion of observed variance, highlighting that although the winter balance estimates are relatively precise they may not necessarily be accurate. On Glaciers 2 and 13, LR and SK are better able to estimate observed SWE values but winter balance estimates differ considerably between the two interpolation methods due to extrapolation into the accumulation area. SK is a non-parametric interpolation method that relies heavily on regular and dense sampling so extrapolation is sensitive to marginal data values and the data mean. LR employs parameters that act as proxies for physical processes, which provides insight into drivers of SWE distribution, constrains extrapolation values and can be spatially transferred. It is therefore critical that future winter balance studies report which interpolation method is used to estimate winter balance, the ability for the model to estimate observed measurements and the uncertainty that results from fitting the interpolation model.

For our study glaciers, the total winter balance uncertainty ranges from 0.03 (8%) to 0.15 (54%) m w.e. depending primarily on the interpolation method. The smallest winter balance uncertainty source is the representation of grid cell SWE. Future studies could reduce winter balance uncertainty by increasing the spatial distribution of snow depth sampling rather than obtaining many measurements within a single grid cell. In our work, increased sampling within the accumulation area would better constrain SWE extrapolation and decrease uncertainty. Our results indicate that using extrapolated data to compare with winter balance estimates from remote sensing or modelling studies may produce misleading results. If possible, comparison

studies should use observed SWE data rather than interpolated winter balance values.

Snow distribution patterns are found to differ considerably between glaciers, highlighting strong intra- and inter-basin variability and accumulation drivers acting on multiple scales. SWE distribution on Glacier 4 is highly variable, as indicated by shorter range distance, higher nugget value and lower explained variance. Glaciers 2 and 13 have lower SWE variability and elevation is the primary control of observed variation. Despite challenges in accurately estimating winter balance, our data are consistent with a previously reported linear decrease in SWE with increased distance from the main topographic divide along the continental side of the St. Elias Mountains. This trend indicates that glacier location within a mountain range has a large influence on winter balance.

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## SUPPLEMENTARY MATERIAL

### *Topographic parameters*

First, cross-validation is used to obtain a set of  $\beta_i$  values that have greater predictive ability. We select 1000 random subsets (2/3 values) of the data to fit the LR and the remaining data (1/3 values) are used to calculate a root mean squared error (RMSE) (Kohavi and others, 1995). Regression coefficients resulting in the lowest RMSE are selected. Second, we use model averaging to take into account uncertainty when selecting predictors and to also maximize predictive ability (Madigan and Raftery, 1994). Models are generated by calculating a set of  $\beta_i$  for all possible combinations of predictors. Following a Bayesian framework, model averaging involves weighting all models by their posterior model probabilities (Raftery and others, 1997). To obtain the final regression coefficients, the  $\beta_i$  values from each model are weighted according to the relative predictive success of the model, as assessed by the Bayesian Information Criterion (BIC) value (Burnham and Anderson, 2004). BIC penalizes more complex models, which further reduces the risk of overfitting.

Topographic parameters are easy to calculate proxies for physical processes, such as orographic precipitation, solar radiation effects, wind redistribution and preferential deposition. We derive all parameters (Table 5) for our study from a SPOT-5 DEM (40×40 m) (Korona and others, 2009). Two DEMs are stitched together to encompass the Donjek Range. An iterative 3D-coregistration algorithm (Berthier and others, 2007) is used to correct the horizontal ( $\sim 2$  m E,  $\sim 4$  m N) and vertical (5.4 m) discrepancy between the two DEMs before stitching.

Visual inspection of the curvature fields calculated using the full DEM shows a noisy spatial distribution that did not vary smoothly. To smooth the DEM, various smoothing algorithms and window sizes are applied and the combination that produces the highest correlation between topographic parameters and SWE is chosen. Inverse-distance weighted, Gaussian and grid cell averaging smoothing all with window sizes of 3×3, 5×5, 7×7 and 9×9 are used. Grid cell average smoothing with a 7×7 window resulted in the highest overall correlation between curvature (second derivative) and SWE as well as slope (first derivative) and SWE. We use the smoothed DEM to calculate curvature, slope, aspect and “northness”.

**Table 5.** Description of topographic parameters used in the linear regression.

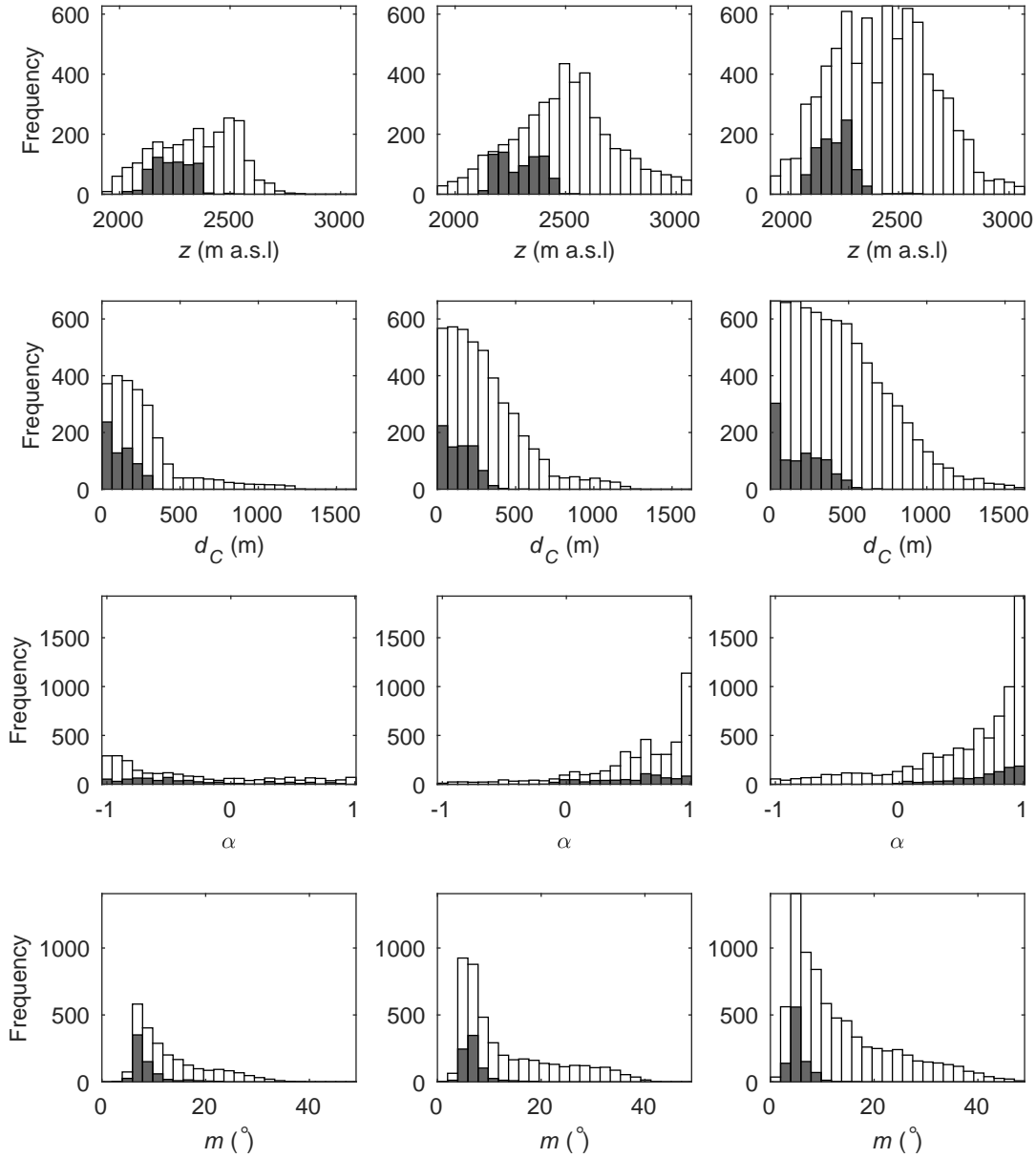
Topographic parameter	Definition	Calculation method	Notes	Source
Elevation ( $z$ )		Values taken directly from DEM		
Distance from centreline ( $d_C$ )		Minimum distance between the Easting and Northing of the north-west corner of each grid cell and a manually defined centreline		
Slope ( $m$ )	Angle between a plane tangential to the surface (gradient) and the horizontal	<code>r.slope.aspect</code> module in GRASS GIS software run through QGIS		Mitášová and Hofierka (1993); Hofierka and others (2009); Olaya (2009)
Aspect ( $\alpha$ )	Dip direction of the slope	<code>r.slope.aspect</code> module in GRASS GIS software run through QGIS	$\sin(\alpha)$ , a linear quantity describing a slope as north/south facing, is used in the regression	Mitášová and Hofierka (1993); Hofierka and others (2009); Olaya (2009)
Mean curvature ( $\kappa$ )	Average of profile (direction of the surface gradient) and tangential curvature (direction of the contour tangent)	<code>r.slope.aspect</code> module in GRASS GIS software run through QGIS	mean-concave (positive values) terrain with relative accumulation and mean-convex (negative values) terrain with relative scouring	Mitášová and Hofierka (1993); Hofierka and others (2009); Olaya (2009)
“Northness” ( $N$ )	−1 represents a vertical, south facing slope, a value of +1 represents a vertical, north facing slope, and a flat surface yields 0	Product of the cosine of aspect and sine of slope		Molotch and others (2005)
Wind exposure/shelter parameter ( $S_x$ )		Executable obtained from Adam Winstral that follows the procedure outlined in Winstral and others (2002)	Calculation based on selecting a cell within a certain angle and distance from the cell of interest that has the greatest upward slope relative to the cell of interest	Winstral and others (2002)

**Table 6.** Snow density values used for interpolating density based on snow pit (SP) densities and Federal Sampler (FS) densities. Four interpolation methods are chosen: (1) using a mean snow density for all three glaciers (Range mean density), (2) using a mean density for each glacier (Glacier mean density), (3) using a regression between density and elevation (Elevation regression), and (4) inverse-distance weighted mean density (not shown).

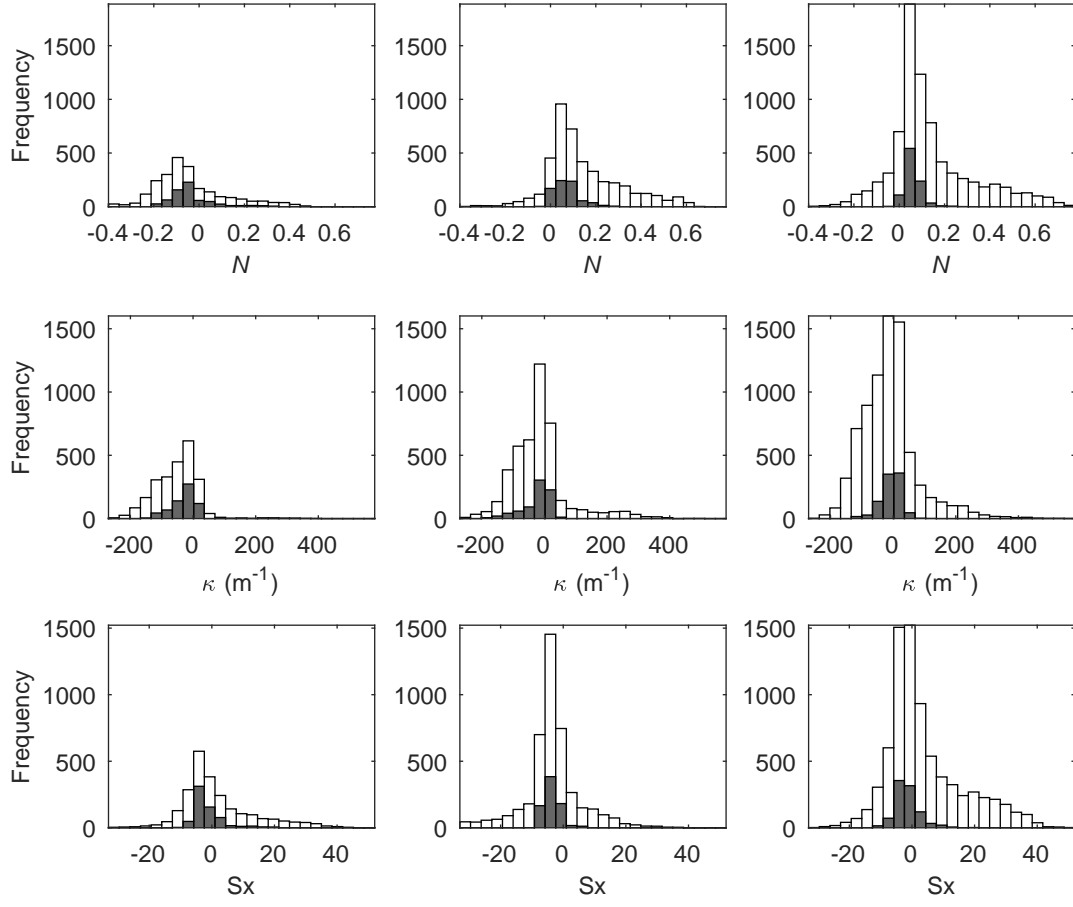
		SP density ( $\text{kg m}^{-3}$ )	FS density ( $\text{kg m}^{-3}$ )
Range mean density		342	316
Glacier mean density	G4	348	327
	G2	333	326
	G13	349	307
Elevation regression	G4	$0.03z + 274$	$-0.16z + 714$
	G2	$-0.14z + 659$	$0.24z - 282$
	G13	$-0.20z + 802$	$0.12z + 33$

**Table 7.** Range and nugget values for simple kriging interpolation

	Range (m)	Nugget ( $\times 10^3 \text{ m w.e.}$ )
<b>G4</b>	90	10.5
<b>G2</b>	404	3.6
<b>G13</b>	444	4.8



**Fig. 10.** Distribution of topographic parameters over Glacier 4 (left), Glacier 2 (middle) and Glacier 13 (right) are shown in white. Distribution of topographic parameter values from sampled grid cells in shown in gray. Topographic parameters include elevation ( $z$ ), distance from centerline ( $d_C$ ), aspect ( $\alpha$ ), slope ( $m$ ), northness ( $N$ ), mean curvature ( $\kappa$ ), and winter redistribution ( $S_x$ ).



**Fig. 11.** See Figure 10