

1 Estimating winter balance and its uncertainty from direct 2 measurements of snow depth and density on alpine glaciers

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11 **ABSTRACT.** Accurately estimating winter surface mass balance on glaciers
12 is central to assessing glacier health and predicting glacier runoff. However,
13 measuring and modelling snow distribution is inherently difficult in moun-
14 tainous terrain. Here we explore rigorous statistical methods of estimating
15 winter balance and its uncertainty from multiscale measurements of snow
16 depth and density. In May 2016 we collected over 9000 manual measurements
17 of snow depth across three glaciers in the St. Elias Mountains, Yukon,
18 Canada. Linear regression, combined with cross correlation and Bayesian
19 model averaging, as well as ordinary kriging are used to interpolate point-
20 scale values to glacier-wide estimates of winter balance. Elevation and a wind-
21 redistribution parameter exhibit the highest correlations with winter balance,
22 but the relationship varies considerably between glaciers. A Monte Carlo
23 analysis reveals that the interpolation itself introduces more uncertainty than
24 the assignment of snow density or the representation of grid-scale variability.
25 For our study glaciers, the winter balance uncertainty from all assessed sources

ranges from 0.03 m w.e. (8%) to 0.15 m w.e. (54%). Despite the challenges associated with estimating winter balance, our results are consistent with a regional-scale winter-balance gradient.

INTRODUCTION

Winter surface mass balance, or “winter balance”, is the net accumulation and ablation of snow over the winter season (Cogley and others, 2011), which constitutes glacier mass input. Winter balance (B_w) is half of the seasonally resolved mass balance, initializes summer ablation conditions and must be estimated to simulate energy and mass exchange between the land and atmosphere (e.g. Hock, 2005; Réveillet and others, 2016). Effectively representing the spatial distribution of snow on glaciers is also central to monitoring surface runoff and its downstream effects (e.g. Clark and others, 2011).

Winter balance (~~WB~~) is notoriously difficult to estimate (e.g. Dadić and others, 2010; Cogley and others, 2011). Snow distribution in alpine regions is highly variable with short correlation length scales (e.g. Anderton and others, 2004; Egli and others, 2011; Grünwald and others, 2010; Helbig and van Herwijnen, 2017; López-Moreno and others, 2011, 2013; Machguth and others, 2006; Marshall and others, 2006) and is influenced by dynamic interactions between the atmosphere and complex topography, operating on multiple spatial and temporal scales (~~e.g. Barry, 1992; Liston and Elder, 2006; Clark and others, 2011~~) (e.g. Barry, 1992; Liston and Elder, 2006; Clark and others, 2011; Scipión and others, 2013). Simultaneously extensive, high resolution and accurate snow distribution measurements on glaciers are therefore difficult to ~~obtain~~ (e.g. Cogley and others, 2011; McGrath and others, 2015). ~~Physically based models are acquire~~ (e.g. Cogley and others, 2011; McGrath and others, 2015) and obtaining such measurements is further complicated by the inaccessibility of many glacierized regions during the winter. ~~Use of physically based models to estimate winter balance is~~ computationally intensive and ~~require~~ requires detailed meteorological data to drive ~~them~~ the models (Dadić and others, 2010). As a result, there is significant uncertainty in estimates of winter balance, thus limiting the ability of models to represent current and projected glacier conditions.

Studies that have focused on obtaining detailed estimates of ~~WB~~ B_w have used a wide range of observational techniques, including direct measurement of snow depth and density (e.g. Cullen and others, 2017), lidar or photogrammetry (e.g. Sold and others, 2013) and ground-penetrating radar (e.g. Machguth and others, 2006; Gusmeroli and others, 2014; McGrath and others, 2015). Spatial coverage of direct measurements

55 is generally limited and often comprises an elevation transect along the glacier centreline (e.g. Kaser and
56 others, 2003). Measurements are ~~often~~ typically interpolated using linear regression on only a few topographic
57 parameters (e.g. MacDougall and Flowers, 2011), with elevation being the most common. Other established
58 techniques include hand contouring (e.g. Tangborn and others, 1975), kriging (e.g. Hock and Jensen, 1999)
59 and attributing measured winter balance values to elevation bands (e.g. Thibert and others, 2008). Physical
60 snow models have been used to estimate spatial patterns of winter balance (e.g. Mott and others, 2008; Schuler
61 and others, 2008; Dadić and others, 2010) but availability of the required meteorological data generally
62 prohibits their widespread application. Error analysis is rarely undertaken and few studies have thoroughly
63 investigated uncertainty in spatially distributed estimates of winter balance (c.f. Schuler and others, 2008).

64 More sophisticated snow-survey designs and statistical models of snow distribution are widely used
65 in the field of snow science. Surveys described in the snow science literature are generally spatially
66 extensive and designed to measure snow depth and density throughout a basin, ensuring that all terrain
67 types are sampled. A wide array of measurement interpolation methods are used, including linear
68 (e.g. López-Moreno and others, 2010) and non-linear regressions (e.g. Molotch and others, 2005) that
69 include numerous terrain parameters, as well as geospatial interpolation (~~e.g. Erxleben and others, 2002~~)
70 (e.g. Erxleben and others, 2002; Cullen and others, 2017) including various forms of kriging. Different
71 interpolation methods are also combined; for example, regression kriging (see Supplementary Material) adds
72 kriged residuals to a field obtained with linear regression (e.g. Balk and Elder, 2000). Physical snow models
73 such as SnowTran-3D (Liston and Sturm, 1998), Alpine3D (Lehning and others, 2006), and SnowDrift3D
74 (Schneiderbauer and Prokop, 2011) are widely used, and errors in estimating snow distribution have been
75 examined from theoretical (e.g. Trujillo and Lehning, 2015) and applied perspectives (e.g. Turcan and Loijens,
76 1975; Woo and Marsh, 1978; Deems and Painter, 2006).

77 The goals of this study are to (1) critically examine methods of converting direct snow depth and density
78 measurements to distributed estimates of winter balance and (2) identify sources of uncertainty, evaluate
79 their magnitude and assess their combined contribution to uncertainty in glacier-wide winter balance. We
80 focus on commonly applied, low-complexity methods of measuring and estimating winter balance in the
81 interest of making our results broadly applicable.

82 STUDY SITE

83 The St. Elias Mountains (Fig. 1a) rise sharply from the Pacific Ocean, creating a significant climatic gradient
84 between coastal maritime conditions, generated by Aleutian–Gulf of Alaska low-pressure systems, and interior

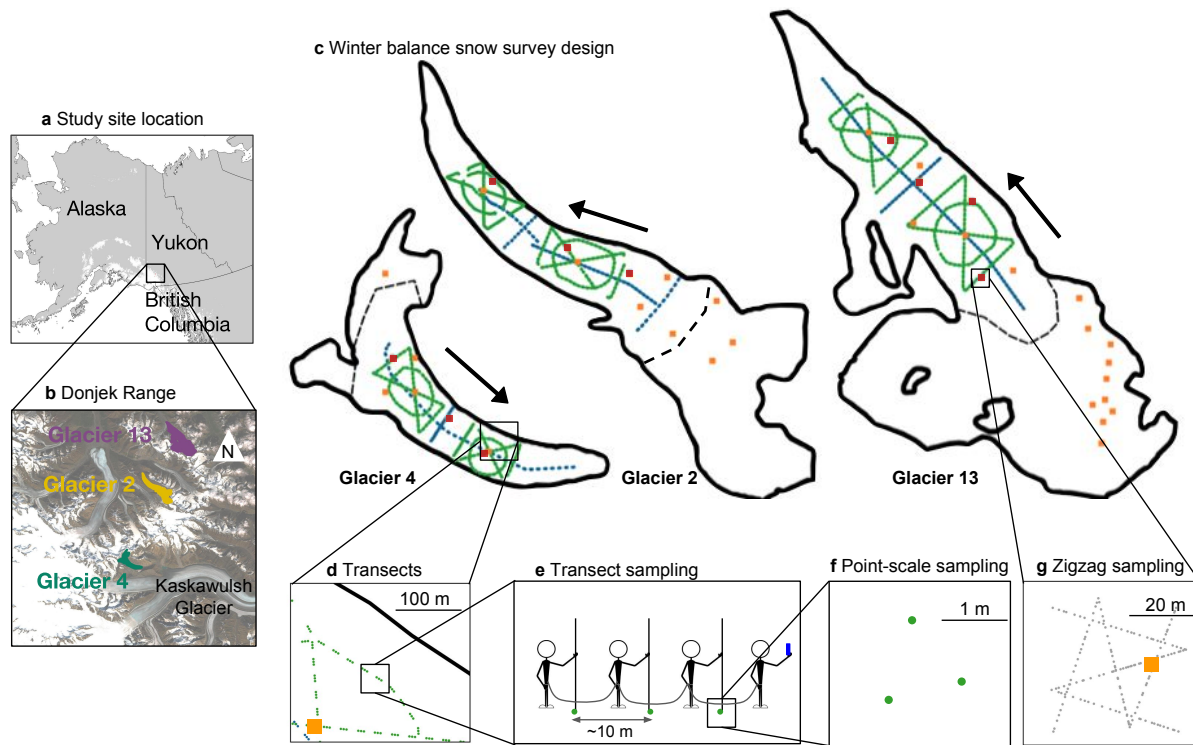


Fig. 1. Study area location and sampling design for Glaciers 4, 2 and 13. (a) Study region in the Donjek Range of the St. Elias Mountains of Yukon, Canada. (b) Study glaciers located along a southwest-northeast transect through the Donjek Range. The local topographic divide is shown as a dashed line. Imagery from Landsat8 (5 September 2013, data available from the U.S. Geological Survey). (c) Details of the snow-survey sampling design, with centreline and transverse transects (blue dots), hourglass and circle designs (green dots) and locations of snow density measurements (orange squares). Arrows indicate ice-flow directions. Approximate location of ELA on each glacier is shown as a black dashed line. (d) Close up of linear and curvilinear transects. (e) Configuration of navigator and observers. (f) Point-scale snow-depth sampling. (g) Linear-random snow-depth measurements in ‘zigzag’ design (grey-red dots) with one density measurement (orange square) per zigzag.

continental conditions, driven by the Yukon–Mackenzie high-pressure system (Taylor-Barge, 1969). The boundary between the two climatic zones is generally aligned with the divide between the Hubbard and Kaskawulsh Glaciers, approximately 130 km from the coast. Research on snow distribution and glacier mass balance in this area is limited. A series of research programs, including Project “Snow Cornice” and the Icefield Ranges Research Project, were operational in the 1950s and 60s (Wood, 1948; Danby and others, 2003) and in the last 30 years, there have been a few long-term studies on selected alpine glaciers (e.g. Clarke, 2014) as well as several regional studies of glacier mass balance and dynamics (e.g. Arendt and others, 2008; Burgess and others, 2013; Waechter and others, 2015).

Table 1. Physical characteristics of the study glaciers and May 2016 winter-balance survey details, including number of snow-depth measurement locations along transects (n_T), total length of transects (d_T), number of combined snow pit and Federal Sampler density measurement locations (n_p) and number of zigzag surveys (n_{zz}).

	Location	Location	Elevation (m a.s.l)			Slope (°)	Area	
	UTM Zone 7	UTM Zone 7	Mean	Range	ELA	Mean	$n_T d_T$ (km²)	$n_p n_{zz}$
height	Glacier 4	595470 E 6740730 N	2344	1958–2809	~2500	12.8	3.8	4–7 May 2016 649 13.1 10 3
	Glacier 2	601160 E 6753785 N	2495	1899–3103	~2500	13.0	7.0	8–11 May 2016 762 13.6 11 3
	Glacier 13	604602 E 6763400 N	2428	1923–3067	~2380	13.4	12.6	

93 We carried out winter balance surveys on three unnamed glaciers in the Donjek Range of the St. Elias
 94 Mountains. The Donjek Range is located approximately 40 km to the east of the regional mountain divide
 95 and has an area of about 30×30 km². Glacier 4, Glacier 2 and Glacier 13 (labelling adopted from Crompton
 96 and Flowers (2016)) are located along a southwest-northeast transect through the range (Fig. 1b, Table 1).
 97 These small alpine glaciers are generally oriented southeast-northwest, with Glacier 4 having a predominantly
 98 southeast aspect and Glaciers 2 and 13 have generally northwest aspects. The glaciers are situated in valleys
 99 with steep walls and have simple geometries. Based on a detailed study of Glacier 2 (Wilson and others,
 100 2013) and related theoretical modelling (Wilson and Flowers, 2013) we suspect all of the study glaciers to
 101 be polythermal.

Table 2. Details of the May 2016 winter-balance survey, including number of snow-depth measurement locations along transects (n_T), total length of transects (d_T), number of combined snow pit and Federal Sampler density measurement locations (n_p), number of zigzag surveys (n_{zz}), number (as percent of total number of gridcells, and of the number of gridcells in the ablation area) of gridcells sampled (n_s) and the elevation range (as percent of total elevations range and of ablation-area elevation range).

	Date	n_T	d_T (km)	n_p	n_{zz}	n_s	Elevation range (m a.s.l.)
Glacier 4	4–7 May 2016	649	13.1	7	3	<u>295</u> (12%, 21%)	<u>2015–2539</u> (62%, 97%)
Glacier 2	8–11 May 2016	762	13.6	7	3	<u>353</u> (8%, 14%)	<u>2151–2541</u> (32%, 47%)
Glacier 13	12–15 May 2016	941	18.1	20 19	4	<u>468</u> (6%, 14%)	<u>2054–2574</u> (45%, 62%)

METHODS

Estimating glacier-wide winter balance (B_w) involves transforming measurements of snow depth and density into values of winter balance distributed across a defined grid (b_w). We do this in four steps. (1) Obtain direct measurements of snow depth and density in the field. (2) Assign density values to all depth-measurement locations to calculate point-scale values of WB_{b_w} at each location. (Winter balance, measured in units of metres water equivalent (m w.e.), can be estimated as the product of snow depth and depth-averaged density. (3) Average all point-scale values of b_w within each gridcell of a digital elevation model (DEM) to obtain the gridcell-averaged $WB_{gridcell-averaged b_w}$. (4) Interpolate and extrapolate these gridcell-averaged WB_{b_w} values to obtain estimates of WB (in m w.e.) in b_w in each gridcell across the domain. B_w is then calculated by taking the average of all gridcell-averaged b_w values for each glacier. For brevity, we refer to these four steps as (1) field measurements, (2) density assignment, (3) gridcell-averaged WB_{b_w} and (4) distributed WB_{b_w} . Detailed methodology for each step is outlined below. We use the SPIRIT SPOT-5 DEM (40×40 m) from 2005 (Korona and others, 2009) throughout this study.

Field measurements

Our sampling campaign involved four people and occurred between 5–15 May 2016, which falls within the period of historical peak snow accumulation in southwestern Yukon (Yukon Snow Survey Bulletin and Water Supply Forecast, May 1, 2016). Snow depth is generally accepted to be more variable than density (Elder and others, 1991; Clark and others, 2011; López-Moreno and others, 2013) so we chose a sampling design that resulted in a high ratio (~55:1) of snow depth to density measurements. In total, we collected more than 9000 snow-depth measurements and more than 100 density measurements throughout the study area (Table).

During the field campaign there were two small accumulation events. The first, on 6 May 2016, also involved high winds so accumulation could not be determined. The second, on 10 May 2016, resulted in 0.01 m w.e accumulation measured at one location on Glacier 2. Assuming both accumulation events contributed a uniform 0.01 m w.e accumulation to all study glaciers then our survey did not capture ~3% and ~2% of estimated B_w on Glaciers 4 and 2, respectively. We therefore assume that these accumulation events were negligible and apply no correction. Positive temperatures and clear skies occurred between 11–16 May 2016, which we suspect resulted in melt occurring on Glacier 13. The snow in the lower part of the ablation area of Glacier 13 was isothermal and showed clear signs of melt and metamorphosis. The total amount of melt

during the study period was estimated using a degree-day model and found to be small (<0.01 m w.e., see Supplementary Material) so no corrections were made.

Sampling design

The snow surveys were designed to capture variability in snow depth at regional, basin, gridcell and point scales (Clark and others, 2011). To capture variability at the regional scale we chose three glaciers along a transect aligned with the dominant precipitation gradient (Fig. 1b) (Taylor-Barge, 1969). To account for basin-scale variability, snow depth was measured along linear and curvilinear transects on each glacier (Fig. 1c) with a sample spacing of 10–60 m (Fig. 1d). Sample spacing was constrained by protocols for safe glacier travel, while survey scope was constrained by the need to complete all surveys within the period of peak accumulation. We selected centreline and transverse transects as the most commonly used survey designs in winter balance studies (e.g. Kaser and others, 2003; Machguth and others, 2006) as well as an hourglass pattern with an inscribed circle, which allows for sampling in multiple directions and easy travel (personal communication from C. Parr, 2016). To capture variability at the grid scale, we densely sampled up to four gridcells on each glacier using a linear-random sampling design (Shea and Jamieson, 2010) we term a ‘zigzag’. To capture point-scale variability, each observer made 3–4 depth measurements within ~ 1 m (Fig. 1ef) at each transect measurement location. ~~In total, we collected more than 9000 snow-depth measurements throughout the study area (Table 1).~~

Snow depth: transects

~~Winter balance can be estimated as the product of snow depth and depth-averaged density. Snow depth is generally accepted to be more variable than density (Elder and others, 1991; Clark and others, 2011; López-Moreno and others, 2013) so we chose a sampling design that resulted in a high ratio ($\sim 55:1$) of snow depth to density measurements. Our sampling campaign involved four people and occurred between 5–15 May 2016, which falls within the period of historical peak snow accumulation in southwestern Yukon (Yukon Snow Survey Bulletin and Water Supply Forecast, May 1, 2016).~~ While roped-up for glacier travel with fixed distances between observers, the lead observer used a single-frequency GPS unit (Garmin GPSMAP 64s) to navigate between predefined transect measurement locations (Fig. 1e). The remaining three observers used 3.2 m graduated aluminum avalanche probes to make snow-depth measurements (Kinar and Pomeroy, 2015). The locations of each set of depth measurements, made by the second, third and fourth observers, are estimated using the recorded location of the first observer, the approximate distance between observers and the direction of travel. The 3–4 point-scale depth

measurements are averaged to obtain a single depth measurement at each transect measurement location.
When considering snow variability at the point scale as a source of uncertainty in snow depth measurements,
we find that the mean standard deviation of point-scale snow depth measurements is found to be <7% of
the mean snow depth for all study glaciers.

Snow-depth sampling was concentrated in the ablation area to ensure that only snow from the current accumulation season was measured. The boundary between snow and firn in the accumulation area can be difficult to detect and often misinterpreted, especially when using an avalanche probe (Grünwald and others, 2010; Sold and others, 2013). We intended to use a firn corer to measure winter balance in the accumulation area, but cold snow combined with positive air temperatures led to cores being unrecoverable. Successful snow depth ~~and density~~ measurements within the accumulation area were made either in snow pits or using a Federal Sampler (described below) to unambiguously identify the snow–firn transition.

Snow depth: zigzags

~~To capture snow depth variability within a single DEM gridecell, we implemented a linear random zigzag sampling design (Shea and Jamieson, 2010).~~ We measured depth at random intervals of 0.3–3.0 m along two ‘Z’-shaped patterns (Shea and Jamieson, 2010), resulting in 135–191 measurements per zigzag, within three to four ~~40 × 40~~ 40 × 40 m gridcells (Fig. 1g) per glacier. Random intervals were machine-generated from a uniform distribution in sufficient numbers that each survey was unique. Zigzag locations were randomly chosen within the upper, middle and lower regions of the ablation area of each glacier. ~~A fourth zigzag was measured~~ Extra time in the field allowed us to measure a fourth zigzag on Glacier 13 in the central ablation area at ~2200 m a.s.l.

Snow density

Snow density was measured using a Snowmetrics wedge cutter in three snow pits on each glacier, ~~as well as with a Geo Scientific Ltd. metric Federal Sampler.~~ Within the snow pits (SP), we measured a vertical density profile (in ~~5–10~~ cm increments) with the ~~5 × 10 × 10~~ 5 × 5 × 10 cm wedge-shaped cutter (250 cm³) and a Presola 1000 g spring scale ~~(e.g. Gray and Male, 1981; Fierz and others, 2009)~~ (e.g. Gray and Male, 1981; Fierz and others, 2009; Kinar and Pomeroy, 2015). Wedge-cutter error is approximately ±6% (e.g. Proksch and others, 2016; Carroll, 1977). Uncertainty in estimating density from ~~snow-pit~~ SP measurements also stems from incorrect assignment of density to layers that cannot be sampled (e.g. ice lenses and hard layers). We attempt to quantify this uncertainty by varying estimated ice-layer thickness by ±1 cm (≤100%) of the recorded thickness, ice layer density between 700 and 900 kg m⁻³ and

the density of layers identified as being too hard to sample (but not ice) between 600 and 700 kg m⁻³. When considering all three sources of uncertainty, the range of integrated density values is always less than 15% of the reference density. Depth-averaged densities for shallow pits (<50 cm) that contain ice lenses are particularly sensitive to changes in prescribed density and ice-lens thickness.

While ~~snow-pits~~ SP provide the most accurate measure of snow density, digging and sampling a ~~snow~~ pit-SP is time and labour intensive. Therefore, a ~~Federal-Snow-Geo Scientific Ltd. metric Federal~~ Sampler (FS) (Clyde, 1932) with a 3.2–3.8 cm diameter sampling tube, which directly measures depth-integrated snow-water equivalent, was used to augment the ~~snow-pit~~ SP measurements. A minimum of three ~~Federal~~ Sampler-FS measurements were taken at each of 7–19 locations on each glacier and an additional eight ~~Federal-Sampler-FS~~ measurements were co-located with ~~each snow-pit-profile~~ two SP profiles for each glacier. Measurements for which the snow core length inside the sampling tube was less than 90% of the snow depth were discarded. Densities at each measurement location (eight at each ~~snow-pit~~ SP, three elsewhere) were then averaged, with the standard deviation taken to represent the uncertainty.

~~During the field campaign there were two small accumulation events. The first, on 6 May 2016, also involved high winds so accumulation could not be determined. The second, on 10 May 2016, resulted in 0.01 m w.e accumulation measured at one location on Glacier 2. Positive temperatures and clear skies occurred between 11–16 May 2016, which we suspect resulted in melt occurring on Glacier 13. The snow in the lower part of the ablation area of Glacier 13 was isothermal and showed clear signs of melt and metamorphosis. The total amount of accumulation and melt during the study period could not be estimated so no corrections were made.~~ The mean standard deviation of FS-derived density was $\leq 4\%$ of the mean density for all glaciers.

Density assignment

Measured snow density must be interpolated or extrapolated to estimate point-scale ~~winter-balance~~ b_w at each snow-depth sampling location. We employ four commonly used methods to interpolate and extrapolate density (Table 3): (1) calculate mean density over an entire mountain range (e.g. Cullen and others, 2017), (2) calculate mean density for each glacier (e.g. Elder and others, 1991; McGrath and others, 2015), (3) linear regression of density on elevation for each glacier (e.g. Elder and others, 1998; Molotch and others, 2005) and (4) calculate mean density using inverse-distance weighting (e.g. Molotch and others, 2005) for each glacier. Densities derived from ~~snow-pit-(SP)-measurements and the Federal Sampler-(FS)-~~ SP and FS measurements are treated separately, for reasons explained below, resulting in eight possible methods of assigning density.

Table 3. Eight methods used to estimate snow density at unmeasured locations. Total number of resulting density values given in parentheses, with n_T the total number of snow-depth measurement locations along transects (Table 1).

Method code	Source of measured snow density		Density assignment method
	<i>Snow pit</i>	<i>Federal</i>	
		<i>Sampler</i>	
S1	■		Mean of measurements
F1		■	across all glaciers (1)
S2	■		Mean of measurements
F2		■	for each glacier (3)
S3	■		Regression of density on
F3		■	elevation for a glacier (n_T)
S4	■		Inverse distance weighted
F4		■	mean for a glacier (n_T)

Gridcell-averaged winter balance

We average one to six (mean of 2.1 measurements) point-scale values of ~~WB within each 40 × 40 m~~ b_w within each DEM gridcell to obtain the gricell-averaged ~~WB~~ b_w . The locations of individual measurements have uncertainty due to the error in the horizontal position given by the GPS unit and the estimation of observer location based on the recorded GPS positions of the navigator. This location uncertainty could result in the incorrect assignment of a point-scale ~~WB~~ b_w measurement to a particular gridcell. However, this source of error is not further investigated because we assume that the uncertainty ~~in gricell-averaged WB resulting from incorrect locations of point-scale b_w values~~ is captured in the ~~zigzag measurements uncertainty derived from zigzag measurements, as~~ described below. ~~Uncertainty Error~~ due to having multiple observers ~~was also evaluated. There are~~ is also evaluated by conducting an analysis of variance (ANOVA) of snow-depth measurement along a transect and testing for differences between observers. We find no significant differences between snow-depth measurements made by observers along any transect ($p > 0.05$), with the exception of the first transect on Glacier 4 (51 measurements) ~~—, where snow depth values collected by one observer were, on average, greater than the snow depth measurements taken by the other two observers ($p < 0.01$). Since this was the first transect and the only one to show differences by observer, this difference can be considered~~

an anomaly. We conclude that observer bias is not an important effect in this study and therefore apply no observer corrections to the data.

Distributed winter balance

Gridcell-averaged values of $WB - b_w$ are interpolated and extrapolated across each glacier using linear regression (LR) and simple kriging (SK) ordinary kriging (OK). The regression-LR relates gridcell-averaged WB and b_w to various topographic parameters, as this method and we use this method because it is simple and has precedent for success (e.g. McGrath and others, 2015). Instead of a basic regression-LR however, we use cross-validation and to prevent data overfitting as well as model averaging to test allow for all combinations of the chosen topographic parameters. We compare the regression approach with simple kriging (SK) LR approach with OK, a data-driven interpolation method free of any physical interpretation (e.g. Hock and Jensen, 1999).

Linear regression

In the regression-LR, we use commonly applied topographic parameters as in McGrath and others (2015), including elevation, slope, aspect, curvature, “northness” and a wind-redistribution parameter (S_x from Winstral and others (2002)); we add distance-from-centreline as an additional parameter. Topographic parameters are standardized for use in the LR. For details on data and methods used to estimate the topographic parameters see the Supplementary Material and Pulwinski (2017). Our sampling design ensured that the ranges of topographic parameters associated with our measurement locations represent more than 70% of the total area of each glacier (except elevation on Glacier 2, where our measurements captured only 50%). Topographic parameters are standardized and then weighted by

The goal of the LR is to obtain a set of fitted regression coefficients (β_i) calculated by minimizing the sum of squares of the vertical deviations of each datum from the regression line (Davis and Sampson, 1986). For details on data and methods used to estimate the topographic parameters see the Supplementary Material. To that correspond to each topographic parameter and to a model intercept. The LR implemented in this study is an extension of a basic multiple linear regression; we use cross-validation to avoid overfitting the data and model averaging to incorporate every possible combination of topographic parameters; cross-validation and model averaging are implemented.

First, cross-validation is used to obtain a set of β_i values that have the greatest predictive ability (Kohavi and others, 1995). We randomly select 1000 subsets of the data (2/3 of the values) to fit the LR and fit a basic multiple linear regression (implemented in MATLAB) to the data subsets, thus obtaining

1000 sets of β_i . The basic multiple linear regression calculates a set of β_i by minimizing the sum of squares of the vertical deviations of each datum from the regression line (Davis and Sampson, 1986). Distributed b_w is then calculated using each set of β_i by weighting topographic parameters by their corresponding β_i values for all DEM gridcells. We then use the remaining data (1/3 of the values) to calculate a root mean squared error (RMSE) (Kohavi and others, 1995) between the estimated b_w and the observed b_w for corresponding locations. From the 1000 sets of β_i values, we select the set that results in the lowest RMSE.

Second, we use model averaging to account for uncertainty when selecting predictors and to maximize the model's predictive ability (Madigan and Raftery, 1994). Models are generated by calculating a set of β_i (as described above) for all possible combinations of topographic parameters, resulting in 2^7 models (i.e. 2^7 sets of β_i with the greatest predictive ability for each linear combination of topographic parameters). Using a Bayesian framework, model averaging involves weighting all models by their posterior model probabilities (Raftery and others, 1997). To obtain the final regression coefficients, the β_i values from each model are weighted according to the We weight the models according to their relative predictive success of the model, as assessed by the value of the Bayesian Information Criterion (BIC) (Burnham and Anderson, 2004). BIC penalizes more complex models, which further reduces the risk of overfitting. The distributed WB is then final set of β_i is then the weighted sum of β_i from all models. Distributed b_w is obtained by applying the resulting regression coefficients final set of β_i to the topographic parameters associated with each gridcell.

~~Simple Ordinary~~ kriging

~~Simple kriging (SK)~~ Kriging is a data-driven method of estimating variables at unsampled locations by using the isotropic spatial correlation (covariance) of measured values to find a set of optimal weights (Davis and Sampson, 1986; Li and Heap, 2008). ~~Simple kriging~~ Kriging assumes spatial correlation between sampling locations that are distributed across a surface and then applies the correlation to interpolate between these locations. Many forms of kriging have been developed to accommodate different data types (e.g. Li and Heap, 2008, and sources within). Ordinary kriging (OK) is the most basic form of kriging where the mean of the estimated field is unknown. Unlike LR, OK is not useful for generating hypotheses to explain the physical controls on snow distribution, nor can it be used to estimate winter balance on unmeasured glaciers. However, we chose to use OK because it does not require external inputs and is therefore a means of obtaining B_w that is free of physical interpretation beyond the information contained in the covariance matrix.

We used the DiceKriging R package (Roustant and others, 2012) to calculate the maximum likelihood covariance matrix, as well as the range distance (θ) and nugget for gridcell-averaged values of winter balance. The range distance is a measure of data correlation length and the nugget is the residual that encompasses sampling-error variance as well as the spatial variance at distances less than the minimum sample spacing (Li and Heap, 2008). ~~Unlike topographic regression, simple kriging is not useful for generating hypotheses to explain the physical controls on snow distribution, nor can it be used to estimate winter balance on unmeasured glaciers.~~ A Matérn covariance function with $\nu=5/2$ is used to define a stationary and isotropic covariance and covariance kernels are parameterized as in Rasmussen and Williams (2006).

Uncertainty analysis using a Monte Carlo approach

Three sources of uncertainty are considered separately: the uncertainty due to (1) grid-scale variability of b_w (σ_{GS}), (2) the assignment of snow density (σ_ρ) and (3) interpolating and extrapolating gridcell-averaged values of b_w (σ_{INT}). To quantify the uncertainty of grid-scale and interpolation uncertainty on estimates of ~~glacier-wide WB~~ B_w we conduct a Monte Carlo analysis, which uses repeated random sampling of input variables to calculate a distribution of output variables (Metropolis and Ulam, 1949). We repeat the random sampling process 1000 times, resulting in a distribution of values of the ~~glacier-wide WB~~ B_w based on uncertainties associated with the four steps outlined above. ~~We use the standard deviation of this distribution as a useful metric of uncertainty on the glacier-wide WB.~~ Three Individual sources of uncertainty are ~~considered separately: the uncertainty due to (1) grid-scale variability of WB (σ_{GS}), (2) the assignment of snow density (σ_ρ) and (3) interpolating and extrapolating gridcell-averaged values of WB (σ_{INT}).~~ These individual sources of uncertainty are propagated through the conversion of snow depth and density measurements to ~~glacier-wide WB~~ B_w . Finally, the combined effect of all three sources of uncertainty on the ~~glacier-wide WB~~ B_w is quantified. We use the standard deviation of the distribution of B_w as a useful metric of B_w uncertainty. Density assignment uncertainty is calculated as the standard deviation of the eight resulting values of B_w . We calculate a relative uncertainty, as the normalized sum of differences between every pair of one hundred distributed ~~WB~~ b_w estimates including σ_{GS} and σ_{INT} , to investigate the spatial patterns in b_w uncertainty.

Grid-scale uncertainty (σ_{GS})

We make use of the zigzag surveys to quantify the true variability of ~~WB~~ b_w at the grid scale. Our limited data do not permit a spatially-resolved assessment of grid-scale uncertainty, so we characterize this uncertainty as uniform across each glacier and represent it by a normal distribution. The distribution is centred at zero and

has a standard deviation equal to the mean standard deviation of all zigzag measurements for each glacier. For each iteration of the Monte Carlo, ~~WB~~ $\underline{b_w}$ values are randomly chosen from the distribution and added to the values of gridcell-averaged ~~WB~~ $\underline{b_w}$. These perturbed gridcell-averaged values of ~~WB~~ $\underline{b_w}$ are then used in the interpolation. We represent uncertainty in ~~glacier-wide WB~~ $\underline{B_w}$ due to grid-scale uncertainty (σ_{GS}) as the standard deviation of the resulting distribution of ~~glacier-wide WB~~ $\underline{B_w}$ estimates.

Density assignment uncertainty (σ_ρ)

We incorporate uncertainty due to the method of density assignment by carrying forward all eight density interpolation methods (Table 3) when estimating ~~glacier-wide WB~~ $\underline{B_w}$. By choosing to retain even the least plausible options, as well as the questionable FS data, this approach results in a generous assessment of uncertainty. We represent the ~~glacier-wide WB~~ $\underline{B_w}$ uncertainty due to density assignment uncertainty (σ_ρ) as the standard deviation of ~~glacier-wide WB~~ $\underline{B_w}$ estimates calculated using each density assignment method.

Interpolation uncertainty (σ_{INT})

We represent the uncertainty due to interpolation/~~extrapolation~~ of gridcell-averaged ~~WB~~ $\underline{b_w}$ in different ways for LR and ~~SK~~ \underline{OK} . LR interpolation uncertainty is represented by a multivariate normal distribution of possible regression coefficients (β_i). The standard deviation of each distribution is calculated using the covariance of ~~regression coefficients~~ $\underline{\beta_i}$ as outlined in Bagos and Adam (2015), which ensures that ~~regression coefficients~~ $\underline{\beta_i}$ are internally consistent. The β_i distributions are randomly sampled and used to calculate gridcell-estimated ~~WB~~ $\underline{b_w}$.

~~SK~~ \underline{OK} interpolation uncertainty is represented by the ~~95% confidence interval for standard deviation for each~~ gridcell-estimated ~~values of WB value of~~ $\underline{b_w}$ generated by the DiceKriging package. ~~From this confidence interval, the standard deviation of each gridcell-estimated WB is then calculated.~~ The standard deviation of ~~glacier-wide WB~~ $\underline{B_w}$ is then found by taking the square root of the average variance of each gridcell-estimated ~~WB~~ $\underline{b_w}$. The final distribution of ~~glacier-wide WB~~ $\underline{B_w}$ values is centred at the ~~glacier-wide WB estimated with SK~~ $\underline{B_w}$ estimated with ~~OK~~ \underline{OK} . For simplicity, the standard deviation of ~~glacier-wide WB~~ $\underline{B_w}$ values that result from either LR or ~~SK interpolation~~ $\underline{OK interpolation/extrapolation}$ uncertainty is referred to as σ_{INT} .

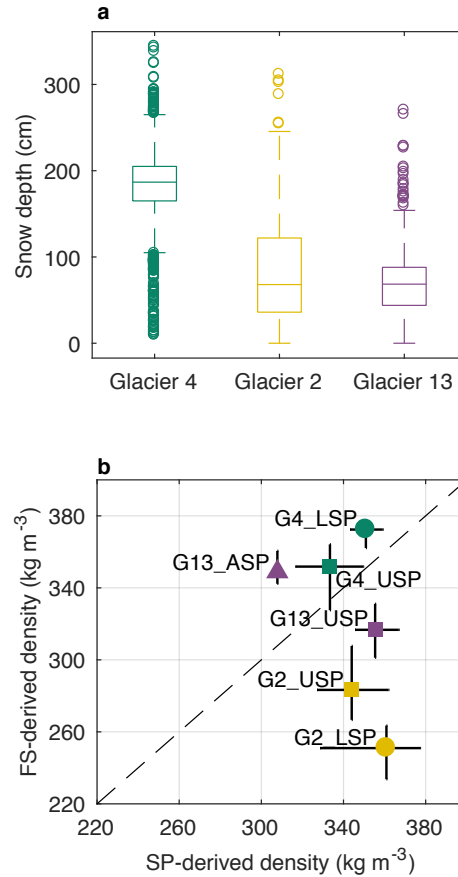


Fig. 2. Measured snow depth and density. (a) Boxplot of measured snow depth on Glaciers 4, 2 and 13 with the first quartiles (box), median (line within box), minimum and maximum values excluding outliers (bar) and outliers (circles), which are defined as being outside of the range of 1.5 times the quartiles (approximately $\pm 2.7\sigma$). (b) Comparison of depth-averaged densities estimated using Federal Sampler (FS) measurements and a wedge cutter in a snow pit (SP) for Glacier 4 (G4), Glacier 2 (G2) and Glacier 13 (G13). Labels indicate ~~snow-pit~~ SP locations in the accumulation area (ASP), upper ablation area (USP) and lower ablation area (LSP). Error bars for SP-derived densities are calculated by varying the thickness and density of layers that are too hard to sample, and error bars for FS-derived densities are the standard deviation of measurements taken at one location. One-to-one line is dashed.

RESULTS AND DISCUSSION

Field measurements

Snow depth

Mean snow depth varied systematically across the study region, with Glacier 4 having the highest mean snow depth and Glacier 13 having the lowest (Fig. 2a). At each measurement location, the median range of measured depths (3–4 points) as a percent of the mean local depth is 2%, 11% and 12%, for Glaciers 4, 2 and 13, respectively. While Glacier 4 has the lowest point-scale variability, as assessed above, it also has

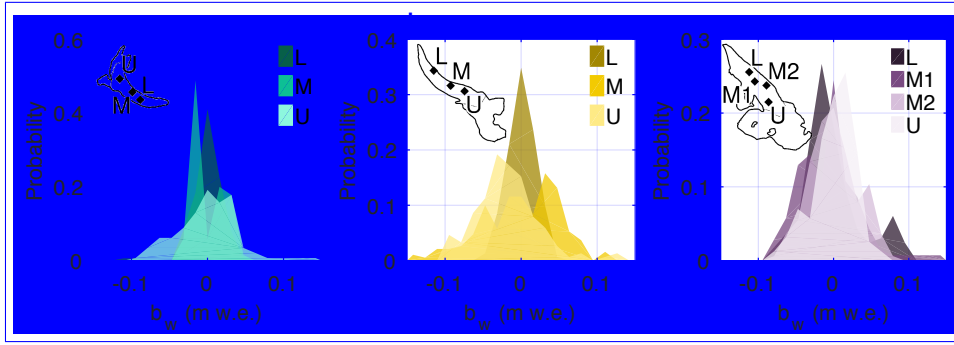


Fig. 3. Distributions of estimated winter-balance values for each zigzag survey in lower (L), middle (M) and upper (U) ablation areas (insets). Local mean has been subtracted. (a) Glacier 4. (b) Glacier 2. (c) Glacier 13.

the highest proportion of outliers, indicating a more variable snow depth across the glacier. The average standard deviation of all zigzag depth measurements is 0.07 m, 0.17 m and 0.14 m, for Glaciers 4, 2 and 13, respectively. When converted to values of $WB - b_w$ using the local FS-derived density measurement, the average standard deviation is 0.027 m w.e., 0.035 m w.e. and 0.040 m w.e. $WB - Winter-balance$ data for each zigzag are not normally distributed (Fig. 3).

363 Snow density

Contrary to expectation, co-located FS and SP measurements are found to be uncorrelated ($R^2 = 0.25$, Fig. 2b). The $Federal-Sampler-FS$ appears to oversample in deep snow and undersample in shallow snow. Oversampling by small-diameter (3.2–3.8 cm) sampling tubes has been observed in previous studies, with a percent error between 6.8% and 11.8% (e.g. Work and others, 1965; Fames and others, 1982; Conger and McClung, 2009). Studies that use $Federal-Samplers-FS$ often apply a 10% correction to all measurements for this reason (e.g. Molotch and others, 2005). Oversampling has been attributed to slots “shaving” snow into the tube as it is rotated (e.g. Dixon and Boon, 2012) and to snow falling into the slots, particularly for snow samples with densities $>400 \text{ kg m}^{-3}$ and snow depths $>1 \text{ m}$ (e.g. Beaumont and Work, 1963). Undersampling is likely to occur due to loss of snow from the bottom of the sampler (Turcan and Loijens, 1975). Loss by this mechanism may have occurred in our study, given the isothermal and melt-affected snow conditions observed over the lower reaches of Glaciers 2 and 13. Relatively poor $Federal-Sampler-FS$ spring-scale sensitivity also calls into question the reliability of measurements for snow depths $<20 \text{ cm}$.

Our FS-derived density values are positively correlated with snow depth ($R^2 = 0.59$). This relationship could be a result of physical processes, such as compaction in deep snow and preferential formation of depth hoar in shallow snow, but is more likely a result of measurement artefacts for a number of reasons. First, the

total range of densities measured by the ~~Federal Sampler~~ FS seems improbably large (227–431 kg m⁻³) ~~given~~
~~the conditions at the~~. At the time of sampling ~~the snow pack had little new snow, which confounds the~~
~~low density values, and was not yet saturated and had few ice lenses, which confounds the high density~~
~~values~~. Moreover, the range of FS-derived values is much larger than ~~than that~~ of SP-derived values when
co-located measurements are compared. Second, compaction effects of the magnitude required to explain the
density differences between SP and FS measurements would not be expected at the measured snow depths
(up to 340 cm). Third, no linear relationship exists between depth and SP-derived density ($R^2 = 0.05$). These
findings suggest that the ~~Federal Sampler~~ FS measurements have a bias for which we have not identified a
suitable correction. ~~Despite this bias, we use FS-derived densities to generate a range of possible b_w estimates~~
~~and to provide a generous estimate of uncertainty arising from density assignment.~~

Density assignment

Given the lack of correlation between co-located SP- and FS-derived densities (Fig. 2), we use the densities
derived from these two methods separately (Table 3). SP-derived regional (S1) and glacier-mean (S2) densities
are within one standard deviation of the corresponding FS-derived densities (F1 and F2) although SP-derived
density values are larger (see Supplementary Material, Table ~~S2~~S3). For both SP- and FS-derived densities,
the mean density for any given glacier (S2 or F2) is within one standard deviation of the mean across all
glaciers (S1 or F1). Correlations between elevation and SP- and FS-derived densities are generally high
($R^2 > 0.5$) but vary between glaciers (Supplementary material, Table ~~S2~~S3). For any given glacier, the
standard deviation of the 3–4 SP- or FS-derived densities is <13% of the mean of those values (S2 or F2)
(Supplementary material, Table ~~S2~~S3). We adopt S2 (glacier-wide mean of SP-derived densities) as the
reference method of density assignment. Though the method described by S2 does not account for known
basin-scale spatial variability in snow density (e.g. Wetlaufer and others, 2016), it is commonly used in winter
balance studies (e.g. Elder and others, 1991; McGrath and others, 2015; Cullen and others, 2017).

Gridcell-averaged winter balance

The distributions of gridcell-averaged ~~WB~~ b_w values for the individual glaciers are similar to those in Fig. 2a
but with fewer outliers ~~—(see Supplementary Material, Fig. S4)~~. The standard deviations of ~~WB~~ b_w values
determined from the zigzag surveys are almost twice as large as the mean standard deviation of point-scale
~~WB~~ b_w values within a gridcell measured along transects ~~—(see Supplementary Material, Fig. S5)~~. However,
a small number of gridcells sampled in transect surveys have standard deviations in ~~WB~~ b_w that exceed

Table 4. Glacier-wide winter balance ($\text{WB-}B_w$, m w.e.) estimated using linear regression and simple-ordinary kriging for the three study glaciers. Root mean squared error (RMSE, m w.e.) is computed as the average of all RMSE values between gridcell-averaged values of $\text{WB-}b_w$ (the data) that were randomly selected and excluded from interpolation (1/3 of all data) and those estimated by interpolation. RMSE as a percent of the glacier-wide-WB-}B_w is shown in brackets.

	Linear regression		Ordinary kriging	
	$\text{WB-}B_w$	RMSE	$\text{WB-}B_w$	RMSE
G4	0.58	0.15 (26%)	0.62	0.13 (21) <u>0.11 (18%)</u>
G2	0.58	0.10 (17%)	0.37 <u>0.35</u>	0.07 (19) <u>0.06 (18%)</u>
G13	0.38	0.08 (21%)	0.27	0.07 (26) <u>0.06 (21%)</u>

0.25 m w.e. (~ 10 times greater than those for zigzag surveys). ~~We nevertheless assume that the gridecell uncertainty is captured with dense sampling in zigzag gridecells.~~

~~Distribution of coefficients (β_i) determined by linear regression of gridecell-averaged WB on DEM-derived topographic parameters for the eight different density assignment methods (Table 3). Coefficients are calculated using standardized data, so values can be compared across parameters. Regression coefficients that are not significant are assigned a value of zero. Topographic parameters include elevation (z), distance from centreline (d_C), slope (m), curvature (κ) and wind redistribution (Sx). Aspect (α) and “northness” (N) are not shown because coefficient values are zero in every case. The box plot shows first quartiles (box), median (line within box), mean (circle within box), minimum and maximum values excluding outliers (bars) and outliers (gray dots), which are defined as being outside of the range of 1.5 times the quartiles (approximately $\pm 2.7\sigma$).~~

Distributed winter balance

~~Distributed winter balance~~

~~Relative uncertainty in distributed winter balance (WB) (Fig. 4) found using linear regression (top row) and simple kriging (bottom row). Values closer to one indicate higher relative uncertainty. Ice flow directions are indicated by arrows.~~

Linear regression

The highest values of estimated b_w are found in the upper portions of the accumulation areas of Glaciers 2 and 13 (Fig. 4). These areas also correspond to large values of elevation, slope, and wind redistribution. Extrapolation of the positive relation between b_w and elevation, as well as slope and Sx for Glacier 2, results

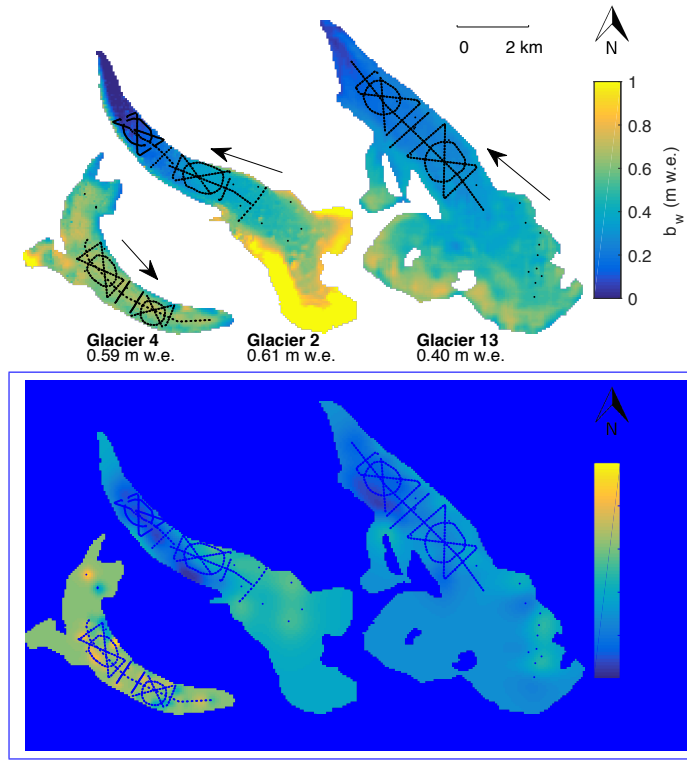


Fig. 4. Spatial distribution of winter balance ($\text{WB } b_w$) estimated using linear regression (top row) and simple-ordinary kriging (bottom row) with densities assigned as per S2 (Table 3). The linear regression (LR) method involves multiplying regression coefficients, found using cross validation and model averaging, by topographic parameters for each gridcell. Ordinary kriging (OK) uses the covariance of measured values to find a set of optimal weights for estimating values at unmeasured locations. Locations of snow-depth measurements made in May 2016 are shown as black dots. Ice-flow directions are indicated by arrows. Values of glacier-wide-WB- B_w are given below labels.

in high b_w estimates and large relative uncertainty in these estimates (Fig. 5). On Glacier 4, the distributed b_w and the relative uncertainty are almost uniform (Fig. 4) due to the small regression coefficients for all topographic parameters. The explained variance of the LR-estimated b_w differs considerably between glaciers (Fig. 6), with the best correlation between modelled- and observed- b_w occurring for Glacier 2. LR is an especially poor predictor of b_w on Glacier 4, where B_w can be estimated equally well using the mean of the data. RMSE is also highest for Glacier 4 (Table 4).

Ordinary kriging

For all three glaciers, large areas that correspond to locations far from measurements have b_w estimates equal to the kriging mean. Distributed b_w estimated with OK on Glacier 4 is mostly uniform except for local deviations close to measurement locations (Fig. 4) and relative uncertainty is highest close to measurement locations. Distributed b_w varies more smoothly on Glaciers 2 and 13 (Fig. 4). Glacier 2 has a distinct region

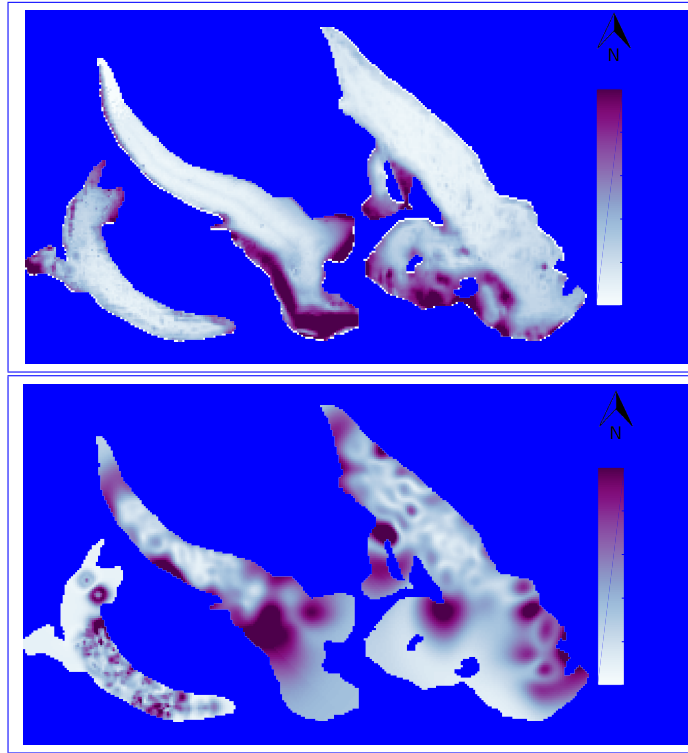


Fig. 5. Relative uncertainty in distributed winter balance (b_w) (Fig. 4) found using linear regression (top row) and ordinary kriging (bottom row). Values closer to one indicate higher relative uncertainty. Ice-flow directions are indicated by arrows.

of low estimated b_w (~ 0.1 m w.e.) in the lower part of the ablation area, which corresponds to a wind-scoured region of the glacier. Glacier 13 has the lowest estimated mean b_w and only small deviations from this mean at measurement locations (Fig. 4). Relative uncertainty vary considerably across the three study glaciers with the greatest uncertainty just outside of the region with observed b_w (Fig. 5). As expected, explained variance of OK-estimated b_w is high for both Glaciers 2 and 13 (Fig. 6) because OK is a data-fitting algorithm. However, explained variance (Fig. 6) for Glacier 4 is relatively low and RMSE is relatively high (Table 4), indicating a highly variable distribution of b_w .

Uncertainty analysis using a Monte Carlo approach

Linear Regression

Glacier-wide winter balance is affected by uncertainty introduced by the representativeness of gridcell-averaged values of b_w (σ_{GS}), choosing a method of density assignment (σ_ρ), and interpolating/extrapolating b_w values across the domain (σ_{INT}). Using a Monte Carlo analysis, we find that interpolation uncertainty contributes more to B_w uncertainty than grid-scale uncertainty or density

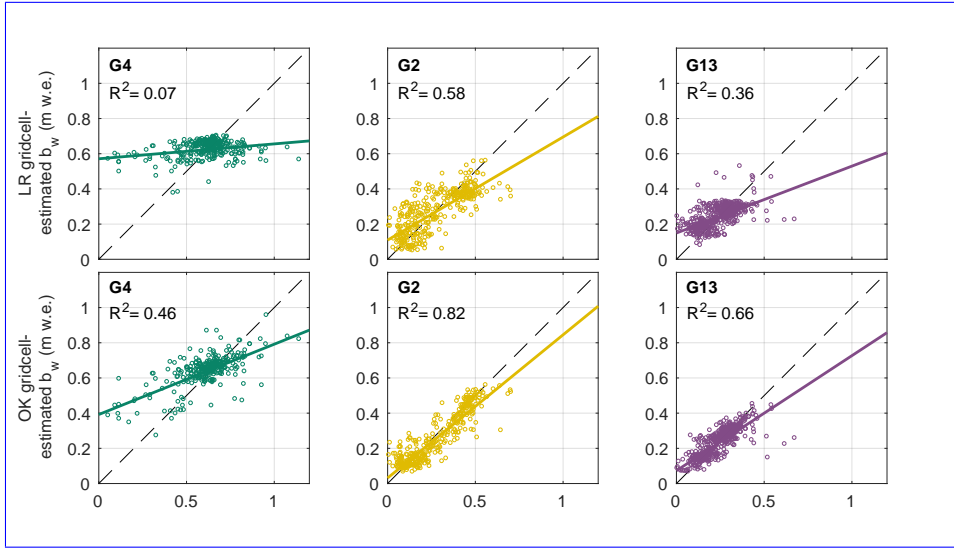


Fig. 6. Winter balance (b_w) estimated by linear regression (LR, top row) or ordinary kriging (OK, bottom row) versus the grid-cell averaged b_w data for Glacier 4 (left), Glacier 2 (middle) and Glacier 13 (right). Each circle represents a single gridcell. Explained variance (R^2) is provided. Best-fit (solid) and one-to-one (dashed) lines are shown.

assignment method. In other words, the distribution of B_w that arises from grid-scale uncertainty and the differences in distributions between methods of density assignment are smaller than the distribution that arises from interpolation uncertainty (Fig. 7 and Table 5). The B_w distributions obtained using LR and OK overlap for a given glacier, but the distribution modes differ (Fig. 7). OK-estimated values of b_w in the accumulation area are generally lower (Fig. 4), which lowers the B_w estimate. The uncertainty in OK-estimated values of B_w is large, and unrealistic B_w values of 0 m w.e. can be estimated (Fig. 7).

The values of B_w for our study glaciers (using LR and S2 density assignment method), with an uncertainty equal to one standard deviation of the distribution found with Monte Carlo analysis, are: 0.59 ± 0.03 m w.e. for Glacier 4, 0.61 ± 0.05 m w.e. for Glacier 2 and 0.40 ± 0.03 m w.e. for Glacier 13. The B_w uncertainty from

Table 5. Standard deviation ($\times 10^{-2}$ m w.e.) of glacier-wide winter balance (B_w) distributions arising from uncertainties in grid-scale b_w (σ_{GS}), density assignment (σ_ρ), interpolation (σ_{INT}) and all three sources combined (σ_{ALL}) for linear regression (left columns) and ordinary kriging (right columns)

	Linear regression				Ordinary kriging			
	σ_{GS}	σ_ρ	σ_{INT}	σ_{ALL}	σ_{GS}	σ_ρ	σ_{INT}	σ_{ALL}
Glacier 4	0.86	1.90	2.13	2.90	0.18	2.16	14.35	14.64
Glacier 2	1.80	3.37	3.09	4.90	0.80	2.06	12.65	13.14
Glacier 13	1.12	1.68	2.80	3.20	0.57	1.30	9.74	10.48

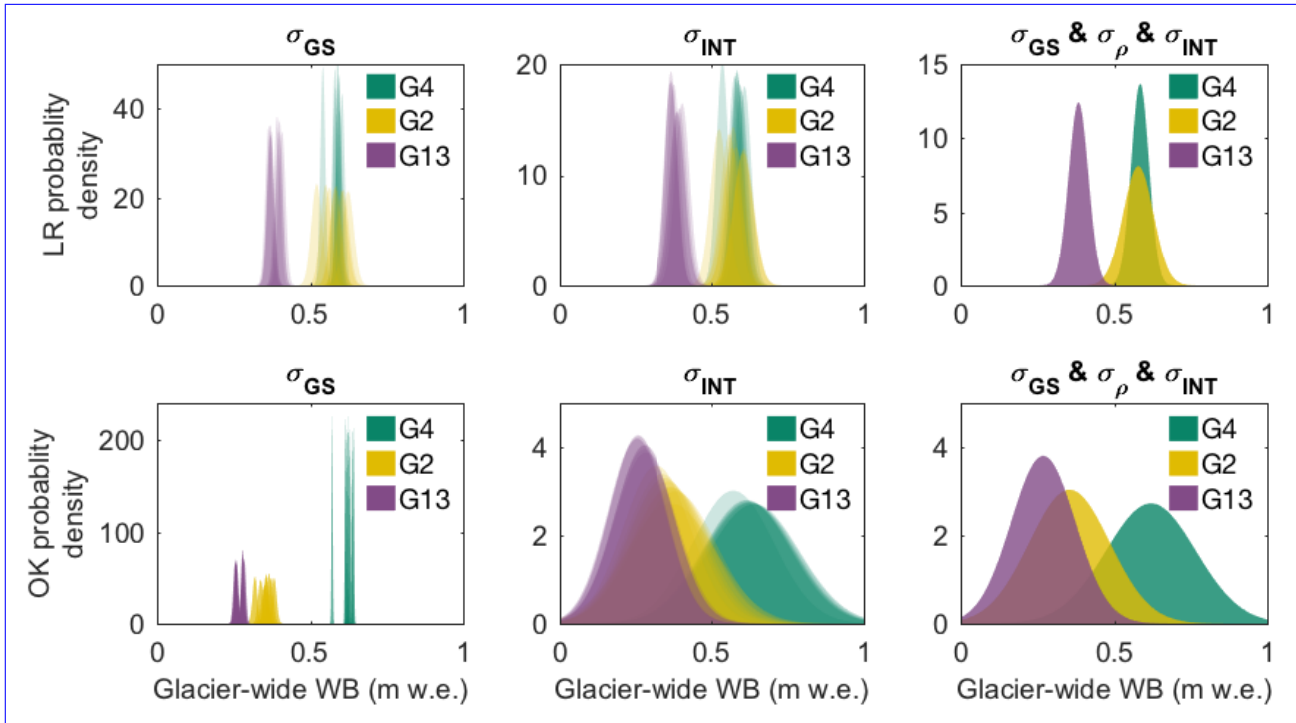


Fig. 7. ~~Winter~~ Distributions of glacier-wide winter balance (WB_{B_w}) estimated by linear regression for Glaciers 4 (LRG4), top row 2 (G2) or simple kriging and 13 (SK, bottom row G13) versus the grid-cell averaged WB data for Glacier 4 that arise from various sources of uncertainty. B_w distribution arising from grid-scale uncertainty (σ_{GS}) (left column); Glacier 2, B_w distribution arising from interpolation uncertainty (σ_{INT}) (middle column). B_w distribution arising from a combination of σ_{GS} , σ_{INT} and Glacier 13 density assignment uncertainty (σ_{ρ}) (right column). Each circle represents a single gridcell. Results are shown for interpolation by linear regression (LR, top row) and ordinary kriging (OK, bottom row). Best-fit Left two columns include eight distributions per glacier (solid colour) and one-to-one each corresponds to a density assignment method (dashed S1–S4 and F1–F4) lines are shown.

the three investigated sources of uncertainty ranges from 0.03 m w.e (5%) to 0.05 m w.e (8%) for LR estimates and from 0.10 m w.e (37%) to 0.15 m w.e (24%) for ordinary-kriging estimates (Table 4).

DISCUSSION

Distributed winter balance

Linear regression

Of the topographic parameters in the linear regression LR, elevation (z) is the most significant predictor of gridcell-averaged WB_{B_w} for Glaciers 2 and 13, while wind redistribution (Sx) is the most significant predictor for Glacier 4 (Fig. 8; Fig. 4). As expected, gridcell-averaged WB_{B_w} is positively correlated with elevation where the correlation is significant. It is possible that the elevation correlation was accentuated

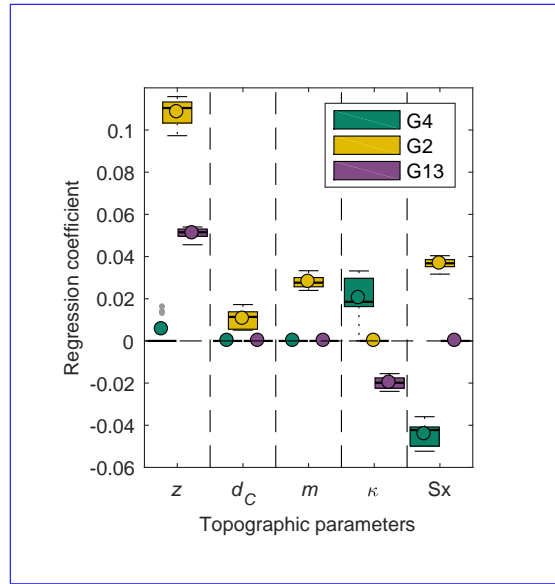


Fig. 8. Distribution of coefficients (β_i) determined by linear regression of gridcell-averaged b_w on DEM-derived topographic parameters for the eight different density assignment methods (Table 3). Coefficients are calculated using standardized data, so values can be compared across parameters. Regression coefficients that are not significant are assigned a value of zero. Topographic parameters include elevation (z), distance from centreline (d_C), slope (m), curvature (κ) and wind redistribution (Sx). Aspect (α) and “northness” (N) are not shown because coefficient values are zero in every case. The box plot shows first quartiles (box), median (line within box), mean (circle within box), minimum and maximum values excluding outliers (bars) and outliers (gray dots), which are defined as being outside of the range of 1.5 times the quartiles (approximately $\pm 2.7\sigma$).

470 due to melt onset for Glacier 13 in particular. ~~Many studies~~ Glacier 2 had little snow at the terminus likely
 471 due to steep slopes and wind-scouring but the snow did not appear to have been affected by melt. Our
 472 results are consistent with many studies that have found elevation to be the most significant predictor of
 473 winter-balance data (e.g. Machguth and others, 2006; McGrath and others, 2015). However, WB elevation
 474 gradients vary considerably between glaciers (e.g. Winther and others, 1998) and other factors, such as
 475 glacier shape and orientation relative to dominant wind direction, are strong predictors of the winter-balance
 476 distribution (Machguth and others, 2006; Grabiec and others, 2011). Some studies find no significant
 477 correlation between WB on glaciers and topographic parameters, with seasonal snow accumulation
 478 data (e.g. Machguth and others, 2006; Grünwald and others, 2014; McGrath and others, 2015). The
 479 b_w -elevation gradient is 13 mm 100 m⁻¹ on Glacier 2 and 7 mm 100 m⁻¹ on Glacier 13. These gradients are
 480 consistent with those reported for a few glaciers in Svalbard (Winther and others, 1998) but are considerably
 481 smaller than many reported b_w -elevation gradients, which range from about 60 to 240 mm 100 m⁻¹

(e.g. Hagen and Liestøl, 1990; Tveit and Killingtveit, 1994; Winther and others, 1998). Extrapolating linear relationships to unmeasured locations typically results in considerable estimation error, as seen by the large b_w values (Fig. 4) and large relative uncertainty (Fig. 5) in the high-elevation regions of Glaciers 2 and 13. The low correlation between b_w and elevation on Glacier 4 is consistent with Grabiec and others (2011) and López-Moreno and others (2011), who conclude that highly variable distributions of snow can be attributed to complex interactions between topography and the atmosphere that ~~could not cannot~~ be easily quantified (e.g. Grabiec and others, 2011; López-Moreno and others, 2011). ~~Extrapolating relationships to unmeasured locations, especially the accumulation area, is susceptible to large uncertainties (Fig. 5). This extrapolation has a considerable effect on values of glacier-wide WB, as the highest values of WB are typically found in the accumulation area (Fig. 4).~~ The snow on Glacier 4 also did not appear to have been affected by melt and it is hypothesized that significant wind-redistribution processes, that were not captured by the Sx parameter, covered ice-topography and produced a relatively uniform snow depth across the glacier.

Gridcell-averaged ~~WB~~ b_w is negatively correlated with Sx on Glacier 4, counter-intuitively indicating less snow in what would be interpreted as sheltered areas. Gridcell-averaged ~~WB~~ b_w is positively correlated with Sx on Glaciers 2 and 13. ~~Similarly, gridecell-averaged WB is positively correlated with curvature on Glacier 4 and negatively correlated on Glaciers 2 and 13. Wind redistribution and preferential deposition of snow are known to have a large influence on snow distribution at sub-basin scales (e.g. Dadić and others, 2010; Winstral and others, 2013; Gerber and others, 2017). Our~~ Our results corroborate those of McGrath and others (2015) in a study of six glaciers in Alaska (DEM resolutions of 5 m) where elevation and Sx were the only significant parameters for all glaciers; Sx regression coefficients were smaller than elevation regression coefficients, and in some cases, negative. While our results point to wind having an impact on snow distribution, ~~but~~ the wind redistribution parameter (Sx) may not adequately capture these effects at our study sites. For example, Glacier 4 ~~is located in a curved valley with steep side~~ has a curvilinear plan-view profile and is surrounded by steep valley walls, so specifying a single cardinal direction for wind may not be adequate. Further, the scale of deposition may be smaller than the resolution of the Sx parameter estimated from the DEM. ~~Our results corroborate those of McGrath and others (2015) in a study of six glaciers in Alaska (DEM resolutions of 5 m) where elevation and Sx were the only significant parameters for all glaciers; Sx regression coefficients were smaller than elevation regression coefficients, and in some cases, negative. In addition to wind redistribution,~~ Creation of a parametrization for sublimation

from blowing snow ~~has also~~, which has been shown to be an important mechanism of mass loss from ridges (e.g. Musselman and others, 2015). ~~Incorporating such losses, as well as redistribution and preferential deposition, may be important for improving representations of distributed winter balance,~~ may also increase the explanatory power of LR for our study sites.

We find that transfer of LR coefficients between glaciers results in large estimation errors. Regression coefficients from Glacier 4 produce the highest ~~root-mean-squared-error~~ RMSE (0.38 m w.e. on Glacier 2 and 0.40 m w.e. on Glacier 13, see Table 4 for comparison) and ~~glacier-wide WB~~ B_w values are the same for all glaciers (0.64 m w.e.) due to the dominance of the regression intercept. Even if the ~~regression~~ LR is performed with ~~WB~~ b_w values from all glaciers combined, the resulting coefficients produce large ~~root-mean-squared errors~~ RMSE when applied to individual glaciers (0.31 m w.e., 0.15 m w.e. and 0.14 m w.e. for Glaciers 4, 2 and 13, respectively). Our results are consistent with those of Grünwald and others (2013), who found that local statistical models cannot be transferred across basins and that regional-scale models are not able to explain the majority of observed variance in winter balance.

~~Simple~~ Ordinary kriging

~~Fitted kriging parameters, including the nugget and spatial correlation length, can provide insight into important scales of winter balance variability. The model fitted to the gridecell-averaged values of WB for Glacier 4 has a short correlation length (90 m) and large nugget (see Supplementary Material Table S3), suggesting variability in winter balance at smaller scales. Conversely, Glaciers 2 and 13 have longer correlation lengths (~ 450 m) and smaller nuggets, suggesting variability at larger scales. Additionally, simple kriging is better able to estimate values of WB for Glaciers 2 and 13 than for Glacier 4 (Fig. 6). Due to a paucity of data, simple kriging produces almost uniform gridcell-estimated values of winter balance b_w in the accumulation area of each glacier, inconsistent with observations described in the literature (e.g. Machguth and others, 2006; Grabiec and others, 2011). Extrapolation using simple kriging Glacier 4 has the highest estimated mean with large deviations from the mean at measurement locations. The longer correlation lengths of the data for Glaciers 2 and 13 result in a more smoothly varying distributed b_w . As expected, extrapolation using OK leads to large uncertainty (Fig. 5), further emphasizing the need for spatially distributed point-scale measurements.~~

LR and ~~SK~~ OK comparison

~~Glacier-wide WB estimates found using both LR and SK are~~ LR and OK produce similar estimates of distributed b_w (Fig. 5) and B_w (~ 0.58 0.60 m w.e., Table 4) for Glacier 4 but both are relatively poor

542 predictors of $\text{WB-}b_w$ in measured gridcells (Table 4 Fig. 6). For Glaciers 2 and 13, SK-OK estimates are
 543 more than $0.1 \sim 0.22$ m w.e. (~~up to 40%~~ 39%) and ~ 0.11 m w.e. (30%) lower than LR estimates, respectively
 544 (Table 4). RMSE as a percentage of the B_w is lower for OK than LR only for Glacier 4 but the absolute
 545 RMSE of OK is ~ 0.03 m w.e. lower for all glaciers, likely because OK is a data-fitting interpolation method
 546 (Table 4). RMSE as a percentage of the glacier-wide WB are comparable between LR and SK-OK (Table
 547 4) with an average RMSE of 22%. This comparability is interesting, given that all of the data were used to
 548 generate the SK-OK model, while only 2/3 were used in the LR. Tests in which only 2/3 of the data were
 549 used in the OK model yielded similar results to those in which all data were used. Gridcell-estimated values
 550 of $\text{WB-}b_w$ found using LR and SK-OK differ markedly in the upper accumulation areas of Glaciers 2 and
 551 13 (Fig. 4), where observations are sparse and topographic parameters, such as elevation, vary considerably.
 552 The influence of elevation results in substantially higher LR-estimated values of $\text{WB-}b_w$ at high elevation,
 553 whereas $\text{SK-estimated values approximate the nearest data}$ $\text{OK-estimated values are more uniform}$. Estimates
 554 of ablation-area-wide $\text{WB-}B_w$ differ by $< 76\%$ between LR and SK-OK on each glacier, further emphasizing
 555 the combined ~~role-influence~~ of interpolation method and measurement scarcity in the accumulation area on
 556 glacier-wide $\text{WB-}B_w$ estimates.

557 ~~Distributions of glacier-wide winter balance (WB) for Glaciers 4 (G4), 2 (G2) and 13 (G13) that arise from~~
 558 ~~various sources of uncertainty. WB distribution arising from grid-scale uncertainty (σ_{GS}) (left column). WB~~
 559 ~~distribution arising from interpolation uncertainty (σ_{INT}) (middle column). WB distribution arising from~~
 560 ~~a combination of σ_{GS} , σ_{INT} and density assignment uncertainty (σ_ρ) (right column). Results are shown for~~
 561 ~~interpolation by linear regression (LR, top row) and simple kriging (SK, bottom row). Left two columns~~
 562 ~~include eight distributions per glacier (colour) and each corresponds to a density assignment method (S1–S4~~
 563 ~~and F1–F4).~~

564 Uncertainty analysis using a Monte Carlo approach

565 ~~Uncertainty analysis~~

566 ~~Glacier-wide winter balance is affected by uncertainty introduced by the representativeness of~~
 567 ~~gridecell-averaged values of WB (σ_{GS}), choosing a method of density assignment (σ_ρ), and interpolating~~
 568 ~~WB values across the domain (σ_{INT}). Using a Monte Carlo analysis, we find that interpolation uncertainty~~
 569 ~~contributes more to WB uncertainty than grid-scale uncertainty or density assignment method. In other~~
 570 ~~words, the distribution of glacier-wide WB that arises from grid-scale uncertainty and the differences in~~
 571 ~~distributions between methods of density assignment are smaller than the distribution that arises from~~

interpolation uncertainty (Fig. 7 and Table 5). The WB distributions obtained using LR and SK overlap for a given glacier, but the distribution modes differ (Fig. 7). For reasons outlined above, SK-estimated values of WB in the accumulation area are generally lower, which lowers the glacier-wide WB estimate. The uncertainty in SK-estimated values of WB is large, and unrealistic glacier-wide values of WB of 0 m w.e. can be estimated (Fig. 7). Our Interpolation/extrapolation of b_w data is the largest contributor of B_w uncertainty in our study. These results caution strongly against including ~~extrapolated values of WB~~ values of B_w in comparisons with remote sensing- or model-derived estimates of ~~WB~~ B_w . If possible, such comparisons should be restricted to point-scale data.

Standard deviation ($\times 10^{-2}$ m w.e.) of glacier-wide winter balance distributions arising from uncertainties in grid-scale WB (σ_{GS}), density assignment (σ_{ρ}), interpolation (σ_{INT}) and all three sources combined (σ_{ALL}) for linear regression (left columns) and simple kriging (right columns) $\sigma_{GS} \sigma_{\rho} \sigma_{INT} \sigma_{ALL} \sigma_{GS} \sigma_{\rho} \sigma_{INT} \sigma_{ALL}$

	σ_{GS}	σ_{ρ}	σ_{INT}	σ_{ALL}	σ_{GS}	σ_{ρ}	σ_{INT}	σ_{ALL}
Glacier 4	0.86	1.90	2.13	2.90	0.85	2.15	14.05	14.72
Glacier 2	1.80	3.37	3.09	4.90	2.53	2.03	13.78	13.44
Glacier 13	1.12	1.68	2.80	3.20	1.15	1.27	9.65	10.43

Grid-scale uncertainty (σ_{GS}) is the smallest assessed contributor to overall ~~WB~~ B_w uncertainty. This result is consistent with the generally smoothly-varying snow depths encountered in zigzag surveys, and previously reported ice-roughness lengths on the order of centimetres (e.g. Hock, 2005) compared to snow depths on the order of decimetres to metres. Given our assumption that zigzags are an adequate representation of grid-scale variability, the low ~~WB~~ B_w uncertainty arising from σ_{GS} implies that subgrid-scale sampling need not be a high priority for reducing overall uncertainty. Our assumption that the 3–4 zigzag surveys can be used to estimate glacier-wide σ_{GS} may be flawed, particularly in areas with debris cover, crevasses and steep slopes.

Our analysis did not include uncertainty arising from ~~a number of sources, which we assume either to be encompassed by the sources investigated or to be negligible contributors. These sources of uncertainty include~~ density measurement errors associated with the **Federal Sampler** FS, wedge cutters and spring scales, from vertical and horizontal errors in the DEM ~~and or from~~ error associated with estimating measurement locations –

~~The values of glacier-wide WB for our study glaciers (using LR and S2 density assignment method), with an uncertainty equal to one standard deviation of the distribution found with Monte Carlo analysis, are:~~ 0.59 ± 0.03 m w. e. for Glacier 4, 0.61 ± 0.05 m w.e. for Glacier 2 and 0.40 ± 0.03 m w.e. for Glacier 13. The glacier-wide WB uncertainty from combined based on the GPS position of the lead observer. We assume that these sources of uncertainty ~~ranges from 0.03 m w. e (5%) to 0.05 m w.e (8%) for linear regression estimates~~

602 ~~and from 0.10 m w.e (37%) to 0.15 m w.e (24%) for simple kriging estimates (Table 4).~~ are either encompassed
 603 by the sources investigated or are negligible.

604 ~~Context and caveats~~ Regional winter-balance gradient

605 ~~Regional winter-balance gradient~~

606 Although we find considerable inter- and intra-basin variability in winter balance, our results are consistent
 607 with a regional-scale winter-balance gradient for the continental side of the St. Elias Mountains (Fig. 9).
 608 Winter-balance data are compiled from Taylor-Barge (1969), the three glaciers presented in this paper and
 609 two ~~snow pits~~ SP we analyzed near the head of the Kaskawulsh Glacier between 20–21 May 2016. The
 610 data show a linear decrease of $0.024 \text{ m w.e. km}^{-1}$ ($R^2 = 0.85$) in winter balance with distance from the
 611 regional topographic divide between the Kaskawulsh and Hubbard Glaciers, as identified by Taylor-Barge
 612 (1969). While the three study glaciers fit the regional trend, the same relationship would not apply if just
 613 the Donjek Range were considered. We hypothesize that interaction between meso-scale weather patterns
 614 and large-scale mountain topography is a major driver of regional-scale winter balance. Further insight into
 615 regional-scale patterns of winter balance in the St. Elias Mountains could be gained by investigating moisture
 616 source trajectories and the contribution of orographic precipitation.

617 ~~Limitations and future work~~

618 Limitations and future work

619 The potential limitations of our work include the restriction of our data to a single year, minimal sampling
 620 in the accumulation area, the problem of uncorrelated SP- and FS-derived densities, a sampling design that
 621 could not be optimized ~~a-priori~~ a priori, the assumption of spatially uniform subgrid variability and lack of
 622 more finely resolved DEMs.

623 Inter-annual variability in winter balance is not considered in our study. A number of studies have found
 624 temporal stability in spatial patterns of snow distribution and that statistical models based on topographic
 625 parameters could be applied reliably between years (e.g. Grünewald and others, 2013). For example, Walmsley
 626 (2015) analyzed more than 40 years of winter balance recorded on two Norwegian glaciers and found that
 627 snow distribution is spatially heterogeneous yet exhibits robust temporal stability. Contrary to this, Crochet
 628 and others (2007) found that snow distribution in Iceland differed considerably between years and depended
 629 primarily on the dominant wind direction over the course of a winter. Therefore, multiple years of snow depth

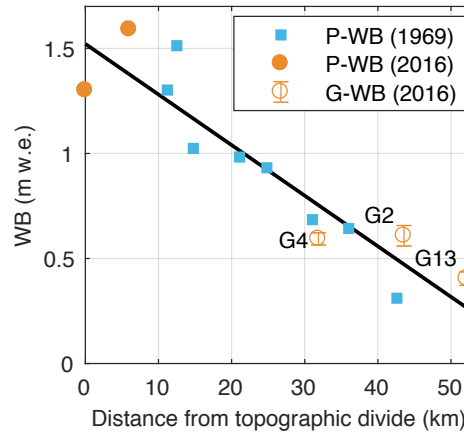


Fig. 9. Relationship between winter balance (~~WB~~) and linear distance from the regional topographic divide between the Kaskawulsh and Hubbard Glaciers in the St. Elias Mountains. Point-scale values of ~~WB~~-winter balance from snow-pit data reported by Taylor-Barge (1969) (blue boxes, P-WB). LR-estimated glacier-wide ~~WB~~-winter balance (B_w) calculated using density assignment S2 for Glaciers 4 (G4), 2 (G2) and 13 (G13) with errors bars calculated as the standard deviation of Monte Carlo-derived ~~WB~~- B_w distributions (this study) (open orange circles, G-WB). Point-scale ~~WB~~-winter balance estimated from snow-pit data at two locations in the accumulation area of the Kaskawulsh Glacier, collected in May 2016 (unpublished data, SFU Glaciology Group) (filled orange dots, P-WB). Black line indicates best fit ($R^2 = 0.85$).

and density measurements, that are not necessarily consecutive, are needed to better understand inter-annual variability ~~in winter balance distribution of~~ winter balance within the Donjek Range.

There is a conspicuous lack of data in the accumulation areas of our study glaciers. With increased sampling in the accumulation area, interpolation uncertainties would be reduced where they are currently greatest and the ~~linear regression~~-LR would be better constrained. Although certain regions of the glaciers remain inaccessible for direct measurements, other methods of obtaining winter-balance measurements, including ground-penetrating radar and DEM differencing with photogrammetry or lidar, could be used in conjunction with manual probing to increase the spatial coverage of measurements.

The lack of correlation between SP- and FS-derived densities needs to be reconciled. Contrary to our results, most studies that compare SP- and FS-derived densities report minimal discrepancy (e.g. Dixon and Boon, 2012, and sources within). Additional co-located density measurements are needed to better compare the two methods of obtaining density values. Comparison with other ~~Federal Samplers~~-FS would also be informative. Even with this limitation, density assignment was, fortunately, not the largest source of uncertainty in estimating glacier-wide winter balance.

Our sampling design was chosen to achieve broad spatial coverage of the ablation area, but is likely too finely resolved along transects for many mass-balance surveys to replicate. An optimal sampling design would minimize uncertainty in winter balance while reducing the number of required measurements. Analysis of the estimated winter balance obtained using subsets of the data is underway to make recommendations on optimal transect configuration and along-track spacing of measurements. López-Moreno and others (2010) found that 200–400 observations are needed within a non-glacierized alpine basin (6 km^2) to obtain accurate and robust snow distribution models. Similar guidelines would be useful for glacierized environments.

In this study, we assume that the subgrid variability of winter balance is uniform across a given glacier. Contrary to this assumption, McGrath and others (2015) found greater variability of winter-balance values close to the terminus. Testing our assumption could be a simple matter of prioritizing the labour-intensive zigzags surveys. To ensure consistent quantification of subgrid variability, zigzag survey measurements could also be tested against other measurements methods, such as lidar.

DEM gridcell size is known to influence values of computed topographic parameters (Zhang and Montgomery, 1994; Garbrecht and Martz, 1994; Guo-an and others, 2001; López-Moreno and others, 2010). The relationship between topographic parameters and winter balance is, therefore, not independent of DEM gridcell size. For example, Kienzle (2004) and López-Moreno and others (2010) found that a decrease in spatial resolution of the DEM results in a decrease in the importance of curvature and an increase in the importance of elevation in ~~regressions~~ LR of snow distribution on topographic parameters in non-glacierized basins. The importance of curvature in our study is affected by the DEM smoothing that we applied to obtain a spatially continuous curvature field (see Supplementary Material, Fig. S1). A comparison of regression coefficients from high-resolution DEMs obtained from various sources and sampled with various gridcell sizes could be used to characterize the dependence of topographic parameters on DEMs, and therefore assess the robustness of inferred relationships between winter balance and topographic parameters.

CONCLUSION

We estimate winter balance for three glaciers (termed Glacier 2, Glacier 4 and Glacier 13) in the St. Elias Mountains, Yukon, Canada from multiscale snow depth and density measurements. Linear regression and ~~simple-ordinary~~ kriging are used to obtain estimates of distributed winter balance (b_w). We use Monte Carlo analysis to evaluate the contributions of interpolation, ~~the~~ assignment of snow density and grid-scale variability of winter balance to uncertainty in estimates of glacier-wide winter balance (B_w).

Values of ~~glacier-wide winter balance~~ B_w estimated using linear regression and ~~simple ordinary~~ kriging differ by up to 0.24 m w.e. ($\sim 50\%$). We find that interpolation uncertainty is the largest assessed source of uncertainty in ~~glacier-wide winter balance~~ B_w (7% for linear-regression estimates and ~~32% for simple kriging~~ 34% for ordinary kriging estimates). Uncertainty resulting from the method of density assignment is comparatively low, despite the wide range of methods explored. Given our representation of grid-scale variability, the resulting ~~winter balance~~ B_w uncertainty is small indicating that extensive subgrid-scale sampling is not required to reduce overall uncertainty.

Our results suggest that processes governing distributed ~~winter balance~~ b_w differ between glaciers, highlighting the importance of regional-scale winter-balance studies. The estimated distribution of ~~winter balance~~ b_w on Glacier 4 is characterized by high variability, as indicated by the poor correlation between estimated and observed values and large number of data outliers. Glaciers 2 and 13 appear to have lower spatial variability, with elevation being the dominant predictor of gridcell-averaged ~~winter balance~~ b_w . A wind-redistribution parameter is found to be a weak but significant predictor of ~~winter balance~~ b_w , though conflicting relationships between glaciers make it difficult to interpret. The major limitations of our work include the restriction of our data to a single year and minimal sampling in the accumulation area. Although challenges persist when estimating winter balance, our data are consistent with a regional-scale winter-balance gradient for the continental side of the St. Elias Mountains.

AUTHOR CONTRIBUTION STATEMENT

AP planned and executed the data collection, performed all calculations and drafted the manuscript. GF conceived of the study, contributed to field planning and data collection, oversaw all stages of the work and edited the manuscript. VR provided guidance with statistical methods and edited the manuscript.

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