JOURNAL OF GLACIOLOGY



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Journal:	Journal of Glaciology
Manuscript ID	JOG-17-0123
Manuscript Type:	Article
Date Submitted by the Author:	01-Sep-2017
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Keywords:	Snow, Accumulation, Glacier mass balance

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Estimating winter balance and its uncertainty from direct

² measurements of snow depth and density on alpine glaciers

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ABSTRACT. Accurately estimating winter surface mass balance on glaciers is central to assessing glacier health and predicting glacier runoff. However, measuring and modelling snow distribution is inherently difficult in mountainous terrain. Here we explore rigorous statistical methods of estimating winter balance and its uncertainty from multiscale measurements of snow depth and density. In May 2016 we collected over 9000 manual measurements of snow depth across three glaciers in the St. Elias Mountains, Yukon, Canada. Linear regression, combined with cross correlation and Bayesian model averaging, as well as simple kriging are used to interpolate point-scale values to glacier-wide estimates of winter balance. Elevation and a wind-redistribution parameter exhibit the highest correlations with winter balance, but the relationship varies considerably between glaciers. A Monte Carlo analysis reveals that the interpolation itself introduces more uncertainty than the assignment of snow density or the representation of grid-scale variability. For our study glaciers, the winter balance uncertainty from all assessed sources ranges from $0.03\,\mathrm{m\,w.e.}$ (8%) to $0.15\,\mathrm{m\,w.e.}$ (54%). Despite the challenges associated with estimating winter balance, our results are consistent with a regional-scale winter-balance gradient.

26 INTRODUCTION

Winter surface mass balance, or "winter balance", is the net accumulation and ablation of snow over the 27 winter season (Cogley and others, 2011), which constitutes glacier mass input. Winter balance is half of the 28 seasonally resolved mass balance, initializes summer ablation conditions and must be estimated to simulate energy and mass exchange between the land and atmosphere (e.g. Hock, 2005; Réveillet and others, 2016). 30 Effectively representing the spatial distribution of snow is also central to monitoring surface runoff and its 31 downstream effects (e.g. Clark and others, 2011). 32 Winter balance (WB) is notoriously difficult to estimate. Snow distribution in alpine regions is highly 33 variable with short correlation length scales (e.g. Anderton and others, 2004; Egli and others, 2011; Grünewald 34 and others, 2010; Helbig and van Herwijnen, 2017; López-Moreno and others, 2011, 2013; Machguth and others, 2006; Marshall and others, 2006) and is influenced by dynamic interactions between the atmosphere 36 and complex topography, operating on multiple spatial and temporal scales (e.g. Barry, 1992; Liston and 37 Elder, 2006; Clark and others, 2011). Simultaneously extensive, high resolution and accurate snow distribution 38 measurements on glaciers are therefore difficult to obtain (e.g. Cogley and others, 2011; McGrath and others, 39 2015). Physically based models are computationally intensive and require detailed meteorological data to 40 drive them (Dadić and others, 2010). As a result, there is significant uncertainty in estimates of winter balance, thus limiting the ability of models to represent current and projected glacier conditions. Studies that have focused on obtaining detailed estimates of WB have used a wide range of observational 43 techniques, including direct measurement of snow depth and density (e.g. Cullen and others, 2017), lidar 44 or photogrammerty (e.g. Sold and others, 2013) and ground-penetrating radar (e.g. Machguth and others, 45 2006; Gusmeroli and others, 2014; McGrath and others, 2015). Spatial coverage of direct measurements 46 is generally limited and comprises an elevation transect along the glacier centreline (e.g. Kaser and others, 2002). Measurements are often interpolated using linear regression on only a few topographic parameters (e.g. 48 MacDougall and Flowers, 2011), with elevation being the most common. Other established techniques include 49 hand contouring (e.g. Tangborn and others, 1975), kriging (e.g. Hock and Jensen, 1999) and attributing 50 measured winter balance values to elevation bands (e.g. Thibert and others, 2008). Physical snow models 51 have been used to estimate spatial patterns of winter balance (e.g. Mott and others, 2008; Schuler and others, 52 2008; Dadić and others, 2010) but availability of the required meteorological data generally prohibits their 53 widespread application. Error analysis is rarely undertaken and few studies have thoroughly investigated uncertainty in spatially distributed estimates of winter balance (c.f. Schuler and others, 2008).

More sophisticated snow-survey designs and statistical models of snow distribution are widely used in 56 the field of snow science. Surveys described in the snow science literature are generally spatially extensive 57 and designed to measure snow depth and density throughout a basin, ensuring that all terrain types are 58 sampled. A wide array of measurement interpolation methods are used, including linear (e.g. López-Moreno and others, 2010) and non-linear regressions (e.g. Molotch and others, 2005) that include numerous terrain parameters, as well as geospatial interpolation (e.g. Erxleben and others, 2002) including various forms 61 of kriging. Different interpolation methods are also combined; for example, regression kriging adds kriged residuals to a field obtained with linear regression (e.g. Balk and Elder, 2000). Physical snow models such as 63 Alpine3D (Lehning and others, 2006) and SnowDrift3D (Schneiderbauer and Prokop, 2011) are widely used, and errors in estimating snow distribution have been examined from theoretical (e.g. Trujillo and Lehning, 2015) and applied perspectives (e.g. Turcan and Loijens, 1975; Woo and Marsh, 1978; Deems and Painter, 2006). 67 The goals of this study are to (1) critically examine methods of converting direct snow depth and density 68 measurements to distributed estimates of winter balance and (2) identify sources of uncertainty, evaluate their magnitude and assess their combined contribution to uncertainty in glacier-wide winter balance. We

focus on commonly applied, low-complexity methods of measuring and estimating winter balance in the

73 STUDY SITE

interest of making our results broadly applicable.

The St. Elias Mountains (Fig. 1a) rise sharply from the Pacific Ocean, creating a significant climatic gradient between coastal maritime conditions, generated by Aleutian–Gulf of Alaska low-pressure systems, and interior continental conditions, driven by the Yukon–Mackenzie high-pressure system (Taylor-Barge, 1969). The boundary between the two climatic zones is generally aligned with the divide between the Hubbard and Kaskawulsh Glaciers, approximately 130 km from the coast. Research on snow distribution and glacier mass balance in this area is limited. A series of research programs, including Project "Snow Cornice" and the Icefield Ranges Research Project, were operational in the 1950s and 60s (Wood, 1948; Danby and others, 2003) and in the last 30 years, there have been a few long-term studies on selected alpine glaciers (e.g. Clarke, 2014) as well as several regional studies of glacier mass balance and dynamics (e.g. Arendt and others, 2008; Burgess and others, 2013; Waechter and others, 2015).

We carried out winter balance surveys on three unnamed glaciers in the Donjek Range of the St. Elias

Mountains. The Donjek Range is located approximately 40 km to the east of the regional mountain divide

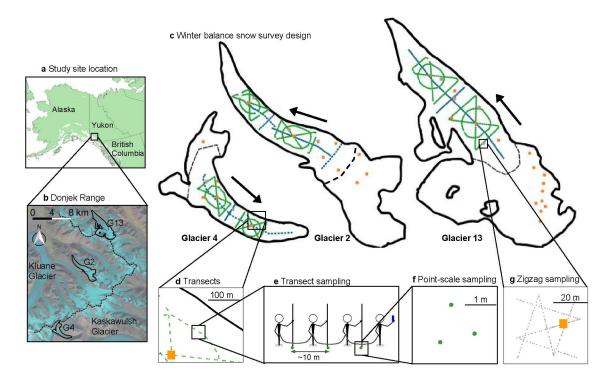


Fig. 1. Study area location and sampling design for Glaciers 4, 2 and 13. (a) Study region in the Donjek Range of the St. Elias Mountains of Yukon, Canada. (b) Study glaciers located along a southwest-northeast transect through the Donjek Range. The local topographic divide is shown as a dashed line. Imagery from Landsat8 (5 September 2013, data available from the U.S. Geological Survey). (c) Details of the snow-survey sampling design, with centreline and transverse transects (blue dots), hourglass and circle designs (green dots) and locations of snow density measurements (orange squares). Arrows indicate ice-flow directions. Approximate location of ELA on each glacier is shown as a black dashed line. (d) Close up of linear and curvilinear transects. (e) Configuration of navigator and observers. (f) Point-scale snow-depth sampling. (g) Linear-random snow-depth measurements in 'zigzag' design (grey dots) with one density measurement (orange square) per zigzag.

and has an area of about $30 \times 30 \,\mathrm{km^2}$. Glacier 4, Glacier 2 and Glacier 13 (labelling adopted from Crompton and Flowers (2016)) are located along a southwest-northeast transect through the range (Fig. 1b, Table 1). These small alpine glaciers are generally oriented southeast-northwest, with Glacier 4 having a predominantly southeast aspect and Glaciers 2 and 13 have generally northwest aspects. The glaciers are situated in valleys with steep walls and have simple geometries. Based on a detailed study of Glacier 2 (Wilson and others, 2013) and related theoretical modelling (Wilson and Flowers, 2013) we suspect all of the study glaciers to be polythermal.

Table 1. Physical characteristics of the study glaciers and May 2016 winter-balance survey details, including number of snow-depth measurement locations along transects $(n_{\rm T})$, total length of transects $(d_{\rm T})$, number of combined snow pit and Federal Sampler density measurement locations (n_{ρ}) and number of zigzag surveys (n_{zz}) .

	Location	Elevation (m a.s.l)		.s.l)	Slope ($^{\circ}$)	Area	Survey	Survey Details			
	UTM Zone 7	Mean	Range	ELA	Mean	(km^2)	Dates	n_{T}	$d_{\mathrm{T}}~(\mathrm{km})$	$n_{ ho}$	n_{zz}
Glacier 4	595470 E	2344	1958–2809	~2500	12.8	3.8	4–7 May 2016	649	13.1	10	3
	6740730 N										
Glacier 2	$601160~\mathrm{E}$	2495	1899-3103	\sim 2500	13.0	7.0	8–11 May 2016	762	13.6	11	3
	6753785 N										
Glacier 13	$604602~\mathrm{E}$	2428	1923–3067	~2380	13.4	12.6	12–15 May 2016	941	18.1	20	4
	6763400 N	2420									

93 METHODS

Estimating glacier-wide winter balance involves transforming measurements of snow depth and density into values of winter balance distributed across a defined grid. We do this in four steps. (1) Obtain direct measurements of snow depth and density in the field. (2) Assign density values to all depth-measurement locations to calculate point-scale values of WB at each location. (3) Average all point-scale values within each gridcell of a digital elevation model (DEM) to obtain the gricell-averaged WB. (4) Interpolate and extrapolate these gridcell-averaged WB values to obtain estimates of WB (in mw.e.) in each gridcell across the domain. For brevity, we refer to these four steps as (1) field measurements, (2) density assignment, (3) gridcell-averaged WB and (4) distributed WB. Detailed methodology for each step is outlined below.

Field measurements

103 Sampling design

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The snow surveys were designed to capture variability in snow depth at regional, basin, gridcell and point 104 scales (Clark and others, 2011). To capture variability at the regional scale we chose three glaciers along 105 a transect aligned with the dominant precipitation gradient (Fig. 1) (Taylor-Barge, 1969). To account for 106 basin-scale variability, snow depth was measured along linear and curvilinear transects on each glacier (Fig. 107 1c) with a sample spacing of 10–60 m (Fig. 1d). Sample spacing was constrained by protocols for safe glacier 108 travel, while survey scope was constrained by the need to complete all surveys within the period of peak 109 accumulation. We selected centreline and transverse transects as the most commonly used survey designs 110 in winter balance studies (e.g. Kaser and others, 2002; Machguth and others, 2006) as well as an hourglass 111

pattern with an inscribed circle, which allows for sampling in multiple directions and easy travel (personal communication from C. Parr, 2016). To capture variability at the grid scale, we densely sampled up to four gridcells on each glacier using a linear-random sampling design we term a 'zigzag'. To capture point-scale variability, each observer made 3–4 depth measurements within ~1 m (Fig. 1e) at each transect measurement location. In total, we collected more than 9000 snow-depth measurements throughout the study area (Table 1).

118 Snow depth: transects

Winter balance can be estimated as the product of snow depth and depth-averaged density. Snow depth 119 is generally accepted to be more variable than density (Elder and others, 1991; Clark and others, 2011; 120 López-Moreno and others, 2013) so we chose a sampling design that resulted in a high ratio ($\sim 55:1$) of snow 121 depth to density measurements. Our sampling campaign involved four people and occurred between 5-15 122 May 2016, which falls within the period of historical peak snow accumulation in southwestern Yukon (Yukon 123 Snow Survey Bulletin and Water Supply Forecast, May 1, 2016). While roped-up for glacier travel with fixed 124 distances between observers, the lead observer used a single-frequency GPS unit (Garmin GPSMAP 64s) to 125 navigate between predefined transect measurement locations (Fig. 1e). The remaining three observers used 126 3.2 m graduated aluminum avalanche probes to make snow-depth measurements. The locations of each set 127 of depth measurements, made by the second, third and fourth observers, are estimated using the recorded 128 129 location of the first observer, the approximate distance between observers and the direction of travel. Snow-depth sampling was concentrated in the ablation area to ensure that only snow from the current 130 accumulation season was measured. The boundary between snow and firn in the accumulation area can be 131 difficult to detect and often misinterpreted, especially when using an avalanche probe (Grünewald and others, 132 2010; Sold and others, 2013). We intended to use a firn corer to measure winter balance in the accumulation 133 area, but cold snow combined with positive air temperatures led to cores being unrecoverable. Successful 134 snow depth and density measurements within the accumulation area were made either in snow pits or using 135

137 Snow depth: zigzags

136

To capture snow-depth variability within a single DEM gridcell, we implemented a linear-random zigzag sampling design (Shea and Jamieson, 2010). We measured depth at random intervals of 0.3–3.0 m along two 'Z'-shaped patterns, resulting in 135–191 measurements per zigzag, within three to four 40 × 40 m gridcells (Fig. 1g) per glacier. Random intervals were machine-generated from a uniform distribution in sufficient

a Federal Sampler (described below) to unambiguously identify the snow-firn transition.

numbers that each survey was unique. Zigzag locations were randomly chosen within the upper, middle and lower regions of the ablation area of each glacier. A fourth zigzag was measured on Glacier 13 in the central ablation area at \sim 2200 m a.s.l.

Snow density was measured using a Snowmetrics wedge cutter in three snow pits on each glacier, as well as

145 Snow density

with a Geo Scientific Ltd. metric Federal Sampler. Within the snow pits (SP), we measured a vertical density profile (in 5 cm increments) with the $5 \times 10 \times 10$ cm wedge-shaped cutter (250 cm³) and a Presola 1000 g 148 spring scale (e.g. Gray and Male, 1981; Fierz and others, 2009). Wedge-cutter error is approximately $\pm 6\%$ 149 (e.g. Proksch and others, 2016; Carroll, 1977). Uncertainty in estimating density from snow-pit measurements 150 also stems from incorrect assignment of density to layers that cannot be sampled (e.g. ice lenses and hard 151 layers). We attempt to quantify this uncertainty by varying estimated ice-layer thickness by ± 1 cm ($\leq 100\%$) 152 of the recorded thickness, ice layer density between 700 and 900 kg m⁻³ and the density of layers identified 153 as being too hard to sample (but not ice) between 600 and 700 kg m⁻³. When considering all three sources 154 of uncertainty, the range of integrated density values is always less than 15% of the reference density. Depth-155 averaged densities for shallow pits (<50 cm) that contain ice lenses are particularly sensitive to changes in 156 prescribed density and ice-lens thickness. 157 While snow pits provide the most accurate measure of snow density, digging and sampling a snow pit is 158 time and labour intensive. Therefore, a Federal Snow Sampler (FS) (Clyde, 1932), which directly measures 159 depth-integrated snow-water equivalent, was used to augment the snow pit measurements. A minimum of 160 three Federal Sampler measurements were taken at each of 7–19 locations on each glacier and an additional 161 eight Federal Sampler measurements were co-located with each snow pit profile. Measurements for which the 162 snow core length inside the sampling tube was less than 90% of the snow depth were discarded. Densities at 163 each measurement location (eight at each snow pit, three elsewhere) were then averaged, with the standard 164 deviation taken to represent the uncertainty. 165 During the field campaign there were two small accumulation events. The first, on 6 May 2016, also involved 166 high winds so accumulation could not be determined. The second, on 10 May 2016, resulted in 0.01 m w.e 167 accumulation measured at one location on Glacier 2. Positive temperatures and clear skies occurred between 168 11–16 May 2016, which we suspect resulted in melt occurring on Glacier 13. The snow in the lower part of 169 the ablation area of Glacier 13 was isothermal and showed clear signs of melt and metamorphosis. The total 170

Table 2. Eight methods used to estimate snow density at unmeasured locations. Total number of resulting density values given in parentheses, with n_T the total number of snow-depth measurement locations along transects (Table 1).

Method	Source of	measured	Density assignment		
code	snow o	lensity	method		
0040	Snow pit	Federal	income d		
	Zitow pit	Sampler			
S1	•		Mean of measurements		
F1			across all glaciers (1)		
S2			Mean of measurements		
F2			for each glacier (3)		
S3	-		Regression of density on		
F3			elevation for a glacier (n_T)		
S4			Inverse distance weighted		
F4			mean for a glacier (n_T)		

amount of accumulation and melt during the study period could not be estimated so no corrections were made.

173 Density assignment

Measured snow density must be interpolated or extrapolated to estimate point-scale winter balance at each 174 snow-depth sampling location. We employ four commonly used methods to interpolate and extrapolate 175 density (Table 2): (1) calculate mean density over an entire mountain range (e.g. Cullen and others, 2017), 176 (2) calculate mean density for each glacier (e.g. Elder and others, 1991; McGrath and others, 2015), (3) 177 linear regression of density on elevation for each glacier (e.g. Elder and others, 1998; Molotch and others, 178 2005) and (4) calculate mean density using inverse-distance weighting (e.g. Molotch and others, 2005) for 179 each glacier. Densities derived from snow-pit (SP) measurements and the Federal Sampler (FS) are treated 180 separately, for reasons explained below, resulting in eight possible methods of assigning density. 181

182 Gridcell-averaged winter balance

We average one to six (mean of 2.1 measurements) point-scale values of WB within each $40 \times 40 \,\mathrm{m}$ DEM gridcell to obtain the gricell-averaged WB. The locations of individual measurements have uncertainty due to the error in the horizontal position given by the GPS unit and the estimation of observer location based on the

recorded GPS positions of the navigator. This location uncertainty could result in the incorrect assignment of a point-scale WB to a particular gridcell. However, this source of error is not further investigated because we assume that the uncertainty in gridcell-averaged WB is captured in the zigzag measurements described below. Uncertainty due to having multiple observers was also evaluated. There are no significant differences between snow-depth measurements made by observers along any transect (p>0.05), with the exception of the first transect on Glacier 4 (51 measurements).

192 Distributed winter balance

Gridcell-averaged values of WB are interpolated and extrapolated across each glacier using linear regression (LR) and simple kriging (SK). The regression relates gridcell-averaged WB and various topographic parameters, as this method is simple and has precedent for success (e.g. McGrath and others, 2015). Instead of a basic regression however, we use cross-validation and model averaging to test all combinations of the topographic parameters. We compare the regression approach with simple kriging (SK), a data-driven interpolation method free of any physical interpretation (e.g. Hock and Jensen, 1999).

In the regression, we use commonly applied topographic parameters as in McGrath and others (2015),

199 Linear regression

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including elevation, slope, aspect, curvature, "northness" and a wind-redistribution parameter; we add 201 distance-from-centreline as an additional parameter. Our sampling design ensured that the ranges of 202 topographic parameters associated with our measurement locations represent more than 70% of the total 203 area of each glacier (except elevation on Glacier 2, where our measurements captured only 50%). Topographic 204 parameters are standardized and then weighted by a set of fitted regression coefficients (β_i) calculated by 205 minimizing the sum of squares of the vertical deviations of each datum from the regression line (Davis and 206 Sampson, 1986). For details on data and methods used to estimate the topographic parameters see the 207 Supplementary Material. 208 To avoid overfitting the data and to incorporate every possible combination of topographic parameters, 209 cross-validation and model averaging are implemented. First, cross-validation is used to obtain a set of β_i 210 values that have the greatest predictive ability. We randomly select 1000 subsets of the data (2/3 of the 211 values) to fit the LR and use the remaining data (1/3) of the values to calculate a root mean squared error 212 (RMSE) (Kohavi and others, 1995). From the 1000 sets of β_i values, we select the set that results in the lowest 213 RMSE. Second, we use model averaging to account for uncertainty when selecting predictors and to maximize 214 the model's predictive ability (Madigan and Raftery, 1994). Models are generated by calculating a set of β_i 215

as described above for all possible combinations of topographic parameters (2^7 models). Using a Bayesian framework, model averaging involves weighting all models by their posterior model probabilities (Raftery and others, 1997). To obtain the final regression coefficients, the β_i values from each model are weighted according to the relative predictive success of the model, as assessed by the value of the Bayesian Information Criterion (BIC) (Burnham and Anderson, 2004). BIC penalizes more complex models which further reduces the risk of overfitting. The distributed WB is then obtained by applying the resulting regression coefficients to the topographic parameters associated with each gridcell.

223 Simple kriging

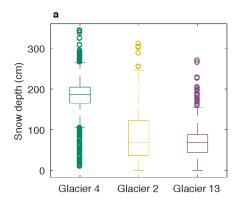
Simple kriging (SK) is a data-driven method of estimating variables at unsampled locations by using the 224 isotropic spatial correlation (covariance) of measured values to find a set of optimal weights (Davis and 225 Sampson, 1986; Li and Heap, 2008). Simple kriging assumes spatial correlation between sampling locations 226 that are distributed across a surface and then applies the correlation to interpolate between these locations. 227 228 We used the DiceKriging R package (Roustant and others, 2012) to calculate the maximum likelihood covariance matrix, as well as the range distance (θ) and nugget for gridcell-averaged values of winter balance. 229 The range distance is a measure of data correlation length and the nugget is the residual that encompasses 230 sampling-error variance as well as the spatial variance at distances less than the minimum sample spacing 231 232 (Li and Heap, 2008). Unlike topographic regression, simple kriging is not useful for generating hypotheses to explain the physical controls on snow distribution, nor can it be used to estimate winter balance on 233 unmeasured glaciers. 234

Uncertainty analysis

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To quantify the uncertainty on estimates of glacier-wide WB we conduct a Monte Carlo analysis, which uses 236 repeated random sampling of input variables to calculate a distribution of output variables (Metropolis and 237 Ulam, 1949). We repeat the random sampling process 1000 times, resulting in a distribution of values of the 238 glacier-wide WB based on uncertainties associated with the four steps outlined above. We use the standard 239 deviation of this distribution as a useful metric of uncertainty on the glacier-wide WB. Three sources of 240 uncertainty are considered separately: the uncertainty due to (1) grid-scale variability of WB ($\sigma_{\rm GS}$), (2) 241 the assignment of snow density (σ_{ρ}) and (3) interpolating and extrapolating gridcell-averaged values of WB 242 (σ_{INT}) . These individual sources of uncertainty are propagated through the conversion of snow depth and 243 density measurements to glacier-wide WB. Finally, the combined effect of all three sources of uncertainty on 244

- 245 the glacier-wide WB is quantified. We calculate a relative uncertainty as the normalized sum of differences
- between every pair of one hundred distributed WB estimates including $\sigma_{\rm GS}$ and $\sigma_{\rm INT}$.
- 247 Grid-scale uncertainty (σ_{GS})
- 248 We make use of the zigzag surveys to quantify the true variability of WB at the grid scale. Our limited data
- do not permit a spatially-resolved assessment of grid-scale uncertainty, so we characterize this uncertainty
- 250 as uniform across each glacier and represent it by a normal distribution. The distribution is centred at zero
- 251 and has a standard deviation equal to the mean standard deviation of all zigzag measurements for each
- 252 glacier. For each iteration of the Monte Carlo, WB values are randomly chosen from the distribution and
- 253 added to the values of gridcell-averaged WB. These perturbed gridcell-averaged values of WB are then used
- in the interpolation. We represent uncertainty in glacier-wide WB due to grid-scale uncertainty ($\sigma_{\rm GS}$) as the
- 255 standard deviation of the resulting distribution of glacier-wide WB estimates.
- 256 Density assignment uncertainty (σ_{ρ})
- 257 We incorporate uncertainty due to the method of density assignment by carrying forward all eight density
- 258 interpolation methods (Table 2) when estimating glacier-wide WB. By choosing to retain even the least
- 259 plausible options, as well as the questionable FS data, this approach results in a generous assessment of
- uncertainty. We represent the glacier-wide WB uncertainty due to density assignment uncertainty (σ_{ρ}) as
- 261 the standard deviation of glacier-wide WB estimates calculated using each density assignment method.
- 262 Interpolation uncertainty (σ_{INT})
- 263 We represent the uncertainty due to interpolation of gridcell-averaged WB in different ways for LR and
- SK. LR interpolation uncertainty is represented by a multivariate normal distribution of possible regression
- coefficients (β_i) . The standard deviation of each distribution is calculated using the covariance of regression
- coefficients as outlined in Bagos and Adam (2015), which ensures that regression coefficients are internally
- consistent. The β_i distributions are randomly sampled and used to calculate gridcell-estimated WB.
- 268 SK interpolation uncertainty is represented by the 95% confidence interval for gridcell-estimated values of
- WB generated by the DiceKriging package. From this confidence interval, the standard deviation of each
- 270 gridcell-estimated WB is then calculated. The standard deviation of glacier-wide WB is then found by taking
- 271 the square root of the average variance of each gridcell-estimated WB. The final distribution of glacier-wide
- 272 WB values is centred at the glacier-wide WB estimated with SK. For simplicity, the standard deviation of
- 273 glacier-wide WB values that result from either LR or SK interpolation uncertainty is referred to as $\sigma_{\rm INT}$.



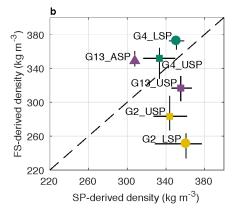


Fig. 2. Measured snow depth and density. (a) Boxplot of measured snow depth on Glaciers 4, 2 and 13 with the first quartiles (box), median (line within box), minimum and maximum values excluding outliers (bar) and outliers (circles), which are defined as being outside of the range of 1.5 times the quartiles (approximately $\pm 2.7\sigma$). (b) Comparison of depth-averaged densities estimated using Federal Sampler (FS) measurements and a wedge cutter in a snow pit (SP) for Glacier 4 (G4), Glacier 2 (G2) and Glacier 13 (G13). Labels indicate snow pit locations in the accumulation area (ASP), upper ablation area (USP) and lower ablation area (LSP). Error bars for SP-derived densities are calculated by varying the thickness and density of layers that are too hard to sample, and error bars for FS-derived densities are the standard deviation of measurements taken at one location. One-to-one line is dashed.

274 RESULTS AND DISCUSSION

275 Field measurements

276 Snow depth

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Mean snow depth varied systematically across the study region, with Glacier 4 having the highest mean snow depth and Glacier 13 having the lowest (Fig. 2). At each measurement location, the median range of measured depths (3–4 points) as a percent of the mean local depth is 2%, 11% and 12%, for Glaciers 4, 2 and 13, respectively. While Glacier 4 has the lowest point-scale variability, as assessed above, it also has

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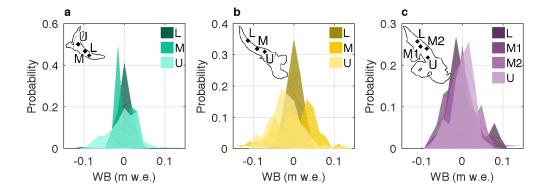


Fig. 3. Distributions of estimated winter-balance values for each zigzag survey in lower (L), middle (M) and upper (U) ablation areas (insets). Local mean has been subtracted. (a) Glacier 4. (b) Glacier 2. (c) Glacier 13.

the highest proportion of outliers, indicating a more variable snow depth across the glacier. The average standard deviation of all zigzag depth measurements is 0.07 m, 0.17 m and 0.14 m, for Glaciers 4, 2 and 13, respectively. When converted to values of WB using the local FS-derived density measurement, the average standard deviation is 0.027 m w.e., 0.035 m w.e. and 0.040 m w.e. WB data for each zigzag are not normally distributed (Fig. 3).

286 Snow density

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Contrary to expectation, co-located FS and SP measurements are found to be uncorrelated ($R^2 = 0.25$, 287 Fig. 2b). The Federal Sampler appears to oversample in deep snow and undersample in shallow snow. 288 Oversampling by small-diameter (3.2–3.8 cm) sampling tubes has been observed in previous studies, with a 289 percent error between 6.8% and 11.8% (e.g. Work and others, 1965; Fames and others, 1982; Conger and 290 McClung, 2009). Studies that use Federal Samplers often apply a 10% correction to all measurements for 291 this reason (e.g. Molotch and others, 2005). Oversampling has been attributed to slots "shaving" snow into 292 the tube as it is rotated (e.g. Dixon and Boon, 2012) and to snow falling into the slots, particularly for snow 293 samples with densities >400 kg m⁻³ and snow depths >1 m (e.g. Beaumont and Work, 1963). Undersampling 294 is likely to occur due to loss of snow from the bottom of the sampler (Turcan and Loijens, 1975). Loss by this 295 mechanism may have occurred in our study, given the isothermal and melt-affected snow conditions observed 296 over the lower reaches of Glaciers 2 and 13. Relatively poor Federal Sampler spring-scale sensitivity also calls 297 into question the reliability of measurements for snow depths < 20 cm. 298

Our FS-derived density values are positively correlated with snow depth ($R^2 = 0.59$). This relationship could be a result of physical processes, such as compaction in deep snow and preferential formation of depth

hoar in shallow snow, but is more likely a result of measurement artefacts for a number of reasons. First, 301 the total range of densities measured by the Federal Sampler seems improbably large $(227-431 \text{ kg m}^{-3})$ given 302 the conditions at the time of sampling. Moreover, the range of FS-derived values is much larger than than of 303 SP-derived values when co-located measurements are compared. Second, compaction effects of the magnitude 304 required to explain the density differences between SP and FS measurements would not be expected at the 305 measured snow depths (up to 340 cm). Third, no linear relationship exists between depth and SP-derived 306 density ($R^2 = 0.05$). These findings suggest that the Federal Sampler measurements have a bias for which 307 we have not identified a suitable correction. 308

309 Density assignment

Given the lack of correlation between co-located SP- and FS-derived densities (Fig. 2), we use the densities 310 derived from these two methods separately (Table 2). SP-derived regional (S1) and glacier-mean (S2) densities 311 are within one standard deviation of the corresponding FS-derived densities (F1 and F2) although SP-derived 312 density values are larger (see Supplementary Material, Table S2). For both SP- and FS-derived densities, the 313 mean density for any given glacier (S2 or F2) is within one standard deviation of the mean across all glaciers 314 (S1 or F1). Correlations between elevation and SP- and FS-derived densities are generally high ($R^2 > 0.5$) but 315 vary between glaciers (Supplementary material, Table S2). For any given glacier, the standard deviation of the 316 3-4 SP- or FS-derived densities is <13\% of the mean of those values (S2 or F2) (Supplementary material, 317 Table S2). We adopt S2 (glacier-wide mean of SP-derived densities) as the reference method of density 318 assignment. Though the method described by S2 does not account for known basin-scale spatial variability 319 in snow density (e.g. Wetlaufer and others, 2016), it is commonly used in winter balance studies(e.g. Elder 320 and others, 1991; McGrath and others, 2015; Cullen and others, 2017). 321

Gridcell-averaged winter balance

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The distributions of gridcell-averaged WB values for the individual glaciers are similar to those in Fig. 2a but with fewer outliers. The standard deviations of WB values determined from the zigzag surveys are almost twice as large as the mean standard deviation of point-scale WB values within a gridcell measured along transects. However, a small number of gridcells sampled in transect surveys have standard deviations in WB that exceed 0.25 m w.e. (~10 times greater than those for zigzag surveys). We nevertheless assume that the gridcell uncertainty is captured with dense sampling in zigzag gridcells.

Pulwicki and others: Estimating winter balance and its uncertainty

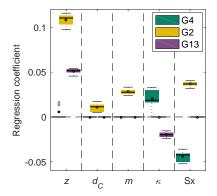


Fig. 4. Distribution of coefficients (β_i) determined by linear regression of gridcell-averaged WB on DEM-derived topographic parameters for the eight different density assignment methods (Table 2). Coefficients are calculated using standardized data, so values can be compared across parameters. Regression coefficients that are not significant are assigned a value of zero. Topographic parameters include elevation (z), distance from centreline (d_C) , slope (m), curvature (κ) and wind redistribution (Sx). Aspect (α) and "northness" (N) are not shown because coefficient values are zero in every case. The box plot shows first quartiles (box), median (line within box), mean (circle within box), minimum and maximum values excluding outliers (bars) and outliers (gray dots), which are defined as being outside of the range of 1.5 times the quartiles (approximately $\pm 2.7\sigma$).

Distributed winter balance

330 Linear Regression

Of the topographic parameters in the linear regression, elevation (z) is the most significant predictor of

332 gridcell-averaged WB for Glaciers 2 and 13, while wind redistribution (Sx) is the most significant predictor

Table 3. Glacier-wide winter balance (WB, mw.e.) estimated using linear regression and simple kriging for the three study glaciers. Root mean squared error (RMSE, mw.e.) is computed as the average of all RMSE values between gridcell-averaged values of WB (the data) that were randomly selected and excluded from interpolation (1/3 of all data) and those estimated by interpolation. RMSE as a percent of the glacier-wide WB is shown in brackets.

	Linea	r regression	Simple kriging			
	WB	RMSE	WB	RMSE		
G4	0.58	0.15~(26%)	0.62	0.13 (21%)		
G2	0.58	0.10~(17%)	0.37	0.07~(19%)		
G13	0.38	0.08~(21%)	0.27	0.07~(26%)		

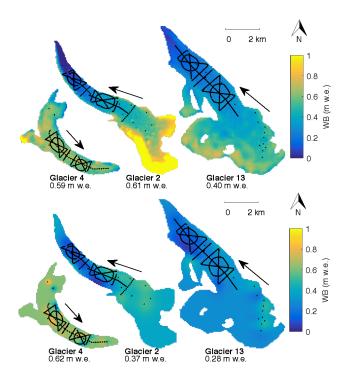


Fig. 5. Spatial distribution of winter balance (WB) estimated using linear regression (top row) and simple kriging (bottom row) with densities assigned as per S2 (Table 2). Locations of snow-depth measurements are shown as black dots. Ice-flow directions are indicated by arrows. Values of glacier-wide WB are given below labels.

for Glacier 4 (Fig. 4, Fig. 5). As expected, gridcell-averaged WB is positively correlated with elevation where the correlation is significant. It is possible that the elevation correlation was accentuated due to melt onset for Glacier 13 in particular. Many studies have found elevation to be the most significant predictor of winter-balance data (e.g. Machguth and others, 2006; McGrath and others, 2015). However, WB-elevation gradients vary considerably between glaciers (e.g. Winther and others, 1998) and other factors, such as glacier shape and orientation relative to dominant wind direction, are strong predictors of the winter-balance distribution (Machguth and others, 2006; Grabiec and others, 2011). Some studies find no significant correlation between WB on glaciers and topographic parameters, with highly variable distributions of snow attributed to complex interactions between topography and the atmosphere that could not be easily quantified (e.g. Grabiec and others, 2011; López-Moreno and others, 2011). Extrapolating relationships to unmeasured locations, especially the accumulation area, is susceptible to large uncertainties (Fig. 6). This extrapolation has a considerable effect on values of glacier-wide WB, as the highest values of WB are typically found in the accumulation area (Fig. 5).

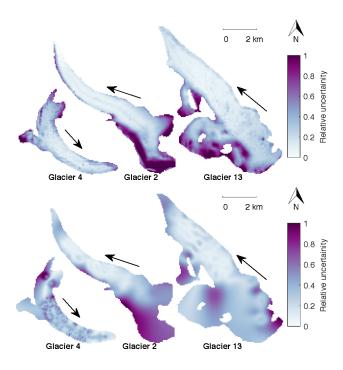


Fig. 6. Relative uncertainty in distributed winter balance (WB) (Fig. 5) found using linear regression (top row) and simple kriging (bottom row). Values closer to one indicate higher relative uncertainty. Ice-flow directions are indicated by arrows.

Gridcell-averaged WB is negatively correlated with Sx on Glacier 4, counter-intuitively indicating less snow in what would be interpreted as sheltered areas. Gridcell-averaged WB is positively correlated with Sx on Glaciers 2 and 13. Similarly, gridcell-averaged WB is positively correlated with curvature on Glacier 4 and negatively correlated on Glaciers 2 and 13. Wind redistribution and preferential deposition of snow are known to have a large influence on snow distribution at sub-basin scales (e.g. Dadić and others, 2010; Winstral and others, 2013; Gerber and others, 2017). Our results point to wind having an impact on snow distribution, but the wind redistribution parameter (Sx) may not adequately capture these effects at our study sites. For example, Glacier 4 is located in a curved valley with steep side walls, so specifying a single cardinal direction for wind may not be adequate. Further, the scale of deposition may be smaller than the resolution of the Sx parameter estimated from the DEM. Our results corroborate those of McGrath and others (2015) in a study of six glaciers in Alaska (DEM resolutions of 5 m) where elevation and Sx were the only significant parameters for all glaciers; Sx regression coefficients were smaller than elevation regression coefficients, and in some cases, negative. In addition to wind redistribution, sublimation from blowing snow has also been shown to be an important mechanism of mass loss from ridges (e.g. Musselman and others,

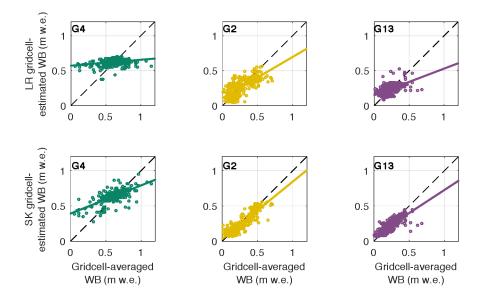


Fig. 7. Winter balance (WB) estimated by linear regression (LR, top row) or simple kriging (SK, bottom row) versus the grid-cell averaged WB data for Glacier 4 (left), Glacier 2 (middle) and Glacier 13 (right). Each circle represents a single gridcell. Best-fit (solid) and one-to-one (dashed) lines are shown.

2015). Incorporating such losses, as well as redistribution and preferential deposition, may be important for improving representations of distributed winter balance.

We find that transfer of LR coefficients between glaciers results in large estimation errors. Regression coefficients from Glacier 4 produce the highest root mean squared error (0.38 m w.e. on Glacier 2 and 0.40 m w.e. on Glacier 13, see Table 3 for comparison) and glacier-wide WB values are the same for all glaciers (0.64 m w.e.) due to the dominance of the regression intercept. Even if the regression is performed with WB values from all glaciers combined, the resulting coefficients produce large root mean squared errors when applied to individual glaciers (0.31 m w.e., 0.15 m w.e. and 0.14 m w.e. for Glaciers 4, 2 and 13, respectively). Our results are consistent with those of Grünewald and others (2013), who found that local statistical models cannot be transferred across basins and that regional-scale models are not able to explain the majority of observed variance in winter balance.

371 Simple kriging

Fitted kriging parameters, including the nugget and spatial correlation length, can provide insight into important scales of winter-balance variability. The model fitted to the gridcell-averaged values of WB for Glacier 4 has a short correlation length (90 m) and large nugget (see Supplementary Material Table S3), suggesting variability in winter balance at smaller scales. Conversely, Glaciers 2 and 13 have longer correlation

lengths (~450 m) and smaller nuggets, suggesting variability at larger scales. Additionally, simple kriging is better able to estimate values of WB for Glaciers 2 and 13 than for Glacier 4 (Fig. 7). Due to a paucity of data, simple kriging produces almost uniform gridcell-estimated values of winter balance in the accumulation area of each glacier, inconsistent with observations described in the literature (e.g. Machguth and others, 2006; Grabiec and others, 2011). Extrapolation using simple kriging leads to large uncertainty (Fig. 6), further emphasizing the need for spatially distributed point-scale measurements.

LR and SK comparison

Glacier-wide WB estimates found using both LR and SK are $\sim 0.58 \,\mathrm{m}$ w.e. for Glacier 4 but both are poor 383 predictors of WB in measured gridcells (Table 3). For Glaciers 2 and 13, SK estimates are more than 0.1 m w.e. 384 (up to 40%) lower than LR estimates (Table 3). RMSE as a percentage of the glacier-wide WB are comparable 385 between LR and SK (Table 3) with an average RMSE of 22%. This comparability is interesting, given that 386 all of the data were used to generate the SK model, while only 2/3 were used in the LR. Gridcell-estimated 387 values of WB found using LR and SK differ markedly in the upper accumulation areas of Glaciers 2 and 388 13 (Fig. 5), where observations are sparse and topographic parameters, such as elevation, vary considerably. 389 The influence of elevation results in substantially higher LR-estimated values of WB at high elevation, 390 whereas SK-estimated values approximate the nearest data. Estimates of ablation-area-wide WB differ by 391 <7% between LR and SK on each glacier, further emphasizing the combined role of interpolation method 392 393 and measurement scarcity in the accumulation area on glacier-wide WB estimates.

Uncertainty analysis

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Glacier-wide winter balance is affected by uncertainty introduced by the representativeness of gridcell-395 averaged values of WB (σ_{GS}), choosing a method of density assignment (σ_{ρ}), and interpolating WB values 396 across the domain (σ_{INT}). Using a Monte Carlo analysis, we find that interpolation uncertainty contributes 397 more to WB uncertainty than grid-scale uncertainty or density assignment method. In other words, the 398 distribution of glacier-wide WB that arises from grid-scale uncertainty and the differences in distributions 399 between methods of density assignment are smaller than the distribution that arises from interpolation 400 uncertainty (Fig. 8 and Table 4). The WB distributions obtained using LR and SK overlap for a given 401 glacier, but the distribution modes differ (Fig. 8). For reasons outlined above, SK-estimated values of WB in 402 the accumulation area are generally lower, which lowers the glacier-wide WB estimate. The uncertainty in 403 SK-estimated values of WB is large, and unrealistic glacier-wide values of WB of 0 m w.e. can be estimated 404 (Fig. 8). Our results caution strongly against including extrapolated values of WB in comparisons with 405

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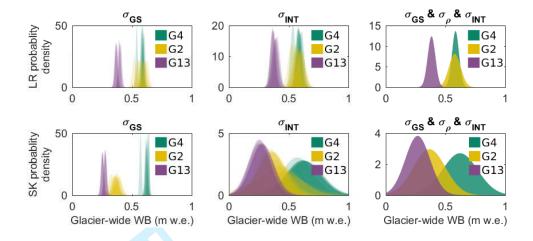


Fig. 8. Distributions of glacier-wide winter balance (WB) for Glaciers 4 (G4), 2 (G2) and 13 (G13) that arise from various sources of uncertainty. WB distribution arising from grid-scale uncertainty (σ_{GS}) (left column). WB distribution arising from interpolation uncertainty (σ_{INT}) (middle column). WB distribution arising from a combination of σ_{GS} , σ_{INT} and density assignment uncertainty (σ_{ρ}) (right column). Results are shown for interpolation by linear regression (LR, top row) and simple kriging (SK, bottom row). Left two columns include eight distributions per glacier (colour) and each corresponds to a density assignment method (S1–S4 and F1–F4).

remote sensing- or model-derived estimates of WB. If possible, such comparisons should be restricted to point-scale data.

Grid-scale uncertainty (σ_{GS}) is the smallest assessed contributor to overall WB uncertainty. This result is consistent with the generally smoothly-varying snow depths encountered in zigzag surveys, and previously reported ice-roughness lengths on the order of centimetres (e.g. Hock, 2005) compared to snow depths on the order of decimetres to metres. Given our assumption that zigzags are an adequate representation of grid-scale

Table 4. Standard deviation (×10⁻² m w.e.) of glacier-wide winter balance distributions arising from uncertainties in grid-scale WB (σ_{GS}), density assignment (σ_{ρ}), interpolation (σ_{INT}) and all three sources combined (σ_{ALL}) for linear regression (left columns) and simple kriging (right columns)

	Linear regression				Simple kriging					
	$\sigma_{ m GS}$	$\sigma_{ ho}$	σ_{INT}	σ_{ALL}	$\sigma_{ m GS}$	$\sigma_{ ho}$	σ_{INT}	σ_{ALL}		
Glacier 4	0.86	1.90	2.13	2.90	0.85	2.15	14.05	14.72		
Glacier 2	1.80	3.37	3.09	4.90	2.53	2.03	13.78	13.44		
Glacier 13	1.12	1.68	2.80	3.20	1.15	1.27	9.65	10.43		

- variability, the low WB uncertainty arising from $\sigma_{\rm GS}$ implies that subgrid-scale sampling need not be a high
- 413 priority for reducing overall uncertainty. Our assumption that the 3–4 zigzag surveys can be used to estimate
- 414 glacier-wide $\sigma_{\rm GS}$ may be flawed, particularly in areas with debris cover, crevasses and steep slopes.
- Our analysis did not include uncertainty arising from a number of sources, which we assume either to
- 416 be encompassed by the sources investigated or to be negligible contributors. These sources of uncertainty
- 417 include density measurement errors associated with the Federal Sampler, wedge cutters and spring scales,
- 418 vertical and horizontal errors in the DEM and error associated with estimating measurement locations.
- The values of glacier-wide WB for our study glaciers (using LR and S2 density assignment method), with
- 420 an uncertainty equal to one standard deviation of the distribution found with Monte Carlo analysis, are:
- 421 0.59 ± 0.03 m w.e. for Glacier 4, 0.61 ± 0.05 m w.e. for Glacier 2 and 0.40 ± 0.03 m w.e. for Glacier 13. The
- 422 glacier-wide WB uncertainty from combined sources of uncertainty ranges from 0.03 m w.e (5%) to 0.05 m
- 423 w.e (8%) for linear-regression estimates and from 0.10 m w.e (37%) to 0.15 m w.e (24%) for simple-kriging
- 424 estimates (Table 3).

425 Context and caveats

- 426 Regional winter-balance gradient
- 427 Although we find considerable inter- and intra-basin variability in winter balance, our results are consistent
- 428 with a regional-scale winter-balance gradient for the continental side of the St. Elias Mountains (Fig. 9).
- Winter-balance data are compiled from Taylor-Barge (1969), the three glaciers presented in this paper and
- 430 two snow pits we analyzed near the head of the Kaskawulsh Glacier between 20-21 May 2016. The data
- show a linear decrease of $0.024\,\mathrm{m\,w.e.~km^{-1}}$ ($\mathrm{R}^2=0.85$) in winter balance with distance from the regional
- 432 topographic divide between the Kaskawulsh and Hubbard Glaciers, as identified by Taylor-Barge (1969).
- 433 While the three study glaciers fit the regional trend, the same relationship would not apply if just the Donjek
- Range were considered. We hypothesize that interaction between meso-scale weather patterns and large-scale
- 435 mountain topography is a major driver of regional-scale winter balance. Further insight into regional-scale
- 436 patterns of winter balance in the St. Elias Mountains could be gained by investigating moisture source
- 437 trajectories and the contribution of orographic precipitation.
- 438 Limitations and future work
- 439 The potential limitations of our work include the restriction of our data to a single year, minimal sampling
- 440 in the accumulation area, the problem of uncorrelated SP- and FS-derived densities, a sampling design that

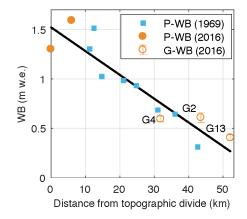


Fig. 9. Relationship between winter balance (WB) and linear distance from the regional topographic divide between the Kaskawulsh and Hubbard Glaciers in the St. Elias Mountains. Point-scale values of WB from snow-pit data reported by Taylor-Barge (1969) (blue boxes, P-WB). LR-estimated glacier-wide WB calculated using density assignment S2 for Glaciers 4 (G4), 2 (G2) and 13 (G13) with errors bars calculated as the standard deviation of Monte Carlo-derived WB distributions (this study) (open orange circles, G-WB). Point-scale WB estimated from snow-pit data at two locations in the accumulation area of the Kaskawulsh Glacier, collected in May 2016 (unpublished data, SFU Glaciology Group) (filled orange dots, P-WB). Black line indicates best fit (R² = 0.85).

could not be optimized a priori, the assumption of spatially uniform subgrid variability and lack of more finely resolved DEMs.

Inter-annual variability in winter balance is not considered in our study. A number of studies have found temporal stability in spatial patterns of snow distribution and that statistical models based on topographic parameters could be applied reliably between years (e.g. Grünewald and others, 2013). For example, Walmsley (2015) analyzed more than 40 years of winter balance recorded on two Norwegian glaciers and found that snow distribution is spatially heterogeneous yet exhibits robust temporal stability. Contrary to this, Crochet and others (2007) found that snow distribution in Iceland differed considerably between years and depended primarily on the dominant wind direction over the course of a winter. Therefore, multiple years of snow depth and density measurements, that are not necessarily consecutive, are needed to better understand inter-annual variability in winter-balance distribution within the Donjek Range.

There is a conspicuous lack of data in the accumulation areas of our study glaciers. With increased sampling in the accumulation area, interpolation uncertainties would be reduced where they are currently greatest and the linear regression would be better constrained. Although certain regions of the glaciers remain inaccessible for direct measurements, other methods of obtaining winter-balance, including ground-penetrating radar

and DEM differencing with photogrammetry or lidar, could be used in conjunction with manual probing to 456 increase the spatial coverage of measurements. 457 The lack of correlation between SP- and FS-derived densities needs to be reconciled. Contrary to our 458 results, most studies that compare SP- and FS-derived densities report minimal discrepancy (e.g. Dixon 459 and Boon, 2012, and sources within). Additional co-located density measurements are needed to better 460 compare the two methods of obtaining density values. Comparison with other Federal Samplers would also 461 be informative. Even with this limitation, density assignment was, fortunately, not the largest source of 462 uncertainty in estimating glacier-wide winter balance. 463 Our sampling design was chosen to achieve broad spatial coverage of the ablation area, but is likely too 464 finely resolved along transects for many mass-balance surveys to replicate. An optimal sampling design would 465 minimize uncertainty in winter balance while reducing the number of required measurements. Analysis of 466 the estimated winter balance obtained using subsets of the data is underway to make recommendations on 467 optimal transect configuration and along-track spacing of measurements. López-Moreno and others (2010) 468 found that 200-400 observations are needed within a non-glacierized alpine basin (6 km²) to obtain accurate 469 and robust snow distribution models. Similar guidelines would be useful for glacierized environments. 470 In this study, we assume that the subgrid variability of winter balance is uniform across a given glacier. 471 Contrary to this assumption, McGrath and others (2015) found greater variability of winter-balance values close to the terminus. Testing our assumption could be a simple matter of prioritizing the labour-intensive 473 zigzags surveys. To ensure consistent quantification of subgrid variability, zigzag survey measurements could 474 also be tested against other measurements methods, such as lidar. 475 DEM gridcell size is known to influence values of computed topographic parameters (Zhang and 476 Montgomery, 1994; Garbrecht and Martz, 1994; Guo-an and others, 2001; López-Moreno and others, 2010). 477 The relationship between topographic parameters and winter balance is, therefore, not independent of DEM gridcell size. For example, Kienzle (2004) and López-Moreno and others (2010) found that a decrease in 479 spatial resolution of the DEM results in a decrease in the importance of curvature and an increase in 480 the importance of elevation in regressions of snow distribution on topographic parameters in non-glacierized 481 basins. The importance of curvature in our study is affected by the DEM smoothing that we applied to obtain 482 a spatially continuous curvature field (see Supplementary Material). A comparison of regression coefficients 483 from high-resolution DEMs obtained from various sources and sampled with various gridcell sizes could be 484

- used to characterize the dependence of topographic parameters on DEMs, and therefore assess the robustness of inferred relationships between winter balance and topographic parameters.
- 487 CONCLUSION
- 488 We estimate winter balance for three glaciers (termed Glacier 2, Glacier 4 and Glacier 13) in the St. Elias
- 489 Mountains, Yukon, Canada from multiscale snow depth and density measurements. Linear regression and
- 490 simple kriging are used to obtain estimates of distributed winter balance. We use Monte Carlo analysis to
- evaluate the contributions of interpolation, the assignment of snow density and grid-scale variability of winter
- 492 balance to uncertainty in glacier-wide winter balance.
- Values of glacier-wide winter balance estimated using linear regression and simple kriging differ by up
- 494 to $0.24\,\mathrm{m}\,\mathrm{w.e.}$ ($\sim 50\%$). We find that interpolation uncertainty is the largest assessed source of uncertainty
- 495 in glacier-wide winter balance (5% for linear-regression estimates and 32% for simple-kriging estimates).
- 496 Uncertainty resulting from the method of density assignment is comparatively low, despite the wide range of
- 497 methods explored. Given our representation of grid-scale variability, the resulting winter balance uncertainty
- 498 is small indicating that extensive subgrid-scale sampling is not required to reduce overall uncertainty.
- Our results suggest that processes governing distributed winter balance differ between glaciers, highlighting
- 500 the importance of regional-scale winter-balance studies. The estimated distribution of winter balance on
- 501 Glacier 4 is characterized by high variability, as indicated by the poor correlation between estimated and
- 502 observed values and large number of data outliers. Glaciers 2 and 13 appear to have lower spatial variability,
- 503 with elevation being the dominant predictor of gridcell-averaged winter balance. A wind-redistribution
- 504 parameter is found to be a weak but significant predictor of winter balance, though conflicting relationships
- 505 between glaciers make it difficult to interpret. Although challenges persist when estimating winter balance,
- our data are consistent with a regional-scale winter-balance gradient for the continental side of the St. Elias
- 507 Mountains.

508 AUTHOR CONTRIBUTION STATEMENT

- 509 AP planned and executed the data collection, performed all calculations and drafted the manuscript. GF
- 510 conceived of the study, contributed to field planning and data collection, oversaw all stages of the work and
- 511 edited the manuscript. VR provided guidance with statistical methods and edited the manuscript.

512 ACKNOWLEDGEMENTS

- 513 We thank the Kluane First Nation (KFN), Parks Canada and the Yukon Territorial Government for granting
- 514 us permission to work in KFN Traditional Territory and Kluane National Park and Reserve. We are
- 515 grateful for financial support provided by the Natural Sciences and Engineering Research Council of Canada,
- 516 Simon Fraser University and the Northern Scientific Training Program. We kindly acknowledge Kluane Lake
- 517 Research Station, Sian Williams, Lance Goodwin and Trans North pilot Dion Parker for facilitating field
- 518 logistics. We are grateful to Alison Criscitiello and Coline Ariagno for all aspects of field assistance and Sarah
- 519 Furney for assistance with data entry. Thank you to Etienne Berthier for providing us with the SPIRIT SPOT-
- 520 5 DEM and for assistance in DEM correction. We are grateful to Derek Bingham and Michael Grosskopf for
- assistance with the statistics, including simple kriging. Luke Wonneck, Leif Anderson and Jeff Crompton all
- 522 provided thoughtful and constructive comments on drafts of the manuscript.

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