

Optimizing snow survey design for winter balance of alpine glaciers

Alexandra PULWICKI,¹ Gwenn E. FLOWERS,¹

¹ *Department of Earth Sciences, Faculty of Science, Simon Fraser University, Burnaby, BC, Canada*

Correspondence: Alexandra Pulwicksi <apulwick@sfu.ca>

ABSTRACT.

INTRODUCTION

Estimates of basin-wide seasonal snow accumulation are critical for the availability and timing of surface runoff, especially in mountainous regions. On glaciers, the distribution of snow is half of the seasonally resolved mass balance, initializes ablation conditions and affects energy and mass exchange between the land and atmosphere (e.g. Hock, 2005; Réveillet and others, 2016). The net accumulation and ablation of snow on a glacier over a winter season is known as the winter surface mass balance, or “winter balance” (WB) (Cogley and others, 2011).

Snow distribution is spatially variable so properties, such as snow depth, must be measured over an extensive area. In addition, the period of peak accumulation is short so snow measurement must be completed quickly and efficiently. As a result, extensive and high-resolution measurements of snow depth are nearly impossible to obtain. Snow surveys must therefore be optimized in the extent and spacing of snow measurement locations, especially when labour-intensive methods like snow probing are used.

Optimal sampling schemes for snow probing are central to accurately estimating snow distribution and mass balance from *in situ* measurements. Measuring snow depth and travelling between measurement locations is both time consuming and can disturb the snow so care must be taken to choose a sampling scheme that avoids bias, allows for the greatest variability to be measured and minimizes distance travelled (Shea and Jamieson, 2010). There are a number of different designs that have been employed to obtain point measurements, including pure random (e.g. Elder and others, 1991), linear random (e.g. Shea and Jamieson, 2010), nested (e.g. Schweizer and others, 2008), gridded random (e.g. Bellaire and Schweizer, 2008; Elder and others, 2009;

26 Bellaire and Schweizer, 2011) and gridded (e.g. Molotch and Bales, 2005; Kronholm and others, 2004; López-
27 Moreno and others, 2011). Sampling designs that incorporate randomness are favourable because they limit
28 sampling bias by varying sample spacing and direction. However, they are less efficient than sampling designs
29 that incorporate grids. Grid-style sampling designs minimize travel distance but measurements are biased by
30 regularly spaced intervals and linear orientations, which could result in an under representation of the snow
31 variability (Kronholm and others, 2004) (check this ref??).

32 Snow surveys on glaciers are conducted to estimate winter balance and multi-year sampling programs are
33 often established to monitor changes in winter balance with time. An optimized sampling design requires (1)
34 a sampling pattern that captures spatial variability and minimizes travel distance and (2) knowledge of the
35 minimum number of measurement locations needed to accurately estimate WB. The sampling pattern used for
36 most winter balance programs does not include randomness and measurements are typically collected along
37 the glacier midline. However, midline transects are known to underestimate winter balance so transverse
38 transects are often added to improve the reliability of the sampling scheme (e.g. Walmsley, 2015). An
39 hourglass with inscribed circle (personal communication from C. Parr, 2016) is an alternative sampling
40 design that is attractive because it is able to capture changes in WB with elevation but is not biased along
41 the midline and is easy to travel. To our knowledge, no study has yet compared the ability of these two
42 sampling designs to capture spatial variability in WB. There are few studies that investigate the number of
43 measurement locations needed to effectively sample WB distribution (c.f. Walmsley, 2015). ? investigated
44 the number of measurement locations needed to estimate glacier mass balance, but snow is known to vary
45 at much shorter length scales than melt, so an investigation into WB survey design is needed. (I think this
46 paragraph needs more citations...)

47 The goal of our work is to provide insight into ways to optimize WB sampling design by investigating various
48 sampling patterns and number of measurement locations. The role of sub-gridcell variability in choosing a
49 sampling design is investigated by varying the noise introduced to the assumed WB distribution. We examine
50 three study glaciers with differing spatial patterns of WB to determine the applicability of our conclusions
51 between glaciers.

52 STUDY SITE

53 We investigate sampling design for winter balance surveys on three unnamed glaciers in the Donjek Range
54 of the St. Elias Mountains. Glacier 4, Glacier 2 and Glacier 13 (labelling adopted from Crompton and
55 Flowers (2016)) are small alpine glaciers with simple geometries. The glaciers are generally oriented southeast-

northwest in valleys with steep walls. A detailed analysis of estimating winter balance on these three glaciers is presented in Pulwinski and others (2017).

METHODS

Computer model WB

The computer model portion of our work uses a prescribed WB distribution to test possible sampling designs. Gridcell values of WB that fall within each sampling design are extracted from the prescribed WB distribution and then used to estimate a new WB distribution. The WB distribution derived from various sampling designs is then directly compared to the prescribed WB distribution to estimate spatially resolved error. For each study glacier, the prescribed WB distribution is equivalent to the distribution presented in Pulwinski and others (2017). The prescribed WB was estimated using a linear regression fitted to WB data on each glacier, which were obtained from direct measurements of snow depth and density.

We investigate numerous sampling designs. Sampling designs are based on a sampling pattern and number of measurement locations. We chose various sampling patterns that could be used for a snow survey (Figure 2). Midline (M) and midline with transverse transects (M+T) are the most common survey designs used in WB studies (e.g. Machguth and others, 2006). The midline survey aims to capture changes in WB with elevation and transverse transects provide observation of lateral variations in WB. Hourglass (H) and inscribed circle (C) allow for sampling in multiple directions and are easy to travel (personal communication from C. Parr, 2016). We use hourglass and circle patterns separately and combined. Finally, a random pattern (R) of measurement locations is used. All sampling patterns are restricted to the ablation area, where terrain is accessible and direct measurements of snow depth are easy to obtain. For comparison, we also present results from a random sample pattern that spans the entire glacier, which is known to be the most accurate sampling pattern (ref?). For all sampling patterns we estimate WB using n measurement locations, where n ranges from a minimum of eight (constrained by using all seven topographic parameters for interpolation) to a maximum determined by the number of gridcells within a sampling pattern. The measurement locations are evenly distributed within the sampling pattern.

To simulate the process of measuring WB from the assumed distribution, we first obtain WB values from the prescribed WB distribution at selected measurement locations for each sampling pattern. Then, we add a low or high amount of noise to the WB data. Low noise is defined by a normal distribution that is centred at zero and has a standard deviation equal to the mean standard deviation of WB data from a series of

high-density gridcell-scale surveys on each glacier (see Pulwinski and others, 2017, for details). High noise is defined in the same way as low noise but the standard deviation of the normal distribution is five times larger. The standard deviation of low noise is $\sim 5\%$ of the glacier-wide WB, while high noise is $\sim 25\%$ of the glacier-wide WB. A random number from the high or low noise distribution is chosen for each datum and added to the value of WB.

A linear regression is then used to interpolate the modified values of WB for each glacier. WB is regressed on topographic parameters that have been derived from a SPOT-5 digital elevation model (see Pulwinski and others, 2017, for details). The topographic parameters include elevation, slope, aspect, distance from glacier centreline, “northness”, curvature and a wind redistribution parameter. The linear regression calculates regression coefficients that minimize the sum of squares between estimated WB and WB input data. The resulting regression coefficients are then applied to the topographic parameters associated with each gridcell to obtain distributed WB. RMSE is calculated by taking the square root of the mean difference between all gridcells in the prescribed WB distribution and the WB distribution derived with the sampling design.

The process of adding random noise to sampled WB values and fitting a regression to estimate WB is repeated 100 times. Each repetition uses a different set of random noise resulting in a range of WB and RMSE values. A mean WB and RMSE from all runs is then calculated.

Measured values of WB

Measured values of WB are found by obtaining direct measurement of snow depth and density. Snow depth was measured using a 3.2m graduated aluminium avalanche probe. Measurement locations followed linear and curvilinear transects, which were similar between study glaciers, with a sample spacing of 10–60m. Spacing was constrained by protocols for safe glacier travel. Each observer made 3–4 depth measurements within ~ 1 m at each transect measurement location. We restricted snow-depth sampling to the ablation area, where the clear districting between snow and ice ensure that only snow from the current accumulation season is measured. See Pulwinski and others (2017) for details on measuring snow depth along transects. In total, we collected more than 9000 snow-depth measurements throughout the study area. Snow density was measured using a wedge cutter in three snow pits that spanned a large portion of the elevation on each glacier. A mean density was then calculated for each glacier and this value was use dot convert snow depth at all measurement locations to values of point-scale WB. All point-scale WB values located within a common gridcell are averaged to obtain values of gridcell-scale WB, which are then used in the linear regression.

114 The process of estimating distributed WB using various sampling designs is then applied to measured
 115 values of WB. Sampling designs are derived from all measurement locations for each study glacier (Figure
 116 ??). As above, midline, midline with transects, circle, hourglass, circle with hourglass and random sampling
 117 patterns are used. All possible values of n are investigated, but the number of measurement locations is more
 118 limited when WB data are used. One hundred iterations of adding random noise, both low and high, and
 119 then executing a linear regression to estimate distributed WB are then completed, as above.

120 RESULTS AND DISCUSSION

121 CONCLUSION

122 ACKNOWLEDGEMENTS

123 We thank the Kluane First Nation (KFN), Parks Canada and the Yukon Territorial Government for granting
 124 us permission to work in KFN Traditional Territory and Kluane National Park and Reserve. We are
 125 grateful for financial support provided by the Natural Sciences and Engineering Research Council of Canada,
 126 Simon Fraser University and the Northern Scientific Training Program. We kindly acknowledge Kluane Lake
 127 Research Station, Sian Williams, Lance Goodwin and Trans North pilot Dion Parker for facilitating field
 128 logistics. We are grateful to Alison Criscitiello and Coline Ariagno for all aspects of field assistance and Sarah
 129 Furney for assistance with data entry. Thank you to Etienne Berthier for providing us with the SPIRIT SPOT-
 130 5 DEM and for assistance in DEM correction. We are grateful to Derek Bingham and Michael Grosskopf for
 131 assistance with statistics.

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