Uncertainties in estimating winter balance from direct measurements on glaciers

Alexandra PULWICKI,[1] Gwenn E. FLOWERS,[1] Valentina RADIĆ,[2]

[1] *Simon Fraser University, Burnaby, BC, Canada*
[2] *University of British Columbia, Vancouver, BC, Canada*
Correspondence: Alexandra Pulwicki <apulwick@sfu.ca>

ABSTRACT. Accurately estimating winter surface mass balance on glaciers is central to quantifying overall mass balance and melt runoff. However, measuring and modelling snow distribution and variability is inherently difficult in alpine terrain, resulting in high winter balance uncertainty. The goals of this paper are to examine methods and sources of error when converting snow measurements to estimates of winter balance and to gain a more comprehensive understanding of uncertainties inherent in this process. We extensively measure snow depth and density, at various spatial scales, on three glaciers in the St. Elias Mountains, Yukon. Elevation is found to be the dominant driver of accumulation variability but the relationship varies between glaciers. Wind redistribution and preferential deposition are also shown to affect snow distribution, but more complex parametrization is needed to fully capture wind effects. Through Monte Carlo analysis we find that interpolation of SWE measurements is the largest source of winter balance uncertainty. Snow distribution patterns differ considerably between glaciers, highlighting strong inter- and intra-basin variability. Despite the challenges associated with accurately and precisely estimating winter balance, our results are consistent with the previously reported regional accumulation gradient.

INTRODUCTION

Winter surface mass balance, or "winter balance", is the net accumulation and ablation of snow over the winter season (**?**), which constitutes glacier mass input. Accurate estimation of winter surface mass balance is critical for correctly simulating the summer and overall mass balance of a glacier (e.g. **?**). Effectively representing the spatial distribution of snow is also important for simulating snow and ice melt as well as energy and mass exchange between the land and atmosphere, which allows for better monitoring of surface runoff and its downstream effects (e.g. **?**). Snow distribution is sensitive to a number of complex process that partially depend on glacier location, topography, and orientation (e.g. **????**). Current models are not able to fully represent these processes so there is a significant source of uncertainty that undermines the ability of models to represent current and projected glacier conditions (**?**).

Winter balance is notoriously difficult to estimate. Snow distribution in alpine regions is highly variable and influenced by dynamic interactions between the atmosphere and complex topography, operating on multiple spatial and temporal scales (e.g. **???**). Extensive, high resolution and accurate snow distribution measurements on glaciers are almost impossible to achieve due to limitations of the various methods used to quantify snow water equivalent (e.g. **??**). For example, snow probes yield accurate point measurements but have negligible spatial coverage. Conversely, gravimetric methods yield spatially

extensive measurements of mass change but cannot capture spatial variability of snow within a basin (**?**).

Most glacier mass balance programs that employ direct measurements estimate winter balance in a similar way to summer balance, where snow depth measurements taken at a few stake locations are interpolated using basic methods (e.g. **????**). However, this equivalence is likely inappropriate. Melt is strongly affected by air temperature and solar radiation (e.g. **?**), both of which are consistent across large spatial domains (e.g. **?**). Conversely, snow distribution is largely driven by precipitation (e.g. **?**) and wind patterns (e.g. **??**), which are known to be highly heterogeneous in alpine environments (e.g. **?**). Snow distribution is therefore highly variable and has short correlation length scales (e.g. **????????**), contributing to a high level of uncertainty in mass balance models that few studies have directly addressed.

Those studies that have focused on obtaining detailed estimates of winter balance have used a wide range of techniques to measure snow water equivalent, including direct measurement of snow depth and density (e.g. **?**), lidar/photogrammerty (e.g. **?**) and ground penetrating radar (e.g. **???**). Spatial coverage of measurements is often limited and often consists of an elevation transect along the glacier centreline (e.g. **??**). Interpolation of these measurements is primarily done with a linear regression that includes only a few topographic parameters (e.g. **?**), with elevation being the most common. Other established techniques include hand contouring (e.g. **?**), kriging (e.g. **?**)

and attributing measured accumulation values to elevation bands (e.g. **?**). Physical snow models have been applied on only a few glaciers (e.g. **??**) but a lack of detailed meteorological data generally prohibits their wide spread application. Error analysis is rarely undertaken and to our knowledge, no studies have thoroughly investigated uncertainty in spatially distributed estimates ofwinter balance estimates.

More sophisticated models and measurement techniques of snow distribution are available and widely used in the field of snow science. Surveys described in the snow science literature are generally spatially extensive and designed to measure snow depth and density throughout a basin and ensure that all terrain types are sampled. A wide array of measurement interpolation methods are used, including linear (e.g. **?**) and non-linear regressions (e.g. **?**) that include numerous terrain parameters as well as geospatial interpolation (e.g. **?**) such as kriging, and interpolation methods are often combined (e.g. regression kriging) to yield improved fit (e.g. **?**). Physical snow models such as Alpine3D (**?**) and SnowDrift3D (**?**) are continuously being improved and tested within the snow science literature. Error analysis has been considered from both a theoretical (e.g. **?**) and applied perspective (e.g. **???**).

The precision and accuracy of winter balance estimates can likely be improved by incorporating more sophisticated tools and interpolation methodologies, and by gaining a more comprehensive understanding of inherent uncertainties. The overall goals of our work are to (1) critically examine methods of moving from direct snow depth and density measurements to estimating winter balance and to (2) identify sources of uncertainty, evaluate their magnitude and assess their combined contribution to uncertainty in winter balance. We focus on commonly applied low-complexity methods of measuring and estimating winter balance with the hope of making our results broadly applicable.

STUDY SITE

Winter balance surveys were conducted on three glaciers in the Donjek Range of the St. Elias Mountains, located in south western Yukon, Canada (Figure **??**, Table **??**). The Donjek Range is approximately 30×30 km and Glacier 4, Glacier 2 and Glacier 13 (labelling adopted from **?**) are located along a SW-NE transect through the range. These small, polythermal alpine glaciers are generally oriented SE-NW, with Glacier 4 predominantly southeast facing and Glaciers 2 and 13 generally northwest facing. The glaciers have simple geometries and have steep head and valley walls. The St. Elias Mountains rise sharply from the Pacific Ocean, creating a significant climatic gradient between coastal maritime conditions, generated by Aleutian–Gulf of Alaska low-pressure systems, and interior continental conditions, driven by the Yukon–Mackenzie high-pressure system (**?**). The boarder between the two climatic zones shifts between Divide Station (**??** km from the ocean) and the head of the Kaskawulsh Glacier (**??**km from the ocean) based on synoptic conditions. The Donjek Range is located approximately 40 km to the east of the divide between the

Hubbard and Kaskawulsh Glaciers (**?**). Research on snow distribution and glacier mass balance in this area is limited. A series of research programs were operational in the 1960s (**??**) and long-term studies on a few alpine glaciers have arisen in the last 30 years (e.g. **?**).

METHODS

Estimating glacier midwinter balance involves transforming measurements of snow depth and density into distributed estimates of snow water equivalent (SWE). We do this in four steps: (1) We obtain direct measurements of snow depth and density in the field. (2) We interpolate density measurements to all depth-measurement locations in order to calculate the SWE at each of these locations. This is necessary because we measure density at relatively few locations of depth. (3) We average all SWE values within each gridcell of a digital elevation model (DEM). (4) We interpolate and extrapolate these gridcell averaged SWE values to obtain a spatially distributed winter balance (in m w.e.) across the glacier surface. We choose to use a linear regression between gridcell average SWE and topographic parameters, as well as simple kriging for this process of interpolation and extrapolation. The specific winter balance is then calculated as the areally-averaged SWE. For brevity, we refer to these four steps as (1) field measurements, (2) distributed snow density, (3) gridcell average SWE and (4) distributed SWE. Detailed methodology for each step is outlined below.

Field measurements

Sampling design
The snow surveys were designed to capture variability in snow depth at regional, basin, gridcell and point spatial scales (**?**). To capture variability at the regional scale we choose three glaciers along the precipitation gradient in the St. Elias Mountains, Yukon (Figure **??**b) (**?**). To account for basin-scale variability, snow depth was measured along linear and curvilinear transects on each glacier (Figure **??**c) with sample spacing of $10 - 60$ m (Figure **??**d). We selected centreline and transverse transects because they are commonly used for winter balance estimates (e.g. **??**) as well as an hourglass pattern with an inscribed circle, which allows for sampling in multiple directions and easy travel (Parr, C., 2016 personal communication). To capture point-scale variability, we took 3–4 depth measurements within $\sim$1 m of each other (Figure **??**e) at each transect measurement location. To capture variability at the gridcell scale, we densely sample up to four gridcells on each glacier using a linear-random sampling design termed 'zigzag'. In total, we collected more than 9000 snow depth measurements throughout the study area (Table **??**).

Snow depth: transects
SWE can be estimated as the product of the snow depth and depth-averaged density. Snow depth is generally accepted to be more variable than density (**???**) so we chose a sampling design that resulted in a ratio of approximately 55:1 snow depth to snow density measurements. Our sampling campaign involved four people and occurred

Table 1. Physical characteristics of study glaciers and May 2016 winter balance survey details for Glacier 4 (G4), Glacier 2 (G2), and Glacier 13 (G13), including number of snow-depth measurement locations along transects (n_T), total length of transects (d_T), number of combined snow pit (SP) and Federal Sampler (FS) density measurement locations (n_ρ) and number of zigzag surveys (n_{zz}).

	Location	Elevation (m a.s.l)			Slope (°)	Area	Date	Survey Details			
	UTM Zone 7	Mean	Range	ELA	Mean	(km)		n_T	d_T (km)	n_ρ	n_{zz}
G4	595470 E 6740730 N	2344	1958–2809		12.8	3.8	4–7 May 2016	649	13.1	7	3
G2	601160 E 6753785 N	2495	1899–3103		13.0	7.0	8–11 May 2016	762	13.6	7	3
G13	604602 E 6763400 N	2428	1923–3067		13.4	12.6	12–15 May 2016	941	18.1	19	4

between 5–15 May, 2016, which corresponds to the historical peak seasonal snow accumulation in Yukon (Yukon Snow Survey Bulletin and Water Supply Forecast, May 1, 2016). While roped-up for glacier travel at fixed distances between observers, the lead observer used a single-frequency GPS unit (Garmin GPSMAP 64s) to navigate between predefined transect measurement locations (Figure **??**e). The remaining three observers used 3.2 m graduated aluminium avalanche probes to make snow depth measurements. The location of each set of depth measurements, taken by the second, third and fourth observers, was approximated based on the recorded location of the first observer and the direction of travel.

Snow depth sampling was concentrated in the ablation area to ensure that only snow from the current accumulation season was measured. The boundary between snow and firn in the accumulation area, especially when using an avalanche probe, can be difficult to detect and often misinterpreted (**??**). We intended to use a firn corer to measure SWE in the accumulation area, but cold snow combined with positive air temperatures led to cores being unrecoverable. Successful snow depth and density measurements within the accumulation area were made either in snow pits or using a Federal Sampler to unambiguously identify the snow–firn transition.

Snow depth: zigzags
To capture variability within a single DEM gridcell, we implemented a linear-random sampling design, termed 'zigzag' (**?**). We measured depth at random intervals ($0.3 - 3.0$ m) along two 'Z'-shaped transects within three to four 40×40 m gridcells (Figure **??**g) resulting in $135 - 191$ measurements in each zigzag. Zigzag locations were randomly chosen within the upper, middle, and lower portions of the ablation area of each glacier. We were able to measure a fourth zigzag on Glacier 13 that was located in the central ablation area ($\sim$2200 m a.s.l.).

Snow density
Snow density was measured using a wedge cutter in three snowpits on each glacier as well as a using a Federal Sampler. Within the snowpit (SP), we measured a vertical density profile by inserting a $5 \times 10 \times 10$ cm wedge-shaped cutter (250 cm^3) in 5 cm increments and then weighing the samples with a spring scale (e.g. **??**). Uncertainty in estimating density from snow pits stems from incorrect assignment of density to layers that could not be sampled

(i.e. ice lenses and hard layers). We attempt to quantify this uncertainty by varying three values: ice layer thickness by ± 1 cm ($\leq 100\%$) of the recorded thickness, ice layer density between 700 and 900 kg m^{-3} and the density of layers identified as being too hard to sample (but not ice) between 600 and 700 kg m^{-3}. When considering all three sources of uncertainty, the range of integrated density values is always less than 15% of the reference density. Density values for shallow pits that contain ice lenses are particularly sensitive to changes in prescribed density and ice lens thickness.

While snow pits provide the most accurate measure of snow density, digging and sampling a snow pit is time and labour intensive. Therefore, a Federal Snow Sampler (FS) (**?**), which directly measures depth-integrated SWE, was used to augment the snowpit measurements. A minimum of three FS measurements were taken at each of $7-19$ locations on each glacier and an additional eight FS measurements were co-located with each snow pit profile. Measurements where the snow core length inside the FS was less than 90% of the snow depth were discarded. Density values at each measurement location were then averaged and error is taken to be the standard deviation of these measurements.

During the field campaign there were two small accumulation events. The first, on 6 May 2016, also involved high winds so accumulation could not be determined. The second, on 10 May 2016, resulted in 0.01 m w.e accumulation measured at one location on Glacier 2. Positive temperatures and clear skies occurred between 11–16 May 2016, which we suspect resulted in melt occurring on Glacier 13. The snow in the lower part of the ablation area of Glacier 13 was isothermal and showed clear signs of melt and metamorphosis. The total amount of accumulation and melt during the study period could not be estimated so no corrections were made.

Distributed snow density

Measured snow density must be interpolated or extrapolated to estimate SWE at each snow-depth sampling location. We employ four separate methods that are commonly used to interpolate density (Table **??**): (1) calculating mean density over an entire mountain range (e.g. **?**), (2) calculating mean density for each glacier (e.g. **??**), (3) linear regression of density on elevation for each glacier (e.g. **??**) and (4) inverse-distance weighted density (e.g. **?**). SP- and FS-derived densities are treated separately, for reasons explained below, resulting in eight possible methods of assigning density.
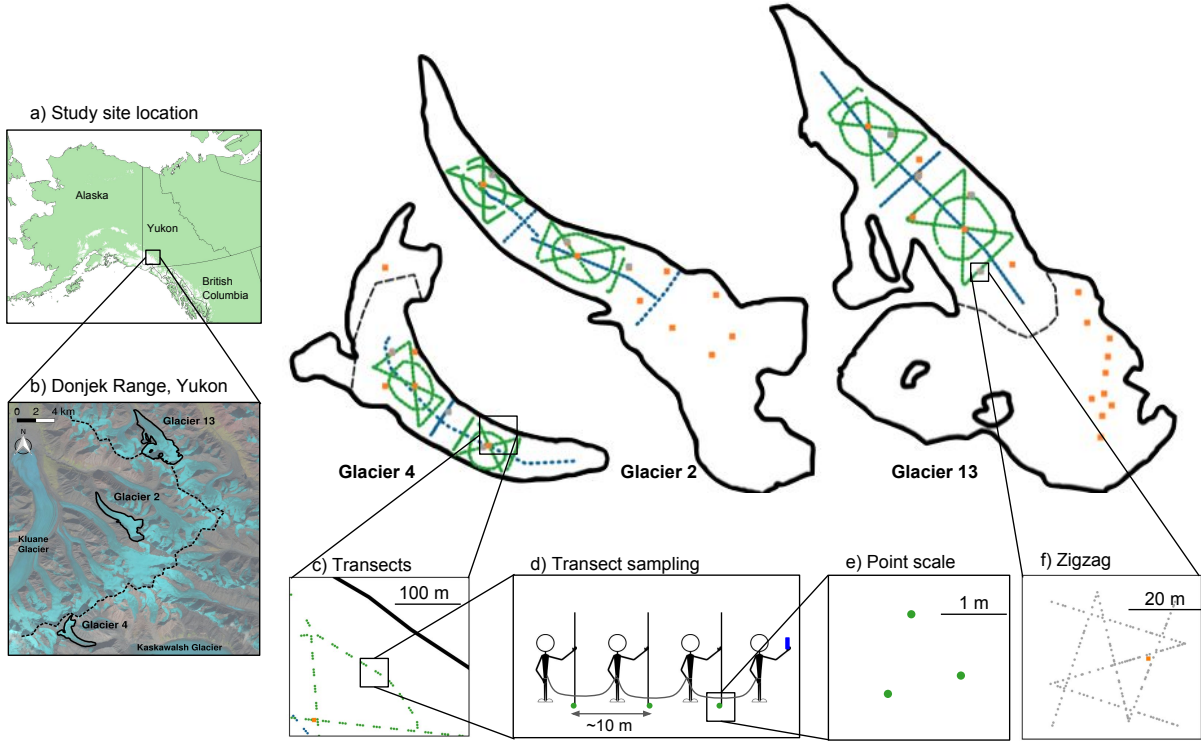
Fig. 1. Study area location and sampling design for Glaciers 4, 2 and 13. (a) The study region is located in the Donjek Range of the St. Elias Mountains of Yukon, Canada. (b) Study glaciers are located along a SW-NE transect through the Donjek Range. The local topographic divide is shown as a dashed line. Imagery from ??. (c) Details of the snow survey sampling design. Centreline and transverse transects are shown in blue dots, hourglass and circle design are shown in green dots. Orange squares are locations of snow density measurements. Arrows indicate glacier flow direction and the approximate location of each ELA is shown as a black dashed line. (d) Linear and curvilinear transects typically consist of sets of three measurement locations, (e) spaced ~10 m apart. (f) At each location, three snow-depth measurements are made. (f) Linear-random snow-depth measurements in 'zigzag' design are shown as grey dots.

Table 2. Description of density interpolation methods used to calculate SWE used in the topographic regression. Abbreviations with 'S' used snowpit-derived densities and abbreviations with an 'F' used Federal Sampler-derived densities.

| | Snow density source | | Estimation method |
	Snowpit	*Federal Sampler*	
S1	■		Mean of all glaciers
F1		■	
S2	■		Glacier mean
F2		■	
S3	■		Linear regression of elevation and density for each glacier
F3		■	
S4	■		Inverse distance weighted mean
F4		■	

Gridcell average SWE

We average SWE values within each DEM-aligned gridcell (40×40 m). The locations of measurements have considerable uncertainty both from the error of the GPS unit ($2.7 - 4.6$ m) and the estimation of observer location based on the GPS unit. These errors could easily result in the incorrect assignment of a SWE measurement to a certain gridcell but this source of variability was not further investigated because we assume that SWE variability is captured in the zigzag measurements described below. There are no significant differences between observers ($p > 0.05$), with the exception of the first transect on Glacier 4. No corrections to the data based on observer differences are applied.

Distributed SWE

Linear regression

SWE are interpolated and extrapolated for each glacier using linear regression (LR) as well as simple kriging (SK). Linear regressions relate observed SWE to gridcell values of DEM-derived topographic parameters (**?**). We choose to include elevation, distance from centreline, slope, aspect, curvature, "northness" and a wind redistribution parameter in the LR. Our sampling design ensured that the ranges of topographic parameters covered by the measurements represent more than 70% of the total area of each glacier (except for the elevation range on Glacier 2, which is 50%). For details on data and methods used to estimate the topographic parameters see the Supplementary Material. Topographic parameters are weighted by a set of fitted regression coefficients (β_i). Regression coefficients are calculated by minimizing the sum of squares of the

vertical deviations of each data point from the regression line (**?**). Snow depth data are highly variable so there is a possibility for the LR to fit to this data noise, a process known as overfitting. To prevent overfitting, cross-validation and model averaging are implemented (see Supplementary Material). The distributed estimate of SWE is found by using regression coefficients to estimate SWE at each gridcell. Specific winter balance is calculated as the aerially-averaged, integrated SWE for each glacier ([m w.e.]).

Simple kriging
Simple kriging (SK) estimates SWE values at unsampled locations by using the isotropic spatial correlation (covariance) of measured SWE to find a set of optimal weights (**??**). SK assumes that if sampling points are distributed throughout a surface, the degree of spatial correlation of the observed surface can be determined and the surface can then be interpolated between sampling points. We used the `DiceKriging` R package (**?**) to calculate the maximum likelihood covariance matrix, as well as range distance (θ) and nugget. The range distance is a measure of data correlation length and the nugget is the residual that encompasses sampling-error variance as well as the spatial variance at distances less than the minimum sample spacing (**?**).

Uncertainty analysis
To quantify effects of uncertainty on the winter balance estimate, we conduct a Monte Carlo experiment, which uses repeated random sampling to calculate a numerical solution (**?**). This random sampling process is done 1000 times, which results in a distribution of possible winter balance values based on uncertainty within the data processing steps. We quantify the effect of uncertainty as the standard deviation of the distribution. Three sources of uncertainty, which encompass error and uncertainty within each processing step, are considered: (1) density uncertainty, (2) SWE uncertainty and (3) interpolation uncertainty. Individual sources of uncertainty are propagated through the process of converting snow measurements to winter balance. Then, all three uncertainty sources are considered together and their combined effect on winter balance uncertainty is quantified.

SWE uncertainty (σ_{SWE})
To estimate winter balance, we must represent SWE within a gridcell with a single value despite the fact that each gridcell contains a distribution of SWE values. The resulting uncertainty from this SWE representation is characterized by generating a normal distribution, with a standard deviation equal to the mean standard deviation of all zigzags on each glacier. For each iteration of the Monte Carlo, a set of random values is generated from the distribution and added to the observed SWE values. These perturbed SWE values are then used to estimate winter balance. The winter balance uncertainty due to SWE uncertainty (σ_{SWE}) is calculated as the standard deviation of the resulting distribution of winter balance estimates.

Density uncertainty (σ_{ρ})
We incorporate uncertainty in interpolating density measurements by carrying forward all eight density interpolation options when estimating winter balance. The density measurement and interpolation methods used in our study encompass a broad spectrum of possible density values. The winter balance uncertainty due to density uncertainty (σ_{ρ}) is calculated as the standard deviation of winter balance estimates calculated using each density interpolation option.

Interpolation uncertainty (σ_{INT})
We represent the uncertainty in fitting an interpolation model to observed data in different ways for LR and SK. LR uncertainty is represented by obtaining a multivariate normal distribution of possible β_i values. The standard deviation of each distribution is calculated using the covariance of regression coefficients as outlined in **?**. The β_i distributions are randomly sampled and the new β_i values are used to estimate winter balance. SK uncertainty is derived from the 95% confidence interval SWE surfaces generated within the `DiceKriging` package. The standard deviation of each gridcell is then calculated from the confidence interval surfaces and the glacier wide standard deviation is found by taking the square root of the average variance. The distribution of winter balance values is centred at the SK winter balance estimate and has a standard deviation equal to the glacier wide standard deviation. For consistency, the standard deviation of winter balance values that result from either LR or SK interpolation uncertainty is referred to as σ_{INT}.

RESULTS AND DISCUSSION
Field measurements
Despite the lack of measurements in the accumulation area, especially along steep head walls, we observed a wide range of snow depth on all three study glaciers (Figure **??**). Glacier 4 has the highest mean snow depth and a high proportion of outliers, indicating a more variable snow depth overall. Glacier 13 has the lowest mean snow depth and a narrower distribution of observed values. At each measurement location, the median range of measured depths ($3 - 4$ points) as a percent of the mean depth at that location is 2%, 11%, and 12%, for Glaciers 4, 2 and 13, respectively.

Mean snow pit (SP) and Federal Sampler (FS) density values are within one standard deviation of each other for each glacier and over all three glaciers. The standard deviation of glacier-wide mean density is less than 10% of the mean density. However, FS densities have a larger range of values ($227 - 431\mathrm{kg\ m^{-3}}$) when compared to SP densities ($299 - 381\mathrm{kg\ m^{-3}}$). The mean SP densities are within one standard deviation between glaciers, whereas mean FS densities are not.

Co-located FS and SP measurements are not correlated and we find that FS density values are positively correlated with snow depth ($R^2 = 0.59$, p<0.01). This positive relationship could be a result of physical processes, such as compaction, but is more likely a result of measurement
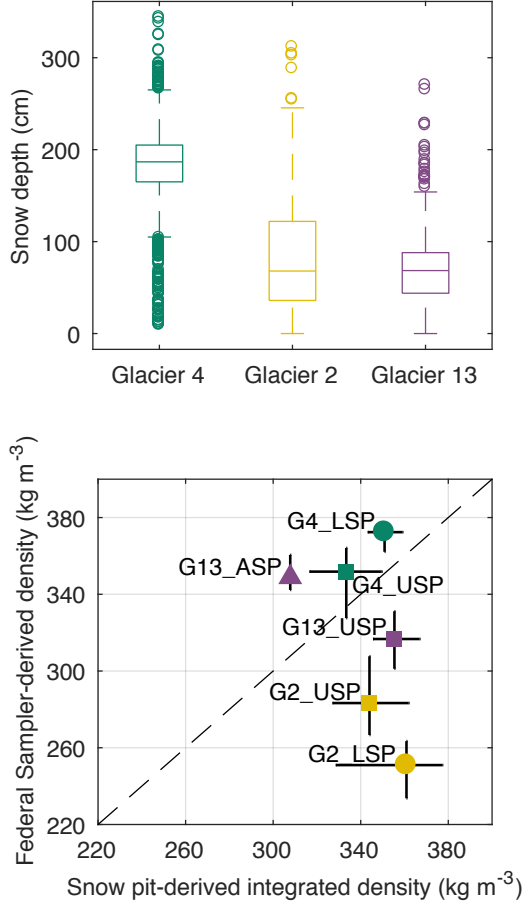
Fig. 2. (Left) Boxplot of measured snow depth on Glaciers 4, 2 and 13. The box shows first quartiles, the line within the box indicates data median, bars indicate minimum and maximum values (excluding outliers), and circles show outliers, which are defined as being outside of the range of 1.5 times the quartiles (approximately $\pm 2.7\sigma$). (Right) Comparison of integrated density estimated using wedge cutters in a snow pit and density estimated using Federal Sampler measurements for Glacier 4 (G04), Glacier 2 (G02) and Glacier 13 (G13). Snow pits were distributed in the accumulation area (ASP), upper ablation area (USP) and lower ablation area (LSP). Error bars are minimum and maximum values.

artefacts for a number of reasons. First, the range of densities measured by the Federal sampler is large and the extreme values seem unlikely to exist in our study region, which experiences a continental snow pack with minimal mid-winter melt events. Second, compaction effects would likely be small at these study glaciers because of the relatively shallow snow pack (deepest measurement was 340 cm). Third, no linear relationship exists between depth and SP density ($R^2 = 0.05$). Together, these findings indicate that the FS measurements have a bias which is challenging to correct for.

The FS appears to oversample in deep snow and undersample in shallow snow. Oversampling by small diameter (area of 10–12 cm^2) sampling tubes has been observed in previous studies, with a percent error between +6.8% and 11.8% (e.g. **???**). Studies that use Federal Samplers often apply a 10% correction to all measurements (e.g. **?**). Oversampling has been attributed to slots "shaving" snow into the tube as it is rotated (e.g. **?**) and to snow falling into the slots, particularly when snow samples had densities greater than $400 \, \text{kg} \, \text{m}^{-3}$ and snow depth greater than 1 m (e.g. **?**). Undersampling is likely to occur due to snow falling out of the bottom of the sampler (**?**), which likely occurred in our study since a large portion of the lower elevation snow on both Glaciers 2 and 13 was melt affected and weak, allowing for easier lateral displacement of the snow as the sampler was extracted. Relatively poor FS spring scale sensitivity also made it difficult to obtain accurate measurements of small snow quantities.

Distributed density

Since we find no correlation between co-located SP and FS densities (Figure **??**), each set of density values is used for all four density interpolation options. Regional and glacier mean densities are higher when SP densities are used (see Supplementary Material Table **??**). Density gradient with elevation differs between SP and FS densities (see Supplementary Material Table **??**). At Glaciers 2 and 13, SP density decreases with elevation, likely indicating melt and/or compaction at lower elevations. SP density is independent of elevation on Glacier 4. FS density increases with elevation on Glacier 2 and there is no relationship with elevation on Glaciers 4 and 13. There is a positive linear relation between measured snow density and depth for all FS measurements but no correlation exists between SP density and elevation. Considering these results, of the four interpolation methods used our preferred method is a glacier-wide mean of SP densities. Many winter balance studies assume uniform density (e.g. **???**) and it is realistic for future studies to measure snow density profiles at a few locations in the study basin.

gridcell average

In an attempt to capture the spatial variability of SWE in a gridcell, we use a zigzag sampling scheme, which offers a relatively easy way to take a large number of probe measurements. The average standard deviation of all zigzags on Glacier 4 is $\sigma_{\text{G4ZZ}} = 0.027$ m w.e., on Glacier 2 is $\sigma_{\text{G2ZZ}} = 0.035$ m w.e. and on Glacier 13 is $\sigma_{\text{G13ZZ}} = 0.040$ m w.e. SWE measurements for each zigzag are not normally distributed about the mean SWE (Figure **??**). For simplicity, we assume uniform SWE uncertainty within gridcells across each glacier and represent this uncertainty by a normal distribution with the mean zigzag standard deviation for each glacier.

Each measured gridcell contains one to six measurements which are then averaged to give SWE gridcell average values. The distribution of grid-cell SWE values for each glacier is similar to that of Figure **??** but with fewer outliers. The zigzag standard deviation is almost two times larger than the mean standard deviation within gridcells measured along transects. However, a small number of gridcells sampled along transects have standard deviations that exceed 0.25 m w.e. We deem these values to be outliers but further work on the distribution of gridcell
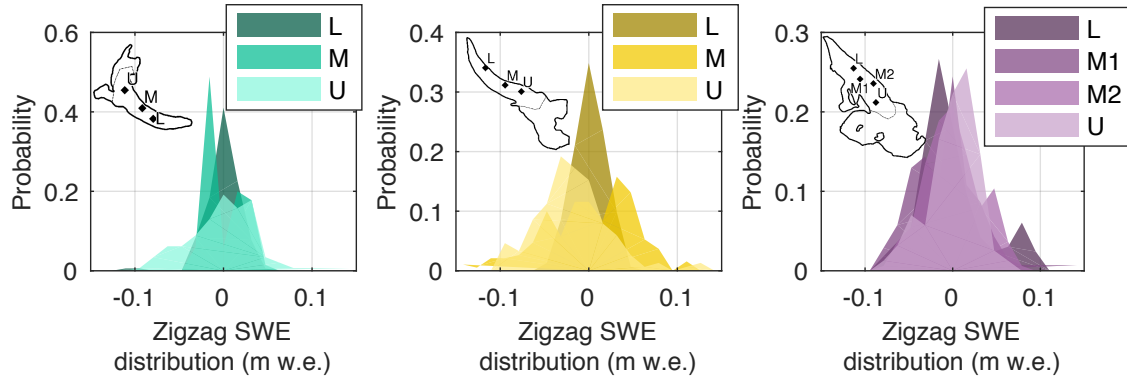
Fig. 3. Distribution of zigzag SWE values with the local mean subtracted on Glacier 4 (upper panel), Glacier 2 (middle panel) and Glacier 13 (lower panel). Zigzags are distributed throughout the ablation area of each glacier, with one located in the lower portion (L), one in the middle portion (M), and one in the upper portion (U). There were two zigzags in the middle ablation area of Glacier 13.
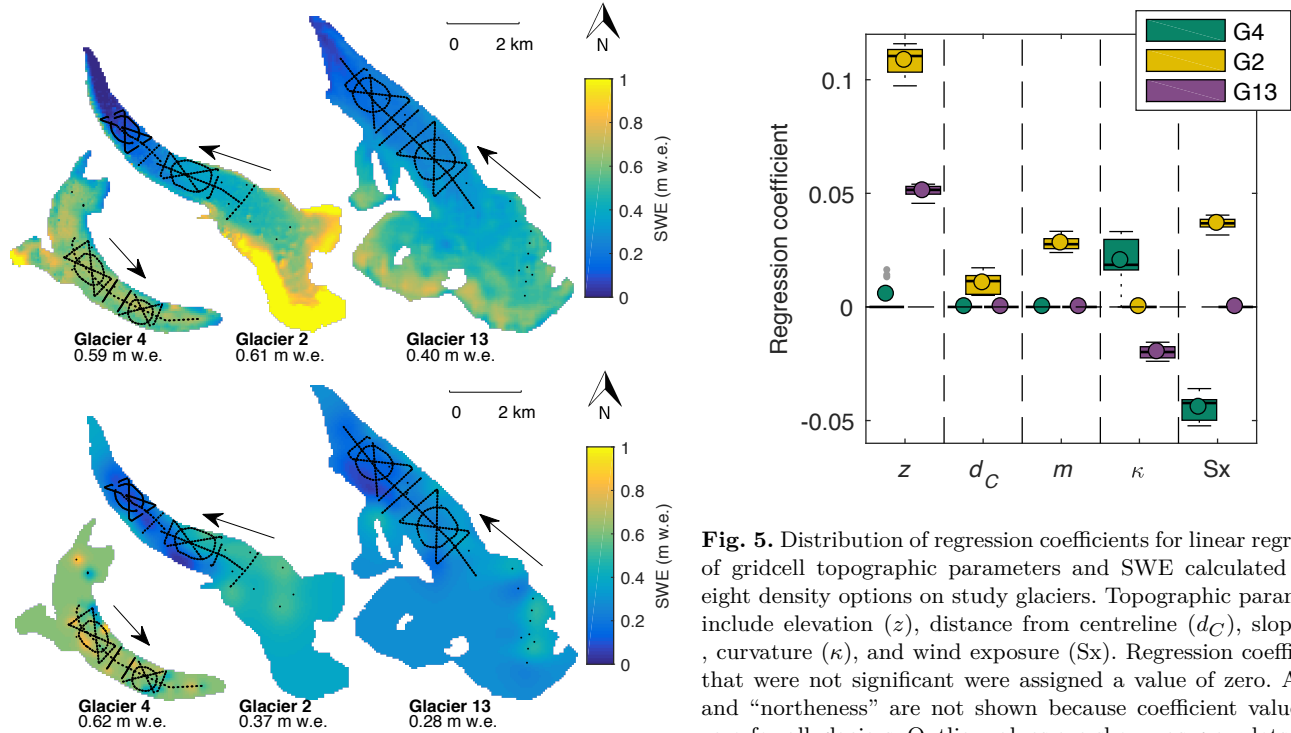

Fig. 5. Distribution of regression coefficients for linear regression of gridcell topographic parameters and SWE calculated using eight density options on study glaciers. Topographic parameters include elevation (z), distance from centreline (d_C), slope (m), curvature (κ), and wind exposure (Sx). Regression coefficients that were not significant were assigned a value of zero. Aspect and "northeness" are not shown because coefficient values are zero for all glaciers. Outlier values are shown as gray dots.

Fig. 4. Spatial distribution of SWE estimated using linear regression (upper) and simple kriging (lower). Grid-cell SWE observations are found using glacier wide mean snow pit density and are shown as black dots. Glacier flow directions are indicated by arrows. Specific winter balance values are also shown.

variability is needed. Therefore, we assume that the gridcell variability is captured with dense sampling in zigzag gridcells. Since gridcell variability is relatively easy to quantify using zigzags, there is little need to take multiple measurements within a gridcell along a transect. Instead, transect spacing can be decreased to allow for greater spatial extent of sampling, which would better capture basin-scale variability.

Interpolated SWE

The choice of interpolation method affects the specific winter balance (Table **??**). When using LR, the winter balance on Glaciers 4 and 2 are similar in magnitude. SK produces the highest winter balance on Glacier 4 and the lowest winter balance on Glacier 13. Winter balance estimated by SK is ∼30% lower than winter balance estimated by LR on Glaciers 2 and 13. However, when only the ablation area is considered, LR and SK produce winter balance estimates that differ by less than 7% for all glaciers. Extrapolation of observed SWE into the accumulation area appears to have a large effect on winter balance estimates. SWE estimated with LR and SK differ considerably in the

Table 3. Specific winter balance (WB [m w.e.]) estimated using linear regression and simple kriging interpolation for study glaciers. Average root mean squared error (RMSE [m w.e.]) between estimated and observed gridcells for all points, which were randomly selected and excluded from interpolation, is also shown. RMSE as a percent of the WB is shown in brackets.

	Linear Regression		Simple Kriging	
	WB	RMSE	WB	RMSE
G4	0.582	0.153 (26%)	0.616	0.134 (22%)
G2	0.577	0.102 (18%)	0.367	0.073 (20%)
G13	0.381	0.080 (21%)	0.271	0.068 (25%)

upper accumulation areas of Glaciers 2 and 13 (Figure **??**). The significant influence of elevation in the LR results in substantially higher SWE values at high elevation, whereas the accumulation area of the SK estimates approximate the mean observed SWE.

Linear Regression
Analysis of topographic parameters reveals that elevation is the most significant predictor for Glacier 2 and 13, while wind distribution is the most significant predictor for Glacier 4 (Figure **??**). Elevation, as the predictor, is positively correlated with SWE, meaning that gridcells at higher elevation show higher SWE. While on Glacier 4 wind

Fig. 6. Uncertainty of SWE estimated using linear regression (top) and simple kriging (bottom). Uncertainty is a relative quantity measured by taking the sum of differences between one hundred estimates of distributed winter balance that include SWE uncertainty and, in the case of linear regression, regression uncertainty. The sum is then normalized for each glacier. Glacier flow directions are indicated by arrows.

distribution parameter is negative (i.e. negative correlation with SWE), which indicates less snow in 'sheltered' areas, on the other two glaciers wind distribution is positive. Similarly, curvature is positively correlated for Glacier 4 and negatively correlated for the other two glaciers. It is possible that the elevation correlation was accentuated, especially on Glacier 13, during the field campaign due to warmer than normal temperatures and an early (1–2 weeks) start to the melt season (Yukon Snow Survey Bulletin and Water Supply Forecast, May 1, 2016). The southwestern Yukon winter snow pack in 2015 was also well below average, possibly emphasizing effects of early melt onset.

Our mixed insights into dominant predictors of accumulation are consistent with the conflicting results present in the literature. Many winter balance studies have found elevation to be the most significant predictor of SWE (e.g. **??**). However, accumulation elevation gradients vary considerably between glaciers (e.g. **?**) and other factors, such as orientation relative to dominant wind direction and glacier shape, have been noted to affect accumulation distribution (**??**).There are also a number of accumulation studies on glaciers that found no significant correlation between accumulation and topographic parameters and the highly variable snow distribution was attributed to complex local conditions (e.g. **??**).

Wind redistribution and preferential deposition of snow is known to have a large influence on accumulation at sub-basin scales (e.g. **???**). Our results indicate that wind likely has an impact on snow distribution but that the wind redistribution parameter may not adequately represent this impact. For example, Glacier 4 is located in a curved valley with steep side walls so having a single cardinal direction for wind may be inappropriate. Further, the scale of deposition may be smaller than the resolution of the Sx parameter estimated from our DEM. Our results corroborate **?**, who completed a winter balance study on six Alaskan glaciers (DEM resolutions of 5 m) and found that Sx was the only other significant parameter, besides elevation, for all glaciers. Regression coefficients were small (< 0.3) and in some cases, negative. Sublimation from blowing snow has also been shown to be an important mass loss from ridges (e.g. **?**). Incorporating snow loss as well as redistribution and preferential deposition may be needed for accurate representations of seasonal accumulation.

Since we are unable to measure SWE in gridcells that have high topographic parameter values, we must linearly extrapolate relationships. The accumulation area, where there are few observations, is most susceptible to extrapolation errors (Figure **??**). This area typically also has the highest SWE values (Figure **??**), affecting the specific winter balance estimated for the glacier. In our study, the dependence of SWE on elevation, especially on Glacier 2, means that LR extrapolation results in almost 2 m w.e. estimated in the parts of the accumulation area. This exceptionally large estimate of SWE is unlikely for a continental snow pack. Extrapolating a LR that is fitted to predominantly ablation area SWE values is likely erroneous.

While a LR can be used to predict distributed SWE in other basins, we found that transfer of LR coefficients between glaciers results in large estimation error. The lowest
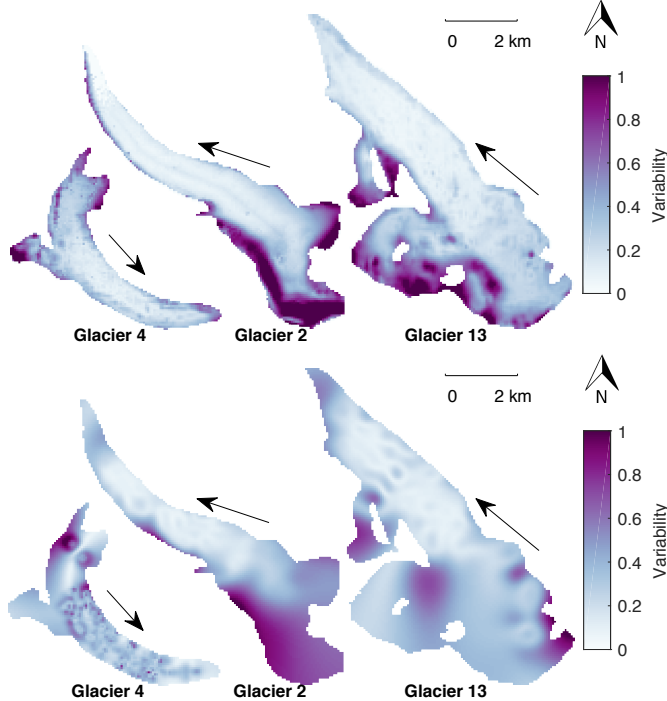
Table 4. Standard deviation ($[\times 10^{-2}$ m w.e.]) of winter balance distributions arising from SWE (σ_{SWE}), density (σ_ρ) and interpolation (σ_{INT}) uncertainty. Result for Glacier 4 (G4), Glacier 2 (G2) and Glacier 13 (G13) are shown.

	Linear Regression			Simple Kriging		
	σ_ρ	σ_{SWE}	σ_{INT}	σ_ρ	σ_{SWE}	σ_{INT}
G4	1.90	0.86	2.13	2.15	0.85	14.05
G2	3.37	1.80	3.09	2.03	2.53	13.78
G13	1.68	1.12	2.80	1.27	1.15	9.65

overall root mean squared error (0.2051 m w.e.) results from calculating a LR using all available observations. Our results are consistent with **?**, who found that local statistical models are able to perform well but they cannot be transferred to different regions and that regional-scale models are not able to explain the majority of variance. The inter-basin variability in our study range is greater than the intra-basin variability.

Simple kriging

For all study glaciers, simple kriging (SK) is a better predictor of observed SWE than LR (Figure **??** and Table **??**). However, the winter balance uncertainty that arises from using SK is large, and unrealistic values of 0 m w.e. winter balance can be estimated. Our observations are generally limited to the ablation area so SK estimates an almost uniform distribution of SWE in the accumulation areas of the study glaciers, which is inconsistent with observations described in the literature (e.g. **??**). Extrapolation using SK leads to large uncertainty (Figure **??**) in estimating winter balance, which further emphasis the need for spatially distributed SWE observations in a glacierized basin.

SK cannot be used to understand physical processes that may be controlling snow distribution and cannot be used to estimate accumulation beyond the study area. However, fitted kriging parameters, including the nugget and spatial correlation length, can provide insight into important scales of variability. Glaciers 2 and 13 have longer correlation lengths and smaller nuggets indicating variability at large scales (see Supplementary Material Table **??**). Conversely, Glacier 4 has a short correlation length and large nugget, indicating that accumulation variability occurs at small scales.

Uncertainty analysis

Specific winter balance is affected by uncertainty introduced when interpolating density (σ_ρ), when calculating gridcell SWE values (σ_{SWE}), and when interpolating observations (σ_{INT}). We find that when using LR and SK, interpolation uncertainty has a larger effect on winter balance uncertainty than density uncertainty or SWE uncertainty. The distribution of winter balance values that arises from SWE uncertainty is much narrower than the distribution that arises from interpolation uncertainty (Figure **??** and Table **??**).

A large contributor to uncertainty arises from extrapolation beyond the sampled region, which results in high uncertainty in estimated SWE in the accumulation area

(Figure **??**). The winter balance distributions obtained using LR and SK overlap for each glacier but the distribution modes differ. SK generally estimating lower winter balance in the accumulation area, which lowers the overall winter balance estimate. It is important to note that although the distributions from LR are narrower than those from SK, that does not necessitate that LR is a more accurate method of estimating winter balance. Based on the sources of uncertainty chosen, LR appears to be more precise than SK but the methods of calculating interpolation uncertainty are different so the distributions should not be directly compared.

SWE uncertainty is the smallest contributor to winter balance uncertainty. Therefore, obtaining the most accurate value of SWE to represent a gridcell, even a relatively large gridcell, does not need to be a priority when designing a snow survey. Many parts of a glacier are characterized by a relatively smooth surface, with roughness lengths on the order of centimetres (e.g. **?**), resulting in low SWE uncertainty. However, we assume that the sampled gridcells are representative of the uncertainty across the entire glacier, which is likely not true for areas with debris cover, crevasses and steep slopes.

Density, SWE, and interpolation uncertainty all contribute to spatial patterns of winter balance uncertainty (Figure **??**). For both LR and SK, the greatest uncertainty in estimated SWE occurs in the accumulation area. When LR is used, estimated SWE is highly sensitive to the elevation regression parameter. In the case of SK, uncertainty is greatest in areas far from observed SWE, which consist of the upper accumulation area on Glaciers 2 and 13. Uncertainty is greatest on Glacier 4 when LR interpolation is used at the upper edges of the accumulation area, which correspond to the locations with extreme values of the wind redistribution parameter. When SK is used for interpolation on Glacier 4, uncertainty is greatest at the measured gridcells, which highlights the short correlation length and the significant effect of density interpolation on the SK SWE estimate.

Using a Monte Carlo experiment to propagate uncertainty allowed us to quantify effects of uncertainty on estimates of winter balance. However, our analysis did not include uncertainty arising from a number of data sources, which we assumed to contribute negligibly to the uncertainty in winter balance or to be encompassed by investigated sources of uncertainty. These sources of uncertainty include error associated with SP and FS density measurement, DEM vertical and horizontal error and error associated with estimating measurement locations.

Mountain range accumulation gradient

An accumulation gradient is observed for the continental side of the St. Elias Mountains (Figure **??**). Accumulation data are compiled from **?**, the three glaciers presented in this paper, as well as two snow pits we dug near the head of the Kaskawulsh Glacier in May 2016. The data show a linear decrease in observed SWE as distance from the main mountain divide (identified by **?**) increases, with a gradient of -0.024 m w.e. km^{-1}. While the three study glaciers fit the regional relationship, the same relationship
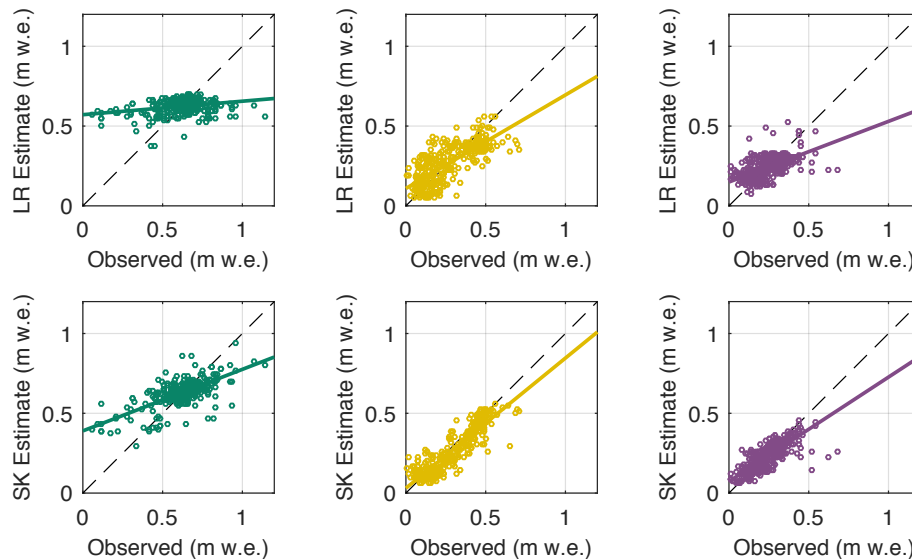
Fig. 7. Estimated gridcell SWE found using linear regression (LR) and simple kriging (SK) plotted against observed values of SWE on Glacier 4 (left), Glacier 2 (middle) and Glacier 13 (right). Line of best fit between estimated and observed SWE is also plotted.

would not apply when just the Donjek Range is considered. Therefore, glacier location within a mountain range also affects glacier-wide winter balance. Interaction between meso-scale weather patterns and mountain topography is a major driver of glacier-wide accumulation. Further insight into mountain-scale accumulation trends can be achieved by investigating moisture source trajectories and orographic precipitation contribution to accumulation.

Limitations and future work

Extensions to this work could include an investigation of experimental design, examining the effects of DEM grid size on winter balance and resolving temporal variability. Our sampling design was chosen to extensively sample the ablation area and is likely too finely resolved for many future mass balance surveys to replicate. Determining a sampling design that minimizes error and reduces the number of measurements, known as data efficiency thresholds, would contribute to optimizing snow surveys in mountainous regions. For example, **?** concluded that $200 - 400$ observations are needed to obtain accurate and robust snow distribution models.

DEM gridcell size is known to significantly affect computed topographic parameters and the ability for a DEM to resolve important hydrological features (i.e. drainage pathways) in the landscape (**????**), which can have implications for calculating a LR that uses topographic parameters. **?** found that a 10 m gridcell size is an optimal compromise between increasing resolution and large data volumes. Further, the importance of topographic parameters in predicting SWE is correlated with DEM grid size (e.g. **??**). A decrease in spatial resolution of the DEM results in a decrease in the importance of curvature and an increase in the importance of elevation. A detailed and ground controlled DEM is therefore needed to identify the features that drive accumulation variability. Even with a

high resolution DEM, microtopography that creates small scale snow variability cannot be resolved. For example, the lower part of Glacier 2 has an undulating ice surface (on the order of 5 m horizontal and 0.5 m vertical) that results in large variability in snow depth.

Temporal variability in accumulation is not considered in our study. While this limits the extent of our conclusions, a number of studies have found temporal stability in spatial patterns of snow accumulation and that terrain-based model could be applied reliable between years (e.g. **?**). For example, **?** analyzed more than 40 years of accumulation recorded on two Norwegian glaciers and found that snow accumulation is spatially heterogeneous yet exhibits robust time stability in its distribution.

CONCLUSION

We estimate spatial accumulation patterns and specific winter balance for three glaciers (labelled as Glacier 2, Glacier 4 and Glacier 13) in the St. Elias mountains from extensive snow depth and density sampling. Our objectives are to (1) examine methods and uncertainties when moving from snow measurements to estimating winter balance and (2) show how snow variability, data error and our methodological choices interact to create uncertainty in our estimate of winter balance.

We find that the method used to interpolate observations has a large effect on winter balance estimates and its associated uncertainty. On Glacier 4, winter balance estimates are consistent between linear regression (LR) and simple kriging (SK) but both explain only a small portion of observed variance, highlighting that although the winter balance estimates are relatively precise they may not necessarily be accurate. On Glaciers 2 and 13, LR and SK are better able to estimate observed SWE values but winter balance estimates differ considerably between the
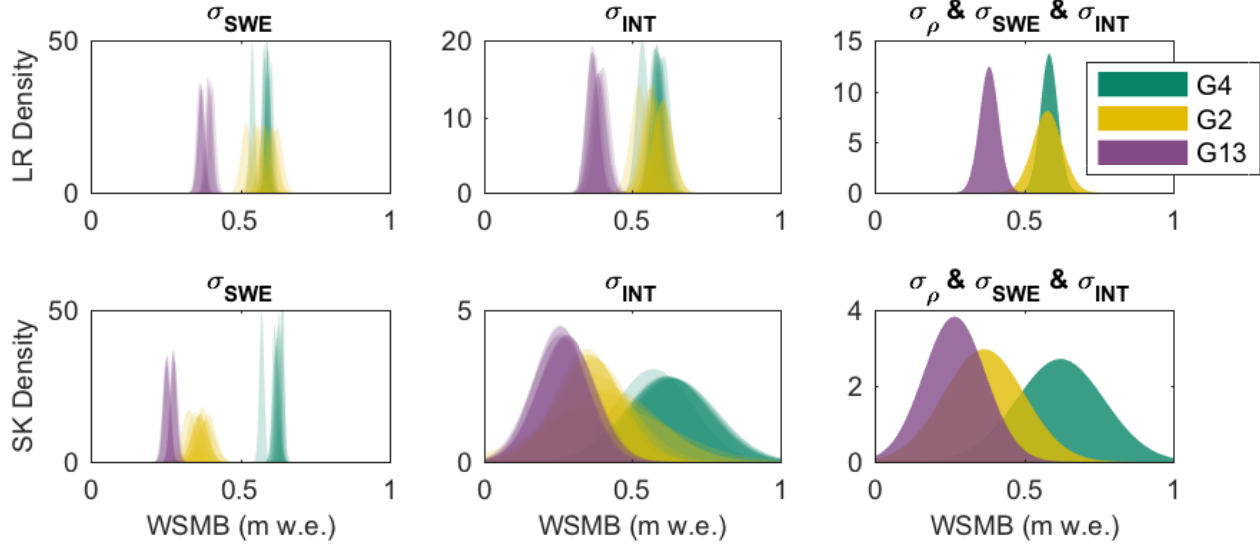
Fig. 8. Distributions of winter balance values that arise from (left) SWE uncertainty (σ_{SWE}), (middle) interpolation uncertainty (σ_{INT}) and (right) all three sources of uncertainty. Results from a linear regression interpolation (top panels) and simple kriging (bottom panels) are shown. Each distribution is calculated using one of eight density interpolation methods for Glacier 4 (G4), Glacier 2 (G2) and Glacier 13 (G13).
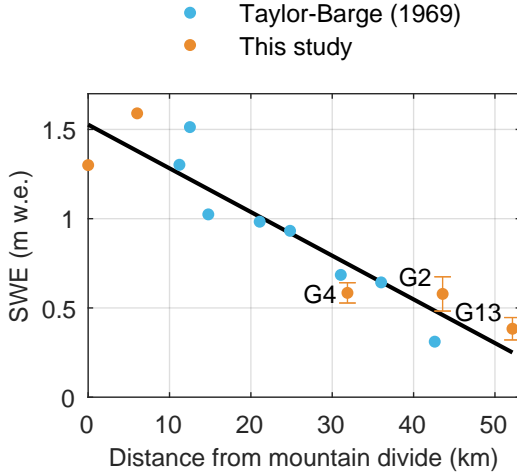

Fig. 9. Relation between SWE and linear distance from St. Elias mountain divide, located at the head of the Kaskawulsh Glacier. Blue dots are snow pit derived SWE values from **?**. Orange dots furthest from the divide are mean winter balance from Glaciers 4, 2 and 13, with 95% confidence interval using a linear regression interpolation. Orange dots close to the divide are snow pit derived SWE value at two locations in the accumulation area of the Kaskawulsh Glacier collect in May 2016. Black line indicates line of best fit ($R^2 = 0.85$).

two interpolation methods due to extrapolation into the accumulation area. SK is a non-parametric interpolation method that relies heavily on regular and dense sampling

so extrapolation is sensitive to marginal data values and the data mean. LR employs parameters that act as proxies for physical processes, which provides insight into drivers of SWE distribution, constrains extrapolation values and can be spatially transferred. It is therefore critical that future winter balance studies report which interpolation method is used to estimate winter balance, the ability for the model to estimate observed measurements and the uncertainty that results from fitting the interpolation model.

For our study glaciers, the total winter balance uncertainty ranges from 0.03 (8%) to 0.15 (54%) m w.e. depending primarily on the interpolation method. The smallest winter balance uncertainty source is the representation of gridcell SWE. Future studies could reduce winter balance uncertainty by increasing the spatial distribution of snow depth sampling rather than obtaining many measurements within a single gridcell. In our work, increased sampling within the accumulation area would better constrain SWE extrapolation and decrease uncertainty. Our results indicate that using extrapolated data to compare with winter balance estimates from remote sensing or modelling studies may produce misleading results. If possible, comparison studies should use observed SWE data rather than interpolated winter balance values.

Snow distribution patterns are found to differ considerably between glaciers, highlighting strong intra- and inter-basin variability and accumulation drivers acting on multiple scales. SWE distribution on Glacier 4 is highly variable, as indicated by shorter range distance, higher nugget value and lower explained variance. Glaciers 2 and 13 have lower SWE variability and elevation is the primary control of observed variation. Despite challenges in accurately estimating winter balance, our data are consistent with a previously reported linear decrease in

SWE with increased distance from the main topographic divide along the continental side of the St. Elias Mountains. This trend indicates that glacier location within a mountain range has a large influence on winter balance.

References

Anderton S, White S and Alvera B (2004) Evaluation of spatial variability in snow water equivalent for a high mountain catchment. *Hydrological Processes*, **18**(3), 435–453 (doi: 10.1002/hyp.1319)

Bagos PG and Adam M (2015) On the Covariance of Regression Coefficients. *Open Journal of Statistics*, **5**(07), 680 (doi: 10.4236/ojs.2015.57069)

Balk B and Elder K (2000) Combining binary decision tree and geostatistical methods to estimate snow distribution in a mountain watershed. *Water Resources Research*, **36**(1), 13–26 (doi: 10.1029/1999WR900251)

Barry RG (1992) *Mountain weather and climate*. Psychology Press

Beacount RT and Work RA (1963) Snow sampling results from three sampler. *International Association of Scientific Hydrology. Bulletin*, **8**(4), 74–78 (doi: 10.1080/02626666309493359)

Bernhardt M, Zängl G, Liston G, Strasser U and Mauser W (2009) Using wind fields from a high-resolution atmospheric model for simulating snow dynamics in mountainous terrain. *Hydrological processes*, **23**(7), 1064–1075 (doi: 10.1002/hyp.7208)

Berthier E, Arnaud Y, Kumar R, Ahmad S, Wagnon P and Chevallier P (2007) Remote sensing estimates of glacier mass balances in the Himachal Pradesh (Western Himalaya, India). *Remote Sensing of Environment*, **108**(3), 327–338

Blöschl G, Kirnbauer R and Gutknecht D (1991) Distributed snow melt simulations in an alpine catchment. *Water Resources Research*, **27**(12), 3171–3179

Burnham KP and Anderson DR (2004) Multimodel Inference: Understanding AIC and BIC in Model Selection. *Sociological Methods & Research*, **33**(2), 261–304 (doi: 10.1177/0049124104268644)

Clark MP, Hendrikx J, Slater AG, Kavetski D, Anderson B, Cullen NJ, Kerr T, Örn Hreinsson E and Woods RA (2011) Representing spatial variability of snow water equivalent in hydrologic and land-surface models: A review. *Water Resources Research*, **47**(7) (doi: 10.1029/2011WR010745)

Clarke GK, Collins SG and Thompson DE (1984) Flow, thermal structure, and subglacial conditions of a surge-type glacier. *Canadian Journal of Earth Sciences*, **21**(2), 232–240 (doi: 10.1139/e84-024)

Clyde GD (1932) Circular No. 99-Utah Snow Sampler and Scales for Measuring Water Content of Snow

Cogley J, Hock R, Rasmussen L, Arendt A, Bauder A, Braithwaite R, Jansson P, Kaser G, Möller M, Nicholson L and others (2011) Glossary of glacier mass balance and related terms

Conger SM and McClung DM (2009) Comparison of density cutters for snow profile observations. *Journal of Glaciology*, **55**(189), 163–169

Crompton JW and Flowers GE (2016) Correlations of suspended sediment size with bedrock lithology and glacier dynamics. *Annals of Glaciology*, 1–9 (doi: 10.1017/aog.2016.6)

Cullen NJ, Anderson B, Sirguey P, Stumm D, Mackintosh A, Conway JP, Horgan HJ, Dadic R, Fitzsimons SJ and Lorrey A (2017) An 11-year record of mass balance of Brewster Glacier, New Zealand, determined using a geostatistical approach. *Journal of Glaciology*, **63**(238), 199–217 (doi: 10.1017/jog.2016.128)

Dadic R, Mott R, Lehning M and Burlando P (2010) Parameterization for wind-induced preferential deposition of snow. *Journal of Geophysical Research: Earth Surface (2003–2012)*, **115** (doi: 10.1029/2009JF001261)

Danby RK, Hik DS, Slocombe DS and Williams A (2003) Science and the St. Elias: an evolving framework for sustainability in North America's highest mountains. *The Geographical Journal*, **169**(3), 191–204 (doi: 10.1111/1475-4959.00084)

Davis JC and Sampson RJ (1986) *Statistics and data analysis in geology*, volume 646. Wiley New York et al.

Deems JS and Painter TH (2006) Lidar measurement of snow depth: accuracy and error sources. In *Proceedings of the International Snow Science Workshop*, 1–6

Dixon D and Boon S (2012) Comparison of the SnowHydro snow sampler with existing snow tube designs. *Hydrological Processes*, **26**(17), 2555–2562, ISSN 1099-1085 (doi: 10.1002/hyp.9317)

Egli L, Griessinger N and Jonas T (2011) Seasonal development of spatial snow-depth variability across different scales in the Swiss Alps. *Annals of Glaciology*, **52**(58), 216–222 (doi: 10.3189/172756411797252211)

Elder K, Dozier J and Michaelsen J (1991) Snow accumulation and distribution in an alpine watershed. *Water Resources Research*, **27**(7), 1541–1552 (doi: 10.1029/91WR00506)

Elder K, Rosenthal W and Davis RE (1998) Estimating the spatial distribution of snow water equivalence in a montane watershed. *Hydrological Processes*, **12**(1011), 1793–1808 (doi: 10.1002/(SICI)1099-1085(199808/09)12:10/11¡1793::AID-HYP695¿3.0.CO;2-)

Erickson TA, Williams MW and Winstral A (2005) Persistence of topographic controls on the spatial distribution of snow in rugged mountain terrain, Colorado, United States. *Water Resources Research*, **41**(4) (doi: 10.1029/2003WR002973)

Erxleben J, Elder K and Davis R (2002) Comparison of spatial interpolation methods for estimating snow distribution in the Colorado Rocky Mountains. *Hydrological Processes*, **16**(18), 3627–3649 (doi: 10.1002/hyp.1239)

Fames PE, Peterson N, Goodison B and Richards RP (1982) Metrication of Manual Snow Sampling Equipment. In *Proceedings of the 50th Western Snow Conference*, 120–132

Fierz C, Armstrong RL, Durand Y, Etchevers P, Greene E, McClung DM, Nishimura K, Satyawali PK and Sokratov SA (2009) *The international classification for seasonal snow on the ground*, volume 25. UNESCO/IHP Paris

Garbrecht J and Martz L (1994) Grid size dependency of parameters extracted from digital elevation models. *Computers & Geosciences*, **20**(1), 85–87, ISSN 0098-3004 (doi: 10.1016/0098-3004(94)90098-1)

Godio A and Rege R (2016) Analysis of georadar data to estimate the snow depth distribution. *Journal of Applied Geophysics*, **129**, 92–100 (doi: 10.1016/j.jappgeo.2016.03.036)

Grabiec M, Puczko D, Budzik T and Gajek G (2011) Snow distribution patterns on Svalbard glaciers derived from radio-echo soundings. *Polish Polar Research*, **32**(4), 393–421 (doi: 10.2478/v10183-011-0026-4)

Gray DM and Male DH (1981) *Handbook of snow: principles, processes, management & use.* Pergamon Press

Grunewald T, Schirmer M, Mott R and Lehning M (2010) Spatial and temporal variability of snow depth and ablation rates in a small mountain catchment. *Cryosphere*, **4**(2), 215–225 (doi: 10.5194/tc-4-215-2010)

Grünewald T, Stötter J, Pomeroy J, Dadic R, Moreno Baños I, Marturià J, Spross M, Hopkinson C, Burlando P and Lehning M (2013) Statistical modelling of the snow depth distribution in open alpine terrain. *Hydrology and Earth System Sciences*, **17**(8), 3005–3021 (doi: 10.5194/hess-17-3005-2013)

Grünewald T, Bühler Y and Lehning M (2014) Elevation dependency of mountain snow depth. *The Cryosphere*, **8**(6), 2381–2394 (doi: 10.5194/tc-8-2381-2014)

Guo-an T, Yang-he H, Strobl J and Wang-qing L (2001) The impact of resolution on the accuracy of hydrologic data derived from DEMs. *Journal of Geographical Sciences*, **11**(4), 393–401, ISSN 1861-9568 (doi: 10.1007/BF02837966)

Gusmeroli A, Wolken GJ and Arendt AA (2014) Helicopter-borne radar imaging of snow cover on and around glaciers in Alaska. *Annals of Glaciology*, **55**(67), 78–88 (doi: 10.3189/2014AoG67A029)

Helbig N and van Herwijnen A (2017) Subgrid parameterization for snow depth over mountainous terrain from flat field snow depth. *Water Resources Research*, **53**(2), 1444–1456, ISSN 0043-1397 (doi: 10.1002/2016WR019872)

Hock R (2005) Glacier melt: a review of processes and their modelling. *Progress in Physical Geography*, **29**(3), 362–391 (doi: 10.1191/0309133305pp453ra)

Hock R and Jensen H (1999) Application of kriging interpolation for glacier mass balance computations. *Geografiska Annaler: Series A, Physical Geography*, **81**(4), 611–619 (doi: 10.1111/1468-0459.00089)

Hofierka J, Mitášová H and Neteler M (2009) Geomorphometry in GRASS GIS. *Developments in Soil Science*, **33**, 387–410 (doi: 10.1016/S0166-2481(08)00017-2)

Kaser G, Fountain A, Jansson P and others (2003) *A manual for monitoring the mass balance of mountain glaciers.* Unesco Paris

Kienzle S (2004) The Effect of DEM Raster Resolution on First Order, Second Order and Compound Terrain Derivatives. *Transactions in GIS*, **8**(1), 83–111, ISSN 1467-9671 (doi: 10.1111/j.1467-9671.2004.00169.x)

Kirchner PB, Bales RC, Molotch NP, Flanagan J and Guo Q (2014) LiDAR measurement of seasonal snow accumulation along an elevation gradient in the southern Sierra Nevada, California. *Hydrology and Earth System Sciences*, **18**(10), 4261–4275, ISSN 1027-5606

Kohavi R and others (1995) A study of cross-validation and bootstrap for accuracy estimation and model selection. In *Proceedings of the Fourteenth International Joint Conference on Artificial Intelligence*, volume 14, 1137–1145

Korona J, Berthier E, Bernard M, Rémy F and Thouvenot E (2009) SPIRIT SPOT 5 stereoscopic survey of Polar Ice: Reference images and topographies during the fourth International Polar Year (2007–2009). *ISPRS Journal of Photogrammetry and Remote Sensing*, **64**(2), 204–212

Lehning M, Völksch I, Gustafsson D, Nguyen TA, Stähli M and Zappa M (2006) ALPINE3D: a detailed model of mountain surface processes and its application to snow hydrology. *Hydrological processes*, **20**(10), 2111–2128

Lehning M, Löwe H, Ryser M and Raderschall N (2008) Inhomogeneous precipitation distribution and snow transport in steep terrain. *Water Resources Research*, **44**(7) (doi: 10.1029/2007WR006545)

Li J and Heap AD (2008) A review of spatial interpolation methods for environmental scientists No. Record 2008/23. *Geoscience Australia*

Liston GE and Elder K (2006) A distributed snow-evolution modeling system (SnowModel). *Journal of Hydrometeorology*, **7**(6), 1259–1276 (doi: 10.1175/JHM548.1)

López-Moreno J, Latron J and Lehmann A (2010) Effects of sample and grid size on the accuracy and stability of regression-based snow interpolation methods. *Hydrological Processes*, **24**(14), 1914–1928, ISSN 1099-1085 (doi: 10.1002/hyp.7564)

López-Moreno J, Fassnacht S, Heath J, Musselman K, Revuelto J, Latron J, Morán-Tejeda E and Jonas T (2013) Small scale spatial variability of snow density and depth over complex alpine terrain: Implications for estimating snow water equivalent. *Advances in Water Resources*, **55**, 40–52, ISSN 0309-1708 (doi: 10.1016/j.advwatres.2012.08.010), snow–Atmosphere Interactions and Hydrological Consequences

López-Moreno JI, Fassnacht S, Beguería S and Latron J (2011) Variability of snow depth at the plot scale: implications for mean depth estimation and sampling strategies. *The Cryosphere*, **5**(3), 617–629 (doi: 10.5194/tc-5-617-2011)

MacDougall AH and Flowers GE (2011) Spatial and temporal transferability of a distributed energy-balance glacier melt model. *Journal of Climate*, **24**(5), 1480–1498 (doi: 10.1175/2010JCLI3821.1)

Machguth H, Eisen O, Paul F and Hoelzle M (2006) Strong spatial variability of snow accumulation observed with helicopter-borne GPR on two adjacent Alpine glaciers. *Geophysical Research Letters*, **33**(13) (doi: 10.1029/2006GL026576)

Madigan D and Raftery AE (1994) Model Selection and Accounting for Model Uncertainty in Graphical Models Using Occam's Window. *Journal of the American Statistical Association*, **89**(428), 1535–1546, ISSN 01621459

Marshall HP, Koh G, Sturm M, Johnson J, Demuth M, Landry C, Deems J and Gleason J (2006) Spatial vari-

ability of the snowpack: Experiences with measurements at a wide range of length scales with several different high precision instruments. In *Proceedings ISSW*, 359–364

McGrath D, Sass L, O'Neel S, Arendt A, Wolken G, Gusmeroli A, Kienholz C and McNeil C (2015) End-of-winter snow depth variability on glaciers in Alaska. *Journal of Geophysical Research: Earth Surface*, **120**(8), 1530–1550 (doi: 10.1002/2015JF003539)

Metropolis N and Ulam S (1949) The Monte Carlo Method. *Journal of the American Statistical Association*, **44**(247), 335–341, ISSN 01621459

Mitášová H and Hofierka J (1993) Interpolation by regularized spline with tension: II. Application to terrain modeling and surface geometry analysis. *Mathematical Geology*, **25**(6), 657–669 (doi: 10.1007/BF00893172)

Molotch N, Colee M, Bales R and Dozier J (2005) Estimating the spatial distribution of snow water equivalent in an alpine basin using binary regression tree models: the impact of digital elevation data and independent variable selection. *Hydrological Processes*, **19**(7), 1459–1479 (doi: 10.1002/hyp.5586)

Mott R, Faure F, Lehning M, Löwe H, Hynek B, Michlmayer G, Prokop A and Schöner W (2008) Simulation of seasonal snow-cover distribution for glacierized sites on Sonnblick, Austria, with the Alpine3D model. *Annals of Glaciology*, **49**(1), 155–160 (doi: 10.3189/172756408787814924)

Musselman KN, Pomeroy JW, Essery RL and Leroux N (2015) Impact of windflow calculations on simulations of alpine snow accumulation, redistribution and ablation. *Hydrological Processes*, **29**(18), 3983–3999 (doi: 10.1002/hyp.10595)

Nolan M, Larsen C and Sturm M (2015) Mapping snow-depth from manned-aircraft on landscape scales at centimeter resolution using Structure-from-Motion photogrammetry. *The Cryosphere Discussions*, **9**, 333–381 (doi: 10.5194/tcd-9-333-2015)

Olaya V (2009) Basic land-surface parameters. *Developments in Soil Science*, **33**, 141–169

Paoli LD and Flowers GE (2009) Dynamics of a small surge-type glacier using one-dimensional geophysical inversion. *Journal of Glaciology*, **55**(194), 1101–1112 (doi: 10.3189/002214309790794850)

Raftery AE, Madigan D and Hoeting JA (1997) Bayesian Model Averaging for Linear Regression Models. *Journal of the American Statistical Association*, **92**(437), 179–191 (doi: 10.1080/01621459.1997.10473615)

Réveillet M, Vincent C, Six D and Rabatel A (2016) Which empirical model is best suited to simulate glacier mass balances? *Journal of Glaciology*, 1–16 (doi: 10.1017/jog.2016.110)

Roustant O, Ginsbourger D and Deville Y (2012) DiceKriging, DiceOptim: Two R packages for the analysis of computer experiments by kriging-based metamodeling and optimization. *Journal of Statistical Software*, **21**, 1–55

Schneiderbauer S and Prokop A (2011) The atmospheric snow-transport model: SnowDrift3D. *Journal of Glaciology*, **57**(203), 526–542 (doi: 10.3189/002214311796905677)

Shea C and Jamieson B (2010) Star: an efficient snow point-sampling method. *Annals of Glaciology*, **51**(54), 64–72 (doi: 10.3189/172756410791386463)

Sold L, Huss M, Hoelzle M, Andereggen H, Joerg PC and Zemp M (2013) Methodological approaches to infer end-of-winter snow distribution on alpine glaciers. *Journal of Glaciology*, **59**(218), 1047–1059 (doi: 10.3189/2013JoG13J015)

Tangborn WV, Krimmel RM and Meier MF (1975) A comparison of glacier mass balance by glaciological, hydrological and mapping methods, South Cascade Glacier, Washington. *International Association of Hydrological Sciences Publication*, **104**, 185–196

Taylor-Barge B (1969) The summer climate of the St. Elias Mountain region. Technical report, DTIC Document

Thibert E, Blanc R, Vincent C and Eckert N (2008) Instruments and Methods Glaciological and volumetric mass-balance measurements: error analysis over 51 years for Glacier de Sarennes, French Alps. *Journal of Glaciology*, **54**(186), 522–532

Trujillo E and Lehning M (2015) Theoretical analysis of errors when estimating snow distribution through point measurements. *The Cryosphere*, **9**(3), 1249–1264 (doi: 10.5194/tc-9-1249-2015)

Turcan J and Loijens H (1975) Accuracy of snow survey data and errors in snow sampler measurements. In *32nd Eastern Snow Conference*, 2–11

Walmsley APU (2015) Long-term observations of snow spatial distributions at Hellstugubreen and Gråsubreen, Norway

Watson FG, Anderson TN, Newman WB, Alexander SE and Garrott RA (2006) Optimal sampling schemes for estimating mean snow water equivalents in stratified heterogeneous landscapes. *Journal of Hydrology*, **328**(3), 432–452 (doi: 10.1016/j.jhydrol.2005.12.032)

Wechsler SP and Kroll CN (2006) Quantifying DEM Uncertainty and its Effect on Topographic Parameters. *Photogrammetric Engineering & Remote Sensing*, **72**(9), 1081–1090, ISSN 0099-1112

Wetlaufer K, Hendrikx J and Marshall L (2016) Spatial Heterogeneity of Snow Density and Its Influence on Snow Water Equivalence Estimates in a Large Mountainous Basin. *Hydrology*, **3**(1), 3 (doi: 10.3390/hydrology3010003)

Winstral A, Elder K and Davis RE (2002) Spatial snow modeling of wind-redistributed snow using terrain-based parameters. *Journal of Hydrometeorology*, **3**(5), 524–538

Winstral A, Marks D and Gurney R (2013) Simulating wind-affected snow accumulations at catchment to basin scales. *Advances in Water Resources*, **55**, 64–79, ISSN 0309-1708 (doi: 10.1016/j.advwatres.2012.08.011), snow–Atmosphere Interactions and Hydrological Consequences

Winther J, Bruland O, Sand K, Killingtveit A and Marechal D (1998) Snow accumulation distribution on Spitsbergen, Svalbard, in 1997. *Polar Research*, **17**, 155–164

Woo MK and Marsh P (1978) Analysis of Error in the Determination of Snow Storage for Small High Arctic Basins. *Journal of Applied Meteorology*, **17**(10), 1537–1541 (doi: 10.1175/1520-0450(1978)017¡1537:AOEITD¿2.0.CO;2)

Wood WA (1948) Project "Snow Cornice": the establishment of the Seward Glacial research station. *Arctic*, 107–112

Work R, Stockwell H, Freeman T and Beaumont R (1965) Accuracy of field snow surveys. Technical report

Zhang W and Montgomery DR (1994) Digital elevation model grid size, landscape representation, and hydrologic simulations. *Water Resources Research*, **30**(4), 1019–1028, ISSN 1944-7973 (doi: 10.1029/93WR03553)

SUPPLEMENTARY MATERIAL

Topographic parameters

First, cross-validation is used to obtain a set of β_i values that have greater predictive ability. We select 1000 random subsets (2/3 values) of the data to fit the LR and the remaining data (1/3 values) are used to calculate a root mean squared error (RMSE) (**?**). Regression coefficients resulting in the lowest RMSE are selected. Second, we use model averaging to take into account uncertainty when selecting predictors and to also maximize predictive ability (**?**). Models are generated by calculating a set of β_i for all possible combinations of predictors. Following a Bayesian framework, model averaging involves weighting all models by their posterior model probabilities (**?**). To obtain the final regression coefficients, the β_i values from each model are weighted according to the relative predictive success of the model, as assessed by the Bayesian Information Criterion (BIC) value (**?**). BIC penalizes more complex models, which further reduces the risk of overfitting.

Topographic parameters are easy to calculate proxies for physical processes, such as orographic precipitation, solar radiation effects, wind redistribution and preferential deposition. We derive all parameters (Table **??**) for our study from a SPOT-5 DEM (40×40 m) (**?**). Two DEMs are stitched together to encompass the Donjek Range. An iterative 3D-coregistration algorithm (**?**) is used to correct the horizontal (~ 2 m E, ~ 4 m N) and vertical (5.4 m) discrepancy between the two DEMs before stitching.

Visual inspection of the curvature fields calculated using the full DEM shows a noisy spatial distribution that did not vary smoothly. To smooth the DEM, various smoothing algorithms and window sizes are applied and the combination that produces the highest correlation between topographic parameters and SWE is chosen. Inverse-distance weighted, Gaussian and gridcell averaging smoothing all with window sizes of 3×3, 5×5, 7×7 and 9×9 are used. gridcell average smoothing with a 7×7 window resulted in the highest overall correlation between curvature (second derivative) and SWE as well as slope (first derivative) and SWE. We use the smoothed DEM to calculate curvature, slope, aspect and "northness".

Table 5. Description of topographic parameters used in the linear regression.

Topographic parameter	Definition	Calculation method	Notes	Source
Elevation (z)		Values taken directly from DEM		
Distance from centreline (d_C)		Minimum distance between the Easting and Northing of the north-west corner of each grid-cell and a manually defined centreline		
Slope (m)	Angle between a plane tangential to the surface (gradient) and the horizontal	`r.slope.aspect` module in GRASS GIS software run through QGIS		???
Aspect (α)	Dip direction of the slope	`r.slope.aspect` module in GRASS GIS software run through QGIS	$\sin(\alpha)$, a linear quantity describing a slope as north/south facing, is used in the regression	???
Mean curvature (κ)	Average of profile (direction of the surface gradient) and tangential curvature (direction of the contour tangent)	`r.slope.aspect` module in GRASS GIS software run through QGIS	mean-concave (positive values) terrain with relative accumulation and mean-convex (negative values) terrain with relative scouring	???
"Northness" (N)	-1 represents a vertical, south facing slope, a value of $+1$ represents a vertical, north facing slope, and a flat surface yields 0	Product of the cosine of aspect and sine of slope		?
Wind exposure/shelter parameter (Sx)		Executable obtained from Adam Winstral that follows the procedure outlined in ?	Calculation based on selecting a cell within a certain angle and distance from the cell of interest that has the greatest upward slope relative to the cell of interest	?

Table 6. Snow density values used for interpolating density based on snow pit (SP) densities and Federal Sampler (FS) densities. Four interpolation methods are chosen: (1) using a mean snow density for all three glaciers (Range mean density), (2) using a mean density for each glacier (Glacier mean density), (3) using a regression between density and elevation (Elevation regression), and (4) inverse-distance weighted mean density (not shown).

		SP density (kg m^{-3})	FS density (kg m^{-3})
Range mean density		342	316
Glacier mean density	G4	348	327
	G2	333	326
	G13	349	307
Elevation regression	G4	$0.03z + 274$	$-0.16z + 714$
	G2	$-0.14z + 659$	$0.24z - 282$
	G13	$-0.20z + 802$	$0.12z + 33$

Table 7. Range and nugget values for simple kriging interpolation

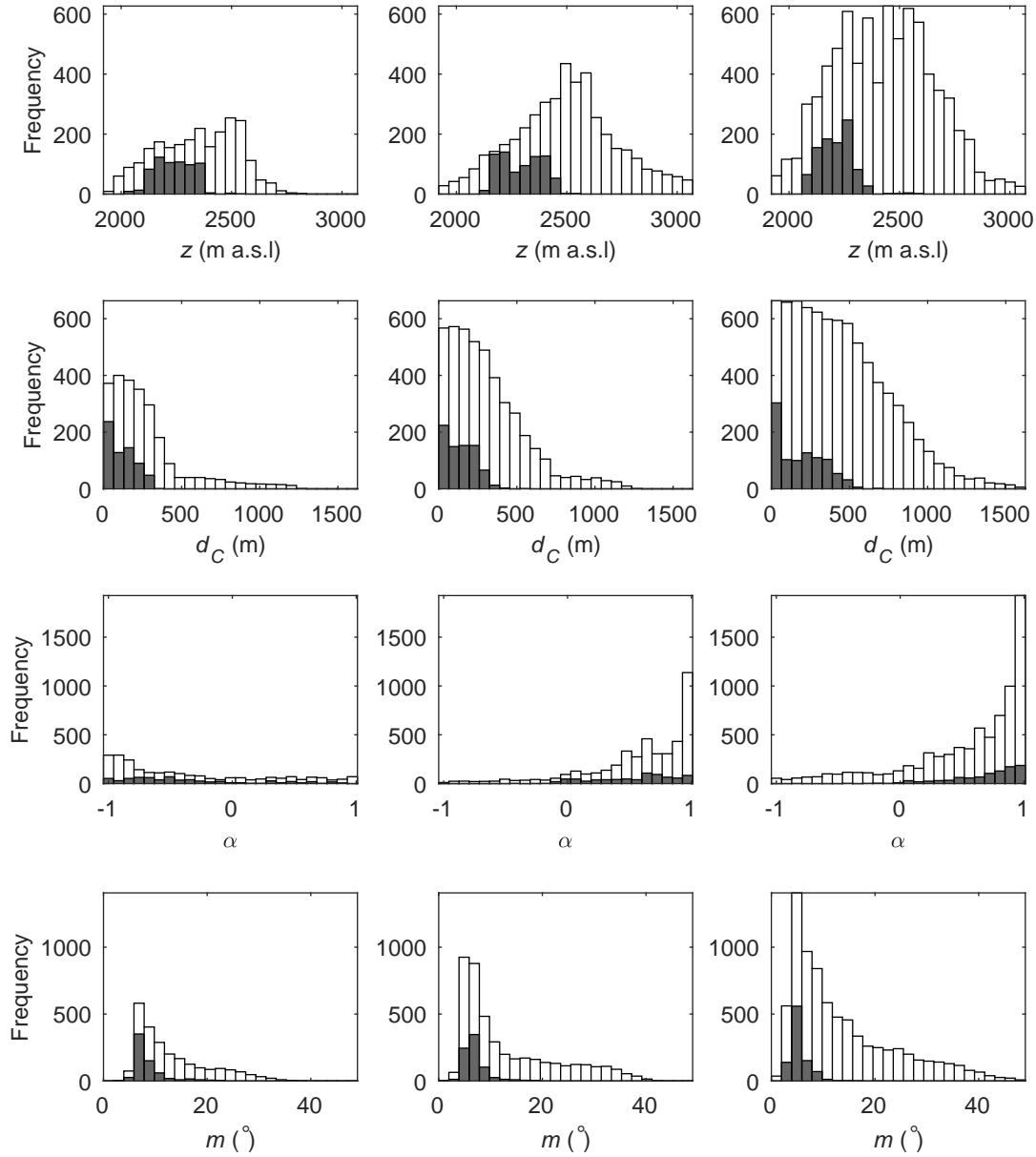|	Range (m)	Nugget ($\times 10^3$ m w.e.)
G4	90	10.5
G2	404	3.6
G13	444	4.8

Fig. 10. Distribution of topographic parameters over Glacier 4 (left), Glacier 2 (middle) and Glacier 13 (right) are shown in white. Distribution of topographic parameter values from sampled gridcells in shown in gray. Topographic parameters include elevation (z), distance from centreline (d_C), aspect (α), slope (m), northness (N), mean curvature (κ), and winter redistribution (Sx).

Fig. 11. See Figure **??**