# Analysis of methods and uncertainties in estimating winter surface mass balance from direct measurements on alpine glaciers

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ABSTRACT. Accurately estimating winter surface mass balance for a glacier is central to quantifying overall mass balance and melt runoff. However, measuring and modelling snow distribution and variability is inherently difficult in alpine terrain, resulting in high winter balance uncertainty. The goal of this paper is to examine methods and sources of error when converting snow measurements to estimates of winter balance and to gain a more comprehensive understanding of uncertainties inherent in this process. We extensively measure snow depth and density, at various spatial scales, on three glaciers in the St. Elias Mountains, Yukon. Elevation is found to be the dominant driver of accumulation variability but the relationship varies between glaciers. Our results also suggest that wind redistribution and preferential deposition affect snow distribution but that more complex parametrization is need to fully capture wind effects. By using a Monte Carlo method to quantify the effects of various sources of uncertainty, we find that interpolation of SWE measurements is the largest source of winter balance uncertainty. Snow distribution patterns differed considerably between glaciers, highlighting strong inter- and intra-basin variability. Accurately and precisely estimating winter balance therefore continues to be a difficult and elusive problem.

#### INTRODUCTION

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Accurate estimation of winter surface mass balance is critical for correctly simulating the summer and 27 overall mass balance of a glacier (Réveillet and others, 2016). Effectively representing spatial distribution of 28 snow is also important for simulating snow and ice melt as well as energy and mass exchange between the 29 land and atmosphere to better monitor surface runoff and its downstream effects (Clark and others, 2011). 30 Snow distribution is sensitive to a number of complex process that partially depend on glacier location, topography, and orientation (Blöschl and others, 1991; Mott and others, 2008; Clark and others, 2011; Sold 32 and others, 2013). Current models are not able to fully represent these processes so the distribution of snow 33 in remote, mountainous locations is not well known. There is, therefore, a significant source of uncertainty 34 that undermines the ability of models to represent current glacier conditions and make predictions of glacier 35 response to a warming climate (Réveillet and others, 2016). 36 Winter surface mass balance is the net accumulation and ablation of snow over the winter season (Cogley 37 and others, 2011), which constitutes glacier mass input. We refer to this quantity as winter balance throughout 38 the paper. Accurate estimates of winter balance are critical for calculating glacier mass balance, not only 39 because winter balance constitutes half of the glacier mass balance but also because the distribution of snow 40 on a glacier initializes the summer balance and high snow albedo contributes to reduced summer melt (Hock, 41 2005; Réveillet and others, 2016). 42 Winter balance is notoriously difficult to estimate. Snow distribution in alpine regions is highly variable and 43 influenced by dynamic interactions between the atmosphere and complex topography, operating on multiple 44 spatial and temporal scales (Barry, 1992; Liston and Elder, 2006; Clark and others, 2011). Extensive, high 45 resolution and accurate accumulation measurements on glaciers are almost impossible to achieve due to cost 46 benefits of the various methods used to quantify snow water equivalent (Cogley and others, 2011; McGrath 47 and others, 2015). For example, snow probes obtain accurate point observations but have negligible spatial 48 coverage. Conversely, gravimetric methods obtain extensive measurements of mass change but cannot capture 49 relevant spatial variability of snow (Cogley and others, 2011). Glacierized regions are also generally remote and challenging to access during the winter due to poor travelling conditions. 51

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Most glacier mass balance programs estimate winter balance in a similar way to summer balance. 52 Measurements of the amount of snow at the end of the winter season are taken at a few stake locations 53 and then basic interpolation methods are used to estimate winter balance (e.g. Hock and Jensen, 1999; 54 MacDougall and Flowers, 2011; Cullen and others, 2017). However, equivalence between summer and winter 55 balance estimation methods is likely inappropriate. Melt is strongly affected by air temperature and solar 56 radiation (Hock, 2005), both of which are consistent across large spatial domains (Barry, 1992). Conversely, 57 snow distribution is largely driven by precipitation (Lehning and others, 2008) and wind patterns (Bernhardt 58 and others, 2009; Musselman and others, 2015), which are known to be highly heterogeneous in alpine 59 environments (Barry, 1992). Snow distribution is therefore highly variable and has short correlation length 60 scales (e.g. Anderton and others, 2004; Egli and others, 2011; Grunewald and others, 2010; Helbig and van 61 Herwijnen, 2017; López-Moreno and others, 2011, 2013; Machguth and others, 2006; Marshall and others, 62 2006). 63 Detailed studies of winter balance are far less common than those of summer balance and uncertainty in 64 winter mass balance currently overshadows differences between summer balance models (Réveillet and others, 65 2016). Studies that focus on estimating winter balance employ a wide range of snow measurement techniques 66 (Sold and others, 2013), including direct measurement (e.g. Cullen and others, 2017), lidar/photogrammerty (e.g. Sold and others, 2013) and ground penetrating radar (e.g. Machguth and others, 2006; Gusmeroli and 68 others, 2014; McGrath and others, 2015). Spatial coverage of measurements is often limited for winter balance 69 studies and typically consists of an elevation transect along the glacier centreline (e.g. Kaser and others, 70 2003; Machguth and others, 2006). Interpolation of these measurements is primarily done by computing 71 a linear regression that includes only a few topographic parameters (e.g. MacDougall and Flowers, 2011), 72 with elevation being the most common. Other applied techniques include hand contouring (e.g. Tangborn 73 and others, 1975), kriging (e.g. Hock and Jensen, 1999) and attributing measured accumulation values to 74 elevation bands (source??). Physical snow models have been applied on a few glaciers (Mott and others, 75 2008; Dadic and others, 2010) but a lack of detailed meteorological data generally prohibits their wide-76 spread application. Error analysis is rarely considered and to our knowledge, no studies have investigated 77 uncertainty in winter balance estimates. 78 There is a disparity in snow survey sophistication within glacier winter balance studies when compared to 79

snow science studies. Winter mass balance surveys employ similar techniques and methods as snow science

surveys (e.g. Elder and others, 1991; Deems and Painter, 2006; Nolan and others, 2015; Godio and Rege, 2016)

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but favour more simple approaches (Kaser and others, 2003; Sold and others, 2013). Snow science surveys are generally extensive and designed to measure snow throughout the basin and ensure that all terrain types are 83 sampled. A wide array of measurement interpolation methods are used, including linear (e.g. López-Moreno 84 and others, 2010) and non-linear regressions (e.g. Molotch and others, 2005) and geospatial interpolation (e.g. 85 Erxleben and others, 2002) such as kriging, and methods are often combined to yield improved fit (e.g. Balk 86 87 and Elder, 2000). Physical snow models, such as Alpine3D (Lehning and others, 2006) and SnowDrift3D (Schneiderbauer and Prokop, 2011), are continuously being improved and tested within the snow science 88 literature. Snow survey error has been considered from both a theoretical (Trujillo and Lehning, 2015) and 89 applied perspective (Turcan and Loijens, 1975; Woo and Marsh, 1978; Deems and Painter, 2006). 90 The precision and accuracy of winter balance estimates can likely be improved by incorporating snow 91 science tools and interpolation methodologies and by gaining a more comprehensive understanding of 92 uncertainties inherent when estimating winter balance on glaciers. Ultimately, we need a thorough knowledge 93 of the processes that affect spatial and temporal snow variability and an effective method to predict snow accumulation. The contribution of our work toward these goals is to (1) examine methods and uncertainties 95 when moving from direct snow depth and density measurements to estimating winter balance and (2) show 96 how snow variability, data error and our methodological choices interact to create uncertainty in our estimate of winter balance. We focus on commonly applied low-complexity methods of measuring and predicting winter 98 balance with the hope of making our results broadly applicable to current and future winter mass balance 99 programs. 100

#### 101 STUDY SITE

Winter balance surveys were conducted on three glaciers in the Donjek Range of the St. Elias Mountains, 102 located in the south western Yukon, Canada. The Donjek Range is approximately  $30 \times 30$  km and Glacier 103 4, Glacier 2, and Glacier 13 (labelling adopted from Crompton and Flowers (2016)) are located along a 104 SW-NE transect through the range. There is a local topographic divide in the Donjek Range that follows 105 an "L" shape, with one glacier located in each of the south, north, and east regions (Figure 1). These mid-106 sized alpine glaciers are generally oriented SE-NW, with Glacier 4 dominantly south facing and Glaciers 107 2 and 13 generally north facing. The glaciers are low angled with steep head walls and steep valley walls. 108 The St. Elias mountains boarder the Pacific Ocean and rise sharply, creating a significant climatic winter 109 gradient between coastal maritime conditions, generated by Aleutian-Gulf of Alaska low-pressure systems, 110 and interior continental conditions, determined by Yukon-Mackenzie high-pressure system (Taylor-Barge, 111

Table 1. Physical details of study glaciers

	T 43	Elevation (m a.s.l)		Slope ( $^{\circ}$ )	Area
	Location	Mean	Range	Mean	(km)
G4	595470 E	2344	1958–2809	12.8	3.8
	6740730 N	2044	1990-2009		
G2	601160 E	2495	1899–3103	13.0	7.0
G2	6753785 N				
G13	$604602~\mathrm{E}$	2428	1923-3067	13.4	12.6
	6763400  N	2120			

112 1969). The average dividing line between the two climatic zones shifts between Divide Station and the head
113 of the Kaskawalsh Glacier based on synoptic conditions. The Donjek Range is located approximately 40 km
114 to the east of the head of the Kaskawalsh Glacier. Research on snow distribution and glacier mass balance
115 in the St. Elias is limited. A series of research programs were operational in the 1960s (Wood, 1948; Danby
116 and others, 2003) and long-term studies on a few alpine glaciers have arisen in the last 30 years (e.g. Clarke
117 and others, 1984; Paoli and Flowers, 2009).

# 118 METHODS

Estimating winter balance involves transforming snow depth and density measurements to distributed 119 estimates of snow water equivalent (SWE). We use four main processing steps. First, we obtain measurements 120 of snow depth and density. Since density is measured more sparsely than depth, the second step is to 121 interpolate density measurements to all depth measurement locations and to calculate the SWE at each 122 measurement location. Third, we average all SWE values within one grid cell of a digital elevation model 123 (DEM) with given spatial resolution to produce a single value of SWE for each grid cell. Fourth, we interpolate 124 SWE values to obtain a distributed estimate of SWE across the surface of the glacier. We choose to use a 125 linear regression between SWE and topographic parameters as well as simple kriging to interpolation grid 126 cell SWE. To estimate the specific winter balance we then calculate aerially-averaged integrated SWE. For 127 brevity, we refer to these four steps as (1) field measurements, (2) distributed snow density, (3) grid cell 128 average SWE and (4) distributed SWE. Detailed methodology for each step is outlined below. 129

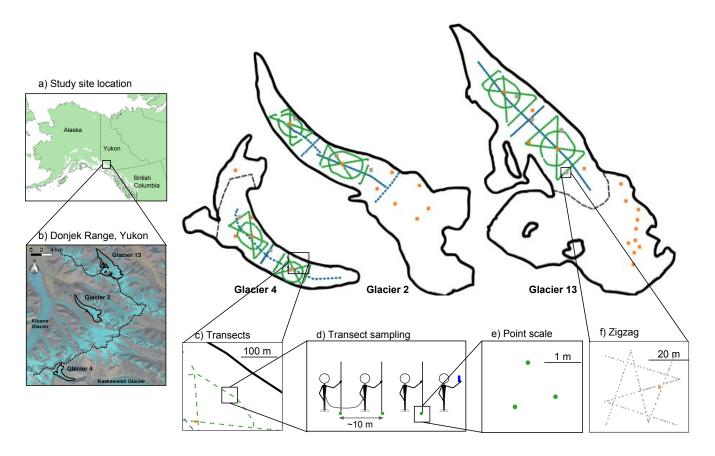


Fig. 1. Sampling design for Glaciers 4, 2 and 13, located in the Donjek Range, Yukon (a,b). Centreline and transverse transects are shown in blue dots, hourglass and circle design are shown in green dots. (c) Linear and curvilinear transects typically consist of sets of three measurement locations, spaced ~10 m apart (d). (e) At each measurement location, three snow depth observation are made. (f) Linear-random snow depth measurements in 'zigzag' design are shown as grey dots. Orange squares are locations of snow density measurements.

# Field measurements

131 Sampling design

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- 132 The sampling design attempted to capture depth variability at multiple spatial scales. We measured winter
- balance at three glaciers along the precipitation gradient in the St. Elias Mountains, Yukon (Taylor-Barge,

Table 2. Details of snow survey conducted in May 2016 at Glacier 4 (G4), Glacier 2 (G2), and Glacier 13 (G13). Values shown include number of snow depth measurement locations along transects  $(n_T)$ , total length of transects  $(d_T \text{ [km]})$ , number of combined SP and FS density measurement locations  $(n_\rho)$  and number of zigzag  $(n_{zz})$ .

	Date	$n_T$	$d_T$	$n_{ ho}$	$n_{zz}$
<b>G4</b>	May 4–7	649	13.1	7	3
G2	May 8–11	762	13.6	7	3
G13	May 12–15	941	18.1	19	4

1969) in an attempt to account for range-scale variability (Clark and others, 2011). We measured winter 134 balance on Glaciers 4, 2, and 13, which are located increasingly far from the head of the Kaskawalsh Glacier 135 (Figure 1b). Snow depth was measured along linear and curvilinear transects to account for basin-scale 136 variability. At each measurement location, three values of snow depth were recorded to account for point-137 scale variability (Clark and others, 2011). We selected centreline and transverse transects with sample spacing 138 139 of 10-60 m (Figure 1d) to capture previously established correlations between elevation and accumulation (e.g. Machguth and others, 2006; Walmsley, 2015) as well as accumulation differences between ice-marginal 140 and centre accumulation. We also implemented an hourglass and circle design (Figure 1), which allows for 141 sampling in all directions and easy travel (Parr, C., 2016 personal communication). At each measurement 142 location, we took 3-4 depth measurements within  $\sim 1$  m of each other (Figure 1e), resulting in more than 143 9,000 snow depth measurements throughout the study area. 144

# 145 $Snow\ depth$

The estimated SWE is the product of the snow depth and depth-averaged density. Snow depth is generally 146 accepted to be more variable than density (Elder and others, 1991; Clark and others, 2011; López-Moreno and 147 others, 2013) so we chose a sampling design with relatively small measurement spacing along transects that 148 resulted in a ratio of approximately 55:1 snow depth to snow density measurements. Our sampling campaign 149 involved four people and occurred between May 5 and 15, 2015, which corresponds to the historical peak 150 accumulation in the Yukon (Yukon Snow Survey Bulletin and Water Supply Forecast, May 1, 2016). While 151 roped-up for glacier travel at fixed distances between observers, the lead person used a single frequency 152 GPS (Garmin GPSMAP 64s) to navigate as close to the predefined transect measurement locations as 153 possible (Figure 1). The remaining three people used 3.2 m aluminium avalanche probes to take snow depth 154 measurements. The location of each set of depth measurements, taken by the second, third and fourth 155 observers, was approximated based on the recorded location of the first person. 156

Snow depth sampling was primarily done in the ablation area to ensure that only snow from the current accumulation season was measured. Determining the boundary between snow and firn in the accumulation area, especially when using an avalanche probe, is difficult and often incorrect (Grunewald and others, 2010; Sold and others, 2013). We intended to use a firn corer to extract snow cores in the accumulation area but due to environmental conditions we were unable to obtain cohesive cores. Successful measurements within the accumulation area were done either in a snow pit or using a Federal Sampler with shovel validation so that we could identify the snow-firn transition based on a change in snow crystal size and density.

164 Zigzags

To capture variability at spatial scales smaller than a DEM grid cell, we implemented a linear-random sampling design, termed 'zigzag' (Shea and Jamieson, 2010). We measured depth at random intervals (0.3-3.0 m) along two 'Z'-shaped transects within three to four  $40 \times 40$  m squares (Figure 1c) resulting in 135-191 measurement points for each zigzag. Zigzag locations were randomly chosen within the upper ( $\sim$ 2350 m a.s.l.), middle ( $\sim$ 2250 m a.s.l.), and lower portions ( $\sim$ 2150 m a.s.l.) of the ablation area of each glacier. We were able to measure a fourth zigzag on Glacier 13 that was located in the middle ablation area ( $\sim$ 2200 m a.s.l.).

172 Snow density

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Snow density was measured using a wedge cutter in three snowpits on each glacier. We measured a vertical density profile by inserting a  $5 \times 10 \times 10$  cm wedge-shaped cutter (250 cm<sup>3</sup>) in 5 cm increments to extract snow

samples and then weighed the samples with a spring scale (e.g. Gray and Male, 1981; Fierz and others, 2009).

176 Uncertainty in estimating density from snow pits stems from measurement errors and incorrect assignment

of density to layers that could not be sampled (i.e. ice lenses and 'hard' layers).

While snow pits provide the most accurate measure of snow density, digging and sampling a snow pit is time and labour intensive. Therefore, a Federal Snow Sampler (FS) (Clyde, 1932), which measures bulk SWE, was used to augment the spatial extent of density measurements. A minimum of three measurements were taken at each of 7-19 locations on each glacier and an additional eight FS measurements were co-located with each snow pit profile. Measurements where the snow core length inside the FS was less than 90% of the snow depth were assumed to be an incorrect sample and were excluded. Density values were then averaged for each location.

During the field campaign there were two small accumulation events. The first, on May 6, also involved high winds so accumulation could not be determined. The second, on May 10, resulted in 0.01 m w.e accumulation at one location on Glacier 2. Warm temperatures and clear skies occurred between May 11 and 16, which we believed resulted in significant melt occurring on Glacier 13. The snow in the lower part of the ablation area was isothermal and showed clear signs of melt and snow metamorphosis. The total amount of accumulation and melt during the study period could not be estimated so no corrections were made.

# 191 Distributed snow density

Measured density is interpolated to estimate SWE at each depth sampling location. We chose four separate methods that are commonly applied to interpolate density: (1) mean density over an entire range (e.g. Cullen

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**Table 3.** Description of density interpolation methods used to calculate SWE used in the topographic regression. Abbreviations with 'S' used snowpit-derived densities and abbreviations with an 'F' used Federal Sampler-derived densities.

	Snow den	sity source	Estimation		
	Snowpit	$Federal \ Sampler$	method		
S1 F1	•	•	Mean of all glaciers		
S2 F2	•	•	Glacier mean		
S3 F3	•	•	Linear regression of elevation and density for each glacier		
S4 F4		•	Inverse distance weighted mean		

and others, 2017), (2) mean density for each glacier (e.g. Elder and others, 1991; McGrath and others, 2015), (3) linear regression of density with elevation (e.g. Elder and others, 1998; Molotch and others, 2005) and (4) inverse-distance weighted density (e.g. Molotch and others, 2005). SP and FS densities are treated separately, for reasons explained below, which results in eight density interpolation options (Table 3).

# Grid cell average SWE

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We average SWE values within each DEM-aligned grid cell. The locations of measurements have considerable uncertainty both from the error of the GPS unit (2.7-4.6 m) and the estimation of observer location based on the GPS unit. These errors could easily result in the incorrect assignment of a SWE measurement to a certain grid cell but this source of variability was not further investigated because we assume that SWE variability is captured in the zigzag measurements described below. There are no significant differences between observers (p>0.05), with the exception of the first transect on Glacier 4. No corrections to the data based on observer differences are applied.

# Distributed SWE

207 Linear regression

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208 SWE are interpolated and extrapolated for each glacier using linear regression (LR) as well as simple kriging (SK). Linear regressions relate observed SWE to grid cell values of DEM-derived topographic parameters 209 (Davis and Sampson, 1986). We choose to include elevation, distance from centreline, slope, aspect, curvature, 210 "northness" and a wind redistribution parameter in the LR. Topographic parameters are weighted by a set of 211 fitted regression coefficients ( $\beta_i$ ). Regression coefficients are calculated by minimizing the sum of squares of 212 the vertical deviations of each data point from the regression line (Davis and Sampson, 1986). The distributed 213 estimate of SWE is found by using regression coefficients to estimate SWE at each grid cell. Specific winter 214 balance is calculated as the aerially-averaged, integrated SWE for each glacier ([m w.e.]). 215 Snow depth data are highly variable so there is a possibility for the LR to fit to this data noise, a process 216 known as overfitting. To prevent overfitting, cross-validation and model averaging are implemented. First, 217 cross-validation is used to obtain a set of  $\beta_i$  values that have greater predictive ability. We select 1000 random 218 subsets (2/3 values) of the data to fit the LR and the remaining data (1/3 values) are used to calculate a root 219 mean squared error (RMSE) (Kohavi and others, 1995). Regression coefficients resulting in the lowest RMSE 220 are selected. Second, we use model averaging to take into account uncertainty when selecting predictors and 221 to also maximize predictive ability (Madigan and Raftery, 1994). Models are generated by calculating a set 222 of  $\beta_i$  for all possible combinations of predictors. Following a Bayesian framework, model averaging involves 223 weighting all models by their posterior model probabilities (Raftery and others, 1997). To obtain the final 224 regression coefficients, the  $\beta_i$  values from each model are weighted according to the relative predictive success 225 of the model, as assessed by the Bayesian Information Criterion (BIC) value (Burnham and Anderson, 2004). 226 BIC penalizes more complex models, which further reduces the risk of overfitting. 227

# Topographic parameters

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Topographic parameters are easy to calculate proxies for physical processes, such as orographic precipitation, solar radiation effects, wind redistribution and preferential deposition. We derive all parameters (Table 4) for our study from a SPOT-5 DEM ( $40 \times 40$  m) (Korona and others, 2009). Two DEMs are stitched together to encompass the Donjek Range. An iterative 3D-coregistration algorithm (Berthier and others, 2007) is used to correct the horizontal ( $\sim 2$  m E,  $\sim 4$  m N) and vertical (5.4 m) discrepancy between the two DEMs before stitching.

Visual inspection of the curvature fields calculated using the full DEM shows a noisy spatial distribution that did not vary smoothly. To smooth the DEM, various smoothing algorithms and window sizes are applied and the combination that produces the highest correlation between topographic parameters and SWE is chosen. Inverse-distance weighted, Gaussian and grid cell averaging smoothing all with window sizes of  $3\times3$ ,  $5\times5$ ,  $7\times7$  and  $9\times9$  are used. Grid cell average smoothing with a  $7\times7$  window resulted in the highest overall correlation between curvature (second derivative) and SWE as well as slope (first derivative) and SWE. We use the smoothed DEM to calculate curvature, slope, aspect and "northness".

242 Simple kriging

Simple kriging (SK) estimates SWE values at unsampled locations by using the isotropic spatial correlation 243 (covariance) of measured SWE to find a set of optimal weights (Davis and Sampson, 1986; Li and Heap, 2008). 244 SK assumes that if sampling points are distributed throughout a surface, the degree of spatial correlation of 245 the observed surface can be determined and the surface can then be interpolated between sampling points. We 246 used the DiceKriging R package (Roustant and others, 2012) to calculate the maximum likelihood covariance 247 matrix, as well as range distance  $(\theta)$  and nugget. The range distance is a measure of data correlation length 248 and the nugget is the residual that encompasses sampling-error variance as well as the spatial variance at 249 distances less than the minimum sample spacing (Li and Heap, 2008). 250

#### 251 Quantifying effects of uncertainty

We identify three major sources of uncertainty within the process of translating snow measurements to 252 winter balance. These uncertainty sources encompass error and uncertainty within each processing step. 253 When calculating distributed density, the density interpolation method is the largest source of uncertainty. 254 We therefore carry all density interpolation options forward in the estimation of winter balance. When 255 calculating a grid cell average SWE, uncertainty stems from a distribution of SWE values within each grid 256 cell, which is assumed to be caused by random effects that are unbiased and unpredictable (Watson and 257 others, 2006). We therefore choose to characterize SWE uncertainty by generating a normal distribution of 258 SWE values for each measured grid cell. The normal distribution has a mean equal to the grid cell average 259 SWE and a standard deviation equal to the mean standard deviation of all zigzags on each glacier. When 260 obtaining interpolated SWE, the best fit interpolation itself has uncertainty based on the data that are 261 used to fit the regression line or kriging surface. LR uncertainty is represented by obtaining a multivariate 262 normal distribution of possible  $\beta_i$  values. The standard deviation of each distribution is calculated using 263 the covariance of regression coefficients as outlined in Bagos and Adam (2015). SK uncertainty is calculated 264

 ${\bf Table~4.~Description~of~topographic~parameters~used~in~the~linear~regression.}$ 

Topographic parameter	Definition	Calculation method	Notes	Source
Elevation $(z)$		Values taken directly from DEM Minimum distance between the Easting and Northing of the		
Distance from centreline $(d_C)$		northwest corner of each grid cell and a manually defined centreline		
Slope (m)	Angle between a plane tangential to the surface (gradient) and the horizontal	r.slope.aspect module in GRASS GIS software run through QGIS		Mitášová and Hofierka (1993); Hofierka and others (2009); Olaya (2009)
Aspect ( $\alpha$ )	Dip direction of the slope	r.slope.aspect module in GRASS GIS software run through QGIS	$\sin(\alpha)$ , a linear quantity describing a slope as north/south facing, is used in the regression	Mitášová and Hofierka (1993); Hofierka and others (2009); Olaya (2009)
$\begin{array}{ccc} \textbf{Mean} & \textbf{curvature} \\ (\kappa) & & \end{array}$	Average of profile (direction of the surface gradient) and tangential curvature (direction of the contour tangent)	r.slope.aspect module in GRASS GIS software run through QGIS	mean-concave (positive values) terrain with relative accumulation and mean-convex (negative values) terrain with relative scouring	Mitášová and Hofierka (1993); Hofierka and others (2009); Olaya (2009)
"Northness" $(N)$	-1 represents a vertical, south facing slope, a value of +1 represents a vertical, north facing slope, and a flat surface yields 0	Product of the cosine of aspect and sine of slope		Molotch and others (2005)

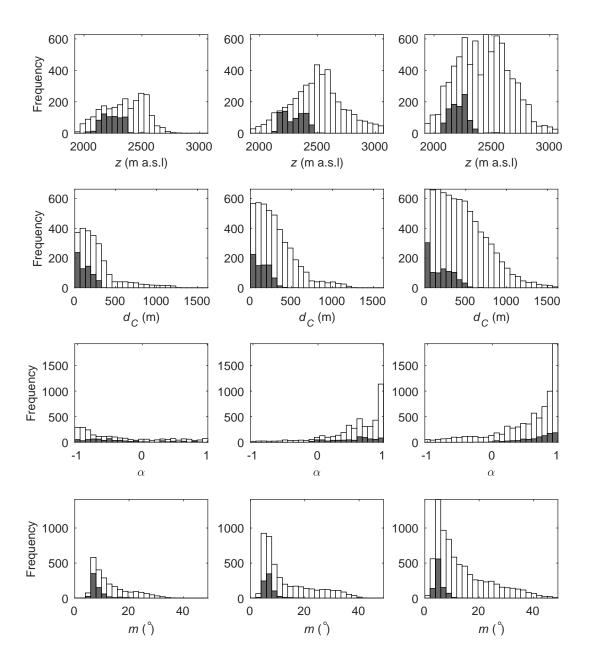


Fig. 2. Distribution of topographic parameters over Glacier 4 (left), Glacier 2 (middle) and Glacier 13 (right) are shown in white. Distribution of topographic parameter values from sampled grid cells in shown in gray. Topographic parameters include elevation (z), distance from centreline  $(d_C)$ , aspect  $(\alpha)$ , slope (m), northness (N), mean curvature  $(\kappa)$ , and winter redistribution (Sx).

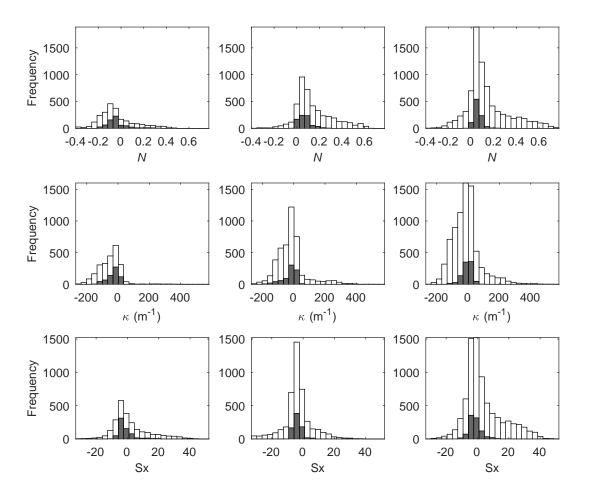


Fig. 3. See Figure 2

using the DiceKriging package and is returned as an upper and lower 95% confidence interval for SWE at each grid cell. We refer to the three uncertainty sources as (1) density uncertainty, (2) SWE uncertainty and (3) interpolation uncertainty.

To quantify the effects of the three uncertainty sources on the final winter balance estimate, we conduct a Monte Carlo experiment, which uses repeated random sampling to calculate a numerical solution (Metropolis and Ulam, 1949). In our study, we randomly sample the distributions for SWE uncertainty and interpolation uncertainty and carry these values through the data processing steps to obtain a value of winter balance. First, random values from the distribution of SWE values for each grid cell are independently chosen. Then, LR or SK is used to interpolate these SWE values. With the LR, a set of  $\beta_i$  values and their distributions

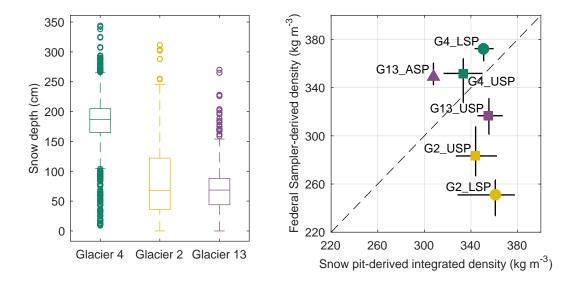


Fig. 4. (Left) Boxplot of measured snow depth on Glaciers 4, 2 and 13. The box shows first quartiles, the line within the box indicates data median, bars indicate minimum and maximum values (excluding outliers), and circles show outliers, which are defined as being outside of the range of 1.5 times the quartiles (approximately  $\pm 2.7\sigma$ ). (Right) Comparison of integrated density estimated using wedge cutters in a snow pit and density estimated using Federal Sampler measurements for Glacier 4 (G04), Glacier 2 (G02) and Glacier 13 (G13). Snow pits were distributed in the accumulation area (ASP), upper ablation area (USP) and lower ablation area (LSP). Error bars are minimum and maximum values.

are calculated and the  $\beta_i$  distributions are randomly sampled. These new  $\beta_i$  values are used to calculate winter balance. With SK, a distribution of winter balance is calculated from the 95% confidence interval kriging surfaces. Density uncertainty is accounted for by repeating the process for each density interpolation method. This random sampling process is done 1000 times, which results in a distribution of possible winter balance values based on uncertainty within the data processing steps.

# RESULTS

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#### Measurements

A wide range of snow depth is observed on all three study glaciers (Figure 4). Glacier 4 has the highest mean snow depth and a high proportion of outliers, indicating a more variable snow depth overall. Glacier 13 has the lowest mean snow depth and a narrower distribution of observed values. At each measurement location,

the median range of measured depths (3-4 points) as a percent of the mean depth at that location is 2%, and 12%, for Glaciers 4, 2 and 13, respectively.

Mean SP and FS density values are within one standard deviation of each other for each glacier and over 286 all three glaciers. The standard deviation of glacier-wide mean density is less than 10% of the mean density. 287 However, FS densities have a larger range of values  $(227 - 431 \text{kg m}^{-3})$  when compared to SP densities 288  $(299 - 381 \text{kg m}^{-3})$ . The mean SP densities are within one standard deviation between glaciers, whereas 289 mean FS densities are not. 290 Uncertainty in SP density is largely due to sampling error of exceptionally dense snow layers. We quantify 291 this uncertainty by varying three values. Ice layer density is varied between 700 and 900 kg m<sup>-3</sup>, ice layer 292 thickness is varied by  $\pm 1$  cm of the recorded thickness, and the density of layers identified as being too hard 293

to sample (but not ice) is varied between 600 and 700 kg  $m^{-3}$ . The range of integrated density values is

always less than 15% of the reference density, with the largest ranges present on Glacier 2. Density values

296 for shallow pits that contain ice lenses are particularly sensitive to changes in density and ice lens thickness.

# 297 Distributed density

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We find no correlation between co-located SP and FS densities (Figure 4) so each set of density values is used 298 for all four density interpolation options. Regional and glacier mean densities are higher when SP densities 299 are used (Table 5). The slope of a linear regression of density with elevation differs between SP and FS 300 densities (Table 5). At Glaciers 2 and 13, SP density decreases with elevation, likely indicating melt and/or 301 compaction at lower elevations. SP density is independent of elevation on Glacier 4. FS density increases with 302 elevation on Glacier 2 and there is no relationship with elevation on Glaciers 4 and 13. There is a positive 303 linear relation ( $R^2 = 0.59$ , p<0.01) between measured snow density and depth for all FS measurements. No 304 correlation exists between SP density and elevation. 305

# Grid cell average

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SWE observations within a DEM grid cell are averaged. Between one and six measurement locations are in each measured grid cell. The distribution of grid-cell SWE values for each glacier is similar to that of Figure 4 but with fewer outliers. SWE measurements for each zigzag are not normally distributed about the mean SWE (Figure 5). The average standard deviation of all zigzags on Glacier 4 is  $\sigma_{G4} = 0.027$  m w.e., on Glacier 2 is  $\sigma_{G2} = 0.035$  m w.e. and on Glacier 13 is  $\sigma_{G13} = 0.040$  m w.e.

**Table 5.** Snow density values used for interpolating density based on snow pit (SP) densities and Federal Sampler (FS) densities. Four interpolation methods are chosen: (1) using a mean snow density for all three glaciers (Range mean density), (2) using a mean density for each glacier (Glacier mean density), (3) using a regression between density and elevation (Elevation regression), and (4) inverse-distance weighted mean density (not shown).

		SP density	FS density
		$({ m kg} { m m}^{-3})$	$({ m kg} { m m}^{-3})$
Range mean density		342	316
	G4	348	327
Glacier	G2	333	326
mean density	G13	349	307
T1	G4	0.03z + 274	-0.16z + 714
Elevation	G2	-0.14z + 659	0.24z - 282
regression	G13	-0.20z + 802	0.12z + 33

# Interpolated SWE

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The choice of interpolation method affects the specific winter balance (Table 6). SK produces the highest winter balance on Glacier 4 and the lowest winter balance on Glacier 13. winter balance estimated by SK is ~30% lower than winter balance estimated by LR on Glaciers 2 and 13. When using LR, the winter balance on Glaciers 4 and 2 are similar in magnitude.

The predictive ability of SK and LR differ on the study glaciers. Generally, SK is better able to predict SWE at observed grid cells (Figure 6) and RMSE for all glaciers is lower for SK estimates (Table 6). Glacier 13 has the lowest RMSE regardless of interpolation method, indicating lower SWE variability. The highest RMSE and the lowest correlation between estimated and observed SWE is seen on Glacier 4 ( $R^2 = 0.12$ ), which emphasizes the highly variable snow distribution. The highest correlation between estimated and observed SWE is on Glacier 2 when SK is used for interpolation ( $R^2 = 0.84$ ) (Figure 6). Residuals using LR and SK for all glaciers are normally distributed.

The importance of topographic parameters in the LR differs for the three study glaciers (Figure 7). The most important topographic parameter for Glacier 4 is wind redistribution. However, the wind redistribution coefficient is negative, which indicates less snow in 'sheltered' areas. Curvature is also a significant predictor of accumulation and the positive correlation indicates that concave areas are more likely to have higher

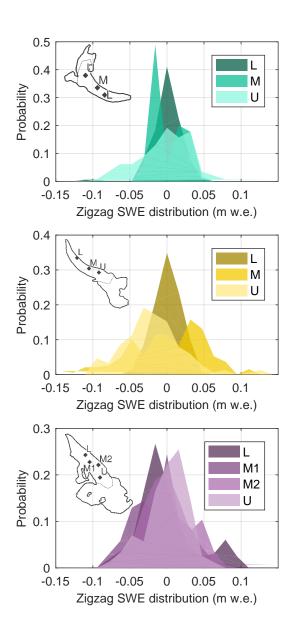


Fig. 5. Distribution of zigzag SWE values with the local mean subtracted on Glacier 4 (upper panel), Glacier 2 (middle panel) and Glacier 13 (lower panel). Zigzags are distributed throughout the ablation area of each glacier, with one located in the lower portion (L), one in the middle portion (M), and one in the upper portion (U). There were two zigzags in the middle ablation area of Glacier 13.

SWE. For Glacier 2, the most important topographic parameter is elevation, which is positively correlated with elevation. Wind redistribution is the second most important topographic parameter and has a positive

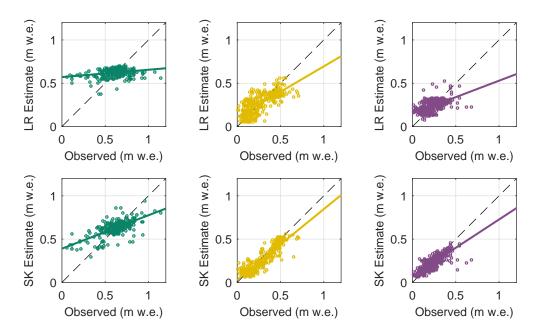
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**Table 6.** Specific winter balance (WB [m w.e.]) estimated using linear regression and simple kriging interpolation for study glaciers. Average root mean squared error (RMSE [m w.e.]) between estimated and observed grid cells for all points, which were randomly selected and excluded from interpolation, is also shown. RMSE as a percent of the WB is shown in brackets.

	Linear	r Regression	Simple Kriging		
	WB RMSE		WB	RMSE	
G4	0.582	0.153 (26%)	0.616	0.134 (22%)	
G2	0.577	0.102 (18%)	0.367	0.073 (20%)	
G13	0.381	0.080 (21%)	0.271	0.068 (25%)	

correlation, which indicates that 'sheltered' areas are likely to have high accumulation. The most important topographic parameter for Glacier 13 is elevation. The coefficient is positive, which means that cells at higher elevation have higher SWE. Curvature is also a significant topographic parameter but the correlation is negative, indicating less accumulation in concave areas. Most of the topographic parameters are not



**Fig. 6.** Estimated grid cell SWE found using linear regression (LR) and simple kriging (SK) plotted against observed values of SWE on Glacier 4 (left), Glacier 2 (middle) and Glacier 13 (right). Line of best fit between estimated and observed SWE is also plotted.

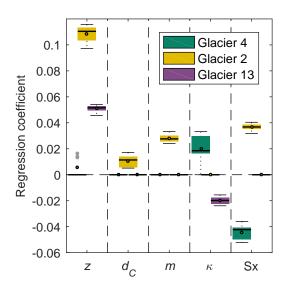


Fig. 7. Distribution of regression coefficients for linear regression of grid cell topographic parameters and SWE calculated using eight density options on study glaciers. Topographic parameters include elevation (z), distance from centreline  $(d_C)$ , slope (m), curvature  $(\kappa)$ , and wind exposure (Sx). Regression coefficients that were not significant were assigned a value of zero. Aspect and "northeness" are not shown because coefficient values are zero for all glaciers. Outlier values are shown as gray dots.

significant predictors of accumulation on Glacier 13. Aspect and "northness" are not significant predictors of accumulation on all study glaciers.

Our sampling design ensured that the ranges of topographic parameters covered by the measurements represented more than 70% of the total area of each glacier (except for the elevation range on Glacier 2, which was 50%). However, we were not able to sample at locations with extreme parameter values and the distribution of the sampled parameters generally differed from the full distribution.

Spatial patterns of SWE found using LR are similar between Glaciers 2 and 13 and differ considerably for Glacier 4 (Figure 8). Estimated SWE on Glacier 4 is relatively uniform, which results from the low predictive ability of the LR. Areas with high wind redistribution values (sheltered), especially in the accumulation area, have the lowest values of SWE. The map of modelled SWE on Glacier 2 closely matches that of elevation, which highlights the strong dependence of SWE on elevation. Glacier 2 has the largest range of estimated SWE (0-1.92 m w.e). The area of high estimated accumulation in the southwest region of the glacier results from the combination of high elevation and Sx values. The low SWE values at the terminus arise from low

Table 7. Range and nugget values for simple kriging interpolation

	Range	Nugget		
	(m)	$(\times 10^3 \text{m w.e.})$		
G4	90	10.5		
G2	404	3.6		
G13	444	4.8		

elevation and Sx values close to zero. The map of estimated SWE on Glacier 13 also closely follows elevation.

348 However, the lower correlation between SWE and elevation results in a relatively small range of distributed

349 SWE values.

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There are large differences in spatial patterns of estimated winter balance for the three study glaciers 350 found using SK (Figure 8). On Glacier 4, the isotropic correlation length is considerably shorter compared 351 to Glacier 2 and Glacier 13 (Table 7), which results in a relatively uniform SWE distribution over the glacier 352 with small deviations at measured grid cells. Nugget values for the study glaciers also differ, with the nugget 353 of Glacier 4 more than twice as large as that of Glacier 2 and Glacier 13 (Table 7). Glacier 2 has two distinct 354 and relatively uniform areas of estimated accumulation. The lower ablation area has low SWE ( $\sim 0.1 \text{ m w.e.}$ ) 355 and the upper ablation and accumulation areas have higher SWE values ( $\sim 0.6$  m w.e.). Glacier 13 does not 356 appear to have any strong patterns and accumulation is generally low ( $\sim 0.1-0.5$  m w.e.). 357

SWE estimated with LR and SK differ considerably in the upper accumulation areas of Glaciers 2 and 13.

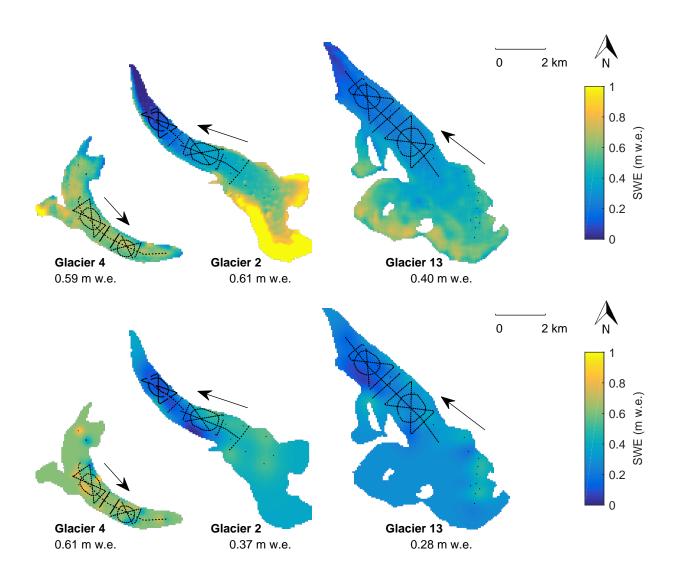
The significant influence of elevation in the LR results in substantially higher SWE values at high elevation,

whereas the accumulation area of the SK estimates approximate the mean observed SWE.

Transferring LR coefficients between glaciers results in a high RMSE across the mountain range. The lowest overall RMSE (0.2051 m w.e.) results from calculating a LR using all available observations. Elevation is the only significant topographic predictor for a range-scale LR ( $\beta_z = 0.0525$ ).

# Quantifying effects of uncertainty

Specific winter balance is affected by uncertainty introduced when interpolating density (density uncertainty), when calculating grid cell SWE values (SWE uncertainty), and when interpolating observations (interpolation uncertainty). We find that when using LR and SK, interpolation uncertainty has a larger effect on winter balance uncertainty than density uncertainty or SWE uncertainty. The probability density function (PDF)



**Fig. 8.** Spatial distribution of SWE estimated using linear regression (upper) and simple kriging (lower). Grid-cell SWE observations are found using glacier wide mean snow pit density and are shown as black dots. Glacier flow directions are indicated by arrows. Specific winter balance values are also shown.

that arises from SWE uncertainty is much narrower than the PDF that arises from interpolation uncertainty (Figure 9 and Table 8).

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The total winter balance uncertainty from SK interpolation is 3 to 5 times greater than uncertainty from LR interpolation. The PDFs overlap between the two interpolation methods although the PDF modes have lower winter balance values when SK is used for Glaciers 2 and 13 and higher for Glacier 4. SK results in winter balance distributions that overlap between glaciers and there is also a small probability of estimating a

Table 8. Standard deviation ([×10<sup>-2</sup> m w.e.]) of specific winter balance estimated using linear regression (LR) and simple kriging (SK) when uncertainty is introduced. Density uncertainty ( $\sigma_{\rho}$ ) is the standard deviation of winter balance estimated using SWE data with different density interpolation methods. SWE uncertainty ( $\sigma_{\text{SWE}}$ ) is approximated by a normal distribution about the local SWE value with standard deviation equal to the glacierwide mean zigzag standard deviation. LR interpolation uncertainty ( $\sigma_{INT}$ ) is accounted for by varying the regression coefficients with a normal distribution with standard deviation calculated from regression covariance. SK interpolation uncertainty ( $\sigma_{\text{INT}}$ ) is taken from the range of distributed SWE estimates calculated by the DiceKriging package. Result for Glacier 4 (G4), Glacier 2 (G2) and Glacier 13 (G13) are shown.

	Linear Regression		Simple Kriging			
	$\sigma_{ ho}$	$\sigma_{ m SWE}$	$\sigma_{INT}$	$\sigma_{ ho}$	$\sigma_{ m SWE}$	$\sigma_{ m INT}$
G4	1.90	0.86	2.13	2.15	0.85	14.05
G2	3.37	1.80	3.09	2.03	2.53	13.78
G13	1.68	1.12	2.80	1.27	1.15	9.65

winter balance value of 0 m w.e. for Glaciers 2 and 13. LR results in overlapping winter balance distributions for Glaciers 2 and 4, with the PDF peak of Glacier 4 being slightly higher than that of Glacier 2.

Density, SWE, and interpolation uncertainty all contribute to spatial patterns of winter balance uncertainty 377 (Figure 10). For both LR and SK, the greatest uncertainty in estimated SWE occurs in the accumulation 378 area. When LR is used, estimated SWE is highly sensitive to the elevation regression parameter. In the case 379 of SK, uncertainty is greatest in areas far from observed SWE, which consist of the upper accumulation area 380 on Glaciers 2 and 13. uncertainty is greatest on Glacier 4 when LR interpolation is used at the upper edges 381 382 of the accumulation area, which correspond to the locations with extreme values of the wind redistribution parameter. When SK is used for interpolation on Glacier 4, uncertainty is greatest at the measured grid 383 cells, which highlights the short correlation length and the large effect of density interpolation on the SK 384 accumulation estimate. 385

# DISCUSSION

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#### Measurements

Our study suffers from lack of data in the accumulation area, especially along steep head walls. Snow probing cannot be used reliably in the accumulation area because the snow-firn transition is often difficult to determine. Sold and others (2013) noted that a systematic bias can result from incorrect values of winter

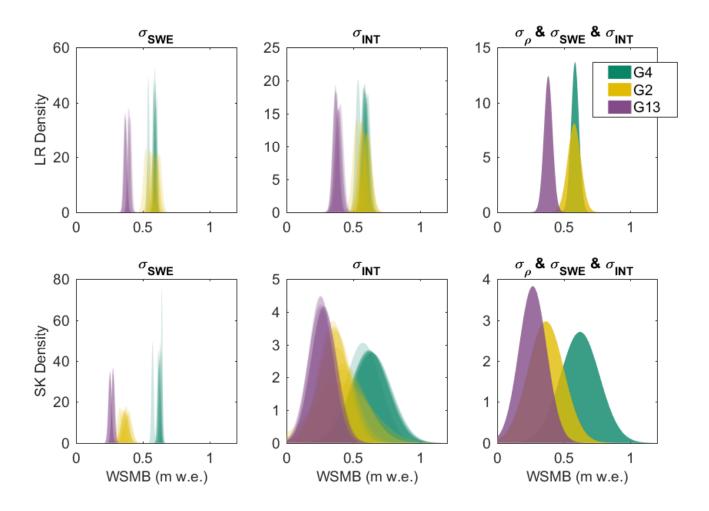


Fig. 9. Probability density functions (PDFs) fitted to distributions of specific winter balance values that arise from (left) SWE uncertainty ( $\sigma_{SWE}$ ), (middle) interpolation uncertainty ( $\sigma_{INTERP}$ ) and (right) all three sources of uncertainty. Results from a linear regression interpolation (top panels) and simple kriging (bottom panels) are shown. Each PDF is calculated using one of eight density interpolation methods for Glacier 4 (G4), Glacier 2 (G2) and Glacier 13 (G13).

balance, particularly because inaccessible areas such as cliffs and ridges have relatively shallow accumulations (due to wind erosion), while heavily crevassed areas can accumulate deep snow packs. Measuring SWE in the accumulation area is difficult and subject to large errors regardless of the data collection method.

We measured snow density by sampling a snow pit (SP) and by using a Federal Sampler (FS). We found that FS and SP measurements are not correlated and that FS density values are positively correlated with snow depth. This positive relationship could be a result of physical processes, such as compaction, but is

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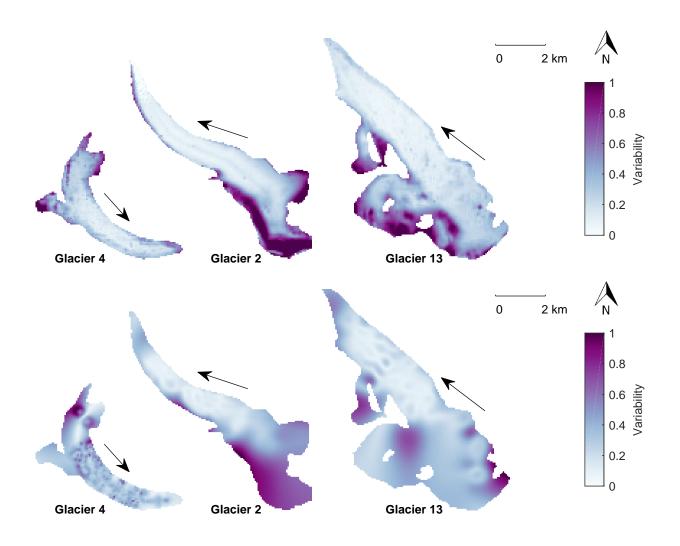


Fig. 10. Uncertainty of SWE estimated using linear regression (top) and simple kriging (bottom). Uncertainty is a relative quantity measured by taking the sum of differences between one hundred estimates of distributed winter balance that include SWE uncertainty and, in the case of linear regression, regression uncertainty. The sum is then normalized for each glacier. Glacier flow directions are indicated by arrows.

more likely a result of measurement artefacts for a number of reasons. First, the range of densities measured by the Federal sampler is large (225–410 kg m<sup>-3</sup>) and the extreme values seem unlikely to exist in our study region, which experiences a continental snow pack with minimal mid-winter melt events. Second, compaction effects would likely be small at these study glaciers because of the relatively shallow snow pack (deepest measurement was 340 cm). Third, no linear relationship exists between depth and SP density ( $R^2 = 0.05$ ).

Together, these reasons lead us to conclude that the Federal Sampler measurements are biased but in a way 402 that cannot be easily corrected. 403

The FS appears to oversample in deep snow and undersample in shallow snow. Oversampling by small 404 diameter (area of 10-12 cm<sup>2</sup>) sampling tubes has been observed in previous studies, with a percent error 405 between +6.8% and 11.8% (Work and others, 1965; Fames and others, 1982; Conger and McClung, 2009). 406 407 Studies that use Federal Samplers often apply a 10% correction to all measurements (e.g. Molotch and others, 2005). Dixon and Boon (2012) attributed oversampling to slots "shaving" snow into the tube as it is rotated, 408 as well as cutter design forcing snow into the tube. Beauont and Work (1963) found that FS oversampled 409 due to snow falling into the greater area of slots only when snow samples had densities greater than 400 410 kg m<sup>-3</sup> and snow depth greater than 1 m. Undersampling is likely to occur due to snow falling out of the 411 bottom of the sampler (Turcan and Loijens, 1975). It is likely that this occurred during our study since a 412 large portion of the lower elevation snow on both Glaciers 2 and 13 was melt affected and thin, allowing for 413 easier lateral displacement of the snow as the sampler was extracted. For example, on Glacier 13 the snow 414 surface had been affected by radiation melt (especially at lower elevations where the snow was shallower) 415 and the surface would collapse when the sampler was inserted into the snow. It is also difficult to measure 416 the weight of the sampler and snow with the spring scale when there was little snow because the weight was 417 at the lower limit of what could be detected by the scale. Therefore, FS appears to oversample in deep snow 418 due to compaction and/or shaving snow and to undersample in shallow snow due to snow falling out of the 419 sampling tube. 420

#### Distributed density 421

We choose four different density interpolation methods and separate SP and FS measurements for a total of 422 eight density interpolation options. Despite the wide range of measured density values and different types of 423 density interpolation, density does not appear to strongly affect winter balance estimates and is usually not 424 the dominant source of winter balance uncertainty. Our preferred density interpolation is to use a glacier-425 wide mean of SP densities. Many winter balance studies assume uniform density (e.g. Elder and others, 1991; 426 McGrath and others, 2015; Cullen and others, 2017) and it is realistic for future studies to measure snow 427 density profiles at a few locations in the study basin. SP measurements are chosen over FS measurements 428 because of the bias observed in FS densities. However, using a glacier-wide mean snow density omits known 429 430

spatial variability in snow density (Wetlaufer and others, 2016).

# 431 Grid cell average

The zigzag sampling scheme offers a relatively easy way to take a large number of probe measurements in 432 order to capture spatial variability of SWE in a grid cell. While the distribution of SWE values at each 433 zigzag is qualitatively consistent in our study, future studies would benefit from increasing the number of 434 zigzags and focusing on areas with both high variability (e.g. debris covered ice) and low variability (e.g. 435 accumulation area) to determine how variability differs across the glacier. 436 Since such a large number of points are needed to characterize the variability in a grid cell there is little 437 advantage to measuring and then averaging snow depth at multiple measurement locations. Rather, time 438 should be spent extensively characterizing grid-cell variability in a few locations and to then decrease the 439 spacing of transect measurements to extend their spatial coverage over the glacier. In our study, the grid cell 440 variability appeared to be captured with dense sampling in select grid cells but the basin-scale variability 441 was not captured because sampling was limited to the ablation area. By decreasing transect spacing, grid 442

# 444 Interpolated SWE

445 Linear regression

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- Elevation is the only topographic parameter that offered insight into topographic controls on accumulation.
- Even so, elevation had little predictive ability for Glacier 4 and the correlation was moderate on Glacier
- 448 13. It is possible that the elevation correlation was accentuated, especially on Glacier 13, during the field
- campaign due to warmer than normal temperatures and an early (1-2 weeks) start to the melt season
- 450 (Yukon Snow Survey Bulletin and Water Supply Forecast, May 1, 2016). The southwestern Yukon winter
- 451 snow pack in 2015 was also well below average, possibly emphasizing effects of early melt onset.

cells would only have one or two measurements but more grid cells could be measured.

Our mixed insights into dominant predictors of accumulation are consistent with the conflicting results 452 present in the literature. Many winter balance studies have found elevation to be the most significant 453 predictor of SWE (e.g. Machguth and others, 2006; McGrath and others, 2015). However, accumulation-454 elevation gradients vary considerably between glaciers (Winther and others, 1998) and other factors, such as 455 orientation relative to dominant wind direction and glacier shape, have been noted to affect accumulation 456 distribution (Machguth and others, 2006; Grabiec and others, 2011). Machguth and others (2006), Grünewald 457 and others (2014) and Kirchner and others (2014) observed elevation trends in snow accumulation for the 458 lower parts of their study basins but no correlation or even a decrease in SWE with elevation for the upper 459 portion of their basins. Helbig and van Herwijnen (2017) suggest that an increase in accumulation with 460

elevation can better be approximated by a power law (of the form  $y = ax^k$  with k 1). There are also a number of accumulation studies on glaciers that found no significant correlation between accumulation and topographic parameters and the highly variable snow distribution was attributed to complex local conditions (e.g. Grabiec and others, 2011; López-Moreno and others, 2011).

Wind redistribution and preferential deposition of snow is known to have a large influence on accumulation at sub-basin scales(Dadic and others, 2010; Winstral and others, 2013). The wind redistribution parameter

466 used in our study is found to be a small but significant predictor of accumulation on Glacier 4 (negative 467 correlation) and Glacier 2 (positive correlation). This result indicates that wind likely has an impact on 468 snow distribution but that the wind redistribution parameter is perhaps not the most appropriate way to 469 characterize the effect of wind on our study glaciers. For example, Glacier 4 is located in a curved valley 470 with steep side walls so having a single cardinal direction for wind may be inappropriate. Examining wind 471 redistribution parameter values that assume wind moving up or down glacier and changing direction to follow 472 the valley could allow the wind redistribution parameter to explain more of the variance in SWE. Further, 473 the scale of deposition may be smaller than the resolution of the Sx parameter in the relatively large DEM 474 475 grid cells in our study. An investigation of the wind redistribution parameter with finer DEM resolution is also needed. Our results corroborate McGrath and others (2015), who completed a winter balance study on 476 six Alaskan glaciers (DEM resolutions of 5m) and found that Sx was the only other significant parameter, 477 besides elevation, for all glaciers. Regression coefficients were small (< 0.3) and in some cases, negative. 478 Sublimation from blowing snow has also been shown to be an important mass loss from ridges (Musselman 479 and others, 2015). Incorporating snow loss as well as redistribution and preferential deposition may be needed 480 for accurate representations of seasonal accumulation. 481

Since we are unable to measure SWE in grid cells that have high topographic parameter values, we must extrapolate relationships linearly. The accumulation area, where there are few observations, is most susceptible to extrapolation errors. This area typically also has the highest SWE values, affecting the specific winter balance estimated for the glacier. In our study, the dependence of SWE on elevation, especially on Glacier 2, means that LR extrapolation results in almost 2 m w.e. estimated in the parts of the accumulation area. This exceptionally large estimate of SWE is unlikely for a continental snow pack. Extrapolating a LR that is fitted to predominantly ablation area SWE values is likely erroneous.

While a LR can be used to predict distributed SWE in other basins, we found that transfer of LR coefficients between glaciers results in large estimation error. Applying LR coefficients to unmeasured basins therefore

results in high winter balance uncertainty. The LR fitted to all observed data produced the best overall predictor of SWE in the Donjek Range. Our results are consistent with Grünewald and others (2013), who found that local statistical models are able to perform well but they cannot be transferred to different regions and that regional-scale models are not able to explain the majority of variance. The inter-basin variability in our study range is greater than the intra-basin variability.

#### 496 Simple kriging

For all study glaciers, simple kriging (SK) is a better predictor of observed SWE than LR. However, the winter balance uncertainty that arises from using SK is large, and unrealistic values of 0 m w.e. winter balance can be estimated. Our observations are generally limited to the ablation area so SK estimates an almost uniform distribution of SWE in the accumulation areas of the study glaciers, which is inconsistent with observations described in the literature (e.g. Machguth and others, 2006; Grabiec and others, 2011). Extrapolation using SK leads to large uncertainty in estimating winter balance, which further emphasis the need for SWE observations in the accumulation area.

SK cannot be used to understand physical processes that may be controlling snow distribution and cannot be used to estimate accumulation beyond the study area. However, fitted kriging parameters, including the nugget and spatial correlation length, can provide insight into important scales of variability. Glaciers 2 and large long correlation lengths and small nuggets indicating variability at large scales. Conversely, Glacier 4 has a short correlation length and large nugget, indicating that accumulation variability occurs at small scales. Using a higher resolution sampling design and DEM may allow us to capture more of the variability on Glacier 4 and to perhaps improve the predictive ability of both LR and SK interpolation.

A number of studies that relate SWE to topographic parameters have found success when using a regression tree interpolation model, which is a non-linear regression method (e.g. Elder and others, 1998; Erickson and others, 2005; López-Moreno and others, 2010). Many relationships between accumulation and topographic parameters have been observed to be non-linear so regression tree are valuable in snow modelling and may vield improved results (Erxleben and others, 2002; Molotch and others, 2005).

# 516 Quantifying effects of variability

Interpolation uncertainty is the greatest contributor to winter balance uncertainty for both SK and LR. A large contributor to uncertainty arises from extrapolation beyond the sampled region, which results in high uncertainty in estimated SWE in the accumulation area. The winter balance distributions obtained using LR and SK overlap for each glacier but the distribution modes differ, with SK generally estimating lower winter

balance in the accumulation area, which lowers the overall winter balance estimate. It is important to note 521 that although the distributions from LR are narrower than those from SK, that does not necessitate that 522 LR is a more accurate method of estimating winter balance. Based on the sources of uncertainty chosen, LR 523 appears to be more precise than SK but the methods of calculating interpolation uncertainty are different 524 so the distributions should not be directly compared. 525 526 SWE uncertainty is the smallest contributor to winter balance uncertainty. Therefore, obtaining the most accurate value of SWE to represent a grid cell, even a relatively large grid cell, does not need to be a priority 527 when designing a snow survey. Many parts of a glacier are characterized by a relatively smooth surface, with 528 roughness lengths on the order of centimeters (Hock, 2005) resulting in low snow depth uncertainty. However, 529 we assume that the sampled grid cells are representative of the uncertainty across the entire glacier, which 530 is likely not true for areas with debris cover, crevasses and steep slopes. 531 Using a Monte Carlo experiment to propagate uncertainty allowed us to quantify effects of uncertainty on 532 estimates of winter balance. However, our analysis did not include uncertainty arising from a number of data 533 sources, which we assumed to contribute negligibly to the uncertainty in winter balance or to be encompassed 534 535 by investigated sources of uncertainty. These sources of uncertainty include error associated with SP and FS density measurement, DEM vertical and horizontal error and error associated with estimating measurement 536

# Mountain range accumulation gradient

locations.

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An accumulation gradient is observed for the continental side of the St. Elias Mountains (Figure 11). 539 Accumulation data are compiled from Taylor-Barge (1969), the three glaciers presented in this paper, as 540 well as two snow pits we dug near the head of the Kaskawalsh Glacier in May 2016. The data show a 541 linear decrease in observed SWE as distance from the main mountain divide (identified by Taylor-Barge 542 (1969)) increases, with a gradient of -0.024 m w.e. km<sup>-1</sup>. While the three study glaciers fit the regional 543 relationship, the same relationship would not apply when just the Donjek Range is considered. Therefore, 544 glacier location within a mountain range also affects glacier-wide winter balance. Interaction between meso-545 scale weather patterns and mountain topography is a major driver of glacier-wide accumulation. Further 546 insight into mountain-scale accumulation trends can be achieved by investigating moisture source trajectories 547 and orographic precipitation contribution to accumulation. 548

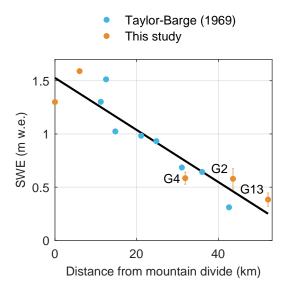


Fig. 11. Relation between SWE and linear distance from St. Elias mountain divide, located at the head of the Kaskawalsh Glacier. Blue dots are snow pit derived SWE values from Taylor-Barge (1969). Orange dots furthest from the divide are mean winter balance from Glaciers 4, 2 and 13, with 95% confidence interval using a linear regression interpolation. Orange dots close to the divide are snow pit derived SWE value at two locations in the accumulation area of the Kaskawalsh Glacier collect in May 2016. Black line indicates line of best fit ( $\mathbb{R}^2 = 0.85$ ).

#### 549 Limitations and future work

Extensions to this work could include an investigation of experimental design, examining the effects of DEM 550 grid size on winter balance and resolving temporal variability. Our sampling design was chosen to extensively 551 sample the ablation area and is likely too finely resolved for many future mass balance surveys to replicate. 552 Determining a sampling design that minimizes error and reduces the number of measurements, known as 553 data efficiency thresholds, would contribute to optimizing snow surveys in mountainous regions. For example, 554 López-Moreno and others (2010) concluded that 200 – 400 observations are needed to obtain accurate and 555 robust snow distribution models. 556 DEM grid cell size is known to significantly affect computed topographic parameters and the ability for 557 a DEM to resolve important hydrological features (i.e. drainage pathways) in the landscape (Zhang and 558 Montgomery, 1994; Garbrecht and Martz, 1994; Guo-an and others, 2001; López-Moreno and others, 2010), 559 which can have implications for calculating a LR that uses topographic parameters. Zhang and Montgomery 560 (1994) found that a 10 m grid cell size is an optimal compromise between increasing resolution and large data 561

volumes. Further, the importance of topographic parameters in predicting SWE is correlated with DEM grid 562 size (e.g. Kienzle, 2004; López-Moreno and others, 2010). A decrease in spatial resolution of the DEM results 563 in a decrease in the importance of curvature and an increase in the importance of elevation. A detailed and 564 ground controlled DEM is therefore needed to identify the features that drive accumulation variability. Even 565 with a high resolution DEM, microtopography that creates small scale snow variability cannot be resolved. 566 567 For example, the lower part of Glacier 2 has an undulating ice surface (on the order of 5 m horizontal and 0.5 m vertical) that results in large variability in snow depth. Future studies could also evaluate the effects of 568 DEM uncertainty on elevation and derived topographic parameters (e.g. Guo-an and others, 2001; Wechsler 569 and Kroll, 2006). 570 Temporal variability in accumulation is not considered in our study. While this limits the extent of our 571 conclusions, a number of studies have found temporal stability in spatial patterns of snow accumulation 572 and that terrain-based model could be applied reliable between years (e.g. Grünewald and others, 2013). 573 For example, Walmsley (2015) analyzed more than 40 years of accumulation recorded on two Norwegian 574 glaciers and found that snow accumulation is spatially heterogeneous yet exhibits robust time stability in its 575

# CONCLUSION

distribution.

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mountains from extensive snow depth and density sampling. Our objectives are to (1) examine methods and 579 uncertainties when moving from snow measurements to estimating winter balance and (2) show how snow 580 variability, data error and our methodological choices interact to create uncertainty in our estimate of winter 581 balance. 582 Overall, elevation is the dominant driver of SWE distribution but results vary between glaciers. 583 Accumulation spatial patterns and scales of variability are considerably different on Glacier 4 when compared 584 to Glaciers 2 and 13. Glaciers 2 and 13 have a dominant elevation-accumulation trend and long spatial 585 correlation lengths. No topographic parameters are able to explain snow distribution on Glacier 4 and 586 a short correlation length and large nugget indicate variability at shorter length scales. Our results also 587 suggest that wind redistribution and preferential distribution are significant drivers of SWE distribution but 588 these effects are not captured by the wind redistribution parameter used. Improved modelling of wind effects 589 on accumulation through modification of the wind redistribution parameter as well as increased physical 590 modelling are needed. A LR applied to our study glaciers resulted in little insight into dominant physical 591

We estimate spatial accumulation patterns and specific winter balance for three glaciers in the St. Elias

processes indicating that accumulation is controlled by complex interactions between topography and the atmosphere and that a finer resolution DEM is needed to resolve SWE distribution and potentially relevant topographic parameters, such as curvature and wind redistribution.

Glacier accumulation is strongly affected by interactions between topography and atmospheric processes at the basin- and range-scale. Although we could not conclusively identify processes at the basin scale due to low predictive ability of the LRs, there is a dominant trend in accumulation at the regional scale. We identify a clear linear decrease in SWE with increased distance from the main topographic divide along the continental side of the St. Elias Mountains. This trend indicates that glacier location within a mountain range has a large influence on winter balance. Further investigation of meso-scale weather patterns could provide insight into relevant processes that affect accumulation at the range scale.

We also quantify the effects of variability from density interpolation, grid cell SWE calculation as well as interpolation method on uncertainty in estimating winter balance. We conduct a Monte Carlo experiment to propagate variability through the process of estimating accumulation from snow measurements. The largest source of uncertainty in our study stems from variability in interpolation method, both within and between methods. We find that SK results in high uncertainty and the distribution of winter balance estimates encompasses unrealistic values. Spatial distribution of interpolation variability indicates that the accumulation area is the greatest area of uncertainty. This large variability is a result of the accumulation area being poorly sampled, sensitive to estimates of dominant regression coefficients, and having the largest values of estimated SWE within the glacier. Density and SWE variability are found to be small contributors to winter balance uncertainty. We conclude that the choice of interpolation method in combination with sampling design, especially in the accumulation area, has a major impact on the uncertainty in winter balance estimates.

Our thorough analysis of linear regression to estimate winter balance and rigorous approach to quantifying uncertainty has resulted in no significant insights into the controls on alpine glacier snow accumulation. Snow distribution patterns differed considerably between glaciers, highlighting strong inter- and intra-basin variability. Our results indicate that SWE interpolation uncertainty overshadows both measurement and density interpolation uncertainty for all glaciers. A universal predictor of distributed SWE continues to elude researchers and accumulation variability due to complex interactions between topography and the atmosphere needs to be further investigated at finer resolutions to better estimate winter balance.

# 621 References

- 622 Anderton S, White S and Alvera B (2004) Evaluation of spatial variability in snow water equivalent for a
- high mountain catchment. Hydrological Processes, 18(3), 435–453 (doi: 10.1002/hyp.1319)
- 624 Bagos PG and Adam M (2015) On the Covariance of Regression Coefficients. Open Journal of Statistics,
- **5**(07), 680 (doi: 10.4236/ojs.2015.57069)
- 626 Balk B and Elder K (2000) Combining binary decision tree and geostatistical methods to estimate snow dis-
- tribution in a mountain watershed. Water Resources Research, **36**(1), 13–26 (doi: 10.1029/1999WR900251)
- 628 Barry RG (1992) Mountain weather and climate. Psychology Press
- 629 Beauont RT and Work RA (1963) Snow sampling results from three sampler. International Association of
- 630 Scientific Hydrology. Bulletin, 8(4), 74–78 (doi: 10.1080/02626666309493359)
- 631 Bernhardt M, Zängl G, Liston G, Strasser U and Mauser W (2009) Using wind fields from a high-resolution
- atmospheric model for simulating snow dynamics in mountainous terrain. Hydrological processes, 23(7),
- 633 1064–1075 (doi: 10.1002/hyp.7208)
- 634 Berthier E, Arnaud Y, Kumar R, Ahmad S, Wagnon P and Chevallier P (2007) Remote sensing estimates
- of glacier mass balances in the Himachal Pradesh (Western Himalaya, India). Remote Sensing of
- 636 Environment, 108(3), 327–338
- 637 Blöschl G, Kirnbauer R and Gutknecht D (1991) Distributed snow melt simulations in an alpine catchment.
- 638 Water Resources Research, **27**(12), 3171–3179
- 639 Burnham KP and Anderson DR (2004) Multimodel Inference: Understanding AIC and BIC in Model
- Selection. Sociological Methods & Research, 33(2), 261–304 (doi: 10.1177/0049124104268644)
- 641 Clark MP, Hendrikx J, Slater AG, Kavetski D, Anderson B, Cullen NJ, Kerr T, Orn Hreinsson E and Woods
- RA (2011) Representing spatial variability of snow water equivalent in hydrologic and land-surface models:
- 643 A review. Water Resources Research, 47(7) (doi: 10.1029/2011WR010745)
- 644 Clarke GK, Collins SG and Thompson DE (1984) Flow, thermal structure, and subglacial conditions of a
- surge-type glacier. Canadian Journal of Earth Sciences, 21(2), 232–240 (doi: 10.1139/e84-024)
- 646 Clyde GD (1932) Circular No. 99-Utah Snow Sampler and Scales for Measuring Water Content of Snow
- 647 Cogley J, Hock R, Rasmussen L, Arendt A, Bauder A, Braithwaite R, Jansson P, Kaser G, Möller M,
- Nicholson L and others (2011) Glossary of glacier mass balance and related terms
- 649 Conger SM and McClung DM (2009) Comparison of density cutters for snow profile observations. Journal
- of Glaciology, **55**(189), 163–169

651 Crompton JW and Flowers GE (2016) Correlations of suspended sediment size with bedrock lithology and

- glacier dynamics. Annals of Glaciology, 1–9 (doi: 10.1017/aog.2016.6)
- 653 Cullen NJ, Anderson B, Sirguey P, Stumm D, Mackintosh A, Conway JP, Horgan HJ, Dadic R, Fitzsimons
- 654 SJ and Lorrey A (2017) An 11-year record of mass balance of Brewster Glacier, New Zealand, determined
- using a geostatistical approach. *Journal of Glaciology*, **63**(238), 199–217 (doi: 10.1017/jog.2016.128)
- 656 Dadic R, Mott R, Lehning M and Burlando P (2010) Parameterization for wind-induced preferen-
- 657 tial deposition of snow. Journal of Geophysical Research: Earth Surface (2003–2012), 115 (doi:
- 658 10.1029/2009JF001261)

- 659 Danby RK, Hik DS, Slocombe DS and Williams A (2003) Science and the St. Elias: an evolving framework
- 660 for sustainability in North America's highest mountains. The Geographical Journal, 169(3), 191–204 (doi:
- 661 10.1111/1475-4959.00084)
- 662 Davis JC and Sampson RJ (1986) Statistics and data analysis in geology, volume 646. Wiley New York et al.
- 663 Deems JS and Painter TH (2006) Lidar measurement of snow depth: accuracy and error sources. In
- 664 Proceedings of the International Snow Science Workshop, 1–6
- 665 Dixon D and Boon S (2012) Comparison of the SnowHydro snow sampler with existing snow tube designs.
- 666 Hydrological Processes, **26**(17), 2555–2562, ISSN 1099-1085 (doi: 10.1002/hyp.9317)
- 667 Egli L, Griessinger N and Jonas T (2011) Seasonal development of spatial snow-depth variability across dif-
- 668 ferent scales in the Swiss Alps. Annals of Glaciology, **52**(58), 216–222 (doi: 10.3189/172756411797252211)
- 669 Elder K, Dozier J and Michaelsen J (1991) Snow accumulation and distribution in an alpine watershed.
- 670 Water Resources Research, 27(7), 1541–1552 (doi: 10.1029/91WR00506)
- 671 Elder K, Rosenthal W and Davis RE (1998) Estimating the spatial distribution of snow water equivalence
- in a montane watershed.  $Hydrological\ Processes,\ 12(1011),\ 1793-1808\ (doi:\ 10.1002/(SICI)1099-1808)$
- 673 1085(199808/09)12:10/11;1793::AID-HYP695;3.0.CO;2-)
- 674 Erickson TA, Williams MW and Winstral A (2005) Persistence of topographic controls on the spatial
- distribution of snow in rugged mountain terrain, Colorado, United States. Water Resources Research,
- 676 **41**(4) (doi: 10.1029/2003WR002973)
- 677 Erxleben J, Elder K and Davis R (2002) Comparison of spatial interpolation methods for estimating
- snow distribution in the Colorado Rocky Mountains. Hydrological Processes, 16(18), 3627–3649 (doi:
- 679 10.1002/hyp.1239)

- 680 Fames PE, Peterson N, Goodison B and Richards RP (1982) Metrication of Manual Snow Sampling
- Equipment. In Proceedings of the 50th Western Snow Conference, 120–132
- 682 Fierz C, Armstrong RL, Durand Y, Etchevers P, Greene E, McClung DM, Nishimura K, Satyawali PK
- and Sokratov SA (2009) The international classification for seasonal snow on the ground, volume 25.
- 684 UNESCO/IHP Paris

- 685 Garbrecht J and Martz L (1994) Grid size dependency of parameters extracted from digital elevation models.
- 686 Computers & Geosciences, **20**(1), 85–87, ISSN 0098-3004 (doi: 10.1016/0098-3004(94)90098-1)
- 687 Godio A and Rege R (2016) Analysis of georadar data to estimate the snow depth distribution. Journal of
- 688 Applied Geophysics, **129**, 92–100 (doi: 10.1016/j.jappgeo.2016.03.036)
- 689 Grabiec M, Puczko D, Budzik T and Gajek G (2011) Snow distribution patterns on Svalbard glaciers derived
- from radio-echo soundings. Polish Polar Research, **32**(4), 393–421 (doi: 10.2478/v10183-011-0026-4)
- 691 Gray DM and Male DH (1981) Handbook of snow: principles, processes, management & use. Pergamon Press
- 692 Grunewald T, Schirmer M, Mott R and Lehning M (2010) Spatial and temporal variability of snow depth
- and ablation rates in a small mountain catchment. Cryosphere, 4(2), 215–225 (doi: 10.5194/tc-4-215-2010)
- 694 Grünewald T, Stötter J, Pomeroy J, Dadic R, Moreno Baños I, Marturià J, Spross M, Hopkinson C, Burlando
- 695 P and Lehning M (2013) Statistical modelling of the snow depth distribution in open alpine terrain.
- 696 Hydrology and Earth System Sciences, 17(8), 3005–3021 (doi: 10.5194/hess-17-3005-2013)
- 697 Grünewald T, Bühler Y and Lehning M (2014) Elevation dependency of mountain snow depth. The
- 698 Cryosphere, 8(6), 2381–2394 (doi: 10.5194/tc-8-2381-2014)
- 699 Guo-an T, Yang-he H, Strobl J and Wang-qing L (2001) The impact of resolution on the accuracy of
- 700 hydrologic data derived from DEMs. Journal of Geographical Sciences, 11(4), 393–401, ISSN 1861-9568
- 701 (doi: 10.1007/BF02837966)
- 702 Gusmeroli A, Wolken GJ and Arendt AA (2014) Helicopter-borne radar imaging of snow cover on and around
- 703 glaciers in Alaska. Annals of Glaciology, 55(67), 78–88 (doi: 10.3189/2014AoG67A029)
- 704 Helbig N and van Herwijnen A (2017) Subgrid parameterization for snow depth over mountainous
- terrain from flat field snow depth. Water Resources Research, 53(2), 1444–1456, ISSN 0043-1397 (doi:
- 706 10.1002/2016WR019872)
- 707 Hock R (2005) Glacier melt: a review of processes and their modelling. Progress in Physical Geography.
- **29**(3), 362–391 (doi: 10.1191/0309133305pp453ra)

709 Hock R and Jensen H (1999) Application of kriging interpolation for glacier mass balance computations.

- 710 Geografiska Annaler: Series A, Physical Geography, **81**(4), 611–619 (doi: 10.1111/1468-0459.00089)
- 711 Hofierka J, Mitášová H and Neteler M (2009) Geomorphometry in GRASS GIS. Developments in Soil Science,
- **33**, 387–410 (doi: 10.1016/S0166-2481(08)00017-2)
- 713 Kaser G, Fountain A, Jansson P and others (2003) A manual for monitoring the mass balance of mountain
- 714 *qlaciers*. Unesco Paris

- 715 Kienzle S (2004) The Effect of DEM Raster Resolution on First Order, Second Order and Compound Terrain
- Derivatives. Transactions in GIS, 8(1), 83–111, ISSN 1467-9671 (doi: 10.1111/j.1467-9671.2004.00169.x)
- 717 Kirchner PB, Bales RC, Molotch NP, Flanagan J and Guo Q (2014) LiDAR measurement of seasonal snow
- accumulation along an elevation gradient in the southern Sierra Nevada, California. Hydrology and Earth
- 719 System Sciences, **18**(10), 4261–4275, ISSN 1027-5606
- 720 Kohavi R and others (1995) A study of cross-validation and bootstrap for accuracy estimation and model
- selection. In Proceedings of the Fourteenth International Joint Conference on Artificial Intelligence,
- volume 14, 1137–1145
- 723 Korona J, Berthier E, Bernard M, Rémy F and Thouvenot E (2009) SPIRIT SPOT 5 stereoscopic survey
- of Polar Ice: Reference images and topographies during the fourth International Polar Year (2007–2009).
- 725 ISPRS Journal of Photogrammetry and Remote Sensing, 64(2), 204–212
- 726 Lehning M, Völksch I, Gustafsson D, Nguyen TA, Stähli M and Zappa M (2006) ALPINE3D: a detailed
- model of mountain surface processes and its application to snow hydrology. Hydrological processes, 20(10),
- 728 2111-2128
- 729 Lehning M, Löwe H, Ryser M and Raderschall N (2008) Inhomogeneous precipitation distribution and snow
- transport in steep terrain. Water Resources Research, 44(7) (doi: 10.1029/2007WR006545)
- 731 Li J and Heap AD (2008) A review of spatial interpolation methods for environmental scientists No. Record
- 732 2008/23. Geoscience Australia
- 733 Liston GE and Elder K (2006) A distributed snow-evolution modeling system (SnowModel). Journal of
- 734 Hydrometeorology, **7**(6), 1259–1276 (doi: 10.1175/JHM548.1)
- 735 López-Moreno J, Latron J and Lehmann A (2010) Effects of sample and grid size on the accuracy and
- stability of regression-based snow interpolation methods. Hydrological Processes, 24(14), 1914–1928, ISSN
- 737 1099-1085 (doi: 10.1002/hyp.7564)

- 738 López-Moreno J, Fassnacht S, Heath J, Musselman K, Revuelto J, Latron J, Morán-Tejeda E and Jonas T
- 739 (2013) Small scale spatial variability of snow density and depth over complex alpine terrain: Implications
- for estimating snow water equivalent. Advances in Water Resources, 55, 40–52, ISSN 0309-1708 (doi:
- 741 10.1016/j.advwatres.2012.08.010), snow-Atmosphere Interactions and Hydrological Consequences
- 742 López-Moreno JI, Fassnacht S, Beguería S and Latron J (2011) Variability of snow depth at the plot scale:
- implications for mean depth estimation and sampling strategies. The Cryosphere, 5(3), 617–629 (doi:
- 744 10.5194/tc-5-617-2011)

- 745 MacDougall AH and Flowers GE (2011) Spatial and temporal transferability of a distributed energy-balance
- 746 glacier melt model. Journal of Climate, 24(5), 1480–1498 (doi: 10.1175/2010JCLI3821.1)
- Machguth H, Eisen O, Paul F and Hoelzle M (2006) Strong spatial variability of snow accumulation observed
- with helicopter-borne GPR on two adjacent Alpine glaciers. Geophysical Research Letters, 33(13) (doi:
- 749 10.1029/2006GL026576)
- 750 Madigan D and Raftery AE (1994) Model Selection and Accounting for Model Uncertainty in Graphical
- Models Using Occam's Window. Journal of the American Statistical Association, 89(428), 1535–1546,
- 752 ISSN 01621459
- 753 Marshall HP, Koh G, Sturm M, Johnson J, Demuth M, Landry C, Deems J and Gleason J (2006) Spatial
- variability of the snowpack: Experiences with measurements at a wide range of length scales with several
- different high precision instruments. In *Proceedings ISSW*, 359–364
- 756 McGrath D, Sass L, O'Neel S, Arendt A, Wolken G, Gusmeroli A, Kienholz C and McNeil C (2015) End-
- of-winter snow depth variability on glaciers in Alaska. Journal of Geophysical Research: Earth Surface,
- 758 **120**(8), 1530–1550 (doi: 10.1002/2015JF003539)
- 759 Metropolis N and Ulam S (1949) The Monte Carlo Method. Journal of the American Statistical Association,
- 760 **44**(247), 335–341, ISSN 01621459
- 761 Mitášová H and Hofierka J (1993) Interpolation by regularized spline with tension: II. Application to terrain
- modeling and surface geometry analysis. *Mathematical Geology*, **25**(6), 657–669 (doi: 10.1007/BF00893172)
- 763 Molotch N, Colee M, Bales R and Dozier J (2005) Estimating the spatial distribution of snow water equivalent
- in an alpine basin using binary regression tree models: the impact of digital elevation data and independent
- variable selection. *Hydrological Processes*, **19**(7), 1459–1479 (doi: 10.1002/hyp.5586)
- 766 Mott R, Faure F, Lehning M, Löwe H, Hynek B, Michlmayer G, Prokop A and Schöner W (2008) Simulation
- of seasonal snow-cover distribution for glacierized sites on Sonnblick, Austria, with the Alpine 3D model.

- 768 Annals of Glaciology, **49**(1), 155–160 (doi: 10.3189/172756408787814924)
- 769 Musselman KN, Pomeroy JW, Essery RL and Leroux N (2015) Impact of windflow calculations on simulations
- of alpine snow accumulation, redistribution and ablation. Hydrological Processes, 29(18), 3983–3999 (doi:
- 771 10.1002/hyp.10595)

- 772 Nolan M, Larsen C and Sturm M (2015) Mapping snow-depth from manned-aircraft on landscape scales
- at centimeter resolution using Structure-from-Motion photogrammetry. The Cryosphere Discussions, 9,
- 774 333–381 (doi: 10.5194/tcd-9-333-2015)
- 775 Olaya V (2009) Basic land-surface parameters. Developments in Soil Science, 33, 141–169
- 776 Paoli LD and Flowers GE (2009) Dynamics of a small surge-type glacier using one-dimensional geophysical
- inversion. Journal of Glaciology, **55**(194), 1101–1112 (doi: 10.3189/002214309790794850)
- 778 Raftery AE, Madigan D and Hoeting JA (1997) Bayesian Model Averaging for Linear Regression Models.
- Journal of the American Statistical Association, **92**(437), 179–191 (doi: 10.1080/01621459.1997.10473615)
- 780 Réveillet M, Vincent C, Six D and Rabatel A (2016) Which empirical model is best suited to simulate glacier
- mass balances? *Journal of Glaciology*, 1–16 (doi: 10.1017/jog.2016.110)
- Roustant O, Ginsbourger D and Deville Y (2012) DiceKriging, DiceOptim: Two R packages for the analysis
- of computer experiments by kriging-based metamodeling and optimization. Journal of Statistical Software,
- 784 **21**, 1–55
- 785 Schneiderbauer S and Prokop A (2011) The atmospheric snow-transport model: SnowDrift3D. Journal of
- 786 Glaciology, **57**(203), 526–542 (doi: 10.3189/002214311796905677)
- 787 Shea C and Jamieson B (2010) Star: an efficient snow point-sampling method. Annals of Glaciology, 51(54),
- 788 64–72 (doi: 10.3189/172756410791386463)
- 789 Sold L, Huss M, Hoelzle M, Andereggen H, Joerg PC and Zemp M (2013) Methodological approaches to
- 790 infer end-of-winter snow distribution on alpine glaciers. Journal of Glaciology, 59(218), 1047–1059 (doi:
- 791 10.3189/2013JoG13J015)
- 792 Tangborn WV, Krimmel RM and Meier MF (1975) A comparison of glacier mass balance by glaciological,
- 793 hydrological and mapping methods, South Cascade Glacier, Washington. International Association of
- 794 Hydrological Sciences Publication, **104**, 185–196
- 795 Taylor-Barge B (1969) The summer climate of the St. Elias Mountain region. Technical report, DTIC
- 796 Document

797 Trujillo E and Lehning M (2015) Theoretical analysis of errors when estimating snow distribution through

- point measurements. The Cryosphere, 9(3), 1249–1264 (doi: 10.5194/tc-9-1249-2015)
- 799 Turcan J and Loijens H (1975) Accuracy of snow survey data and errors in snow sampler measurements. In
- 32nd Eastern Snow Conference, 2–11
- 801 Walmsley APU (2015) Long-term observations of snow spatial distributions at Hellstugubreen and
- 802 Gråsubreen, Norway

- Watson FG, Anderson TN, Newman WB, Alexander SE and Garrott RA (2006) Optimal sampling schemes
- for estimating mean snow water equivalents in stratified heterogeneous landscapes. Journal of Hydrology,
- **328**(3), 432–452 (doi: 10.1016/j.jhydrol.2005.12.032)
- 806 Wechsler SP and Kroll CN (2006) Quantifying DEM Uncertainty and its Effect on Topographic Parameters.
- Photogrammetric Engineering & Remote Sensing, 72(9), 1081–1090, ISSN 0099-1112
- 808 Wetlaufer K, Hendrikx J and Marshall L (2016) Spatial Heterogeneity of Snow Density and Its Influence
- on Snow Water Equivalence Estimates in a Large Mountainous Basin. Hydrology, 3(1), 3 (doi:
- 810 10.3390/hydrology3010003)
- 811 Winstral A, Elder K and Davis RE (2002) Spatial snow modeling of wind-redistributed snow using terrain-
- based parameters. Journal of Hydrometeorology, 3(5), 524–538
- 813 Winstral A, Marks D and Gurney R (2013) Simulating wind-affected snow accumulations at
- catchment to basin scales. Advances in Water Resources, 55, 64–79, ISSN 0309-1708 (doi:
- 10.1016/j.advwatres.2012.08.011), snow-Atmosphere Interactions and Hydrological Consequences
- Winther J, Bruland O, Sand K, Killingtveit A and Marechal D (1998) Snow accumulation distribution on
- Spitsbergen, Svalbard, in 1997. Polar Research, 17, 155–164
- 818 Woo MK and Marsh P (1978) Analysis of Error in the Determination of Snow Storage for
- Small High Arctic Basins. Journal of Applied Meteorology, 17(10), 1537–1541 (doi: 10.1175/1520-
- 820 0450(1978)017;1537:AOEITD;2.0.CO;2)
- Wood WA (1948) Project "Snow Cornice": the establishment of the Seward Glacial research station. Arctic,
- 822 107-112
- Work R, Stockwell H, Freeman T and Beaumont R (1965) Accuracy of field snow surveys. Technical report
- 824 Zhang W and Montgomery DR (1994) Digital elevation model grid size, landscape representation,
- and hydrologic simulations. Water Resources Research, 30(4), 1019–1028, ISSN 1944-7973 (doi:
- 826 10.1029/93WR03553)