

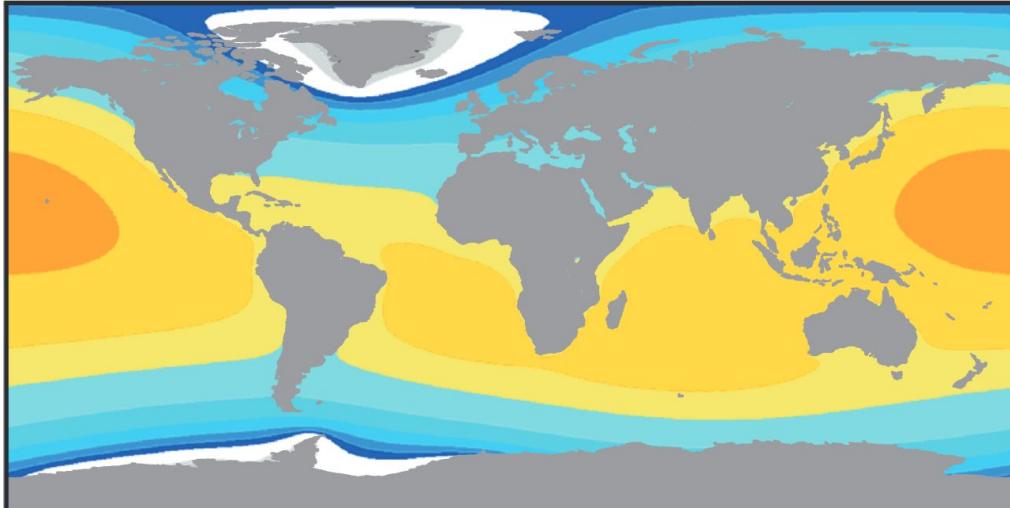
SFU



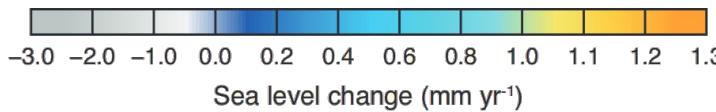
Senior supervisor: Gwenn Flowers  
Supervisor: Valentina Radić  
Supervisor: Kirsten Zickfeld  
External: Joseph Shea

# Multi-scale investigation of winter balance on alpine glaciers

# BACKGROUND

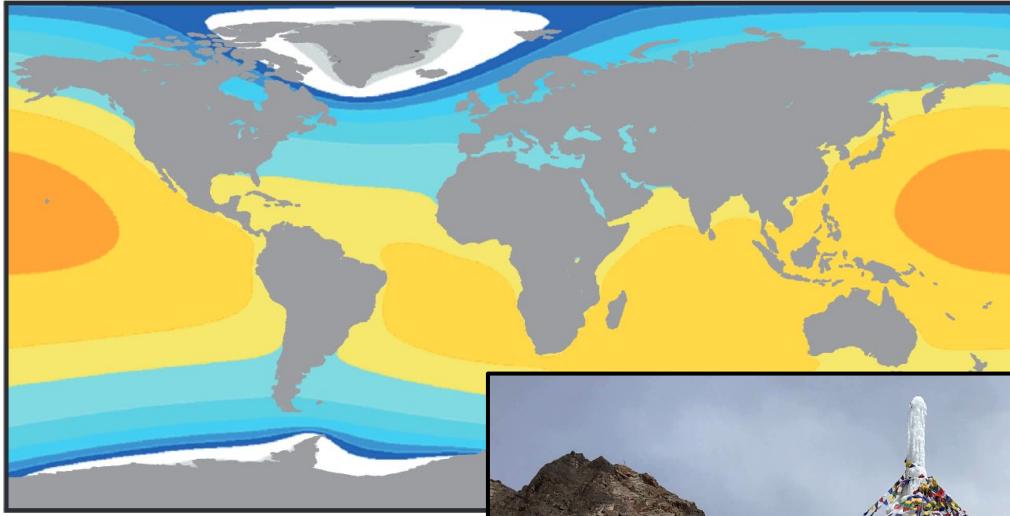


(IPCC 2013)



SEA LEVEL  
RISE

# BACKGROUND



(IPCC 2013)



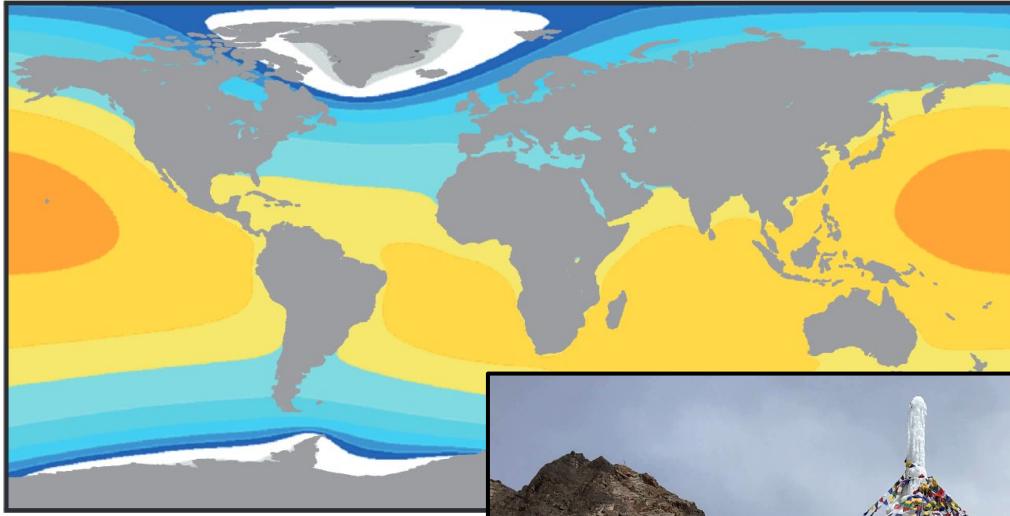
**WATER  
AVAILABILITY**

*(icestupa.org)*

**SEA LEVEL  
RISE**



# BACKGROUND



(IPCC 2013)



**WATER  
AVAILABILITY**

*(icestupa.org)*



**SEA LEVEL  
RISE**

**MONITOR GLACIERS**

# BACKGROUND

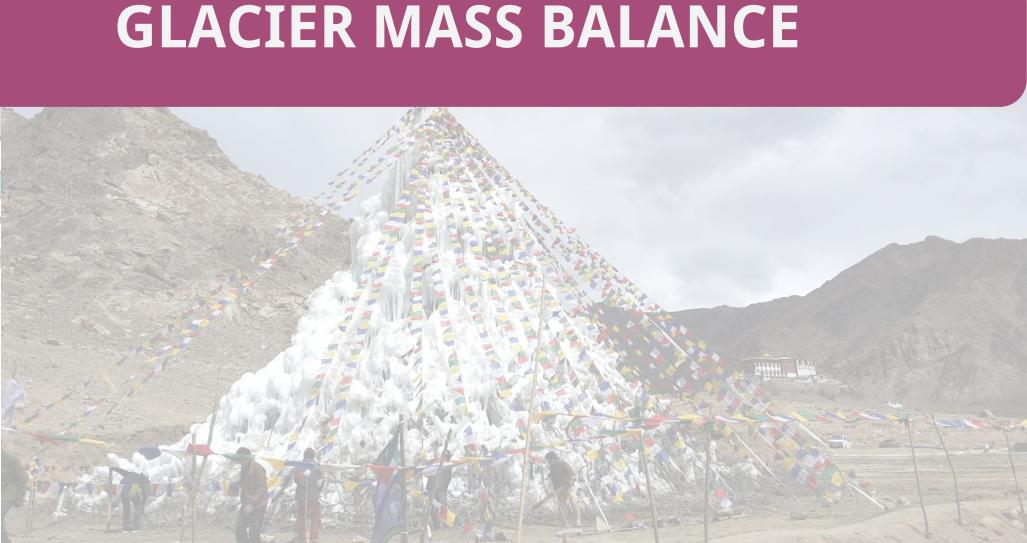


WATER  
AVAILABILITY

*(icestupa.org)*

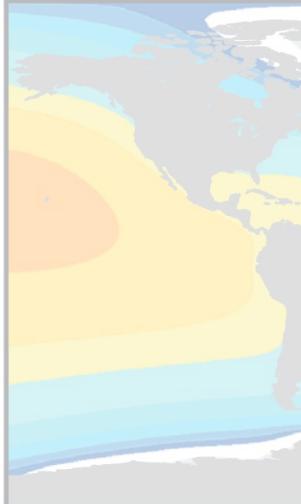
GLACIER MASS BALANCE

SEA LEVEL  
RISE

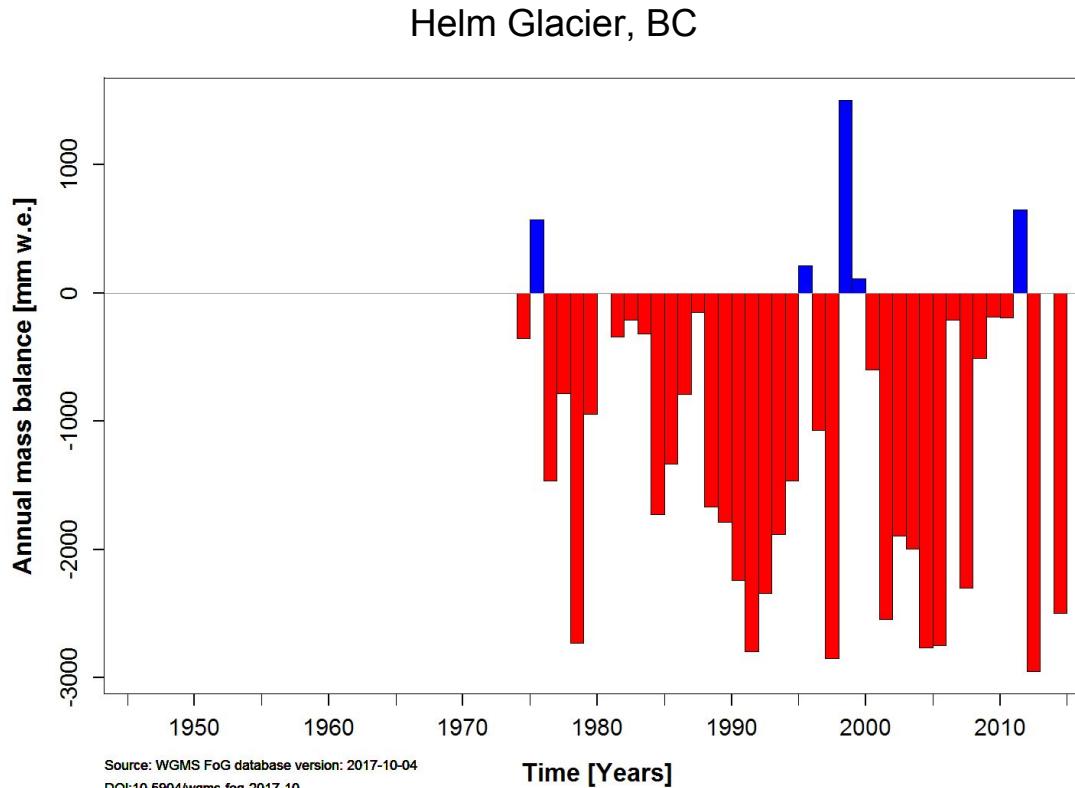


MONITOR GLACIERS

# BACKGROUND



WATER  
AVAILABILITY



MONITOR GLACIERS

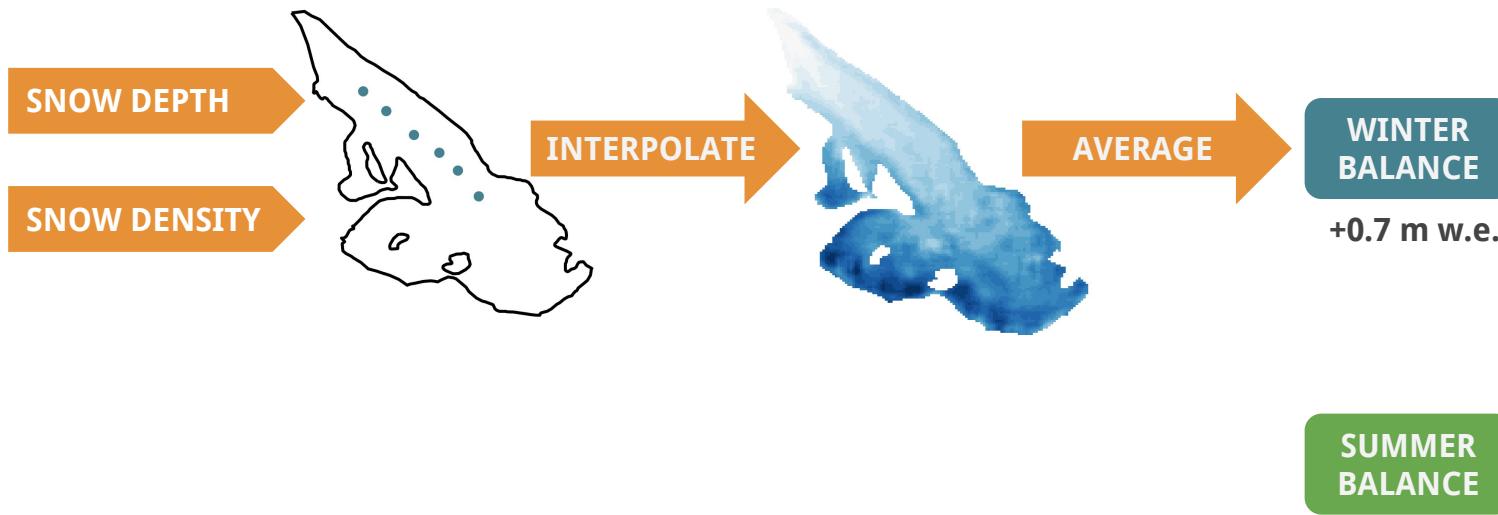
# BACKGROUND

WINTER  
BALANCE

SUMMER  
BALANCE

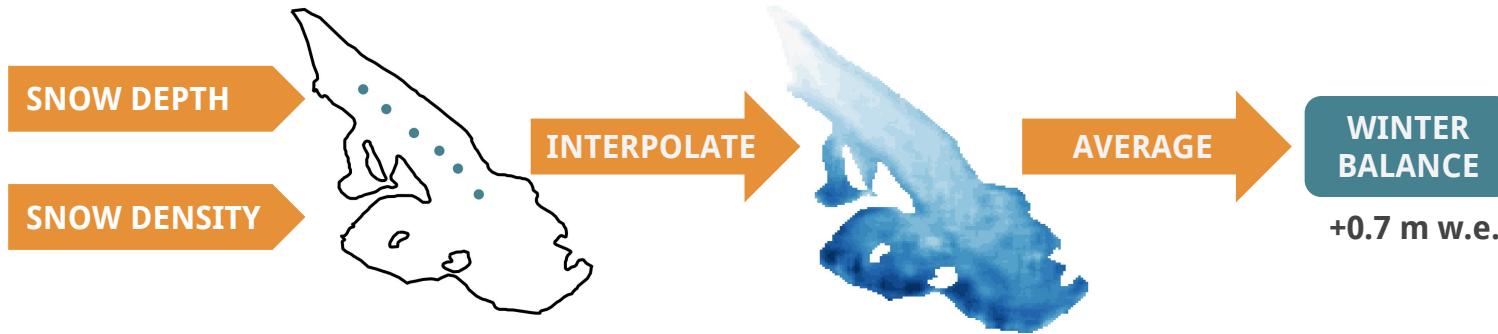
# BACKGROUND

END OF WINTER

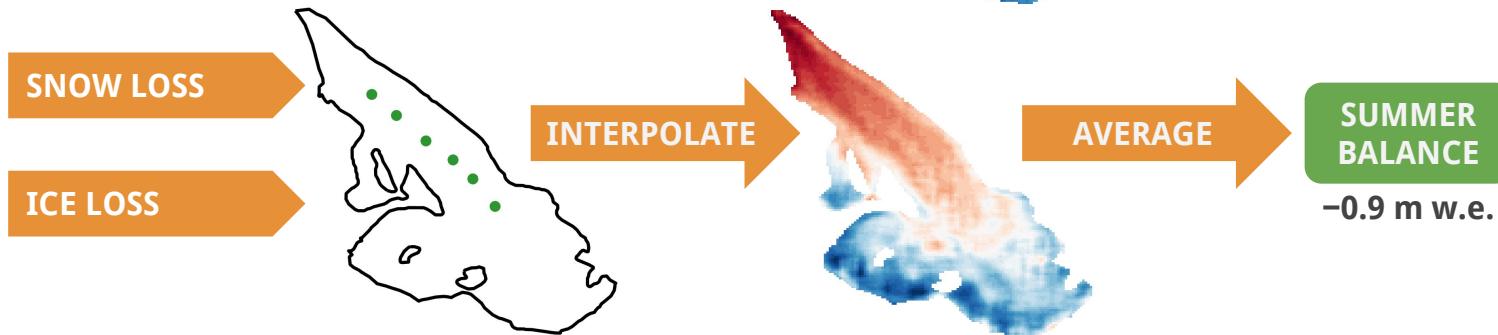


# BACKGROUND

END OF WINTER



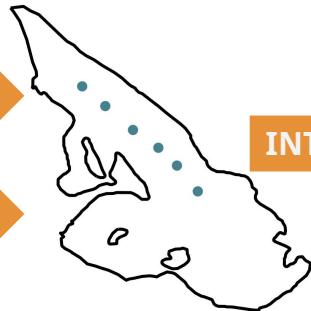
END OF SUMMER



# BACKGROUND

END OF WINTER

SNOW DEPTH



INTERPOLATE

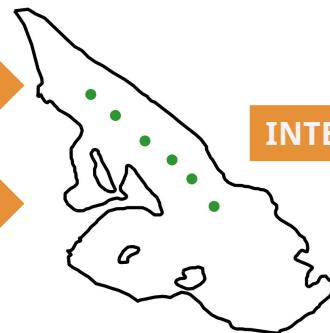


AVERAGE

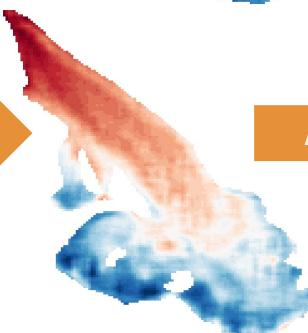
WINTER  
BALANCE

+0.7 m w.e.

SNOW DENSITY



INTERPOLATE



AVERAGE

SUMMER  
BALANCE

-0.9 m w.e.

SNOW LOSS

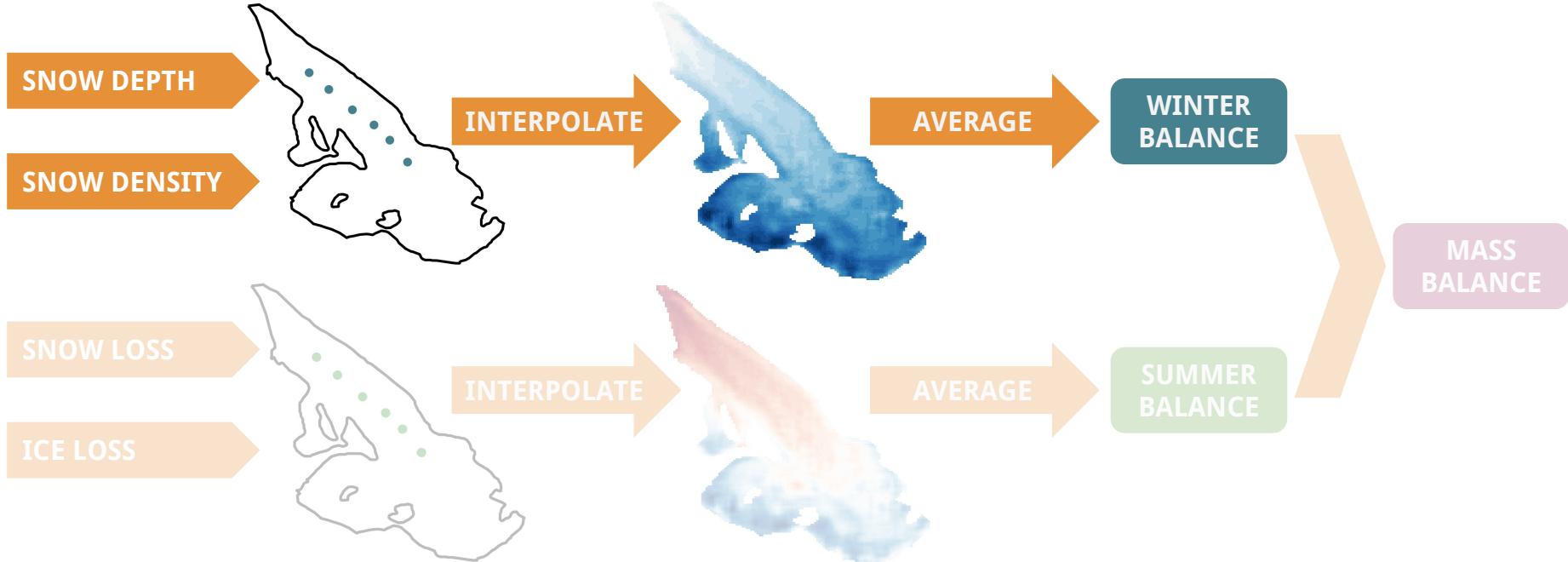
ICE LOSS

MASS  
BALANCE

-0.2 m w.e.

# BACKGROUND

END OF WINTER



# BACKGROUND

END OF WINTER



=



×



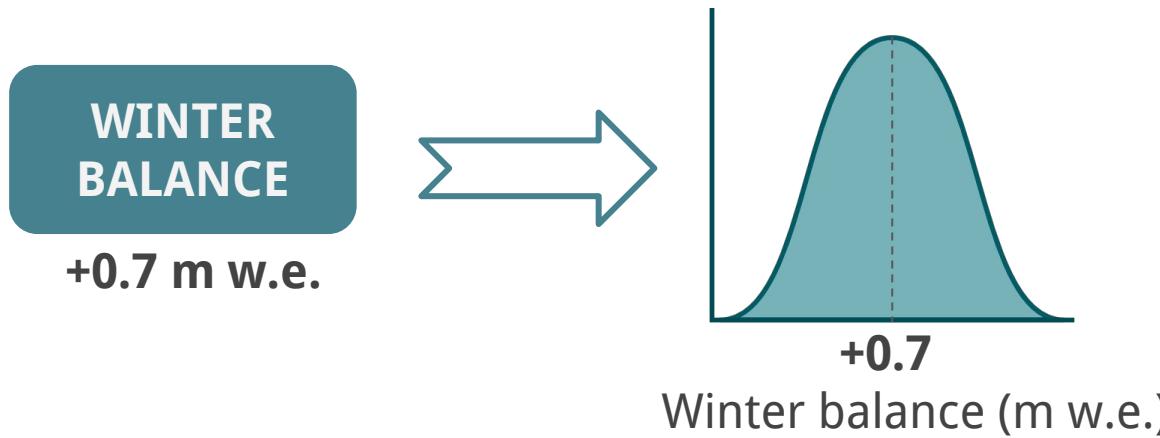
Units: meters water equivalent  
(m w.e.)

Probing  
GPR  
Repeat lidar

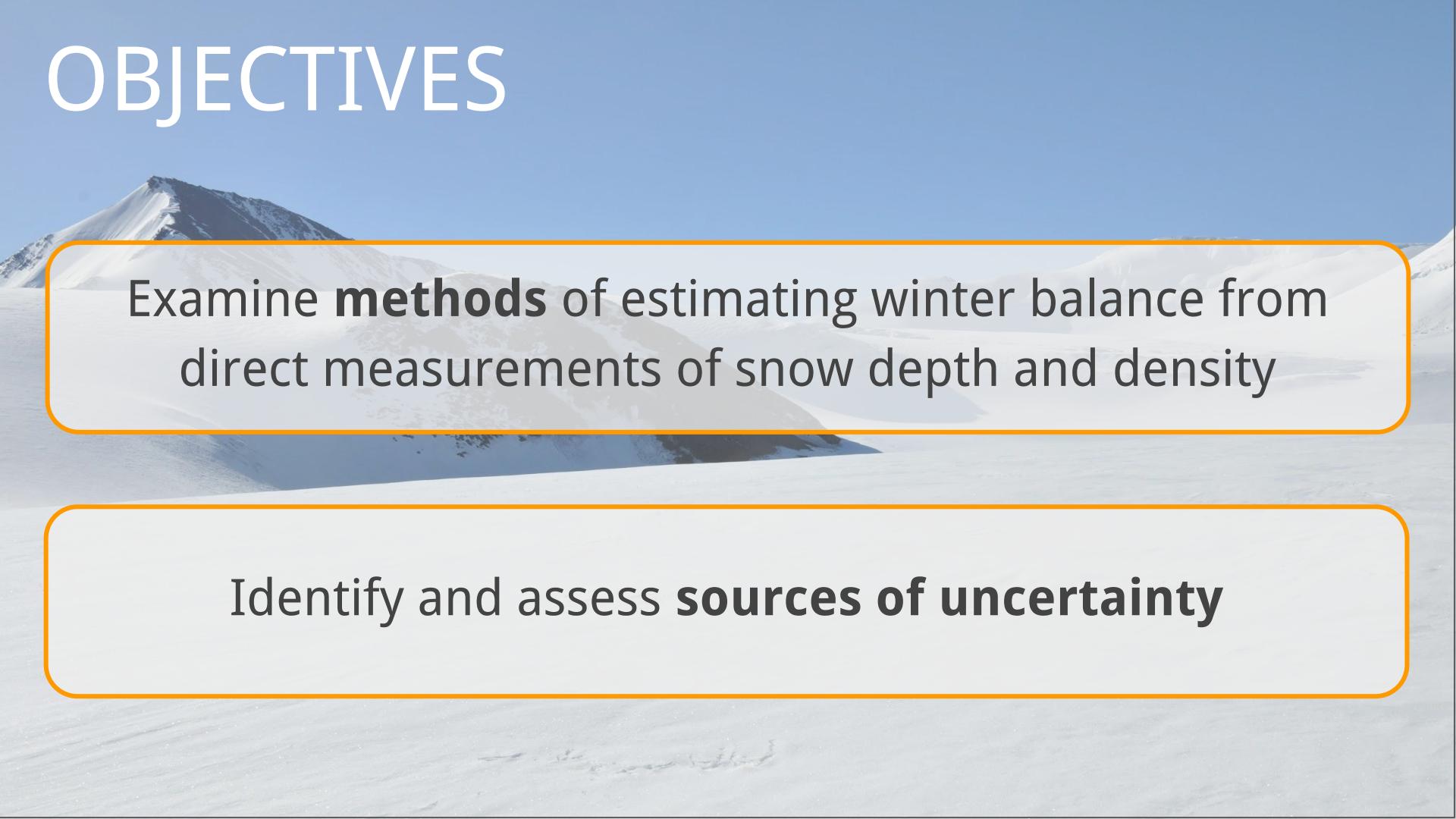
Snow pit  
Snow core

# BACKGROUND

END OF WINTER



# OBJECTIVES

The background of the slide features a wide-angle photograph of a mountainous landscape covered in white snow. The peaks are sharp and dark, contrasting with the bright snow and the clear, pale blue sky above.

Examine **methods** of estimating winter balance from direct measurements of snow depth and density

Identify and assess **sources of uncertainty**

# OBJECTIVE I

Examine **methods** of estimating winter balance from direct measurements of snow depth and density

END OF WINTER

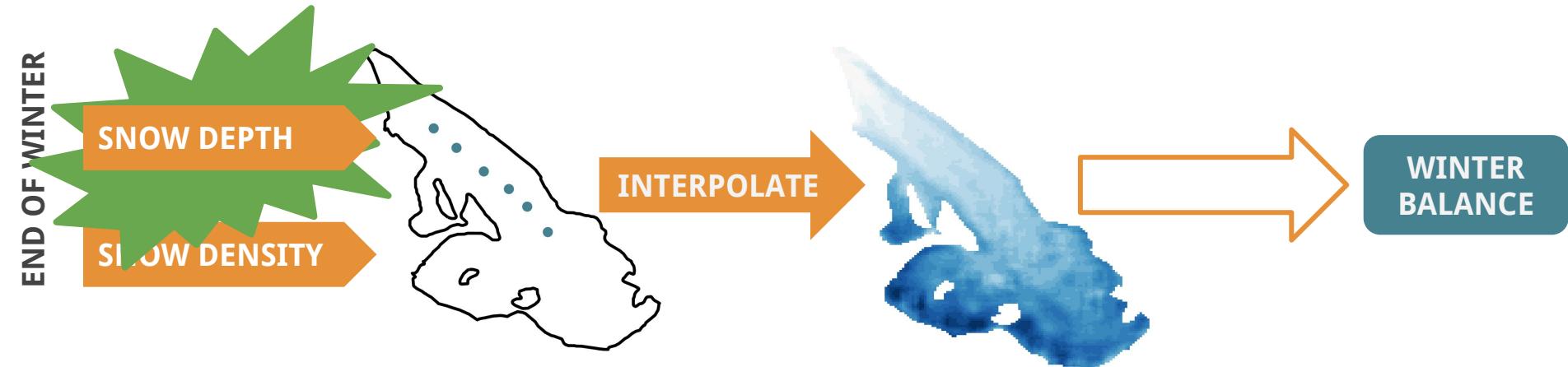
SNOW DEPTH

SNOW DENSITY

INTERPOLATE

WINTER  
BALANCE

# OBJECTIVE I



# SNOW DEPTH - METHODS

## SCALES OF VARIABILITY

Point scale



Gridcell scale



Basin scale

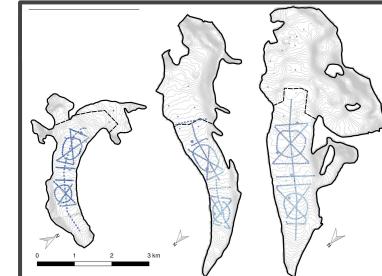
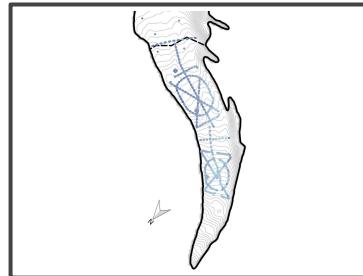
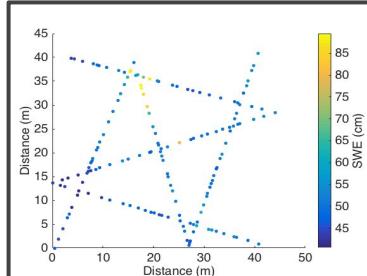


Regional scale



602 May 9

314	129	129	126	UM
315	133.5	133.5	133.5	
316	136	135	140.5	
317	143	143	142.5	
318	144	142	128	
319	129	150	130	
320	137	131	131.5	
321	150	149.5	155	
322	131	131	133	
323	119	125	154	

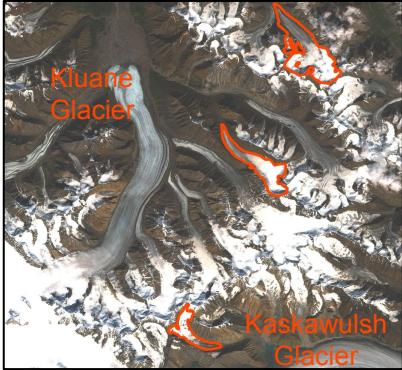


# SNOW DEPTH - METHODS

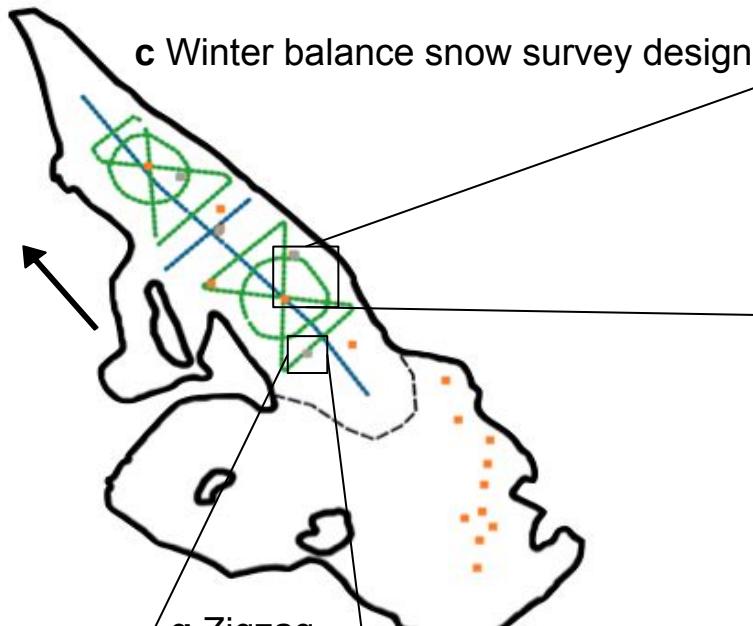
a Study site location



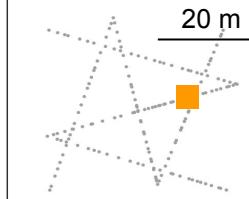
b Donjek Range



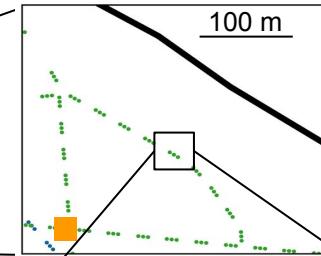
c Winter balance snow survey design



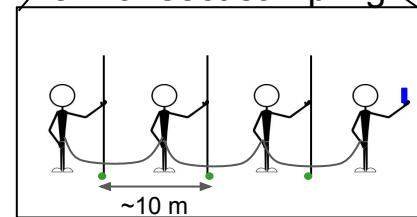
g Zigzag sampling



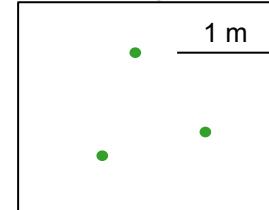
d Transects



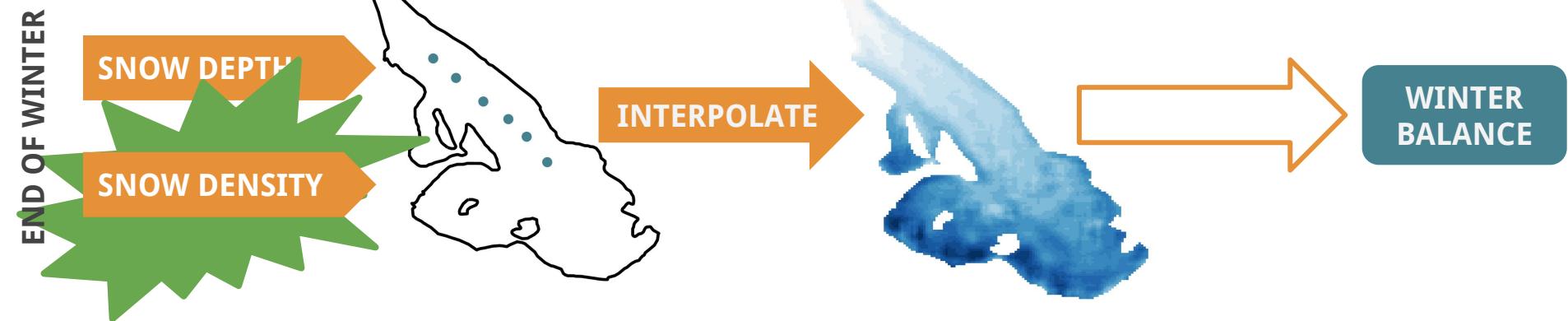
e Transect sampling



f Point-scale sampling



# OBJECTIVE I

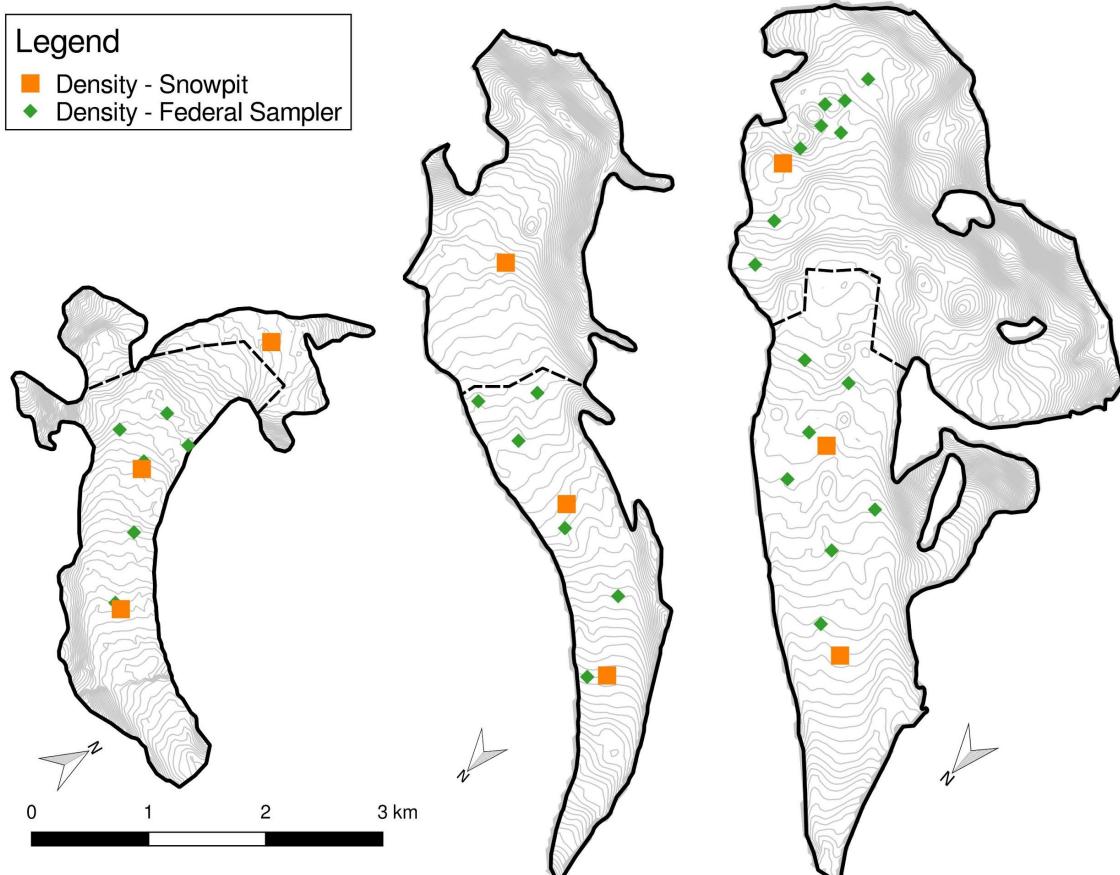


# SNOW DEPTH - METHODS

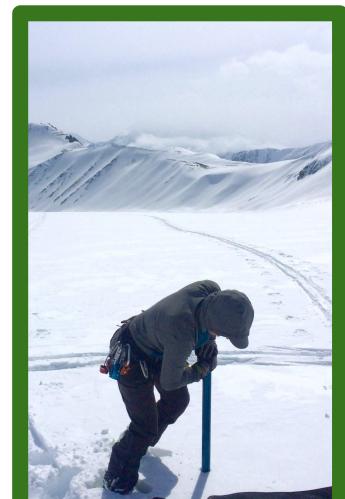


Legend

- Density - Snowpit
- ◆ Density - Federal Sampler

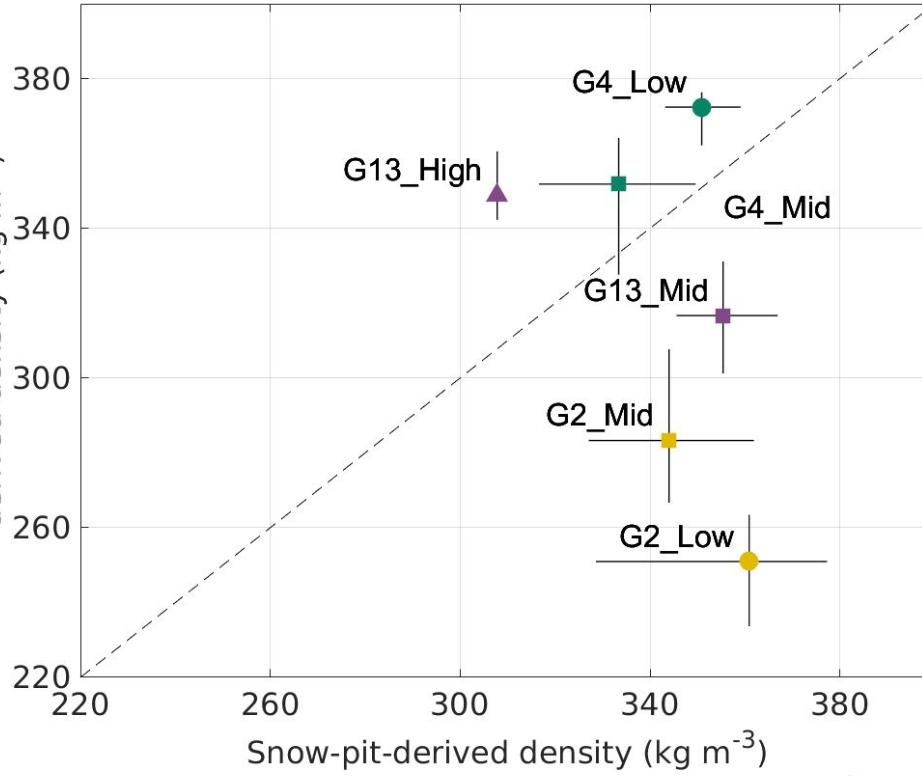


# SNOW DENSITY - RESULTS



Federal-Sampler-

derived density ( $\text{kg m}^{-3}$ )



# SNOW DENSITY - RESULTS

## EIGHT METHODS OF ESTIMATING DENSITY

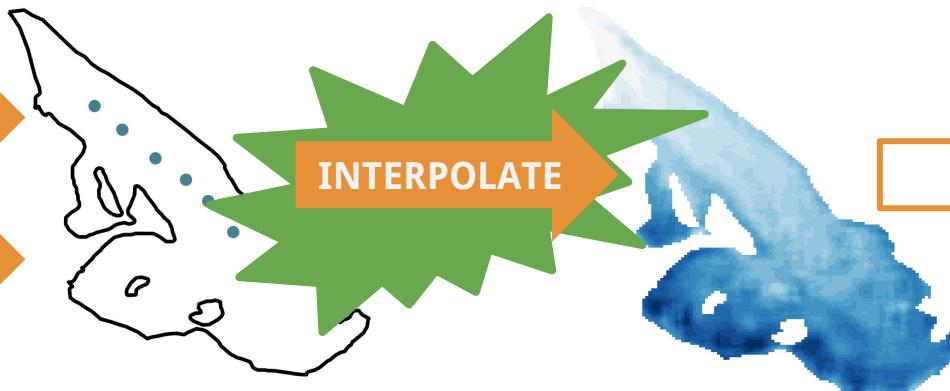
Source of measured snow density	Density assignment method
<i>Snow pit</i>	<i>Federal Sampler</i>
❄️	Mean of measurements across all glaciers
❄️	Mean of measurements for each glacier
❄️	Regression of density on elevation for a glacier
❄️	Inverse distance weighted mean for a glacier

# OBJECTIVE I

END OF WINTER

SNOW DEPTH

SNOW DENSITY



WINTER  
BALANCE

# INTERPOLATION - METHODS

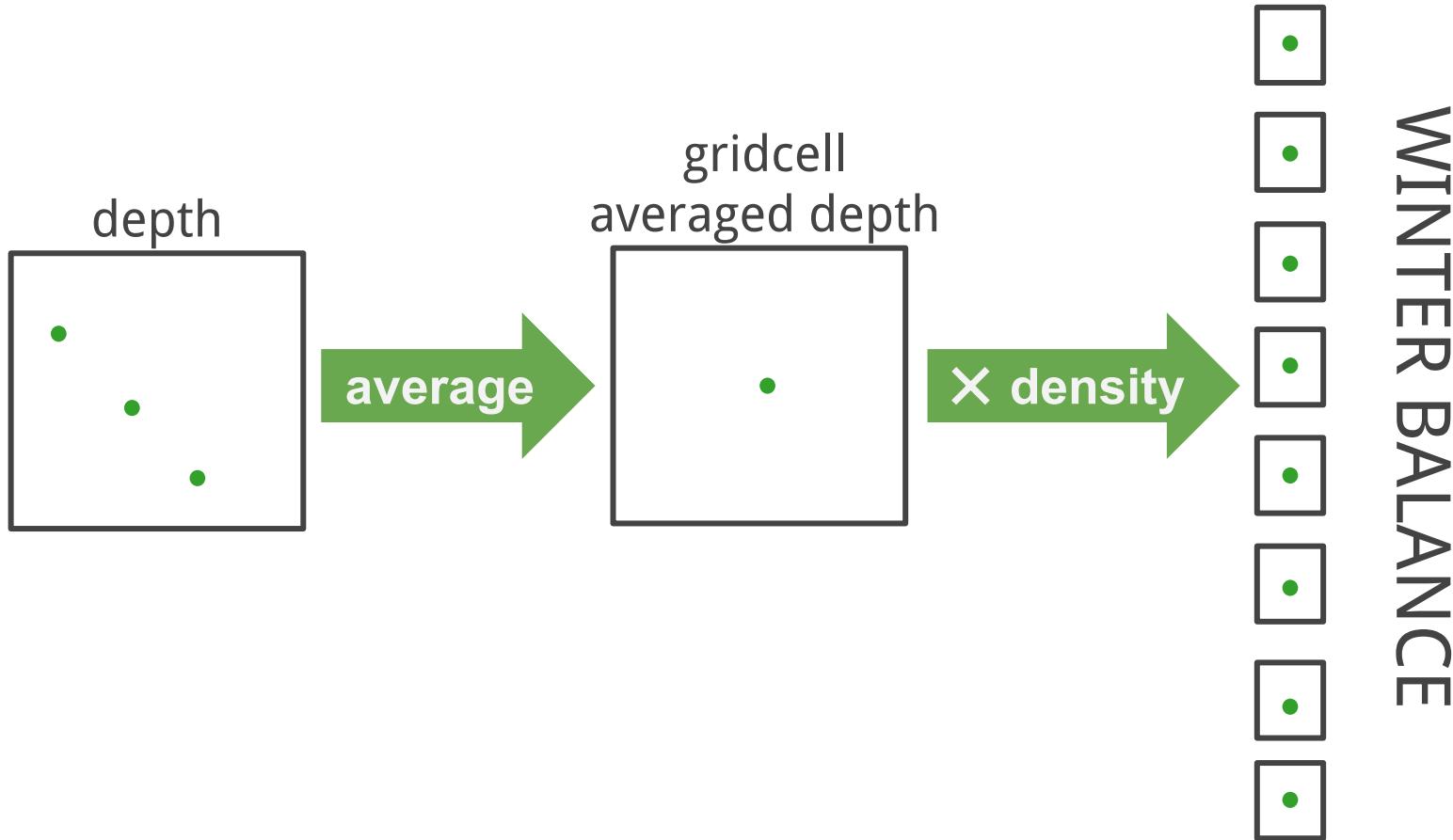
## LINEAR REGRESSION

- Multiple linear regression of winter balance on topographic parameters derived from SPOT-5 DEM (40 m)
- Cross-validation and model averaging (BIC)

## SIMPLE KRIGING

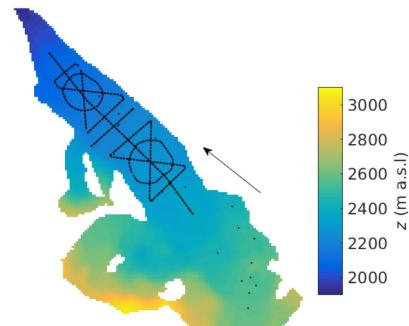
## REGRESSION KRIGING

# INTERPOLATION - INPUT DATA

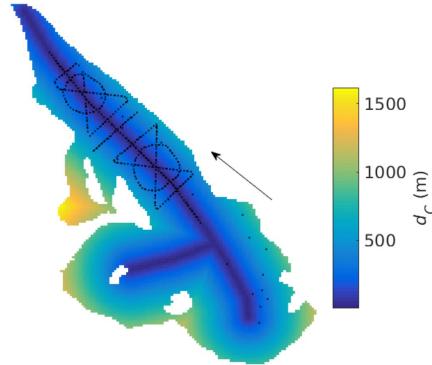


# INTERPOLATION - INPUT DATA

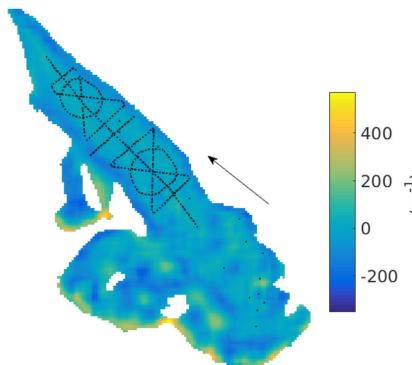
Elevation



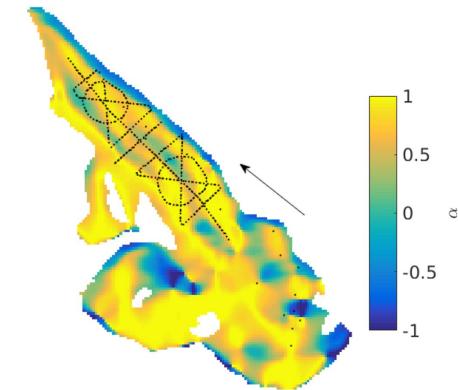
Distance from centreline



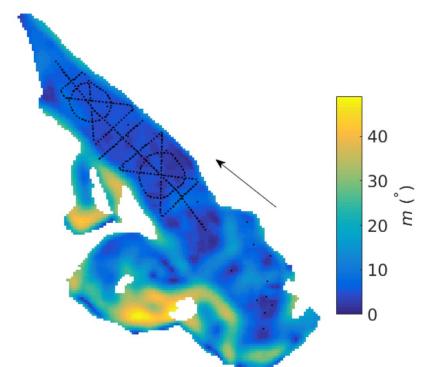
Curvature



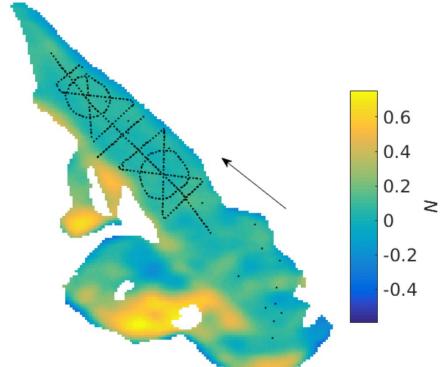
Aspect



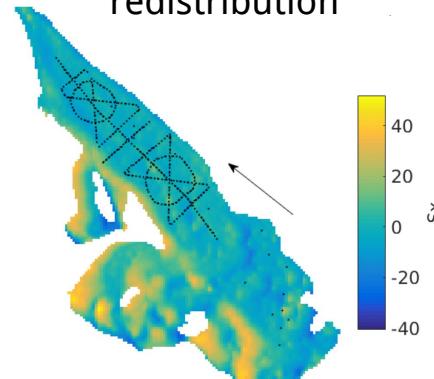
Slope



Northness

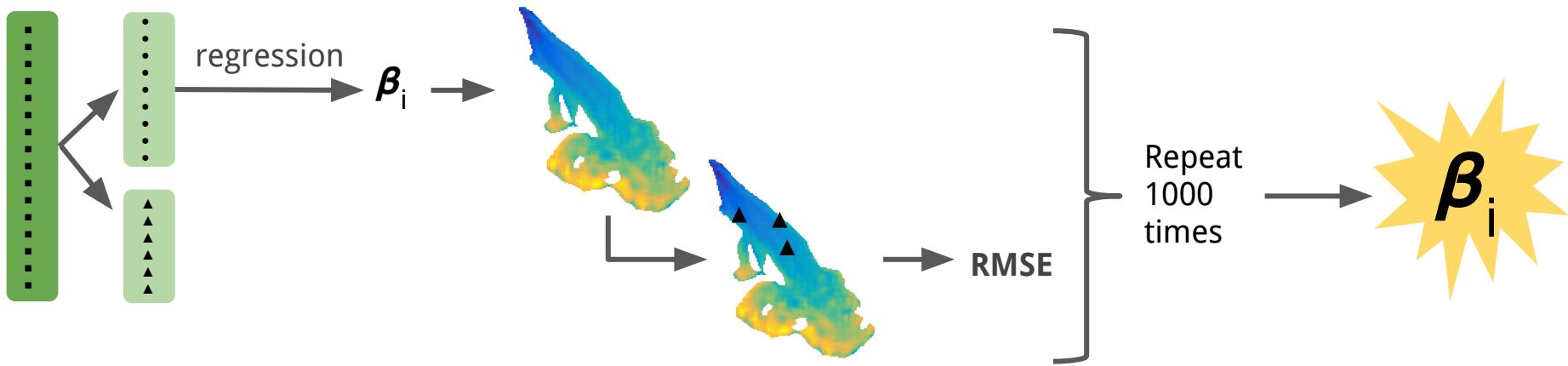


Measure of wind  
redistribution



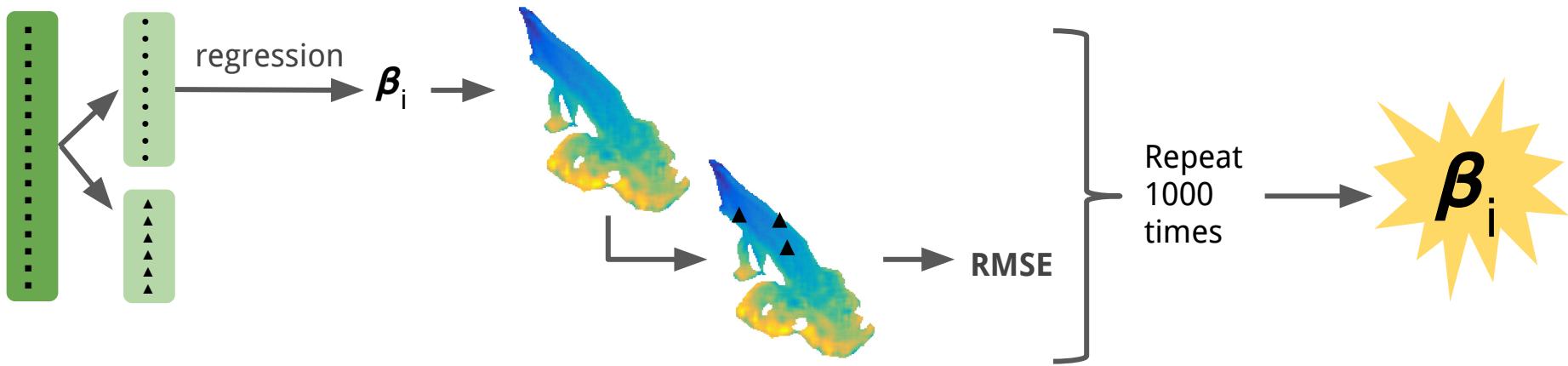
# INTERPOLATION - METHODS

## CROSS VALIDATION



# INTERPOLATION - METHODS

## CROSS VALIDATION

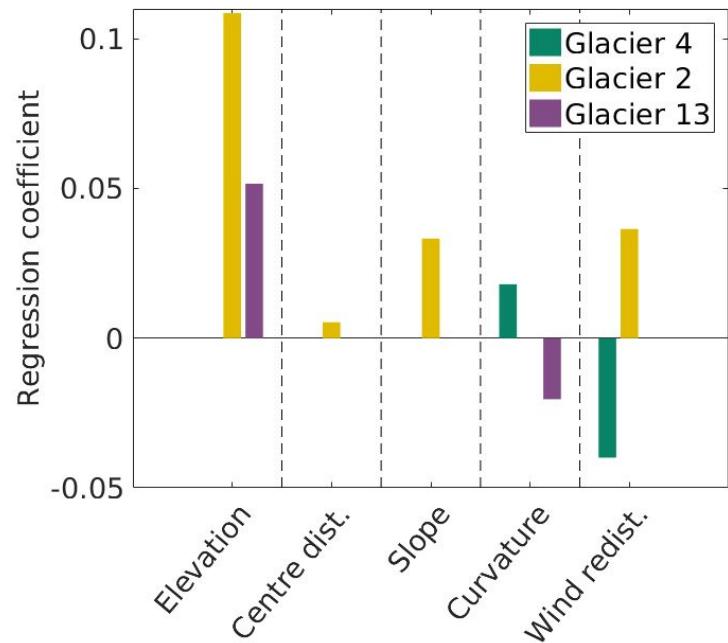


## MODEL AVERAGING

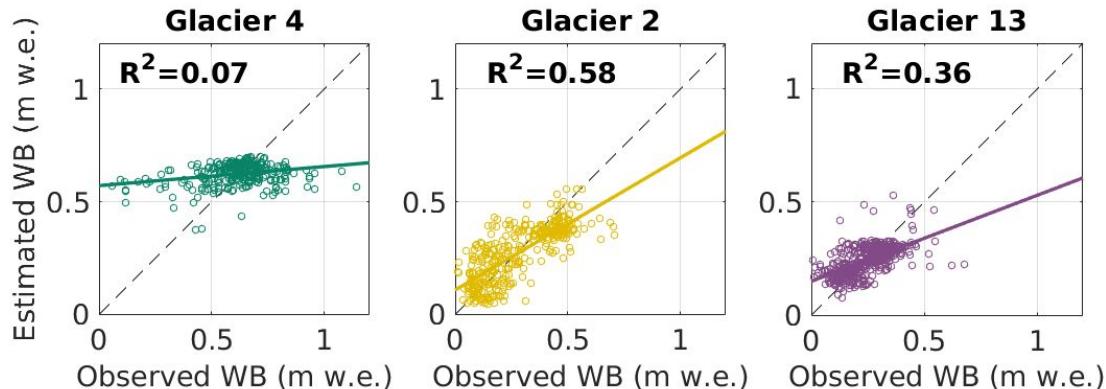
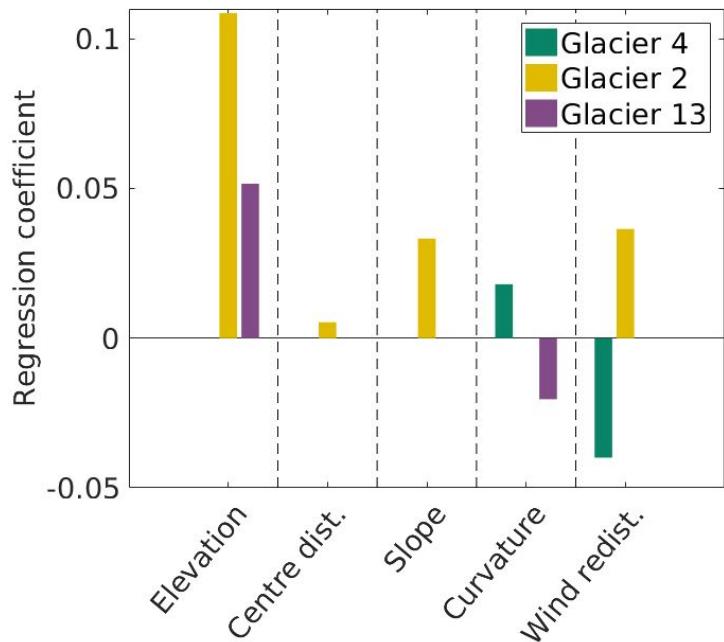
$\beta_1 \quad \beta_1, \beta_2 \quad \beta_1, \beta_2, \beta_3 \quad \beta_2, \beta_3 \quad \beta_2, \beta_3, \beta_4 \quad \beta_1, \beta_2, \beta_3, \beta_4 \quad \dots \quad \beta_1, \beta_2, \beta_3, \beta_4, \beta_5, \beta_6, \beta_7$

⇒ Bayesian information criterion (BIC) weighting

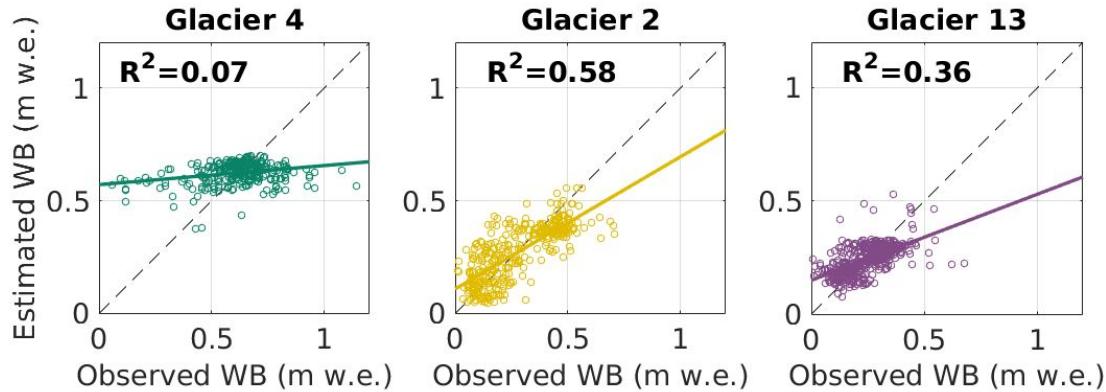
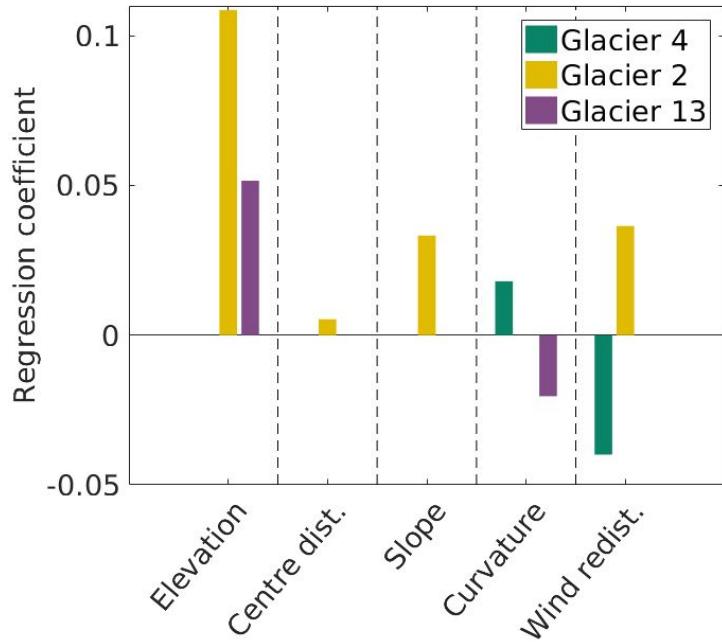
# INTERPOLATION - RESULTS



# INTERPOLATION - RESULTS

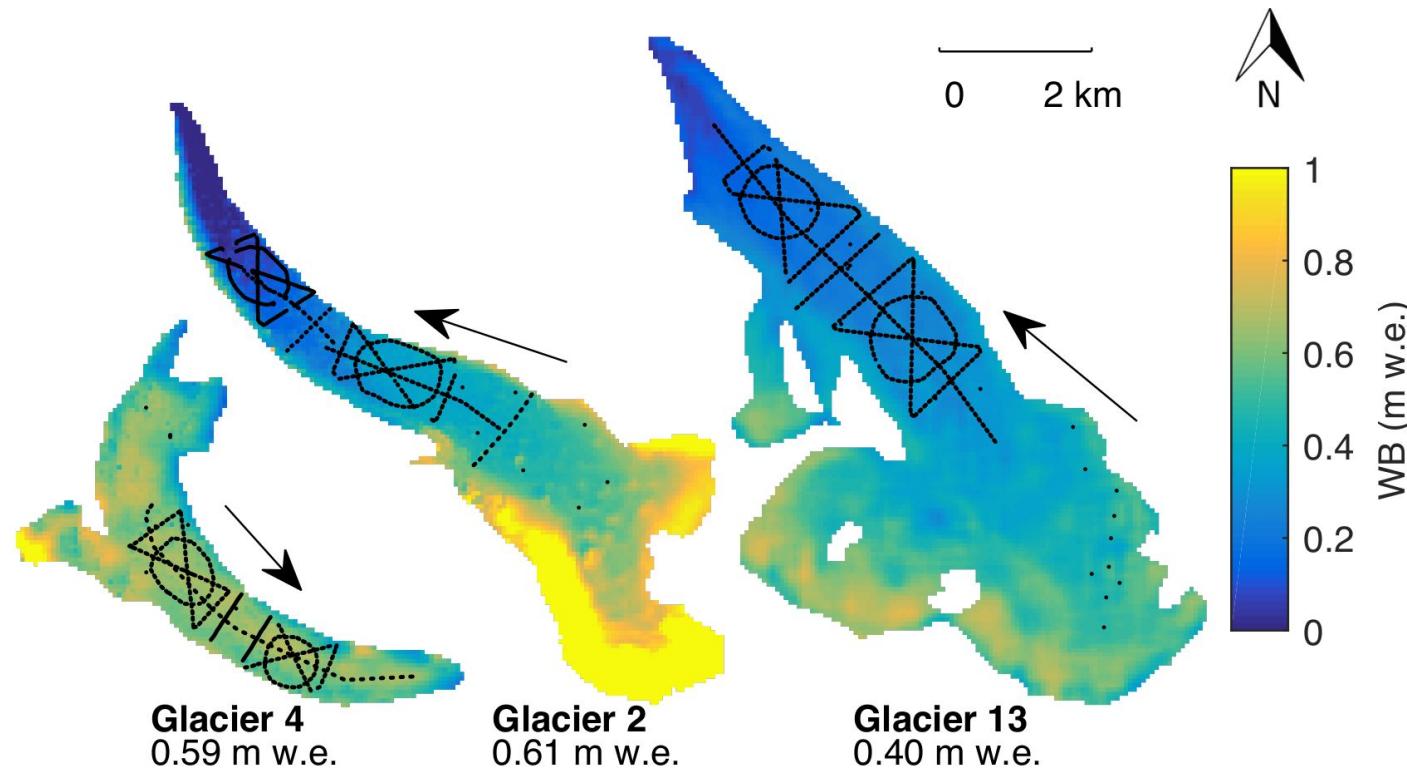


# INTERPOLATION - RESULTS



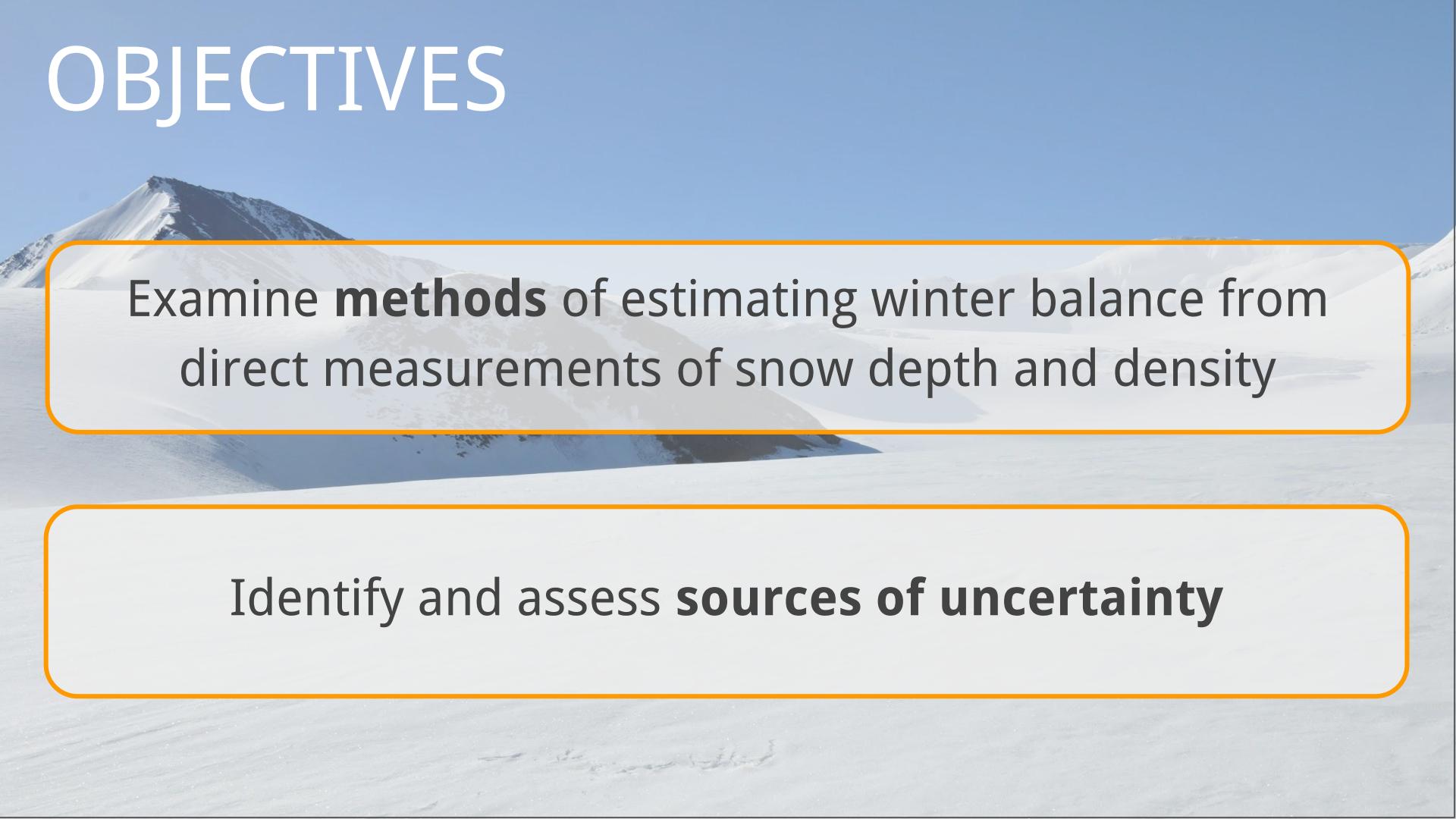
- ✳ Processes governing winter balance differ between glaciers
  - Elevation dominates
  - Wind processes likely important but not adequately captured

# DISTRIBUTED WINTER BALANCE



EIGHT REALIZATIONS DUE TO DENSITY ESTIMATES

# OBJECTIVES

The background of the slide features a wide-angle photograph of a mountainous landscape covered in white snow. The peaks are sharp and dark, contrasting with the bright snow and the clear, pale blue sky above.

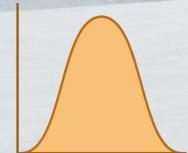
Examine **methods** of estimating winter balance from direct measurements of snow depth and density

Identify and assess **sources of uncertainty**

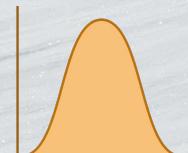
# OBJECTIVE II

Identify and assess **sources of uncertainty**

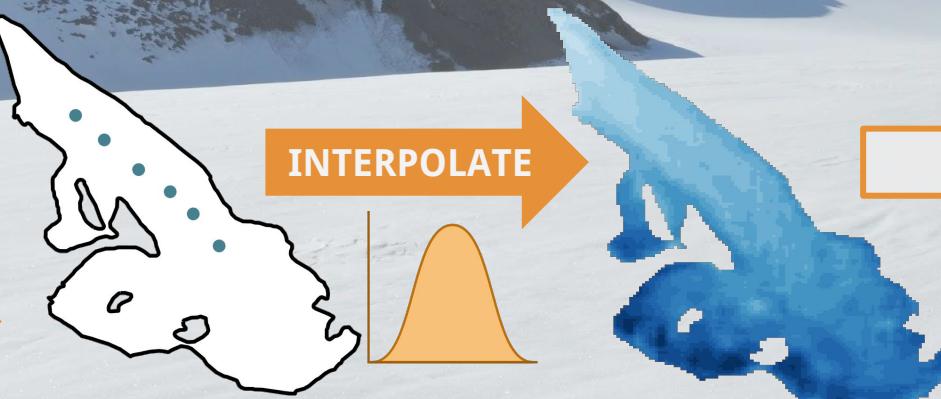
SNOW DEPTH



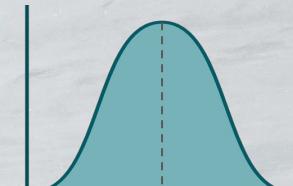
SNOW DENSITY



INTERPOLATE



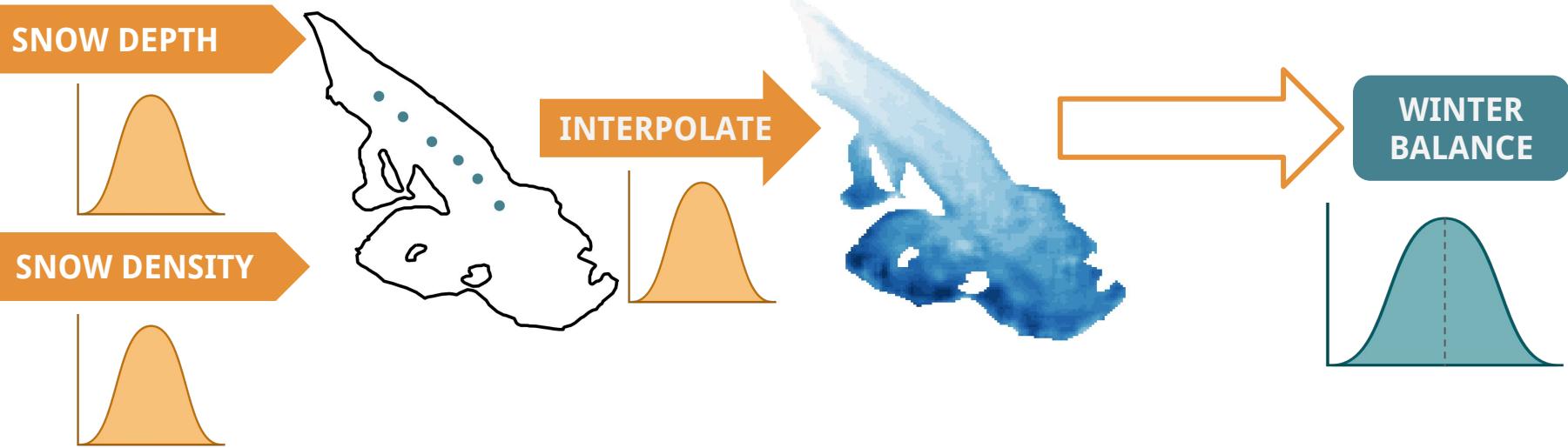
WINTER BALANCE



END OF WINTER

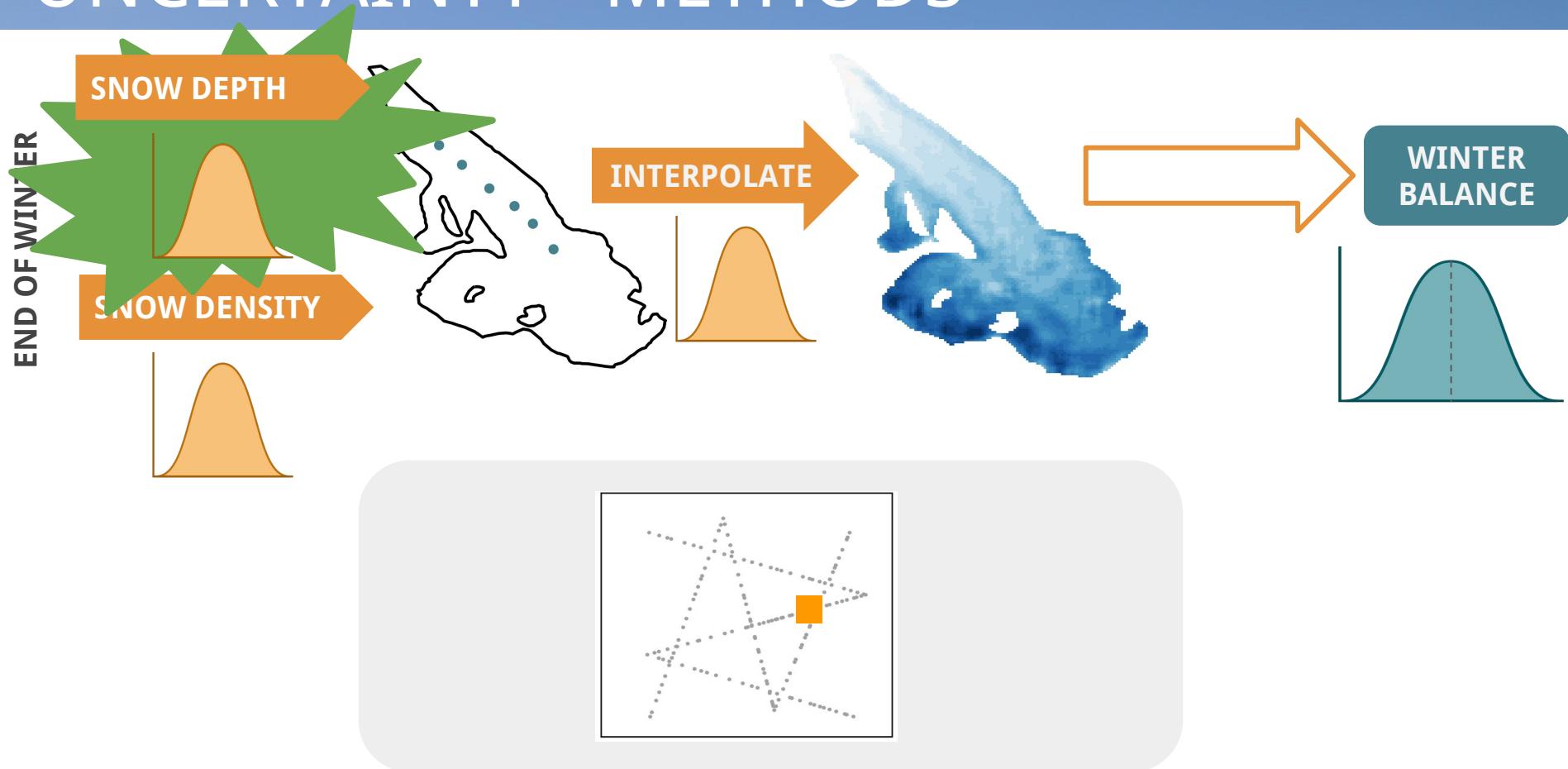
# UNCERTAINTY - METHODS

END OF WINTER

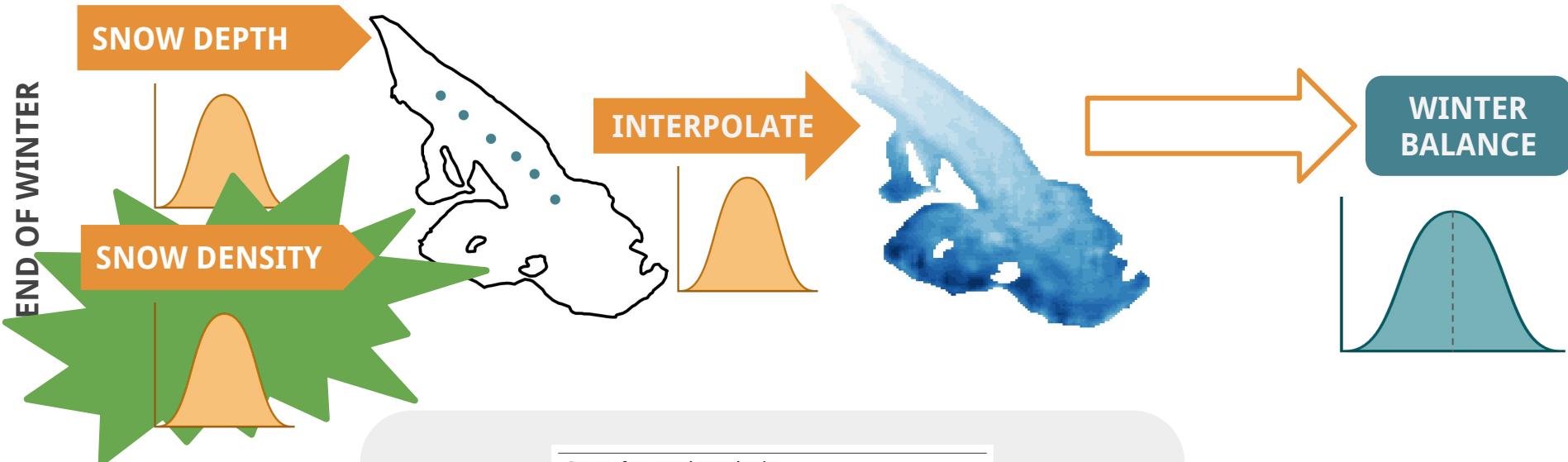


MONTE CARLO METHOD

# UNCERTAINTY - METHODS



# UNCERTAINTY - METHODS

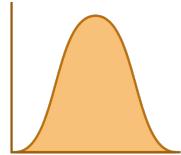


Source of measured snow density	Density assignment method
Snow pit	Federal Sampler
*	*
	Mean of measurements across all glaciers
*	*
	Mean of measurements for each glacier
*	*
	Regression of density on elevation for a glacier
*	*
	Inverse distance weighted mean for a glacier

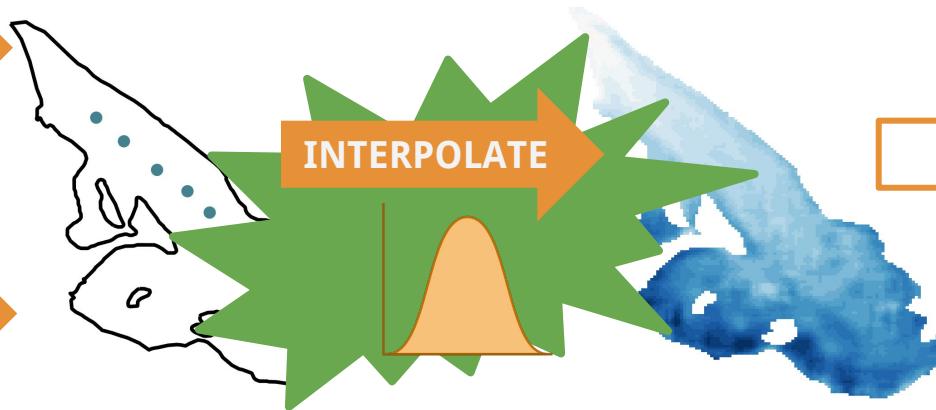
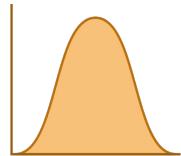
# UNCERTAINTY - METHODS

END OF WINTER

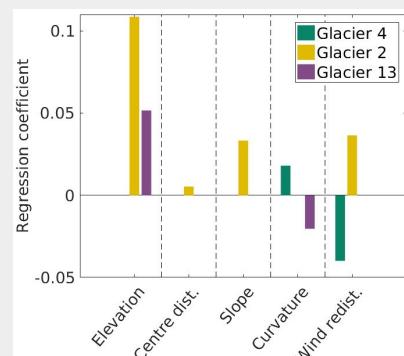
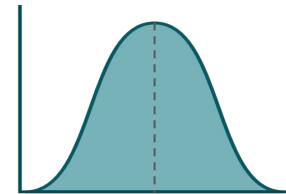
SNOW DEPTH



SNOW DENSITY



WINTER BALANCE



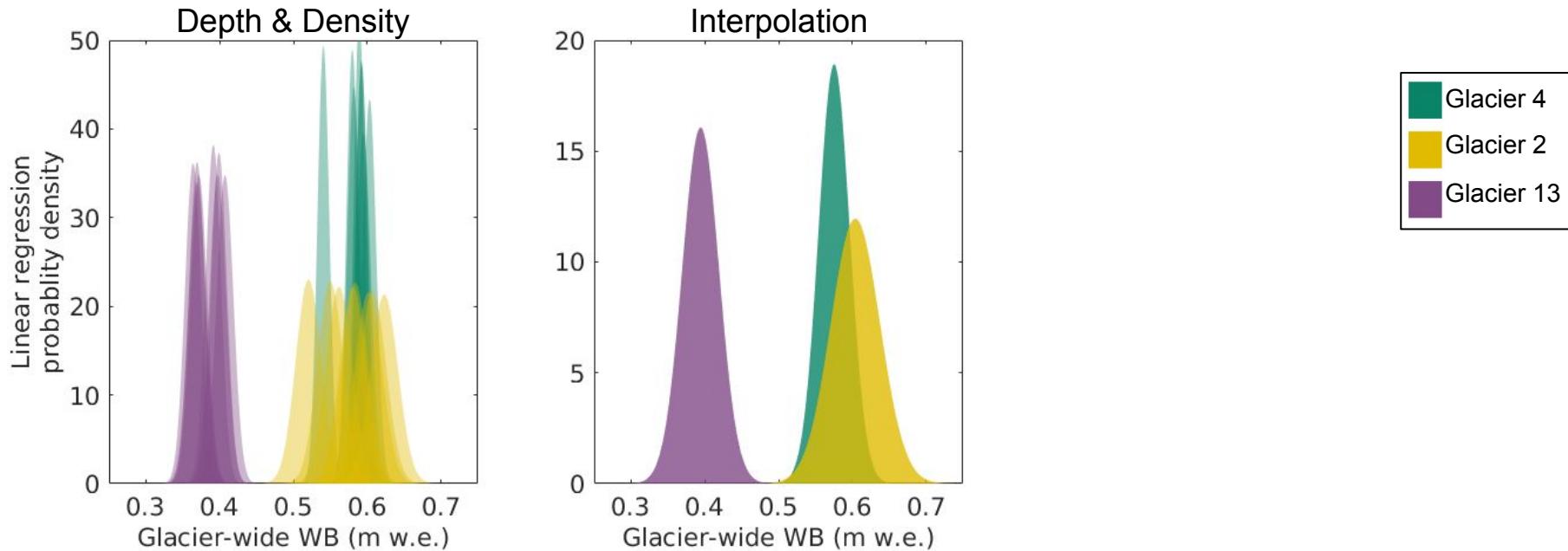
# UNCERTAINTY - RESULTS



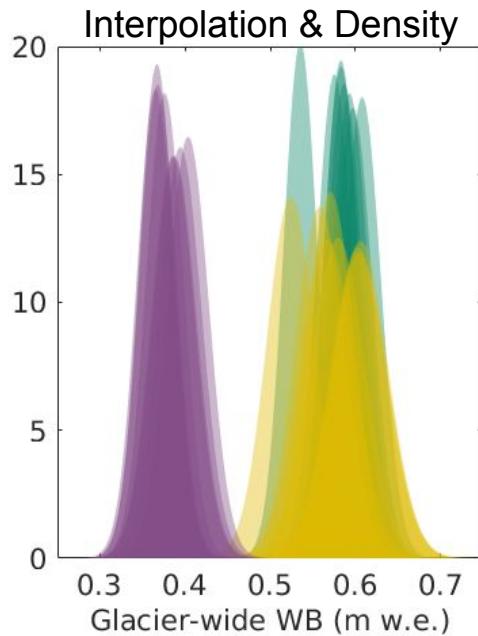
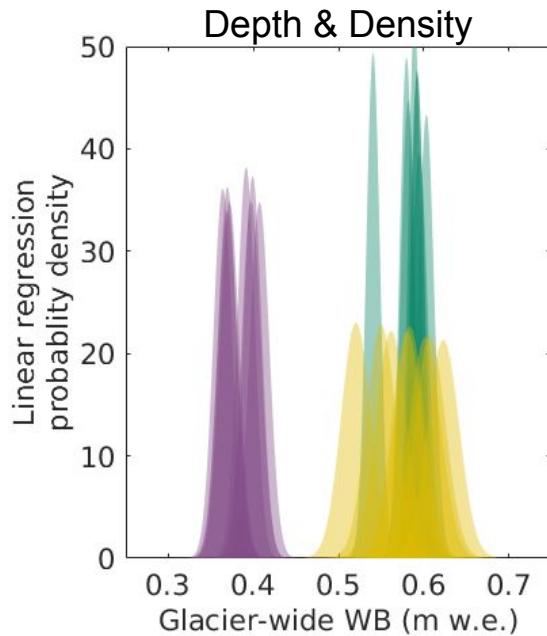
# UNCERTAINTY - RESULTS



# RESULTS - UNCERTAINTY

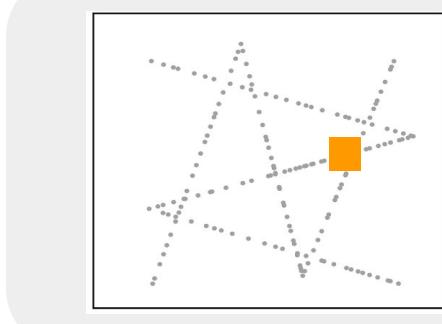
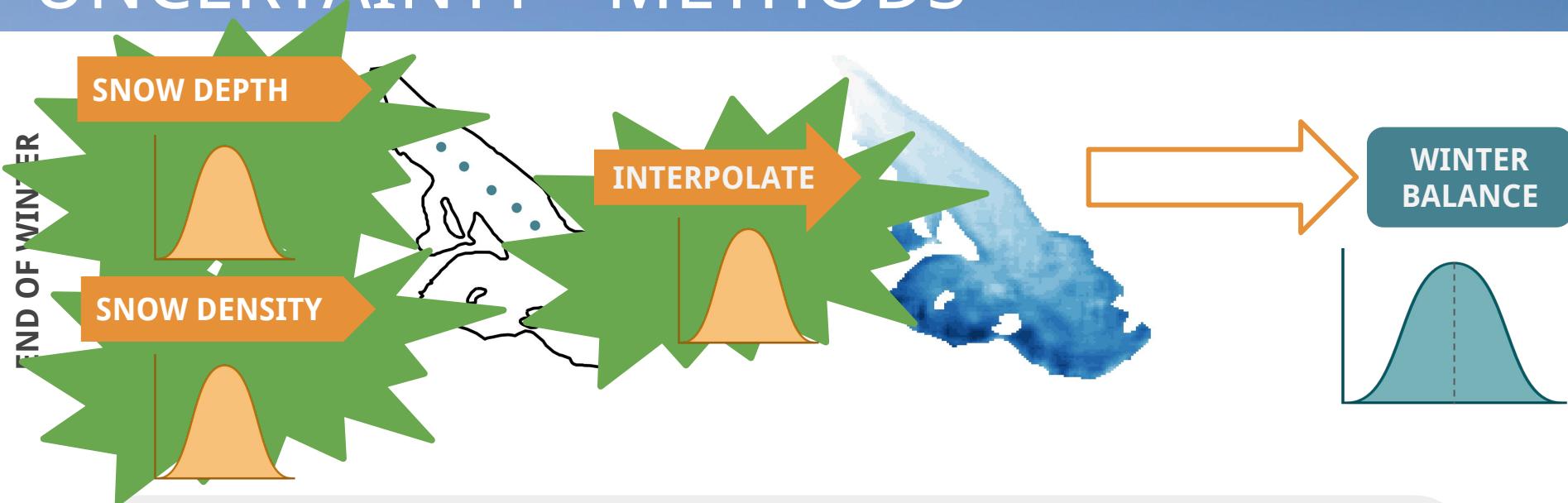


# UNCERTAINTY - RESULTS

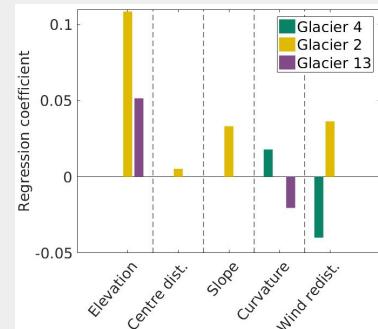


Glacier 4  
Glacier 2  
Glacier 13

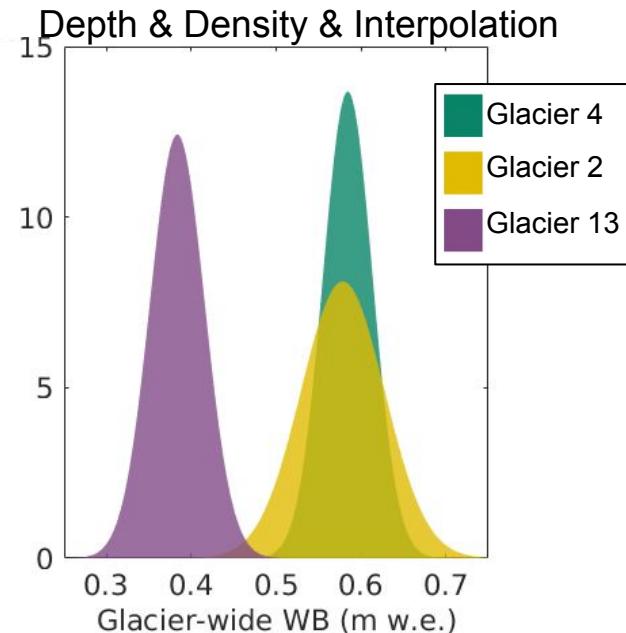
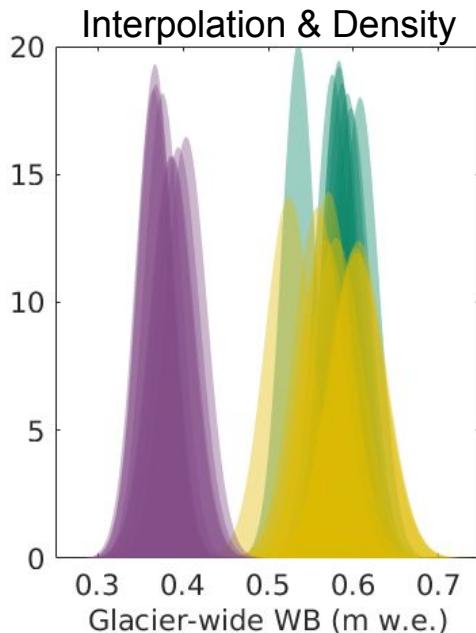
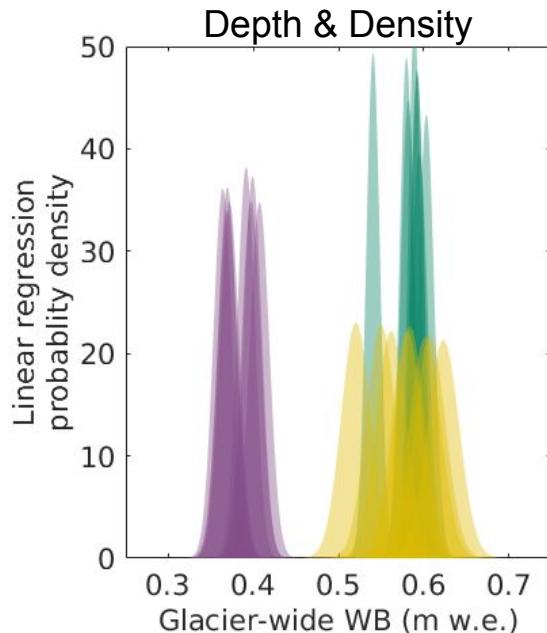
# UNCERTAINTY - METHODS



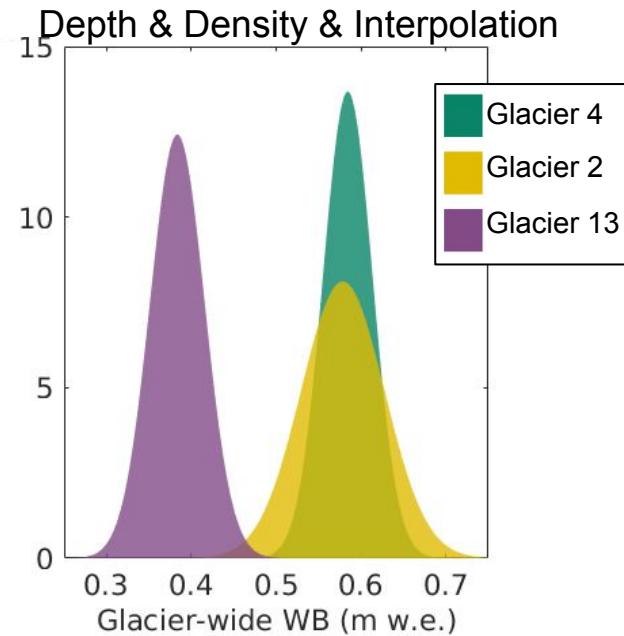
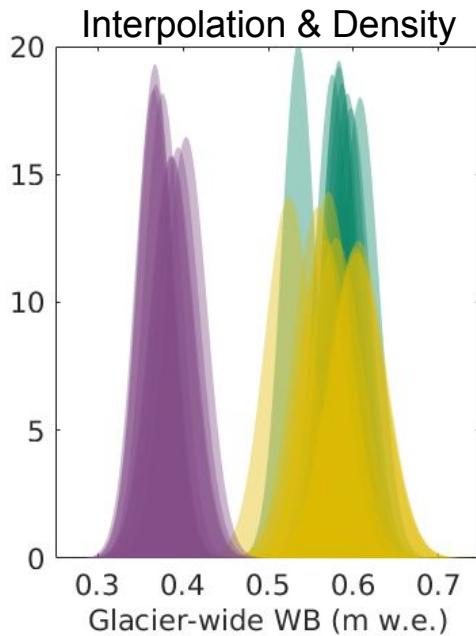
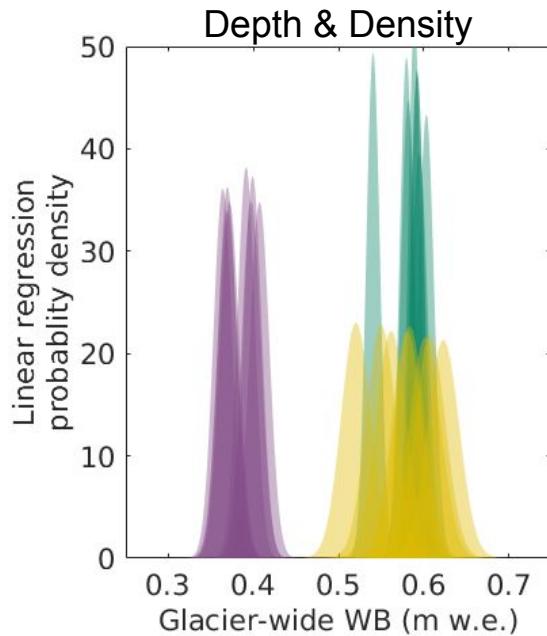
Source of measured snow density	Federal Sampler	Density assignment method
*	*	Mean of measurements across all glaciers
*	*	Mean of measurements for each glacier
*	*	Regression of density on elevation for a glacier
*	*	Inverse distance weighted mean for a glacier



# UNCERTAINTY - RESULTS

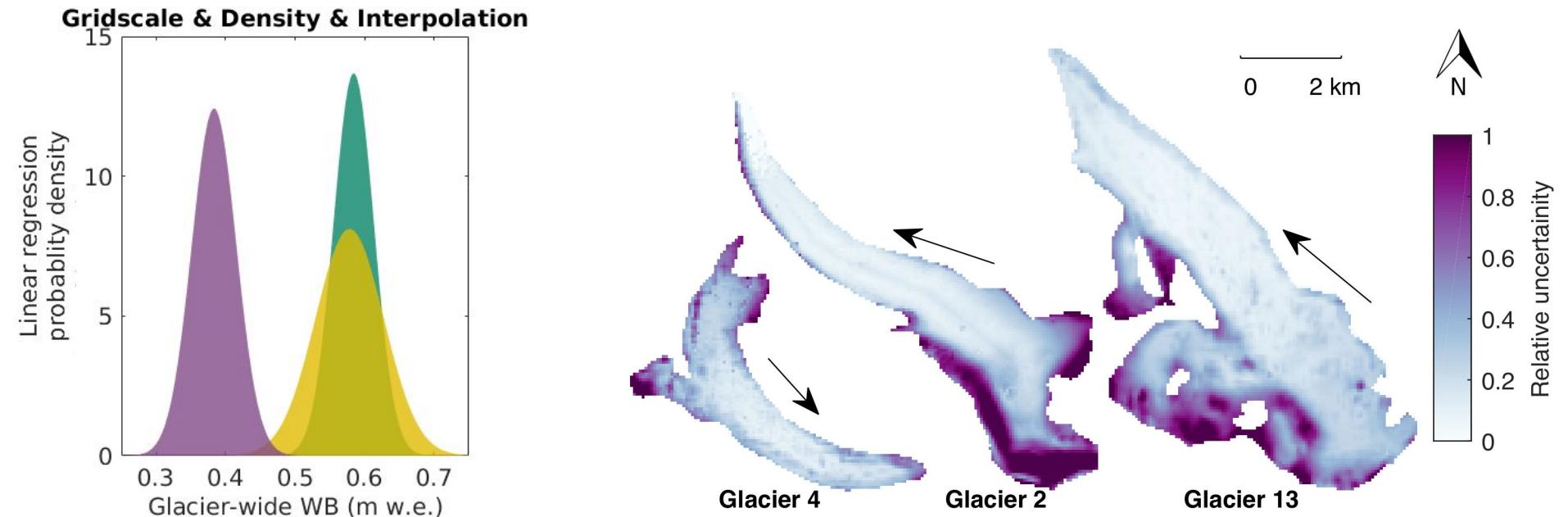


# UNCERTAINTY - RESULTS



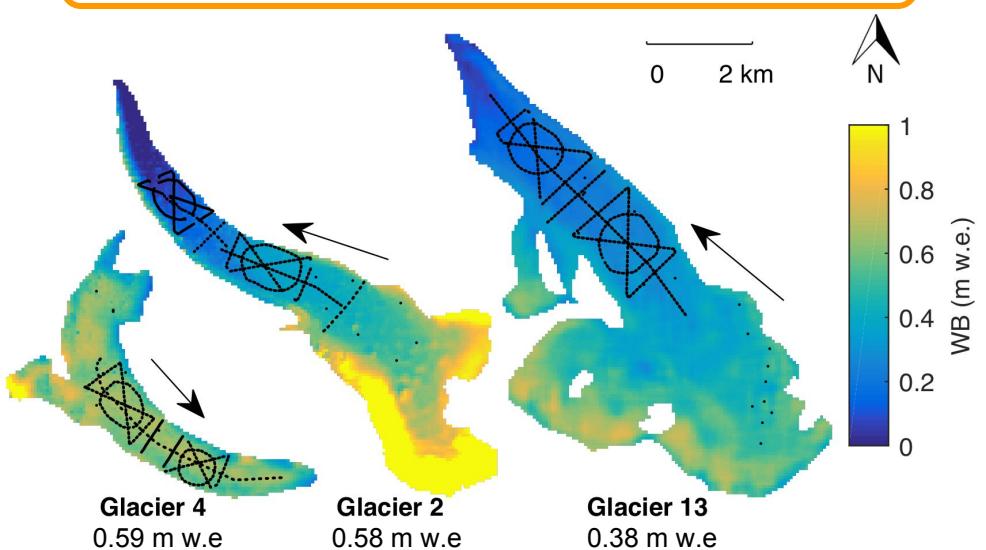
- \* Interpolation is the largest assessed source of uncertainty in winter balance → use interpolated values with caution
- \* Uncertainty from snow depth and density measurement is low

# UNCERTAINTY - RESULTS

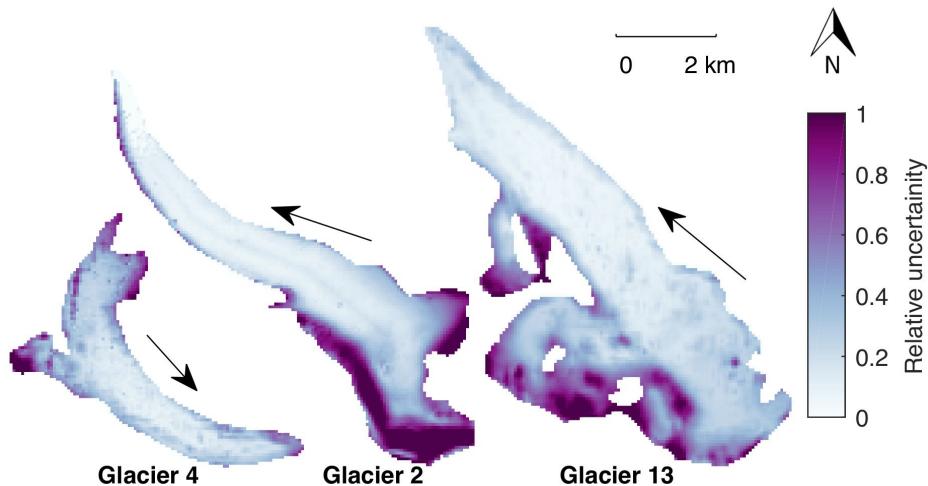


# DISTRIBUTED WINTER BALANCE

## WINTER BALANCE

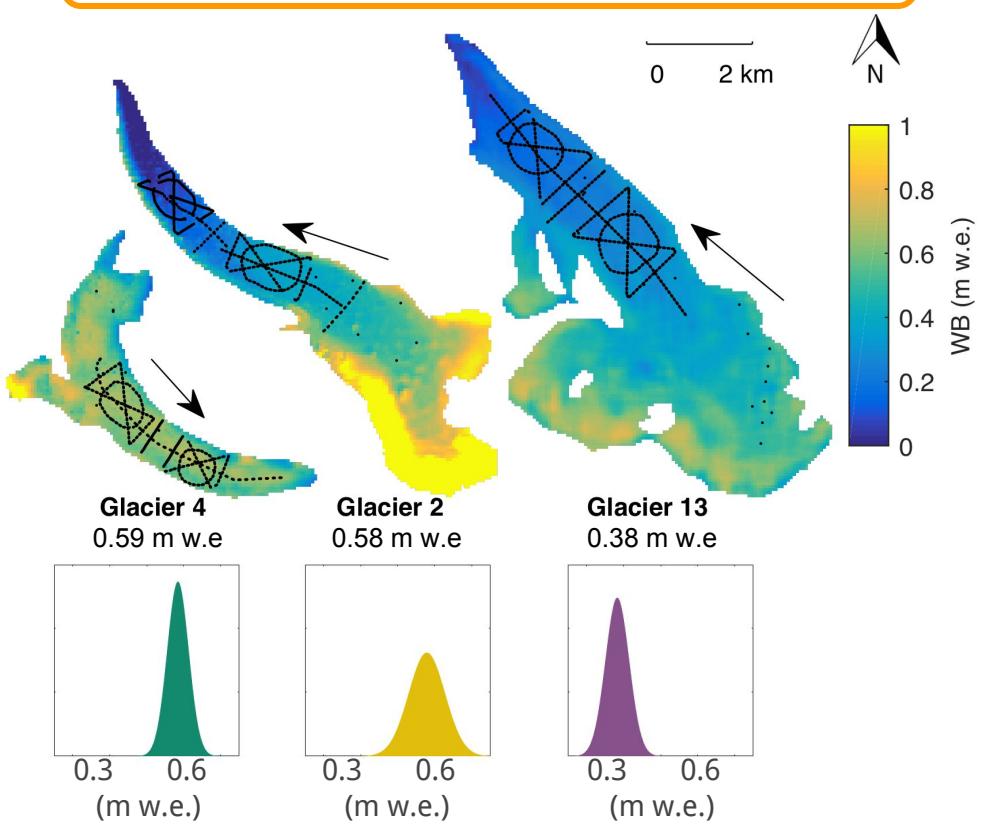


## RELATIVE UNCERTAINTY

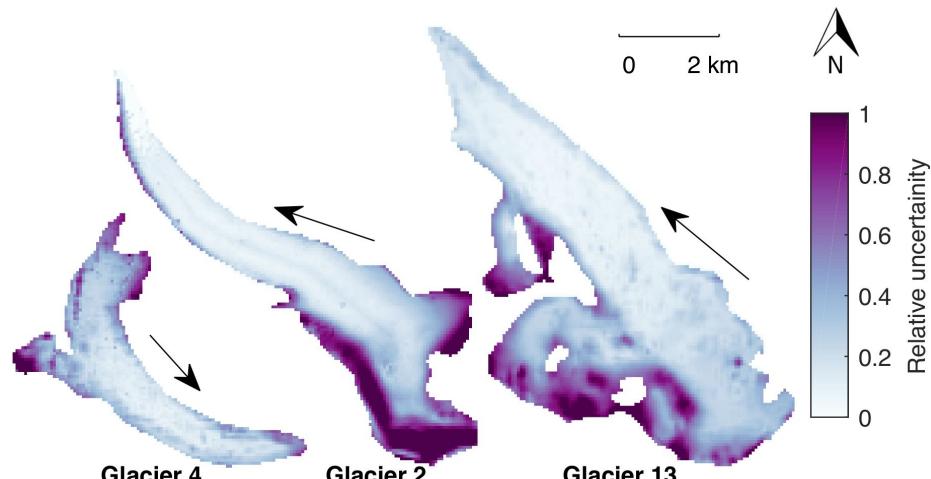


# DISTRIBUTED WINTER BALANCE

## WINTER BALANCE



## RELATIVE UNCERTAINTY

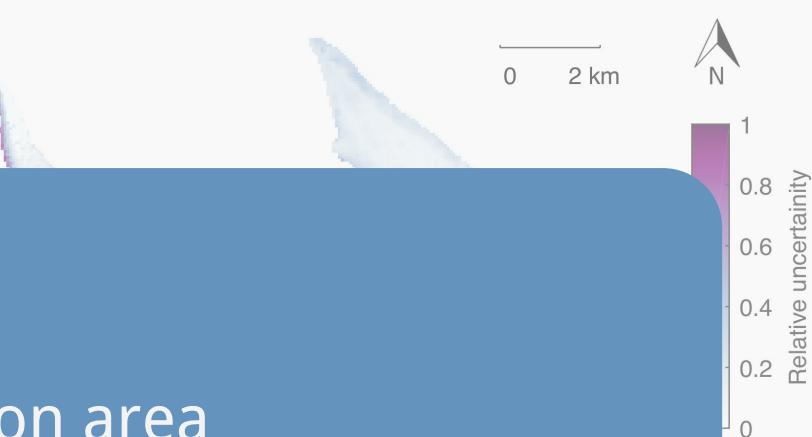


# DISTRIBUTED WINTER BALANCE

## WINTER BALANCE



## RELATIVE UNCERTAINTY



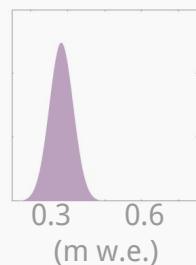
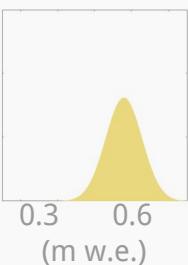
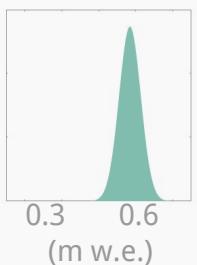
## MAIN LIMITATIONS

- ❄ Data restricted to single year
- ❄ Minimal sampling in accumulation area

0.59 m w.e.

0.61 m w.e.

0.40 m w.e.



# SUMMARY

## METHODS

- ⌘ Multiscale snow-depth and density measurements
- ⌘ Linear regression and Monte Carlo analysis used to estimate winter balance

## RESULTS

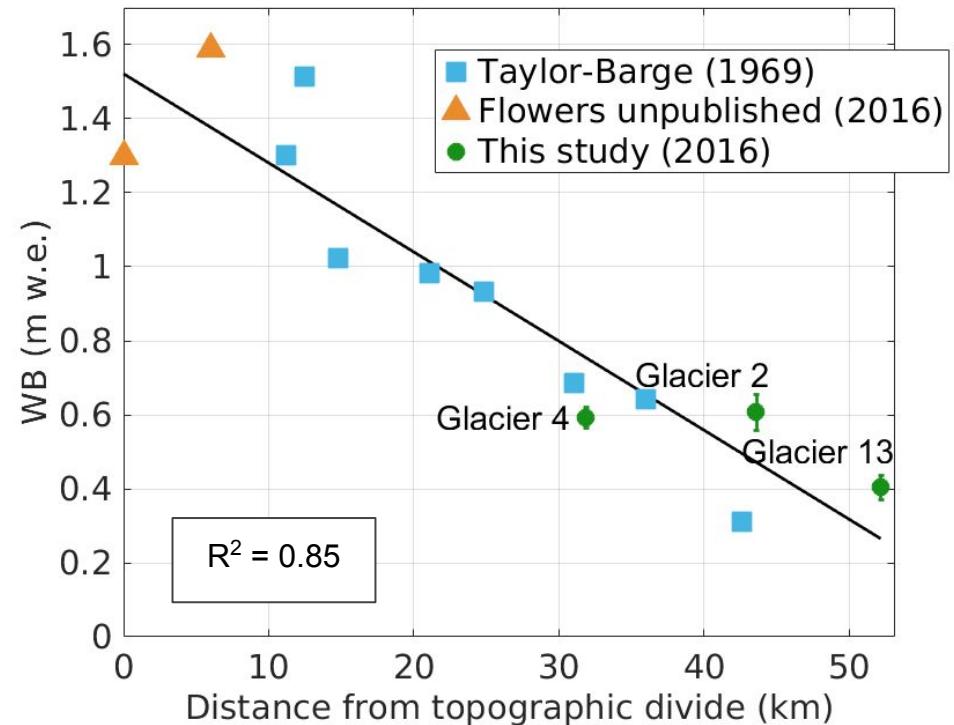
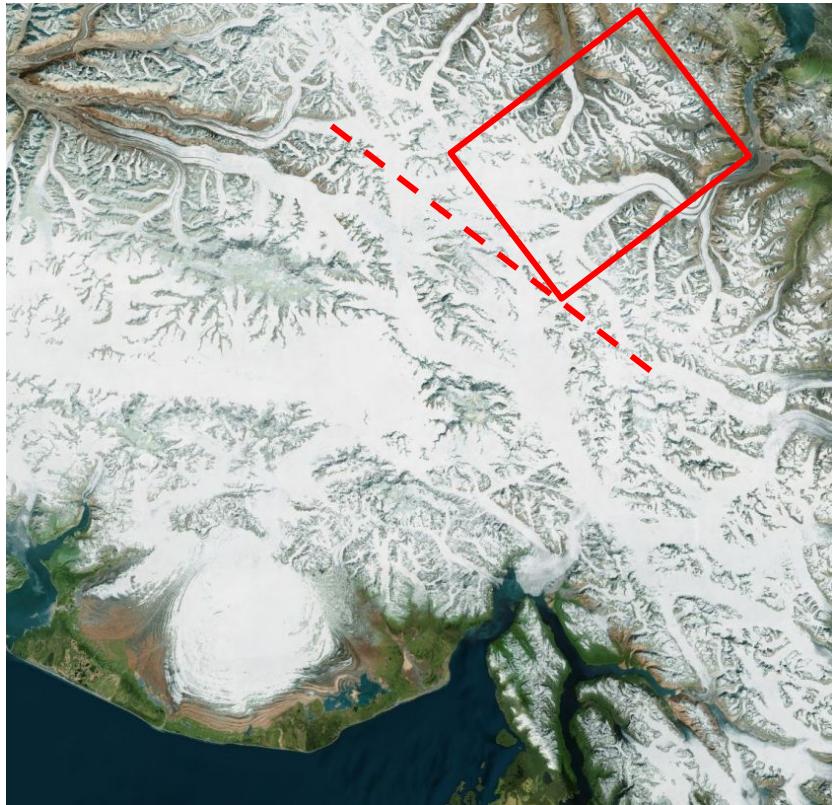
- ⌘ Processes governing winter balance differ between glaciers
- ⌘ Sources of uncertainty: **interpolation**, *depth & density*
- ⌘ Basin coverage more important than high resolution sampling

## LIMITATIONS

- ⌘ Multi-year data and accumulation area measurements needed



# REGIONAL WINTER BALANCE GRADIENT

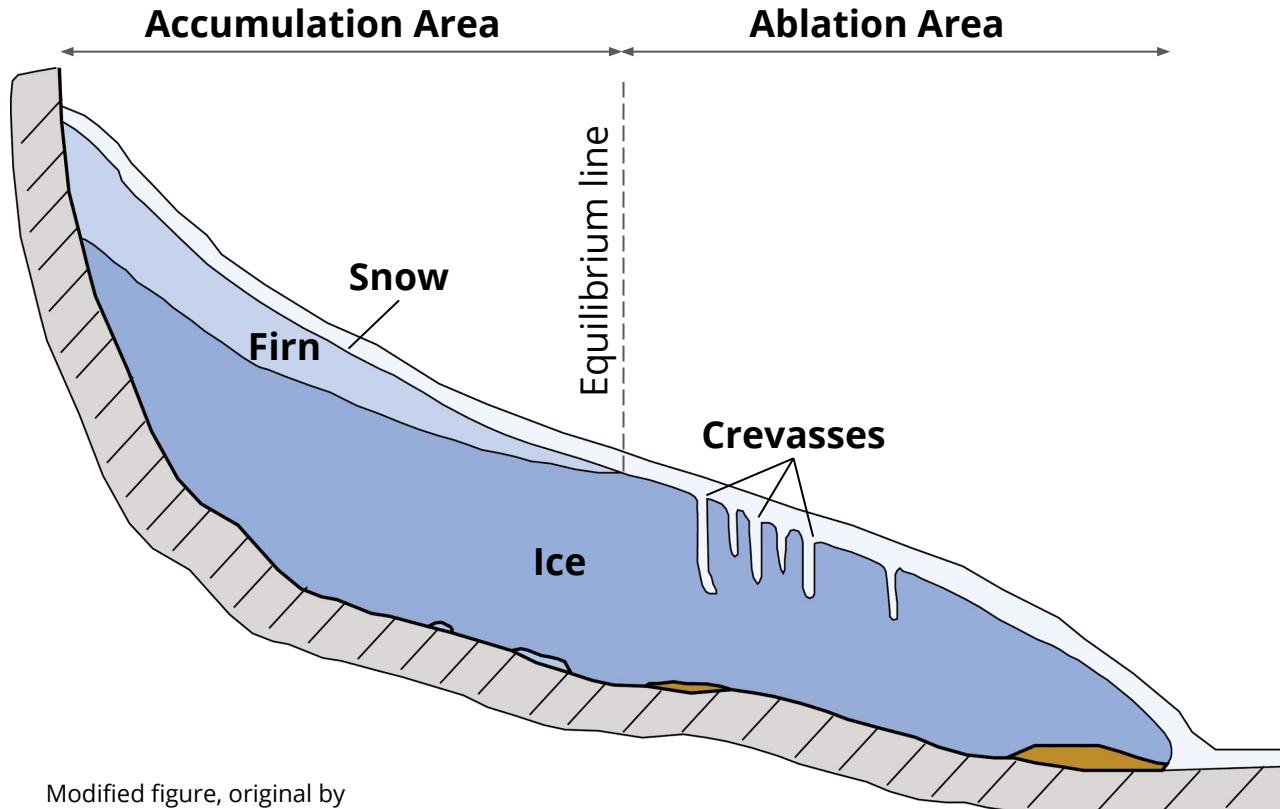


# STUDY GLACIERS

Table 1.2: Physical characteristics of the study glaciers and May 2016 winter-balance survey details, including number of snow-depth measurement locations along transects ( $n_T$ ), total length of transects ( $d_T$ ), number of combined snow pit and Federal Sampler density measurement locations ( $n_p$ ) and number of zigzag surveys ( $n_{zz}$ ).

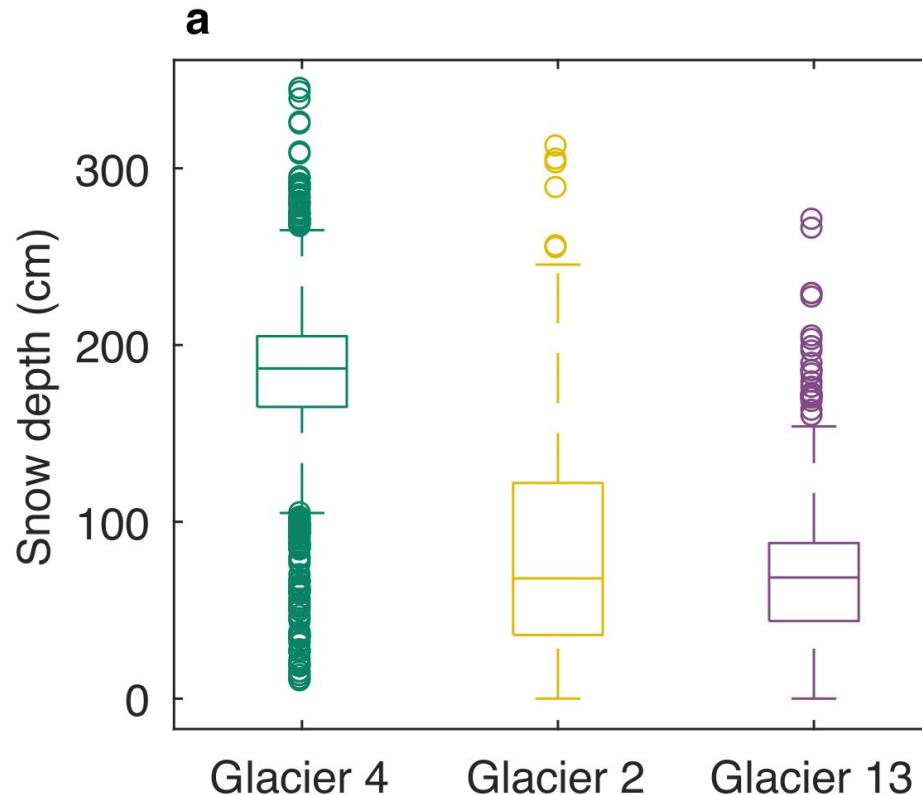
	Location UTM Zone 7	Elevation (m a.s.l)			Slope (°) Mean	Area (km <sup>2</sup> )	Survey Dates	Survey Details			
		Mean	Range	ELA				$n_T$	$d_T$ (km)	$n_p$	$n_{zz}$
Glacier 4	595470 E 6740730 N	2344	1958–2809	~2500	12.8	3.8	4–7 May 2016	649	13.1	10	3
Glacier 2	601160 E 6753785 N	2495	1899–3103	~2500	13.0	7.0	8–11 May 2016	762	13.6	11	3
Glacier 13	604602 E 6763400 N	2428	1923–3067	~2380	13.4	12.6	12–15 May 2016	941	18.1	20	4

# ALPINE GLACIER

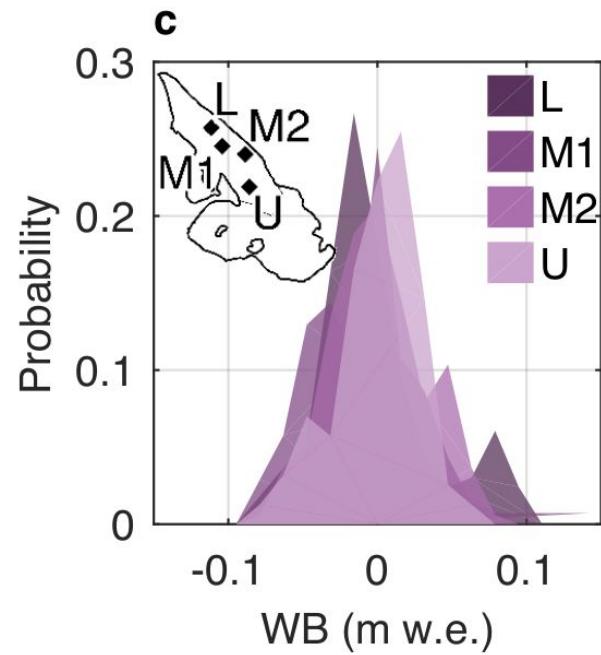
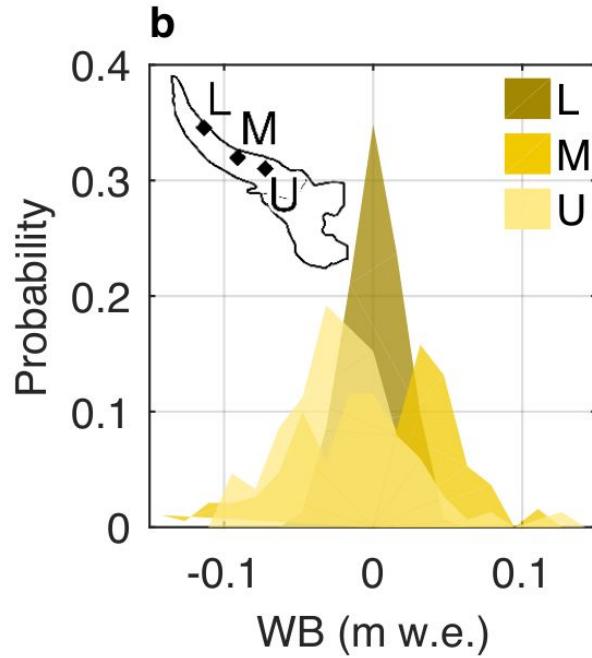
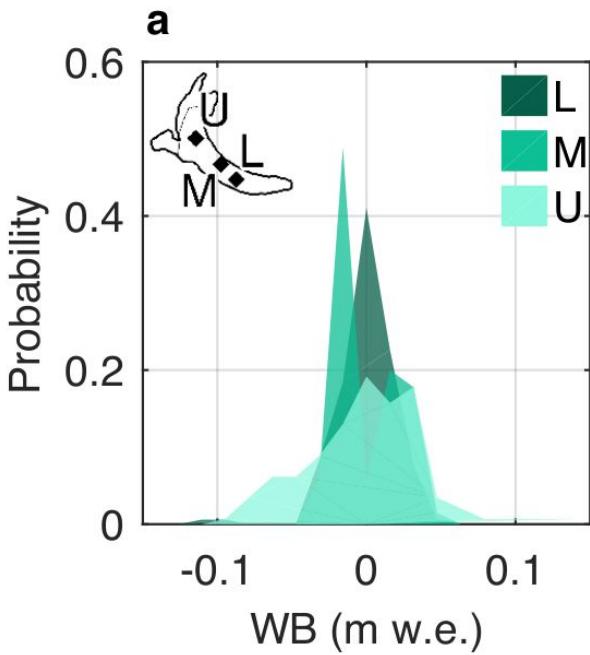


Modified figure, original by  
Martin Funk

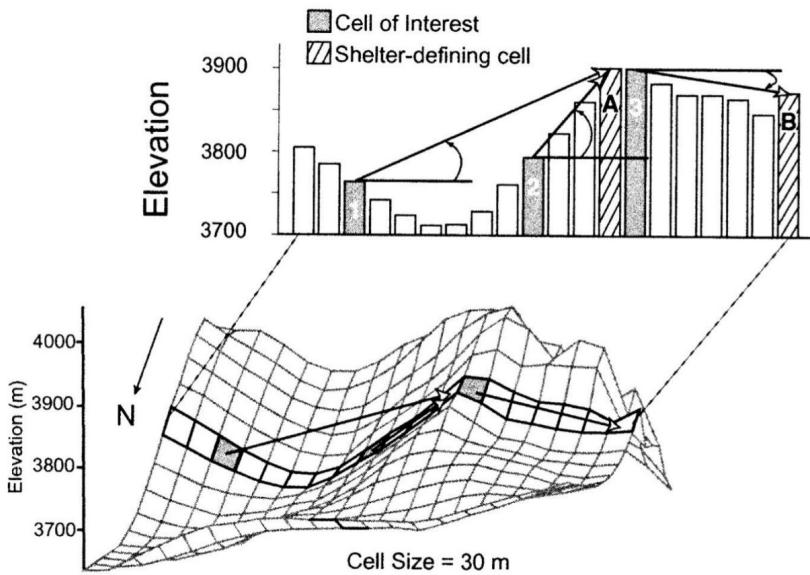
# SNOW DEPTH



# ZIGZAG PDFs

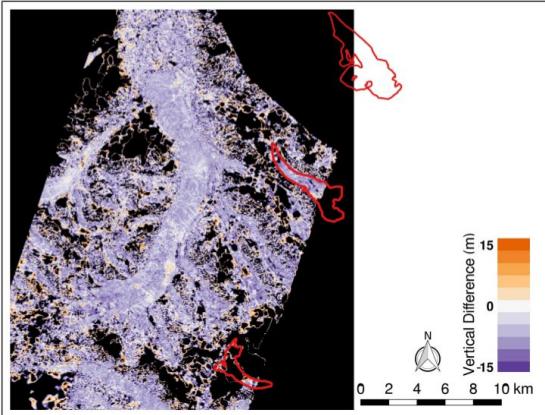


# WIND REDISTRIBUTION PARAMETER ( $S_x$ )

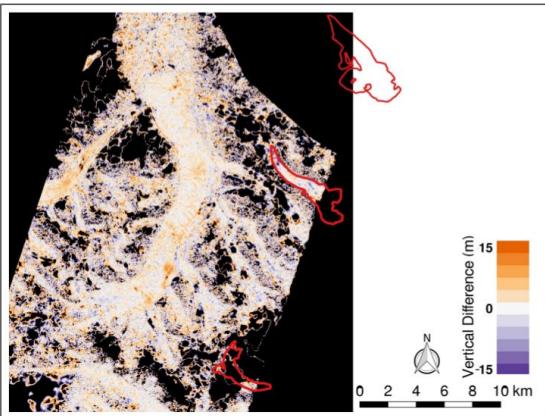


Example of  $S_x$  calculations for three cells of interest along a  $270^\circ$  search vector. As depicted, with  $d_{max}$  set equal to 300 m, the shelter-defining cell for cells 1 and 2 is cell A, producing positive  $S_x$  values. The shelter-defining cell for cell 3 is cell B, producing a negative  $S_x$ . Had  $d_{max}$  been equal to 100 m, the search for the shelter-defining cell for cell 1 would not extend across the valley, thus producing a negative  $S_x$  for cell 1, while  $S_x$  for cell 2 would remain the same and that for cell 3 would be slightly lower. Image and description from (Winstral and others, 2002).

# DEM CORRECTIONS



(a) Difference between original DEMs



(b) Difference between corrected DEMs.

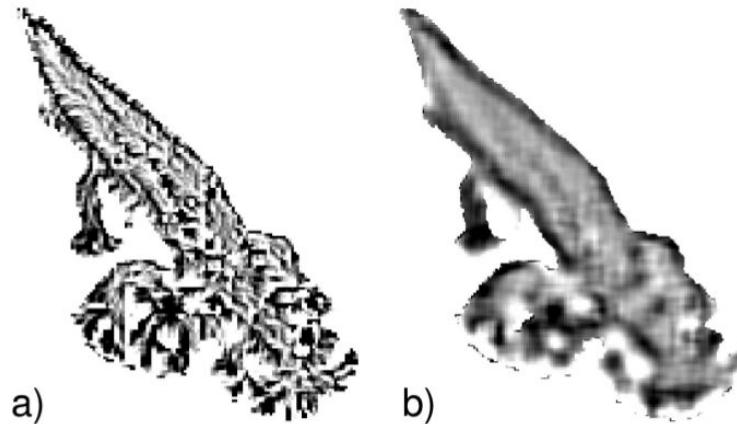
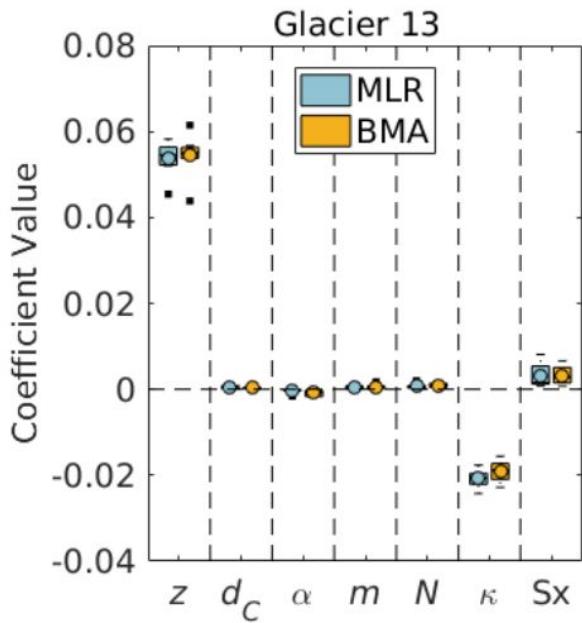
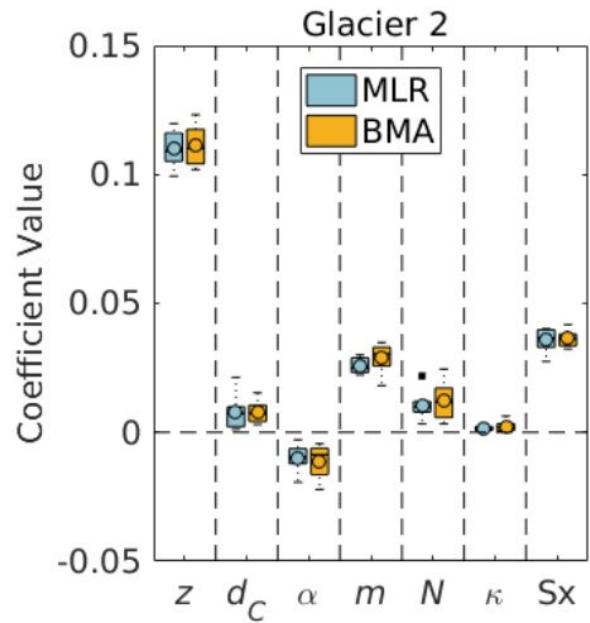
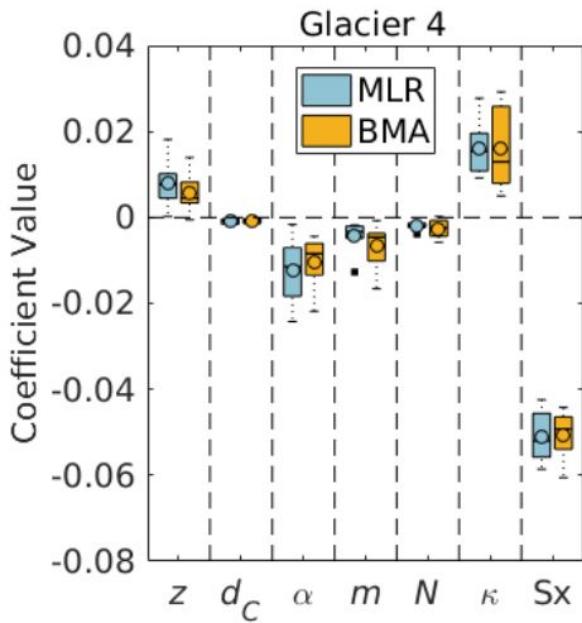
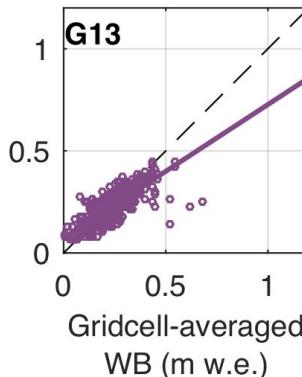
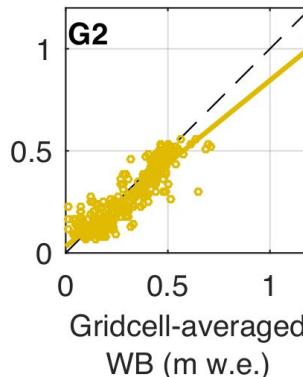
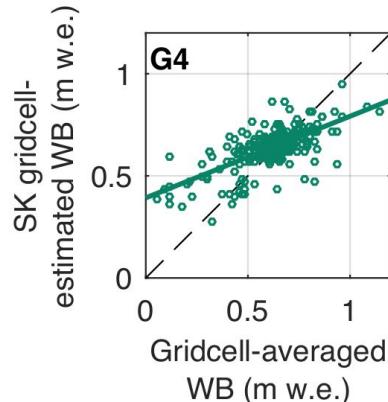
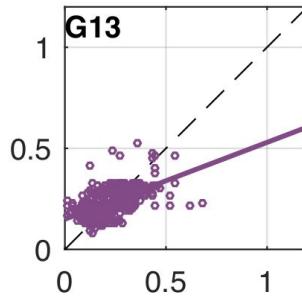
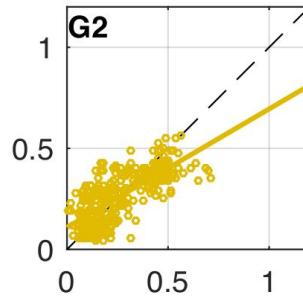
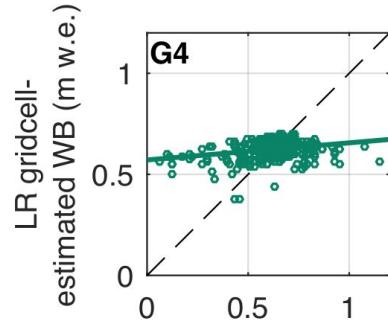


Figure 4.8: (a) Curvature found using the original DEM. (b) Curvature found using the smoothed ( $7 \times 7$  window moving average) DEM.

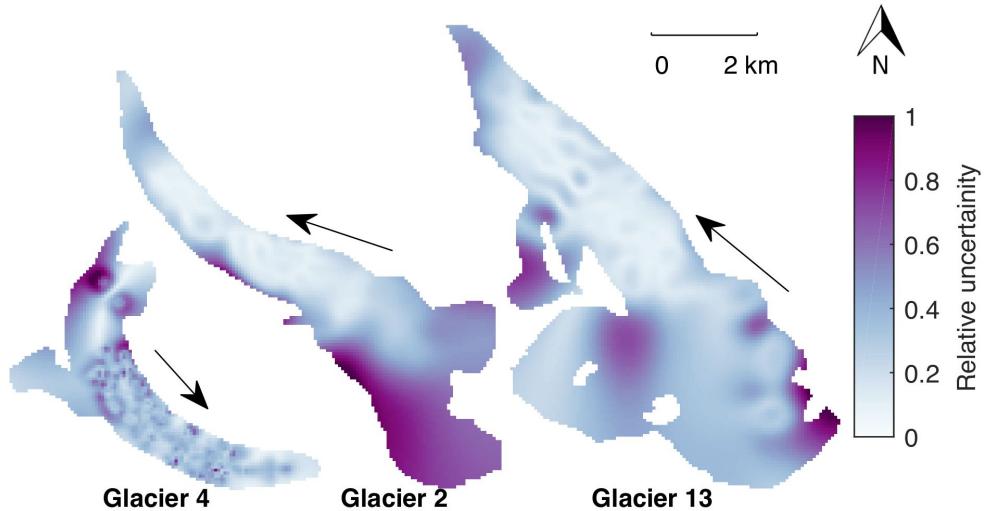
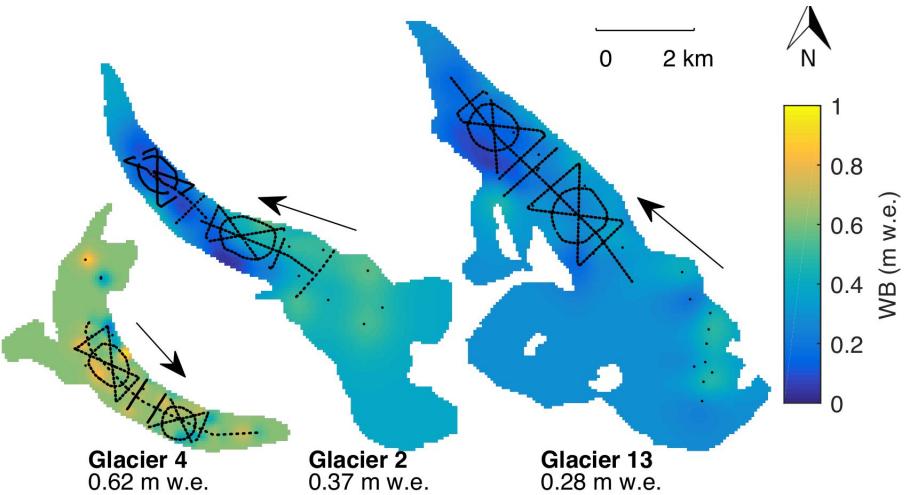
# LR - MLR vs BMA



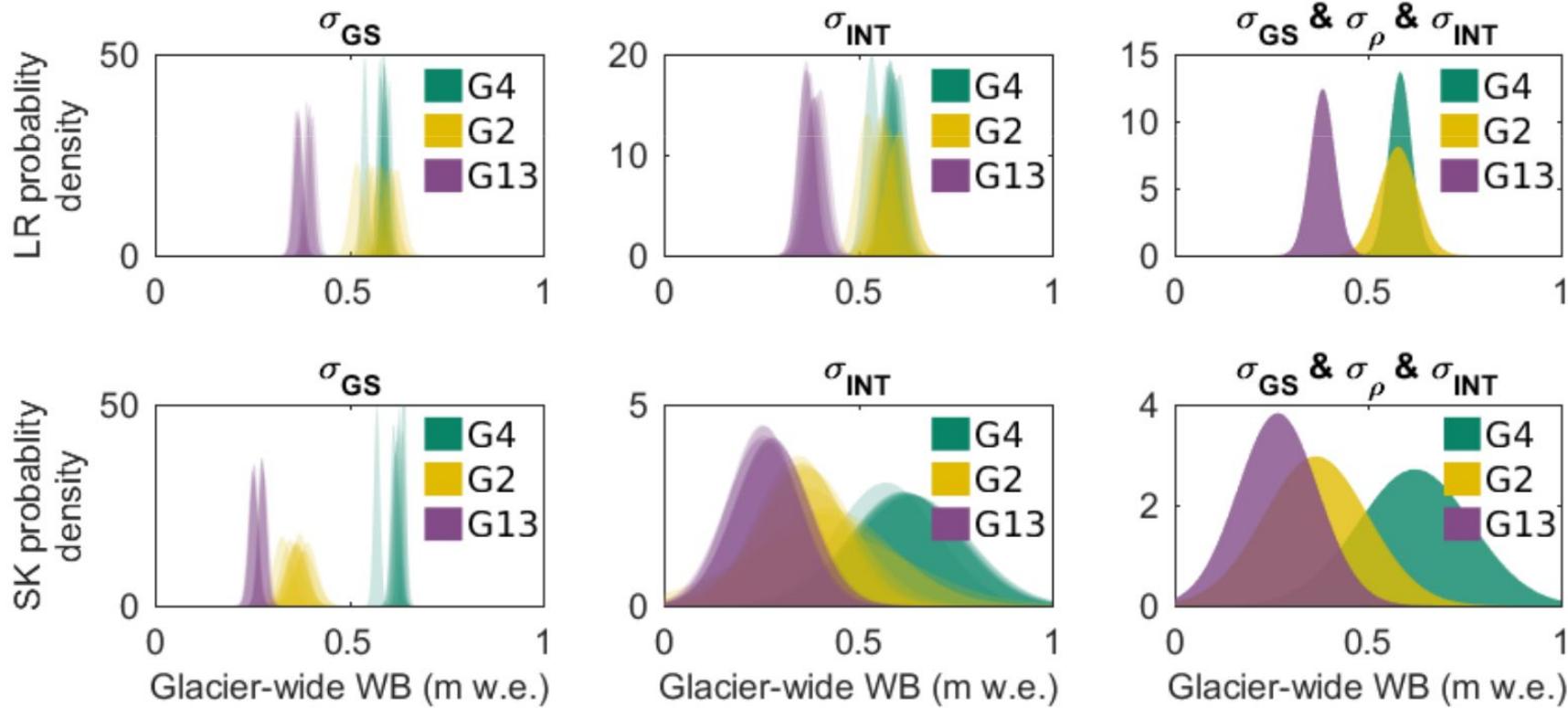
# LR AND SK ESTIMATES - GOF



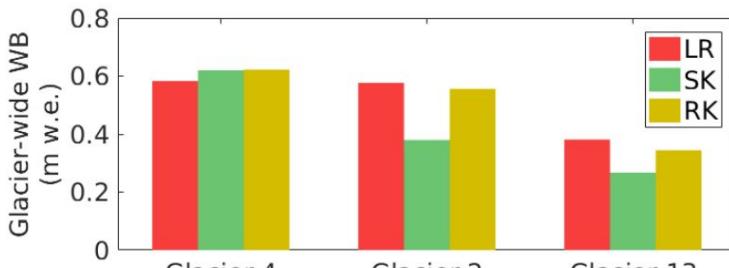
# SIMPLE KRIGING



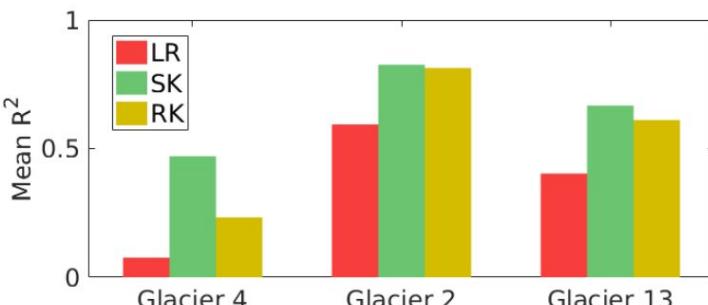
# WB PDFs FOR LR AND SK



# COMPARISON OF INTERPOLATIONS



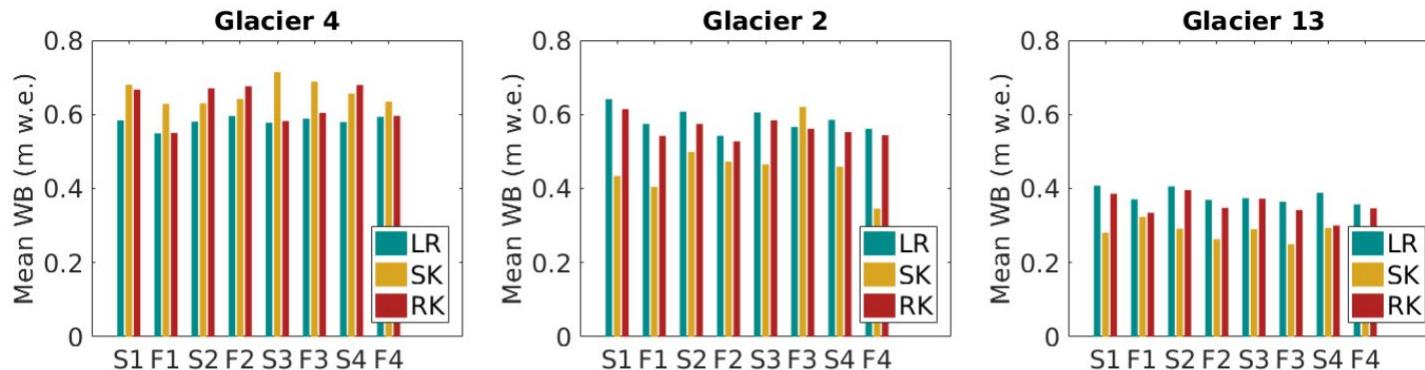
(a)



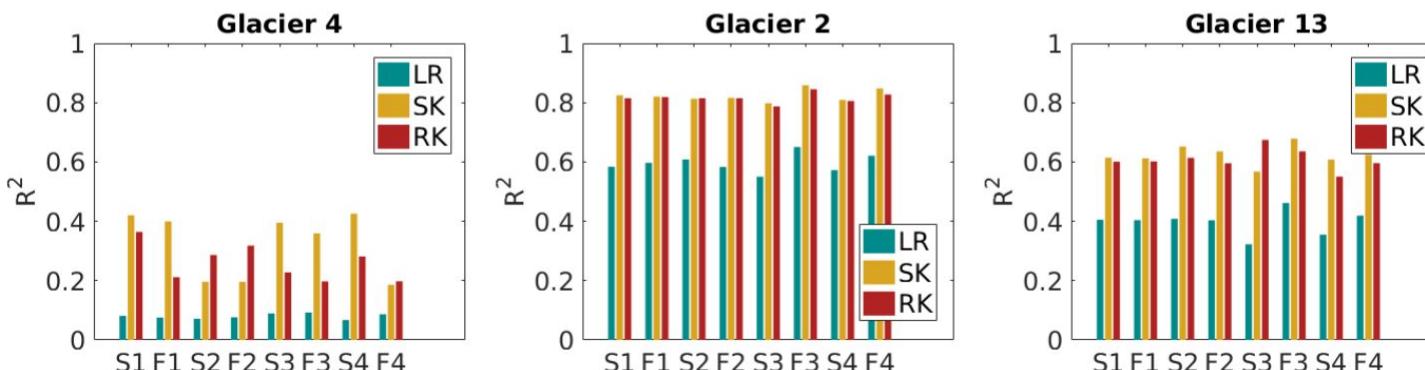
(b)

Figure 5.33: Comparison of winter balance (WB) and  $R^2$  for topographic regression (LR), simple kriging (SK) and regression kriging (RK), averaged over density assignment methods. (a) Glacier-wide WB. (b) Mean correlation coefficient ( $R^2$ ) between observed winter balance and estimated winter balance at sampling locations.

# COMPARISON OF INTERPOLATION WITH DENSITY

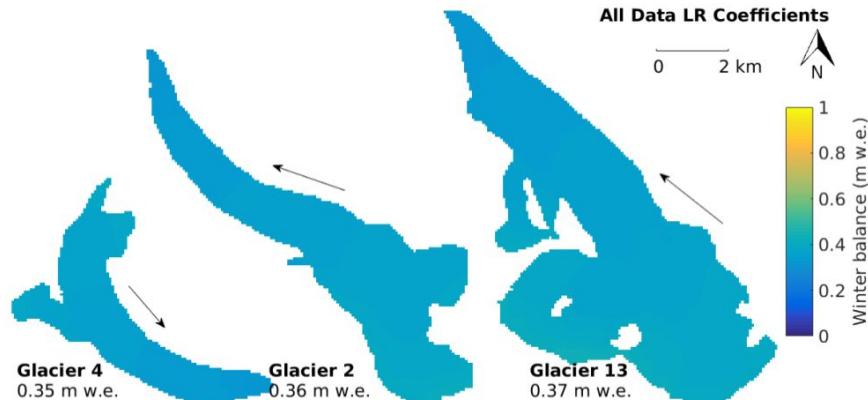
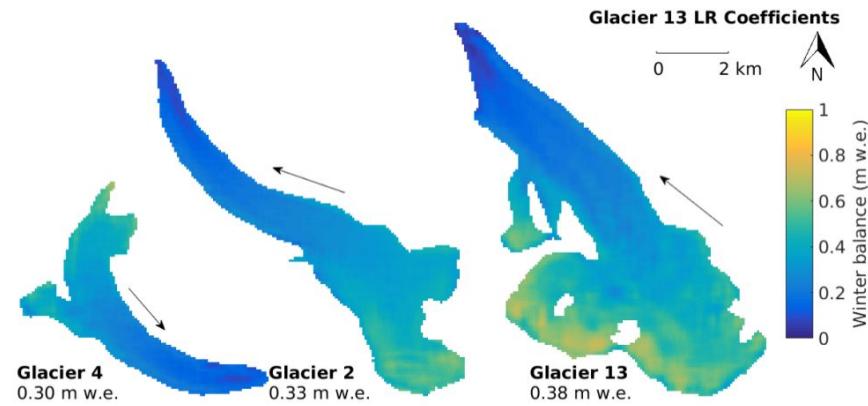
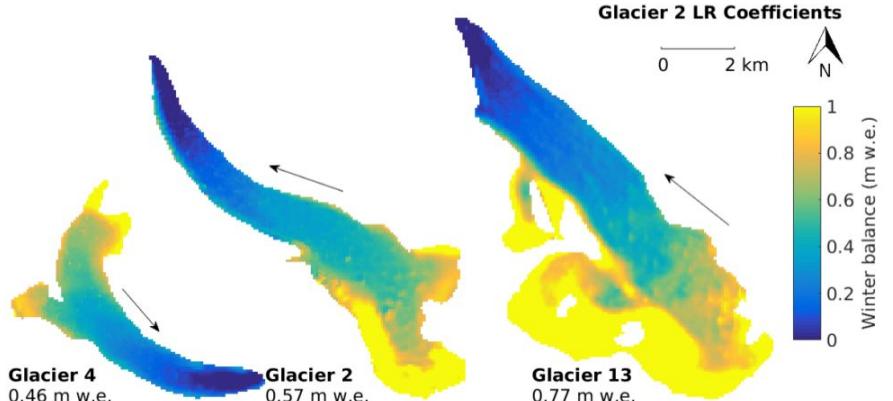
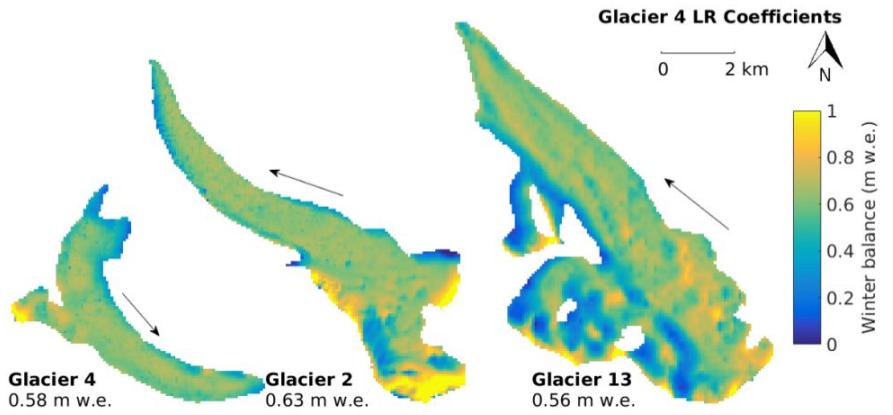


(a)

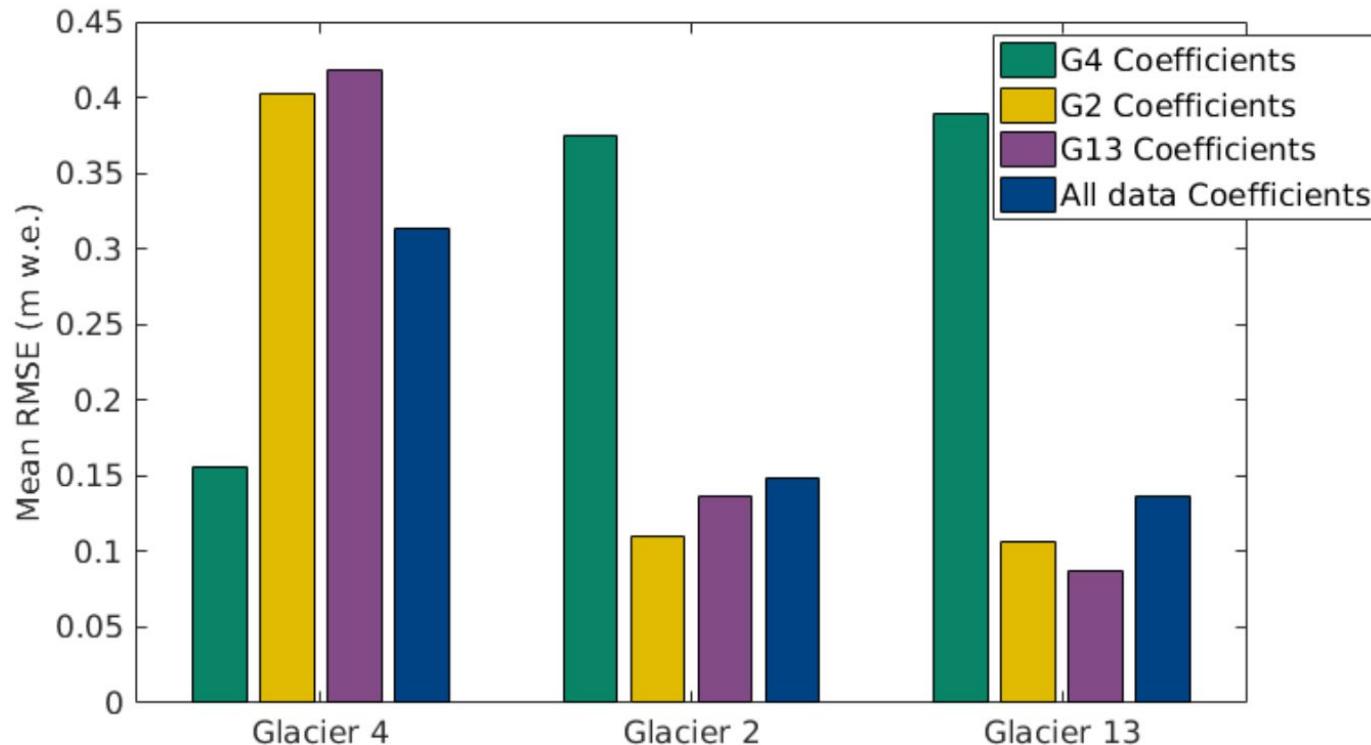


(b)

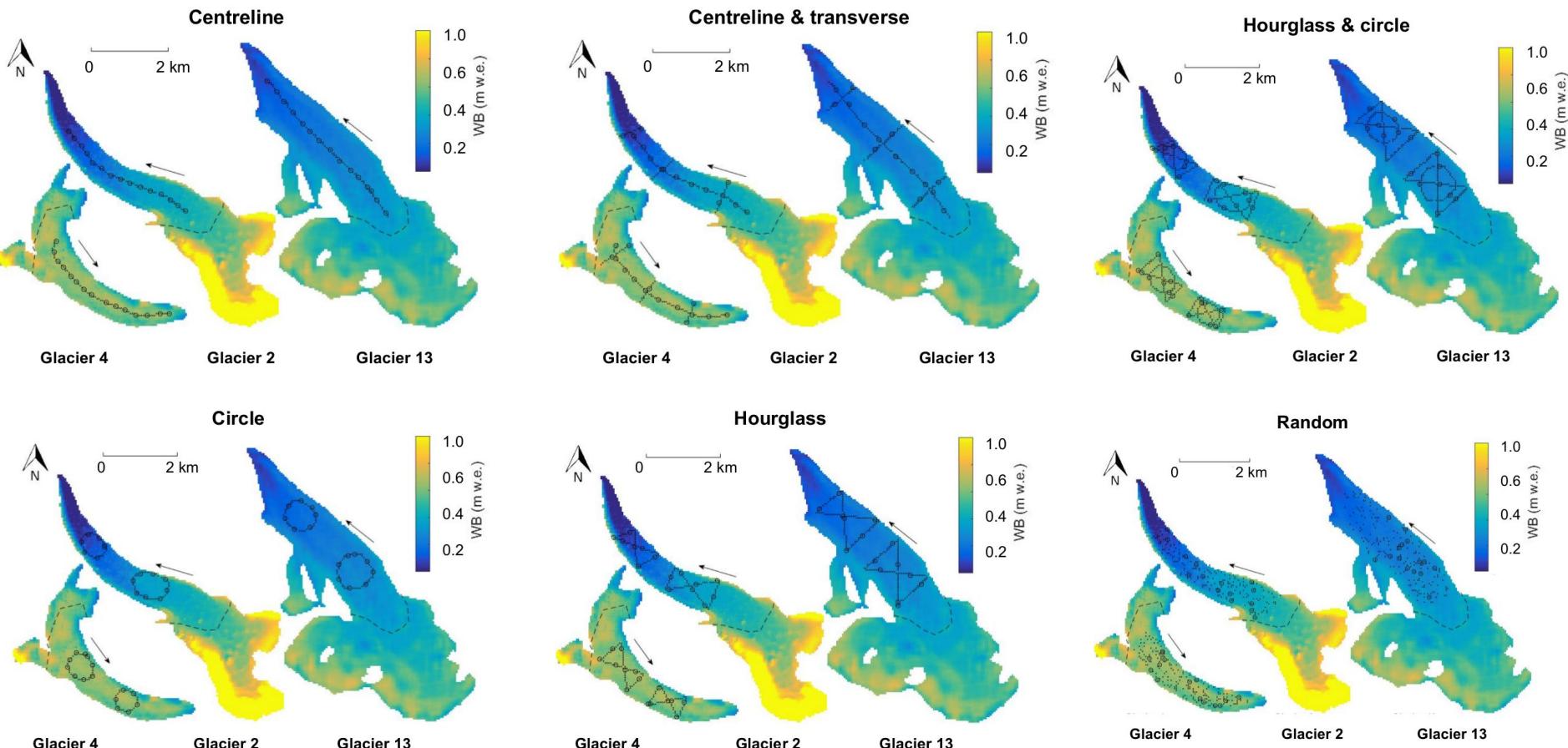
# LR TRANSFERABILITY



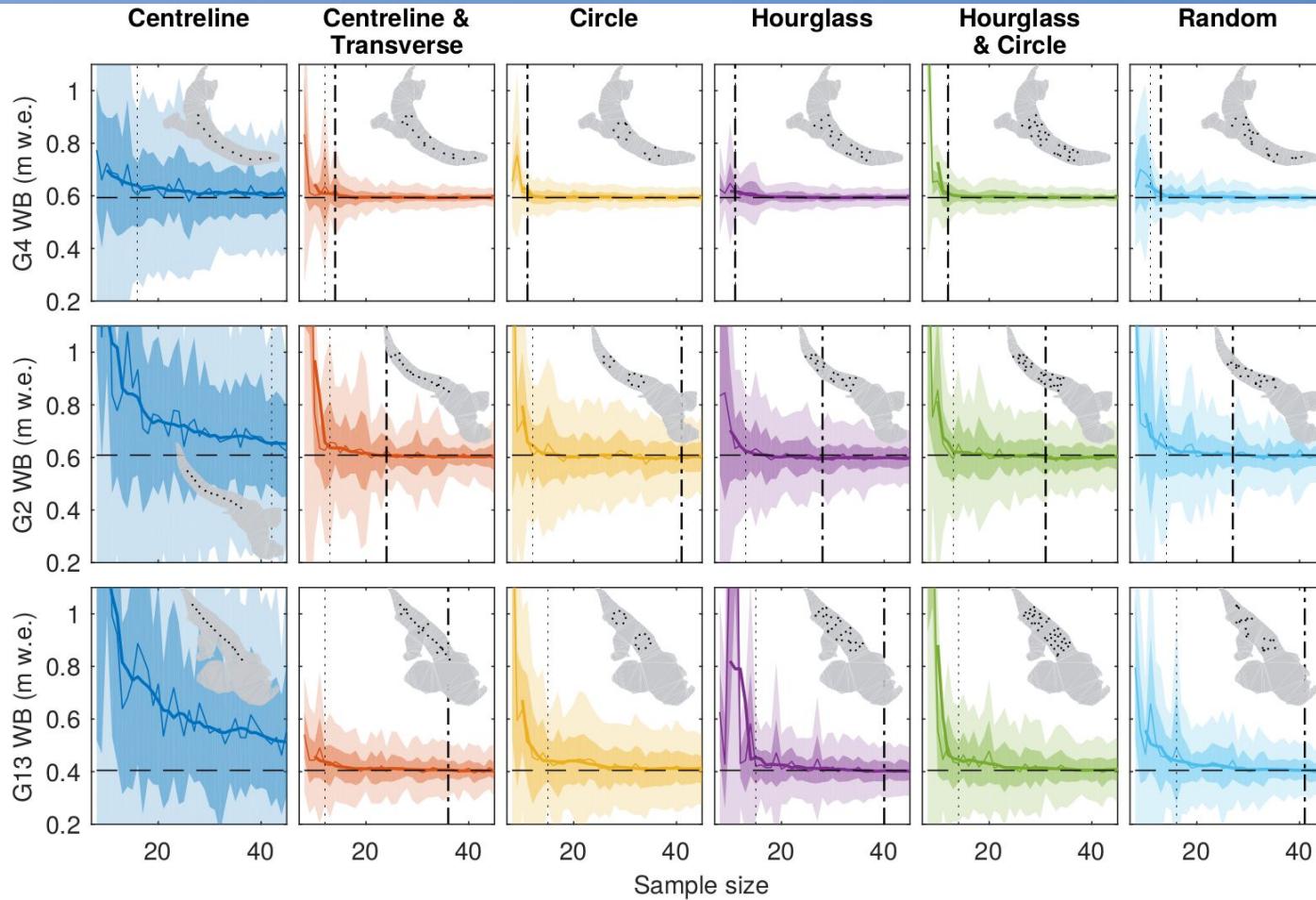
# TRANSFERABILITY ERROR



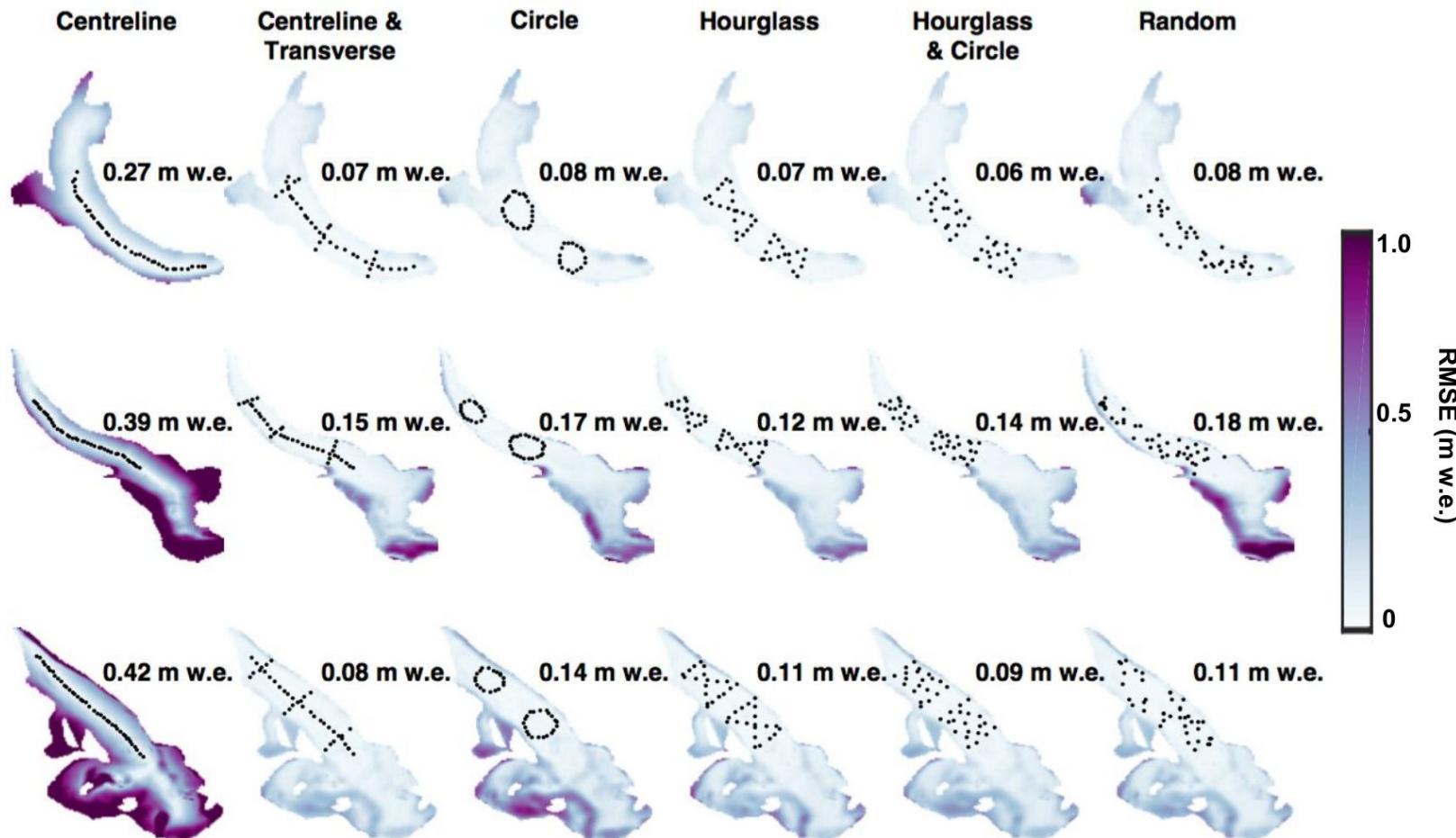
# SAMPLING SCHEMES



# SYNTHETIC DATA - SAMPLING DESIGN



# SYNTHETIC DATA ERROR



# REAL DATA SAMPLING DESIGN WB

