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# Estimating winter balance and its uncertainty from direct

## measurements of snow depth and density on alpine glaciers

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ABSTRACT. Accurately estimating winter surface mass balance on glaciers is central to assessing glacier health and predicting glacier runoff. However, measuring and modelling snow distribution is inherently difficult in mountainous terrain. Here we explore rigorous statistical methods of estimating winter balance and its uncertainty from multiscale measurements of snow depth and density. In May 2016 we collected over 9000 manual measurements of snow depth across three glaciers in the St. Elias Mountains, Yukon, Canada. Linear regression, combined with cross correlation and Bayesian model averaging, as well as simple kriging are used to interpolate point-scale values to glacier-wide estimates of winter balance. Elevation and a wind-redistribution parameter exhibit the highest correlations with winter balance, but the relationship varies considerably between glaciers. A Monte Carlo analysis reveals that the interpolation itself introduces more uncertainty than the assignment of snow density or the representation of grid-scale variability. For our study glaciers, the winter balance uncertainty from all assessed sources ranges from  $0.03 \,\mathrm{m}$  w.e. (8%) to  $0.15 \,\mathrm{m}$  w.e. (54%). Despite the challenges associated with estimating winter balance, our results are consistent with a regional-scale winter-balance gradient.

#### 26 INTRODUCTION

Winter surface mass balance, or "winter balance", is the net accumulation and ablation of snow over the 27 winter season (Cogley and others, 2011), which constitutes glacier mass input. Winter balance is half of the 28 seasonally resolved mass balance, initializes summer ablation conditions and must be estimated to simulate 29 energy and mass exchange between the land and atmosphere (e.g. Hock, 2005; Réveillet and others, 2016). 30 Effectively representing the spatial distribution of snow is also central to monitoring surface runoff and its 31 downstream effects (e.g. Clark and others, 2011). 32 Winter balance (WB) is notoriously difficult to estimate (e.g. Dadić and others, 2010; Cogley and others, 33 2011). Snow distribution in alpine regions is highly variable with short correlation length scales (e.g. Anderton 34 and others, 2004; Egli and others, 2011; Grünewald and others, 2010; Helbig and van Herwijnen, 2017; López-35 Moreno and others, 2011, 2013; Machguth and others, 2006; Marshall and others, 2006) and is influenced by 36 dynamic interactions between the atmosphere and complex topography, operating on multiple spatial and 37 temporal scales (e.g. Barry, 1992; Liston and Elder, 2006; Clark and others, 2011). Simultaneously extensive, 38 high resolution and accurate snow distribution measurements on glaciers are therefore difficult to obtain 39 (e.g. Cogley and others, 2011; McGrath and others, 2015) and is further complicated by the inaccessibility 40 of many glacierized regions during the winter. Physically based models are computationally intensive and 41 require detailed meteorological data to drive them (Dadić and others, 2010). As a result, there is significant 42 uncertainty in estimates of winter balance, thus limiting the ability of models to represent current and 43 projected glacier conditions. 44 Studies that have focused on obtaining detailed estimates of WB have used a wide range of observational 45 techniques, including direct measurement of snow depth and density (e.g. Cullen and others, 2017), lidar 46 or photogrammerty (e.g. Sold and others, 2013) and ground-penetrating radar (e.g. Machguth and others, 47 2006; Gusmeroli and others, 2014; McGrath and others, 2015). Spatial coverage of direct measurements is generally limited and comprises an elevation transect along the glacier centreline (e.g. Kaser and others, 49 2003). Measurements are often interpolated using linear regression on only a few topographic parameters (e.g. 50 MacDougall and Flowers, 2011), with elevation being the most common. Other established techniques include hand contouring (e.g. Tangborn and others, 1975), kriging (e.g. Hock and Jensen, 1999) and attributing 52 measured winter balance values to elevation bands (e.g. Thibert and others, 2008). Physical snow models 53 have been used to estimate spatial patterns of winter balance (e.g. Mott and others, 2008; Schuler and others, 2008; Dadić and others, 2010) but availability of the required meteorological data generally prohibits their 55

widespread application. Error analysis is rarely undertaken and few studies have thoroughly investigated uncertainty in spatially distributed estimates of winter balance (c.f. Schuler and others, 2008).

More sophisticated snow-survey designs and statistical models of snow distribution are widely used in the 58 field of snow science. Surveys described in the snow science literature are generally spatially extensive and 59 designed to measure snow depth and density throughout a basin, ensuring that all terrain types are sampled. 60 61 A wide array of measurement interpolation methods are used, including linear (e.g. López-Moreno and others, 2010) and non-linear regressions (e.g. Molotch and others, 2005) that include numerous terrain parameters, as well as geospatial interpolation (e.g. Erxleben and others, 2002; Cullen and others, 2017) including various 63 forms of kriging. Different interpolation methods are also combined; for example, regression kriging adds 64 kriged residuals to a field obtained with linear regression (e.g. Balk and Elder, 2000). Physical snow models such as SnowTran-3D (Liston and Sturm, 1998), Alpine3D (Lehning and others, 2006), and SnowDrift3D 66 (Schneiderbauer and Prokop, 2011) are widely used, and errors in estimating snow distribution have been 67 examined from theoretical (e.g. Trujillo and Lehning, 2015) and applied perspectives (e.g. Turcan and Loijens, 68 1975; Woo and Marsh, 1978; Deems and Painter, 2006). 69 70 The goals of this study are to (1) critically examine methods of converting direct snow depth and density

The goals of this study are to (1) critically examine methods of converting direct snow depth and density
measurements to distributed estimates of winter balance and (2) identify sources of uncertainty, evaluate
their magnitude and assess their combined contribution to uncertainty in glacier-wide winter balance. We
focus on commonly applied, low-complexity methods of measuring and estimating winter balance in the
interest of making our results broadly applicable.

#### 75 STUDY SITE

The St. Elias Mountains (Fig. 1a) rise sharply from the Pacific Ocean, creating a significant climatic gradient 76 between coastal maritime conditions, generated by Aleutian-Gulf of Alaska low-pressure systems, and interior 77 continental conditions, driven by the Yukon-Mackenzie high-pressure system (Taylor-Barge, 1969). The 78 boundary between the two climatic zones is generally aligned with the divide between the Hubbard and 79 Kaskawulsh Glaciers, approximately 130 km from the coast. Research on snow distribution and glacier mass 80 balance in this area is limited. A series of research programs, including Project "Snow Cornice" and the Icefield Ranges Research Project, were operational in the 1950s and 60s (Wood, 1948; Danby and others, 82 2003) and in the last 30 years, there have been a few long-term studies on selected alpine glaciers (e.g. Clarke, 83 2014) as well as several regional studies of glacier mass balance and dynamics (e.g. Arendt and others, 2008; Burgess and others, 2013; Waechter and others, 2015). 85

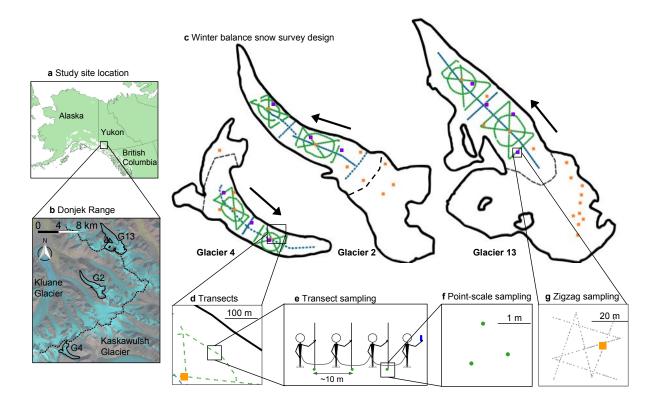


Fig. 1. Study area location and sampling design for Glaciers 4, 2 and 13. (a) Study region in the Donjek Range of the St. Elias Mountains of Yukon, Canada. (b) Study glaciers located along a southwest-northeast transect through the Donjek Range. The local topographic divide is shown as a dashed line. Imagery from Landsat8 (5 September 2013, data available from the U.S. Geological Survey). (c) Details of the snow-survey sampling design, with centreline and transverse transects (blue dots), hourglass and circle designs (green dots) and locations of snow density measurements (orange squares). Arrows indicate ice-flow directions. Approximate location of ELA on each glacier is shown as a black dashed line. (d) Close up of linear and curvilinear transects. (e) Configuration of navigator and observers. (f) Point-scale snow-depth sampling. (g) Linear-random snow-depth measurements in 'zigzag' design (purple dots) with one density measurement (orange square) per zigzag.

We carried out winter balance surveys on three unnamed glaciers in the Donjek Range of the St. Elias Mountains. The Donjek Range is located approximately 40 km to the east of the regional mountain divide and has an area of about 30 × 30 km<sup>2</sup>. Glacier 4, Glacier 2 and Glacier 13 (labelling adopted from Crompton and Flowers (2016)) are located along a southwest-northeast transect through the range (Fig. 1b, Table 1). These small alpine glaciers are generally oriented southeast-northwest, with Glacier 4 having a predominantly southeast aspect and Glaciers 2 and 13 have generally northwest aspects. The glaciers are situated in valleys with steep walls and have simple geometries. Based on a detailed study of Glacier 2 (Wilson and others,

**Table 1.** Physical characteristics of the study glaciers.

	Location		Ele	vation (m a	Slope (°)	Area	
	UTM	Zone 7	Mean Range		ELA	Mean	$(km^2)$
Glacier 4	$595470~\mathrm{E}$	6740730  N	2344	1958-2809	$\sim 2500$	12.8	3.8
Glacier 2	601160 E	6753785 N	2495	1899-3103	$\sim 2500$	13.0	7.0
Glacier 13	$604602 \; \mathrm{E}$	6763400 N	2428	1923-3067	~2380	13.4	12.6

2013) and related theoretical modelling (Wilson and Flowers, 2013) we suspect all of the study glaciers to be polythermal.

#### 95 METHODS

Estimating glacier-wide winter balance involves transforming measurements of snow depth and density into 96 values of winter balance distributed across a defined grid. We do this in four steps. (1) Obtain direct 97 measurements of snow depth and density in the field. (2) Assign density values to all depth-measurement 98 locations to calculate point-scale values of WB at each location. (3) Average all point-scale values within 99 each gridcell of a digital elevation model (DEM) to obtain the gricell-averaged WB. (4) Interpolate and 100 extrapolate these gridcell-averaged WB values to obtain estimates of WB (in mw.e.) in each gridcell across 101 the domain. Glacier-wide WB is then calculated by taking the average of all gridcell-averaged WB values 102 for each glacier. For brevity, we refer to these four steps as (1) field measurements, (2) density assignment, 103

Table 2. Details of the May 2016 winter-balance survey, including number of snow-depth measurement locations along transects  $(n_{\rm T})$ , total length of transects  $(d_{\rm T})$ , number of combined snow pit and Federal Sampler density measurement locations  $(n_{\rho})$ , number of zigzag surveys  $(n_{\rm zz})$ , number (and as percent of total number of gridcells) of gridcells sampled  $(n_{\rm S})$  and the elevation range (and as percent of total elevations range).

	Date	$n_{\mathrm{T}}$	$d_{\mathrm{T}}$ (km)	$n_{ ho}$	$n_{zz}$	$n_{ m S}$	Elevation range (ma.s.l.)
Glacier 4	4–7 May 2016	649	13.1	7	3	295	2015–2539
						(12%, 21%)	(62%, 97%)
Glacier 2	8–11 May 2016	762	13.6	7	3	353	2151 – 2541
						(8%, 14%)	(32%,47%)
Glacier 13	12–15 May 2016	941	18.1	19	4	468	2054 – 2574
						(6%, 14%)	(45%,62%)

(3) gridcell-averaged WB and (4) distributed WB. Detailed methodology for each step is outlined below. We use the SPIRIT SPOT-5 DEM (40×40 m) from 2005 (Korona and others, 2009) throughout this study.

### 106 Field measurements

!!!!!!!!!!! In total, we collected more than 9000 snow-depth measurements throughout the study area (Table 107 1). Winter balance can be estimated as the product of snow depth and depth-averaged density. Our sampling 108 campaign involved four people and occurred between 5-15 May 2016, which falls within the period of historical 109 peak snow accumulation in southwestern Yukon (Yukon Snow Survey Bulletin and Water Supply Forecast, 110 May 1, 2016). During the field campaign there were two small accumulation events. The first, on 6 May 111 2016, also involved high winds so accumulation could not be determined. The second, on 10 May 2016, 112 resulted in 0.01 m w.e accumulation measured at one location on Glacier 2. Positive temperatures and clear 113 skies occurred between 11–16 May 2016, which we suspect resulted in melt occurring on Glacier 13. The 114 snow in the lower part of the ablation area of Glacier 13 was isothermal and showed clear signs of melt and 115 metamorphosis. The total amount of accumulation and melt during the study period was not be estimated 116 so no corrections were made. 117

#### 118 Sampling design

The snow surveys were designed to capture variability in snow depth at regional, basin, gridcell and point 119 scales (Clark and others, 2011). To capture variability at the regional scale we chose three glaciers along 120 a transect aligned with the dominant precipitation gradient (Fig. 1) (Taylor-Barge, 1969). To account for 121 basin-scale variability, snow depth was measured along linear and curvilinear transects on each glacier (Fig. 122 1c) with a sample spacing of 10–60 m (Fig. 1d). Sample spacing was constrained by protocols for safe glacier 123 travel, while survey scope was constrained by the need to complete all surveys within the period of peak 124 accumulation. We selected centreline and transverse transects as the most commonly used survey designs 125 in winter balance studies (e.g. Kaser and others, 2003; Machguth and others, 2006) as well as an hourglass 126 pattern with an inscribed circle, which allows for sampling in multiple directions and easy travel (personal 127 communication from C. Parr, 2016). To capture variability at the grid scale, we densely sampled up to four 128 gridcells on each glacier using a linear-random sampling design (Shea and Jamieson, 2010) we term a 'zigzag'. 129 To capture point-scale variability, each observer made 3-4 depth measurements within  $\sim 1$  m (Fig. 1f) at 130 each transect measurement location. 131

132 Snow depth: transects

Snow depth is generally accepted to be more variable than density (Elder and others, 1991; Clark and others, 133 2011; López-Moreno and others, 2013) so we chose a sampling design that resulted in a high ratio ( $\sim$ 55:1) of 134 snow depth to density measurements. While roped-up for glacier travel with fixed distances between observers, 135 the lead observer used a single-frequency GPS unit (Garmin GPSMAP 64s) to navigate between predefined 136 137 transect measurement locations (Fig. 1e). The remaining three observers used 3.2 m graduated aluminum avalanche probes to make snow-depth measurements. The locations of each set of depth measurements, made 138 by the second, third and fourth observers, are estimated using the recorded location of the first observer, the 139 approximate distance between observers and the direction of travel. The 3-4 point-scale depth measurements 140 are averaged to obtain a single depth measurement at each transect measurement location. When considering 141 snow variability at the point scale as a source of uncertainty in snow depth measurements, we find that the 142 mean standard deviation of point-scale snow depth measurements is found to be <7% of the mean snow 143 depth for all study glaciers. 144 Snow-depth sampling was concentrated in the ablation area to ensure that only snow from the current 145 accumulation season was measured. The boundary between snow and firn in the accumulation area can be 146 difficult to detect and often misinterpreted, especially when using an avalanche probe (Grünewald and others, 147

accumulation season was measured. The boundary between snow and firn in the accumulation area can be difficult to detect and often misinterpreted, especially when using an avalanche probe (Grünewald and others, 2010; Sold and others, 2013). We intended to use a firn corer to measure winter balance in the accumulation area, but cold snow combined with positive air temperatures led to cores being unrecoverable. Successful snow depth measurements within the accumulation area were made either in snow pits or using a Federal Sampler (described below) to unambiguously identify the snow firn transition.

151 Sampler (described below) to unambiguously identify the snow-firn transition.

152 Snow depth: zigzags

153 We measured depth at random intervals of 0.3–3.0 m along two 'Z'-shaped patterns (Shea and Jamieson,

154 2010), resulting in 135–191 measurements per zigzag, within three to four  $40 \times 40$  m gridcells (Fig. 1g) per

155 glacier. Random intervals were machine-generated from a uniform distribution in sufficient numbers that

each survey was unique. Zigzag locations were randomly chosen within the upper, middle and lower regions

of the ablation area of each glacier. Extra time in the field allowed us to measure a fourth zigzag on Glacier

158 13 in the central ablation area at  $\sim$ 2200 m a.s.l.

159 Snow density

160 Snow density was measured using a Snowmetrics wedge cutter in three snow pits on each glacier. Within

the snow pits (SP), we measured a vertical density profile (in 5 cm increments) with the  $5 \times 10 \times 10$  cm

wedge-shaped cutter (250 cm<sup>3</sup>) and a Presola 1000 g spring scale (e.g. Gray and Male, 1981; Fierz and others, 162 2009). Wedge-cutter error is approximately  $\pm 6\%$  (e.g. Proksch and others, 2016; Carroll, 1977). Uncertainty 163 in estimating density from SP measurements also stems from incorrect assignment of density to layers that 164 cannot be sampled (e.g. ice lenses and hard layers). We attempt to quantify this uncertainty by varying 165 estimated ice-layer thickness by  $\pm 1$  cm (<100%) of the recorded thickness, ice layer density between 700 166 and  $900 \,\mathrm{kg} \,\mathrm{m}^{-3}$  and the density of layers identified as being too hard to sample (but not ice) between 600167 and 700 kg m<sup>-3</sup>. When considering all three sources of uncertainty, the range of integrated density values 168 is always less than 15% of the reference density. Depth-averaged densities for shallow pits (<50 cm) that 169 contain ice lenses are particularly sensitive to changes in prescribed density and ice-lens thickness. 170 While SP provide the most accurate measure of snow density, digging and sampling a SP is time and 171 labour intensive. Therefore, a Geo Scientific Ltd. metric Federal Sampler (FS) (Clyde, 1932) with a 3.2– 172 3.8 cm diameter sampling tube, which directly measures depth-integrated snow-water equivalent, was used 173 to augment the snow pit measurements. A minimum of three FS measurements were taken at each of 7–19 174 locations on each glacier and an additional eight FS measurements were co-located with each snow pit profile. 175 176 Measurements for which the snow core length inside the sampling tube was less than 90% of the snow depth were discarded. Densities at each measurement location (eight at each snow pit, three elsewhere) were then 177 averaged, with the standard deviation taken to represent the uncertainty. The mean standard deviation of 178 FS-derived density was  $\leq 4\%$  of the mean density for all glaciers.

#### Density assignment

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Measured snow density must be interpolated or extrapolated to estimate point-scale winter balance at each 181 snow-depth sampling location. We employ four commonly used methods to interpolate and extrapolate 182 density (Table 3): (1) calculate mean density over an entire mountain range (e.g. Cullen and others, 2017), 183 (2) calculate mean density for each glacier (e.g. Elder and others, 1991; McGrath and others, 2015), (3) 184 linear regression of density on elevation for each glacier (e.g. Elder and others, 1998; Molotch and others, 185 186 2005) and (4) calculate mean density using inverse-distance weighting (e.g. Molotch and others, 2005) for each glacier. Densities derived from SP and FS measurements are treated separately, for reasons explained 187 below, resulting in eight possible methods of assigning density. 188

#### Gridcell-averaged winter balance 189

We average one to six (mean of 2.1 measurements) point-scale values of WB within each  $40 \times 40 \,\mathrm{m}$  DEM 190 gridcell to obtain the gricell-averaged WB. The locations of individual measurements have uncertainty due to 191

**Table 3.** Eight methods used to estimate snow density at unmeasured locations. Total number of resulting density values given in parentheses, with  $n_T$  the total number of snow-depth measurement locations along transects (Table 1).

Method	Source of	measured	Density assignment		
code	snow o	density	method		
code	Snow pit	Federal	movilou.		
	Snow pu	Sampler			
S1			Mean of measurements		
F1			across all glaciers (1)		
S2			Mean of measurements		
F2			for each glacier (3)		
S3			Regression of density on		
F3		•	elevation for a glacier $(n_T)$		
S4			Inverse distance weighted		
F4			mean for a glacier $(n_T)$		

the error in the horizontal position given by the GPS unit and the estimation of observer location based on the recorded GPS positions of the navigator. This location uncertainty could result in the incorrect assignment of a point-scale WB to a particular gridcell. However, this source of error is not further investigated because we assume that the uncertainty in gridcell-averaged WB is captured in the zigzag measurements described below. Error due to having multiple observers is also evaluated by conducting an analysis of variance (ANOVA) of snow-depth measurement along a transect and testing for differences between observers. We find no significant differences between snow-depth measurements made by observers along any transect (p>0.05), with the exception of the first transect on Glacier 4 (51 measurements), where snow depth values collected by one observer were, on average, greater than the snow depth measurements taken by the other two observers (p<0.01). Since this was the first transect completed and the only one to show differences by observer, this difference can be considered an anomaly. This result shows that observer bias is likely to not affect the results of this study and no corrections to the data based on observer were applied.

#### Distributed winter balance

Gridcell-averaged values of WB are interpolated and extrapolated across each glacier using linear regression (LR) and simple kriging (SK). The LR relates gridcell-averaged WB and various topographic parameters, as this method is simple and has precedent for success (e.g. McGrath and others, 2015). Instead of a basic LR

however, we use cross-validation and model averaging to test all combinations of the topographic parameters. 208

We compare the LR approach with SK, a data-driven interpolation method free of any physical interpretation

(e.g. Hock and Jensen, 1999). 210

#### Linear regression 211

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In the LR, we use commonly applied topographic parameters as in McGrath and others (2015), including 212 elevation, slope, aspect, curvature, "northness" and a wind-redistribution parameter (Sx from Winstral 213 and others (2002)); we add distance-from-centreline as an additional parameter. Topographic parameters are 214 standardized for use in the LR. For details on data and methods used to estimate the topographic parameters 215 216 see the Supplementary Material. Our sampling design ensured that the ranges of topographic parameters associated with our measurement locations represent more than 70% of the total area of each glacier (except 217 elevation on Glacier 2, where our measurements captured only 50%).

The goal of the LR is to obtain a set of fitted regression coefficients  $(\beta_i)$  that correspond to each topographic 219 parameter and to a model intercept. The LR implemented in this study is an extension of a basic multiple linear regression; we use cross-validation to avoid overfitting the data and model averaging to incorporate 221 every possible combination of topographic parameters. 222

First, cross-validation is used to obtain a set of regression coefficients that have the greatest predictive 223 ability (Kohavi and others, 1995). We randomly select 1000 subsets of the data (2/3 of the values) and fit 224 a basic multiple linear regression (implemented in MATLAB) to the data subsets, thus obtaining 1000 sets 225 of regression coefficients. The basic multiple linear regression calculates a set of regression coefficients by 226 minimizing the sum of squares of the vertical deviations of each datum from the regression line (Davis and 227 Sampson, 1986). Distributed winter balance is then calculated by weighting each topographic parameter by 228 the corresponding regression coefficient for all DEM gridcells. We then use the remaining data (1/3) of the 229 values) to calculate a root mean squared error (RMSE) between the estimated WB and the observed WB for 230 corresponding locations. From the 1000 sets of  $\beta_i$  values, we select the set that results in the lowest RMSE. 231 Second, we use model averaging to account for uncertainty when selecting predictors and to maximize 232 the model's predictive ability (Madigan and Raftery, 1994). Models are generated by calculating a set of 233 regression coefficients as described above for all possible combinations of topographic parameters (resulting in 234 2<sup>7</sup> models, or sets of regression coefficients). Using a Bayesian framework, model averaging involves weighting 235 all models by their posterior model probabilities (Raftery and others, 1997). The models (i.e. sets of regression 236 coefficients) are weighted according to the relative predictive success of the model, as assessed by the value 237

of the Bayesian Information Criterion (BIC) (Burnham and Anderson, 2004). BIC penalizes more complex models which further reduces the risk of overfitting. The final set of regression coefficients is then the weighted sum of regression coefficients from all models. Distributed WB is obtained by applying the final set of regression coefficients to the topographic parameters associated with each gridcell.

#### 242 Simple kriging

SK is a data-driven method of estimating variables at unsampled locations by using the isotropic spatial 243 244 correlation (covariance) of measured values to find a set of optimal weights (Davis and Sampson, 1986; Li and Heap, 2008). SK assumes spatial correlation between sampling locations that are distributed across a 245 surface and then applies the correlation to interpolate between these locations. We used the DiceKriging 246 R package (Roustant and others, 2012) to calculate the maximum likelihood covariance matrix, as well as 247 the range distance  $(\theta)$  and nugget for gridcell-averaged values of winter balance. The range distance is a 248 measure of data correlation length and the nugget is the residual that encompasses sampling-error variance 249 as well as the spatial variance at distances less than the minimum sample spacing (Li and Heap, 2008). A 250 Matére covariance function with  $\nu=5/2$  is used to define a stationary and isotropic covariance and covariance 251 kernels are parameterized as in Rasmussen and Williams (2006). Unlike LR, SK is not useful for generating 252 hypotheses to explain the physical controls on snow distribution, nor can it be used to estimate winter 253 balance on unmeasured glaciers. 254

#### 255 Uncertainty analysis using a Monte Carlo approach

Three sources of uncertainty are considered separately: the uncertainty due to (1) grid-scale variability of 256 WB ( $\sigma_{GS}$ ), (2) the assignment of snow density ( $\sigma_{\rho}$ ) and (3) interpolating and extrapolating gridcell-averaged 257 values of WB ( $\sigma_{\text{INT}}$ ). To quantify the uncertainty of grid-scale and interpolation uncertainty on estimates of 258 glacier-wide WB we conduct a Monte Carlo analysis, which uses repeated random sampling of input variables 259 to calculate a distribution of output variables (Metropolis and Ulam, 1949). We repeat the random sampling 260 process 1000 times, resulting in a distribution of values of the glacier-wide WB based on uncertainties 261 associated with the four steps outlined above. Density assignment uncertainty is calculated as the standard 262 deviation of the eight resulting values of glacier-wide winter balance. Individual sources of uncertainty are 263 propagated through the conversion of snow depth and density measurements to glacier-wide WB. Finally, the 264 combined effect of all three sources of uncertainty on the glacier-wide WB is quantified. We use the standard 265 deviation of this distribution as a useful metric of uncertainty on the glacier-wide WB. We calculate a relative 266

uncertainty as the normalized sum of differences between every pair of one hundred distributed WB estimates including  $\sigma_{GS}$  and  $\sigma_{INT}$ .

269 Grid-scale uncertainty ( $\sigma_{GS}$ )

We make use of the zigzag surveys to quantify the true variability of WB at the grid scale. Our limited data 270 do not permit a spatially-resolved assessment of grid-scale uncertainty, so we characterize this uncertainty 271 as uniform across each glacier and represent it by a normal distribution. The distribution is centred at zero 272 and has a standard deviation equal to the mean standard deviation of all zigzag measurements for each 273 glacier. For each iteration of the Monte Carlo, WB values are randomly chosen from the distribution and 274 added to the values of gridcell-averaged WB. These perturbed gridcell-averaged values of WB are then used 275 in the interpolation. We represent uncertainty in glacier-wide WB due to grid-scale uncertainty ( $\sigma_{\rm GS}$ ) as the 276 standard deviation of the resulting distribution of glacier-wide WB estimates. 277

278 Density assignment uncertainty  $(\sigma_{\rho})$ 

We incorporate uncertainty due to the method of density assignment by carrying forward all eight density interpolation methods (Table 3) when estimating glacier-wide WB. By choosing to retain even the least plausible options, as well as the questionable FS data, this approach results in a generous assessment of uncertainty. We represent the glacier-wide WB uncertainty due to density assignment uncertainty ( $\sigma_{\rho}$ ) as the standard deviation of glacier-wide WB estimates calculated using each density assignment method.

284 Interpolation uncertainty ( $\sigma_{\text{INT}}$ )

We represent the uncertainty due to interpolation of gridcell-averaged WB in different ways for LR and SK. LR interpolation uncertainty is represented by a multivariate normal distribution of possible regression coefficients ( $\beta_i$ ). The standard deviation of each distribution is calculated using the covariance of regression coefficients as outlined in Bagos and Adam (2015), which ensures that regression coefficients are internally consistent. The  $\beta_i$  distributions are randomly sampled and used to calculate gridcell-estimated WB.

SK interpolation uncertainty is represented by the standard deviation for each gridcell-estimated value of WB generated by the DiceKriging package. The standard deviation of glacier-wide WB is then found by taking the square root of the average variance of each gridcell-estimated WB. The final distribution of glacier-wide WB values is centred at the glacier-wide WB estimated with SK. For simplicity, the standard deviation of glacier-wide WB values that result from either LR or SK interpolation uncertainty is referred

295 to as  $\sigma_{\rm INT}$ .

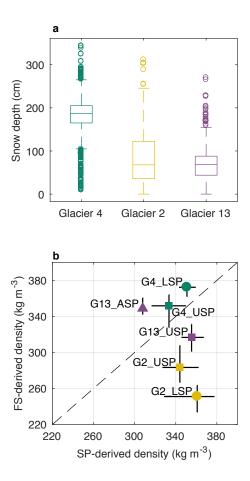


Fig. 2. Measured snow depth and density. (a) Boxplot of measured snow depth on Glaciers 4, 2 and 13 with the first quartiles (box), median (line within box), minimum and maximum values excluding outliers (bar) and outliers (circles), which are defined as being outside of the range of 1.5 times the quartiles (approximately  $\pm 2.7\sigma$ ). (b) Comparison of depth-averaged densities estimated using Federal Sampler (FS) measurements and a wedge cutter in a snow pit (SP) for Glacier 4 (G4), Glacier 2 (G2) and Glacier 13 (G13). Labels indicate SP locations in the accumulation area (ASP), upper ablation area (USP) and lower ablation area (LSP). Error bars for SP-derived densities are calculated by varying100 the thickness and density of layers that are too hard to sample, and error bars for FS-derived densities are the standard deviation of measurements taken at one location. One-to-one line is dashed.

#### RESULTS AND DISCUSSION

#### Field measurements

298 Snow depth

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Mean snow depth varied systematically across the study region, with Glacier 4 having the highest mean snow depth and Glacier 13 having the lowest (Fig. 2a). At each measurement location, the median range of measured depths (3–4 points) as a percent of the mean local depth is 2%, 11% and 12%, for Glaciers 4, 2 and 13, respectively. While Glacier 4 has the lowest point-scale variability, as assessed above, it also has

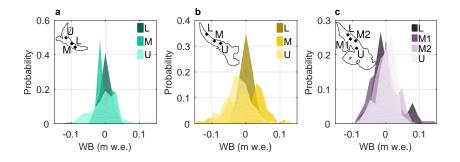


Fig. 3. Distributions of estimated winter-balance values for each zigzag survey in lower (L), middle (M) and upper (U) ablation areas (insets). Local mean has been subtracted. (a) Glacier 4. (b) Glacier 2. (c) Glacier 13.

the highest proportion of outliers, indicating a more variable snow depth across the glacier. The average standard deviation of all zigzag depth measurements is 0.07 m, 0.17 m and 0.14 m, for Glaciers 4, 2 and 13, respectively. When converted to values of WB using the local FS-derived density measurement, the average standard deviation is 0.027 m w.e., 0.035 m w.e. and 0.040 m w.e. WB data for each zigzag are not normally distributed (Fig. 3).

#### Snow density

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Contrary to expectation, co-located FS and SP measurements are found to be uncorrelated ( $R^2 = 0.25$ , 309 Fig. 2b). The FS appears to oversample in deep snow and undersample in shallow snow. Oversampling by 310 small-diameter sampling tubes has been observed in previous studies, with a percent error between 6.8% 311 and 11.8% (e.g. Work and others, 1965; Fames and others, 1982; Conger and McClung, 2009). Studies that 312 use FS often apply a 10% correction to all measurements for this reason (e.g. Molotch and others, 2005). 313 Oversampling has been attributed to slots "shaving" snow into the tube as it is rotated (e.g. Dixon and Boon, 314 2012) and to snow falling into the slots, particularly for snow samples with densities  $>400\,\mathrm{kg}\,\mathrm{m}^{-3}$  and snow 315 depths >1 m (e.g. Beaumont and Work, 1963). Undersampling is likely to occur due to loss of snow from the 316 bottom of the sampler (Turcan and Loijens, 1975). Loss by this mechanism may have occurred in our study, 317 given the isothermal and melt-affected snow conditions observed over the lower reaches of Glaciers 2 and 13. 318 Relatively poor FS spring-scale sensitivity also calls into question the reliability of measurements for snow 319 depths  $<20\,\mathrm{cm}$ . 320

Our FS-derived density values are positively correlated with snow depth ( $R^2 = 0.59$ ). This relationship could be a result of physical processes, such as compaction in deep snow and preferential formation of depth hoar in shallow snow, but is more likely a result of measurement artefacts for a number of reasons. First,

the total range of densities measured by the FS seems improbably large  $(227-431 \text{ kg m}^{-3})$ . At the time of 324 sampling the snow pack had little fresh snow, which confounds the low density values, and was not yet 325 saturated and had few ice lenses, which confounds the high density values. Moreover, the range of FS-326 derived values is much larger than than of SP-derived values when co-located measurements are compared. 327 Second, compaction effects of the magnitude required to explain the density differences between SP and 328 329 FS measurements would not be expected at the measured snow depths (up to 340 cm). Third, no linear relationship exists between depth and SP-derived density ( $R^2 = 0.05$ ). These findings suggest that the FS 330 measurements have a bias for which we have not identified a suitable correction. Despite this bias, we use 331 FS-derived densities to generate a range of possible WB estimates and to provide a generous estimate of 332 uncertainty arising from density assignment. 333

#### Density assignment

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Given the lack of correlation between co-located SP- and FS-derived densities (Fig. 2), we use the densities 335 derived from these two methods separately (Table 3). SP-derived regional (S1) and glacier-mean (S2) densities 336 are within one standard deviation of the corresponding FS-derived densities (F1 and F2) although SP-derived 337 density values are larger (see Supplementary Material, Table S2). For both SP- and FS-derived densities, the 338 mean density for any given glacier (S2 or F2) is within one standard deviation of the mean across all glaciers 339 (S1 or F1). Correlations between elevation and SP- and FS-derived densities are generally high ( $R^2 > 0.5$ ) but 340 vary between glaciers (Supplementary material, Table S2). For any given glacier, the standard deviation of the 341 3-4 SP- or FS-derived densities is <13\% of the mean of those values (S2 or F2) (Supplementary material, 342 Table S2). We adopt S2 (glacier-wide mean of SP-derived densities) as the reference method of density 343 assignment. Though the method described by S2 does not account for known basin-scale spatial variability 344 in snow density (e.g. Wetlaufer and others, 2016), it is commonly used in winter balance studies (e.g. Elder 345 and others, 1991; McGrath and others, 2015; Cullen and others, 2017). 346

#### Gridcell-averaged winter balance

The distributions of gridcell-averaged WB values for the individual glaciers are similar to those in Fig. 2a but with fewer outliers (see Supplementary Material). The standard deviations of WB values determined from the zigzag surveys are almost twice as large as the mean standard deviation of point-scale WB values within a gridcell measured along transects (see Supplementary Material). However, a small number of gridcells sampled in transect surveys have standard deviations in WB that exceed 0.25 m w.e. (~10 times greater than those for zigzag surveys).

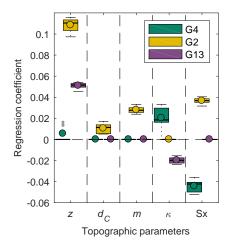


Fig. 4. Distribution of coefficients  $(\beta_i)$  determined by linear regression of gridcell-averaged WB on DEM-derived topographic parameters for the eight different density assignment methods (Table 3). Coefficients are calculated using standardized data, so values can be compared across parameters. Regression coefficients that are not significant are assigned a value of zero. Topographic parameters include elevation (z), distance from centreline  $(d_C)$ , slope (m), curvature  $(\kappa)$  and wind redistribution (Sx). Aspect  $(\alpha)$  and "northness" (N) are not shown because coefficient values are zero in every case. The box plot shows first quartiles (box), median (line within box), mean (circle within box), minimum and maximum values excluding outliers (bars) and outliers (gray dots), which are defined as being outside of the range of 1.5 times the quartiles (approximately  $\pm 2.7\sigma$ ).

#### 354 Distributed winter balance

355 Linear Regression

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Of the topographic parameters in the LR, elevation (z) is the most significant predictor of gridcell-averaged

WB for Glaciers 2 and 13, while wind redistribution (Sx) is the most significant predictor for Glacier 4

Table 4. Glacier-wide winter balance (WB, m w.e.) estimated using linear regression and simple kriging for the three study glaciers. Root mean squared error (RMSE, m w.e.) is computed as the average of all RMSE values between gridcell-averaged values of WB (the data) that were randomly selected and excluded from interpolation (1/3 of all data) and those estimated by interpolation. RMSE as a percent of the glacier-wide WB is shown in brackets.

	Linea	r regression	Simple kriging			
	WB	RMSE	WB	RMSE		
<b>G4</b>	0.58	0.15 (26%)	0.62	0.13 (21%)		
G2	0.58	0.10~(17%)	0.37	0.07~(19%)		
G13	0.38	0.08~(21%)	0.27	0.07~(26%)		

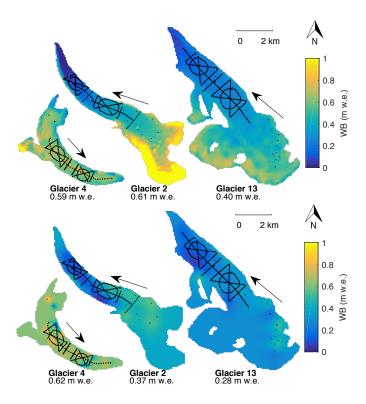
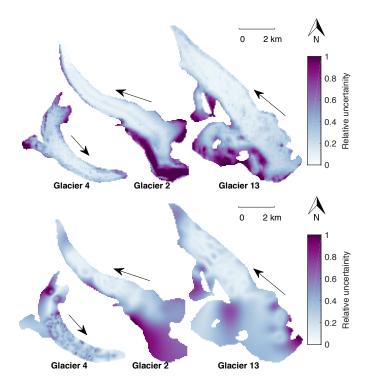


Fig. 5. Spatial distribution of winter balance (WB) estimated using linear regression (top row) and simple kriging (bottom row) with densities assigned as per S2 (Table 3). The linear regression method involves multiplying regression coefficients, found using cross validation and model averaging, by topographic parameters for each gridcell. Simple kriging uses the covariance of measured values to find a set of optimal weights for estimating values at unmeasured locations. Locations of snow-depth measurements taken in May 2016 are shown as black dots. Ice-flow directions are indicated by arrows. Values of glacier-wide WB are given below labels.

(Fig. 4). As expected, gridcell-averaged WB is positively correlated with elevation where the correlation 358 is significant. It is possible that the elevation correlation was accentuated due to melt onset for Glacier 359 13 in particular. Our results are consistent with many studies that have found elevation to be the most 360 significant predictor of winter-balance data (e.g. Machguth and others, 2006; McGrath and others, 2015). 361 The WB-elevation gradient is  $13 \,\mathrm{mm}/100 \,\mathrm{m}$  on Glacier 2 and  $7 \,\mathrm{mm}/100 \,\mathrm{m}$  on Glacier 13. These gradients 362 are consistent with those reported for a few glaciers in Svalbard (Winther and others, 1998) but considerably 363 smaller than many reported WB-elevation gradients, which range from about 60-240 mm/100 m (e.g. Hagen 364 and Liestøl, 1990; Tveit and Killingtveit, 1994; Winther and others, 1998). Extrapolating linear relationships 365 to unmeasured locations typically results in large uncertainties, as seen by the large WB values (Fig. 5) and 366 large relative uncertainty (Fig. 6) in the high-elevation regions of the accumulation areas of Glaciers 2 and 367 13. The low of correlation between WB and elevation Glacier 4 is consistent with Grabiec and others (2011) 368



**Fig. 6.** Relative uncertainty in distributed winter balance (WB) (Fig. 5) found using linear regression (top row) and simple kriging (bottom row). Values closer to one indicate higher relative uncertainty. Ice-flow directions are indicated by arrows.

and López-Moreno and others (2011), who conclude that highly variable distributions of snow are attributed to complex interactions between topography and the atmosphere that could not be easily quantified.

Gridcell-averaged WB is negatively correlated with Sx on Glacier 4, counter-intuitively indicating less snow in what would be interpreted as sheltered areas. Gridcell-averaged WB is positively correlated with Sx on Glaciers 2 and 13. Similarly, gridcell-averaged WB is positively correlated with curvature on Glacier 4 and negatively correlated on Glaciers 2 and 13. Our results corroborate those of McGrath and others (2015) in a study of six glaciers in Alaska (DEM resolutions of 5 m) where elevation and Sx were the only significant parameters for all glaciers; Sx regression coefficients were smaller than elevation regression coefficients, and in some cases, negative. While our results point to wind having an impact on snow distribution, the wind redistribution parameter (Sx) may not adequately capture these effects at our study sites. For example, Glacier 4 is located in a curved valley with steep side walls, so specifying a single cardinal direction for wind may not be adequate. Further, the scale of deposition may be smaller than the resolution of the Sx parameter estimated from the DEM. Creation of a parametrization for sublimation from blowing snow, which has been

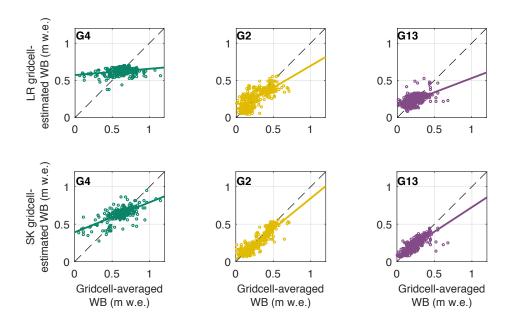


Fig. 7. Winter balance (WB) estimated by linear regression (LR, top row) or simple kriging (SK, bottom row) versus the grid-cell averaged WB data for Glacier 4 (left), Glacier 2 (middle) and Glacier 13 (right). Each circle represents a single gridcell. Best-fit (solid) and one-to-one (dashed) lines are shown.

shown to be an important mechanism of mass loss from ridges (e.g. Musselman and others, 2015), may also improve explanatory power of LR for our study sites.

We find that transfer of LR coefficients between glaciers results in large estimation errors. Regression coefficients from Glacier 4 produce the highest root mean squared error (0.38 m w.e. on Glacier 2 and 0.40 m w.e. on Glacier 13, see Table 4 for comparison) and glacier-wide WB values are the same for all glaciers (0.64 m w.e.) due to the dominance of the regression intercept. Even if the LR is performed with WB values from all glaciers combined, the resulting coefficients produce large root mean squared errors when applied to individual glaciers (0.31 m w.e., 0.15 m w.e. and 0.14 m w.e. for Glaciers 4, 2 and 13, respectively). Our results are consistent with those of Grünewald and others (2013), who found that local statistical models cannot be transferred across basins and that regional-scale models are not able to explain the majority of observed variance in winter balance.

## Simple kriging

Fitted kriging parameters, including the nugget and spatial correlation length, can provide insight into important scales of winter-balance variability. The model fitted to the gridcell-averaged values of WB for Glacier 4 has a short correlation length (90 m) and large nugget (see Supplementary Material Table S3), suggesting variability in winter balance at smaller scales. Conversely, Glaciers 2 and 13 have longer correlation

lengths (~450 m) and smaller nuggets, suggesting variability at larger scales. Additionally, SK is better able to estimate values of WB for Glaciers 2 and 13 than for Glacier 4 (Fig. 7). Due to a paucity of data, SK produces almost uniform gridcell-estimated values of winter balance in the accumulation area of each glacier, inconsistent with observations described in the literature (e.g. Machguth and others, 2006; Grabiec and others, 2011). As expected, extrapolation using SK leads to large uncertainty (Fig. 6), further emphasizing the need for spatially distributed point-scale measurements.

### 404 LR and SK comparison

Glacier-wide WB estimates found using both LR and SK are  $\sim 0.58 \,\mathrm{m}\,\mathrm{w.e.}$  for Glacier 4 but both are poor 405 predictors of WB in measured gridcells (Table 4). For Glaciers 2 and 13, SK estimates are more than 0.1 m w.e. 406 (up to 40%) lower than LR estimates (Table 4). RMSE as a percentage of the glacier-wide WB are comparable 407 between LR and SK (Table 4) with an average RMSE of 22%. This comparability is interesting, given that 408 all of the data were used to generate the SK model, while only 2/3 were used in the LR (consistent with 409 the best SK model estimated with 2/3 of the data). Gridcell-estimated values of WB found using LR and 410 SK differ markedly in the upper accumulation areas of Glaciers 2 and 13 (Fig. 5), where observations are 411 sparse and topographic parameters, such as elevation, vary considerably. The influence of elevation results in 412 substantially higher LR-estimated values of WB at high elevation, whereas SK-estimated values approximate 413 the nearest data. Estimates of ablation-area-wide WB differ by <7% between LR and SK on each glacier, 414 further emphasizing the combined role of interpolation method and measurement scarcity in the accumulation 415 area on glacier-wide WB estimates. 416

#### 417 Uncertainty analysis

Glacier-wide winter balance is affected by uncertainty introduced by the representativeness of gridcell-418 averaged values of WB ( $\sigma_{GS}$ ), choosing a method of density assignment ( $\sigma_{\rho}$ ), and interpolating/extrapolating 419 WB values across the domain  $(\sigma_{\text{INT}})$ . Using a Monte Carlo analysis, we find that interpolation uncertainty 420 contributes more to WB uncertainty than grid-scale uncertainty or density assignment method. In other 421 words, the distribution of glacier-wide WB that arises from grid-scale uncertainty and the differences in 422 distributions between methods of density assignment are smaller than the distribution that arises from 423 interpolation uncertainty (Fig. 8 and Table 5). The WB distributions obtained using LR and SK overlap 424 for a given glacier, but the distribution modes differ (Fig. 8). For reasons outlined above, SK-estimated 425 values of WB in the accumulation area are generally lower, which lowers the glacier-wide WB estimate. The 426 uncertainty in SK-estimated values of WB is large, and unrealistic glacier-wide values of WB of 0 m w.e. can 427

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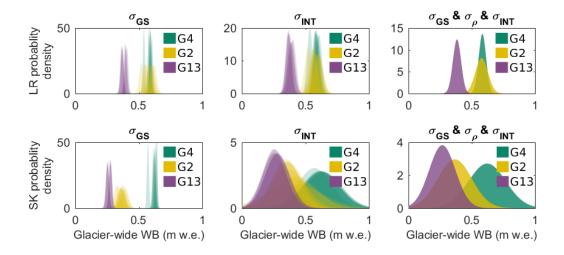


Fig. 8. Distributions of glacier-wide winter balance (WB) for Glaciers 4 (G4), 2 (G2) and 13 (G13) that arise from various sources of uncertainty. WB distribution arising from grid-scale uncertainty ( $\sigma_{GS}$ ) (left column). WB distribution arising from interpolation uncertainty ( $\sigma_{INT}$ ) (middle column). WB distribution arising from a combination of  $\sigma_{GS}$ ,  $\sigma_{INT}$  and density assignment uncertainty ( $\sigma_{\rho}$ ) (right column). Results are shown for interpolation by linear regression (LR, top row) and simple kriging (SK, bottom row). Left two columns include eight distributions per glacier (colour) and each corresponds to a density assignment method (S1–S4 and F1–F4).

be estimated (Fig. 8). Our results caution strongly against including interpolated/extrapolated values of WB in comparisons with remote sensing- or model-derived estimates of WB. If possible, such comparisons should be restricted to point-scale data.

Grid-scale uncertainty ( $\sigma_{GS}$ ) is the smallest assessed contributor to overall WB uncertainty. This result is consistent with the generally smoothly-varying snow depths encountered in zigzag surveys, and previously reported ice-roughness lengths on the order of centimetres (e.g. Hock, 2005) compared to snow depths on the

**Table 5.** Standard deviation (×10<sup>-2</sup> m w.e.) of glacier-wide winter balance (WB) distributions arising from uncertainties in grid-scale WB ( $\sigma_{GS}$ ), density assignment ( $\sigma_{\rho}$ ), interpolation ( $\sigma_{INT}$ ) and all three sources combined ( $\sigma_{ALL}$ ) for linear regression (left columns) and simple kriging (right columns)

	Linear regression				Simple kriging			
	$\sigma_{ m GS}$	$\sigma_{ ho}$	$\sigma_{INT}$	$\sigma_{ALL}$	$\sigma_{ m GS}$	$\sigma_{ ho}$	$\sigma_{INT}$	$\sigma_{ALL}$
Glacier 4	0.86	1.90	2.13	2.90	0.85	2.15	14.05	14.72
Glacier 2	1.80	3.37	3.09	4.90	2.53	2.03	13.78	13.44
Glacier 13	1.12	1.68	2.80	3.20	1.15	1.27	9.65	10.43

- order of decimetres to metres. Given our assumption that zigzags are an adequate representation of grid-scale
- variability, the low WB uncertainty arising from  $\sigma_{\rm GS}$  implies that subgrid-scale sampling need not be a high
- 436 priority for reducing overall uncertainty. Our assumption that the 3-4 zigzag surveys can be used to estimate
- 437 glacier-wide  $\sigma_{GS}$  may be flawed, particularly in areas with debris cover, crevasses and steep slopes.
- 438 Our analysis did not include uncertainty arising from density measurement errors associated with the FS,
- 439 wedge cutters and spring scales, from vertical and horizontal errors in the DEM or from error associated with
- estimating measurement locations based on the GPS position of the lead observer. We assume that these
- 441 sources of uncertainty are either encompassed by the sources investigated or negligible.
- The values of glacier-wide WB for our study glaciers (using LR and S2 density assignment method), with
- an uncertainty equal to one standard deviation of the distribution found with Monte Carlo analysis, are:
- $0.59 \pm 0.03$  m w.e. for Glacier 4,  $0.61 \pm 0.05$  m w.e. for Glacier 2 and  $0.40 \pm 0.03$  m w.e. for Glacier 13. The
- glacier-wide WB uncertainty from the three investigated sources of uncertainty ranges from 0.03 m w.e (5%)
- 446 to  $0.05\,\mathrm{m}$  w.e (8%) for LR estimates and from  $0.10\,\mathrm{m}$  w.e (37%) to  $0.15\,\mathrm{m}$  w.e (24%) for simple-kriging
- 447 estimates (Table 4).

#### 448 Context and caveats

- 449 Regional winter-balance gradient
- 450 Although we find considerable inter- and intra-basin variability in winter balance, our results are consistent
- 451 with a regional-scale winter-balance gradient for the continental side of the St. Elias Mountains (Fig. 9).
- 452 Winter-balance data are compiled from Taylor-Barge (1969), the three glaciers presented in this paper and
- 453 two snow pits we analyzed near the head of the Kaskawulsh Glacier between 20–21 May 2016. The data
- show a linear decrease of  $0.024\,\mathrm{m\,w.e.~km^{-1}}$  ( $\mathrm{R}^2=0.85$ ) in winter balance with distance from the regional
- 455 topographic divide between the Kaskawulsh and Hubbard Glaciers, as identified by Taylor-Barge (1969).
- 456 While the three study glaciers fit the regional trend, the same relationship would not apply if just the Donjek
- Range were considered. We hypothesize that interaction between meso-scale weather patterns and large-scale
- 458 mountain topography is a major driver of regional-scale winter balance. Further insight into regional-scale
- 459 patterns of winter balance in the St. Elias Mountains could be gained by investigating moisture source
- 460 trajectories and the contribution of orographic precipitation.
- 461 Limitations and future work
- 462 The potential limitations of our work include the restriction of our data to a single year, minimal sampling
- in the accumulation area, the problem of uncorrelated SP- and FS-derived densities, a sampling design that

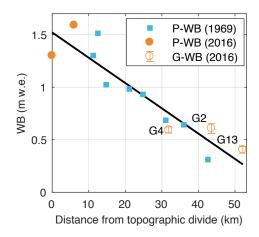


Fig. 9. Relationship between winter balance (WB) and linear distance from the regional topographic divide between the Kaskawulsh and Hubbard Glaciers in the St. Elias Mountains. Point-scale values of WB from snow-pit data reported by Taylor-Barge (1969) (blue boxes, P-WB). LR-estimated glacier-wide WB calculated using density assignment S2 for Glaciers 4 (G4), 2 (G2) and 13 (G13) with errors bars calculated as the standard deviation of Monte Carlo-derived WB distributions (this study) (open orange circles, G-WB). Point-scale WB estimated from snow-pit data at two locations in the accumulation area of the Kaskawulsh Glacier, collected in May 2016 (unpublished data, SFU Glaciology Group) (filled orange dots, P-WB). Black line indicates best fit ( $\mathbb{R}^2 = 0.85$ ).

could not be optimized a priori, the assumption of spatially uniform subgrid variability and lack of more finely resolved DEMs.

Inter-annual variability in winter balance is not considered in our study. A number of studies have found temporal stability in spatial patterns of snow distribution and that statistical models based on topographic parameters could be applied reliably between years (e.g. Grünewald and others, 2013). For example, Walmsley (2015) analyzed more than 40 years of winter balance recorded on two Norwegian glaciers and found that snow distribution is spatially heterogeneous yet exhibits robust temporal stability. Contrary to this, Crochet and others (2007) found that snow distribution in Iceland differed considerably between years and depended primarily on the dominant wind direction over the course of a winter. Therefore, multiple years of snow depth and density measurements, that are not necessarily consecutive, are needed to better understand inter-annual variability in winter-balance distribution within the Donjek Range.

There is a conspicuous lack of data in the accumulation areas of our study glaciers. With increased sampling in the accumulation area, interpolation uncertainties would be reduced where they are currently greatest and the LR would be better constrained. Although certain regions of the glaciers remain inaccessible for direct measurements, other methods of obtaining winter-balance, including ground-penetrating radar and DEM

differencing with photogrammetry or lidar, could be used in conjunction with manual probing to increase the spatial coverage of measurements.

The lack of correlation between SP- and FS-derived densities needs to be reconciled. Contrary to our results, most studies that compare SP- and FS-derived densities report minimal discrepancy (e.g. Dixon and Boon, 2012, and sources within). Additional co-located density measurements are needed to better compare the two methods of obtaining density values. Comparison with other FS would also be informative. Even with this limitation, density assignment was, fortunately, not the largest source of uncertainty in estimating glacier-wide winter balance.

Our sampling design was chosen to achieve broad spatial coverage of the ablation area, but is likely too finely resolved along transects for many mass-balance surveys to replicate. An optimal sampling design would minimize uncertainty in winter balance while reducing the number of required measurements. Analysis of the estimated winter balance obtained using subsets of the data is underway to make recommendations on optimal transect configuration and along-track spacing of measurements. López-Moreno and others (2010) found that 200–400 observations are needed within a non-glacierized alpine basin (6 km<sup>2</sup>) to obtain accurate and robust snow distribution models. Similar guidelines would be useful for glacierized environments.

In this study, we assume that the subgrid variability of winter balance is uniform across a given glacier.

Contrary to this assumption, McGrath and others (2015) found greater variability of winter-balance values

close to the terminus. Testing our assumption could be a simple matter of prioritizing the labour-intensive

zigzags surveys. To ensure consistent quantification of subgrid variability, zigzag survey measurements could

also be tested against other measurements methods, such as lidar.

DEM gridcell size is known to influence values of computed topographic parameters (Zhang and 499 Montgomery, 1994; Garbrecht and Martz, 1994; Guo-an and others, 2001; López-Moreno and others, 2010). 500 The relationship between topographic parameters and winter balance is, therefore, not independent of DEM 501 502 gridcell size. For example, Kienzle (2004) and López-Moreno and others (2010) found that a decrease in spatial resolution of the DEM results in a decrease in the importance of curvature and an increase in the 503 importance of elevation in LR of snow distribution on topographic parameters in non-glacierized basins. 504 The importance of curvature in our study is affected by the DEM smoothing that we applied to obtain a 505 spatially continuous curvature field (see Supplementary Material). A comparison of regression coefficients 506 from high-resolution DEMs obtained from various sources and sampled with various gridcell sizes could be 507

used to characterize the dependence of topographic parameters on DEMs, and therefore assess the robustness of inferred relationships between winter balance and topographic parameters.

We estimate winter balance for three glaciers (termed Glacier 2, Glacier 4 and Glacier 13) in the St. Elias

#### 510 CONCLUSION

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Mountains, Yukon, Canada from multiscale snow depth and density measurements. Linear regression and 512 simple kriging are used to obtain estimates of distributed winter balance. We use Monte Carlo analysis to 513 evaluate the contributions of interpolation, the assignment of snow density and grid-scale variability of winter 514 balance to uncertainty in glacier-wide winter balance. 515 Values of glacier-wide winter balance estimated using linear regression and simple kriging differ by up 516 to  $0.24 \,\mathrm{m}$  w.e. ( $\sim 50\%$ ). We find that interpolation uncertainty is the largest assessed source of uncertainty 517 in glacier-wide winter balance (5\% for linear-regression estimates and 32\% for simple-kriging estimates). 518 519 Uncertainty resulting from the method of density assignment is comparatively low, despite the wide range of methods explored. Given our representation of grid-scale variability, the resulting winter balance uncertainty 520 is small indicating that extensive subgrid-scale sampling is not required to reduce overall uncertainty. 521 Our results suggest that processes governing distributed winter balance differ between glaciers, highlighting 522 the importance of regional-scale winter-balance studies. The estimated distribution of winter balance on 523 Glacier 4 is characterized by high variability, as indicated by the poor correlation between estimated and 524 observed values and large number of data outliers. Glaciers 2 and 13 appear to have lower spatial variability, 525 with elevation being the dominant predictor of gridcell-averaged winter balance. A wind-redistribution 526 parameter is found to be a weak but significant predictor of winter balance, though conflicting relationships 527 between glaciers make it difficult to interpret. The major limitations of our work include the restriction 528 of our data to a single year and minimal sampling in the accumulation area. Although challenges persist 529 when estimating winter balance, our data are consistent with a regional-scale winter-balance gradient for the 530

#### AUTHOR CONTRIBUTION STATEMENT

continental side of the St. Elias Mountains.

AP planned and executed the data collection, performed all calculations and drafted the manuscript. GF conceived of the study, contributed to field planning and data collection, oversaw all stages of the work and edited the manuscript. VR provided guidance with statistical methods and edited the manuscript.

#### 536 ACKNOWLEDGEMENTS

- 537 We thank the Kluane First Nation (KFN), Parks Canada and the Yukon Territorial Government for granting
- 538 us permission to work in KFN Traditional Territory and Kluane National Park and Reserve. We are
- 539 grateful for financial support provided by the Natural Sciences and Engineering Research Council of Canada,
- 540 Simon Fraser University and the Northern Scientific Training Program. We kindly acknowledge Kluane Lake
- 541 Research Station, Sian Williams, Lance Goodwin and Trans North pilot Dion Parker for facilitating field
- 542 logistics. We are grateful to Alison Criscitiello and Coline Ariagno for all aspects of field assistance and Sarah
- 543 Furney for assistance with data entry. Thank you to Etienne Berthier for providing us with the SPIRIT SPOT-
- 544 5 DEM and for assistance in DEM correction. We are grateful to Derek Bingham and Michael Grosskopf for
- 545 assistance with the statistics, including simple kriging. Luke Wonneck, Leif Anderson and Jeff Crompton all
- 546 provided thoughtful and constructive comments on drafts of the manuscript.

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