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# Estimating winter balance and its uncertainty from direct

# measurements of snow depth and density on alpine glaciers

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ABSTRACT. Accurately estimating winter surface mass balance on glaciers is central to assessing glacier health and predicting glacier runoff. However, measuring and modelling snow distribution is inherently difficult in mountainous terrain. Here we explore rigorous statistical methods of estimating winter balance and its uncertainty from multiscale measurements of snow depth and density. In May 2016 we collected over 9000 manual measurements of snow depth across three glaciers in the St. Elias Mountains, Yukon, Canada. Linear regression, combined with cross correlation and Bayesian model averaging, as well as simple kriging are used to interpolate point-scale values to glacier-wide estimates of winter balance. Elevation and a wind-redistribution parameter exhibit the highest correlations with winter balance, but the relationship varies considerably between glaciers. A Monte Carlo analysis reveals that the interpolation itself introduces more uncertainty than the assignment of snow density or the representation of grid-scale variability. For our study glaciers, the winter balance uncertainty from all assessed sources ranges from  $0.03 \,\mathrm{m}$  w.e. (8%) to  $0.15 \,\mathrm{m}$  w.e. (54%). Despite the challenges associated with estimating winter balance, our results are consistent with a regional-scale winter-balance gradient.

## 26 INTRODUCTION

Winter surface mass balance, or "winter balance", is the net accumulation and ablation of snow over the 27 winter season (Cogley and others, 2011), which constitutes glacier mass input. Winter balance is half of the 28 seasonally resolved mass balance, initializes summer ablation conditions and must be estimated to simulate 29 energy and mass exchange between the land and atmosphere (e.g. Hock, 2005; Réveillet and others, 2016). 30 Effectively representing the spatial distribution of snow is also central to monitoring surface runoff and its 31 downstream effects (e.g. Clark and others, 2011). 32 Winter balance (WB) is notoriously difficult to estimate (e.g. Dadić and others, 2010; Cogley and others, 33 2011). Snow distribution in alpine regions is highly variable with short correlation length scales (e.g. Anderton 34 and others, 2004; Egli and others, 2011; Grünewald and others, 2010; Helbig and van Herwijnen, 2017; López-35 Moreno and others, 2011, 2013; Machguth and others, 2006; Marshall and others, 2006) and is influenced by 36 dynamic interactions between the atmosphere and complex topography, operating on multiple spatial and 37 temporal scales (e.g. Barry, 1992; Liston and Elder, 2006; Clark and others, 2011). Simultaneously extensive, 38 high resolution and accurate snow distribution measurements on glaciers are therefore difficult to obtain 39 (e.g. Cogley and others, 2011; McGrath and others, 2015) and is further complicated by the inaccessibility 40 of many glacierized regions during the winter. Physically based models are computationally intensive and 41 require detailed meteorological data to drive them (Dadić and others, 2010). As a result, there is significant 42 uncertainty in estimates of winter balance, thus limiting the ability of models to represent current and 43 projected glacier conditions. 44 Studies that have focused on obtaining detailed estimates of WB have used a wide range of observational 45 techniques, including direct measurement of snow depth and density (e.g. Cullen and others, 2017), lidar 46 or photogrammerty (e.g. Sold and others, 2013) and ground-penetrating radar (e.g. Machguth and others, 47 2006; Gusmeroli and others, 2014; McGrath and others, 2015). Spatial coverage of direct measurements is generally limited and comprises an elevation transect along the glacier centreline (e.g. Kaser and others, 49 2003). Measurements are often interpolated using linear regression on only a few topographic parameters (e.g. 50 MacDougall and Flowers, 2011), with elevation being the most common. Other established techniques include hand contouring (e.g. Tangborn and others, 1975), kriging (e.g. Hock and Jensen, 1999) and attributing 52 measured winter balance values to elevation bands (e.g. Thibert and others, 2008). Physical snow models 53 have been used to estimate spatial patterns of winter balance (e.g. Mott and others, 2008; Schuler and others, 2008; Dadić and others, 2010) but availability of the required meteorological data generally prohibits their 55

widespread application. Error analysis is rarely undertaken and few studies have thoroughly investigated uncertainty in spatially distributed estimates of winter balance (c.f. Schuler and others, 2008).

More sophisticated snow-survey designs and statistical models of snow distribution are widely used in the 58 field of snow science. Surveys described in the snow science literature are generally spatially extensive and 59 designed to measure snow depth and density throughout a basin, ensuring that all terrain types are sampled. 60 61 A wide array of measurement interpolation methods are used, including linear (e.g. López-Moreno and others, 2010) and non-linear regressions (e.g. Molotch and others, 2005) that include numerous terrain parameters, as well as geospatial interpolation (e.g. Erxleben and others, 2002; Cullen and others, 2017) including various 63 forms of kriging. Different interpolation methods are also combined; for example, regression kriging adds 64 kriged residuals to a field obtained with linear regression (e.g. Balk and Elder, 2000). Physical snow models such as SnowTran-3D (Liston and Sturm, 1998), Alpine3D (Lehning and others, 2006), and SnowDrift3D 66 (Schneiderbauer and Prokop, 2011) are widely used, and errors in estimating snow distribution have been 67 examined from theoretical (e.g. Trujillo and Lehning, 2015) and applied perspectives (e.g. Turcan and Loijens, 68 1975; Woo and Marsh, 1978; Deems and Painter, 2006). 69 70 The goals of this study are to (1) critically examine methods of converting direct snow depth and density

The goals of this study are to (1) critically examine methods of converting direct snow depth and density
measurements to distributed estimates of winter balance and (2) identify sources of uncertainty, evaluate
their magnitude and assess their combined contribution to uncertainty in glacier-wide winter balance. We
focus on commonly applied, low-complexity methods of measuring and estimating winter balance in the
interest of making our results broadly applicable.

#### 75 STUDY SITE

The St. Elias Mountains (Fig. 1a) rise sharply from the Pacific Ocean, creating a significant climatic gradient 76 between coastal maritime conditions, generated by Aleutian-Gulf of Alaska low-pressure systems, and interior 77 continental conditions, driven by the Yukon-Mackenzie high-pressure system (Taylor-Barge, 1969). The 78 boundary between the two climatic zones is generally aligned with the divide between the Hubbard and 79 Kaskawulsh Glaciers, approximately 130 km from the coast. Research on snow distribution and glacier mass 80 balance in this area is limited. A series of research programs, including Project "Snow Cornice" and the Icefield Ranges Research Project, were operational in the 1950s and 60s (Wood, 1948; Danby and others, 82 2003) and in the last 30 years, there have been a few long-term studies on selected alpine glaciers (e.g. Clarke, 83 2014) as well as several regional studies of glacier mass balance and dynamics (e.g. Arendt and others, 2008; Burgess and others, 2013; Waechter and others, 2015). 85

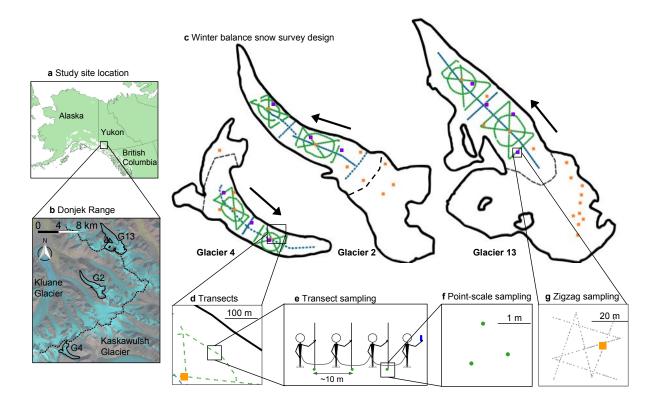


Fig. 1. Study area location and sampling design for Glaciers 4, 2 and 13. (a) Study region in the Donjek Range of the St. Elias Mountains of Yukon, Canada. (b) Study glaciers located along a southwest-northeast transect through the Donjek Range. The local topographic divide is shown as a dashed line. Imagery from Landsat8 (5 September 2013, data available from the U.S. Geological Survey). (c) Details of the snow-survey sampling design, with centreline and transverse transects (blue dots), hourglass and circle designs (green dots) and locations of snow density measurements (orange squares). Arrows indicate ice-flow directions. Approximate location of ELA on each glacier is shown as a black dashed line. (d) Close up of linear and curvilinear transects. (e) Configuration of navigator and observers. (f) Point-scale snow-depth sampling. (g) Linear-random snow-depth measurements in 'zigzag' design (purple dots) with one density measurement (orange square) per zigzag.

We carried out winter balance surveys on three unnamed glaciers in the Donjek Range of the St. Elias Mountains. The Donjek Range is located approximately 40 km to the east of the regional mountain divide and has an area of about 30 × 30 km<sup>2</sup>. Glacier 4, Glacier 2 and Glacier 13 (labelling adopted from Crompton and Flowers (2016)) are located along a southwest-northeast transect through the range (Fig. 1b, Table 1). These small alpine glaciers are generally oriented southeast-northwest, with Glacier 4 having a predominantly southeast aspect and Glaciers 2 and 13 have generally northwest aspects. The glaciers are situated in valleys with steep walls and have simple geometries. Based on a detailed study of Glacier 2 (Wilson and others,

**Table 1.** Physical characteristics of the study glaciers.

	Location		Ele	evation (m a	Slope ( $^{\circ}$ )	Area	
	UTM Zone 7		Mean	Range	ELA	Mean	$(km^2)$
Glacier 4	595470 E	6740730 N	2344	1958-2809	$\sim 2500$	12.8	3.8
Glacier 2	601160 E	6753785  N	2495	1899-3103	$\sim 2500$	13.0	7.0
Glacier 13	604602 E	6763400 N	2428	1923-3067	~2380	13.4	12.6

2013) and related theoretical modelling (Wilson and Flowers, 2013) we suspect all of the study glaciers to be polythermal.

## 95 METHODS

Estimating glacier-wide winter balance involves transforming measurements of snow depth and density into values of winter balance distributed across a defined grid. We do this in four steps. (1) Obtain direct 97 measurements of snow depth and density in the field. (2) Assign density values to all depth-measurement 98 locations to calculate point-scale values of WB at each location. Winter balance can be estimated as the 99 product of snow depth and depth-averaged density. (3) Average all point-scale values within each gridcell of 100 a digital elevation model (DEM) to obtain the gricell-averaged WB. (4) Interpolate and extrapolate these 101 gridcell-averaged WB values to obtain estimates of WB (in m w.e.) in each gridcell across the domain. Glacier-102 103 wide WB is then calculated by taking the average of all gridcell-averaged WB values for each glacier. For brevity, we refer to these four steps as (1) field measurements, (2) density assignment, (3) gridcell-averaged 104

Table 2. Details of the May 2016 winter-balance survey, including number of snow-depth measurement locations along transects  $(n_{\rm T})$ , total length of transects  $(d_{\rm T})$ , number of combined snow pit and Federal Sampler density measurement locations  $(n_{\rho})$ , number of zigzag surveys  $(n_{\rm zz})$ , number (and as percent of total number of gridcells) of gridcells sampled  $(n_{\rm S})$  and the elevation range (and as percent of total elevations range).

	Date	$n_{ m T}$	$d_{\mathrm{T}}$ (km)	$n_{ ho}$	$n_{zz}$	$n_{ m S}$	Elevation range (ma.s.l.)
Glacier 4	4–7 May 2016	649	13.1	7	3	295	2015–2539
						(12%, 21%)	(62%,97%)
Glacier 2	8–11 May 2016	762	13.6	7	3	353	2151-2541
						(8%, 14%)	(32%,47%)
Glacier 13	12–15 May 2016	941	18.1	19	4	468	2054–2574
						(6%, 14%)	(45%,62%)

WB and (4) distributed WB. Detailed methodology for each step is outlined below. We use the SPIRIT SPOT-5 DEM (40×40 m) from 2005 (Korona and others, 2009) throughout this study.

#### 107 Field measurements

Our sampling campaign involved four people and occurred between 5–15 May 2016, which falls within the 108 period of historical peak snow accumulation in southwestern Yukon (Yukon Snow Survey Bulletin and Water 109 Supply Forecast, May 1, 2016). Snow depth is generally accepted to be more variable than density (Elder 110 and others, 1991; Clark and others, 2011; López-Moreno and others, 2013) so we chose a sampling design 111 that resulted in a high ratio ( $\sim$ 55:1) of snow depth to density measurements. In total, we collected more 112 than 9000 snow-depth measurements and more than 100 density measurements throughout the study area 113 (Table 1). 114 During the field campaign there were two small accumulation events. The first, on 6 May 2016, also involved 115 high winds so accumulation could not be determined. The second, on 10 May 2016, resulted in 0.01 m w.e 116 accumulation measured at one location on Glacier 2. Assuming both accumulation events contributed a 117 uniform 0.01 m w.e accumulation to all study glaciers then our survey did not capture  $\sim 3\%$  and  $\sim 2\%$  of 118 estimated glacier-wide winter balance on Glaciers 4 and 2, respectively. We therefore assume that these 119 accumulation events were negligible. Positive temperatures and clear skies occurred between 11–16 May 120 2016, which we suspect resulted in melt occurring on Glacier 13. The snow in the lower part of the ablation 121 area of Glacier 13 was isothermal and showed clear signs of melt and metamorphosis. The total amount of 122 melt during the study period was not estimated so no corrections were made. 123

# 124 Sampling design

The snow surveys were designed to capture variability in snow depth at regional, basin, gridcell and point 125 scales (Clark and others, 2011). To capture variability at the regional scale we chose three glaciers along 126 a transect aligned with the dominant precipitation gradient (Fig. 1) (Taylor-Barge, 1969). To account for 127 basin-scale variability, snow depth was measured along linear and curvilinear transects on each glacier (Fig. 128 1c) with a sample spacing of 10–60 m (Fig. 1d). Sample spacing was constrained by protocols for safe glacier 129 travel, while survey scope was constrained by the need to complete all surveys within the period of peak 130 accumulation. We selected centreline and transverse transects as the most commonly used survey designs 131 in winter balance studies (e.g. Kaser and others, 2003; Machguth and others, 2006) as well as an hourglass 132 pattern with an inscribed circle, which allows for sampling in multiple directions and easy travel (personal 133 communication from C. Parr, 2016). To capture variability at the grid scale, we densely sampled up to four 134

gridcells on each glacier using a linear-random sampling design (Shea and Jamieson, 2010) we term a 'zigzag'.

To capture point-scale variability, each observer made 3–4 depth measurements within  $\sim$ 1 m (Fig. 1f) at

138 Snow depth: transects

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each transect measurement location.

While roped-up for glacier travel with fixed distances between observers, the lead observer used a single-139 140 frequency GPS unit (Garmin GPSMAP 64s) to navigate between predefined transect measurement locations (Fig. 1e). The remaining three observers used 3.2 m graduated aluminum avalanche probes to make snow-141 depth measurements. The locations of each set of depth measurements, made by the second, third and fourth 142 observers, are estimated using the recorded location of the first observer, the approximate distance between 143 observers and the direction of travel. The 3-4 point-scale depth measurements are averaged to obtain a single 144 depth measurement at each transect measurement location. When considering snow variability at the point 145 scale as a source of uncertainty in snow depth measurements, we find that the mean standard deviation of 146 point-scale snow depth measurements is found to be <7% of the mean snow depth for all study glaciers. 147 Snow-depth sampling was concentrated in the ablation area to ensure that only snow from the current 148 accumulation season was measured. The boundary between snow and firm in the accumulation area can be 149 difficult to detect and often misinterpreted, especially when using an avalanche probe (Grünewald and others, 150 2010; Sold and others, 2013). We intended to use a firn corer to measure winter balance in the accumulation 151 area, but cold snow combined with positive air temperatures led to cores being unrecoverable. Successful 152 snow depth measurements within the accumulation area were made either in snow pits or using a Federal 153 Sampler (described below) to unambiguously identify the snow-firn transition. 154

155 Snow depth: zigzags

We measured depth at random intervals of  $0.3-3.0\,\mathrm{m}$  along two 'Z'-shaped patterns (Shea and Jamieson, 2010), resulting in 135–191 measurements per zigzag, within three to four  $40\times40\,\mathrm{m}$  gridcells (Fig. 1g) per glacier. Random intervals were machine-generated from a uniform distribution in sufficient numbers that each survey was unique. Zigzag locations were randomly chosen within the upper, middle and lower regions of the ablation area of each glacier. Extra time in the field allowed us to measure a fourth zigzag on Glacier 13 in the central ablation area at  $\sim\!2200\,\mathrm{m}$  a.s.l.

162 Snow density

Snow density was measured using a Snowmetrics wedge cutter in three snow pits on each glacier. Within 163 the snow pits (SP), we measured a vertical density profile (in 5 cm increments) with the  $5 \times 10 \times 10$  cm 164 wedge-shaped cutter (250 cm<sup>3</sup>) and a Presola 1000 g spring scale (e.g. Gray and Male, 1981; Fierz and others, 165 2009). Wedge-cutter error is approximately  $\pm 6\%$  (e.g. Proksch and others, 2016; Carroll, 1977). Uncertainty 166 in estimating density from SP measurements also stems from incorrect assignment of density to layers that 167 cannot be sampled (e.g. ice lenses and hard layers). We attempt to quantify this uncertainty by varying 168 estimated ice-layer thickness by  $\pm 1$  cm ( $\leq 100\%$ ) of the recorded thickness, ice layer density between 700 169 and 900 kg m<sup>-3</sup> and the density of layers identified as being too hard to sample (but not ice) between 600 170 and 700 kg m<sup>-3</sup>. When considering all three sources of uncertainty, the range of integrated density values 171 is always less than 15\% of the reference density. Depth-averaged densities for shallow pits (<50 cm) that 172 contain ice lenses are particularly sensitive to changes in prescribed density and ice-lens thickness. 173 While SP provide the most accurate measure of snow density, digging and sampling a SP is time and 174 labour intensive. Therefore, a Geo Scientific Ltd. metric Federal Sampler (FS) (Clyde, 1932) with a 3.2-175 176 3.8 cm diameter sampling tube, which directly measures depth-integrated snow-water equivalent, was used to augment the snow pit measurements. A minimum of three FS measurements were taken at each of 7–19 177 locations on each glacier and an additional eight FS measurements were co-located with each snow pit profile. 178 Measurements for which the snow core length inside the sampling tube was less than 90% of the snow depth 179 were discarded. Densities at each measurement location (eight at each snow pit, three elsewhere) were then 180 averaged, with the standard deviation taken to represent the uncertainty. The mean standard deviation of 181 FS-derived density was  $\leq 4\%$  of the mean density for all glaciers. 182

# 183 Density assignment

Measured snow density must be interpolated or extrapolated to estimate point-scale winter balance at each 184 snow-depth sampling location. We employ four commonly used methods to interpolate and extrapolate 185 density (Table 3): (1) calculate mean density over an entire mountain range (e.g. Cullen and others, 2017), 186 (2) calculate mean density for each glacier (e.g. Elder and others, 1991; McGrath and others, 2015), (3) 187 linear regression of density on elevation for each glacier (e.g. Elder and others, 1998; Molotch and others, 188 2005) and (4) calculate mean density using inverse-distance weighting (e.g. Molotch and others, 2005) for 189 each glacier. Densities derived from SP and FS measurements are treated separately, for reasons explained 190 below, resulting in eight possible methods of assigning density. 191

**Table 3.** Eight methods used to estimate snow density at unmeasured locations. Total number of resulting density values given in parentheses, with  $n_T$  the total number of snow-depth measurement locations along transects (Table 1).

Method	Source of	measured	Density assignment		
code	snow o	lensity	$_{ m method}$		
	Snow pit	Federal			
		Sampler			
S1	•		Mean of measurements		
F1			across all glaciers (1)		
S2			Mean of measurements		
F2			for each glacier (3)		
S3			Regression of density on		
F3		•	elevation for a glacier $(n_T)$		
S4			Inverse distance weighted		
F4			mean for a glacier $(n_T)$		

# Gridcell-averaged winter balance

We average one to six (mean of 2.1 measurements) point-scale values of WB within each  $40 \times 40 \,\mathrm{m}$  DEM 193 gridcell to obtain the gricell-averaged WB. The locations of individual measurements have uncertainty due to 194 the error in the horizontal position given by the GPS unit and the estimation of observer location based on the 195 recorded GPS positions of the navigator. This location uncertainty could result in the incorrect assignment of 196 a point-scale WB to a particular gridcell. However, this source of error is not further investigated because we 197 assume that the uncertainty in gridcell-averaged WB is captured in the zigzag measurements described below. 198 Error due to having multiple observers is also evaluated by conducting an analysis of variance (ANOVA) 199 of snow-depth measurement along a transect and testing for differences between observers. We find no 200 significant differences between snow-depth measurements made by observers along any transect (p>0.05), 201 with the exception of the first transect on Glacier 4 (51 measurements), where snow depth values collected by 202 one observer were, on average, greater than the snow depth measurements taken by the other two observers 203 (p<0.01). Since this was the first transect completed and the only one to show differences by observer, this 204 difference can be considered an anomaly. This result shows that observer bias is likely to not affect the results 205 of this study and no corrections to the data based on observer were applied. 206

# Distributed winter balance

- Gridcell-averaged values of WB are interpolated and extrapolated across each glacier using linear regression 208 209 (LR) and simple kriging (SK). The LR relates gridcell-averaged WB and various topographic parameters, as this method is simple and has precedent for success (e.g. McGrath and others, 2015). Instead of a basic LR 210 however, we use cross-validation and model averaging to test all combinations of the topographic parameters. 211 We compare the LR approach with SK, a data-driven interpolation method free of any physical interpretation 212 (e.g. Hock and Jensen, 1999).
- Linear regression 214

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- In the LR, we use commonly applied topographic parameters as in McGrath and others (2015), including 215 elevation, slope, aspect, curvature, "northness" and a wind-redistribution parameter (Sx from Winstral 216 and others (2002)); we add distance-from-centreline as an additional parameter. Topographic parameters are 217 standardized for use in the LR. For details on data and methods used to estimate the topographic parameters 218 see the Supplementary Material. Our sampling design ensured that the ranges of topographic parameters 219 associated with our measurement locations represent more than 70% of the total area of each glacier (except 220 elevation on Glacier 2, where our measurements captured only 50%). 221
- The goal of the LR is to obtain a set of fitted regression coefficients ( $\beta_i$ ) that correspond to each topographic 222 parameter and to a model intercept. The LR implemented in this study is an extension of a basic multiple 223 linear regression; we use cross-validation to avoid overfitting the data and model averaging to incorporate 224 every possible combination of topographic parameters. 225
- First, cross-validation is used to obtain a set of regression coefficients that have the greatest predictive 226 ability (Kohavi and others, 1995). We randomly select 1000 subsets of the data (2/3 of the values) and fit 227 a basic multiple linear regression (implemented in MATLAB) to the data subsets, thus obtaining 1000 sets 228 of regression coefficients. The basic multiple linear regression calculates a set of regression coefficients by 229 minimizing the sum of squares of the vertical deviations of each datum from the regression line (Davis and 230 Sampson, 1986). Distributed winter balance is then calculated by weighting each topographic parameter by 231 the corresponding regression coefficient for all DEM gridcells. We then use the remaining data (1/3) of the 232 values) to calculate a root mean squared error (RMSE) between the estimated WB and the observed WB for 233 corresponding locations. From the 1000 sets of  $\beta_i$  values, we select the set that results in the lowest RMSE. 234 Second, we use model averaging to account for uncertainty when selecting predictors and to maximize 235

the model's predictive ability (Madigan and Raftery, 1994). Models are generated by calculating a set of

regression coefficients as described above for all possible combinations of topographic parameters (resulting in 237 2<sup>7</sup> models, or sets of regression coefficients). Using a Bayesian framework, model averaging involves weighting 238 all models by their posterior model probabilities (Raftery and others, 1997). The models (i.e. sets of regression 239 coefficients) are weighted according to the relative predictive success of the model, as assessed by the value 240 of the Bayesian Information Criterion (BIC) (Burnham and Anderson, 2004). BIC penalizes more complex 241 242 models which further reduces the risk of overfitting. The final set of regression coefficients is then the weighted sum of regression coefficients from all models. Distributed WB is obtained by applying the final set of 243 regression coefficients to the topographic parameters associated with each gridcell. 244

245 Simple kriging

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SK is a data-driven method of estimating variables at unsampled locations by using the isotropic spatial 246 correlation (covariance) of measured values to find a set of optimal weights (Davis and Sampson, 1986; Li 247 and Heap, 2008). SK assumes spatial correlation between sampling locations that are distributed across a 248 surface and then applies the correlation to interpolate between these locations. We used the DiceKriging 249 R package (Roustant and others, 2012) to calculate the maximum likelihood covariance matrix, as well as 250 the range distance  $(\theta)$  and nugget for gridcell-averaged values of winter balance. The range distance is a 251 measure of data correlation length and the nugget is the residual that encompasses sampling-error variance 252 as well as the spatial variance at distances less than the minimum sample spacing (Li and Heap, 2008). A 253 Matére covariance function with  $\nu=5/2$  is used to define a stationary and isotropic covariance and covariance 254 kernels are parameterized as in Rasmussen and Williams (2006). Unlike LR, SK is not useful for generating 255 hypotheses to explain the physical controls on snow distribution, nor can it be used to estimate winter 256 balance on unmeasured glaciers. 257

# Uncertainty analysis using a Monte Carlo approach

Three sources of uncertainty are considered separately: the uncertainty due to (1) grid-scale variability of 259 WB ( $\sigma_{GS}$ ), (2) the assignment of snow density ( $\sigma_{\rho}$ ) and (3) interpolating and extrapolating gridcell-averaged 260 values of WB ( $\sigma_{\text{INT}}$ ). To quantify the uncertainty of grid-scale and interpolation uncertainty on estimates of 261 glacier-wide WB we conduct a Monte Carlo analysis, which uses repeated random sampling of input variables 262 to calculate a distribution of output variables (Metropolis and Ulam, 1949). We repeat the random sampling 263 process 1000 times, resulting in a distribution of values of the glacier-wide WB based on uncertainties 264 associated with the four steps outlined above. Density assignment uncertainty is calculated as the standard 265 deviation of the eight resulting values of glacier-wide winter balance. Individual sources of uncertainty are 266

propagated through the conversion of snow depth and density measurements to glacier-wide WB. Finally, the combined effect of all three sources of uncertainty on the glacier-wide WB is quantified. We use the standard deviation of this distribution as a useful metric of uncertainty on the glacier-wide WB. We calculate a relative uncertainty as the normalized sum of differences between every pair of one hundred distributed WB estimates including  $\sigma_{GS}$  and  $\sigma_{INT}$ .

272 Grid-scale uncertainty ( $\sigma_{GS}$ )

We make use of the zigzag surveys to quantify the true variability of WB at the grid scale. Our limited data 273 do not permit a spatially-resolved assessment of grid-scale uncertainty, so we characterize this uncertainty 274 as uniform across each glacier and represent it by a normal distribution. The distribution is centred at zero 275 and has a standard deviation equal to the mean standard deviation of all zigzag measurements for each 276 glacier. For each iteration of the Monte Carlo, WB values are randomly chosen from the distribution and 277 added to the values of gridcell-averaged WB. These perturbed gridcell-averaged values of WB are then used 278 in the interpolation. We represent uncertainty in glacier-wide WB due to grid-scale uncertainty ( $\sigma_{\rm GS}$ ) as the 279 standard deviation of the resulting distribution of glacier-wide WB estimates. 280

281 Density assignment uncertainty  $(\sigma_{\rho})$ 

We incorporate uncertainty due to the method of density assignment by carrying forward all eight density interpolation methods (Table 3) when estimating glacier-wide WB. By choosing to retain even the least plausible options, as well as the questionable FS data, this approach results in a generous assessment of uncertainty. We represent the glacier-wide WB uncertainty due to density assignment uncertainty ( $\sigma_{\rho}$ ) as the standard deviation of glacier-wide WB estimates calculated using each density assignment method.

287 Interpolation uncertainty  $(\sigma_{\text{INT}})$ 

We represent the uncertainty due to interpolation of gridcell-averaged WB in different ways for LR and SK. LR interpolation uncertainty is represented by a multivariate normal distribution of possible regression coefficients ( $\beta_i$ ). The standard deviation of each distribution is calculated using the covariance of regression coefficients as outlined in Bagos and Adam (2015), which ensures that regression coefficients are internally consistent. The  $\beta_i$  distributions are randomly sampled and used to calculate gridcell-estimated WB.

293 SK interpolation uncertainty is represented by the standard deviation for each gridcell-estimated value 294 of WB generated by the DiceKriging package. The standard deviation of glacier-wide WB is then found 295 by taking the square root of the average variance of each gridcell-estimated WB. The final distribution of

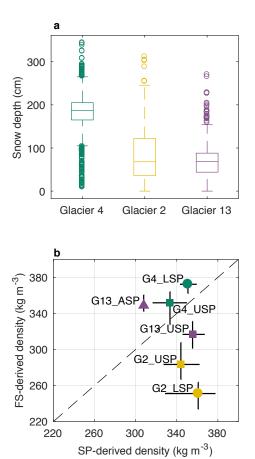


Fig. 2. Measured snow depth and density. (a) Boxplot of measured snow depth on Glaciers 4, 2 and 13 with the first quartiles (box), median (line within box), minimum and maximum values excluding outliers (bar) and outliers (circles), which are defined as being outside of the range of 1.5 times the quartiles (approximately  $\pm 2.7\sigma$ ). (b) Comparison of depth-averaged densities estimated using Federal Sampler (FS) measurements and a wedge cutter in a snow pit (SP) for Glacier 4 (G4), Glacier 2 (G2) and Glacier 13 (G13). Labels indicate SP locations in the accumulation area (ASP), upper ablation area (USP) and lower ablation area (LSP). Error bars for SP-derived densities are calculated by varying100 the thickness and density of layers that are too hard to sample, and error bars for FS-derived densities are the standard deviation of measurements taken at one location. One-to-one line is dashed.

glacier-wide WB values is centred at the glacier-wide WB estimated with SK. For simplicity, the standard deviation of glacier-wide WB values that result from either LR or SK interpolation uncertainty is referred to as  $\sigma_{\text{INT}}$ .

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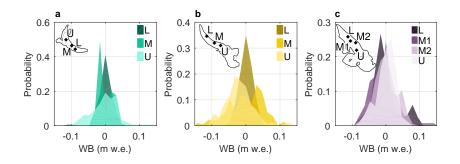


Fig. 3. Distributions of estimated winter-balance values for each zigzag survey in lower (L), middle (M) and upper (U) ablation areas (insets). Local mean has been subtracted. (a) Glacier 4. (b) Glacier 2. (c) Glacier 13.

# RESULTS AND DISCUSSION

#### Field measurements

301 Snow depth

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Mean snow depth varied systematically across the study region, with Glacier 4 having the highest mean 302 snow depth and Glacier 13 having the lowest (Fig. 2a). At each measurement location, the median range 303 of measured depths (3-4 points) as a percent of the mean local depth is 2\%, 11\% and 12\%, for Glaciers 4, 304 305 2 and 13, respectively. While Glacier 4 has the lowest point-scale variability, as assessed above, it also has the highest proportion of outliers, indicating a more variable snow depth across the glacier. The average 306 standard deviation of all zigzag depth measurements is 0.07 m, 0.17 m and 0.14 m, for Glaciers 4, 2 and 13, 307 respectively. When converted to values of WB using the local FS-derived density measurement, the average 308 standard deviation is 0.027 m.w.e., 0.035 m.w.e. and 0.040 m.w.e. WB data for each zigzag are not normally 309 distributed (Fig. 3). 310

#### $Snow \ density$

Contrary to expectation, co-located FS and SP measurements are found to be uncorrelated (R<sup>2</sup> = 0.25, Fig. 2b). The FS appears to oversample in deep snow and undersample in shallow snow. Oversampling by small-diameter sampling tubes has been observed in previous studies, with a percent error between 6.8% and 11.8% (e.g. Work and others, 1965; Fames and others, 1982; Conger and McClung, 2009). Studies that use FS often apply a 10% correction to all measurements for this reason (e.g. Molotch and others, 2005). Oversampling has been attributed to slots "shaving" snow into the tube as it is rotated (e.g. Dixon and Boon, 2012) and to snow falling into the slots, particularly for snow samples with densities >400 kg m<sup>-3</sup> and snow

bottom of the sampler (Turcan and Loijens, 1975). Loss by this mechanism may have occurred in our study, 320 given the isothermal and melt-affected snow conditions observed over the lower reaches of Glaciers 2 and 13. 321 Relatively poor FS spring-scale sensitivity also calls into question the reliability of measurements for snow 322 depths  $<20\,\mathrm{cm}$ . 323 Our FS-derived density values are positively correlated with snow depth ( $R^2 = 0.59$ ). This relationship 324 could be a result of physical processes, such as compaction in deep snow and preferential formation of depth 325 hoar in shallow snow, but is more likely a result of measurement artefacts for a number of reasons. First, 326 the total range of densities measured by the FS seems improbably large (227-431 kg m<sup>-3</sup>). At the time of 327 sampling the snow pack had little fresh snow, which confounds the low density values, and was not yet 328 saturated and had few ice lenses, which confounds the high density values. Moreover, the range of FS-329 derived values is much larger than than of SP-derived values when co-located measurements are compared. 330 Second, compaction effects of the magnitude required to explain the density differences between SP and 331 FS measurements would not be expected at the measured snow depths (up to 340 cm). Third, no linear 332 relationship exists between depth and SP-derived density ( $R^2 = 0.05$ ). These findings suggest that the FS 333 measurements have a bias for which we have not identified a suitable correction. Despite this bias, we use 334 FS-derived densities to generate a range of possible WB estimates and to provide a generous estimate of 335 uncertainty arising from density assignment. 336

depths >1 m (e.g. Beaumont and Work, 1963). Undersampling is likely to occur due to loss of snow from the

# 337 Density assignment

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Given the lack of correlation between co-located SP- and FS-derived densities (Fig. 2), we use the densities 338 derived from these two methods separately (Table 3). SP-derived regional (S1) and glacier-mean (S2) densities 339 are within one standard deviation of the corresponding FS-derived densities (F1 and F2) although SP-derived 340 density values are larger (see Supplementary Material, Table S2). For both SP- and FS-derived densities, the 341 mean density for any given glacier (S2 or F2) is within one standard deviation of the mean across all glaciers 342 (S1 or F1). Correlations between elevation and SP- and FS-derived densities are generally high  $(R^2 > 0.5)$  but 343 vary between glaciers (Supplementary material, Table S2). For any given glacier, the standard deviation of the 344 3-4 SP- or FS-derived densities is <13\% of the mean of those values (S2 or F2) (Supplementary material, 345 Table S2). We adopt S2 (glacier-wide mean of SP-derived densities) as the reference method of density 346 assignment. Though the method described by S2 does not account for known basin-scale spatial variability 347

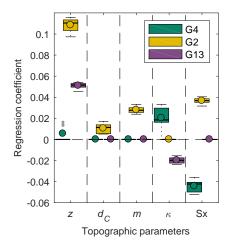


Fig. 4. Distribution of coefficients  $(\beta_i)$  determined by linear regression of gridcell-averaged WB on DEM-derived topographic parameters for the eight different density assignment methods (Table 3). Coefficients are calculated using standardized data, so values can be compared across parameters. Regression coefficients that are not significant are assigned a value of zero. Topographic parameters include elevation (z), distance from centreline  $(d_C)$ , slope (m), curvature  $(\kappa)$  and wind redistribution (Sx). Aspect  $(\alpha)$  and "northness" (N) are not shown because coefficient values are zero in every case. The box plot shows first quartiles (box), median (line within box), mean (circle within box), minimum and maximum values excluding outliers (bars) and outliers (gray dots), which are defined as being outside of the range of 1.5 times the quartiles (approximately  $\pm 2.7\sigma$ ).

in snow density (e.g. Wetlaufer and others, 2016), it is commonly used in winter balance studies (e.g. Elder and others, 1991; McGrath and others, 2015; Cullen and others, 2017).

# Gridcell-averaged winter balance

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The distributions of gridcell-averaged WB values for the individual glaciers are similar to those in Fig. 2a but with fewer outliers (see Supplementary Material). The standard deviations of WB values determined from the zigzag surveys are almost twice as large as the mean standard deviation of point-scale WB values within a gridcell measured along transects (see Supplementary Material). However, a small number of gridcells sampled in transect surveys have standard deviations in WB that exceed 0.25 m w.e. (~10 times greater than those for zigzag surveys).

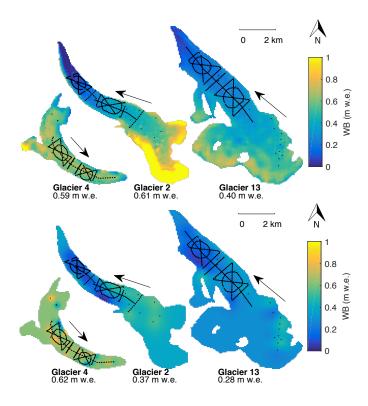


Fig. 5. Spatial distribution of winter balance (WB) estimated using linear regression (top row) and simple kriging (bottom row) with densities assigned as per S2 (Table 3). The linear regression method involves multiplying regression coefficients, found using cross validation and model averaging, by topographic parameters for each gridcell. Simple kriging uses the covariance of measured values to find a set of optimal weights for estimating values at unmeasured locations. Locations of snow-depth measurements taken in May 2016 are shown as black dots. Ice-flow directions are indicated by arrows. Values of glacier-wide WB are given below labels.

## Distributed winter balance

358 Linear Regression

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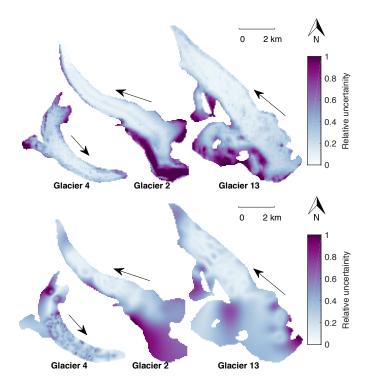
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Of the topographic parameters in the LR, elevation (z) is the most significant predictor of gridcell-averaged

WB for Glaciers 2 and 13, while wind redistribution (Sx) is the most significant predictor for Glacier 4

Table 4. Glacier-wide winter balance (WB, m w.e.) estimated using linear regression and simple kriging for the three study glaciers. Root mean squared error (RMSE, m w.e.) is computed as the average of all RMSE values between gridcell-averaged values of WB (the data) that were randomly selected and excluded from interpolation (1/3 of all data) and those estimated by interpolation. RMSE as a percent of the glacier-wide WB is shown in brackets.

	Linea	r regression	Simple kriging			
	WB	RMSE	WB	RMSE		
G4	0.58	0.15 (26%)	0.62	0.13 (21%)		
G2	0.58	0.10~(17%)	0.37	0.07~(19%)		
G13	0.38	0.08~(21%)	0.27	0.07~(26%)		



**Fig. 6.** Relative uncertainty in distributed winter balance (WB) (Fig. 5) found using linear regression (top row) and simple kriging (bottom row). Values closer to one indicate higher relative uncertainty. Ice-flow directions are indicated by arrows.

(Fig. 4). As expected, gridcell-averaged WB is positively correlated with elevation where the correlation is significant. It is possible that the elevation correlation was accentuated due to melt onset for Glacier 13 in particular. Our results are consistent with many studies that have found elevation to be the most significant predictor of winter-balance data (e.g. Machguth and others, 2006; McGrath and others, 2015). The WB-elevation gradient is 13 mm/100 m on Glacier 2 and 7 mm/100 m on Glacier 13. These gradients are consistent with those reported for a few glaciers in Svalbard (Winther and others, 1998) but considerably smaller than many reported WB-elevation gradients, which range from about 60–240 mm/100 m (e.g. Hagen and Liestøl, 1990; Tveit and Killingtveit, 1994; Winther and others, 1998). Extrapolating linear relationships to unmeasured locations typically results in large uncertainties, as seen by the large WB values (Fig. 5) and large relative uncertainty (Fig. 6) in the high-elevation regions of the accumulation areas of Glaciers 2 and 13. The low of correlation between WB and elevation Glacier 4 is consistent with Grabiec and others (2011) and López-Moreno and others (2011), who conclude that highly variable distributions of snow are attributed to complex interactions between topography and the atmosphere that could not be easily quantified.

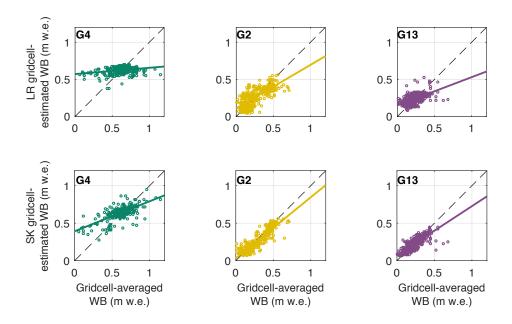


Fig. 7. Winter balance (WB) estimated by linear regression (LR, top row) or simple kriging (SK, bottom row) versus the grid-cell averaged WB data for Glacier 4 (left), Glacier 2 (middle) and Glacier 13 (right). Each circle represents a single gridcell. Best-fit (solid) and one-to-one (dashed) lines are shown.

Gridcell-averaged WB is negatively correlated with Sx on Glacier 4, counter-intuitively indicating less snow in what would be interpreted as sheltered areas. Gridcell-averaged WB is positively correlated with Sx on Glaciers 2 and 13. Similarly, gridcell-averaged WB is positively correlated with curvature on Glacier 4 and negatively correlated on Glaciers 2 and 13. Our results corroborate those of McGrath and others (2015) in a study of six glaciers in Alaska (DEM resolutions of 5 m) where elevation and Sx were the only significant parameters for all glaciers; Sx regression coefficients were smaller than elevation regression coefficients, and in some cases, negative. While our results point to wind having an impact on snow distribution, the wind redistribution parameter (Sx) may not adequately capture these effects at our study sites. For example, Glacier 4 is located in a curved valley with steep side walls, so specifying a single cardinal direction for wind may not be adequate. Further, the scale of deposition may be smaller than the resolution of the Sx parameter estimated from the DEM. Creation of a parametrization for sublimation from blowing snow, which has been shown to be an important mechanism of mass loss from ridges (e.g. Musselman and others, 2015), may also improve explanatory power of LR for our study sites.

We find that transfer of LR coefficients between glaciers results in large estimation errors. Regression coefficients from Glacier 4 produce the highest root mean squared error (0.38 m w.e. on Glacier 2 and 0.40 m w.e. on Glacier 13, see Table 4 for comparison) and glacier-wide WB values are the same for all

glaciers (0.64 m w.e.) due to the dominance of the regression intercept. Even if the LR is performed with WB values from all glaciers combined, the resulting coefficients produce large root mean squared errors when applied to individual glaciers (0.31 m w.e., 0.15 m w.e. and 0.14 m w.e. for Glaciers 4, 2 and 13, respectively). Our results are consistent with those of Grünewald and others (2013), who found that local statistical models cannot be transferred across basins and that regional-scale models are not able to explain the majority of observed variance in winter balance.

# 396 Simple kriging

Fitted kriging parameters, including the nugget and spatial correlation length, can provide insight into 397 important scales of winter-balance variability. The model fitted to the gridcell-averaged values of WB for 398 Glacier 4 has a short correlation length (90 m) and large nugget (see Supplementary Material Table S3), 399 suggesting variability in winter balance at smaller scales. Conversely, Glaciers 2 and 13 have longer correlation 400 lengths (~450 m) and smaller nuggets, suggesting variability at larger scales. Additionally, SK is better able 401 to estimate values of WB for Glaciers 2 and 13 than for Glacier 4 (Fig. 7). Due to a paucity of data, SK 402 produces almost uniform gridcell-estimated values of winter balance in the accumulation area of each glacier, 403 inconsistent with observations described in the literature (e.g. Machguth and others, 2006; Grabiec and 404 others, 2011). As expected, extrapolation using SK leads to large uncertainty (Fig. 6), further emphasizing 405 the need for spatially distributed point-scale measurements. 406

# 407 LR and SK comparison

Glacier-wide WB estimates found using both LR and SK are  $\sim 0.58 \,\mathrm{m}$  w.e. for Glacier 4 but both are poor 408 predictors of WB in measured gridcells (Table 4). For Glaciers 2 and 13, SK estimates are more than 0.1 m w.e. 409 (up to 40%) lower than LR estimates (Table 4). RMSE as a percentage of the glacier-wide WB are comparable 410 between LR and SK (Table 4) with an average RMSE of 22%. This comparability is interesting, given that 411 all of the data were used to generate the SK model, while only 2/3 were used in the LR (consistent with 412 the best SK model estimated with 2/3 of the data). Gridcell-estimated values of WB found using LR and 413 SK differ markedly in the upper accumulation areas of Glaciers 2 and 13 (Fig. 5), where observations are 414 sparse and topographic parameters, such as elevation, vary considerably. The influence of elevation results in 415 substantially higher LR-estimated values of WB at high elevation, whereas SK-estimated values approximate 416 the nearest data. Estimates of ablation-area-wide WB differ by <7% between LR and SK on each glacier, 417 further emphasizing the combined role of interpolation method and measurement scarcity in the accumulation 418 area on glacier-wide WB estimates. 419

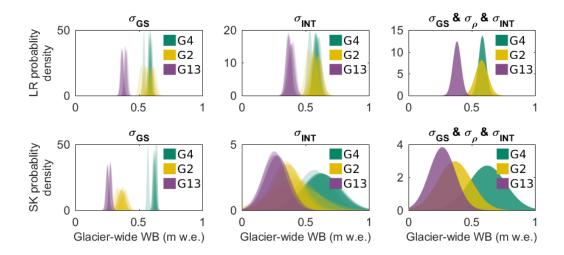


Fig. 8. Distributions of glacier-wide winter balance (WB) for Glaciers 4 (G4), 2 (G2) and 13 (G13) that arise from various sources of uncertainty. WB distribution arising from grid-scale uncertainty ( $\sigma_{GS}$ ) (left column). WB distribution arising from interpolation uncertainty ( $\sigma_{INT}$ ) (middle column). WB distribution arising from a combination of  $\sigma_{GS}$ ,  $\sigma_{INT}$  and density assignment uncertainty ( $\sigma_{\rho}$ ) (right column). Results are shown for interpolation by linear regression (LR, top row) and simple kriging (SK, bottom row). Left two columns include eight distributions per glacier (colour) and each corresponds to a density assignment method (S1–S4 and F1–F4).

## 420 Uncertainty analysis

Glacier-wide winter balance is affected by uncertainty introduced by the representativeness of gridcell-421 averaged values of WB ( $\sigma_{GS}$ ), choosing a method of density assignment ( $\sigma_{\rho}$ ), and interpolating/extrapolating 422 WB values across the domain ( $\sigma_{\text{INT}}$ ). Using a Monte Carlo analysis, we find that interpolation uncertainty 423 contributes more to WB uncertainty than grid-scale uncertainty or density assignment method. In other 424 words, the distribution of glacier-wide WB that arises from grid-scale uncertainty and the differences in 425 distributions between methods of density assignment are smaller than the distribution that arises from 426 interpolation uncertainty (Fig. 8 and Table 5). The WB distributions obtained using LR and SK overlap 427 for a given glacier, but the distribution modes differ (Fig. 8). For reasons outlined above, SK-estimated 428 values of WB in the accumulation area are generally lower, which lowers the glacier-wide WB estimate. The 429 uncertainty in SK-estimated values of WB is large, and unrealistic glacier-wide values of WB of 0 m w.e. can 430 be estimated (Fig. 8). Our results caution strongly against including interpolated/extrapolated values of WB 431 in comparisons with remote sensing- or model-derived estimates of WB. If possible, such comparisons should 432 be restricted to point-scale data. 433

**Table 5.** Standard deviation (×10<sup>-2</sup> m w.e.) of glacier-wide winter balance (WB) distributions arising from uncertainties in grid-scale WB ( $\sigma_{GS}$ ), density assignment ( $\sigma_{\rho}$ ), interpolation ( $\sigma_{INT}$ ) and all three sources combined ( $\sigma_{ALL}$ ) for linear regression (left columns) and simple kriging (right columns)

	Linear regression				Simple kriging			
	$\sigma_{ m GS}$	$\sigma_{ ho}$	$\sigma_{INT}$	$\sigma_{ALL}$	$\sigma_{ m GS}$	$\sigma_{ ho}$	$\sigma_{INT}$	$\sigma_{ALL}$
Glacier 4	0.86	1.90	2.13	2.90	0.85	2.15	14.05	14.72
Glacier 2	1.80	3.37	3.09	4.90	2.53	2.03	13.78	13.44
Glacier 13	1.12	1.68	2.80	3.20	1.15	1.27	9.65	10.43

Grid-scale uncertainty ( $\sigma_{\rm GS}$ ) is the smallest assessed contributor to overall WB uncertainty. This result is consistent with the generally smoothly-varying snow depths encountered in zigzag surveys, and previously reported ice-roughness lengths on the order of centimetres (e.g. Hock, 2005) compared to snow depths on the order of decimetres to metres. Given our assumption that zigzags are an adequate representation of grid-scale variability, the low WB uncertainty arising from  $\sigma_{\rm GS}$  implies that subgrid-scale sampling need not be a high priority for reducing overall uncertainty. Our assumption that the 3–4 zigzag surveys can be used to estimate glacier-wide  $\sigma_{\rm GS}$  may be flawed, particularly in areas with debris cover, crevasses and steep slopes.

Our analysis did not include uncertainty arising from density measurement errors associated with the FS, wedge cutters and spring scales, from vertical and horizontal errors in the DEM or from error associated with estimating measurement locations based on the GPS position of the lead observer. We assume that these sources of uncertainty are either encompassed by the sources investigated or negligible.

The values of glacier-wide WB for our study glaciers (using LR and S2 density assignment method), with an uncertainty equal to one standard deviation of the distribution found with Monte Carlo analysis, are:  $0.59 \pm 0.03 \,\mathrm{m}$  w.e. for Glacier 4,  $0.61 \pm 0.05 \,\mathrm{m}$  w.e. for Glacier 2 and  $0.40 \pm 0.03 \,\mathrm{m}$  w.e. for Glacier 13. The glacier-wide WB uncertainty from the three investigated sources of uncertainty ranges from  $0.03 \,\mathrm{m}$  w.e (5%) to  $0.05 \,\mathrm{m}$  w.e (8%) for LR estimates and from  $0.10 \,\mathrm{m}$  w.e (37%) to  $0.15 \,\mathrm{m}$  w.e (24%) for simple-kriging estimates (Table 4).

# Context and caveats

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- 452 Regional winter-balance gradient
- 453 Although we find considerable inter- and intra-basin variability in winter balance, our results are consistent
- 454 with a regional-scale winter-balance gradient for the continental side of the St. Elias Mountains (Fig. 9).
- 455 Winter-balance data are compiled from Taylor-Barge (1969), the three glaciers presented in this paper and

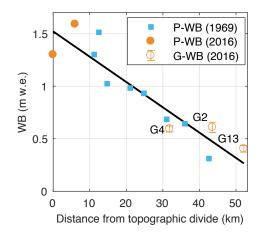


Fig. 9. Relationship between winter balance (WB) and linear distance from the regional topographic divide between the Kaskawulsh and Hubbard Glaciers in the St. Elias Mountains. Point-scale values of WB from snow-pit data reported by Taylor-Barge (1969) (blue boxes, P-WB). LR-estimated glacier-wide WB calculated using density assignment S2 for Glaciers 4 (G4), 2 (G2) and 13 (G13) with errors bars calculated as the standard deviation of Monte Carlo-derived WB distributions (this study) (open orange circles, G-WB). Point-scale WB estimated from snow-pit data at two locations in the accumulation area of the Kaskawulsh Glacier, collected in May 2016 (unpublished data, SFU Glaciology Group) (filled orange dots, P-WB). Black line indicates best fit (R<sup>2</sup> = 0.85).

two snow pits we analyzed near the head of the Kaskawulsh Glacier between 20-21 May 2016. The data 456 show a linear decrease of  $0.024\,\mathrm{m\,w.e.~km^{-1}}$  ( $\mathrm{R^2}=0.85$ ) in winter balance with distance from the regional 457 topographic divide between the Kaskawulsh and Hubbard Glaciers, as identified by Taylor-Barge (1969). 458 While the three study glaciers fit the regional trend, the same relationship would not apply if just the Donjek 459 460 Range were considered. We hypothesize that interaction between meso-scale weather patterns and large-scale mountain topography is a major driver of regional-scale winter balance. Further insight into regional-scale 461 patterns of winter balance in the St. Elias Mountains could be gained by investigating moisture source 462 trajectories and the contribution of orographic precipitation. 463

#### Limitations and future work

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The potential limitations of our work include the restriction of our data to a single year, minimal sampling in the accumulation area, the problem of uncorrelated SP- and FS-derived densities, a sampling design that could not be optimized a priori, the assumption of spatially uniform subgrid variability and lack of more finely resolved DEMs.

Inter-annual variability in winter balance is not considered in our study. A number of studies have found temporal stability in spatial patterns of snow distribution and that statistical models based on topographic

parameters could be applied reliably between years (e.g. Grünewald and others, 2013). For example, Walmsley 471 (2015) analyzed more than 40 years of winter balance recorded on two Norwegian glaciers and found that 472 snow distribution is spatially heterogeneous yet exhibits robust temporal stability. Contrary to this, Crochet 473 and others (2007) found that snow distribution in Iceland differed considerably between years and depended 474 primarily on the dominant wind direction over the course of a winter. Therefore, multiple years of snow depth 475 476 and density measurements, that are not necessarily consecutive, are needed to better understand inter-annual variability in winter-balance distribution within the Donjek Range. 477 There is a conspicuous lack of data in the accumulation areas of our study glaciers. With increased sampling 478 in the accumulation area, interpolation uncertainties would be reduced where they are currently greatest and 479 the LR would be better constrained. Although certain regions of the glaciers remain inaccessible for direct 480 measurements, other methods of obtaining winter-balance, including ground-penetrating radar and DEM 481 differencing with photogrammetry or lidar, could be used in conjunction with manual probing to increase 482 the spatial coverage of measurements. 483 The lack of correlation between SP- and FS-derived densities needs to be reconciled. Contrary to our 484 results, most studies that compare SP- and FS-derived densities report minimal discrepancy (e.g. Dixon and 485 Boon, 2012, and sources within). Additional co-located density measurements are needed to better compare 486 the two methods of obtaining density values. Comparison with other FS would also be informative. Even 487 with this limitation, density assignment was, fortunately, not the largest source of uncertainty in estimating 488 glacier-wide winter balance. 489 Our sampling design was chosen to achieve broad spatial coverage of the ablation area, but is likely too 490 finely resolved along transects for many mass-balance surveys to replicate. An optimal sampling design would 491 minimize uncertainty in winter balance while reducing the number of required measurements. Analysis of 492 the estimated winter balance obtained using subsets of the data is underway to make recommendations on 493 494 optimal transect configuration and along-track spacing of measurements. López-Moreno and others (2010) found that 200-400 observations are needed within a non-glacierized alpine basin (6 km<sup>2</sup>) to obtain accurate 495 and robust snow distribution models. Similar guidelines would be useful for glacierized environments. 496 In this study, we assume that the subgrid variability of winter balance is uniform across a given glacier. 497 Contrary to this assumption, McGrath and others (2015) found greater variability of winter-balance values 498

close to the terminus. Testing our assumption could be a simple matter of prioritizing the labour-intensive

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zigzags surveys. To ensure consistent quantification of subgrid variability, zigzag survey measurements could also be tested against other measurements methods, such as lidar.

DEM gridcell size is known to influence values of computed topographic parameters (Zhang and 502 Montgomery, 1994; Garbrecht and Martz, 1994; Guo-an and others, 2001; López-Moreno and others, 2010). 503 The relationship between topographic parameters and winter balance is, therefore, not independent of DEM 504 505 gridcell size. For example, Kienzle (2004) and López-Moreno and others (2010) found that a decrease in spatial resolution of the DEM results in a decrease in the importance of curvature and an increase in the 506 importance of elevation in LR of snow distribution on topographic parameters in non-glacierized basins. 507 The importance of curvature in our study is affected by the DEM smoothing that we applied to obtain a 508 spatially continuous curvature field (see Supplementary Material). A comparison of regression coefficients 509 from high-resolution DEMs obtained from various sources and sampled with various gridcell sizes could be 510 used to characterize the dependence of topographic parameters on DEMs, and therefore assess the robustness 511 of inferred relationships between winter balance and topographic parameters. 512

#### 513 CONCLUSION

We estimate winter balance for three glaciers (termed Glacier 2, Glacier 4 and Glacier 13) in the St. Elias Mountains, Yukon, Canada from multiscale snow depth and density measurements. Linear regression and simple kriging are used to obtain estimates of distributed winter balance. We use Monte Carlo analysis to evaluate the contributions of interpolation, the assignment of snow density and grid-scale variability of winter balance to uncertainty in glacier-wide winter balance.

Values of glacier-wide winter balance estimated using linear regression and simple kriging differ by up to 0.24 m w.e. (~50%). We find that interpolation uncertainty is the largest assessed source of uncertainty in glacier-wide winter balance (5% for linear-regression estimates and 32% for simple-kriging estimates). Uncertainty resulting from the method of density assignment is comparatively low, despite the wide range of methods explored. Given our representation of grid-scale variability, the resulting winter balance uncertainty is small indicating that extensive subgrid-scale sampling is not required to reduce overall uncertainty.

Our results suggest that processes governing distributed winter balance differ between glaciers, highlighting
the importance of regional-scale winter-balance studies. The estimated distribution of winter balance on
Glacier 4 is characterized by high variability, as indicated by the poor correlation between estimated and
observed values and large number of data outliers. Glaciers 2 and 13 appear to have lower spatial variability,
with elevation being the dominant predictor of gridcell-averaged winter balance. A wind-redistribution

parameter is found to be a weak but significant predictor of winter balance, though conflicting relationships between glaciers make it difficult to interpret. The major limitations of our work include the restriction of our data to a single year and minimal sampling in the accumulation area. Although challenges persist when estimating winter balance, our data are consistent with a regional-scale winter-balance gradient for the continental side of the St. Elias Mountains.

#### AUTHOR CONTRIBUTION STATEMENT

AP planned and executed the data collection, performed all calculations and drafted the manuscript. GF conceived of the study, contributed to field planning and data collection, oversaw all stages of the work and edited the manuscript. VR provided guidance with statistical methods and edited the manuscript.

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