

# Results Observations

## Overview

This document shows an overview of the data that are available for the project. It provides a first look at the processed data and provides figures that visualize the data. Section 1 examines the density data and uncertainty and potential systematic errors associated with measurements made in the snowpits and using a Federal Sampler. Section 2 briefly looks at the snow depths measured at the study glaciers. Section 3 visualizes the collected zigzag data. Section 4 examines the various ways to estimate snow water equivalent (SWE) at each measurement location. It focuses on options for how to interpolate density measurements and then visualizes estimated SWE at the measurement locations.

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# 1 Density Estimates

## 1.1 Basic statistics

The standard deviation of each type of density measurement is less than 10% of the mean density (Table 1). For snowpit derived densities, the mean density is within one standard deviation between glaciers. The densities estimated using the Federal Sampler differed between glacier within one standard deviation. Our density measurements on Glacier 2 were lower than those on Glacier 4, while density measurements taken on Glacier 13 were the same as Both Glaciers 2 and 4. The mean of all Federal Sampler derived density values was skewed by the proportionally large number of measurements obtained on Glacier 13.

Table 1: Statistics of integrated densities measured using Federal Sampler or vertical density profiles (of snow wedge measurements) in snow pits. Mean, standard deviation (std), and number ( $n$ ) of snow density ( $\text{kg m}^{-3}$ ) measurements on study glaciers is shown.

Glacier	Snowpits			Federal Sampler		
	Mean	Std	n	Mean	Std	n
<b>Glacier 4</b>	348	13	3	355	18	7
<b>Glacier 2</b>	333	26	4	286	34	7
<b>Glacier 13</b>	349	26	3	316	40	17
<b>All</b>	342	26	10	318	42	31

## 1.2 Federal Sampler measurements and snow depth

There is a positive linear relation ( $R^2 = 0.59$ ,  $p < 0.01$ ) between measured snow density and depth for all Federal Sampler measurements (Figure 1). This positive relationship could be a result of physical processes, such as compaction, and/or artefacts during data collection; however, it seems more likely that this trend is a result of measurement artefacts for a number of reasons. First, the range of densities measured by the Federal sampler is large ( $225\text{--}410 \text{ kg m}^{-3}$ ) and the extreme values seem unlikely to exist at these study glaciers, which experience a continental snowpack with minimal mid-winter melt events. Previous unpublished density measurements taken on Glacier 2 for five study years have a mean snow density of  $298 \text{ kg m}^{-3}$  and a standard deviation of  $48 \text{ kg m}^{-3}$  (range of  $264\text{--}396 \text{ kg m}^{-3}$  with a maximum density difference of  $110 \text{ kg m}^{-3}$  in any one year) (Flowers, 2016, personal communication). Second, compaction effects would likely be small at these study glaciers because of the relatively shallow snowpack (deepest measurement was 340 cm). Third, no linear relationship exists between depth and snowpit-derived density ( $R^2 = 0.05$ ) as can be seen in a plot of the depth-density relationship in snowpits in Figure 1. Together, these reasons lead us to conclude that the Federal Sampler measurements are biased. Linear detrending can correct the density data but it was decided to use uncorrected data for future analysis.

The Federal Sampler appears to oversample in deep snow and undersample in shallow snow. Oversampling by small diameter (area of  $10\text{--}12 \text{ cm}^2$ ) sampling tubes has been observed in previous studies, with a percent error between  $+6.8\%$  and  $11.8\%$ (???). Studies

that use Federal Samplers often apply a 10% correction to all measurements (e.g. ?). ? attributed oversampling to slots “shaving” snow into the tube as it is rotated as well as cutter design forcing snow into the tube. ? found that only when snow samples had densities greater than  $400 \text{ kg m}^{-3}$  and snow depth greater than 1 m, the Federal Sampler oversampled due to snow falling into the greater area of slots. Undersampling is likely to occur due to snow falling out of the bottom of the sampler (?). It is likely that this occurred during our study since a large portion of the lower elevation snow on both Glaciers 2 and 13 was melt affected and thin, allowing for easier lateral displacement of the snow as the sampler was inserted. For example, on Glacier 13 the snow surface had been affected by radiation melt (especially at lower elevations where the snow was shallower) and the surface would collapse when the sampler was inserted into the snow. It is also difficult to measure the weight of the sampler and snow with the spring scale when there was little snow because the weight was at the lower limit of what could be detected by the scale.

## 1.3 Density uncertainties

### 1.3.1 Snowpit densities

Uncertainty in estimating density from snowpits stems from measurement errors and incorrect assignment of density to layers that could not be sampled (i.e. ice lenses and ‘hard’ layers). To determine a possible range of snowpit-derived integrated snow density values, the original data are used and three quantities are varied. Ice layer density is varied between 700 and  $900 \text{ kg m}^{-3}$ , ice layer thickness is varied by  $\pm 1 \text{ cm}$  of the observed thickness, and the density of layers identified as being too hard to sample (but not ice) was varied between 600 and  $700 \text{ kg m}^{-3}$ .

The range of integrated density values is always less than 15% of the reference density, with the largest ranges present on Glacier 2 (Table 2). Density values for shallow pits that contained ice lenses were particularly sensitive to changes in density and ice lens thickness.

### 1.3.2 Federal Sampler densities

Mean Federal Sampler derived density has a larger range of values over the study glaciers when compared to snowpit densities (Table 3). The percent range is also larger than snowpit densities for many of the measurement locations.

## 1.4 Comparing density from snowpit and Federal Sampler measurements

To compare snowpit-derived densities and Federal Sampler-derived densities, eight Federal Sampler measurements were taken around two snowpit locations on each study glacier. The overall range of Federal Sampler-derived densities is larger than that of the snowpit-derived density values (Figure 2). Within the minimum and maximum snowpit-derived densities, the values are indistinguishable for all snowpit locations, except for the accumulation snowpit on Glacier 13 (‘G13\_ASP’).

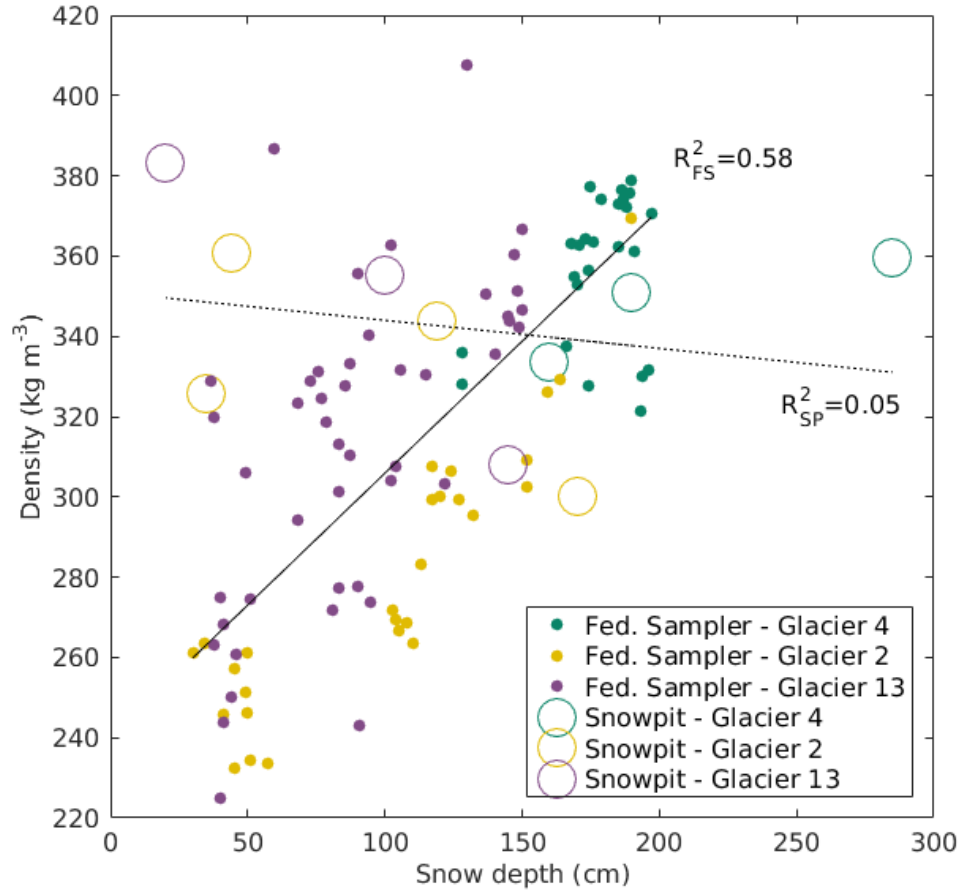


Figure 1: Relationship between measured density and snow depth for all Federal Sampler and snowpit locations. A linear regression of depth and density for Federal Sampler (FS) measurements is shown as a solid line and for snowpits (SP) is shown as a dashed line.

Table 2: Summary of reference and range of integrated snow density calculated from snowpit measurements. The reference density values are calculated with an ice layer density of  $917 \text{ kg m}^{-3}$  and a ‘hard’ snow density of  $600 \text{ kg m}^{-3}$ . To determine the error in estimating integrated snow density, ice density, ice thickness, and the ‘hard’ layer density are varied between  $700$  and  $917 \text{ kg m}^{-3}$ ,  $\pm 1 \text{ cm}$ , and  $500$  and  $600 \text{ kg m}^{-3}$ , respectively.

Snowpit Name	Depth (m)	Density ( $\text{kg m}^{-3}$ )		Range	Range as % of reference value	Elevation (m a.s.l)	Average Temperature ( $^{\circ}$ )
		Reference	Minimum	Maximum			
Glacier 4, Lower	190	350.9	343.2	359.1	15.9	2154	− 4.3
Glacier 4, Upper	160	333.4	316.6	349.6	33.0	2298	− 5.7
Glacier 4, Accumulation	285	359.7	356.6	362.4	5.8	2482	− 6.8
Glacier 2, Lower	44	360.9	328.6	377.3	48.7	2175	− 3.7
Glacier 2, Zone 4A	35	325.8	307.9	344.7	36.8	2261	− 3.4
Glacier 2, Upper	119	344.0	327.1	361.9	34.8	2349	− 6.6
Glacier 2, Accumulation	170	300.2	298.6	303.1	4.5	2550	− 7.4
Glacier 13, Lower	20	383.0	383.0	383.0	0	2139	− 0.1
Glacier 13, Upper	100	355.4	345.6	366.9	21.3	2257	− 1.7
Glacier 13, Accumulation	145	307.8	306.4	308.2	1.8	2521	− 5.6

Table 3: Range of densities estimated from Federal Sampler measurements. The number ( $n$ ) of reliable measurements, as well as the minimum, maximum, and mean density are shown. The density range, given as a percent of the mean density, is also shown. Location refers to the snowpit name as shown in Figure ??

Location	$n$	Density ( $\text{kg m}^{-3}$ )			Range as % of mean (%)	Elevation (m a.s.l)
		Mean	Minimum	Maximum		
G04_Z3A_SWE	3	334	309	358	14	2229
G04_USP	6	311	274	353	22	2298
G04_Z2A_SWE	3	360	303	431	35	2162
G04_LSP	7	272	250	297	13	2154
G04_Z5B_SWE	2	337	324	350	7	2360
G04_Z5A_SWE	3	311	275	351	21	2328
G04_Z5C_SWE	2	361	350	373	6	2332
G02_Z5C_SWE	2	296	245	347	28	2332
G02_USP	7	294	232	353	34	2349
G02_Z7A_SWE	3	326	304	349	12	2403
G02_Z7B_SWE	2	336	320	351	9	2458
G02_Z7C_SWE	3	351	338	365	7	2442
G02_Z3B_SWE	3	349	341	353	3	2172
G02_LSP_SWE	7	331	302	349	13	2175
G13_ASP	8	343	277	395	33	2521
G13_651	3	329	318	345	7	2574
G13_652	2	319	291	346	15	2542
G13_654	3	298	266	318	14	2571
G13_655	1	300	—	—	—	2561
G13_656	3	279	227	315	24	2541
G13_657	3	331	323	338	4	2483
G13_658	2	343	333	354	6	2427
G13_659	3	245	232	258	7	2327
G13_Z7C_SWE	2	270	253	287	9	2297
G13_USP	6	294	247	359	31	2258
G13_Z4C_SWE	4	342	334	350	5	2206
G13_744	3	323	298	347	14	2210
G13_Z3B_SWE	3	333	308	351	12	2156
G13_Z4B_SWE	2	332	312	351	11	2214
G13_Z5A_SWE	3	276	240	301	17	2271
G13_Z5B_SWE	2	255	254	257	1	2226

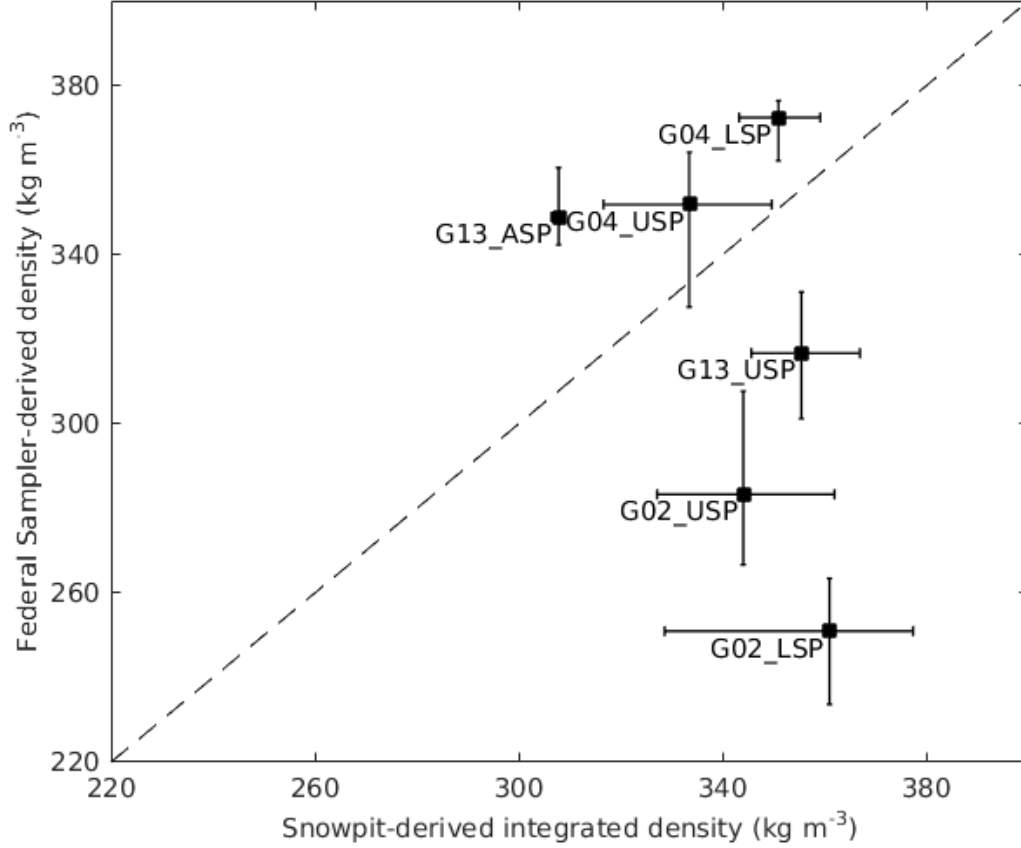


Figure 2: Comparison of integrated density estimated using wedge cutters in a snowpit and density estimated using Federal Sampler measurements for Glacier 4 (G04), Glacier 2 (G02) and Glacier 13 (G13). Error bars are minimum and maximum values for each estimate as reported in Table 2 and 3.

## 1.5 Density and elevation

A linear regression of density on topographic parameters is often used to interpolate density values between measurement locations (e.g. ???). Since the density measurement locations spanned a large portion of the elevation range for each glacier, the density values are regressed on elevation only. Regression slopes differ in both magnitude and sign between snowpit-derived and Federal Sampler-derived densities (Table 4).

Snowpit-derived density decreases with elevation on Glaciers 2 and 13 and does not change with elevation on Glacier 4 (Figure 4). The lower elevation sites on Glaciers 2 and 13 could have been melt affected. Warmer mean snow temperatures at the lower sites (Table 2) indicate that melt has occurred, which would increase snow density. Glacier 4 was probably not affect by melt, as snow temperatures are cool at all snowpit sites.

Opposite relationship are seen in the regression of Federal Sampler-derived densities and elevation (Figure 5). Density increases with elevation on Glacier 2 and there is no relationship with elevation on Glacier 4 and 13. There is a positive relationship between snow density and

Table 4: Summary of linear regressions between integrated density and elevation (m a.s.l.).

Location	Snowpit Regression			Fed. Sampler Regression		
	Equation	$R^2$	$n$	Equation	$R^2$	$n$
Glacier 4	$0.03z+274$	0.16	3	$-0.16z+714$	0.53	7
Glacier 2	$-0.14z+659$	0.75	4	$0.24z-282$	0.72	7
Glacier 13	$-0.20z+802$	$>0.99$	3	$0.12z+33$	0.21	17
All	$-0.12z+618$	0.50	10	$-0.14z+659$	0.75	31

snow depth (Section 1.2) and a positive relationship between snow depth and elevation (Figure 3) on Glacier 2, which results in a positive relationship between snow density and elevation. Since there is no significant relationship between snow depth and elevation on Glaciers 4 and 13, there is no relationship between snow density and elevation.

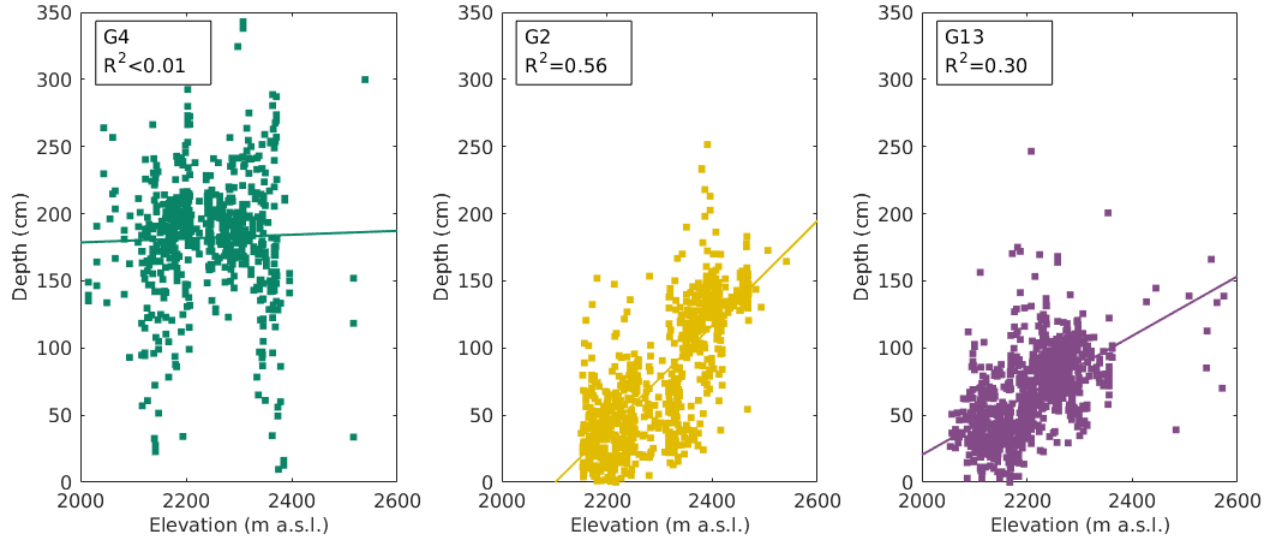


Figure 3: Relationship between measured snow depth and elevation at all sampling locations.



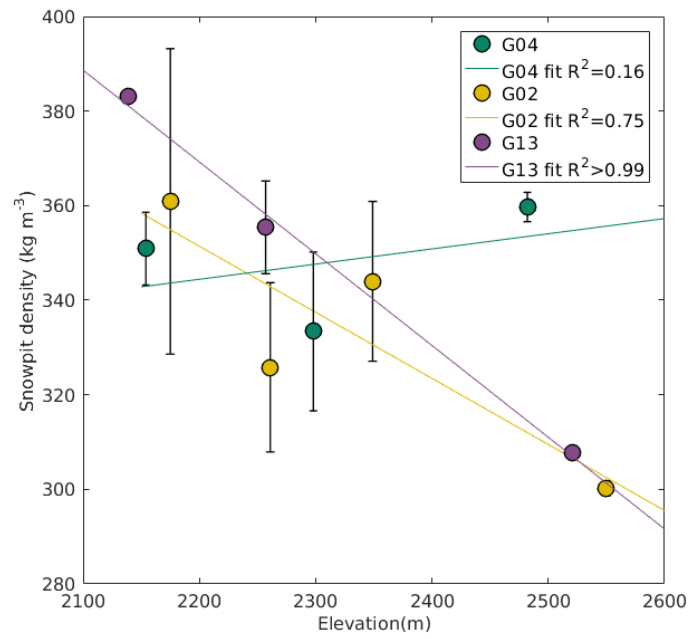


Figure 4: Relationship between snowpit-derived density and elevation for all study glaciers.

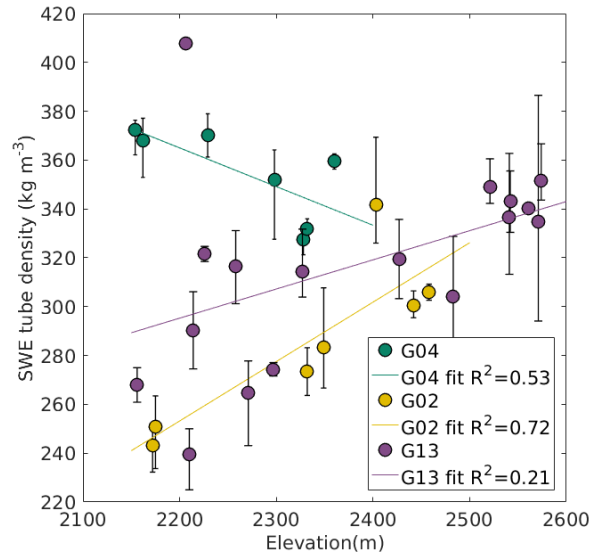


Figure 5: Relationship between Federal Sampler-derived density and elevation for all study glaciers.

## 2 Linear and curvilinear transect snow depth data

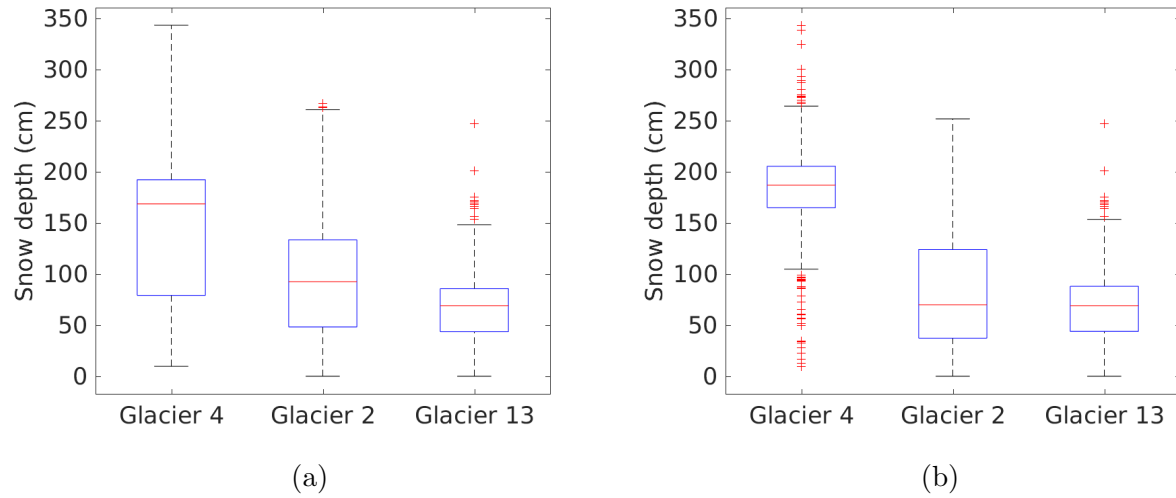


Figure 6: Boxplots of snow depth measured on study glaciers. All snow depth values shown in (a) and snow depth values only from transects (zigzag, snowpit and Federal Sampler measurements excluded) shown in (b). Red line indicates median, blue box shows first quartiles, bars indicate minimum and maximum values (excluding outliers), and red crosses show outliers, which are defined as being outside of the range of 1.5 times the quartiles (approximately  $\pm 2.7\sigma$ ).

Glacier 4 has the largest median and range of snow depth values, while Glacier 13 has the smallest (Figure 6). The boxplot of snow depth on Glacier 4 has different characteristics when only transect data is plotted (zigzag, snowpit and Federal Sampler measurements excluded). The range and IQR are smaller and there are significantly more points that are considered outliers.

### 3 Zigzag snow depth data

A comparison of measured snow depth for each zigzag is shown in Figure 7. The zigzags on Glacier 4 show minimal variability with a small range of values observed and few outliers. The mean depth is significantly larger at the highest elevation zigzag. Zigzags on Glacier 2 show more variability. The range on the middle elevation is the largest of all the zigzags measured and the highest zigzag has many outliers. The zigzags on Glacier 13 do not vary considerably in range, although the lower zigzags show a large number of outliers which may be a result of these locations being close to a supraglacial meltwater channel.

The depths measured in each zigzag are shown in Figures 9, 10, and 11. There is considerable variability both between zigzags and within each zigzag. For example, snow depths in G04.Z5B are more uniform than in G04.Z3A (Figure 9).

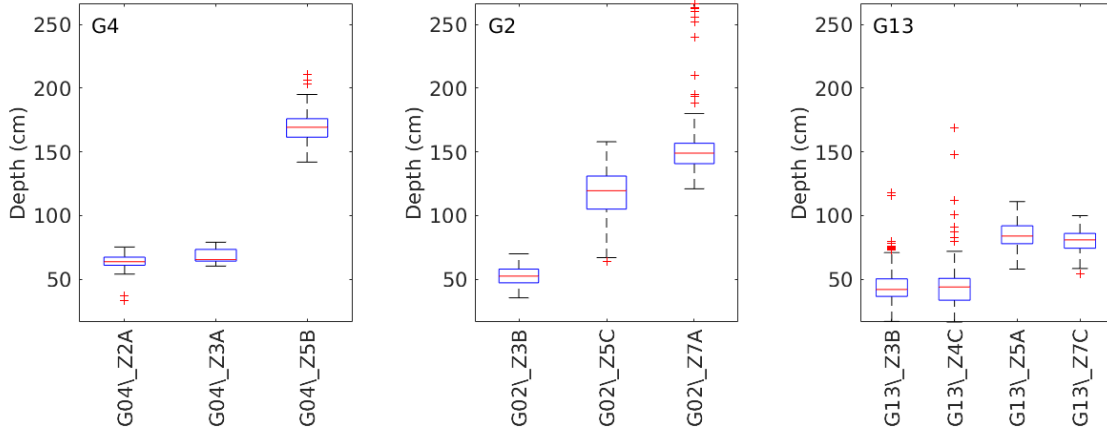


Figure 7: Boxplots of snow depth data measured at each zigzag location. See Figure 8 for locations of each zigzag.

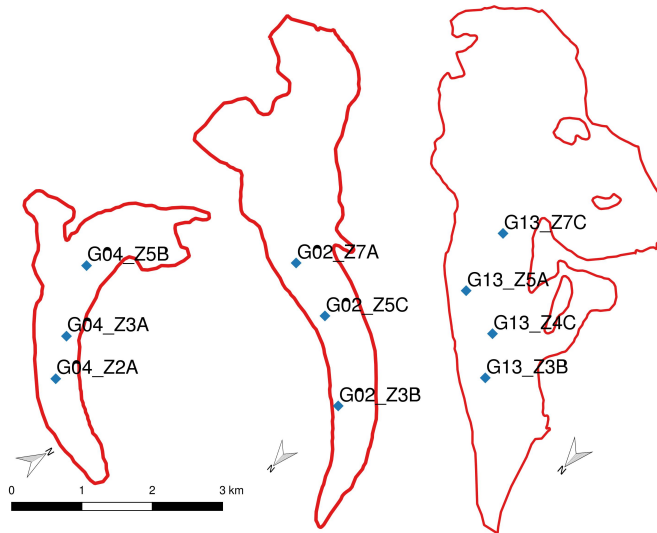


Figure 8: Map of zigzag locations on Glaciers 4, 2 and 13 (left to right).

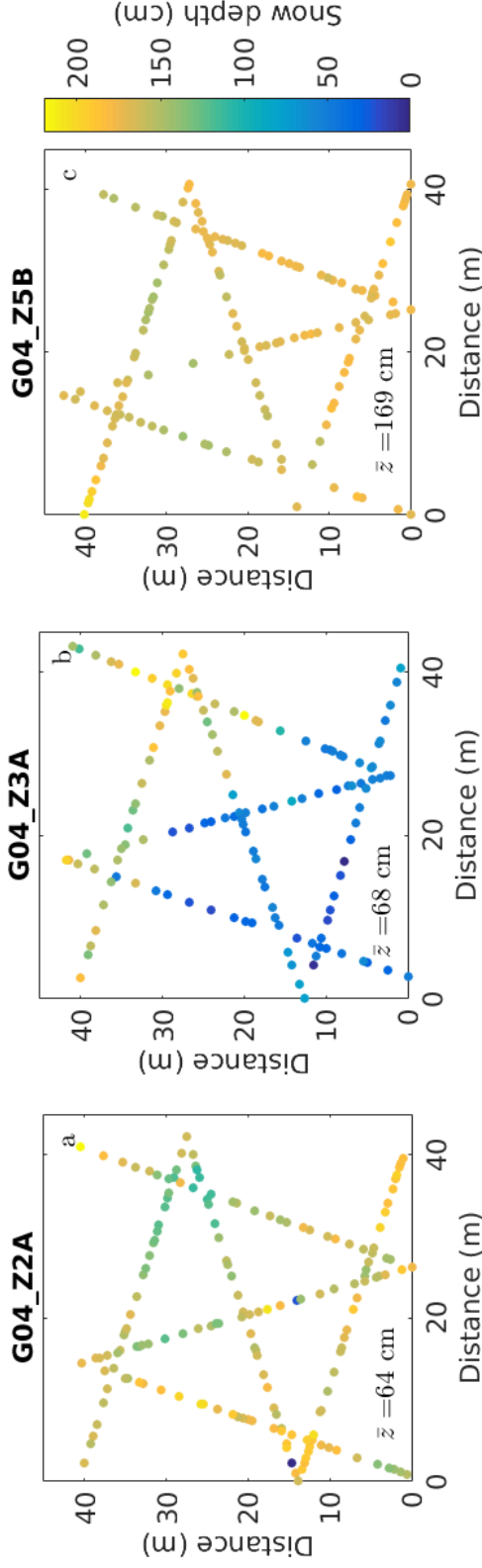


Figure 9: Snow depths measured in zigzags on Glacier 4. Mean depth ( $\bar{z}$ ) is also reported. Zigzag elevations (left to right) are 2162, 2229 and 2360 m a.s.l. See Figure 8 for locations of each zigzag.

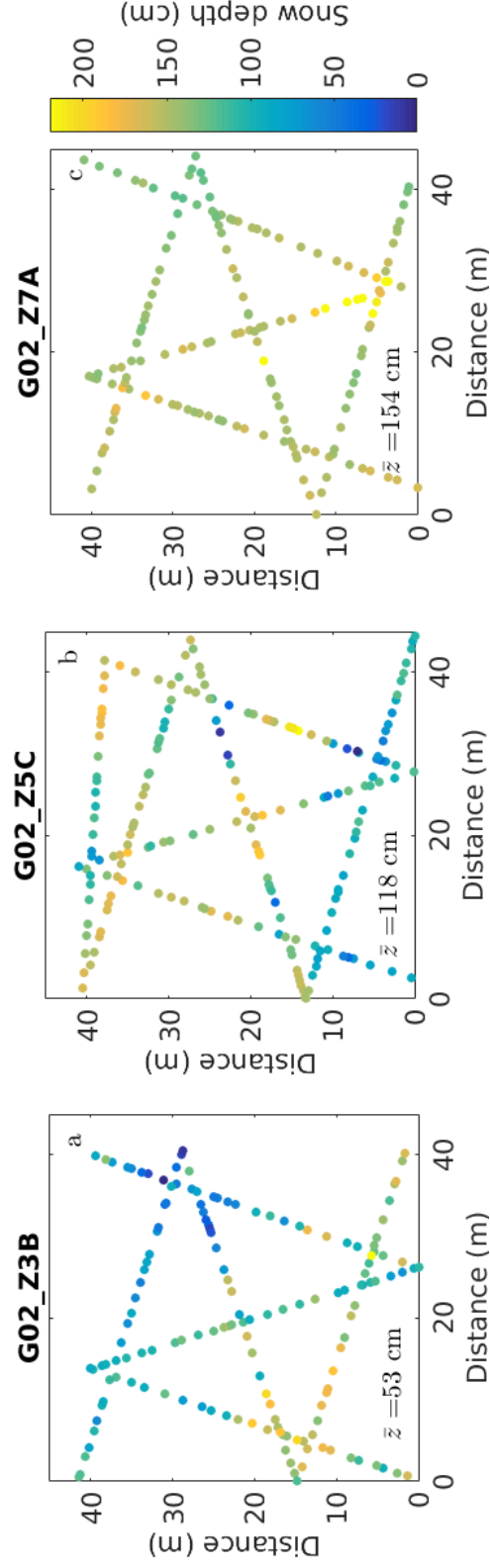


Figure 10: Snow depths measured in zigzags on Glacier 2. Mean depth ( $\bar{z}$ ) is also reported. Zigzag elevations (left to right) are 2172, 2332 and 2403 m a.s.l. See Figure 8 for locations of each zigzag.

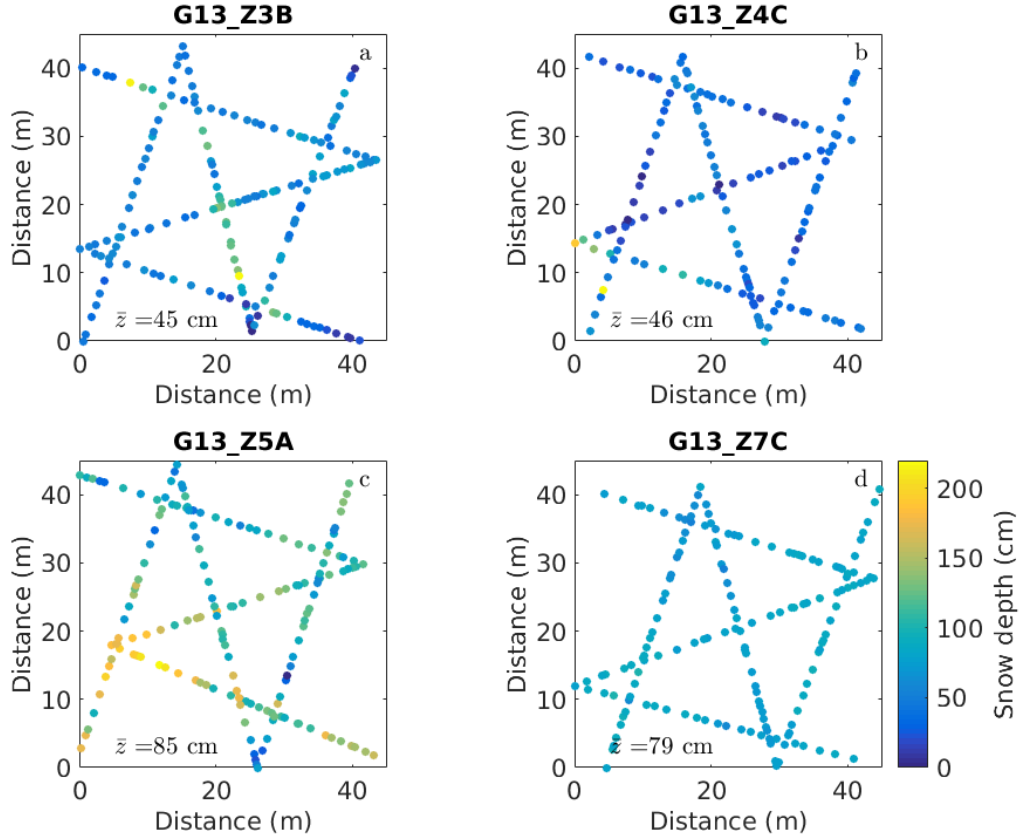


Figure 11: Snow depths measured in zigzags on Glacier 13. Mean depth ( $\bar{z}$ ) is also reported. Zigzag elevations (a-d) are 2156, 2206, 2271 and 2297 m a.s.l. See Figure 8 for locations of each zigzag.

## 4 Snow water equivalent (SWE)

Snow water equivalent (SWE) at sampling locations is estimated using eight density options (Section ??). Estimates of SWE on each glacier are significantly different (Figure 12). Glacier 4 has two main groups of SWE estimates with a number of estimates that overlap (belong to group A and C). The estimate calculated using density F1 has a lower mean than the remaining estimates. Glacier 2 has four different grouping of SWE estimates but all estimates belong to multiple groups so there is no one estimate that differs from the rest. SWE estimates on Glacier 13 found using Federal Sampler-derived densities (Group B) have a higher mean SWE than those found using snowpit-derived densities (Groups A, C and D). The percent difference between the means of the SWE estimates are 12%, 18% and 19% for Glacier 4, 2 and 13, respectively.

Density option 3 (Figures 17 and 18), which uses a linear regression of density with elevation, is used in this study to examine how a regression based on topography could affect SWE estimates. Despite opposite relationships between density and elevation for Federal Sampler-derived densities and snowpit-derived densities (Table 4), the SWE estimates do

not differ significantly for Glaciers 4 and 2. On Glacier 13, these two SWE estimates do differ but all SWE estimates with density F differ from SWE estimates with density S. This systematic difference is perhaps a result of undersampling by the Federal Sampler on Glacier 13. Undersampling could have occurred because a considerable portion of the snowpack had undergone recent melt and snow depths were generally shallow, resulting in snow falling out of the sampling tube.

For all density options, SWE is highest on Glacier 4 and lowest on Glacier 13. Glacier 4 also shows considerable SWE variability within the basin, with both high and low values along a single transect (Figures 13 to 20). The lower, left side of Glacier 2 has low SWE with visible variability along transects. During field data collection, this area was observed to have dune-like ice features ( $\sim 2$  m) with alternating bare ice and wind-deposited snow patches.

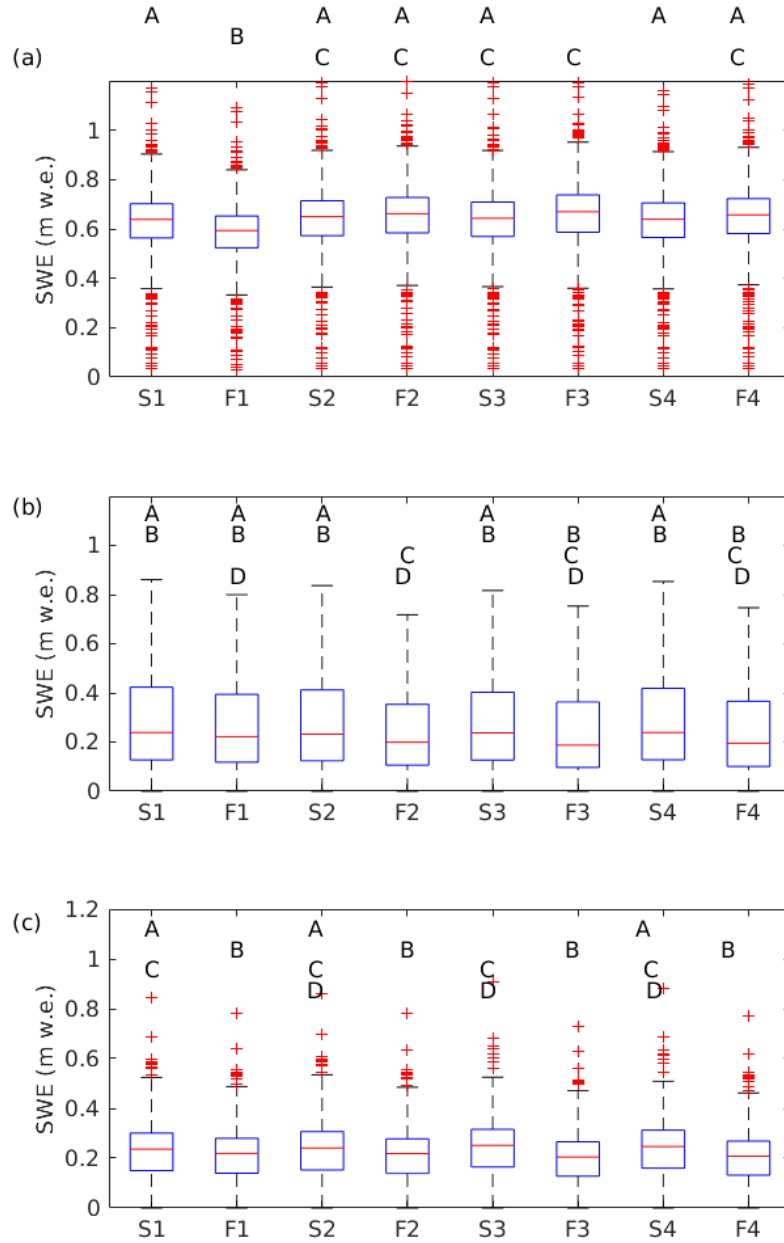


Figure 12: Boxplots of estimated SWE at sampling locations for Glacier 4 (a), Glacier 2 (b) and Glacier 13 (c). The density options using snowpit (S) or Federal Sampler (F) derived densities are mean from all glaciers (1), mean for individual glaciers (2), elevation regression (3) and inverse-distance weighting (4). SWE estimations using various density options were tested for differences using ANOVA ( $p < 0.05$ ). SWE estimates that were not significantly different for each glacier are labelled with the same letter (e.g. all estimates with A on Glacier 4 are significant different than all estimates with B).

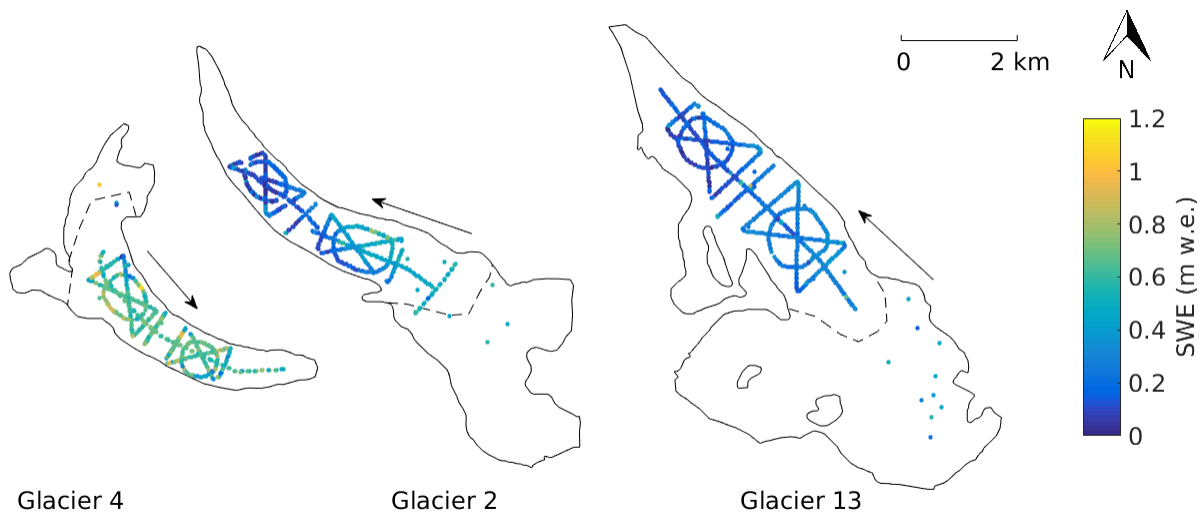


Figure 13: Estimated snow water equivalent (SWE) at measurement locations. Density was taken to be the mean value of all snowpit-derived densities from all glaciers (S1). Arrows show ice-flow direction and dashed lines show approximate ELA. Note that the individual measurement locations overlap on the figure.

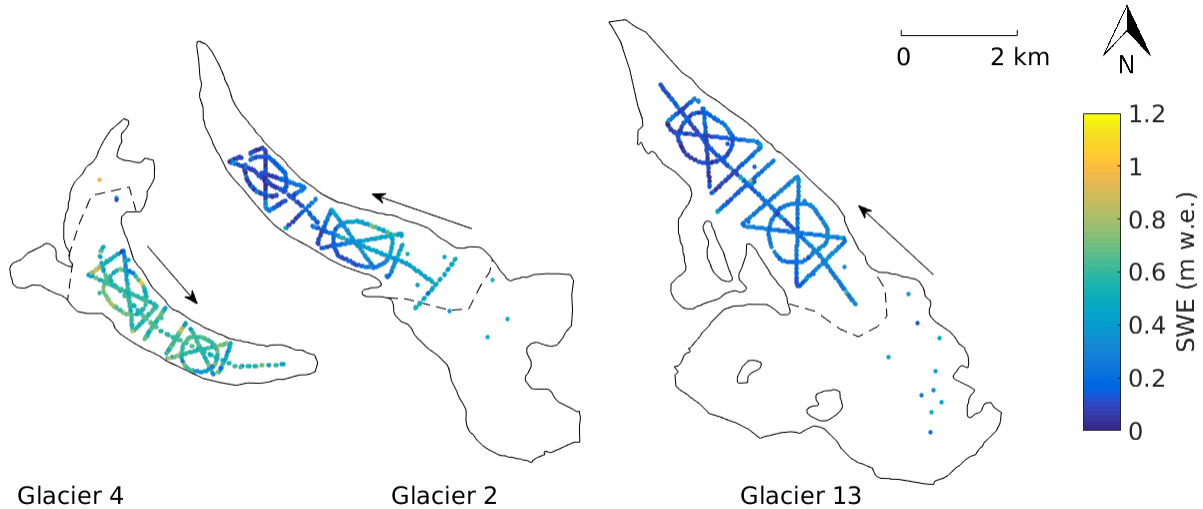


Figure 14: Estimated snow water equivalent (SWE) at measurement locations. Density was taken to be the mean value of all Federal Sampler-derived densities from all glaciers (F1). Arrows show ice-flow direction and dashed lines show approximate ELA. Note that the individual measurement locations overlap on the figure.



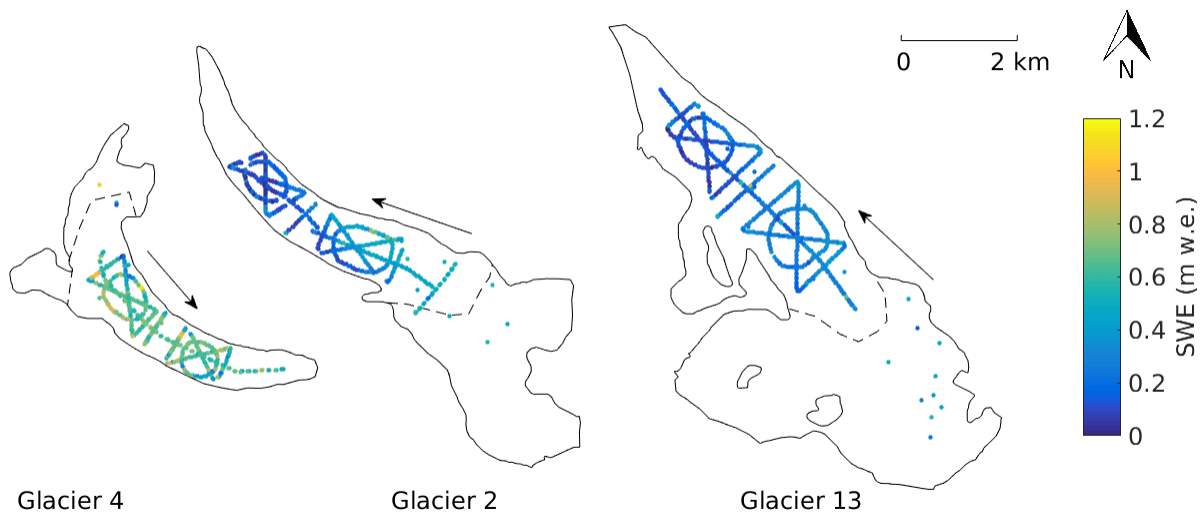


Figure 15: Estimated snow water equivalent (SWE) at measurement locations. Density for each glacier was taken to be the mean value of snowpit-derived densities from that glacier (S2). Arrows show ice-flow direction and dashed lines show approximate ELA. Note that the individual measurement locations overlap on the figure.

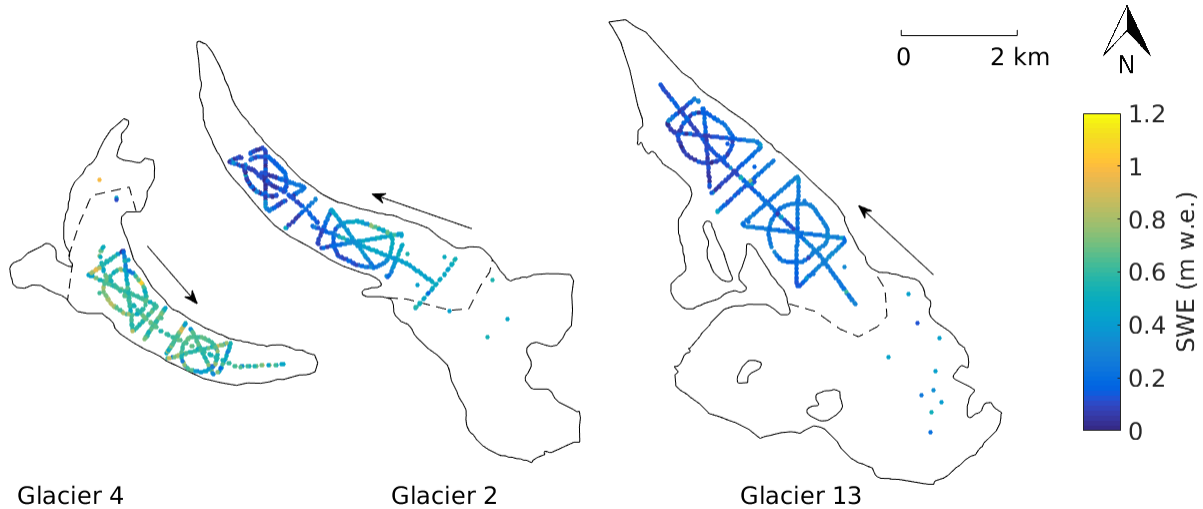


Figure 16: Estimated snow water equivalent (SWE) at measurement locations. Density for each glacier was taken to be the mean value of Federal Sampler-derived densities from that glacier (F2). Arrows show ice-flow direction and dashed lines show approximate ELA. Note that the individual measurement locations overlap on the figure.

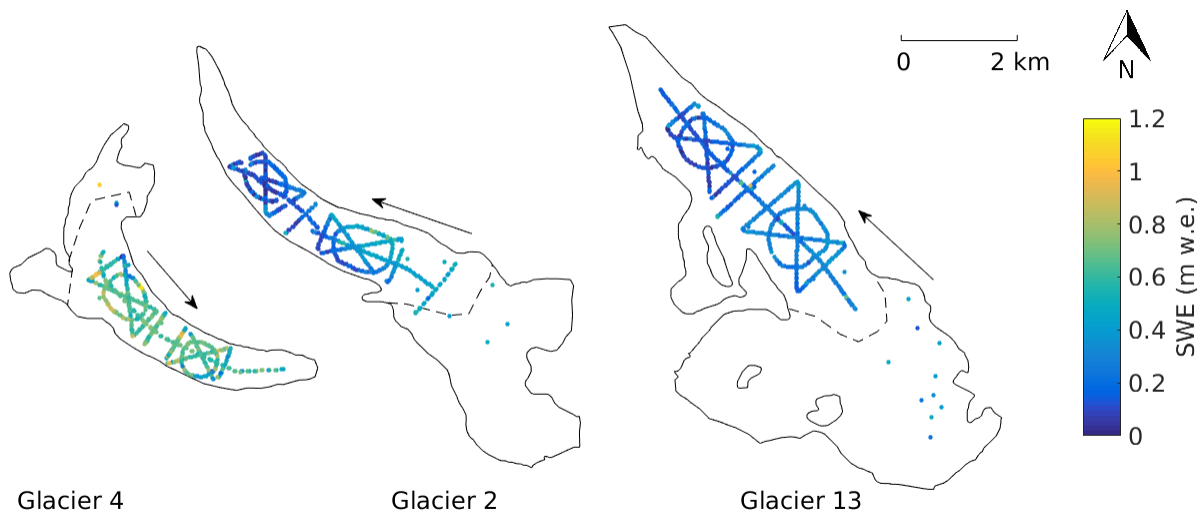


Figure 17: Estimated snow water equivalent (SWE) at measurement locations. Density was determined by using a linear fit between snowpit-derived density and elevation for each glacier (S3). Arrows show ice-flow direction and dashed lines show approximate ELA. Note that the individual measurement locations overlap on the figure.

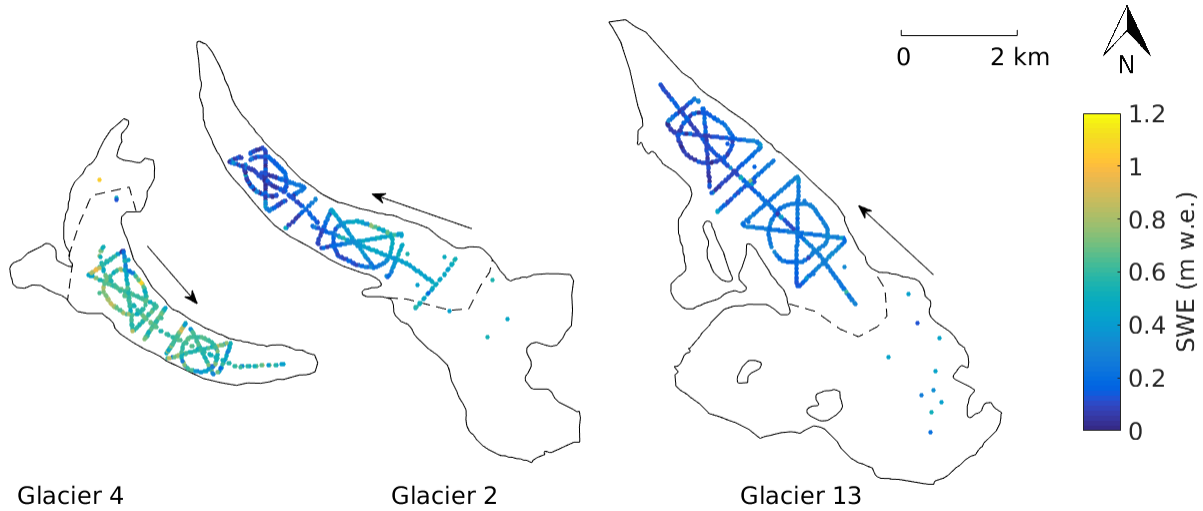


Figure 18: Estimated snow water equivalent (SWE) at measurement locations. Density was determined by using a linear fit between Federal Sampler-derived density and elevation for each glacier (F3). Arrows show ice-flow direction and dashed lines show approximate ELA. Note that the individual measurement locations overlap on the figure.

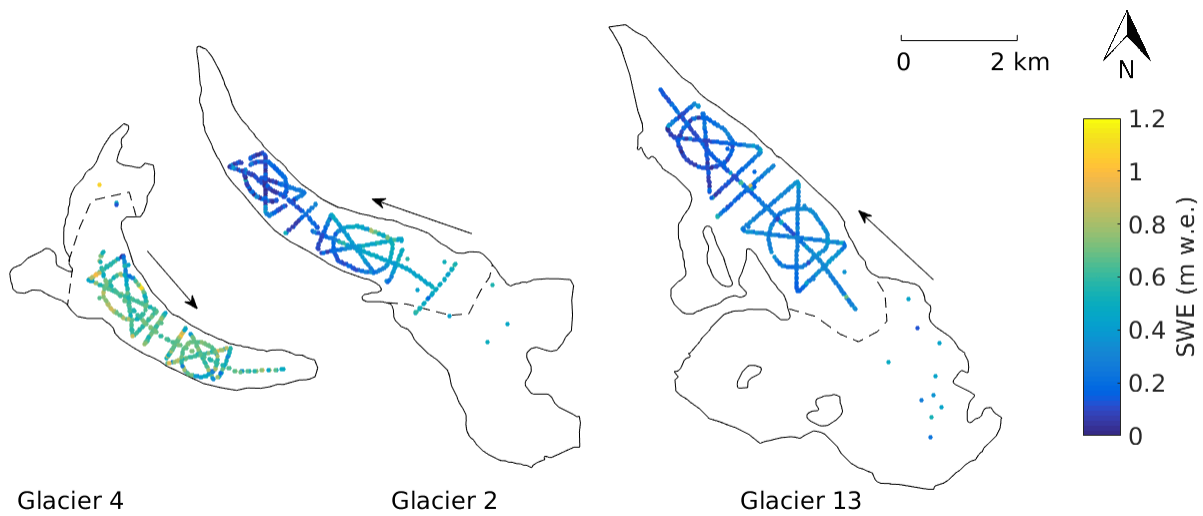


Figure 19: Estimated snow water equivalent (SWE) at measurement locations. Density was calculated using inverse distance weighting using all snowpit-derived densities (S4). Arrows show ice-flow direction and dashed lines show approximate ELA. Note that the individual measurement locations overlap on the figure.

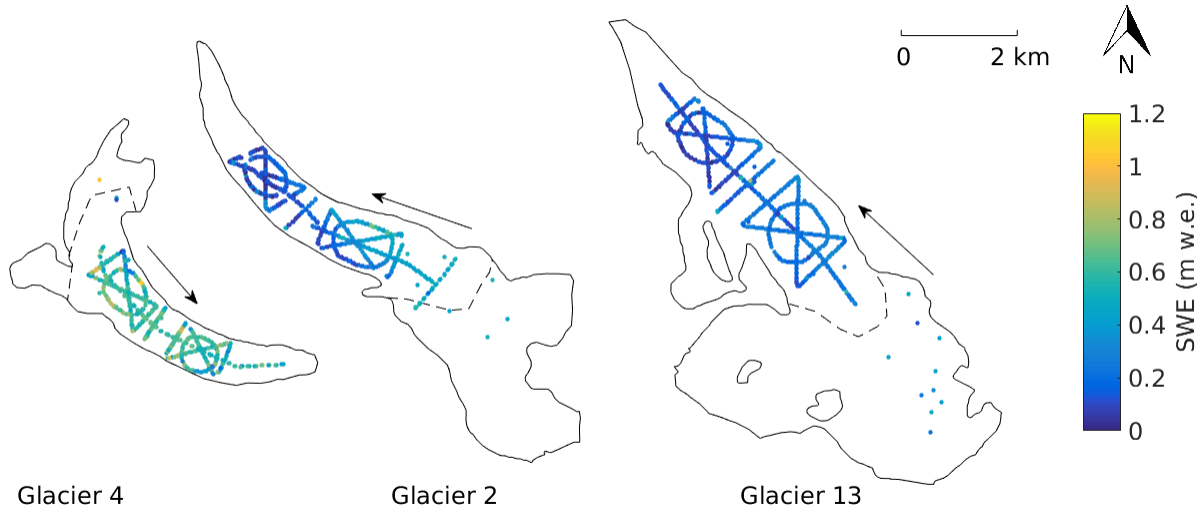


Figure 20: Estimated snow water equivalent (SWE) at measurement locations. Density was calculated using inverse distance weighting using all snowpit-derived densities (F4). Arrows show ice-flow direction and dashed lines show approximate ELA. Note that the individual measurement locations overlap on the figure.