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Estimating winter balance and its uncertainty from direct

measurements of snow depth and density on alpine glaciers

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ABSTRACT. Accurately estimating winter surface mass balance on glaciers is central to assessing glacier health and predicting glacier runoff. However, measuring and modelling snow distribution is inherently difficult in mountainous terrain. Here we explore rigorous statistical methods of estimating winter balance and its uncertainty from multiscale measurements of snow depth and density. In May 2016 we collected over 9000 manual measurements of snow depth across three glaciers in the St. Elias Mountains, Yukon, Canada. Linear regression, combined with cross correlation and Bayesian model averaging, as well as ordinary kriging are used to interpolate pointscale values to glacier-wide estimates of winter balance. Elevation and a windredistribution parameter exhibit the highest correlations with winter balance, but the relationship varies considerably between glaciers. A Monte Carlo analysis reveals that the interpolation itself introduces more uncertainty than the assignment of snow density or the representation of grid-scale variability. For our study glaciers, the winter balance uncertainty from all assessed sources ranges from $0.03\,\mathrm{m\,w.e.}$ (8%) to $0.15\,\mathrm{m\,w.e.}$ (54%). Despite the challenges

associated with estimating winter balance, our results are consistent with a regional-scale winter-balance gradient.

28 INTRODUCTION

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Winter surface mass balance, or "winter balance", is the net accumulation and ablation of snow over the 29 winter season (Cogley and others, 2011), which constitutes glacier mass input. Winter balance (B_{w}) is half 30 of the seasonally resolved mass balance, initializes summer ablation conditions and must be estimated to 31 simulate energy and mass exchange between the land and atmosphere (e.g. Hock, 2005; Réveillet and others, 32 2016). Effectively representing the spatial distribution of snow on glaciers is also central to monitoring surface 33 runoff and its downstream effects (e.g. Clark and others, 2011). 34 Winter balance (WB) is notoriously difficult to estimate (e.g. Dadić and others, 2010; Cogley and others, 2011) 35 Snow distribution in alpine regions is highly variable with short correlation length scales (e.g. Anderton 36 and others, 2004; Egli and others, 2011; Grünewald and others, 2010; Helbig and van Herwijnen, 2017; 37 López-Moreno and others, 2011, 2013; Machguth and others, 2006; Marshall and others, 2006) and 38 is influenced by dynamic interactions between the atmosphere and complex topography, operating on 39 multiple spatial and temporal scales (e.g. Barry, 1992; Liston and Elder, 2006; Clark and others, 2011) 40 (e.g. Barry, 1992; Liston and Elder, 2006; Clark and others, 2011; Scipión and others, 2013). 41 Simultaneously extensive, high resolution and accurate snow distribution measurements on glaciers 42 are therefore difficult to obtain (e.g. Cogley and others, 2011; McGrath and others, 2015). Physically 43 based models are acquire (e.g. Cogley and others, 2011; McGrath and others, 2015) and obtaining such 44 measurements is further complicated by the inaccessibility of many glacierized regions during the winter. 45 Use of physically based models to estimate winter balance is computationally intensive and require-requires 46 detailed meteorological data to drive them the models (Dadić and others, 2010). As a result, there is 47 significant uncertainty in estimates of winter balance, thus limiting the ability of models to represent current 48 49 and projected glacier conditions. Studies that have focused on obtaining detailed estimates of WB-Bw have used a wide range of observational 50 techniques, including direct measurement of snow depth and density (e.g. Cullen and others, 2017), lidar or 51 photogrammerty photogrammetry (e.g. Sold and others, 2013) and ground-penetrating radar (e.g. Machguth 52 and others, 2006; Gusmeroli and others, 2014; McGrath and others, 2015). Spatial coverage of direct

measurements is generally limited and often comprises an elevation transect along the glacier centreline

(e.g. Kaser and others, 2003). Measurements are often-typically interpolated using linear regression on only 55 a few topographic parameters (e.g. MacDougall and Flowers, 2011), with elevation being the most common. 56 Other established techniques include hand contouring (e.g. Tangborn and others, 1975), kriging (e.g. Hock 57 and Jensen, 1999) and attributing measured winter balance values to elevation bands (e.g. Thibert and 58 others, 2008). Physical snow models have been used to estimate spatial patterns of winter balance (e.g. 59 60 Mott and others, 2008; Schuler and others, 2008; Dadić and others, 2010), but availability of the required meteorological data generally prohibits their widespread application. Error analysis is rarely undertaken and 61 few studies have thoroughly investigated uncertainty in spatially distributed estimates of winter balance (c.f. 62 Schuler and others, 2008). 63 More sophisticated snow-survey designs and statistical models of snow distribution are widely used 64 in the field of snow science. Surveys described in the snow science literature are generally spatially 65 extensive and designed to measure snow depth and density throughout a basin, ensuring that all terrain 66 types are sampled. A wide array of measurement interpolation methods are used, including linear 67 (e.g. López-Moreno and others, 2010) and non-linear regressions (e.g. Molotch and others, 2005) that 68 include numerous terrain parameters, as well as geospatial interpolation (e.g. Erxleben and others, 2002) 69 (e.g. Erxleben and others, 2002; Cullen and others, 2017) including various forms of kriging. Different interpolation methods are also combined; for example, regression kriging (see Supplementary Material) adds 71 kriged residuals to a field obtained with linear regression (e.g. Balk and Elder, 2000). Physical snow models 72 such as SnowTran-3D (Liston and Sturm, 1998), Alpine3D (Lehning and others, 2006) and SnowDrift3D (Schneiderbauer and Prokop, 2011) are widely used, and errors in estimating snow distribution have been 74 examined from theoretical (e.g. Trujillo and Lehning, 2015) and applied perspectives (e.g. Turcan and Loijens, 75 1975; Woo and Marsh, 1978; Deems and Painter, 2006). 76 The goals of this study are to (1) critically examine methods of converting direct snow depth and density 77 measurements to distributed estimates of winter balance; and (2) identify sources of uncertainty, evaluate 78 their magnitude and assess their combined contribution to uncertainty in glacier-wide winter balance. We 79 focus on commonly applied, low-complexity methods of measuring and estimating winter balance in the 80 interest of making our results broadly applicable. 81

$_{ m 2}$ STUDY SITE

The St. Elias Mountains (Fig. 1a) rise sharply from the Pacific Ocean, creating a significant climatic gradient between coastal maritime conditions, generated by Aleutian–Gulf of Alaska low-pressure

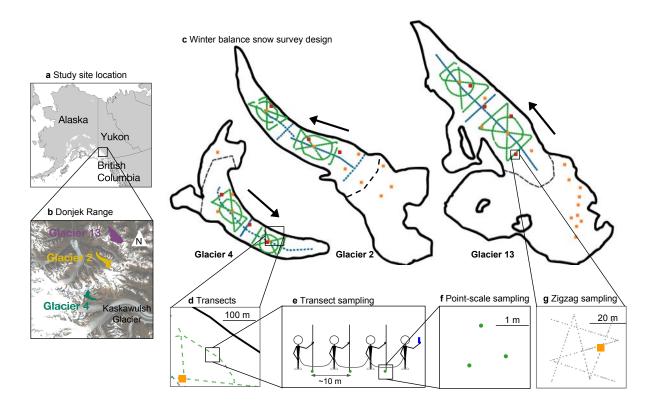


Fig. 1. Study area location and sampling design for Glaciers 4, 2 and 13. (a) Study region in the Donjek Range of the St. Elias Mountains of Yukon, Canada. (b) Study glaciers located along a southwest-northeast transect through the Donjek Range. The local topographic divide is shown as a dashed line. Imagery from Landsat8 (5 September 2013, data available from the U.S. Geological Survey). (c) Details of the snow-survey sampling design, with centreline and transverse transects (blue dots), hourglass and circle designs (green dots) and locations of snow density measurements (orange squares). Arrows indicate ice-flow directions. Approximate location of ELA on each glacier is shown as a black dashed line. (d) Close up of linear and curvilinear transects. (e) Configuration of navigator and observers. (f) Point-scale snow-depth sampling. (g) Linear-random snow-depth measurements in 'zigzag' design (greey red dots) with one density measurement (orange square) per zigzag.

systems, and interior continental conditions, driven by the Yukon-Mackenzie high-pressure system 85 (Taylor-Barge, 1969). The boundary between the two climatic zones is generally aligned with the divide 86 87 between the Hubbard and Kaskawulsh Glaciers, approximately 130 km from the coast. Research on snow distribution and glacier mass balance in this area is limited. A series of research programs, including 88 Project "Snow Cornice" and the Icefield Ranges Research Project, were operational in the 1950s and 89 60s (Wood, 1948; Danby and others, 2003) and in the last 30 years, there have been a few long-term 90 studies on selected alpine glaciers (e.g. Clarke, 2014) as well as several regional studies of glacier mass 91 balance and dynamics (e.g. Arendt and others, 2008; Burgess and others, 2013; Waechter and others, 2015) 92

Table 1. Physical characteristics of the study glaciers and May 2016 winter-balance survey details, including number of snow-depth measurement locations along transects (n_T) , total length of transects (d_T) , number of combined snow pit and Federal Sampler density measurement locations (n_{ρ}) and number of zigzag surveys (n_{zz}) .

	Location	Location	Elevation (m a.s.l)			Slope ($^{\circ}$)	Area	
	UTM Zone	7 UTM Zone 7	Mean	Range	ELA	Mean	$n_{\mathrm{T}} \; d_{\mathrm{T}}$ ((km 2) $n_{ ho} \; n_{\mathrm{zz}}$	
$\mathrm{height} \mathbf{Glacier} \ 4$	$595470 \; \mathrm{E}$	6740730 N	2344	1958-2809	~ 2500	12.8	3.8 4 7 May 2016 649 13.1 10 3	
Glacier 2	601160 E	6753785 N	2495	1899-3103	~ 2500	13.0	7.0 8 11 May 2016 762 13.6 11 3	
Glacier 13	604602 E	6763400 N	2428	1923-3067	\sim 2380	13.4	12.6	

(e.g. Arendt and others, 2008; Berthier and others, 2010; Burgess and others, 2013; Waechter and others, 2015)

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We carried out winter balance surveys on three unnamed glaciers in the Donjek Range of the St. Elias 95 Mountains. The Donjek Range is located approximately 40 km to the east of the regional mountain divide and 96 has an area of about $30 \times 30 \,\mathrm{km^2}$. Glacier 4, Glacier 2 and Glacier 13 (labelling adopted from Crompton and 97 98 Flowers (2016)) are located along a southwest-northeast-southwest-northeast transect through the range (Fig. 1b, Table 1). These small alpine glaciers are generally oriented southeast-northwest outheast-northwest, with 99

Glacier 4 having a predominantly southeast aspect and Glaciers 2 and 13 have generally northwest aspects.

The glaciers are situated in valleys with steep walls and have simple geometries. Based on a detailed study of

Glacier 2 (Wilson and others, 2013) and related theoretical modelling (Wilson and Flowers, 2013) we suspect

all of the study glaciers to be polythermal. 103

METHODS 104

Estimating glacier-wide winter balance $(B_{\rm w})$ involves transforming measurements of snow depth and density 105 into values of winter balance distributed across a defined grid (b_w) . We do this in four steps. (1) Obtain direct 106 measurements of snow depth and density in the field. (2) Assign density values to all depth-measurement 107 108 locations to calculate point-scale values of \overline{WB} b_w at each location. (Winter balance, measured in units of metres water equivalent (m w.e.), can be estimated as the product of snow depth and depth-averaged density. 109 (3) Average all point-scale values of b_{w} within each gridcell of a digital elevation model (DEM) to obtain 110 the gricell-averaged WB gridcell-averaged b_{w} . (4) Interpolate and extrapolate these gridcell-averaged WB b_{w} 111 values to obtain estimates of WB (in m w.e.) in b_w in each gridcell across the domain. B_w is then calculated 112 by taking the average of all gridcell-averaged $b_{\rm w}$ values for each glacier. For brevity, we refer to these four 113

Table 2. Details of the May 2016 winter-balance survey, including number of snow-depth measurement locations along transects $(n_{\rm T})$, total length of transects $(d_{\rm T})$, number of combined snow pit and Federal Sampler density measurement locations (n_{ρ}) , number of zigzag surveys (n_{zz}) , number (as percent of total number of gridcells, and of the number of gridcells in the ablation area) of gridcells sampled $(n_{\rm S})$ and the elevation range (as percent of total elevations range and of ablation-area elevation range).

	$\underbrace{\mathbf{Date}}_{}$	$n_{ m T}$	d_{T} (km)	$\widetilde{n}_{\mathcal{R}}$	$n_{ extsf{zz}}$	$n_{ m S}$	Elevation range (ma.s.l.)
Glacier 4	4–7 May 2016	<u>649</u>	13.1	₹~	$\frac{3}{\sim}$	295	2015-2539
						(12%, 21%)	(62%, 97%)
Glacier 2	<u>8–11 May 2016</u>	762	13.6	₹~	<u>3</u>	353	2151-2541
						(8%, 14%)	(32%, 47%)
Glacier 13	12–15 May 2016	941	18.1	20 - <u>19</u>	4	468	2054 - 2574
						(6%, 14%)	(45%, 62%)

steps as (1) field measurements, (2) density assignment, (3) gridcell-averaged \overline{WB} b_{w} and (4) distributed $\overline{WB}b_{w}$. Detailed methodology for each step is outlined below. We use the SPIRIT SPOT-5 DEM (40×40 m) from 2005 (Korona and others, 2009) throughout this study.

Field measurements

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Our sampling campaign involved four people and occurred between 5-15 May 2016, which falls within 118 the period of historical peak snow accumulation in southwestern Yukon (Yukon Snow Survey Bulletin and 119 Water Supply Forecast, May 1, 2016). Snow depth is generally accepted to be more variable than density 120 (Elder and others, 1991; Clark and others, 2011; López-Moreno and others, 2013) so we chose a sampling 121 design that resulted in a high ratio (\sim 55:1) of snow depth to density measurements. In total, we collected 122 more than 9000 snow-depth measurements and more than 100 density measurements throughout the study 123 area (Table 1). 124 During the field campaign there were two small accumulation events. The first, on 6 May 2016, also involved 125 126 high winds so accumulation could not be determined. The second, on 10 May 2016, resulted in 0.01 m w.e accumulation measured at one location on Glacier 2. Assuming both accumulation events contributed a 127 uniform $0.01 \,\mathrm{m}$ w.e accumulation to all study glaciers then our survey did not capture $\sim 3\%$ and $\sim 2\%$ of 128 estimated $B_{\rm w}$ on Glaciers 4 and 2, respectively. We therefore assume that these accumulation events were 129 negligible and apply no correction. Positive temperatures and clear skies occurred between 11–16 May 2016, 130 which we suspect resulted in melt occurring on Glacier 13. The snow in the lower part of the ablation area 131

- of Glacier 13 was isothermal and showed clear signs of melt and metamorphosis. The total amount of melt
- during the study period was estimated using a degree-day model and found to be small ($\leq 0.01 \,\mathrm{m}$ w.e., see
- 134 Supplementary Material) so no corrections were made.
- 135 Sampling design
- 136 The snow surveys were designed to capture variability in snow depth at regional, basin, gridcell and point
- 137 scales (Clark and others, 2011). To capture variability at the regional scale we chose three glaciers along
- a transect aligned with the dominant precipitation gradient (Fig. 1b) (Taylor-Barge, 1969). To account for
- basin-scale variability, snow depth was measured along linear and curvilinear transects on each glacier (Fig.
- 140 1c) with a sample spacing of 10–60 m (Fig. 1d). Sample spacing was constrained by protocols for safe glacier
- travel, while survey scope was constrained by the need to complete all surveys within the period of peak
- accumulation. We selected centreline and transverse transects as the most commonly used survey designs
- in winter balance studies (e.g. Kaser and others, 2003; Machguth and others, 2006) as well as an hourglass
- pattern with an inscribed circle, which allows for sampling in multiple directions and easy travel (personal
- 145 communication from C. Parr, 2016). To capture variability at the grid scale, we densely sampled up to
- four gridcells on each glacier using a linear-random sampling design (Shea and Jamieson, 2010) we term a
- 'zigzag'. To capture point-scale variability, each observer made 3-4 depth measurements within ~ 1 m (Fig.
- 148 1ef) at each transect measurement location. In total, we collected more than 9000 snow-depth measurements
- 149 throughout the study area (Table 1).
- 150 Snow depth: transects
- 151 Winter balance can be estimated as the product of snow depth and depth-averaged
- 152 density. Snow depth is generally accepted to be more variable than density
- (Elder and others, 1991; Clark and others, 2011; López-Moreno and others, 2013) so we chose a sampling
- 154 design that resulted in a high ratio (~55:1) of snow depth to density measurements. Our sampling campaign
- involved four people and occurred between 5-15 May 2016, which falls within the period of historical peak
- 156 snow accumulation in southwestern Yukon (Yukon Snow Survey Bulletin and Water Supply Forecast, May
- 157 1, 2016). While roped-up for glacier travel with fixed distances between observers, the lead observer used a
- 158 single-frequency GPS unit (Garmin GPSMAP 64s) to navigate between predefined transect measurement
- locations (Fig. 1e). The remaining three observers used 3.2 m graduated aluminum avalanche probes to make
- snow-depth measurements (Kinar and Pomeroy, 2015). The locations of each set of depth measurements,
- 161 made by the second, third and fourth observers, are estimated using the recorded location of the first

- observer, the approximate distance between observers and the direction of travel. The 3-4 point-scale depth
- measurements are averaged to obtain a single depth measurement at each transect measurement location.
- When considering snow variability at the point scale as a source of uncertainty in snow depth measurements,
- we find that the mean standard deviation of point-scale snow depth measurements is <7% of the mean snow
- 166 depth for all study glaciers.
- 167 Snow-depth sampling was concentrated in the ablation area to ensure that only snow from the current
- accumulation season was measured. The boundary between snow and firn in the accumulation area can be
- difficult to detect and often misinterpreted, especially when using an avalanche probe (Grünewald and others,
- 2010; Sold and others, 2013). We intended to use a firn corer to measure winter balance in the accumulation
- area, but cold snow combined with positive air temperatures led to cores being unrecoverable. Successful
- snow depth and density measurements within the accumulation area were made either in snow pits or using
- a Federal Sampler (described below) to unambiguously identify the snow-firn transition.
- 174 Snow depth: ziqzaqs
- 175 To capture snow-depth variability within a single DEM gridcell, we implemented a linear-random zigzag
- 176 sampling design (Shea and Jamieson, 2010). We measured depth at random intervals of 0.3–3.0 m along two
- 177 'Z'-shaped patterns (Shea and Jamieson, 2010), resulting in 135–191 measurements per zigzag, within three
- to four $40 \times 40 \times 40$ m gridcells (Fig. 1g) per glacier. Random intervals were machine-generated from a
- uniform distribution in sufficient numbers that each survey was unique. Zigzag locations were randomly
- 180 chosen within the upper, middle and lower regions of the ablation area of each glacier. A fourth zigzag was
- 181 measured Extra time in the field allowed us to measure a fourth zigzag on Glacier 13 in the central ablation
- area at \sim 2200 m a.s.l.
- 183 Snow density
- 184 Snow density was measured using a Snowmetrics wedge cutter in three snow pits on each glacier, as
- 185 well as with a Geo Scientific Ltd. metric Federal Sampler. Within the snow pits (SP), we measured
- a vertical density profile (in $\frac{5}{10}$ cm increments) with the $\frac{5 \times 10 \times 10}{5 \times 5} \times \frac{5}{10}$ cm wedge-shaped
- 187 cutter (250 cm³) and a Presola 1000 g spring scale (e.g. Gray and Male, 1981; Fierz and others, 2009)
- 188 (e.g. Gray and Male, 1981; Fierz and others, 2009; Kinar and Pomeroy, 2015). Wedge-cutter error is ap-
- proximately $\pm 6\%$ (e.g. Proksch and others, 2016; Carroll, 1977). Uncertainty in estimating density from
- 190 snow-pit SP measurements also stems from incorrect assignment of density to layers that cannot be sampled
- 191 (e.g. ice lenses and hard layers). We attempt to quantify this uncertainty by varying estimated ice-layer

thickness by ± 1 cm ($\leq 100\%$) of the recorded thickness, ice layer density between 700 and $900 \,\mathrm{kg}\,\mathrm{m}^{-3}$ and 192 the density of layers identified as being too hard to sample (but not ice) between 600 and $700 \,\mathrm{kg}\,\mathrm{m}^{-3}$. 193 When considering all three sources of uncertainty, the range of integrated density values is always less than 194 15% of the reference density. Depth-averaged densities for shallow pits (<50 cm) that contain ice lenses are 195 particularly sensitive to changes in prescribed density and ice-lens thickness. 196 197 While snow pits SP provide the most accurate measure of snow density, digging and sampling a snow pit SP is time and labour intensive. Therefore, a Federal Snow Geo Scientific Ltd. metric Federal Sampler 198 (FS) (Clyde, 1932) with a 3.2–3.8 cm diameter sampling tube, which directly measures depth-integrated 199 snow-water equivalent, was used to augment the snow pit-SP measurements. A minimum of three Federal 200 Sampler-FS measurements were taken at each of 7–19 locations on each glacier and an additional eight 201 Federal Sampler-FS measurements were co-located with each snow pit profile two SP profiles for each glacier. 202 Measurements for which the snow core length inside the sampling tube was less than 90% of the snow depth 203 were discarded. Densities at each measurement location (eight at each snow pitSP, three elsewhere) were 204 then averaged, with the standard deviation taken to represent the uncertainty. 205 206 During the field campaign there were two small accumulation events. The first, on 6 May 2016, also involved high winds so accumulation could not be determined. The second, on 10 May 2016, resulted in 0.01 m w.e 207 accumulation measured at one location on Glacier 2. Positive temperatures and clear skies occurred between 208 11 16 May 2016, which we suspect resulted in melt occurring on Glacier 13. The snow in the lower part of 209 the ablation area of Glacier 13 was isothermal and showed clear signs of melt and metamorphosis. The total 210

made The mean standard deviation of FS-derived density was $\leq 4\%$ of the mean density for all glaciers.

amount of accumulation and melt during the study period could not be estimated so no corrections were

Density assignment

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Measured snow density must be interpolated or extrapolated to estimate point-scale winter balance by at each snow-depth sampling location. We employ four commonly used methods to interpolate and extrapolate density (Table 3): (1) calculate mean density over an entire mountain range (e.g. Cullen and others, 2017), (2) calculate mean density for each glacier (e.g. Elder and others, 1991; McGrath and others, 2015), (3) linear regression of density on elevation for each glacier (e.g. Elder and others, 1998; Molotch and others, 2005) and (4) calculate mean density using inverse-distance weighting (e.g. Molotch and others, 2005) for each glacier. Densities derived from snow-pit (SP) measurements and the Federal Sampler (FS) SP and

Table 3. Eight methods used to estimate snow density at unmeasured locations. Total number of resulting density values given in parentheses, with n_T the total number of snow-depth measurement locations along transects (Table 1).

Method	Source of	measured	Density assignment		
code	snow o	$\operatorname{lensity}$	method		
code	$Snow\ pit$	Federal	memod		
	Show pic	Sampler			
S1			Mean of measurements		
F1			across all glaciers (1)		
S2			Mean of measurements		
F2		•	for each glacier (3)		
S3			Regression of density on		
F3		•	elevation for each glacier (n_T)		
S4			Inverse distance weighted		
F4		•	mean for each glacier (n_T)		

221 FS measurements are treated separately, for reasons explained below, resulting in eight possible methods of 222 assigning density.

Gridcell-averaged winter balance

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We average one to six (mean of 2.1 measurements) point-scale values of WB within each 40×40 m- b_w within 224 each DEM gridcell to obtain the gricell-averaged \overline{WBb}_{w} . The locations of individual measurements have 225 uncertainty due to the error in the horizontal position given by the GPS unit and the estimation of observer 226 location based on the recorded GPS positions of the navigator. This location uncertainty could result in the 227 incorrect assignment of a point-scale WB-bw measurement to a particular gridcell. However, this source of 228 error is not further investigated because we assume that the uncertainty in gridcell-averaged WB resulting 229 from incorrect locations of point-scale $b_{\rm w}$ values is captured in the zigzag measurements uncertainty derived 230 231 from zigzag measurements, as described below. Uncertainty Error due to having multiple observers was also evaluated. There are is also evaluated by conducting an analysis of variance (ANOVA) of snow-depth 232 measurements along a transect (amounting to 23 hypothesis tests, one for each transect) and testing for 233 differences between observers. We find no significant differences between snow-depth measurements made by 234 observers along any transect (p>0.05), with the exception of the first transect on Glacier 4 (51 measurements). 235 , where snow depth measurements collected by one observer were, on average, greater than the snow depth 236

measurements taken by the other two observers (p<0.01). Since this was the first transect and the only one to show differences by observer, this difference can be considered an anomaly. We conclude that observer bias is not an important effect in this study and therefore apply no observer corrections to the data.

Distributed winter balance

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Gridcell-averaged values of \overline{WB} - b_w are interpolated and extrapolated across each glacier using linear 241 regression (LR) and simple kriging (SKordinary kriging (OK). The regression LR relates gridcell-averaged 242 243 WB and b_w to various topographic parameters, as this method. We use this method because it is simple and has precedent for success (e.g. McGrath and others, 2015). Instead of a basic regression standard LR however, 244 we use cross-validation and implemented in such a way as to prevent data overfitting, and employ model 245 averaging to test-allow for all combinations of the chosen topographic parameters. We compare the regression 246 approach with simple kriging (SK), a data-driven LR approach with conventional OK, an interpolation 247 method free of any physical interpretation (e.g. Hock and Jensen, 1999) physical interpretation beyond the 248 premise of spatial correlation in the data (e.g. Hock and Jensen, 1999; Rasmussen and Williams, 2006). 249

Linear regression

Material.

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In the regression and multiple linear regression takes the form $\mathbf{y} = \mathbf{X}\boldsymbol{\beta} + \boldsymbol{\epsilon}$, where \mathbf{y} is the dependent variable, 251 the matrix X in our case contains the set of independent regressors (columns) for each spatial location (rows), 252 β is the vector of regression coefficients and ϵ is independent normal white noise with standard deviation σ 253 (e.g. Davis and Sampson, 1986). In the LR, we use commonly applied defined topographic parameters as the 254 regressors as in McGrath and others (2015), including elevation, slope, aspect, curvature, "northness" and a 255 wind-redistribution parameter (Sx from Winstral and others (2002)); we add distance-from-centreline as an 256 additional parameter. Topographic parameters are standardized for use in the LR. The goal of the LR is to 257 obtain a set of fitted regression coefficients β that correspond to each topographic parameter (regressor) and 258 to a model intercept. For details on data and methods used to estimate the topographic parameters see the 259 Supplementary Material and Pulwicki (2017). Our sampling design ensured that the ranges of topographic 260 parameters associated with our measurement locations represent more than 70% of the total area of each 261 glacier (except elevation on Glacier 2, where our measurements captured only 50%). Topographic parameters 262 are standardized and then weighted by a set of fitted regression coefficients (β_i) calculated by minimizing the 263 sum of squares of the vertical deviations of each datum from the regression line (Davis and Sampson, 1986) 264 . For details on data and methods used to estimate the topographic parameters see the Supplementary 265

To-We use a combination of cross validation and model averaging to avoid overfitting the data and to 267 incorporate every possible combination of topographic parameters, cross-validation and model averaging are 268 implemented. First, cross-validation is used to obtain a set of β_i values that have the greatest predictive ability 269 . We, to account for uncertainty in the selected predictors and to maximize the model's predictive ability 270 (Madigan and Raftery, 1994; Kohavi and others, 1995). Since there are 7 predictors, there are 2^7 possible 271 272 subsets of predictors, or equivalently, models. For a given model, we randomly select 1000 subsets of the data (where each subset includes $\sim 2/3$ of the values) to fit the LR and data) and fit a multiple linear 273 regression using least squares (implemented in MATLAB), thus obtaining 1000 sets of β . Distributed $b_{\rm w}$ is 274 then calculated by multiplying the topographic parameters by their corresponding regression coefficients for 275 all DEM gridcells. We use the remaining data ($\sim 1/3$ of the values) to calculate a root mean squared error 276 (RMSE) (Kohavi and others, 1995) between the estimated and observed $b_{\rm w}$ at the measurement locations. 277 From the 1000 sets of β_i g values, we select the set that results in the lowest RMSE. Second, we use model 278 averaging to account for uncertainty when selecting predictors and to maximize the model's predictive ability 279 (Madigan and Raftery, 1994). Models are generated by calculating a set of β_i as described above for all 280 281 possible combinations of topographic parameters (This set of β has the greatest predictive ability for a particular linear combination of topographic parameters. The procedure above is repeated for each of the 282 models, giving the best β for each of the 2^7 models). Using a Bayesian framework, model averaging involves 283 weighting all models by their posterior model probabilities (Raftery and others, 1997). To obtain the final 284 regression coefficients, the β_i values from each model are weighted according to the. 285 With the β 's in hand, we move on to prediction. To do so, we use Bayesian model averaging. We weight the 286 models according to their relative predictive successof the model, as assessed by the value of the Bayesian 287 Information Criterion (BIC) (Burnham and Anderson, 2004). BIC penalizes more complex models which 288 further, which reduces the risk of overfitting. The distributed WB is then obtained by applying the resulting 289 290 regression coefficients to the topographic parameters associated with each grideell, final set of β is then the weighted sum of β from all models. Distributed $b_{\rm w}$ is again calculated by multiplying the topographic 291 parameters by the final set of β for all DEM gridcells. 292

293 Simple Ordinary kriging

Simple kriging (SK) is a data-driven Kriging is a method of estimating dependent variables at unsampled locations by using the isotropic spatial correlation (covariance) spatial correlation of measured values to find a set of optimal weights (Davis and Sampson, 1986; Li and Heap, 2008). Simple kriging Kriging assumes spatial

correlation between sampling locations that are the dependent variables at the sampling locations distributed 297 across a surface and then applies the correlation to interpolate between these locations. We used the 298 DiceKriging R package (Roustant and others, 2012) to calculate the maximum likelihood covariance matrix, 299 as well as the range distance (θ) and nugget for gridcell-averaged values of winter balance. The range distance 300 is a measure of data correlation length and the nugget is the residual that encompasses sampling-error variance 301 302 as well as the spatial variance at distances less than the minimum sample spacing (Li and Heap, 2008). Unlike topographic regression, simple kriging Many forms of kriging have been developed to accommodate 303 different data types (e.g. Li and Heap, 2008, and sources therein). Ordinary kriging (OK) is the simplest 304 form of kriging in cases where the mean of the estimated field is unknown. Unlike LR, OK is not useful for 305 generating hypotheses to explain the physical controls on snow distribution, nor can it be used to estimate 306 winter balance on unmeasured glaciers. However, we chose to use OK because it does not require external 307 inputs and is therefore a means of obtaining $B_{\rm w}$ that is free of physical interpretation beyond the information 308 contained in the covariance matrix. 309

Uncertainty analysis

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To quantify the uncertainty on estimates of glacier-wide WB we conduct a Monte Carlo analysis, 311 which uses repeated random sampling of input variables to calculate a distribution of output variables 312 (Metropolis and Ulam, 1949). We repeat the random sampling process 1000 times, resulting in a distribution 313 of values of the glacier-wide WB based on uncertainties associated with The OK model can be written 314 $y(s) = \mu + z(s) + e$, where μ is the mean and e is independent white noise with standard deviation σ_e 315 (also known as the nugget) that captures the sampling error as well as spatial variation at distances 316 smaller than that observed in the sampling design (Li and Heap, 2008); z(s) follows a mean-zero normal 317 distribution with standard deviation σ_z . The covariance of observations at spatial locations s and s' is 318 written as $Cov(z(s), z(s')) = \sigma_z^2 r(s, s')$ and r is a specified correlation model. We use the DiceKriging 319 package in R (Roustant and others, 2012) to implement ordinary kriging. For our application we employ an 320 isotropic Matérn correlation model with shape parameter $\nu = 5/2$ (see Rasmussen and Williams, 2006). This 321 specification implies a fairly smooth response surface (twice differentiable) and is used in many applications 322 (e.g. Stein, 1999). The model parameters, μ , σ_e , σ_z and range parameter for the Matérn correlation function 323 are estimated using maximum likelihood. There is no closed form solution for these parameter estimates 324 and they are found numerically. To ensure stability of the maximum likelihood solution, we use 500 random 325 restarts of the four steps outlined above. We use the standard deviation of this distribution as a useful 326

metric of uncertainty on the glacier-wide WB. DiceKringing package (each with a different initial value of the parameters).

Uncertainty analysis using a Monte Carlo approach

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Three sources of uncertainty are considered separately: the uncertainty due to (1) grid-scale variability of 330 WB- $b_{w_{\infty}}(\sigma_{GS})$, (2) the assignment of snow density (σ_{ρ}) and (3) interpolating and extrapolating gridcell-331 averaged values of WB b_w (σ_{INT}). These individual To quantify the combined uncertainty due to grid-scale 332 333 variability, method of density assignment and interpolation uncertainty on estimates of $B_{\rm w}$ we conduct a Monte Carlo analysis that uses repeated random sampling of input variables to calculate a distribution of 334 output variables (Metropolis and Ulam, 1949). We repeat the random sampling process 1000 times, resulting 335 in a distribution of values of $B_{\rm w}$ based on uncertainties associated with the four steps we implement to 336 derive $B_{\rm w}$ from distributed snow-depth and density measurements. Individual sources of uncertainty are 337 propagated through the conversion of snow depth and density measurements to glacier-wide WB $B_{\rm w}$. Finally, 338 the combined effect of all three sources of uncertainty on the glacier-wide WB $\mathcal{B}_{\mathbf{w}}$ is quantified. We calculate 339 a relative uncertainty as the normalized sum of differences between every pair of one hundred distributed WB 340 estimates including use the standard deviation of the distribution of $B_{\rm w}$ as a useful metric of $B_{\rm w}$ uncertainty. 341 Density assignment uncertainty is calculated as the standard deviation of the eight resulting values of $B_{\rm w}$. To 342 investigate the spatial patterns in $b_{\rm w}$ uncertainty, we calculate a combined uncertainty, which is equal to the 343 square root of the summed variance of distributed $b_{\rm w}$ that arises from $\sigma_{\rm GS}$, σ_{ρ} and $\sigma_{\rm INT}$. See Supplementary 344 Material (Figs. S5 and S6) for plots of standard deviation of distributed $b_{\rm w}$ arising from individual sources 345 of uncertainty. 346

347 Grid-scale uncertainty (σ_{GS})

We make use of the zigzag surveys to quantify the true variability of WB b_w at the grid scale. Our limited data 348 do not permit a spatially-resolved assessment of grid-scale uncertainty, so we characterize this uncertainty as 349 uniform across each glacier and represent it by a normal distribution. The distribution is centred at zero and 350 351 has a standard deviation equal to the mean standard deviation of all zigzag measurements for each glacier. For each iteration of the Monte Carlo, WB bw values are randomly chosen from the distribution and added 352 to the values of gridcell-averaged $\frac{WB}{b_w}$. These perturbed gridcell-averaged values of $\frac{WB}{b_w}$ are then used 353 in the interpolation. We represent uncertainty in glacier-wide WB-B_W due to grid-scale uncertainty ($\sigma_{\rm GS}$) as 354 the standard deviation of the resulting distribution of glacier-wide WB- \mathcal{B}_{w} estimates. 355

356 Density assignment uncertainty (σ_{ρ})

We incorporate uncertainty due to the method of density assignment by carrying forward all eight density interpolation methods (Table 3) when estimating glacier-wide WB \mathcal{B}_{w} . By choosing to retain even the least plausible options, as well as the questionable FS data, this approach results in a generous assessment of uncertainty. We represent the glacier-wide WB \mathcal{B}_{w} uncertainty due to density assignment uncertainty (σ_{ρ}) as the standard deviation of glacier-wide WB \mathcal{B}_{w} estimates calculated using each density assignment method.

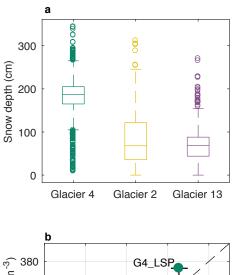
Interpolation uncertainty (σ_{INT}) 362 We represent the uncertainty due to interpolation extrapolation of gridcell-averaged $\frac{WB}{V}$ in different 363 364 ways for LR and SKOK. LR interpolation uncertainty is represented by a multivariate normal distribution 365 of possible regression coefficients $(\beta_{\tau}\beta)$. The standard deviation of each distribution is calculated using the covariance of regression coefficients β as outlined in Bagos and Adam (2015), which ensures that regression 366 coefficients the β values are internally consistent. The β_i distributions are randomly sampled and used to 367 calculate gridcell-estimated $\overline{WB}b_{w}$. 368 SK OK interpolation uncertainty is represented by the 95% confidence interval for standard deviation 369 for each gridcell-estimated values of WB value of $b_{\rm w}$ generated by the DiceKriging package. From this 370 confidence interval, the standard deviation of each gridcell-estimated WB is then calculated. The standard 371 deviation of glacier-wide WB B_{w} is then found by taking the square root of the average variance of each 372 gridcell-estimated \overline{WBb}_w . The final distribution of glacier-wide \overline{WBb}_w values is centred at the glacier-wide 373 WB estimated with SKB_w estimated with OK. For simplicity, the standard deviation of glacier-wide WB 374 values that result B_w values that results from either LR or SK interpolation OK interpolation/extrapolation 375 uncertainty is referred to as σ_{INT} . 376

377 RESULTSAND DISCUSSION

378 Field measurements

379 Snow depth

Mean snow depth varied systematically across the study region, with Glacier 4 having the highest mean snow depth and Glacier 13 having the lowest (Fig. 2a). At each measurement location, the median range of measured depths (3–4 points) as a percent of the mean local depth is 2%, 11% and 12%, for Glaciers 4, 2 and 13, respectively. While Glacier 4 has the lowest point-scale variability, as assessed above, it also has the highest proportion of outliers, indicating a more variable snow depth across the glacier. The average



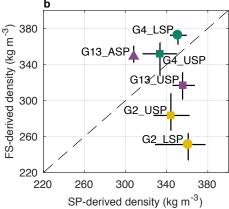


Fig. 2. Measured snow depth and density. (a) Boxplot of measured snow depth on Glaciers 4, 2 and 13 with the first quartiles (box), median (line within box), minimum and maximum values excluding outliers (bar) and outliers (circles), which are defined as being outside of the range of 1.5 times the quartiles (approximately $\pm 2.7\sigma$). (b) Comparison of depth-averaged densities estimated using Federal Sampler (FS) measurements and a wedge cutter in a snow pit (SP) for Glacier 4 (G4), Glacier 2 (G2) and Glacier 13 (G13). Labels indicate snow pit-SP locations in the accumulation area (ASP), upper ablation area (USP) and lower ablation area (LSP). Error bars for SP-derived densities are calculated by varying the thickness and density of layers that are too hard to sample, and error bars for FS-derived densities are the standard deviation of measurements taken at one location. One-to-one line is dashed.

standard deviation of all zigzag depth measurements is 0.07 m, 0.17 m and 0.14 m, for Glaciers 4, 2 and 13, respectively. When converted to values of WB by using the local FS-derived density measurement, the average standard deviation is 0.027 m w.e., 0.035 m w.e. and 0.040 m w.e. WB-Winter-balance data for each zigzag are not normally distributed (Fig. 3).

Snow density

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Contrary to expectation, co-located FS and SP measurements are found to be uncorrelated ($R^2 = 0.25$, Fig. 2b). The Federal Sampler FS appears to oversample in deep snow and undersample in shallow snow.

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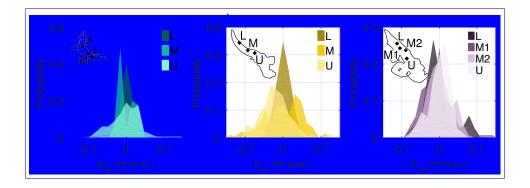


Fig. 3. Distributions of estimated winter-balance values for each zigzag survey in lower (L), middle (M) and upper (U) ablation areas (insets). Local mean has been subtracted. (a) Glacier 4. (b) Glacier 2. (c) Glacier 13.

Oversampling by small-diameter (3.2-3.8 cm) sampling tubes has been observed in previous studies, with a

percent error between 6.8% and 11.8% (e.g. Work and others, 1965; Fames and others, 1982; Conger and 393 McClung, 2009). Studies that use Federal Samplers FS often apply a 10% correction to all measurements for 394 this reason (e.g. Molotch and others, 2005). Oversampling has been attributed to slots "shaving" snow into 395 the tube as it is rotated (e.g. Dixon and Boon, 2012) and to snow falling into the slots, particularly for snow 396 samples with densities $>400\,\mathrm{kg}\,\mathrm{m}^{-3}$ and snow depths $>1\,\mathrm{m}$ (e.g. Beaumont and Work, 1963). Undersampling 397 is likely to occur due to loss of snow from the bottom of the sampler (Turcan and Loijens, 1975). Loss by this 398 mechanism may have occurred in our study, given the isothermal and melt-affected snow conditions observed 399 over the lower reaches of Glaciers 2 and 13. Relatively poor Federal Sampler FS spring-scale sensitivity also 400 calls into question the reliability of measurements for snow depths <20 cm. 401 Our FS-derived density values are positively correlated with snow depth ($R^2 = 0.59$). This relationship 402 could be a result of physical processes, such as compaction in deep snow and preferential formation of depth 403 hoar in shallow snow, but is more likely a result of measurement artefacts for a number of reasons. First, the 404 total range of densities measured by the Federal Sampler-FS seems improbably large (227-431 kg m⁻³)given 405 the conditions at the. At the time of sampling, the snowpack had little new snow, few ice lenses and was 406 407 not saturated; the range of measured densities is therefore difficult to explain with physical conditions. Moreover, the range of FS-derived values is much larger than that of SP-derived values when co-located 408 measurements are compared. Second, compaction effects of the magnitude required to explain the density 409 differences between SP and FS measurements would not be expected at the measured snow depths (up 410 to 340 cm). Third, no linear relationship exists between depth and SP-derived density ($R^2 = 0.05$). These 411 findings suggest that the Federal Sampler FS measurements have a bias for which we have not identified a 412

suitable correction. Despite this bias, we use FS-derived densities to generate a range of possible $b_{\rm w}$ estimates and to provide a generous estimate of uncertainty arising from density assignment.

415 Density assignment

Given the lack of correlation between co-located SP- and FS-derived densities (Fig. 2), we use the densities 416 derived from these two methods separately (Table 3). SP-derived regional (S1) and glacier-mean (S2) densities 417 are within one standard deviation of the corresponding FS-derived densities (F1 and F2) although SP-derived 418 density values are larger (see Supplementary Material, Table \$2S3). For both SP- and FS-derived densities, 419 the mean density for any given glacier (S2 or F2) is within one standard deviation of the mean across all 420 glaciers (S1 or F1). Correlations between elevation and SP- and FS-derived densities are generally high ($R^2 >$ 421 0.5) but vary between glaciers (Supplementary material, Table S2 Material, Table S3). For any given glacier, 422 the standard deviation of the 3-4 SP- or FS-derived densities is <13% of the mean of those values (S2 or 423 F2) (Supplementary material, Table \$2.53). We adopt S2 (glacier-wide mean of SP-derived densities) as the 424 reference method of density assignment. Though the method described by S2 does not account for known 425 basin-scale spatial variability in snow density (e.g. Wetlaufer and others, 2016), it is commonly used in winter 426 balance studies (e.g. Elder and others, 1991; McGrath and others, 2015; Cullen and others, 2017). 427

Gridcell-averaged winter balance

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The distributions of gridcell-averaged WB-bw values for the individual glaciers are similar to those in Fig. 2a 429 but with fewer outliers -(see Supplementary Material, Fig. S4). The standard deviations of $\overline{\text{WB}}$ - b_{w} values 430 determined from the zigzag surveys are almost twice as large as the mean standard deviation of point-scale 431 WB b_w values within a gridcell measured along transects -(see Supplementary Material, Fig. S5). However, 432 a small number of gridcells sampled in transect surveys have standard deviations in $\frac{\text{WB}}{b_w}$ that exceed 433 $0.25\,\mathrm{m}\,\mathrm{w.e.}$ (~ 10 times greater than those for zigzag surveys). We nevertheless assume that the gridcell 434 uncertainty is captured with dense sampling in zigzag gridcells. 435 Distribution of coefficients (β_i) determined by linear regression of gridcell-averaged WB on DEM-derived 436 topographic parameters for the eight different density assignment methods (Table 3). Coefficients are 437 calculated using standardized data, so values can be compared across parameters. Regression coefficients 438 that are not significant are assigned a value of zero. Topographic parameters include elevation (z), distance 439

from centreline (d_C) , slope (m), curvature (κ) and wind redistribution (Sx). Aspect (α) and "northness"

(N) are not shown because coefficient values are zero in every case. The box plot shows first quartiles

(box), median (line within box), mean (circle within box), minimum and maximum values excluding outliers

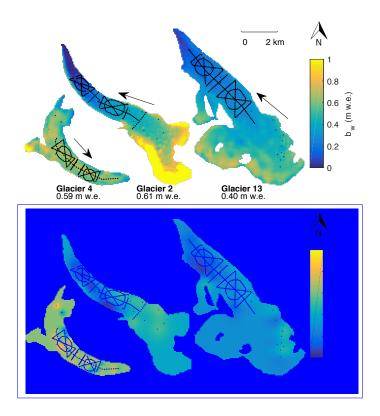


Fig. 4. Spatial distribution of winter balance ($\mathbb{WB}b_{\mathbb{W}}$) estimated using linear regression (top row) and simple ordinary kriging (bottom row) with densities assigned as per S2 (Table 3). The linear regression (LR) method involves multiplying regression coefficients, found using cross validation and model averaging, by topographic parameters for each gridcell. Ordinary kriging (OK) uses the correlation of measured values to find a set of optimal weights for estimating values at unmeasured locations. Locations of snow-depth measurements made in May 2016 are shown as black dots. Ice-flow directions are indicated by arrows. Values of glacier-wide \mathbb{WB} — $\mathbb{B}_{\mathbb{W}}$ are given below labels.

(bars) and outliers (gray dots), which are defined as being outside of the range of 1.5 times the quartiles (approximately $\pm 2.7\sigma$).

445 Distributed winter balance

446 Distributed winter balance

- Relative uncertainty in distributed winter balance (WB) (Fig. 4) found using linear regression (top row) and
- 448 simple kriging (bottom row). Values closer to one indicate higher relative uncertainty. Ice-flow directions are
- 449 indicated by arrows.
- 450 Linear regression
- The highest values of estimated $b_{\rm w}$ are found in the upper portions of the accumulation areas of Glaciers
- 452 2 and 13 (Fig. 4). These areas also correspond to large values of elevation, slope, and wind redistribution.

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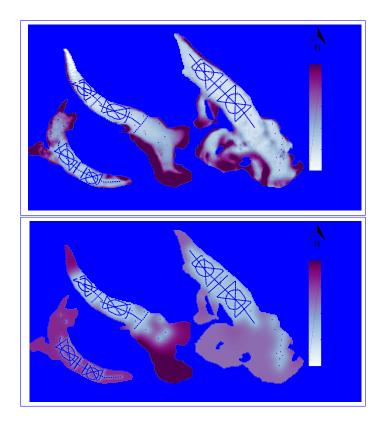


Fig. 5. Combined uncertainty of distributed winter balance $(b_{\rm w})$ for density-assignment method S2 (Fig. 4) found using linear regression (top row) and ordinary kriging (bottom row). Ice-flow directions are indicated by arrows.

Extrapolation of the positive relation between b_w and elevation, as well as slope and Sx for Glacier 2, results in high b_w estimates and large combined uncertainty in these estimates (Fig. 5). On Glacier 4, the distributed b_w is nearly uniform (Fig. 4) due to the small regression coefficients for all topographic parameters. The variance explained by the LR-estimated b_w differs considerably between glaciers (Fig. 6), with the best correlation

Table 4. Glacier-wide winter balance ($\mathbb{WB}_{\mathcal{B}_{\mathbb{W}}}$, m w.e.) estimated using linear regression and simple ordinary kriging for the three study glaciers. Root mean squared error (RMSE, m w.e.) is computed as the average of all RMSE values between gridcell-averaged values of $\mathbb{WB}_{\mathcal{B}_{\mathbb{W}}}$ (the data) that were randomly selected and excluded from interpolation ($\frac{1}{3} \sim \frac{1}{3}$ of all data) and those estimated by interpolation. RMSE as a percent of the glacier-wide $\mathbb{WB}_{\mathcal{B}_{\mathbb{W}}}$ is shown in bracketsparentheses.

	Linear	regression	Ordinary kriging				
	$WB - B_{W}$ RMSE		$\overline{\mathrm{WB}}$ - $\overline{B}_{\mathrm{W}_{\sim}}$	RMSE			
G4	0.58	0.15 (26%)	0.62	0.13 (21 <u>0.11 (18</u> %)			
G2	0.58	0.10~(17%)	$0.37 \underbrace{0.35}_{}$	0.07 (190.06 (18%)			
G13	0.38	0.08 (21%)	0.27	0.07 (260.06 (21%)			

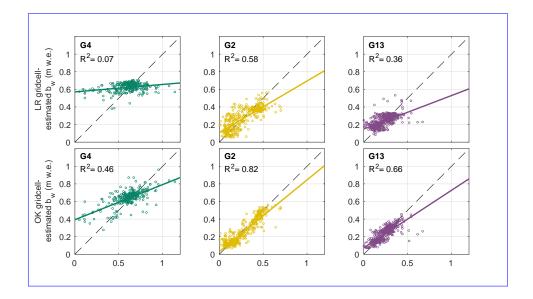


Fig. 6. Winter balance (b_w) estimated by linear regression (LR, top row) or ordinary kriging (OK, bottom row) versus the grid-cell averaged b_w data for Glacier 4 (left), Glacier 2 (middle) and Glacier 13 (right). Each circle represents a single gridcell. Explained variance (\mathbb{R}^2) is provided. Best-fit (solid) and one-to-one (dashed) lines are shown.

between modelled and observed $b_{\rm w}$ occurring for Glacier 2. LR is an especially poor predictor of $b_{\rm w}$ on Glacier 4, where $B_{\rm w}$ can be estimated equally well using the mean of the data. RMSE is also highest for Glacier 4 (Table 4).

Ordinary kriging

For all three glaciers, large areas that correspond to locations far from measurements have $b_{\rm w}$ estimates equal to the kriging mean. Distributed $b_{\rm w}$ estimated with OK on Glacier 4 is mostly uniform except for local deviations close to measurement locations (Fig. 4) and combined uncertainty is high across the glacier. Distributed $b_{\rm w}$ varies more smoothly on Glaciers 2 and 13 (Fig. 4). Glacier 2 has a distinct region of low estimated $b_{\rm w}$ ($\sim 0.1 \,\mathrm{m}$ w.e.) in the lower part of the ablation area, which corresponds to a wind-scoured region of the glacier. Glacier 13 has the lowest estimated mean $b_{\rm w}$ and only small deviations from this mean at measurement locations (Fig. 4). Combined uncertainty varies considerably across the three study glaciers with the greatest uncertainty far from measurement locations (Fig. 5). The variance explained by OK-estimated $b_{\rm w}$ is high for Glaciers 2 and 13 relative to that for Glacier 4 (Fig. 6).

470 Uncertainty analysis using a Monte Carlo approach

471 Linear Regression

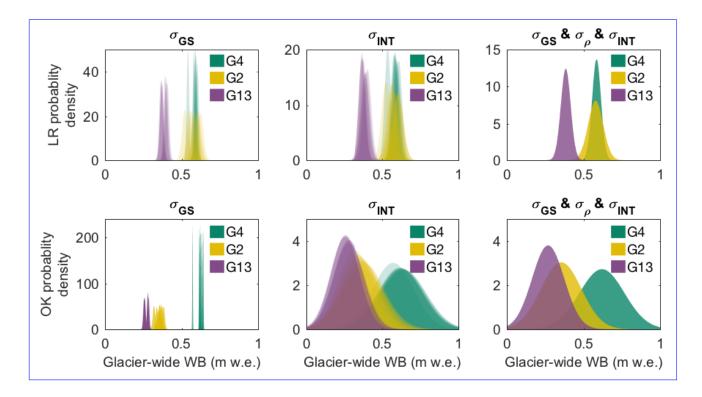


Fig. 7. Winter–Distributions of glacier-wide winter balance (WB $B_{\rm w}$) estimated by linear regression for Glaciers 4 (LRG4), top row2 (G2) or simple kriging and 13 (SK, bottom rowG13) versus the grid-cell averaged WB data for Glacier 4 that arise from various sources of uncertainty. $B_{\rm w}$ distribution arising from grid-scale uncertainty ($\sigma_{\rm GS}$) (left column), Glacier 2 . $B_{\rm w}$ distribution arising from interpolation uncertainty ($\sigma_{\rm INT}$) (middle column). $B_{\rm w}$ distribution arising from a combination of $\sigma_{\rm GS}$, $\sigma_{\rm INT}$ and Glacier 13 density assignment uncertainty (σ_{ρ}) (right column). Each circle represents a single gridcell Results are shown for interpolation by linear regression (LR, top row) and ordinary kriging (OK, bottom row). Best-fit-Left two columns include eight distributions per glacier (solid-colour) and one-to-one each corresponds to a density assignment method (dashedS1–S4 and F1–F4) lines are shown.

Estimates of $B_{\rm w}$ are affected by uncertainty introduced by the representativeness of gridcell-averaged values of 472 $b_{\rm w}$ ($\sigma_{\rm GS}$), choosing a method of density assignment (σ_{ρ}), and interpolating/extrapolating $b_{\rm w}$ values across the 473 domain (σ_{INT}) . Using a Monte Carlo analysis, we find that interpolation uncertainty contributes more to B_{w} 474 uncertainty than grid-scale uncertainty or the method of density assignment (see Supplementary Material). In 475 other words, the distribution of $B_{\rm w}$ that arises from grid-scale uncertainty and the differences in distributions 476 of $B_{\rm w}$ due to different methods of density assignment are generally smaller than the distribution that arises 477 from interpolation uncertainty (Fig. 7 and Table 5). The $B_{\rm w}$ distributions obtained using LR and OK overlap 478 for a given glacier, but the distribution modes differ (Fig. 7). OK-estimated values of $b_{\rm w}$ in the accumulation 479 area are generally lower (Fig. 4), which lowers the $B_{\rm w}$ estimate. The uncertainty in OK-estimated values of 480 $B_{\rm w}$ is large, and unrealistic values (e.g. $B_{\rm w}=0\,{\rm m}\,{\rm w.e.}$) are possible (Fig. 7). 481

Table 5. Standard deviation (×10⁻² m w.e.) of glacier-wide winter balance ($B_{\rm w}$) distributions arising from uncertainties in grid-scale $b_{\rm w}$ ($\sigma_{\rm GS}$), density assignment (σ_{ρ}), interpolation ($\sigma_{\rm INT}$) and all three sources combined ($\sigma_{\rm ALL}$) for linear regression (left columns) and ordinary kriging (right columns)

]	Linear	regressi	on	Ordinary kriging			
	$\sigma_{ m GS}$	$\sigma_{ m p}$	σ_{INT}	<i>SALL</i> €	$\sigma_{ m GS}$	$\sigma_{\!\scriptscriptstyle{R_{\!\scriptscriptstyle{\sim}}}}$	σ_{INT}	SALL.
Glacier 4	0.86	1.90	2.13	2.90	0.18	2.16	14.35	14.64
Glacier 2	1.80	3.37	3.09	4.90	0.80	2.06	12.65	<u>13.14</u>
Glacier 13	1.12	1.68	2.80	3.20	0.57	1.30	$\underbrace{9.74}_{\sim}$	10.48

The values of $B_{\rm w}$ for our study glaciers (using LR and the S2 density assignment), with an uncertainty equal to one standard deviation of the distribution found with Monte Carlo analysis, are: 0.59 ± 0.03 m w.e. for Glacier 4, 0.61 ± 0.05 m w.e. for Glacier 2 and 0.40 ± 0.03 m w.e. for Glacier 13. The $B_{\rm w}$ uncertainty from the three investigated sources of uncertainty ranges from 0.03 m w.e (5%) to 0.05 m w.e (8%) for LR estimates and from 0.10 m w.e (37%) to 0.15 m w.e (24%) for ordinary-kriging estimates.

DISCUSSION

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Distributed winter balance

489 Linear regression

Of the topographic parameters in the linear regression $\mathbb{L}\mathbb{R}$, elevation (z) is the most significant predictor 490 of gridcell-averaged $\frac{WB}{b_w}$ for Glaciers 2 and 13, while wind redistribution (Sx) is the most significant 491 predictor for Glacier 4 (Fig. 8, Fig. 4). As expected, gridcell-averaged $\frac{WB}{b_w}$ is positively correlated with 492 elevation where the correlation is significant. It is possible that the elevation correlation was accentuated 493 due to melt onset for Glacier 13 in particular. Many studies Glacier 2 had little snow at the terminus likely 494 due to steep slopes and wind-scouring but the snow did not appear to have been affected by melt. Our 495 results are consistent with many studies that have found elevation to be the most significant predictor of 496 winter-balance data (e.g. Machguth and others, 2006; McGrath and others, 2015). However, WB-elevation 497 gradients vary considerably between glaciers (e.g. Winther and others, 1998) and other factors, such as 498 499 glacier shape and orientation relative to dominant wind direction, are strong predictors of the winter-balance distribution (Machguth and others, 2006; Grabiec and others, 2011). Some studies find no significant 500 correlation between WB on glaciers and topographic parameters, with seasonal snow accumulation 501 (e.g. Machguth and others, 2006; Grünewald and others, 2014; McGrath and others, 2015). 502

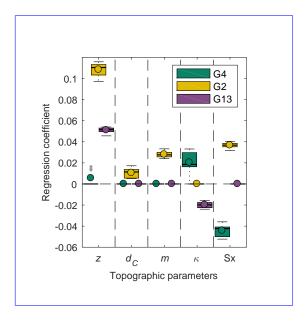


Fig. 8. Distribution of coefficients (β) determined by linear regression of gridcell-averaged b_w on DEM-derived topographic parameters for the eight different density assignment methods (Table 3). Coefficients are calculated using standardized data, so values can be compared across parameters. Regression coefficients that are not significant are assigned a value of zero. Topographic parameters include elevation (z), distance from centreline (d_C), slope (m), curvature (κ) and wind redistribution (Sx). Aspect (α) and "northness" (N) are not shown because coefficient values are zero in every case. The box plot shows first quartiles (box), median (line within box), mean (circle within box), minimum and maximum values excluding outliers (bars) and outliers (gray dots), which are defined as being outside of the range of 1.5 times the quartiles (approximately $\pm 2.7\sigma$).

 $b_{\rm w}$ -elevation gradient is $13\,{\rm mm}\,100\,{\rm m}^{-1}$ on Glacier 2 and $7\,{\rm mm}\,100\,{\rm m}^{-1}$ on Glacier 13. These gradients are consistent with those reported for a few glaciers in Svalbard (Winther and others, 1998) but are considerably smaller than many reported $b_{\rm w}$ -elevation gradients, which range from about 60 to $240\,{\rm mm}\,100\,{\rm m}^{-1}$ (e.g. Hagen and Liestøl, 1990; Tveit and Killingtveit, 1994; Winther and others, 1998). Extrapolating linear relationships to unmeasured locations typically results in considerable estimation error, as seen by the large $b_{\rm w}$ values (Fig. 4) and large combined uncertainty (Fig. 5) in the high-elevation regions of Glaciers 2 and 13. The low correlation between $b_{\rm w}$ and elevation on Glacier 4 is consistent with Grabiec and others (2011) and López-Moreno and others (2011), who conclude that highly variable distributions of snow can be attributed to complex interactions between topography and the atmosphere that could not cannot be easily quantified(e.g. Grabiec and others, 2011; López-Moreno and others, 2011). Extrapolating relationships to unmeasured locations, especially the accumulation area, is susceptible to large uncertainties (Fig. 5). This extrapolation has a considerable effect on values of glacier-wide WB, as the highest values of WB are

typically found in the accumulation area (Fig. 4)... The snow on Glacier 4 also did not appear to have been 515 affected by melt and it is hypothesized that significant wind-redistribution of snow, which was not captured 516 by the Sx parameter, covered ice-topography and produced a relatively uniform snow depth across the 517 518 glacier. Gridcell-averaged $\frac{WB}{b_w}$ is negatively correlated with Sx on Glacier 4, counter-intuitively indicating 519 less snow in what would be interpreted as sheltered areas. Gridcell-averaged $\frac{WB}{b_{W}}$ is positively 520 correlated with Sx on Glaciers 2 and 13. Similarly, gridcell-averaged WB is positively correlated with 521 curvature on Glacier 4 and negatively correlated on Glaciers 2 and 13. Wind redistribution and 522 preferential deposition of snow are known to have a large influence on snow distribution at sub-basin 523 scales (e.g. Dadić and others, 2010; Winstral and others, 2013; Gerber and others, 2017). Our Our results 524 corroborate those of McGrath and others (2015) in a study of six glaciers in Alaska (DEM resolutions of 525 5 m) where elevation and Sx were the only significant parameters for all glaciers; Sx regression coefficients 526 were smaller than elevation regression coefficients, and in some cases, negative. While our results point to 527 wind having an impact on snow distribution, but the wind redistribution parameter (Sx) may not adequately 528 529 capture these effects at our study sites. For example, Glacier 4 is located in a curved valley with steep side has a curvilinear plan-view profile and is surrounded by steep valley walls, so specifying a single cardinal 530 direction for wind may not be adequate. Further, the scale of deposition may be smaller than the resolution 531 of the Sx parameter estimated from the DEM. Our results corroborate those of McGrath and others (2015) 532 in a study of six glaciers in Alaska (DEM resolutions of 5 m) where elevation and Sx were the only significant 533 parameters for all glaciers; Sx regression coefficients were smaller than elevation regression coefficients, and 534 535 in some cases, negative. In addition to wind redistribution, Creation of a parametrization for sublimation from blowing snowhas also, which has been shown to be an important mechanism of mass loss from ridges 536 (e.g. Musselman and others, 2015). Incorporating such losses, as well as redistribution and preferential 537 538 deposition, may be important for improving representations of distributed winter balance, may also increase the explanatory power of LR for our study sites. 539 We find that transfer of LR coefficients between glaciers results in large estimation errors. Regression 540 coefficients from Glacier 4 produce the highest root mean squared error RMSE (0.38 m w.e. on Glacier 2 and 541 $0.40 \,\mathrm{m}$ w.e. on Glacier 13, see Table 4 for comparison) and glacier-wide WB- B_{w} values are the same for all 542 glaciers (0.64 m w.e.) due to the dominance of the regression intercept. Even if the regression-LR is performed 543 with $\frac{\text{WB}}{\text{b}_{\text{W}}}$ values from all glaciers combined, the resulting coefficients produce large root mean squared 544

errors RMSE when applied to individual glaciers (0.31 m w.e., 0.15 m w.e. and 0.14 m w.e. for Glaciers 4, 2 and 13, respectively). Our results are consistent with those of Grünewald and others (2013), who found that local statistical models cannot be transferred across basins and that regional-scale models are not able to explain the majority of observed variance in winter balance.

Simple Ordinary kriging

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550 Fitted kriging parameters, including the nugget and spatial correlation length, can provide insight into important scales of winter-balance variability. The model fitted to the gridcell-averaged values of WB for 551 Glacier 4 has a short correlation length (90 m) and large nugget (see Supplementary Material Table S3), 552 suggesting variability in winter balance at smaller scales. Conversely, Glaciers 2 and 13 have longer correlation 553 lengths (~450 m) and smaller nuggets, suggesting variability at larger scales. Additionally, simple kriging is 554 better able to estimate values of WB for Glaciers 2 and 13 than for Glacier 4 (Fig. 6). Due to a paucity of 555 data, simple ordinary kriging produces almost uniform gridcell-estimated values of winter balance b_{w} in the 556 accumulation area of each glacier, inconsistent with observations described in the literature (e.g. Machguth 557 and others, 2006; Grabiec and others, 2011). Extrapolation using simple kriging Glacier 4 has the highest 558 estimated mean with large deviations from the mean at measurement locations. The longer correlation lengths 559 560 of the data for Glaciers 2 and 13 result in a more smoothly varying distributed $b_{\rm w}$. As expected, extrapolation using OK leads to large uncertainty (Fig. 5), further emphasizing the need for spatially distributed point-scale 561 measurements. 562

563 LR and SK-OK comparison

Glacier-wide WB estimates found using both LR and SK are LR and OK produce similar estimates of 564 distributed $b_{\rm w}$ (Fig. 4) and $B_{\rm w}$ ($\sim 0.580.60$ m w.e., Table 4) for Glacier 4 but both are relatively poor predictors 565 of $\overline{\text{WB}}$ by in measured gridcells (Table 4Fig. 6). For Glaciers 2 and 13, $\overline{\text{SK}}$ estimates are more than 566 $\frac{0.1}{0.1}$ v.e. (up to $\frac{40\%}{0.1}$ 39%) and $\frac{0.11}{0.11}$ m.e. (30%) lower than LR estimates, respectively (Table 4). 567 RMSE as a percentage of the $B_{\rm w}$ is lower for OK than LR only for Glacier 4 but the absolute RMSE of 568 569 OK is ~ 0.03 m w.e. lower for all glaciers, likely because OK is a data-fitting interpolation method (Table 4). RMSEs as a percentage of glacier-wide $\frac{WB}{B_W}$ are comparable between LR and $\frac{SK}{OK}$ (Table 4) with an 570 average RMSE of 22%. This comparability is interesting, given that all of the data were used to generate the 571 SK-OK model, while only $\frac{2}{3} \sim \frac{2}{3}$ were used in the LR. Tests in which only $\sim \frac{2}{3}$ of the data were used in 572 the OK model yielded similar results to those in which all data were used. Gridcell-estimated values of WB 573 b_{w} found using LR and SK-OK differ markedly in the upper accumulation areas of Glaciers 2 and 13 (Fig. 574

their highest values. The influence of elevation results in substantially higher LR-estimated values of \overline{WB} - b_w 576 at high elevation, whereas SK-estimated values approximate the nearest data OK-estimated values are more 577 <u>uniform</u>. Estimates of ablation-area-wide $\frac{WB}{B_W}$ differ by <76% between LR and $\frac{SK}{OK}$ on each glacier, 578 further emphasizing the combined role influence of interpolation method and measurement scarcity in the 579 580 accumulation area on glacier-wide WB $\mathcal{B}_{\mathbf{w}}$ estimates. Distributions of glacier-wide winter balance (WB) for Glaciers 4 (G4), 2 (G2) and 13 (G13) that arise from 581 various sources of uncertainty. WB distribution arising from grid-scale uncertainty (σ_{GS}) (left column). WB 582 distribution arising from interpolation uncertainty (σ_{INT}) (middle column). WB distribution arising from 583 a combination of σ_{GS} , σ_{INT} and density assignment uncertainty (σ_{ρ}) (right column). Results are shown for 584 interpolation by linear regression (LR, top row) and simple kriging (SK, bottom row). Left two columns 585 include eight distributions per glacier (colour) and each corresponds to a density assignment method (S1-S4 586 and F1 F4). 587

4), where observations are sparse and topographic parameters, such as elevation, vary considerably attain

Uncertainty analysis using a Monte Carlo approach

Uncertainty analysis

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Glacier-wide winter balance is affected by uncertainty introduced by the representativeness of 590 gridcell-averaged values of WB (σ_{GS}), choosing a method of density assignment (σ_{ρ}), and interpolating 591 WB values across the domain (σ_{INT}). Using a Monte Carlo analysis, we find that interpolation uncertainty 592 contributes more to WB uncertainty than grid-scale uncertainty or density assignment method. In other 593 words, the distribution of glacier-wide WB that arises from grid-scale uncertainty and the differences in 594 distributions between methods of density assignment are smaller than the distribution that arises from 595 interpolation uncertainty (Fig. 7 and Table 5). The WB distributions obtained using LR and SK overlap 596 for a given glacier, but the distribution modes differ (Fig. 7). For reasons outlined above, SK-estimated 597 values of WB in the accumulation area are generally lower, which lowers the glacier-wide WB estimate. The 598 uncertainty in SK-estimated values of WB is large, and unrealistic glacier-wide values of WB of 0 m w.e. can 599 be estimated (Fig. 7). Our Interpolation/extrapolation of $b_{\rm w}$ data is the largest contributor to $b_{\rm w}$ uncertainty 600 in our study. These results caution strongly against including interpolated/extrapolated values of \overline{WB} b_w in 601 comparisons with remote sensing- or model-derived estimates of $\overline{WBb_w}$. If possible, such comparisons should 602 be restricted to point-scale data. 603

Standard deviation ($\times 10^{-2}$ m w.e.) of glacier-wide winter balance distributions arising from uncertainties 604 in grid-scale WB ($\sigma_{\rm GS}$), density assignment (σ_{ρ}), interpolation ($\sigma_{\rm INT}$) and all three sources combined ($\sigma_{\rm ALL}$) 605 for linear regression (left columns) and simple kriging (right columns) $\sigma_{GS} \sigma_{\varrho} \sigma_{INT} \sigma_{ALL} \sigma_{GS} \sigma_{\varrho} \sigma_{INT} \sigma_{ALL}$ 606 Glacier 4 0.86 1.90 2.13 2.90 0.85 2.15 14.05 14.72 Glacier 2 1.80 3.37 3.09 4.90 2.53 2.03 13.78 13.44 607 Glacier 13 1.12 1.68 2.80 3.20 1.15 1.27 9.65 10.43 608 609 Grid-scale uncertainty (σ_{GS}) is the smallest assessed contributor to overall WB- \mathcal{B}_{W} uncertainty. This result is consistent with the generally smoothly-varying snow depths encountered in zigzag surveys, and previously 610 reported ice-roughness lengths on the order of centimetres (e.g. Hock, 2005) compared to snow depths on the 611 order of decimetres to metres. Given our assumption that zigzags are an adequate representation of grid-scale 612 variability, the low WB- $B_{\rm w}$ uncertainty arising from $\sigma_{\rm GS}$ implies that subgrid-scale sampling need not be a 613 high priority for reducing overall uncertainty. Our assumption that the 3-4 zigzag surveys can be used to 614 estimate glacier-wide σ_{GS} may be flawed, particularly in areas with debris cover, crevasses and steep slopes. 615 Our analysis did not include uncertainty arising from a number of sources, which we assume either to 616 be encompassed by the sources investigated or to be negligible contributors. These sources of uncertainty 617 include density measurement errors associated with the Federal Sampler FS, wedge cutters and spring scales, 618 from vertical and horizontal errors in the DEM and or from error associated with estimating measurement 619 locations -620 The values of glacier-wide WB for our study glaciers (using LR and S2 density assignment method), with 621 an uncertainty equal to one standard deviation of the distribution found with Monte Carlo analysis, are: 622 0.59 ± 0.03 m w. e. for Glacier 4, 0.61 ± 0.05 m w.e. for Glacier 2 and 0.40 ± 0.03 m w.e. for Glacier 13. The 623 glacier-wide WB uncertainty from combined based on the GPS position of the lead observer. We assume that 624 these sources of uncertainty ranges from $0.03\,\mathrm{m}$ w. e (5%) to $0.05\,\mathrm{m}$ w.e (8%) for linear-regression estimates 625 and from 0.10 m w.e (37%) to 0.15 m w.e (24%) for simple-kriging estimates (Table 4), are either encompassed 626

Context and caveats Regional winter-balance gradient

629 Regional winter-balance gradient

by the sources investigated or are negligible.

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Although we find considerable inter- and intra-basin variability in winter balance, our results are consistent with a regional-scale winter-balance gradient for the continental side of the St. Elias Mountains (Fig. 9). Winter-balance data are compiled from Taylor-Barge (1969), the three glaciers presented in this paper and

633 two snow pits SP we analyzed near the head of the Kaskawulsh Glacier between 20–21 May 2016. The

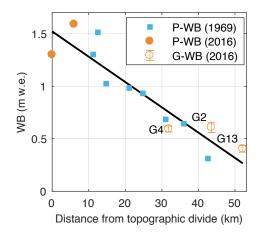


Fig. 9. Relationship between winter balance (WB) and linear distance from the regional topographic divide between the Kaskawulsh and Hubbard Glaciers in the St. Elias Mountains. Point-scale values of WB-winter balance from snow-pit data reported by Taylor-Barge (1969) (blue boxes, P-WB). LR-estimated glacier-wide WB-winter balance ($B_{\rm w}$) calculated using density assignment S2 for Glaciers 4 (G4), 2 (G2) and 13 (G13) with errors bars calculated as the standard deviation of Monte Carlo-derived WB- $B_{\rm w}$ distributions (this study) (open orange circles, G-WB). Point-scale WB-winter balance estimated from snow-pit data at two locations in the accumulation area of the Kaskawulsh Glacier, collected in May 2016 (unpublished data, SFU Glaciology Group) (filled orange dots, P-WB). Black line indicates best fit ($R^2 = 0.85$).

data show a linear decrease of $0.024\,\mathrm{m\,w.e.~km^{-1}}$ ($\mathrm{R}^2=0.85$) in winter balance with distance from the regional topographic divide between the Kaskawulsh and Hubbard Glaciers, as identified by Taylor-Barge (1969). While the three study glaciers fit the regional trend, the same relationship would not apply if just the Donjek Range were considered. We hypothesize that interaction between meso-scale weather patterns and large-scale mountain topography is a major driver of regional-scale winter balance. Further insight into regional-scale patterns of winter balance in the St. Elias Mountains could be gained by investigating moisture source trajectories and the contribution of orographic precipitation.

Limitations and future work

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Limitations and future work

The potential limitations of our work include the restriction of our data to a single year, minimal sampling in the accumulation area, the problem of uncorrelated SP- and FS-derived densities, a sampling design that could not be optimized a prioria priori, the assumption of spatially uniform subgrid variability and lack of more finely resolved DEMs.

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Inter-annual variability in winter balance is not considered in our study. A number of studies have found 647 temporal stability in spatial patterns of snow distribution and that statistical models based on topographic 648 parameters could be applied reliably between years (e.g. Grünewald and others, 2013). For example, Walmsley 649 (2015) analyzed more than 40 years of winter balance recorded on two Norwegian glaciers and found that 650 snow distribution is spatially heterogeneous yet exhibits robust temporal stability. Contrary to this, Crochet 651 652 and others (2007) found that snow distribution in Iceland differed considerably between years and depended primarily on the dominant wind direction over the course of a winter. Therefore, multiple years of snow depth 653 and density measurements, that are not necessarily consecutive, are needed to better understand inter-annual 654 variability in winter-balance distribution of winter balance within the Donjek Range. 655

There is a conspicuous lack of data in the accumulation areas of our study glaciers. With increased sampling in the accumulation area, interpolation uncertainties would be reduced where they are currently greatest and the linear regression-LR would be better constrained. Although certain regions of the glaciers remain inaccessible for direct measurements, other methods of obtaining winter-balance measurements, including ground-penetrating radar and DEM differencing with photogrammetry or lidar, could be used in conjunction with manual probing to increase the spatial coverage of measurements.

The lack of correlation between SP- and FS-derived densities needs to be reconciled. Contrary to our results, most studies that compare SP- and FS-derived densities report minimal discrepancy (e.g. Dixon and Boon, 2012, and sources within). Additional co-located density measurements are needed to better compare the two methods of obtaining density values. Comparison with other Federal Samplers FS would also be informative. Even with this limitation, density assignment was, fortunately, not the largest source of uncertainty in estimating glacier-wide winter balance.

Our sampling design was chosen to achieve broad spatial coverage of the ablation area, but is likely too finely resolved along transects for many mass-balance surveys to replicate. An optimal sampling design would minimize uncertainty in winter balance while reducing the number of required measurements. Analysis of the estimated winter balance obtained using subsets of the data is underway to make recommendations on optimal transect configuration and along-track spacing of measurements. López-Moreno and others (2010) found that 200–400 observations are needed within a non-glacierized alpine basin (6 km²) to obtain accurate and robust snow distribution models. Similar guidelines would be useful for glacierized environments.

In this study, we assume that the subgrid variability of winter balance is uniform across a given glacier. Contrary to this assumption, McGrath and others (2015) found greater variability of winter-balance values close to the terminus. Testing our assumption could be a simple matter of prioritizing the labour-intensive zigzags surveys. To ensure consistent quantification of subgrid variability, zigzag survey measurements could also be tested against other measurements methods, such as lidar.

DEM gridcell size is known to influence values of computed topographic parameters (Zhang and

Montgomery, 1994; Garbrecht and Martz, 1994; Guo-an and others, 2001; López-Moreno and others, 2010). 681 682 The relationship between topographic parameters and winter balance is, therefore, not independent of DEM gridcell size. For example, Kienzle (2004) and López-Moreno and others (2010) found that a decrease in spatial 683 resolution of the DEM results in a decrease in the importance of curvature and an increase in the importance 684 of elevation in regressions LR of snow distribution on topographic parameters in non-glacierized basins. The 685 importance of curvature in our study is affected by the DEM smoothing that we applied to obtain a spatially 686 continuous curvature field (see Supplementary Material, Fig. S1). A comparison of regression coefficients 687 from high-resolution DEMs obtained from various sources and sampled with various gridcell sizes could be 688 used to characterize the dependence of topographic parameters on DEMs, and therefore assess the robustness 689 of inferred relationships between winter balance and topographic parameters. 690

CONCLUSION

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We estimate winter balance for three glaciers (termed Glacier 2, Glacier 4 and Glacier 13) in the St. Elias Mountains, Yukon, Canada from multiscale snow depth and density measurements. Linear regression and simple ordinary kriging are used to obtain estimates of distributed winter balance (b_w). We use Monte Carlo analysis to evaluate the contributions of interpolation, the assignment of snow density and grid-scale variability of winter balance to uncertainty in estimates of glacier-wide winter balance (B_w).

Values of glacier-wide winter balance $B_{\rm w}$ estimated using linear regression and simple ordinary kriging differ by up to 0.24 m w.e. ($\sim 50\%$). We find that interpolation uncertainty is the largest assessed source of uncertainty in glacier-wide winter balance ($5B_{\rm w}$ (7% for linear-regression estimates and 32% for simple-kriging of 34% for ordinary-kriging estimates). Uncertainty resulting from the method of density assignment is comparatively low, despite the wide range of methods explored. Given our representation of grid-scale variability, the resulting winter balance $B_{\rm w}$ uncertainty is small indicating that extensive subgrid-scale sampling is not required to reduce overall uncertainty.

Our results suggest that processes governing distributed winter balance b_{w} differ between glaciers, highlighting the importance of regional-scale winter-balance studies. The estimated distribution of winter balance b_{w} on Glacier 4 is characterized by high variability, as indicated by the poor correlation between

estimated and observed values and large number of data outliers. Glaciers 2 and 13 appear to have lower spatial variability, with elevation being the dominant predictor of gridcell-averaged winter balanceb_w. A wind-redistribution parameter is found to be a weak but significant predictor of winter balanceb_w, though conflicting relationships between glaciers make it difficult to interpret. The major limitations of our work include the restriction of our data to a single year and minimal sampling in the accumulation area. Although challenges persist when estimating winter balance, our data are consistent with a regional-scale winter-balance gradient for the continental side of the St. Elias Mountains.

714 AUTHOR CONTRIBUTION STATEMENT

AP planned and executed the data collection, performed all calculations and drafted analysis and drafted and edited the manuscript. GF conceived of the study, contributed to field planning and data collection, oversaw all stages of the work and edited the manuscript. VR provided guidance with statistical methods on the methods of data analysis and edited the manuscript. DB provided insight into the statistical analysis and edited the manuscript.

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