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April 5, 2019

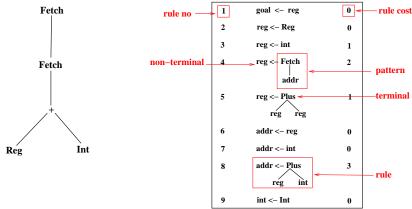
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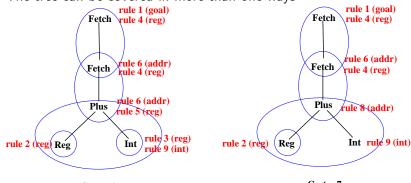
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- Only cases taken into account are different patterns matching a node.
- Say something about normalising instructions

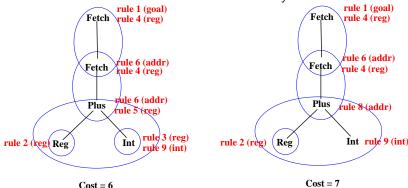
An example expression tree and an example machine:



The tree can be covered in more than one ways

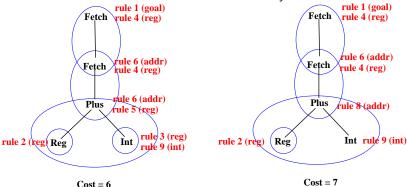


The tree can be covered in more than one ways



We are finally interested in the least cost tree.

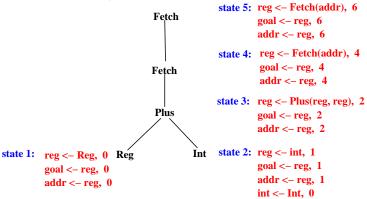
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- We are finally interested in the least cost tree.
- We also want to do some pre-processing before we get any tree,

▶ How is this done? Given a tree,

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 - traverse the tree bottom up. With the help of a transition table, annotate each node of the tree with a state.



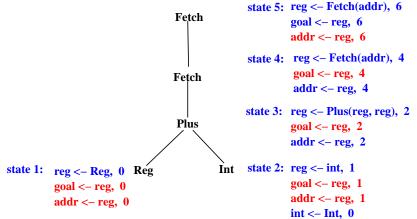
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- ► Transition table: Gives
 - state corresponding to leaf nodes (0-ary terminals).
 - given the states of children, gives state of interior nodes (n-ary terminals).

A second top-down pass determines the instructions to be used at each node assuming that the root is to be evaluated in goal.



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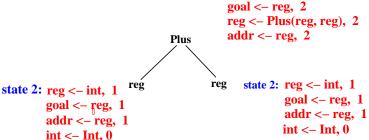
Cost of reducing Int to goal is

```
cost of reducing Int to int (0) + cost of reducing int to reg (1) + cost of reducing reg to goal (0) +
```

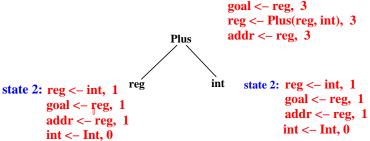
n-ary terminals

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 - ► If both children of Plus are in state 2, in which state would Plus be?

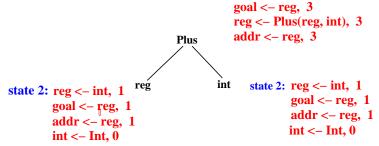
- n-ary terminals
 - ► If both children of Plus are in state 2, in which state would Plus be?
- ► The rule reg ← Plus(reg, reg) gives



► The rule reg ← Plus(reg, int) gives



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► Conclusion: If the leaves of Plus are both in state 2, then Plus will be in

```
state 6: goal <- reg, 2
reg <- Plus(reg, reg), 2
addr <- reg, 2
```

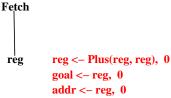
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- ▶ Will this process always terminate?

► Consider computation of the state at Fetch, with reg in the state shown.



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Successive computation of the states for Fetch yield:



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- ► After relativization, the state on the left changes to the state on the right:

```
reg <- Plus(reg, reg), 2 reg <-
goal <- reg, 2 goal <-
addr <- reg, 2 addr <-
```

```
reg <- Plus(reg, reg), 0
goal <- reg, 0
addr <- reg, 0
```

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```

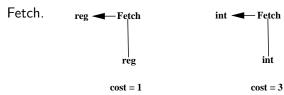
Does this make the resulting transition table different? Obviously not.

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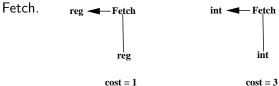
```
\begin{array}{lll} reg <- \ Plus(reg, reg), \ 2 & reg <- \ Plus(reg, reg), \ 0 \\ goal <- \ reg, \ 2 & goal <- \ reg, \ 0 \\ addr <- \ reg, \ 0 & addr <- \ reg, \ 0 \end{array}
```

- Does this make the resulting transition table different? Obviously not.
- Does this necessarily lead to a finite number of states?

► Consider a machine with only these two instructions involving

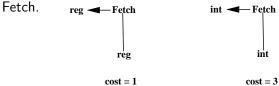


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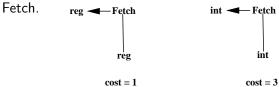
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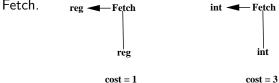
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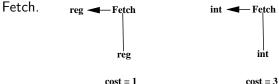
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- Practical solution: If cost difference between any pair of terminals is greater than a threshold, instruction set is rejected.

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- Practical solution: If cost difference between any pair of terminals is greater than a threshold, instruction set is rejected.
- ► Typical instruction sets do not lead to divergence.

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 - State reduction by triangle trimming.

Consider a machine in which the only instructions involving Plus are:



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▶ Also assume that there are two states:

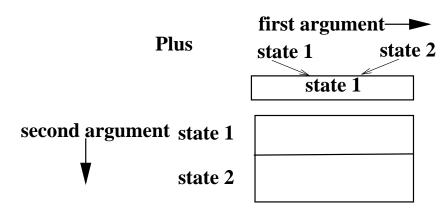
```
state 1: goal <- reg, 0 reg <- Reg, 0 addr <- reg, 0
```

```
state 2: goal <- reg, 1
reg <- int, 1
addr <- reg, 1
int <- Int, 0
```

▶ The normal transition table for Plus:

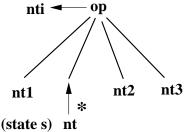


Since the first argument of Plus is a reg, we can project the int ← ... item out of both the states. The resulting transition table for Plus is:



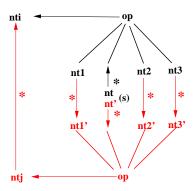
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- Assume that the state has been used in the context of the operator op at the argument position shown

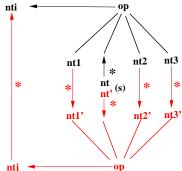


lacktriangle The general situation under which nt $\leftarrow \ldots$ is subsumed by

 $\mathsf{nt'} \leftarrow \ldots \mathsf{is} :$

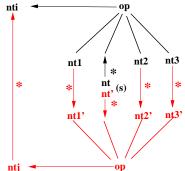


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► The general situation under which nt ← ... is subsumed by $\mathsf{nt'} \leftarrow \ldots \mathsf{is}$:



- The cost of the rule nti ← ...and the black chain reductions should be less than the rule $ntj \leftarrow \dots$ and the red chain reductions.
- Further this should be true in all contexts in which s can be used.



▶ Bottom Up Rewriting based code Generator

- Bottom Up Rewriting based code Generator
- Sample BURG input.

```
BURG's name for node type
                                       user's name for node type
              #define NODEPTR TYPE treepointer
              #define OP LABEL(p) ((p)->op)
    macros to
              #define LEFT CHILD(p) ((p) -> left)
    traverse tree
              #define RIGHT_CHILD(p) ((p) -> right)
              #define STATE LABEL(p) ((p) -> state label)
            용 }
                                 terminals .
              %start goal
              %term Assign=1 Constant=2 Fetch=3 Four=4
              %term Mul=5 Plus=6
                                          rule number
              응응
              con: Constant
                                                   (01;
                                               = 2 (0);
non-terminals addr: con
              addr: Plus(con, reg)
              addr: Plus(con, Mul(Four, req)) = 5 (0);
              reg: Fetch(addr)
pattern -
              req: Assign(addr,req)
                                            = 7 (1);
              qoal: req
                                               = 8 (0);
```

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 - ► Done by a wrapper function reduce(NODEPTR_TYPE p, int goalInt) written by user around BURG generated functions.

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 - At each node selects a rule for evaluating the node.
 - Passes control back to user function with an integer identifying the rule. Actions corresponding to the rule to be managed by the user.

► Here is an outline of a code-generator produced

```
with the help of BURG. Constructs in red are BURG generated.
parse(NODEPTR TYPE p) {
  burg_label(p) /* label the tree */
  reduce(p, 1) /* and reduce it, qoal = 1*/
reduce(NODEPTR_TYPE p, int goalint) {
  int ruleno = burg rule(STATE LABEL(p), goalint);
  short *nts = burg nts[ruleno];
  NODEPTR TYPE kids[10];
  int i;
  /* ... do something with this node... */
  /* process the children of this node */
  burg kids(p, ruleno, kids);
  for (i = 0; nts[i]; i++)
    reduce(kids[i], nts[i]);
```