

CS738: Advanced Compiler Optimizations

Static Single Assignment (SSA)

Amey Karkare

karkare@cse.iitk.ac.in

<http://www.cse.iitk.ac.in/~karkare/cs738>
Department of CSE, IIT Kanpur



Agenda

- ▶ SSA Form
- ▶ Constructing SSA form
- ▶ Properties and Applications

SSA Form

- ▶ Developed by Ron Cytron, Jeanne Ferrante, Barry K. Rosen, Mark N. Wegman, and F. Kenneth Zadeck,
 - ▶ in 1980s while at IBM.
- ▶ *Static Single Assignment* – A variable is assigned only once in program text
 - ▶ May be assigned multiple times if program is executed

What is SSA Form?

- ▶ An Intermediate Representation
- ▶ Sparse representation
 - ▶ Definitions sites are directly associated with use sites
- ▶ Advantage
 - ▶ Directly access points where relevant data flow information is available

SSA IR

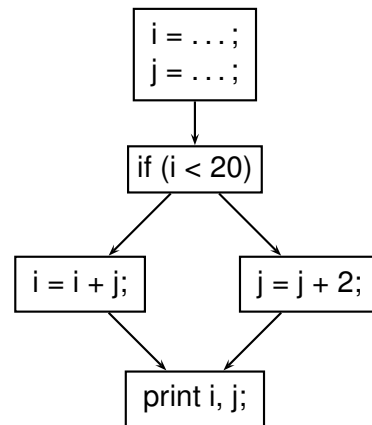
- ▶ In SSA Form
 - ▶ Each variable has exactly one definition
 - ⇒ A use of a variable is reached by exactly one definition
- ▶ Control flow like traditional programs
- ▶ Some *magic* is needed at *join* nodes

Example

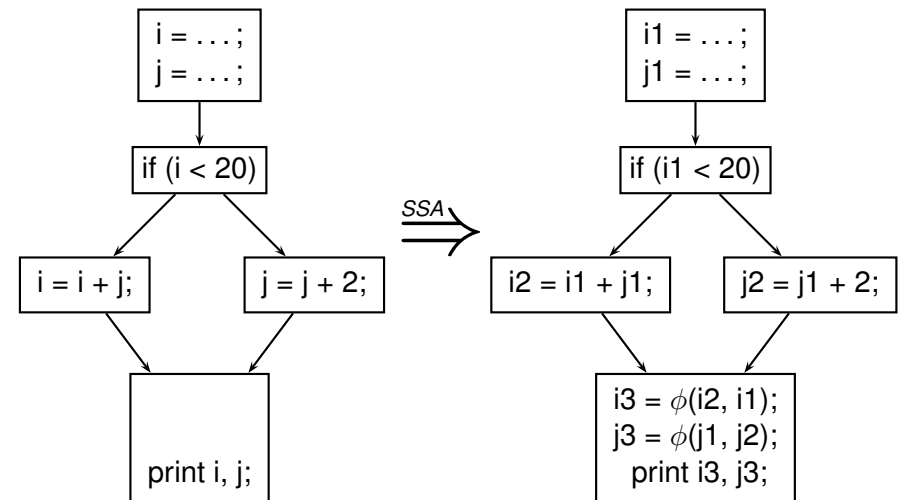
<pre>i = 0; ... i = i + 1; ... j = i * 5; ...</pre>	$\xRightarrow{\text{SSA}}$	<pre>i1 = 0; ... i2 = i1 + 1; ... j1 = i2 * 5; ...</pre>
---	----------------------------	--

SSA Example

```
i = ...;  
j = ...;  
if (i < 20)  
    i = i + j;  
else  
    j = j + 2;  
print i, j;
```



SSA Example



SSA Example

```
i = ...;
j = ...;
if (i < 20)
    i = i + j;
else
    j = j + 2;

print i, j;
```

SSA \Rightarrow

```
i1 = ...;
j1 = ...;
if (i1 < 20)
    i2 = i1 + j1;
else
    j2 = j1 + 2;
i3 =  $\phi$ (i2, i1);
j3 =  $\phi$ (j1, j2);
print i3, j3;
```

The *magic*: ϕ function

- ▶ ϕ is used for selection
 - ▶ One out of multiple values at join nodes
- ▶ Not every join node needs a ϕ
 - ▶ Needed only if multiple definitions reach the node
- ▶ Examples?

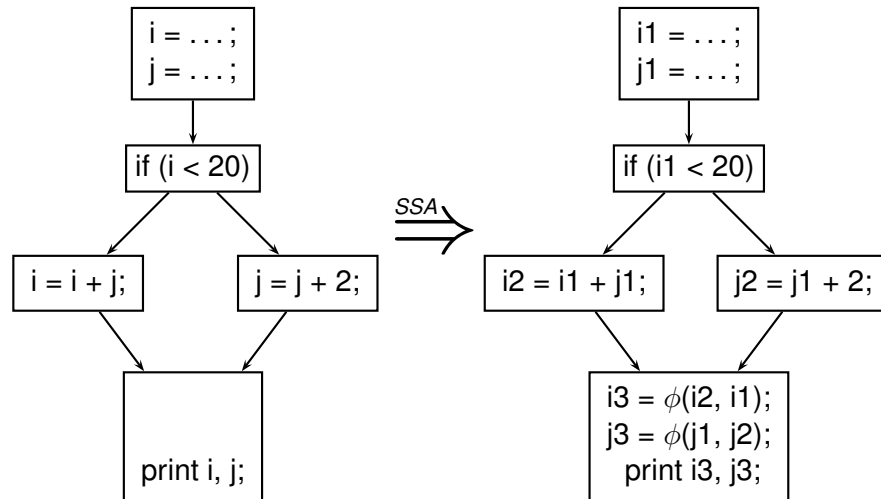
But... What is ϕ ?

- ▶ What does ϕ operation mean in a machine code?
- ▶ ϕ is a conceptual entity
- ▶ Statically equivalent to choosing one of the arguments “non-deterministically”
- ▶ No direct translation to machine code
 - ▶ typically mimicked using “copy” in predecessors
 - ▶ Inefficient
 - ▶ Practically, the inefficiency is compensated by dead code elimination and register allocation passes

Properties of ϕ

- ▶ Placed only at the entry of a join node
- ▶ Multiple ϕ -functions could be placed
 - ▶ for multiple variables
 - ▶ all such ϕ functions execute concurrently
- ▶ n -ary ϕ function at n -way join node
- ▶ gets the value of i -th argument if control enters through i -th edge
 - ▶ Ordering of ϕ arguments according to the edge ordering is important

SSA Example (revisit)



Construction of SSA Form

Assumptions

- ▶ Only scalar variables
 - ▶ Structures, pointers, arrays could be handled
 - ▶ Refer to publications

Dominators

- ▶ Nodes x and y in flow graph
- ▶ x **dominates** y if **every** path from *Entry* to y goes through x
 - ▶ $x \text{ dom } y$
 - ▶ partial order?
- ▶ x **strictly dominates** y if $x \text{ dom } y$ and $x \neq y$
 - ▶ $x \text{ sdom } y$

Computing Dominators

► Equation

$$\text{DOM}(n) = \{n\} \cup \left(\bigcap_{\substack{m \in \text{PRED}(n) \\ \forall n \in N}} \text{DOM}(m) \right),$$

► Initial Conditions:

$$\text{DOM}(n_{\text{Entry}}) = \{n_{\text{Entry}}\}$$

$$\text{DOM}(n) = N, \forall n \in N - \{n_{\text{Entry}}\}$$

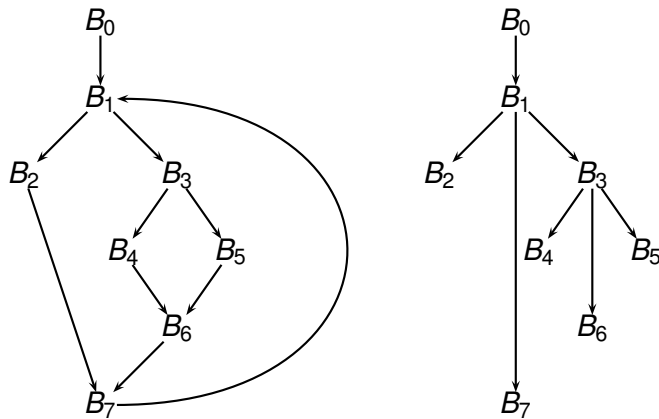
where N is the set of all nodes, n_{Entry} is the node corresponding to the *Entry* block.

► Note that efficient methods exist for computing dominators

Immediate Dominators and Dominator Tree

- x is **immediate dominator** of y if x is the *closest strict dominator* of y
 - unique, if it exists
 - denoted $\text{idom}[y]$
- Dominator Tree
 - A tree showing all immediate dominator relationships

Dominator Tree Example



Dominance Frontier: DF

- Dominance Frontier of x is set of all nodes y s.t.
 - x **dominates a predecessor** of y AND
 - x **does not strictly dominate** y
- Denoted $\text{DF}(x)$
- Why do you think $\text{DF}(x)$ is important for any x ?
 - Think about the information originated in x .

Computing DF

- ▶ $\text{PARENT}(x)$ denotes parent of node x in the dominator tree.
- ▶ $\text{CHILDREN}(x)$ denotes children of node x in the dominator tree.
- ▶ PRED and SUCC from CFG.

$$\text{DF}(x) = \text{DF}_{\text{local}}(x) \cup \left(\bigcup_{z \in \text{CHILDREN}(x)} \text{DF}_{\text{up}}(z) \right)$$

$$\text{DF}_{\text{local}}(x) = \{y \in \text{SUCC}(x) \mid \text{idom}[y] \neq x\}$$

$$\text{DF}_{\text{up}}(z) = \{y \in \text{DF}(z) \mid \text{idom}[y] \neq \text{PARENT}(z)\}$$

Iterated Dominance Frontier

- ▶ Transitive closure of Dominance frontiers on a set of nodes
- ▶ Let S be a set of nodes

$$\text{DF}(S) = \bigcup_{x \in S} \text{DF}(x)$$

$$\text{DF}^1(S) = \text{DF}(S)$$

$$\text{DF}^{i+1}(S) = \text{DF}(S \cup \text{DF}^i(S))$$

- ▶ $\text{DF}^+(S)$ is the fixed point of DF^i computation.

Minimal SSA Form Construction

- ▶ Compute DF^+ set for each flow graph node
- ▶ Place **trivial** ϕ -functions for each variable in the node
 - ▶ trivial ϕ -function at n -ary join: $x = \phi(\overbrace{x, x, \dots, x}^{n\text{-times}})$
- ▶ Rename variables
- ▶ **Why DF^+ ? Why not only DF ?**

Inserting ϕ -functions

```
foreach variable  $v$  {  
     $S = \text{Entry} \cup \{B_n \mid v \text{ defined in } B_n\}$   
    Compute  $\text{DF}^+(S)$   
    foreach  $n$  in  $\text{DF}^+(S)$  {  
        insert  $\phi$ -function for  $v$  at the start of  $B_n$   
    }  
}
```

Renaming Variables (Pseudo Code)

- ▶ Rename from the *Entry* node recursively
 - ▶ For each variable x , maintain a rename stack of $x \mapsto x_{\text{version}}$ mapping
- ▶ For node n
 - ▶ For each assignment $(x = \dots)$ in n
 - ▶ If non- ϕ assignment, rename any use of x with the Top mapping of x from the rename stack
 - ▶ Push the mapping $x \mapsto x_i$ on the rename stack
 - ▶ Replace lhs of the assignment by x_i
 - ▶ $i = i + 1$
- ▶ For the successors of n
 - ▶ Rename ϕ operands through SUCC edge index
- ▶ Recursively rename all child nodes in the dominator tree
- ▶ For each assignment $(x = \dots)$ in n
 - ▶ Pop $x \mapsto \dots$ from the rename stack