Interprocedural Data Flow Analysis

Uday P. Khedker

Department of Computer Science and Engineering, Indian Institute of Technology, Bombay



October 2009

Part 1

About These Slides

CS 618

Interprocedural DFA: About These Slides

CS 618

1/86

Interprocedural DFA: Outline

2/86

Outline

Copyright

These slides constitute the lecture notes for CS618 Program Analysis course at IIT Bombay and have been made available as teaching material accompanying the book:

 Uday Khedker, Amitabha Sanyal, and Bageshri Karkare. Data Flow Analysis: Theory and Practice. CRC Press (Taylor and Francis Group). 2009.

Apart from the above book, some slides are based on the material from the following books

• S. S. Muchnick and N. D. Jones. *Program Flow Analysis*. Prentice Hall Inc. 1981.

These slides are being made available under GNU FDL v1.2 or later purely for academic or research use.

- Issues in interprocedural analysis
- Functional approach
- The classical call strings approach
- Modified call strings approach

Part 3

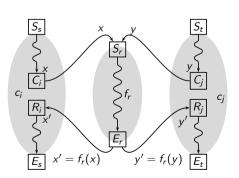
Issues in Interprocedural Analysis

CS 618

Interprocedural DFA: Issues in Interprocedural Analysis

4/86

Inherited and Synthesized Data Flow Information



	Х	Inherited by procedure r from call site c_i in procedure s		
	Inherited by procedure r from call site c_j in procedure t			
	x'	Synthesized by procedure r in s at call site procedure c_i		
17'		Synthesized by procedure r in t at call site procedure c_j		
•		· · · · · · · · · · · · · · · · · · ·		

Data Flow Information

Interprocedural Analysis: Overview

- Extends the scope of data flow analysis across procedure boundaries Incorporates the effects of
 - procedure calls in the caller procedures, and
 - calling contexts in the callee procedures.
- Approaches :
 - ▶ Generic : Call strings approach, functional approach.
 - ► Problem specific : Alias analysis, Points-to analysis, Partial redundancy elimination, Constant propagation



CS 618

Oct 2009

Interprocedural DFA: Issues in Interprocedural Analysis

5/86

Inherited and Synthesized Data Flow Information

• Example of uses of inherited data flow information

Answering questions about formal parameters and global variables:

- ▶ Which variables are constant?
- ▶ Which variables aliased with each other?
- ▶ Which locations can a pointer variable point to?
- Examples of uses of synthesized data flow information

Answering questions about side effects of a procedure call:

- Which variables are defined or used by a called procedure? (Could be local/global/formal variables)
- Most of the above questions may have a May or Must qualifier.



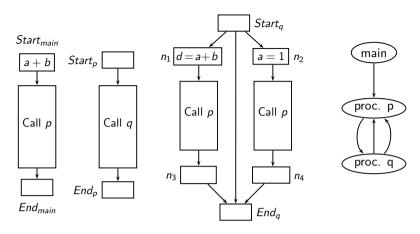
Oct 2009

IIT Bombay

Oct 2009

IIT Bombay

Program Rrepresentation for Interprocedural Data Flow Analysis: Call Multi-Graph



Supergraphs of procedures

Call multi-graph

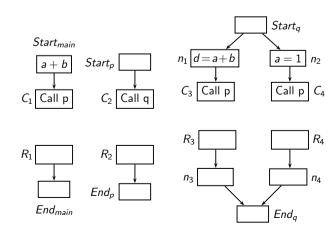
bay ()

Oct 2009

CS 618 Interprocedural DFA: Issues in Interprocedural Analysis

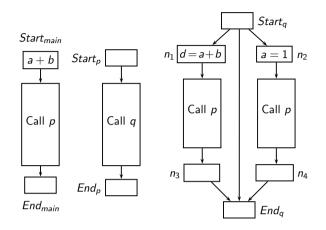
7/86

Program Rrepresentation for Interprocedural Data Flow Analysis: Supergraph



Day Day

Program Rrepresentation for Interprocedural Data Flow Analysis: Supergraph



Oct 2009

CS 618

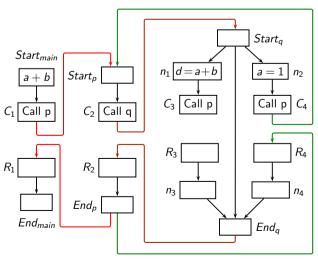
IIT Bombay

CS 618

Interprocedural DFA: Issues in Interprocedural Analysis

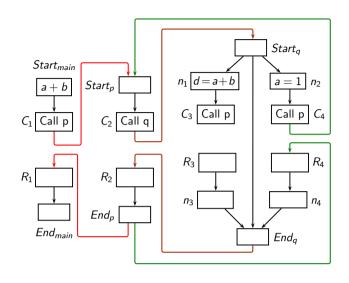
7/86

Program Rrepresentation for Interprocedural Data Flow Analysis: Supergraph





Program Rrepresentation for Interprocedural Data Flow Analysis: Supergraph



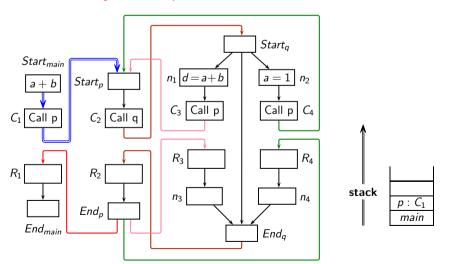
Oct 2009

CS 618

Interprocedural DFA: Issues in Interprocedural Analysis

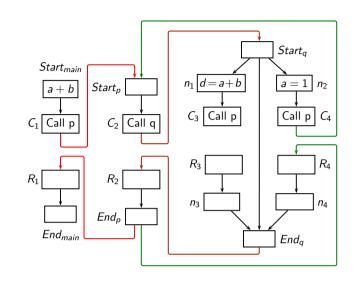
8/86

Validity of Interprocedural Control Flow Paths



Interprocedurally valid control flow path

Program Rrepresentation for Interprocedural Data Flow Analysis: Supergraph



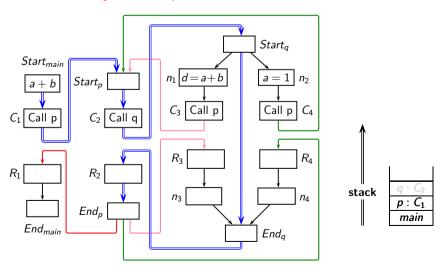
Oct 2009

CS 618

CS 618

8/86

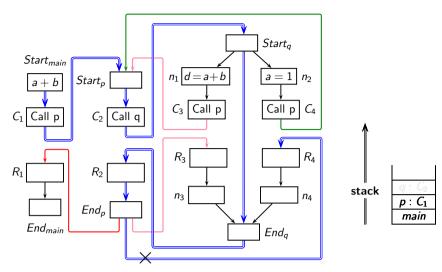
Interprocedural DFA: Issues in Interprocedural Analysis Validity of Interprocedural Control Flow Paths



Interprocedurally valid control flow path



Validity of Interprocedural Control Flow Paths



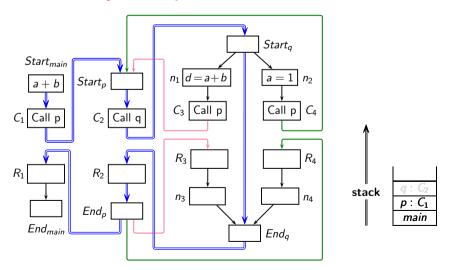
Interprocedurally invalid control flow path

Oct 2009

CS 618 Interprocedural DFA: Issues in Interprocedural Analysis

8/86

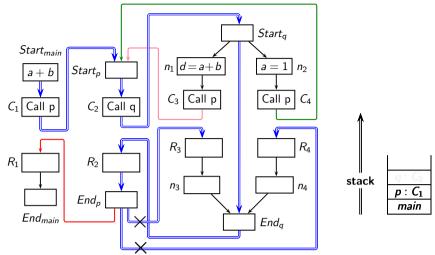
Validity of Interprocedural Control Flow Paths



Interprocedurally valid control flow path

CS 618

Validity of Interprocedural Control Flow Paths



Interprocedurally invalid control flow path

CS 618

Oct 2009

Oct 2009

Interprocedural DFA: Issues in Interprocedural Analysis

9/86

Safety, Precision, and Efficiency of Data Flow Analysis

A path which represents legal control flow

- Data flow analysis uses static representation of programs to compute summary information along paths
- Ensuring Safety. All valid paths must be covered
- Ensuring Precision . Only valid paths should be covered.
- Ensuring Efficency. Only relevant valid paths should be covered.

Subject to merging data flow values at shared program points without creating invalid paths

A path which yields information that affects the summary information.





Oct 2009

CS 618

Flow and Context Sensitivity

- Flow sensitive analysis: Considers intraprocedurally valid paths
- Context sensitive analysis:
 Considers interprocedurally valid paths
- For maximum statically attainable precision, analysis must be both flow and context sensitive.

MFP computation restricted to valid paths only

IIT B



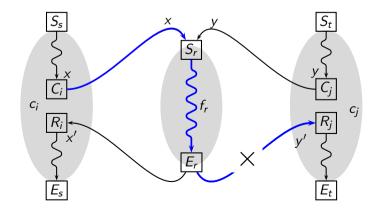
CS 618

Oct 2009

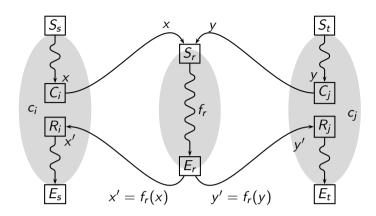
Interprocedural DFA: Issues in Interprocedural Analysis

11/86

Context Sensitivity in Interprocedural Analysis



Context Sensitivity in Interprocedural Analysis



Oct 2009

CS 618

IIT Bombay

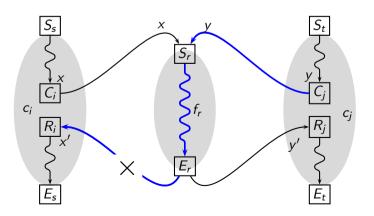
_

CS 618

Interprocedural DFA: Issues in Interprocedural Analysis

11/86

Context Sensitivity in Interprocedural Analysis

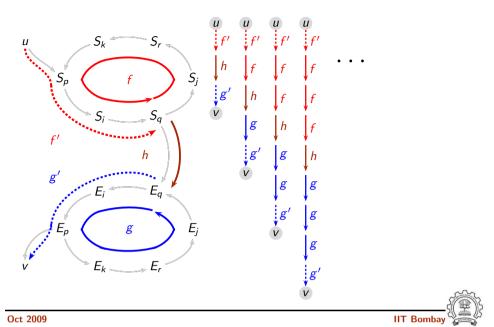






CS 618

Context Sensitivity in Presence of Recursion



CS 618 Interprocedural DFA: Issues in Interprocedural Analysis

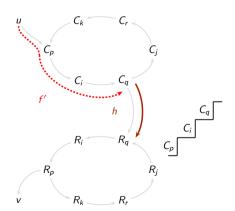
CS 618

13/86

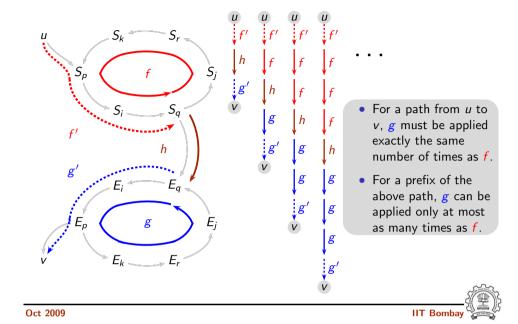
Interprocedural DFA: Issues in Interprocedural Analysis

13/86

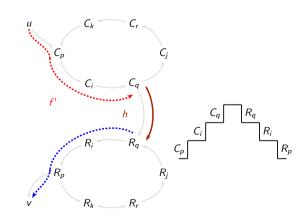
Staircase Diagrams of Interprocedurally Valid Paths



Context Sensitivity in Presence of Recursion



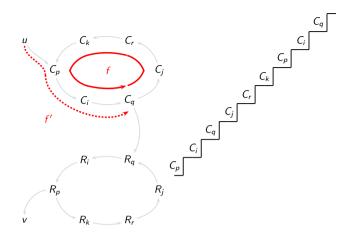
Staircase Diagrams of Interprocedurally Valid Paths







Staircase Diagrams of Interprocedurally Valid Paths

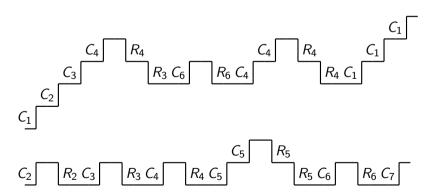


CS 618

Oct 2009

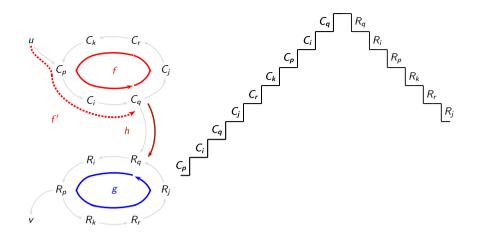
CS 618 Interprocedural DFA: Issues in Interprocedural Analysis 14/86

Staircase Diagrams of Interprocedurally Valid Paths



- "You can descend only as much as you have ascended!"
- Every descending step must match a corresponding ascending step.

Staircase Diagrams of Interprocedurally Valid Paths



Oct 2009

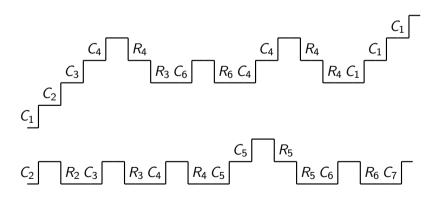
CS 618

CS 618

Interprocedural DFA: Issues in Interprocedural Analysis

14/86

Staircase Diagrams of Interprocedurally Valid Paths



- "You can descend only as much as you have ascended!"
- Every descending step must match a corresponding ascending step.





Flow Insensitivity in Data Flow Analysis

- Assumption: Statements can be executed in any order.
- Instead of computing point-specific data flow information, summary data flow information is computed.

The summary information is required to be a safe approximation of point-specific information for each point.

• $Kill_n(x)$ component is ignored. If statement n kills data flow information, there is an alternate path that excludes n.



Oct 2009

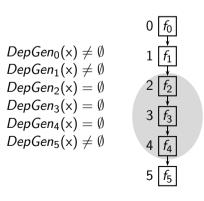
CS 618

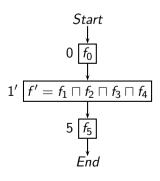
Interprocedural DFA: Issues in Interprocedural Analysis

17/86

Flow Insensitivity in Data Flow Analysis

If $DepGen_n(x) \neq \emptyset$ for some basic block



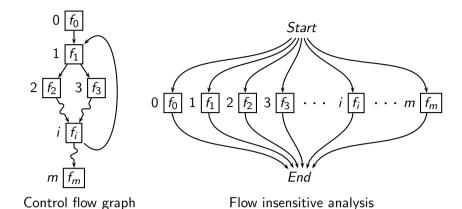


Control flow graph

Flow insensitive analysis

Flow Insensitivity in Data Flow Analysis

Assuming that $DepGen_n(x) = \emptyset$, and $Kill_n(X)$ is ignored for all n



Function composition is replaced by function confluence

CS 618

Oct 2009

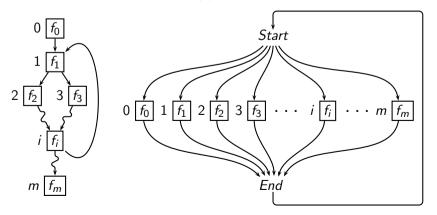
CS 618

Interprocedural DFA: Issues in Interprocedural Analysis

18/86

Flow Insensitivity in Data Flow Analysis

An alternative model if $DepGen_n(x) \neq \emptyset$



Allows arbitrary compositions of flow functions in any order ⇒ Flow insensitivity

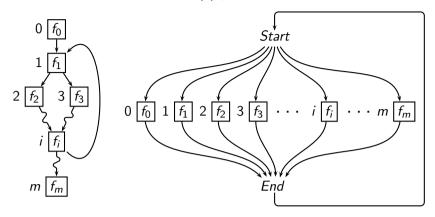




Oct 2009

Flow Insensitivity in Data Flow Analysis

An alternative model if $DepGen_n(x) \neq \emptyset$



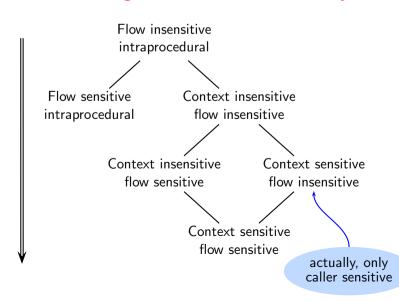
In practice, dependent constraints are collected in a global repository in one pass and then are solved independently

Oct 2009

CS 618 Interprocedural DFA: Issues in Interprocedural Analysis

20/86

Increasing Precision in Data Flow Analysis



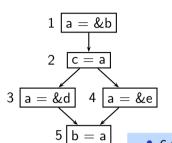
Oct 2009



Example of Flow Insensitive Analysis

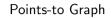
Flow insensitive points-to analysis

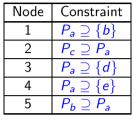
⇒ Same points-to information at each program point

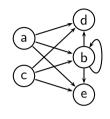


Program

Co	nst	raii	nts





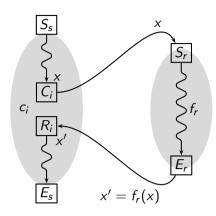


- c does not point to any location in block 1
- c does not point b in block 5
- b does not point to itself at any time

Part 4

Classical Functional Approach

Functional Approach



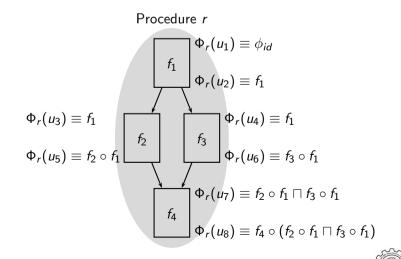
Oct 2009

CS 618 Interprocedural DFA: Classical Functional Approach

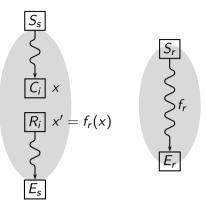
22/86

Notation for Summary Flow Function

For simplicity forward flow is assumed.



Functional Approach



- Compute summary flow functions for each procedure
- Use summary flow functions as the flow function for a call block

IIT Bombay

CS 618

Oct 2009

CS 618

Interprocedural DFA: Classical Functional Approach

23/86

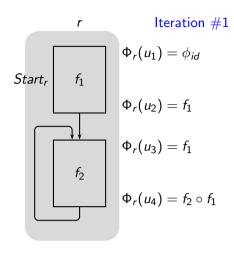
Constructing Summary Flow Function

For simplicity forward flow is assumed.

$$\Phi_r(\textit{Entry}(n)) \ = \ \begin{cases} \phi_{id} & \text{if n is $Start_r$} \\ \prod_{p \in \textit{pred}(n)} \left(\Phi_r(\textit{Exit}(p)) \right) & \text{otherwise} \end{cases}$$

$$\Phi_r(\textit{Exit}(n)) \ = \ \begin{cases} \Phi_s(u) \circ \Phi_r(\textit{Entry}(n)) & \text{if n calls procedure s} \\ f_n \circ \Phi_r(\textit{Entry}(n)) & \text{otherwise} \end{cases}$$

Interprocedural DFA: Classical Functional Approach Constructing Summary Flow Functions



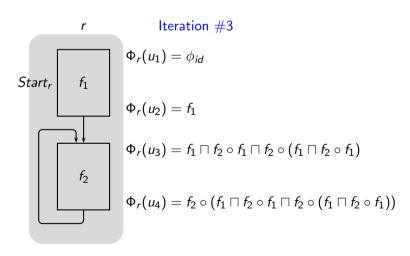
Oct 2009

CS 618

Interprocedural DFA: Classical Functional Approach

24/86

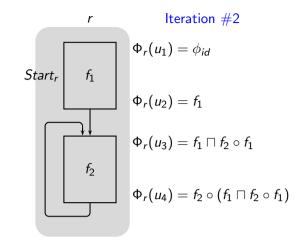
Constructing Summary Flow Functions



Termination is possible only if all function compositions and confluences can be reduced to a finite set of functions



Constructing Summary Flow Functions



Oct 2009

CS 618

IIT Bombay

CS 618

Interprocedural DFA: Classical Functional Approach

25/86

Lattice of Flow Functions for Live Variables Analysis

Component functions (i.e. for a single variable)

Lattice of data flow values	All possible flow functions	Lattice of flow functions
$ \widehat{\perp} = \emptyset $ $ \widehat{\perp} = \{a\} $	$ \begin{array}{c cccc} \operatorname{Gen}_n & \operatorname{Kill}_n & \widehat{f}_n \\ \emptyset & \emptyset & \widehat{\phi}_{id} \\ \emptyset & \{a\} & \widehat{\phi}_{\top} \\ \{a\} & \emptyset & \widehat{\phi}_{\perp} \\ \end{array} $	$\widehat{\phi}_{ op}$ \downarrow $\widehat{\phi}_{id}$ \downarrow $\widehat{\phi}_{\perp}$



Lattice of Flow Functions for Live Variables Analysis

Flow functions for two variables

$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	Lattice of data flow values	All possible flow functions	Lattice of flow functions
	{a} {b}	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\phi_{\top I} \qquad \phi_{I \top}$ $\phi_{I \perp} \qquad \phi_{\perp I}$ $\phi_{I \perp} \qquad \phi_{\perp I}$

Oct 2009

CS 618

Interprocedural DFA: Classical Functional Approach

28/86

Reducing Function Confluences

Assumption: No dependent parts (as in bit vector frameworks). $Kill_n$ is $ConstKill_n$ and Gen_n is $ConstGen_n$.

• When \sqcap is \cup .

$$\begin{array}{lcl} f_3(x) & = & f_2(x) \cup f_1(x) \\ & = & \left((x - \mathsf{Kill}_2) \cup \mathsf{Gen}_2 \right) \ \cup \ \left((x - \mathsf{Kill}_1) \cup \mathsf{Gen}_1 \right) \\ & = & \left(x - \left(\mathsf{Kill}_1 \cap \mathsf{Kill}_2 \right) \right) \ \cup \ \left(\mathsf{Gen}_1 \cup \mathsf{Gen}_2 \right) \end{array}$$

Hence.

$$Kill_3 = Kill_1 \cap Kill_2$$

 $Gen_3 = Gen_1 \cup Gen_2$

Reducing Function Compositions

Assumption: No dependent parts (as in bit vector frameworks). $Kill_n$ is $ConstKill_n$ and Gen_n is $ConstGen_n$.

$$f_3(x) = f_2(f_1(x))$$

$$= f_2((x - Kill_1) \cup Gen_1)$$

$$= (((x - Kill_1) \cup Gen_1) - Kill_2) \cup Gen_2$$

$$= (x - (Kill_1 \cup Kill_2)) \cup (Gen_1 - Kill_2) \cup Gen_2$$

Hence.

CS 618

$$\begin{aligned} \mathsf{Kill}_3 &=& \mathsf{Kill}_1 \cup \mathsf{Kill}_2 \\ \mathsf{Gen}_3 &=& \left(\mathsf{Gen}_1 - \mathsf{Kill}_2\right) \, \cup \, \mathsf{Gen}_2 \end{aligned}$$

Oct 2009



CS 618

Interprocedural DFA: Classical Functional Approach

29/86

Reducing Function Confluences

Assumption: No dependent parts (as in bit vector frameworks). $Kill_n$ is $ConstKill_n$ and Gen_n is $ConstGen_n$.

• When \sqcap is \cap .

$$\begin{array}{lcl} f_3(\mathsf{x}) & = & f_2(\mathsf{x}) \cap f_1(\mathsf{x}) \\ & = & \left((\mathsf{x} - \mathsf{Kill}_2) \cup \mathsf{Gen}_2 \right) \ \cap \ \left((\mathsf{x} - \mathsf{Kill}_1) \cup \mathsf{Gen}_1 \right) \\ & = & \left(\mathsf{x} - \left(\mathsf{Kill}_1 \cup \mathsf{Kill}_2 \right) \right) \ \cup \ \left(\mathsf{Gen}_1 \cap \mathsf{Gen}_2 \right) \end{array}$$

Hence

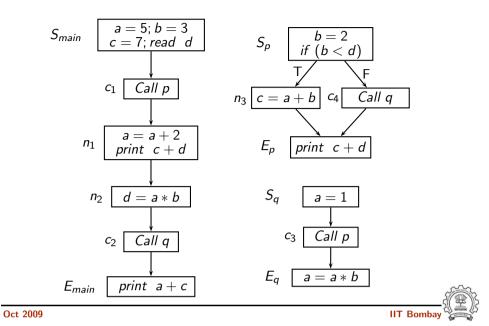
$$Kill_3 = Kill_1 \cup Kill_2$$

 $Gen_3 = Gen_1 \cap Gen_2$





An Example of Interprocedural Liveness Analysis



CS 618

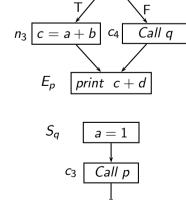
 S_p

CS 618

Interprocedural DFA: Classical Functional Approach

32/86

Computed Summary Flow Function



a = a * b

b = 2

if (b < d)

Sui	Summary Flow Function		
$\Phi_p(E_p)$	$BI_p \cup \{c,d\}$		
$\Phi_p(n_3)$	$(BI_p - \{c\}) \cup \{a, b, d\}$		
$\Phi_p(c_4)$	$(BI_p - \{a, b, c\}) \cup \{d\}$		
$\Phi_p(S_p)$	$(BI_p - \{b,c\}) \cup \{a,d\}$		
$\Phi_q(E_q)$	$\big(BI_q-\{a\}\big)\cup\{a,b\}$		
$\Phi_q(c_3)$	$(BI_q - \{a, b, c\}) \cup \{a, d\}$		
$\Phi_q(S_q)$	$(BI_q - \{a, b, c\}) \cup \{d\}$		

Summary Flow Functions for Interprocedural Liveness Analysis

Proc.	Flow Function	Defining ion Expression –		Iteration $\#1$		Changes in iteration #2	
Д	Function	Expression	Gen	Kill	Gen	Kill	
	$\Phi_{\rho}(E_{\rho})$	f_{E_p}	$\{c,d\}$	Ø			
p	$\Phi_p(n_3)$	$f_{n_3} \circ \Phi_p(E_p)$	$\{a,b,d\}$	{c}			
	$\Phi_p(c_4)$	$f_q \circ \Phi_p(E_p) = \phi_{\top}$	Ø	$\{a,b,c,d\}$	{ <i>d</i> }	$\{a,b,c\}$	
	$\Phi_p(S_p)$	$f_{S_p}\circ (\Phi_p(n_3)\sqcap \Phi_p(c_4))$	$\{a,d\}$	{ <i>b</i> , <i>c</i> }			
	f_p	$\Phi_p(S_p)$	$\{a,d\}$	{ <i>b</i> , <i>c</i> }			
	$\Phi_q(E_q)$	f_{E_q}	$\{a,b\}$	{a}			
q	$\Phi_q(c_3)$	$f_p \circ \Phi_q(E_q)$	$\{a,d\}$	$\{a,b,c\}$			
	$\Phi_q(S_q)$	$f_{S_q} \circ \Phi_q(c_3)$	{d}	$\{a,b,c\}$			
	f_q	$\Phi_q(S_q)$	{ <i>d</i> }	$\{a,b,c\}$			

Oct 2009

CS 618

IIT Bombay 🌋

CS 618

Interprocedural DFA: Classical Functional Approach

33/86

Result of Interprocedural Liveness Analysis

Data flow		Summary flow function		
variable	Name	Name Definition		
		Procedure <i>main</i> , $BI = \emptyset$		
In_{E_m}	$\Phi_m(E_m)$	$BI_m \cup \{a,c\}$	$\{a,c\}$	
In_{c_2}	$\Phi_m(c_2)$	$\big(BI_m-\{a,b,c\}\big)\cup\{d\}$	{ <i>d</i> }	
In _{n2}	$\Phi_m(n_2)$	$\big(BI_m-\{a,b,c,d\}\big)\cup\{a,b\}$	$\{a,b\}$	
In _{n1}	$\Phi_m(n_1)$	$(BI_m - \{a, b, c, d\}) \cup \{a, b, c, d\}$	$\{a,b,c,d\}$	
In_{c_1}	$\Phi_m(c_1)$	$\big(BI_m-\{a,b,c,d\}\big)\cup\{a,d\}$	$\{a,d\}$	
In _{Sm}	$\Phi_m(S_m)$	$BI_m - \{a, b, c, d\}$	Ø	





Result of Interprocedural Liveness Analysis

Data flow	Su	mmary flow function	Data flow		
variable	Name	Definition	value		
In _{E_p}	$\Phi_{\rho}(E_{\rho})$	$BI_p \cup \{c,d\}$	$\{a,b,\ c,d\}$		
In _{n3}	$\Phi_p(n_3)$	$(BI_p - \{c\}) \cup \{a, b, d\}$	$\{a,b,d\}$		
In _{C4}	$\Phi_p(c_4)$	$\big(BI_p-\{a,b,c\}\big)\cup\{d\}$	{ <i>d</i> }		
In_{S_p} $\Phi_p(S_p)$ $(BI_p - \{b,c\}) \cup \{a,d\}$		$\{a,d\}$			
	Procedure q , $BI = \{a, b, c, d\}$				
In _{Eq}			$\{a,b,c,d\}$		
In _{c3}	$\Phi_q(c_3)$	$(BI_q - \{a, b, c\}) \cup \{a, d\}$	$\{a,d\}$		
In _{Sq}	$\Phi_q(S_q)$	$\big(BI_q-\{a,b,c\}\big)\cup\{d\}$	{ <i>d</i> }		



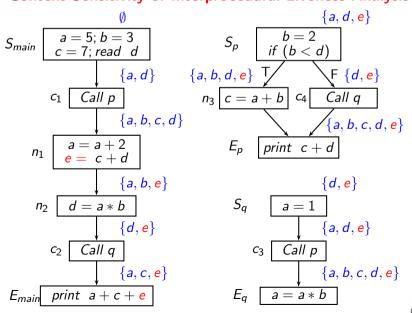
Oct 2009

CS 618

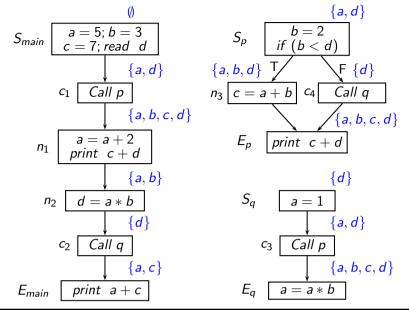
Interprocedural DFA: Classical Functional Approach

36/86

Context Sensitivity of Interprocedural Liveness Analysis



Interprocedural DFA: Classical Functional Approach Result of Interprocedural Liveness Analysis



Oct 2009

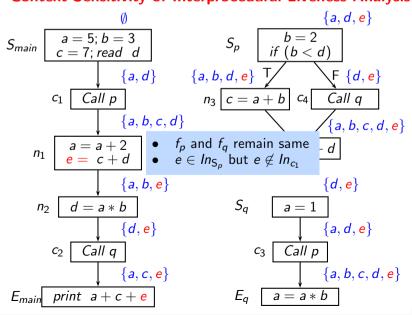
IIT Bombay

CS 618

Interprocedural DFA: Classical Functional Approach

36/86

Context Sensitivity of Interprocedural Liveness Analysis





Limitations of Functional Approach to Interprocedural Data Flow Analysis

- Problems with constructing summary flow functions
 - ▶ Reducing expressions defining flow functions may not be possible when $DepGen_n \neq \emptyset$
 - ▶ May work for some instances of some problems but not for all
- Enumeration based approach
 - ▶ Instead of constructing flow functions, remember the mapping $x \mapsto y$ as input output values
 - ► Reuse output value of a flow function when the same input value is encountered again

Requires the number of values to be finite



Oct 2009

CS 618

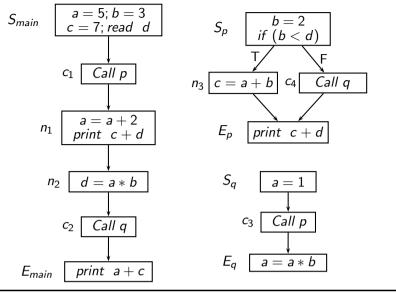
39/86

Summary Flow Functions for Interprocedural Constant Propagation

Interprocedural DFA: Classical Functional Approach

Flow Function	Iteration #1	Changes in iteration #2	Changes in iteration #3	Changes in iteration #4
$\Phi_p(E_p)$	$\langle v_a, 2, v_c, v_d \rangle$			
$\Phi_p(n_3)$	$\langle v_a, 2, v_a + 2, v_d \rangle$			
$\Phi_p(c_4)$	$\left\langle \widehat{T},\widehat{T},\widehat{T},\widehat{T}\right\rangle$	$\langle 2, 2, 3, v_d \rangle$	$\langle \widehat{\perp}, 2, 3, v_d \rangle$	$\left\langle \widehat{\perp},2,\widehat{\perp},v_{d}\right\rangle$
$\Phi_{\rho}(S_{\rho})$	$\langle v_a, 2, v_a + 2, v_d \rangle$	$\langle v_a \sqcap 2, 2, (v_a + 2) \sqcap 3, v_d \rangle$	$\left\langle \widehat{\perp}, 2, \widehat{\perp}, v_d \right\rangle$	
$\Phi_q(E_q)$	$\langle 1, v_b, v_c, v_d \rangle$			
$\Phi_q(c_3)$	$\langle 1, 2, 3, v_d \rangle$	$\langle \widehat{\perp}, 2, 3, v_d \rangle$	$\langle \widehat{\perp}, 2, \widehat{\perp}, v_d \rangle$	
$\Phi_q(S_q)$	$\langle 2, 2, 3, v_d \rangle$	$\langle \widehat{\perp}, 2, 3, v_d \rangle$	$\left\langle \widehat{\perp},2,\widehat{\perp},v_{d}\right\rangle$	

Functional Approach for Constant Propagation Example



Oct 2009

CS 618

IIT Bombay

CS 618

Interprocedural DFA: Classical Functional Approach

40.70

Interprocedural Constant Propagation Using the Functional Approach

Block	Out _n
S _m	$\left\langle 5,3,7,\widehat{\perp}\right angle$
<i>c</i> ₁	$\left\langle \widehat{\perp},2,\widehat{\perp},\widehat{\perp}\right angle$
n_1	$\left\langle \widehat{\perp},2,\widehat{\perp},\widehat{\perp}\right angle$
n_2	$\left\langle \widehat{\perp},2,\widehat{\perp},\widehat{\perp}\right angle$
<i>c</i> ₂	$\left\langle \widehat{\perp},2,\widehat{\perp},\widehat{\perp} \right angle$
E _m	$\left\langle \widehat{\perp},2,\widehat{\perp},\widehat{\perp} \right angle$

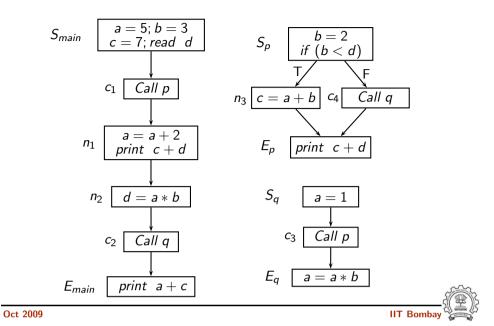
Block	Out _n
S_p	$\left\langle \widehat{\perp},2,\widehat{\perp},\widehat{\perp}\right angle$
n ₃	$\left\langle \widehat{\perp},2,\widehat{\perp},\widehat{\perp} \right angle$
C4	$\left\langle \widehat{\perp},2,\widehat{\perp},\widehat{\perp} \right angle$
E_p	$\left\langle \widehat{\perp},2,\widehat{\perp},\widehat{\perp} \right angle$
S_q	$\left\langle \widehat{\perp},2,\widehat{\perp},\widehat{\perp} \right angle$
<i>c</i> ₃	$\left\langle \widehat{\perp},2,\widehat{\perp},\widehat{\perp} \right angle$
E ₂	$\left\langle \widehat{\perp},2,\widehat{\perp},\widehat{\perp} \right angle$





41/86

Constant Propagation Using Functional Approach

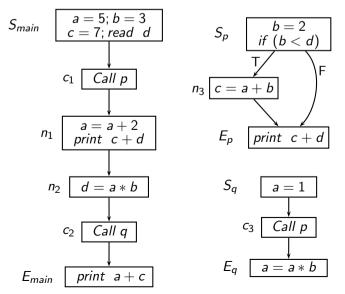


CS 618

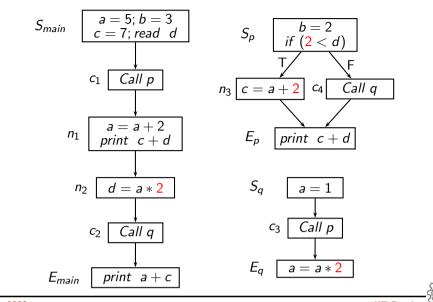
Interprocedural DFA: Classical Functional Approach

42/86

Tutorial Problem for Functional Interprocedural Analysis



Constant Propagation Using Functional Approach



Oct 2009

CS 618

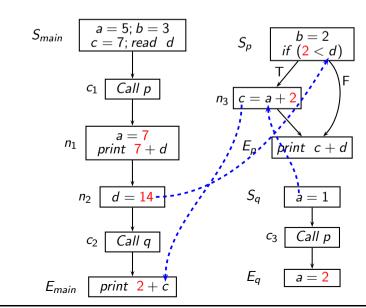
IIT Bombay

CS 618

Interprocedural DFA: Classical Functional Approach

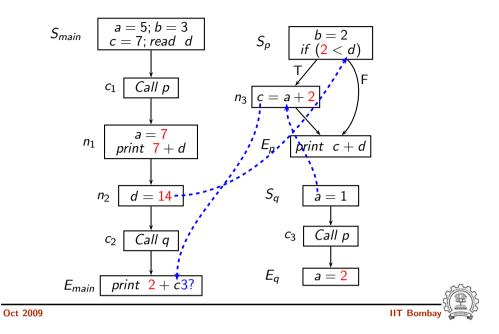
42/86

Tutorial Problem for Functional Interprocedural Analysis





Tutorial Problem for Functional Interprocedural Analysis



CS 618

Oct 2009

Interprocedural DFA: Classical Call Strings Approach

43/86

Classical Full Call Strings Approach

Most general, flow and context sensitive method

- Remember call history
 Information should be propagated back to the correct point
- Call string at a program point:
 - ▶ Sequence of *unfinished calls* reaching that point
 - Starting from the S_{main}

A snap-shot of call stack in terms of call sites



Part 5

Classical Call Strings Approach

CS 618

Interprocedural DFA: Classical Call Strings Approach

44/86

Interprocedural Data Flow Analysis Using Call Strings

- Tagged data flow information
 - ▶ IN_n and OUT_n are sets of the form $\{\langle \sigma, \mathsf{x} \rangle \mid \sigma \text{ is a call string }, \mathsf{x} \in L\}$
 - ▶ The final data flow information is

$$In_n = \prod_{\langle \sigma, \times \rangle \in \mathsf{IN}_n} \mathsf{x}$$

$$Out_n = \prod_{\langle \sigma, \times \rangle \in \mathsf{OUT}_n} \mathsf{x}$$

- Flow functions to manipulate tagged data flow information
 - ▶ Intraprocedural edges manipulate data flow value x
 - Interprocedural edges manipulate call string σ

IIT Bombay

Oct 2009

Overall Data Flow Equations

$$\begin{array}{rcl} \mathsf{IN}_n & = & \left\{ \begin{array}{cc} \langle \lambda, \mathit{BI} \rangle & \textit{n} \text{ is a } S_{\mathit{main}} \\ \biguplus & \mathsf{OUT}_p & \mathsf{otherwise} \end{array} \right. \\ \mathsf{OUT}_n & = & \mathit{DepGEN}_n \end{array}$$

Effectively, $ConstGEN_n = ConstKILL_n = \emptyset$ and $DepKILL_n(X) = X$.

$$X \uplus Y = \{ \langle \sigma, \mathsf{x} \sqcap \mathsf{y} \rangle \mid \langle \sigma, \mathsf{x} \rangle \in X, \ \langle \sigma, \mathsf{y} \rangle \in Y \} \cup \{ \langle \sigma, \mathsf{x} \rangle \mid \langle \sigma, \mathsf{x} \rangle \in X, \ \forall \mathsf{z} \in L, \langle \sigma, \mathsf{z} \rangle \notin Y \} \cup \{ \langle \sigma, \mathsf{y} \rangle \mid \langle \sigma, \mathsf{y} \rangle \in Y, \ \forall \mathsf{z} \in L, \langle \sigma, \mathsf{z} \rangle \notin X \}$$

(We merge underlying data flow values only if the contexts are same.)

Oct 2009

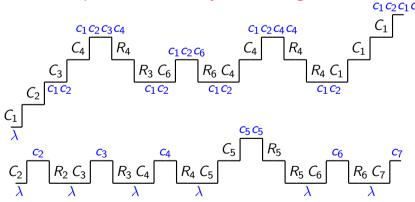


CS 618

Interprocedural DFA: Classical Call Strings Approach

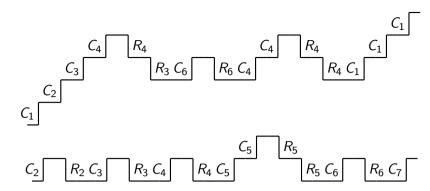
46/86

Interprocedural Validity and Calling Contexts



- "You can descend only as much as you have ascended!"
- Every descending step must match a corresponding ascending step.
- Calling context is represented by the remaining descending steps.

Interprocedural Validity and Calling Contexts



- "You can descend only as much as you have ascended!"
- Every descending step must match a corresponding ascending step.

Oct 2009

CS 618



CS 618

Interprocedural DFA: Classical Call Strings Approach

47/86

Manipulating Values

- Call edge $C_i \rightarrow S_p$ (i.e. call site c_i calling procedure p).
 - Append c_i to every σ .
 - Propagate the data flow values unchanged.

Ascend

- Return edge $E_p \to R_i$ (i.e. p returning the control to call site c_i).
 - ▶ If the last call site is *c_i*, remove it and propagate the data flow value unchanged.

Descend

Block other data flow values.

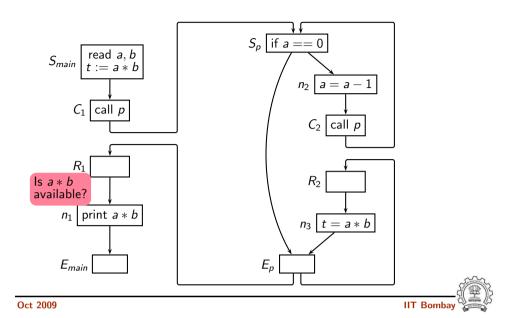
$$DepGEN_n(X) = \begin{cases} \left\{ \langle \sigma \cdot c_i, \mathsf{x} \rangle \mid \langle \sigma, \mathsf{x} \rangle \in X \right\} & n \text{ is } C_i \\ \left\{ \langle \sigma, \mathsf{x} \rangle \mid \langle \sigma \cdot c_i, \mathsf{x} \rangle \in X \right\} & n \text{ is } R_i \\ \left\{ \langle \sigma, f_n(\mathsf{x}) \rangle \mid \langle \sigma, \mathsf{x} \rangle \in X \right\} & \text{ otherwise} \end{cases}$$





Oct 2009

Available Expressions Analysis Using Call Strings Approach

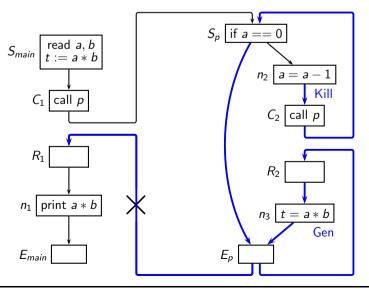


CS 618

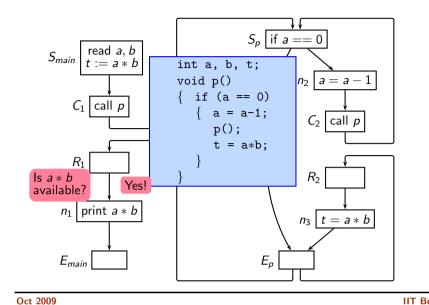
Interprocedural DFA: Classical Call Strings Approach

9/86

Available Expressions Analysis Using Call Strings Approach



Available Expressions Analysis Using Call Strings Approach



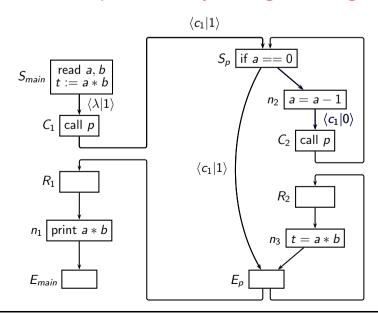
CS 618

CS 618

Interprocedural DFA: Classical Call Strings Approach

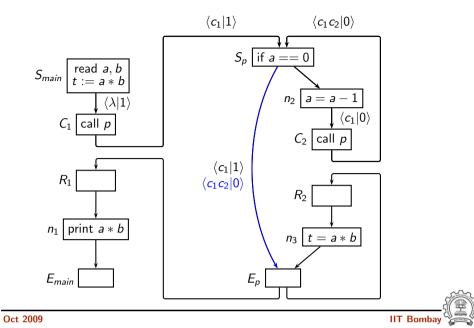
50/86

Available Expressions Analysis Using Call Strings Approach





Available Expressions Analysis Using Call Strings Approach



CS 618

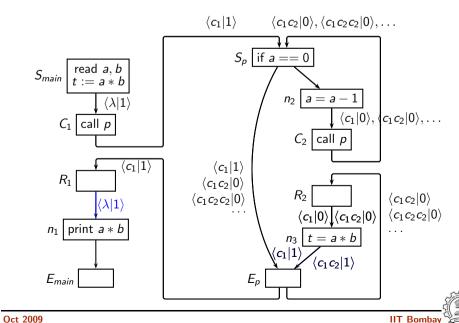
CS 618

Interprocedural DFA: Classical Call Strings Approach

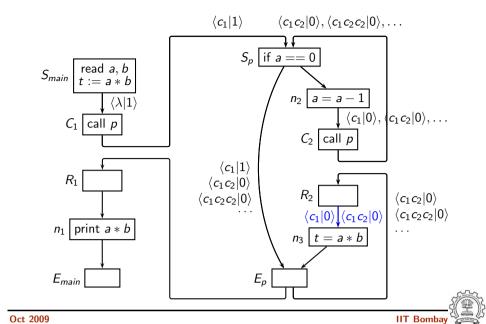
CS 618

50/86

Available Expressions Analysis Using Call Strings Approach



Available Expressions Analysis Using Call Strings Approach



Interprocedural DFA: Classical Call Strings Approach

51/86

Tutorial Problem

Generate a trace of the preceding example in the following format:

Step	Selected		ed Data	Remaining
No.	Node		Value	Work List
140.	Node	IN_n	OUT_n	VVOIK LIST

- Assume that call site c_i appended to a call string σ only if there are at most 2 occurrences of c_i in σ
- What about work list organization?



The Need for Multiple Occurrences of a Call Site

even if data flow values in cyclic call sequence do not change

3 : Gen Gen 4 1. int a.b.c: 2. void main() 8 c = a*b: p(); 5. 6. void p() 7 Path 1 12 Path 2 12 if (...) 9 { p(); 10: Kill 11 10: Kill Is a*b available? 12 11 10. a = a*b: 5 12 11. 9 12. 10 : Kill

Oct 2009

CS 618

Interprocedural DFA: Classical Call Strings Approach

54/86

The Need for Multiple Occurrences of a Call Site

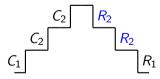
even if data flow values in cyclic call sequence do not change

In terms of staircase diagram

• Interprocedurally valid IFP

$$S_m, n_1, C_1, S_p, C_2, S_p, C_2, S_p, E_p, R_2, \stackrel{\text{Kill}}{n_2}, E_p, R_2, n_2$$

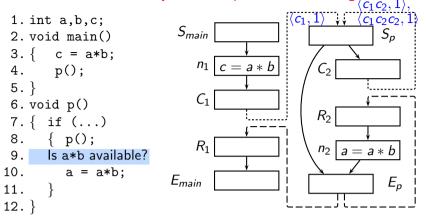
• You cannot descend twice, unless you ascend twice



• Even if the data flow values do not change while ascending, you need to ascend because they may change while descending

The Need for Multiple Occurrences of a Call Site

even if data flow values in cyclic call sequence do not change



Interprocedurally valid IFP

$$S_m, n_1, C_1, S_p, C_2, S_p, C_2, S_p, E_p, R_2, \stackrel{\text{Kill}}{n_2}, E_p, R_2, n_2$$

IIT Bombay

CS 618

Oct 2009

CS 618

Interprocedural DFA: Classical Call Strings Approach

55/86

Terminating Call String Construction

- For non-recursive programs: Number of call strings is finite
- For recursive programs: Number of call strings could be infinite Fortunately, the problem is decidable for finite lattices.
 - ► All call strings upto the following length *must be* constructed
 - $K \cdot (|L| + 1)^2$ for general bounded frameworks (L is the overall lattice of data flow values)
 - o $K \cdot (|\widehat{L}| + 1)^2$ for separable bounded frameworks $(\widehat{L} \text{ is the component lattice for an entity})$
 - o $K \cdot 3$ for bit vector frameworks
 - o 3 occurrences of any call site in a call string for bit vector frameworks
 - \Rightarrow Not a bound but prescribed necessary length
 - ⇒ Large number of long call strings





Classical Call String Length

Notation

- \blacktriangleright *IVP*(n, m): Interprocedurally valid path from block n to block m
- $CS(\rho)$: Number of call nodes in ρ that do not have the matching return node in ρ (length of the call string representing IVP(n, m))

Claim

Let $M = K \cdot (|L| + 1)^2$ where K is the number of distinct call sites in any call chain

Then, for any $\rho = IVP(S_{main}, m)$ such that $CS(\rho) > M$ $\exists \ \rho' = IVP(S_{main}, m) \ \text{such that}$ $CS(\rho') \leq M$, and $f_{\rho}(BI) = f_{\rho'}(BI)$.

 ρ , the longer path, is redundant for data flow analysis

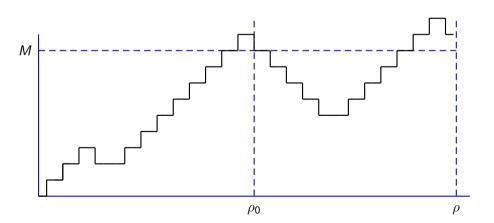


Oct 2009

CS 618

58/86

Interprocedural DFA: Classical Call Strings Approach **Classical Call String Length**



Classical Call String Length

Sharir-Pnueli [1981]

- Consider the smallest prefix ρ_0 of ρ such that $CS(\rho_0) > M$
- Consider a triple $\langle c_i, \alpha_i, \beta_i \rangle$ where
 - α_i is the data flow value reaching call node C_i along ρ and
 - \triangleright β_i is the data flow value reaching the corresponding return node R_i along ρ

If R_i is not in ρ , then $\beta_i = \Omega$ (undefined)

CS 618

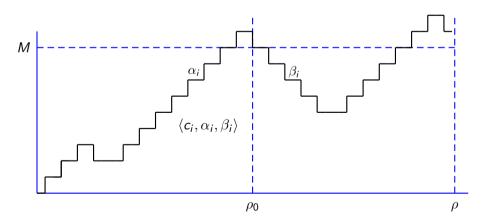
Oct 2009

CS 618

Interprocedural DFA: Classical Call Strings Approach

58/86

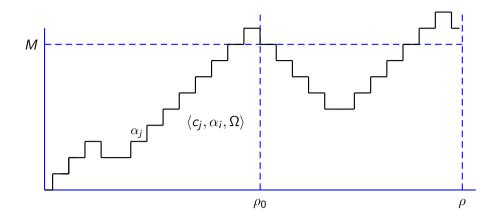
Classical Call String Length







Classical Call String Length

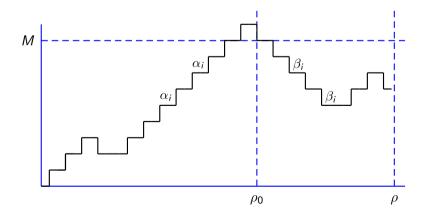


Oct 2009

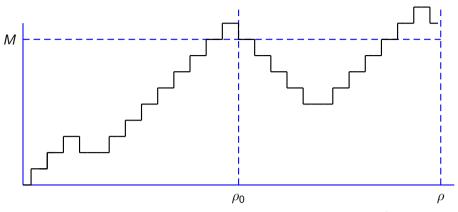
CS 618 Interprocedural DFA: Classical Call Strings Approach 59/86

Classical Call String Length

When β_i is not Ω



Classical Call String Length



- Number of distinct triples $\langle c_i, \alpha_i, \beta_i \rangle$ is $M = K \cdot (|L| + 1)^2$.
- There are at least two calls from the same call site that have the same effect on data flow values

Oct 2009

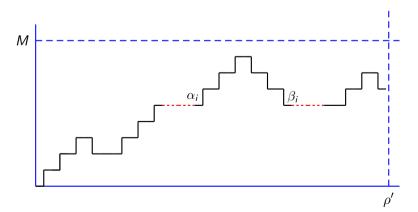
CS 618

Interprocedural DFA: Classical Call Strings Approach

59/86

Classical Call String Length

When β_i is not Ω

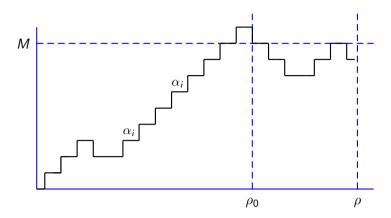






Classical Call String Length

When β_i is Ω



Oct 2009

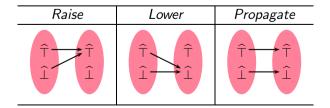
CS 618

Interprocedural DFA: Classical Call Strings Approach

61/86

Tighter Bound for Bit Vector Frameworks

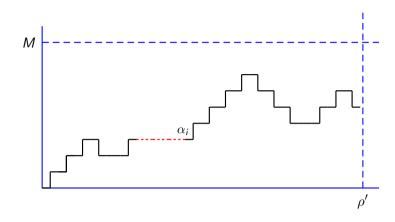
- \widehat{L} is $\{0,1\}$, L is $\{0,1\}^m$
- $\widehat{\sqcap}$ is either boolean AND or boolean OR
- $\widehat{\top}$ and $\widehat{\bot}$ are 0 or 1 depending on $\widehat{\sqcap}$.
- \hat{h} is a bit function and could be one of the following:



Classical Call String Length

When β_i is Ω

CS 618



Oct 2009

CS 618

Oct 2009

Interprocedural DFA: Classical Call Strings Approach

62/86

Tighter Bound for Bit Vector Frameworks

Karkare Khedker 2007

- Validity constraints are imposed by the presence of return nodes
- For every cyclic path consisting on Propagate functions, there exists an acyclic path consisting of Propagate functions
- Source of information is a Raise or Lower function
- Target of is a point reachable by a series of Propagate functions
- Identifies interesting path segments that we need to consider for determining a sufficient set of call strings





Relevant Path Segments for Tigher Bound for Bit Vector Frameworks

Which paths in a supergraph are sufficient to construct maximal call strings?

- All paths from C_i to R_i are abstracted away when a new call node C_i is to be suffixed to a call string
- We should consider maximal interprocedurally valid paths in which there is no path from a return node to a call node
- Consider all four combinations
- Case A: Source is a call node and target is a call node
- Case B: Source is a call node and target is a return node
- Case C: Source is a return node and target is also a return node
- Case D: Source is a return node and target is a call node: Not relevant



Oct 2009

CS 618

65/86

Interprocedural DFA: Classical Call Strings Approach Tighter Length for Bit Vector Frameworks

Case B:

Source is a call node C_S and target is some return node R_T

- $P(Entry \leadsto C_S \leadsto C_T \leadsto R_T)$
 - ▶ Call strings are derived from the paths $P(Entry \leadsto C_S \leadsto C_T \leadsto C_L)$ where C_L is the last call node
 - ▶ Thus there are three acyclic segments $P(Entry \leadsto C_S)$ $P(C_S \leadsto C_T)$, and $P(C_T \leadsto C_L)$
 - ► A call node may be shared in all three
 - ► At most 3 occurrences of a call site
- $P(Entry \leadsto C_T \leadsto C_S \leadsto R_S \leadsto R_T)$
 - C_T is required because of validity constraints
 - ▶ Call strings are derived from the paths $P(Entry \leadsto C_T \leadsto C_S \leadsto C_L)$ where C_I is the last call node
 - ► Again, there are three acyclic segments and at most 3 occurrences of a call site

Tighter Length for Bit Vector Frameworks

Case A:

CS 618

Source is a call node and target is also a call node $P(Entry \leadsto C_S \leadsto C_T)$

- No return node, no validity constraints
- Paths $P(Entry \leadsto C_S)$ and Paths $P(C_S \leadsto C_T)$ can be acyclic
- A call node may be common to both segments
- At most 2 occurrences of a call site

IIT Bombay

CS 618

Oct 2009

Interprocedural DFA: Classical Call Strings Approach

66/86

Tighter Length for Bit Vector Frameworks

Case C:

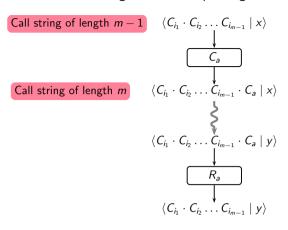
Source is a return node R_S and target is also some return node R_T

- $P(Entry \leadsto C_T \leadsto C_S \leadsto R_S \leadsto R_T)$
- C_T and C_S are required because of validity constraints
- Call strings are derived from the paths $P(Entry \leadsto C_T \leadsto C_S \leadsto C_L)$ where C_L is the last call node
- Again, there are three acyclic segments and at most 3 occurrences of a call site





• Maintain call string suffixes of upto a given length m.



Oct 2009

CS 618

Interprocedural DFA: Classical Call Strings Approach

67/86

Classical Approximate Approach

• Maintain call string suffixes of upto a given length m.

$$\langle C_{i_1} \cdot C_{i_2} \dots C_{i_m} \mid x_1 \rangle \qquad \langle C_{j_1} \cdot C_{i_2} \dots C_{i_m} \mid x_2 \rangle$$

$$\langle C_{i_2} \cdot C_{i_3} \dots C_{i_m} \cdot C_a \mid x_1 \sqcap x_2 \rangle$$

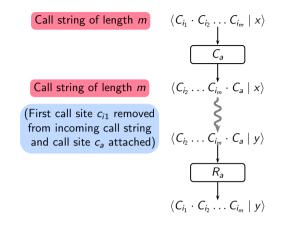
$$\langle C_{i_2} \cdot C_{i_3} \dots C_{i_m} \cdot C_a \mid y \rangle$$

$$\langle C_{i_1} \cdot C_{i_2} \dots C_{i_m} \mid y \rangle \qquad \langle C_{j_1} \cdot C_{i_2} \dots C_{i_m} \mid y \rangle$$

• Practical choices of *m* have been 1 or 2.

Classical Approximate Approach

• Maintain call string suffixes of upto a given length m.



Oct 2009

CS 618

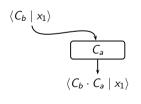
CS 618

Interprocedural DFA: Classical Call Strings Approach

68/86

Approximate Call Strings in Presence of Recursion

• For simplicity, assume m=2



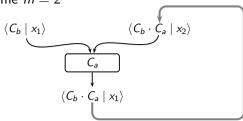






Approximate Call Strings in Presence of Recursion

• For simplicity, assume m=2



 R_a



Oct 2009

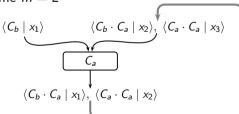
CS 618

Interprocedural DFA: Classical Call Strings Approach

68/86

Approximate Call Strings in Presence of Recursion

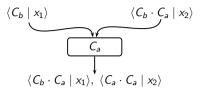
• For simplicity, assume m=2



 R_a

Approximate Call Strings in Presence of Recursion

• For simplicity, assume m=2



 R_a

Oct 2009

CS 618

IIT Bombay

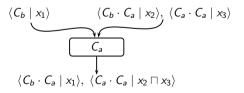
CS 618

Interprocedural DFA: Classical Call Strings Approach

68/86

Approximate Call Strings in Presence of Recursion

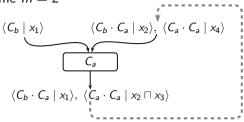
• For simplicity, assume m=2



 R_a

Approximate Call Strings in Presence of Recursion

• For simplicity, assume m=2



 R_a

Oct 2009

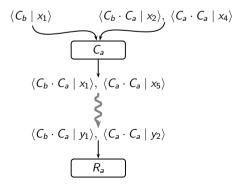
CS 618

Interprocedural DFA: Classical Call Strings Approach

68/86

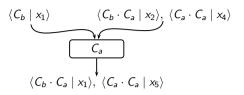
Approximate Call Strings in Presence of Recursion

• For simplicity, assume m=2



Approximate Call Strings in Presence of Recursion

• For simplicity, assume m=2



 R_a

Oct 2009

CS 618

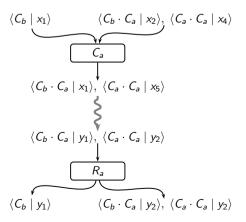
CS 618

Interprocedural DFA: Classical Call Strings Approach

68/86

Approximate Call Strings in Presence of Recursion

• For simplicity, assume m=2

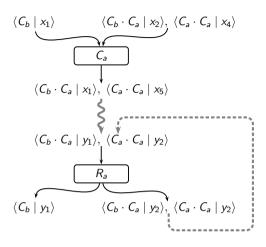






Approximate Call Strings in Presence of Recursion

• For simplicity, assume m=2



Oct 2009

CS 618 Interprocedural DFA: Modified Call Strings Method 69/86

An Overview

- Clearly identifies the exact set of call strings required.
- Value based termination of call string construction. No need to construct call strings upto a fixed length.
- Only as many call strings are constructed as are required.
- Significant reduction in space and time.
- Worst case call string length becomes linear in the size of the lattice instead of the original quadratic.

All this is achieved by a simple change without compromising on the precision, simplicity, and generality of the classical method.

Part 6

Modified Call Strings Method

CS 618

Interprocedural DFA: Modified Call Strings Method

70/86

The Limitation of the Classical Call Strings Method

Required langth of the call string is:

- *K* for non-recursive programs
- $K \cdot (|L| + 1)^2$ for recursive programs



Oct 2009

Oct 2009

- Use exactly the same method with this small change:
 - discard redundant call strings at the start of every procedure, and
 - simulate regeneration of call strings at the end of every procedure.
- Intuition:

- If σ_1 and σ_2 have equal values at S_p ,
- ▶ Then, since σ_1 and σ_2 are transformed in the same manner by traversing the same set of paths.
- ▶ The values associated with them will also be transformed in the same manner and will continue to remain equal at E_p .
- Can equivalence classes change?
 - ▶ During the analysis, equivalence classes may change in the sense that some call strings may move out of one class and may belong to some other class.
 - \triangleright However, the invariant that the equivalence classes are same at S_n and E_p still holds.

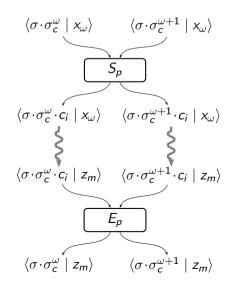
CS 618

Oct 2009

Interprocedural DFA: Modified Call Strings Method

73/86

Safety and Precision of Representation and Regeneration



Representation and Regeneration of Call Strings

• Let shortest (σ, u) denote the shortest call string which has the same value as σ at μ .

$$represent(\langle \sigma, x \rangle, S_p) = \langle shortest(\sigma, S_p), x \rangle$$

$$regenerate(\langle \sigma, y \rangle, E_p) = \{\langle \sigma', y \rangle \mid \sigma \text{ and } \sigma' \text{ have the same}$$

$$value \text{ at } S_p \}$$

- Correctness requirement: Whenever representation is performed at S_p , E_p must be added to the work list
- Efficiency consideration: Desirable order of processing of nodes Intraprocedural noddes → call nodes → return ndoes



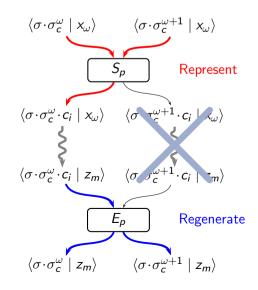
CS 618

Oct 2009

CS 618

Interprocedural DFA: Modified Call Strings Method

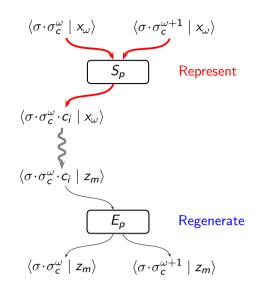
Safety and Precision of Representation and Regeneration







Interprocedural DFA: Modified Call Strings Method Safety and Precision of Representation and Regeneration



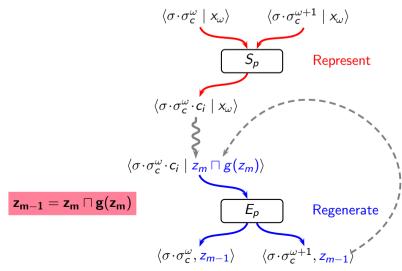
Oct 2009

CS 618

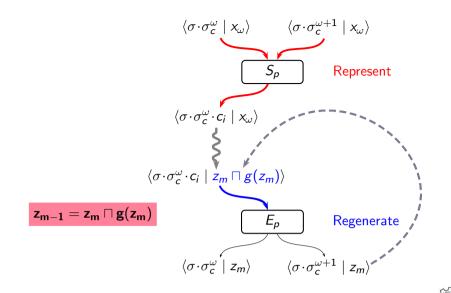
Interprocedural DFA: Modified Call Strings Method

73/86

Safety and Precision of Representation and Regeneration



Safety and Precision of Representation and Regeneration



Oct 2009

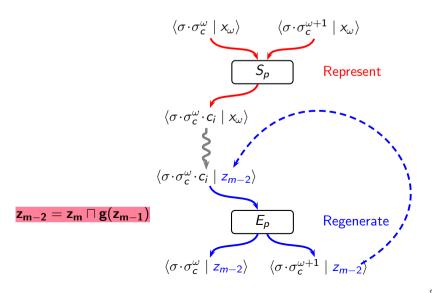
CS 618

CS 618

Interprocedural DFA: Modified Call Strings Method

73/86

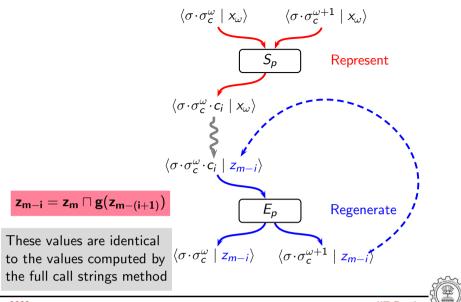
Safety and Precision of Representation and Regeneration







Safety and Precision of Representation and Regeneration



Oct 2009

CS 618

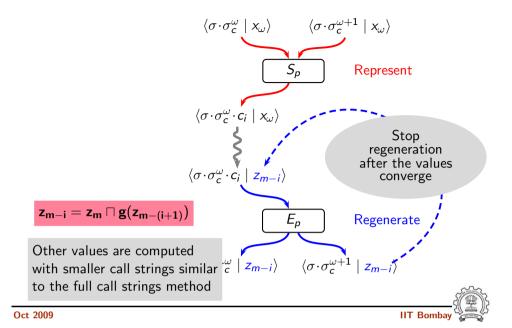
Interprocedural DFA: Modified Call Strings Method

74/86

Equivalence of The Two Methods

- For non-recursive programs, equivalence is obvious
- For recursive program, we prove equivalence using staircase diagrams

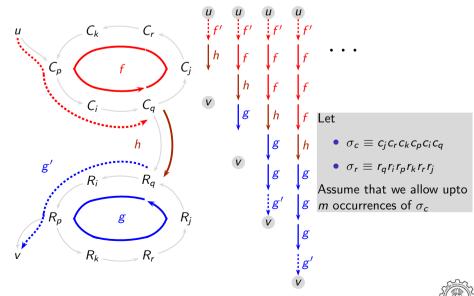
Safety and Precision of Representation and Regeneration



CS 618 Interprocedural DFA: Modified Call Strings Method

75/86

Call Strings for Recursive Contexts





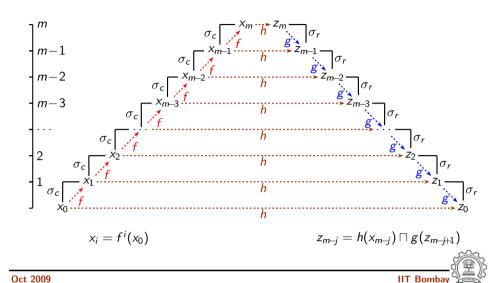
Oct 2009

IIT Bombay

Oct 2009

IIT Bombay

Computing Data Flow Values along Recursive Paths

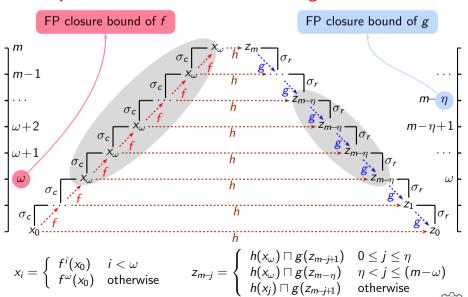


CS 618

Interprocedural DFA: Modified Call Strings Method

78/8

Computation of Data Flow Values along Recursive Paths



Fixed Bound Closure Bound of Flow Function

• n > 0 is the fixed point closure bound of $h: L \mapsto L$ if it is the smallest number such that

$$\forall x \in L, \ h^{n+1}(x) = h^n(x)$$

IIT B

IIT Bombay

CS 618

Oct 2009

CS 618

Interprocedural DFA: Modified Call Strings Method

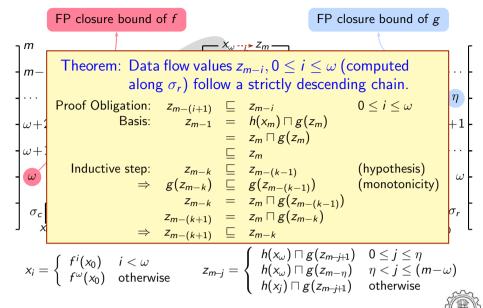
79/86

The Moral of the Story

- In the cyclic call sequence, computation begins from the first call string and influences successive call strings.
- In the cyclic return sequence, computation begins from the last call string and influences the preceding call strings.



Bounding the Call String Length Using Data Flow Values

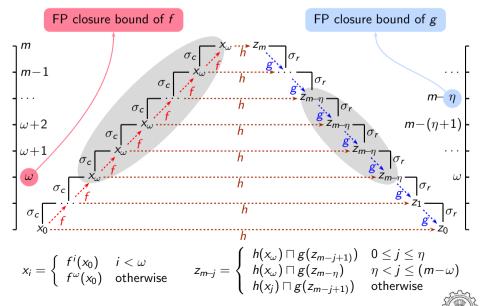


Oct 2009

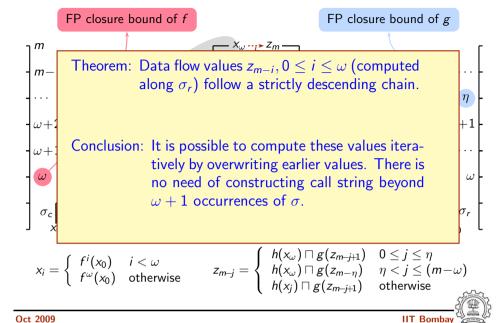
CS 618

Interprocedural DFA: Modified Call Strings Method

Bounding the Call String Length Using Data Flow Values



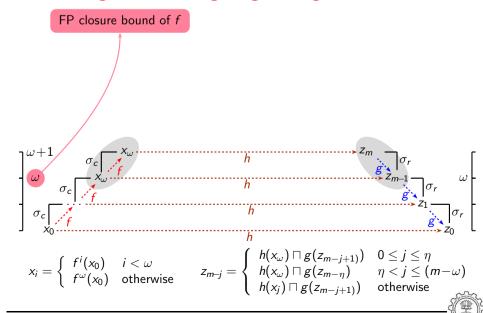
Bounding the Call String Length Using Data Flow Values



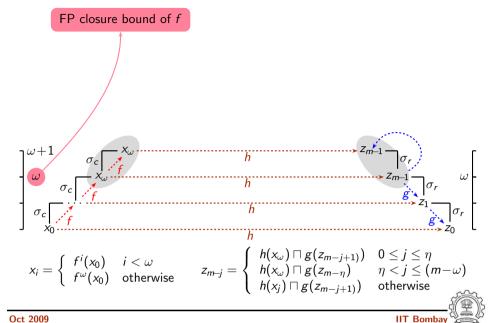
CS 618

Interprocedural DFA: Modified Call Strings Method

Bounding the Call String Length Using Data Flow Values



Bounding the Call String Length Using Data Flow Values

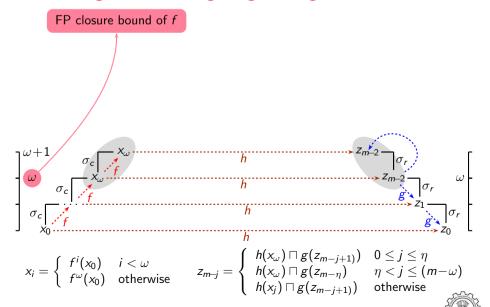


CS 618

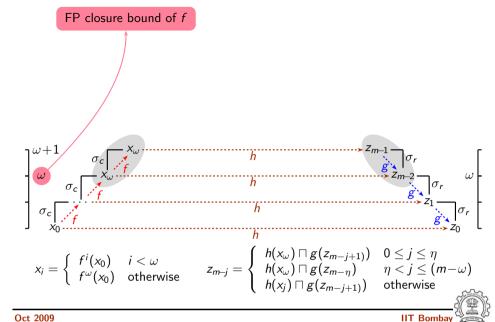
Interprocedural DFA: Modified Call Strings Method

81/80

Bounding the Call String Length Using Data Flow Values



Bounding the Call String Length Using Data Flow Values

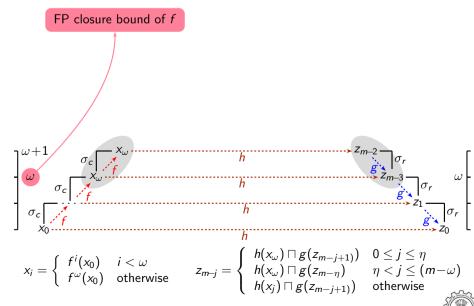


CS 618

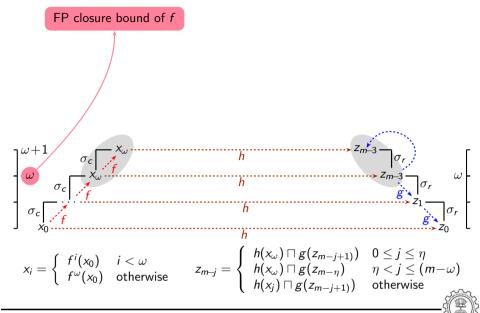
Interprocedural DFA: Modified Call Strings Method

81 /86

Bounding the Call String Length Using Data Flow Values



Bounding the Call String Length Using Data Flow Values

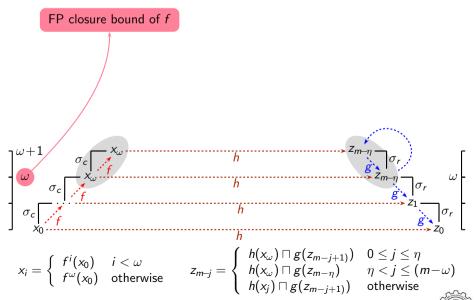


Oct 2009

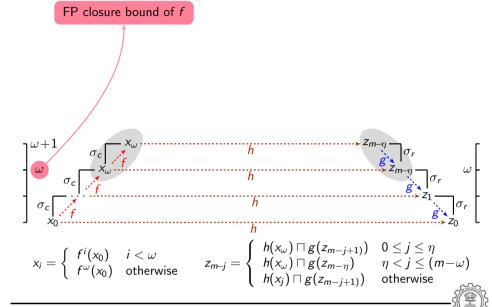
CS 618

Interprocedural DFA: Modified Call Strings Method

Bounding the Call String Length Using Data Flow Values



Bounding the Call String Length Using Data Flow Values



Oct 2009

CS 618

CS 618

Interprocedural DFA: Modified Call Strings Method

Worst Case Length Bound

- Consider a call string $\sigma = \dots (C_i)^1 \dots (C_i)^2 \dots (C_i)^3 \dots (C_i)^j \dots$ Let $j \ge |L| + 1$ Let C_i call procedure p
- All call string ending with C_i reach entry S_D
- Since only |L| distinct values are possible, by the pigeon hole principle, at least two prefixes ending with C_i will carry the same data flow value to S_p .
 - ► The longer prefix will get represented by the shorter prefix
 - \triangleright Since one more C_i is may be suffixed to discover fixed point, j < |L| + 1
- Worst case length in the proposed variant $= K \times (|L| + 1)$
- Original required length = $K \times (|L| + 1)^2$



Approximate Version

- For framework with infinite lattices, a fixed point for cyclic call sequence may not exist.
- Use a demand driven approach:
 - ▶ After a dynamically definable limit (say a number *j*),
 - ▶ Start merging the values and associate them with the last call string
 - Let

$$\sigma_j = \dots (C_i)^1 \dots (C_i)^2 \dots (C_i)^3 \dots (C_i)^j \dots$$

$$\sigma_{j+1} = \dots (C_i)^1 \dots (C_i)^2 \dots (C_i)^3 \dots (C_i)^j \dots (C_i)^{j+1} \dots$$

- $\begin{array}{l} \blacktriangleright \ \ \text{Represent} \ \langle \sigma_j \mid x_j \rangle \ \text{and} \ \langle \sigma_{j+1} \mid x_{j+1} \rangle \\ \ \ \text{by} \ \langle \sigma^j \mid x_j \sqcap x_{j+1} \rangle \end{array}$
- Context sensitive for a depth *j* of recursion. Context insensitive beyond that.
- Assumption: Height of the lattice is finite.



Oct 2009

CS 618

Interprocedural DFA: Modified Call Strings Method

85/86

Some Observations

- Compromising on precision may not be necessary for efficiency.
- Separating the necessary information from redundant information is much more significant.
- Data flow propagation in real programs seems to involve only a small subset of all possible values.
 Much fewer changes than the theoretically possible worst case number of changes.
- A precise modelling of the process of analysis is often an eye opener.

ay (a)

Reaching Definitions Analysis in GCC 4.0

Program	LoC	# <i>F</i>	# <i>C</i>	3K length bound				Proposed Approach		
				K	#CS	Max	Time	#CS	Max	Time
hanoi	33	2	4	4	100000+	99922	3973×10^{3}	8	7	2.37
bit_gray	53	5	11	7	100000+	31374	2705×10^{3}	17	6	3.83
analyzer	288	14	20	2	21	4	20.33	21	4	1.39
distray	331	9	21	6	96	28	322.41	22	4	1.11
mason	350	9	13	8	100000+	22143	432×10^{3}	14	4	0.43
fourinarow	676	17	45	5	510	158	397.76	46	7	1.86
sim	1146	13	45	8	100000+	33546	1427×10^{3}	211	105	234.16
181_mcf	1299	17	24	6	32789	32767	484×10^{3}	41	11	5.15
256_bzip2	3320	63	198	7	492	63	258.33	406	34	200.19

- LoC is the number of lines of code,
- #F is the number of procedures,
- #C is the number of call sites,
- #CS is the number of call strings
- Max denotes the maximum number of call strings reaching any node.
- Analysis time is in milliseconds.

(Implementation was carried out by Seema Ravandale.)

IIT Bombay

Oct 2009

CS 618

Oct 2009

Interprocedural DFA: Modified Call Strings Method

86/8

Tutorial Problem

Perform may points-to analysis using modified call strings method. Make conservative assumptions about must points-to information.

```
main()
{    x = &y;
    z = &x;
    y = &z;
    p(); /* C1 */
}

p()
{    if (...)
    {     p(); /* C2 */
        x = *x;
    }
}
```

- Number of distinct call sites in a call chain K = 2.
- Number of variables: 3
- Number of distinct points-to pairs: $3 \times 3 = 9$
- L is powerset of all points-to pairs
- $|L| = 2^9$
- Langth of the longest call string in Sharir-Pnueli method $2\times(|L|+1)^2=2^{19}+2^{10}+1=5,25,313$
- All call strings upto this length must be constructed by the Sharir-Pnueli method!

Bombay

Oct 2009

Tutorial Problem

Perform may points-to analysis using modified call strings method. Make conservative assumptions about must points-to information.

```
main()
{    x = &y;
    z = &x;
    y = &z;
    p(); /* C1 */
}

p()
{    if (...)
    {     p(); /* C2 */
        x = *x;
    }
}
```

• Modified call strings method requires only three call strings: λ , c_1 , and c_1c_2

