

Data Flow Analysis

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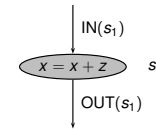
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Agenda

- **Intraprocedural Data Flow Analysis: Classical Examples**
 - Last lecture: Reaching Definitions
 - Today: Available Expressions
 - Discussion about the similarities/differences

AvE Analysis of a Structured Program



$$OUT(s_1) = IN(s_1) - KILL(s_1) \cup GEN(s_1)$$

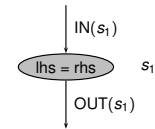
$$GEN(s_1) = \{x + z\}$$

$$KILL(s_1) = E_x$$

Incorrectly marks $x + z$ as available after s_1

$$GEN(s_1) = \emptyset \text{ for this case}$$

AvE Analysis of a Structured Program



$$OUT(s_1) = IN(s_1) - KILL(s_1) \cup GEN(s_1)$$

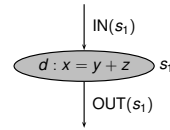
$$GEN(s_1) = \{rhs \mid lhs \text{ is not part of } rhs\}$$

$$KILL(s_1) = E_{lhs}$$

Available Expressions Analysis

- An expression e is available at a point p if
 - **Every** path from the *Entry* to p has at least one evaluation of e
 - There is no assignment to any component variable of e **after the last evaluation** of e prior to p
- Expression e is *generated* by its evaluation
- Expression e is *killed* by assignment to its component variables

AvE Analysis of a Structured Program



$$OUT(s_1) = IN(s_1) - KILL(s_1) \cup GEN(s_1)$$

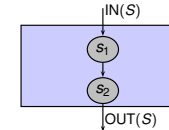
$$GEN(s_1) = \{y + z\}$$

$$KILL(s_1) = E_x$$

where E_x : set of all expression having x as a component

This may not work in general – WHY?

AvE Analysis of a Structured Program



$$GEN(S) = GEN(s_1) - KILL(s_2) \cup GEN(s_2)$$

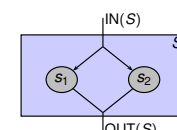
$$KILL(S) = KILL(s_1) - GEN(s_2) \cup KILL(s_2)$$

$$IN(s_1) = IN(S)$$

$$IN(s_2) = OUT(s_1)$$

$$OUT(S) = OUT(s_2)$$

AvE Analysis of a Structured Program



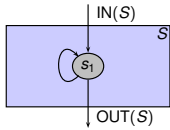
$$GEN(S) = GEN(s_1) \cap GEN(s_2)$$

$$KILL(S) = KILL(s_1) \cup KILL(s_2)$$

$$IN(s_1) = IN(s_2) = IN(S)$$

$$OUT(S) = OUT(s_1) \cap OUT(s_2)$$

AvE Analysis of a Structured Program



$$GEN(S) = GEN(s_1)$$

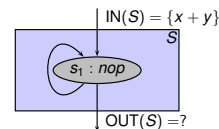
$$KILL(S) = KILL(s_1)$$

$$OUT(S) = OUT(s_1)$$

$$IN(s_1) = IN(S) \cap GEN(s_1) ?$$

$$IN(s_1) = IN(S) \cap OUT(s_1) ??$$

AvE Analysis of a Structured Program

Is $x + y$ available at $OUT(S)$?

AvE for Basic Blocks

- Expr e is available at the start of a block if
 - It is available at the end of all predecessors

$$IN(B) = \bigcap_{P \in \text{PRED}(B)} OUT(P)$$

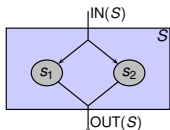
- Expr e is available at the end of a block if
 - Either it is generated by the block
 - Or it is available at the start of the block and not killed by the block

$$OUT(B) = IN(B) - KILL(B) \cup GEN(B)$$

Solving AvE Constraints

- KILL & GEN known for each BB.
- A program with N BBs has $2N$ equations with $2N$ unknowns.
 - Solution is possible.
 - Iterative approach (on the next slide).

AvE Analysis is Approximate



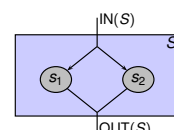
- Assumption: All paths are feasible.

- Example:

```
if (true) s1;
else s2;
```

Fact	Computed	Actual
$GEN(S)$	$GEN(s_1) \cap GEN(s_2)$	$\subseteq GEN(s_1)$
$KILL(S)$	$KILL(s_1) \cup KILL(s_2)$	$\supseteq KILL(s_1)$

AvE Analysis is Approximate



- Thus,

$$\text{true } GEN(S) \supseteq \text{analysis } GEN(S)$$

$$\text{true } KILL(S) \subseteq \text{analysis } KILL(S)$$

- Fewer expressions marked available than actually do!

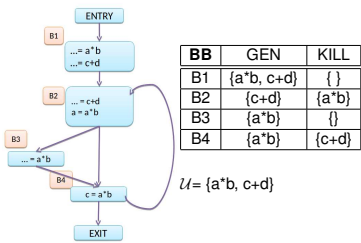
- Later we shall see that this is **SAFE** approximation
 - prevents optimizations
 - but NO wrong optimization

```
for each block B {
    OUT(B) = U; U = "universal" set of all exprs
}
OUT(Entry) = U; // remember reaching defs?
change = true;
while (change) {
    change = false;
    for each block B other than Entry {
        IN(B) = ∩_{P ∈ PRED(B)} OUT(P);
        oldOut = OUT(B);
        OUT(B) = IN(B) - KILL(B) ∪ GEN(B);
        if (OUT(B) ≠ oldOut) then {
            change = true;
        }
    }
}
```

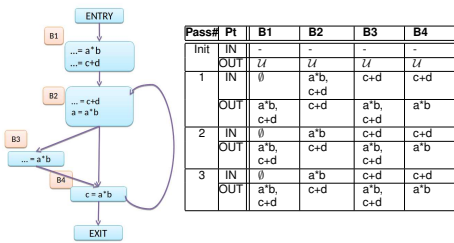
Some Issues

- What is U – the set of *all* expressions?
- How to compute it efficiently?
- Why *Entry* block is initialized differently?

Available Expressions: Example



Available Expressions: Example



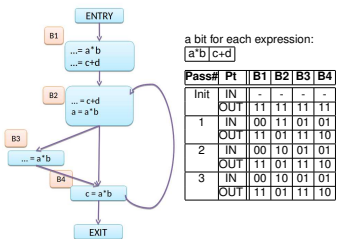
Available Expressions: Application

- Common subexpression elimination in a block B
 - Expression e available at the entry of B
 - e is also computed at a point p in B
 - Components of e are not modified from entry of B to p
- e is "upward exposed" in B
- Expressions generated in B are "downward exposed"

Comparison of RD and AvE

- Some* vs. *All* path property
- Meet operator: \cup vs. \cap
- Initialization of *Entry*: \emptyset
- Initialization of other BBs: \emptyset vs. \mathcal{U}
- Safety: "More" RD vs. "Fewer" AvE

Available Expressions: Bitvectors



Available Expressions: Bitvectors

- Set-theoretic definitions:

$$IN(B) = \bigcap_{P \in \text{PRED}(B)} OUT(P)$$

$$OUT(B) = IN(B) - KILL(B) \cup GEN(B)$$

- Bitvector definitions:

$$IN(B) = \bigwedge_{P \in \text{PRED}(B)} OUT(P)$$

$$OUT(B) = IN(B) \wedge \neg KILL(B) \vee GEN(B)$$

- Bitwise \vee, \wedge, \neg operators

AvE: alternate Initialization

- What if we Initialize:

$$OUT(B) = \emptyset, \forall B \text{ including } Entry$$

- Would we find "extra" available expressions?
 - More opportunity to optimize?
- OR would we miss some expressions that are available?
 - Loose on opportunity to optimize?

Live Variables

- A variable x is live at a point p if
 - There is a point p' along some path in the flow graph starting at p to the *Exit*
 - Value of x could be used at p'
 - There is no definition of x between p and p' along this path
- Otherwise x is dead at p

Live Variables: GEN

- $GEN(B)$: Set of variables whose values may be used in block B prior to any definition
 - Also called "use(B)"
- "upward exposed use" of a variable in B

Live Variables: KILL

- $KILL(B)$: Set of variables defined in block B prior to any use
 - Also called "def(B)"
- "upward exposed definition" of a variable in B

QQ

- Expression e is very busy at a point p if
 - Every** path from p to *Exit* has at least one evaluation of e and there is no assignment to any component variable of e before the first evaluation of e following p on these paths.
- Set up the data flow equations for Very Busy Expressions (VBE). You have to give equations for GEN, KILL, IN, and OUT.
- Think of an optimization/transformation that uses VBE analysis. Briefly describe it (2-3 lines only)
- Will your optimization be *safe* if we replace "*Every*" by "*Some*" in the definition of VBE?

Live Variables: Equations

- Set-theoretic definitions:

$$OUT(B) = \bigcup_{S \in \text{SUCC}(B)} IN(S)$$

$$IN(B) = OUT(B) - KILL(B) \cup GEN(B)$$

- Bitvector definitions:

$$OUT(B) = \bigvee_{S \in \text{SUCC}(B)} OUT(S)$$

$$IN(B) = OUT(B) \wedge \neg KILL(B) \vee GEN(B)$$

- Bitwise \vee, \wedge, \neg operators

Very Busy Expressions

- Expression e is very busy at a point p if
 - Every* path from p to *Exit* has at least one evaluation of e
 - On every path, there is no assignment to any component variable of e before the first evaluation of e following p
- Also called *Anticipable expression*