

## CS738: Advanced Compiler Optimizations

### Interprocedural Data Flow Analysis

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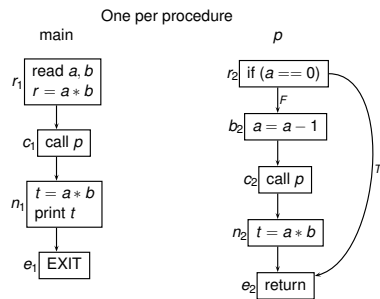
http://www.cse.iitk.ac.in/~karkare/cs738  
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#### Challenges

- Infeasible paths
- Recursion
- Function pointers and virtual functions
- Dynamic functions (functional programs)

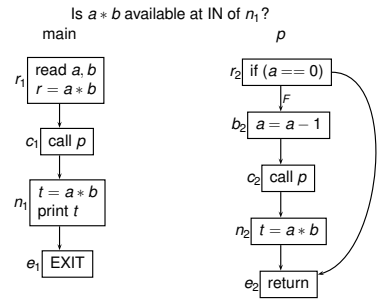
#### Control Flow Graph



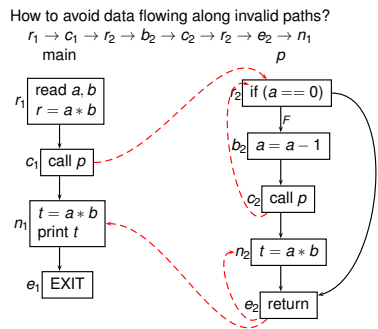
#### Assumptions

- Parameterless procedures, to ignore the problems of
  - *aliasing*
  - recursion stack for formal parameters
- No procedure variables (pointers, virtual functions etc.)

#### Interprocedural Analysis: Why?



#### Infeasible Paths



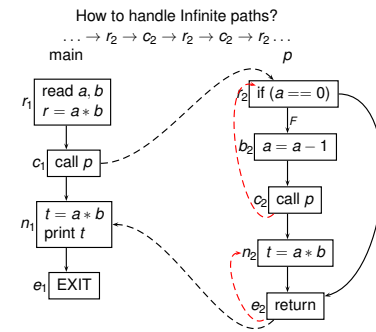
#### Control Flow Graph for Procedure $p$

- Single instruction basic blocks
- Unique exit block, denoted  $e_p$
- Unique entry block, denoted  $r_p$  (root block)
- Edge  $(m, n)$  if direct control transfer from (the end of) block  $m$  to (the start of) block  $n$
- Path:  $(n_1, n_2, \dots, n_k)$ 
  - $(n_i, n_{i+1}) \in \text{Edge set for } 1 \leq i < k$
  - $\text{path}_G(m, n)$ : Set of all path in graph  $G = (N, E)$  leading from  $m$  to  $n$

#### Data Flow Framework

- $(L, F)$ : data flow framework
- $L$ : a meet-semilattice
  - Largest element  $\Omega$
- $F$ : space of propagation functions
  - Closed under composition and meet
  - Contains  $id_L(x) = x$  and  $f_\Omega(x) = \Omega$
- $f_{(m,n)} \in F$  represents propagation function for edge  $(m, n)$  of control flow graph  $G = (N, E)$ 
  - Change of DF values from the *start* of  $m$ , through  $m$ , to the *start* of  $n$

#### Recursion



#### Two Approaches

- Functional approach
  - procedures as structured blocks
  - input-output relation (*functions*) for each block
  - *function* used at call site to compute the effect of procedure on program state
- Call-strings approach
  - single flow graph for whole program
  - value of interest tagged with the history of unfinished procedure calls

M. Sharir, and A. Pnueli. **Two Approaches to Inter-Procedural Data-Flow Analysis.**  
In Jones and Muchnik, editors, Program Flow Analysis: Theory and Applications.  
Prentice-Hall, 1981.

#### Data Flow Equations

$$x_r = \text{BoundaryInfo}$$

$$x_n = \bigwedge_{(m,n) \in E} f_{(m,n)}(x_m) \quad n \in N - r$$

- MFP solution, approximation of MOP

$$y_n = \bigwedge \{f_p(\text{BoundaryInfo}) : p \in \text{path}_G(r, n)\} \quad n \in N$$

#### Functional Approach

- Procedures treated as structures of blocks
- Computes relationship between DF value at entry node and related data at *any* internal node of procedure
- At call site, DF value propagated directly using the computed relation

#### Function Variables

- Target of a function can not be determined statically
- Function Pointers (including virtual functions)
 

```
double (*fun)(double arg);
...
if (cond)
    fun = sqrt;
else
    fun = fabs;
...
fun(x);
```
- Dynamically created functions (in functional languages)
- No static control flow graph!

### Notations and Terminology

### Functional Approach to Interprocedural Analysis

First Representation:

$$G = \bigcup \{G_p : p \text{ is a procedure in program}\}$$

$$G_p = (N_p, E_p, r_p)$$

$$N_p = \text{set of all basic block of } p$$

$$r_p = \text{root block of } p$$

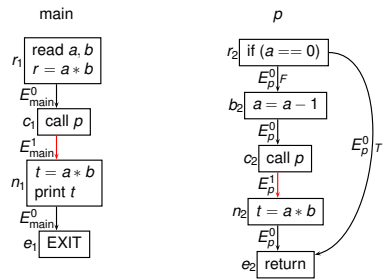
$$E_p = \text{set of edges of } p$$

$$= E_p^0 \cup E_p^1$$

$$(m, n) \in E_p^0 \Leftrightarrow \text{direct control transfer from } m \text{ to } n$$

$$(m, n) \in E_p^1 \Leftrightarrow m \text{ is a call block, and } n \text{ immediately follows } m$$

## Interprocedural Flow Graph: 1<sup>st</sup> Representation



## Interprocedural Flow Graph

Second representation

$$\begin{aligned}
 G^* &= (N^*, E^*, r_1) \\
 r_1 &= \text{root block of main} \\
 N^* &= \bigcup_p N_p \\
 E^* &= E^0 \cup E^1 \\
 E^0 &= \bigcup_p E_p^0 \\
 (m, n) \in E^1 &\Leftrightarrow (m, n) \text{ is either a call edge or a return edge}
 \end{aligned}$$

## Interprocedurally Valid Paths

- ▶  $G^*$  ignores the special nature of call and return edges
- ▶ Not all paths in  $G^*$  are feasible
  - ▶ do not represent potentially valid execution paths
- ▶  $IVP(r_1, n)$ : set of all interprocedurally valid paths from  $r_1$  to  $n$
- ▶ Path  $q \in \text{path}_{G^*}(r_1, n)$  is in  $IVP(r_1, n)$ 
  - ▶ iff sequence of all  $E^1$  edges in  $q$  (denoted  $q_1$ ) is proper

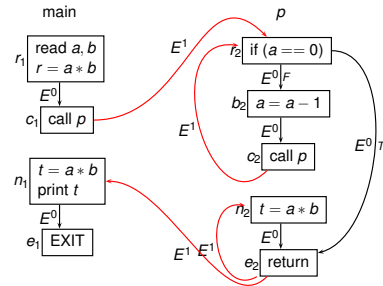
## Proper sequence

- ▶  $q_1$  without any return edge is proper
- ▶ let  $q_1[i]$  be the first return edge in  $q_1$ .  $q_1$  is proper if
  - ▶  $i > 1$ ; and
  - ▶  $q_1[i-1]$  is call edge corresponding to  $q_1[i]$ ; and
  - ▶  $q_1'$  obtained from deleting  $q_1[i-1]$  and  $q_1[i]$  from  $q_1$  is proper

## Interprocedural Flow Graph

- ▶ Call edge  $(m, n)$ :
  - ▶  $m$  is a call block, say calling  $p$
  - ▶  $n$  is root block of  $p$
- ▶ Return edge  $(m, n)$ :
  - ▶  $m$  is an exit block of  $p$
  - ▶  $n$  is a block immediately following a call to  $p$
- ▶ Call edge  $(m, r_p)$  corresponds to return edge  $(e_q, n)$ 
  - ▶ if  $p = q$  and
  - ▶  $(m, n) \in E_s^1$  for some procedure  $s$

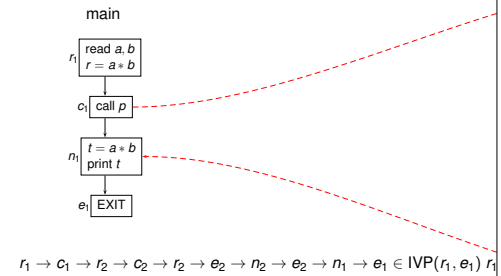
## Interprocedural Flow Graph: 2<sup>nd</sup> Representation



## Interprocedurally Valid Complete Paths

- ▶  $IVP_0(r_p, n)$  for procedure  $p$  and node  $n \in N_p$
- ▶ set of all interprocedurally valid paths  $q$  in  $G^*$  from  $r_p$  to  $n$  s.t.
  - ▶ Each call edge has corresponding return edge in  $q$  restricted to  $E^1$

## IVPs



## Path Decomposition

$$\begin{aligned}
 q &\in IVP(r_{\text{main}}, n) \\
 \Leftrightarrow \\
 q &= q_1 \parallel (c_1, r_{p_2}) \parallel q_2 \parallel \dots \parallel (c_{j-1}, r_{p_j}) \parallel q_j \\
 &\quad \text{where for each } i < j, q_i \in IVP_0(r_{p_i}, c_i) \text{ and } q_j \in IVP_0(r_{p_j}, n)
 \end{aligned}$$