

CS738: Advanced Compiler Optimizations

Data Flow Analysis

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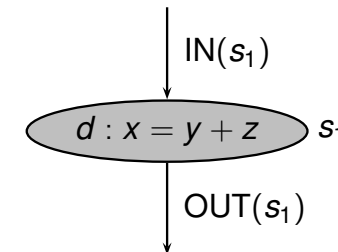
Agenda

- ▶ *Intraprocedural* Data Flow Analysis: Classical Examples
 - ▶ Last lecture: Reaching Definitions
 - ▶ Today: Available Expressions
 - ▶ Discussion about the similarities/differences

Available Expressions Analysis

- ▶ An expression e is available at a point p if
 - ▶ **Every** path from the *Entry* to p has at least one evaluation of e
 - ▶ There is no assignment to any component variable of e **after the last evaluation** of e prior to p
- ▶ Expression e is *generated* by its evaluation
- ▶ Expression e is *killed* by assignment to its component variables

AvE Analysis of a Structured Program



$$OUT(s_1) = IN(s_1) - KILL(s_1) \cup GEN(s_1)$$

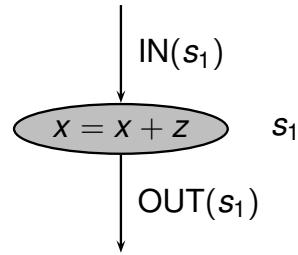
$$GEN(s_1) = \{y + z\}$$

$$KILL(s_1) = E_x$$

where E_x : set of all expression having x as a component

This may not work in general – WHY?

AvE Analysis of a Structured Program



$$\text{OUT}(s_1) = \text{IN}(s_1) - \text{KILL}(s_1) \cup \text{GEN}(s_1)$$

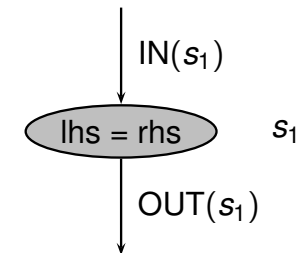
$$\text{GEN}(s_1) = \{x + z\}$$

$$\text{KILL}(s_1) = E_x$$

Incorrectly marks $x + z$ as available after s_1

$$\text{GEN}(s_1) = \emptyset \text{ for this case}$$

AvE Analysis of a Structured Program

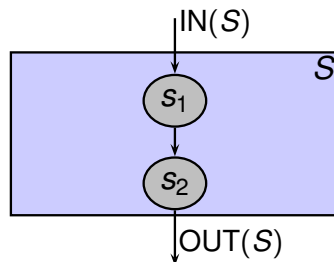


$$\text{OUT}(s_1) = \text{IN}(s_1) - \text{KILL}(s_1) \cup \text{GEN}(s_1)$$

$$\text{GEN}(s_1) = \{\text{rhs} \mid \text{lhs is not part of rhs}\}$$

$$\text{KILL}(s_1) = E_{\text{lhs}}$$

AvE Analysis of a Structured Program



$$\text{GEN}(S) = \text{GEN}(s_1) - \text{KILL}(s_2) \cup \text{GEN}(s_2)$$

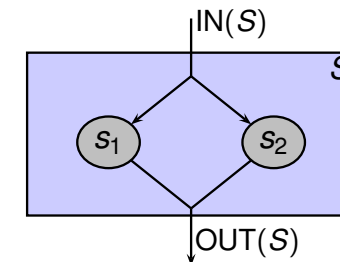
$$\text{KILL}(S) = \text{KILL}(s_1) - \text{GEN}(s_2) \cup \text{KILL}(s_2)$$

$$\text{IN}(s_1) = \text{IN}(S)$$

$$\text{IN}(s_2) = \text{OUT}(s_1)$$

$$\text{OUT}(S) = \text{OUT}(s_2)$$

AvE Analysis of a Structured Program



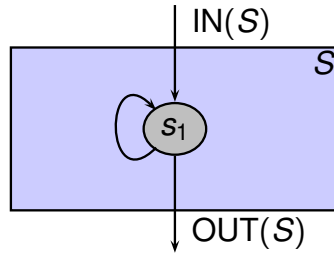
$$\text{GEN}(S) = \text{GEN}(s_1) \cap \text{GEN}(s_2)$$

$$\text{KILL}(S) = \text{KILL}(s_1) \cup \text{KILL}(s_2)$$

$$\text{IN}(s_1) = \text{IN}(s_2) = \text{IN}(S)$$

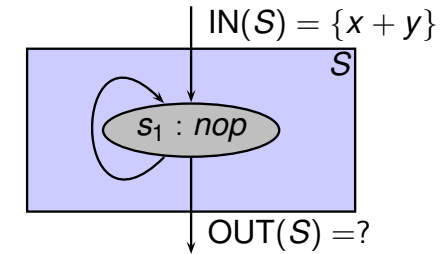
$$\text{OUT}(S) = \text{OUT}(s_1) \cap \text{OUT}(s_2)$$

AvE Analysis of a Structured Program



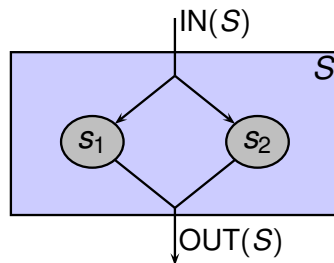
$$\begin{aligned} \text{GEN}(S) &= \text{GEN}(s_1) \\ \text{KILL}(S) &= \text{KILL}(s_1) \\ \text{OUT}(S) &= \text{OUT}(s_1) \\ \text{IN}(s_1) &= \text{IN}(S) \cap \text{GEN}(s_1) \text{ ?} \\ \text{IN}(s_1) &= \text{IN}(S) \cap \text{OUT}(s_1) \text{ ??} \end{aligned}$$

AvE Analysis of a Structured Program



Is $x + y$ available at $\text{OUT}(S)$?

AvE Analysis is Approximate



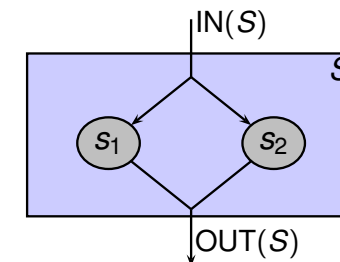
► Assumption: All paths are feasible.

► Example:

```
if (true) s1;
else      s2;
```

	Fact	Computed	Actual
$\text{GEN}(S)$	$=$	$\text{GEN}(s_1) \cap \text{GEN}(s_2) \subseteq$	$\text{GEN}(s_1)$
$\text{KILL}(S)$	$=$	$\text{KILL}(s_1) \cup \text{KILL}(s_2) \supseteq$	$\text{KILL}(s_1)$

AvE Analysis is Approximate



► Thus,

$$\begin{aligned} \text{true GEN}(S) &\supseteq \text{analysis GEN}(S) \\ \text{true KILL}(S) &\subseteq \text{analysis KILL}(S) \end{aligned}$$

► Fewer expressions marked available than actually do!

► Later we shall see that this is **SAFE** approximation

- prevents optimizations
- but NO wrong optimization

AvE for Basic Blocks

- ▶ Expr e is available at the start of a block if
 - ▶ It is available at the end of all predecessors

$$IN(B) = \bigcap_{P \in \text{PRED}(B)} OUT(P)$$

- ▶ Expr e is available at the end of a block if
 - ▶ Either it is generated by the block
 - ▶ Or it is available at the start of the block and not killed by the block

$$OUT(B) = IN(B) - KILL(B) \cup GEN(B)$$

Solving AvE Constraints

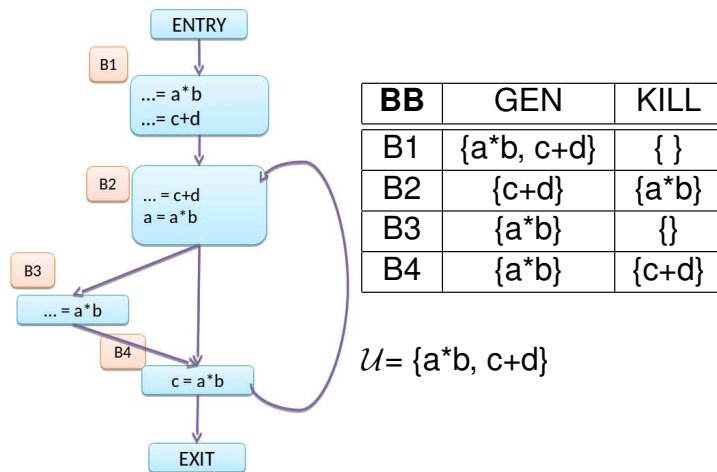
- ▶ KILL & GEN known for each BB.
- ▶ A program with N BBs has $2N$ equations with $2N$ unknowns.
 - ▶ Solution is possible.
 - ▶ Iterative approach (on the next slide).

Some Issues

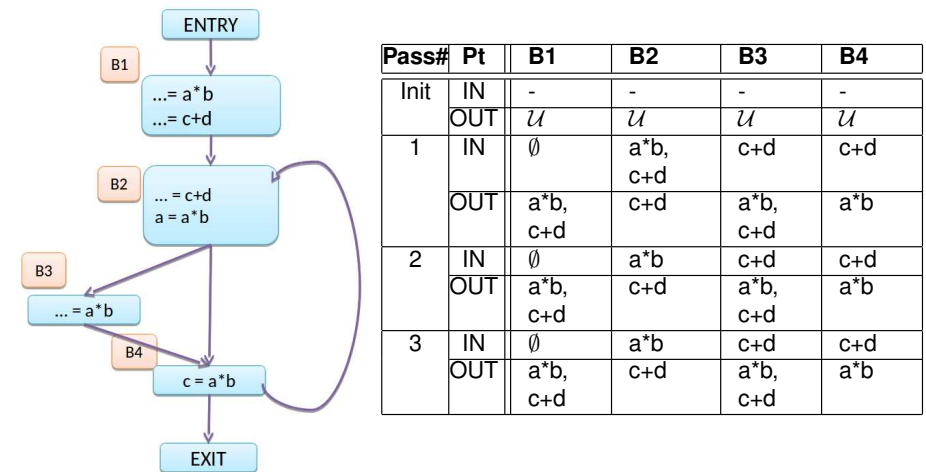
```
for each block  $B$  {  
     $OUT(B) = \mathcal{U}$ ;  $\mathcal{U}$  = "universal" set of all exprs  
}  
 $OUT(Entry) = \emptyset$ ; // remember reaching defs?  
change = true;  
while (change) {  
    change = false;  
    for each block  $B$  other than  $Entry$  {  
         $IN(B) = \bigcap_{P \in \text{PRED}(B)} OUT(P)$ ;  
        oldOut =  $OUT(B)$ ;  
         $OUT(B) = IN(B) - KILL(B) \cup GEN(B)$ ;  
        if ( $OUT(B) \neq \text{oldOut}$ ) then {  
            change = true;  
        }  
    }  
}
```

- ▶ What is \mathcal{U} – the set of *all* expressions?
- ▶ How to compute it efficiently?
- ▶ Why *Entry* block is initialized differently?

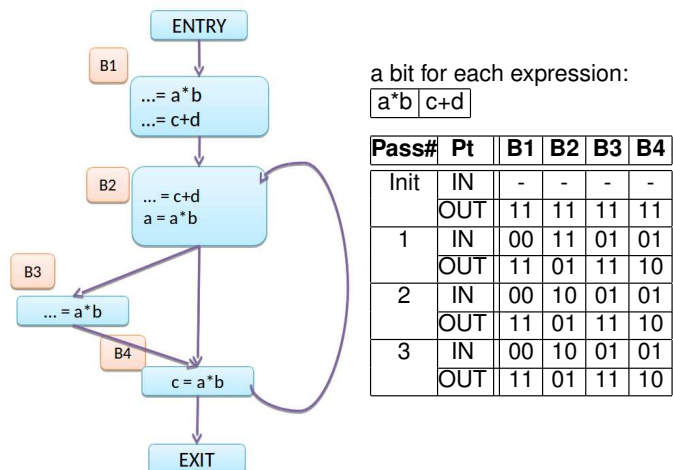
Available Expressions: Example



Available Expressions: Example



Available Expressions: Bitvectors



Available Expressions: Bitvectors

- Set-theoretic definitions:

$$IN(B) = \bigcap_{P \in \text{PRED}(B)} OUT(P)$$

$$OUT(B) = IN(B) - KILL(B) \cup GEN(B)$$

- Bitvector definitions:

$$IN(B) = \bigwedge_{P \in \text{PRED}(B)} OUT(P)$$

$$OUT(B) = IN(B) \wedge \neg KILL(B) \vee GEN(B)$$

- Bitwise \vee, \wedge, \neg operators

Available Expressions: Application

- ▶ Common subexpression elimination in a block B
 - ▶ Expression e available at the entry of B
 - ▶ e is also computed at a point p in B
 - ▶ Components of e are not modified from entry of B to p
- ▶ e is “upward exposed” in B
- ▶ Expressions generated in B are “downward exposed”

Comparison of RD and AvE

- ▶ *Some* vs. *All* path property
- ▶ Meet operator: \cup vs. \cap
- ▶ Initialization of *Entry*: \emptyset
- ▶ Initialization of other BBs: \emptyset vs. \mathcal{U}
- ▶ Safety: “More” RD vs. “Fewer” AvE

AvE: alternate Initialization

- ▶ What if we Initialize:
$$\text{OUT}(B) = \emptyset, \forall B \text{ including } \textit{Entry}$$
- ▶ Would we find “extra” available expressions?
 - ▶ More opportunity to optimize?
- ▶ OR would we miss some expressions that are available?
 - ▶ Loose on opportunity to optimize?

Live Variables

- ▶ A variable x is live at a point p if
 - ▶ There is a point p' along some path in the flow graph starting at p to the *Exit*
 - ▶ Value of x could be used at p'
 - ▶ There is no definition of x between p and p' along this path
- ▶ Otherwise x is dead at p

Live Variables: GEN

- ▶ $\text{GEN}(B)$: Set of variables whose values may be used in block B prior to any definition
 - ▶ Also called “use(B)”
- ▶ “upward exposed use” of a variable in B

Live Variables: KILL

- ▶ $\text{KILL}(B)$: Set of variables defined in block B prior to any use
 - ▶ Also called “def(B)”
- ▶ “upward exposed definition” of a variable in B

Live Variables: Equations

- ▶ Set-theoretic definitions:

$$\text{OUT}(B) = \bigcup_{S \in \text{SUCC}(B)} \text{IN}(S)$$

$$\text{IN}(B) = \text{OUT}(B) - \text{KILL}(B) \cup \text{GEN}(B)$$

- ▶ Bitvector definitions:

$$\text{OUT}(B) = \bigvee_{S \in \text{SUCC}(B)} \text{OUT}(S)$$

$$\text{IN}(B) = \text{OUT}(B) \wedge \neg \text{KILL}(B) \vee \text{GEN}(B)$$

- ▶ Bitwise \vee, \wedge, \neg operators

Very Busy Expressions

- ▶ Expression e is very busy at a point p if
 - ▶ Every path from p to *Exit* has at least one evaluation of e
 - ▶ On every path, there is no assignment to any component variable of e before the first evaluation of e following p
- ▶ Also called *Anticipable expression*

- ▶ Expression e is very busy at a point p if
 - ▶ **Every** path from p to *Exit* has at least one evaluation of e and there is no assignment to any component variable of e before the first evaluation of e following p on these paths.
- ▶ Set up the data flow equations for Very Busy Expressions (VBE). You have to give equations for GEN, KILL, IN, and OUT.
- ▶ Think of an optimization/transformation that uses VBE analysis. Briefly describe it (2-3 lines only)
- ▶ Will your optimization be *safe* if we replace “*Every*” by “*Some*” in the definition of VBE?