

Solution 1

Expr : $\{ u+v, a*b, w+v \}$

BB	Gen	Kill
B1	1 0 0	0 0 0
B2	0 0 0	0 0 1
B3	0 0 0	0 0 0
B4	0 0 1	0 0 0
B5	0 1 0	0 0 0
B6	0 0 0	0 1 0
B7	0 0 0	0 0 0
B8	0 1 0	0 0 0
B9	1 0 0	0 0 0

	Iteration 1		Iteration 2	
BB	In	Out	In	Out
B1	0 0 0	1 0 0	0 0 0	1 0 0
B2	1 0 0	1 0 0	1 0 0	1 0 0
B3	1 0 0	1 0 0	1 0 0	1 0 0
B4	1 0 0	1 0 1	1 0 0	1 0 1
B5	1 0 0	1 1 0	1 0 0	1 1 0
B6	1 1 0	1 0 0	1 1 0	1 0 0
B7	1 1 0	1 1 0	1 1 0	1 1 0
B8	1 0 0	1 1 0	1 0 0	1 1 0
B9	1 0 0	1 0 0	1 0 0	1 0 0

Iteration 1 and 2 gives same information, we will reach a fixed point after 2nd pass.

Solution 2

BB	Gen	Kill
B9	$\{ u, v \}$	ϕ
B8	$\{ a, b \}$	ϕ
B7	ϕ	ϕ
B6	ϕ	ϕ
B5	ϕ	$\{ a \}$
B4	ϕ	$\{ w \}$
B3	ϕ	ϕ
B2	ϕ	ϕ
B1	ϕ	$\{ u \}$

	Iteration 1		Iteration 2		Iteration 3	
BB	Out	In	Out	In	Out	In
B9	ϕ	$\{ u, v \}$	ϕ	$\{ u, v \}$	ϕ	$\{ u, v \}$
B8	$\{ u, v \}$	$\{ u, v, a, b \}$	$\{ u, v \}$	$\{ u, v, a, b \}$	$\{ u, v \}$	$\{ u, v, a, b \}$
B7	$\{ u, v, a, b \}$	$\{ u, v, a, b \}$	$\{ u, v, a, b \}$	$\{ u, v, a, b \}$	$\{ u, v, a, b \}$	$\{ u, v, a, b \}$
B6	$\{ u, v, a, b \}$	$\{ u, v, a, b \}$	$\{ u, v, a, b \}$	$\{ u, v, a, b \}$	$\{ u, v, a, b \}$	$\{ u, v, a, b \}$
B5	$\{ u, v, a, b \}$	$\{ u, v, b \}$	$\{ u, v, a, b \}$	$\{ u, v, b \}$	$\{ u, v, a, b \}$	$\{ u, v, b \}$
B4	ϕ	ϕ	$\{ u, v \}$	$\{ u, v \}$	$\{ u, v \}$	$\{ u, v \}$
B3	$\{ u, v \}$	$\{ u, v \}$	$\{ u, v \}$	$\{ u, v \}$	$\{ u, v \}$	$\{ u, v \}$
B2	$\{ u, v \}$	$\{ u, v \}$	$\{ u, v \}$	$\{ u, v \}$	$\{ u, v \}$	$\{ u, v \}$
B1	$\{ u, v, b \}$	$\{ v, b \}$	$\{ u, v, b \}$	$\{ v, b \}$	$\{ u, v, b \}$	$\{ v, b \}$

Iteration 2 and 3 gives same information, we will reach a fixed point after 3rd pass.

Solution 3

This is a sample solution, there can be variations based on the description provided.

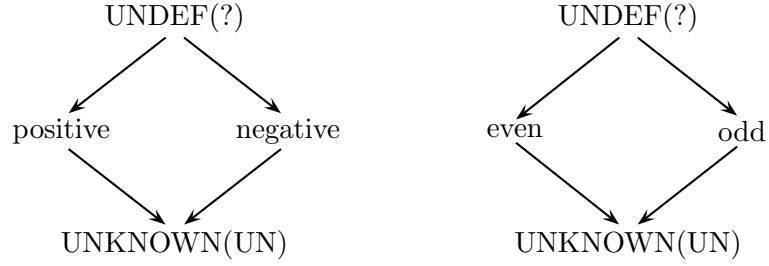
Assumption

? = UNDEF
 pe = positive even
 po = negative odd
 ne = positive even
 no = negative odd
 UN = UNKNOWN

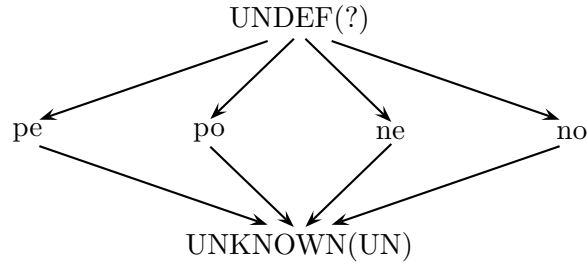
Direction of analysis

Forward

Component lattice



Lattice for positive-negative integers Lattice for odd-even integers



Lattice after merging the two component lattice

Boundary information and meet operation

$\text{In}(\text{Entry}) = ?$

meet of two values can be obtained through lattice.

Transfer Functions

$\mathbf{x} = \mathbf{c}$

where x is variable and c is constant

$\text{Out}_n = \{x \rightarrow \text{type}(c)\}$

$\text{type}(c)$ returns one of the values from set $\{ \text{po}, \text{pe}, \text{no}, \text{ne} \}$ depending upon the type of constant.

$\mathbf{x} = \mathbf{y}$

where x and y both are variables

$$Out_n = \{x \rightarrow type_v(y)\}$$

$type_v(y)$ returns one of the values from set $\{?, po, pe, no, ne, UN\}$ depending upon the In information of variable y.

$$\mathbf{x} = \mathbf{y} + \mathbf{z}$$

where x, y and z are variables

$$Out_n = \{x \rightarrow eval_+(y, z)\}$$

$eval_+$						
$y \backslash z$?	pe	po	ne	no	UN
?	?	?	?	?	?	UN
pe	?	pe	po	UN	UN	UN
po	?	po	pe	UN	UN	UN
ne	?	UN	UN	ne	no	UN
no	?	UN	UN	no	ne	UN
UN	UN	UN	UN	UN	UN	UN

$$\mathbf{x} = \mathbf{y} * \mathbf{z}$$

where x, y and z are variables

$$Out_n = \{x \rightarrow eval_*(y, z)\}$$

$eval_*$						
$y \backslash z$?	pe	po	ne	no	UN
?	?	?	?	?	?	UN
pe	?	pe	pe	ne	ne	UN
po	?	pe	po	ne	no	UN
ne	?	ne	ne	pe	pe	UN
no	?	ne	no	pe	po	UN
UN	UN	UN	UN	UN	UN	UN