HOMEWORK 11 DUE: THURSDAY, JUNE 22

Find the solution of the given initial value problem. Draw the graphs of the solution and of the the non-homogenous part of the DE. (Label your graphs appropriately.)

(1)
$$y'' + 2y' + 2y = \begin{cases} 1 & \text{if } \pi \le t < 2\pi \\ 0 & \text{else} \end{cases}$$
, $y(0) = 0$, $y'(0) = 1$
(2) $y'' + y = \begin{cases} t/2 & \text{if } 0 \le t < 6 \\ 3 & \text{else} \end{cases}$, $y(0) = 0$, $y'(0) = 1$
(3) $y'' + y' + \frac{5}{4}y = \begin{cases} \sin t & \text{if } 0 \le t < \pi \\ 0 & \text{else} \end{cases}$, $y(0) = 0$, $y'(0) = 0$

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$$y'' + y = \begin{cases} t/2 & \text{if } 0 \le t < 6 \\ 3 & \text{else} \end{cases}$$
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$$y'' + y' + \frac{5}{4}y = \begin{cases} \sin t & \text{if } 0 \le t < \pi \\ 0 & \text{else} \end{cases}$$
, $y(0) = 0$, $y'(0) = 0$

(4)
$$y'' + y = u_{3\pi}(t)$$
, $y(0) = 1$, $y'(0) = 0$

(5)
$$y'' + 4y = u_{\pi}(t) - u_{3\pi}(t)$$
, $y(0) = 0$, $y'(0) = 0$