

HOMEWORK 7 & 8

DUE: THURSDAY, JUNE 15

For each of the following matrices:

- (Optional) *Describe* the corresponding linear transformations.
- Write down the corresponding system of differential equations.
- Find the general solution.
- Sketch a phase portrait of the corresponding system.

(Assume that $a, b > 0$ are distinct positive constants and $\theta \in [0, 2\pi]$.)

$$1. \begin{bmatrix} 2 & 0 \\ 0 & 2 \end{bmatrix}$$

$$2. \begin{bmatrix} -2 & 0 \\ 0 & -2 \end{bmatrix}$$

$$3. \begin{bmatrix} 2 & -1 \\ 0 & 3 \end{bmatrix}$$

$$4. \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$$

$$5. \begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix}$$

$$6. \begin{bmatrix} 0 & 2 \\ -2 & -2 \end{bmatrix}$$

$$7. \begin{bmatrix} 0 & 2 \\ -2 & 2 \end{bmatrix}$$

$$8. \begin{bmatrix} 0 & 0 \\ a & b \end{bmatrix}$$

$$9. \begin{bmatrix} 0 & a \\ 0 & b \end{bmatrix}$$

$$10. \begin{bmatrix} 1 & 0 \\ a & 1 \end{bmatrix}$$

$$11. \begin{bmatrix} a & b \\ b & a \end{bmatrix}$$

$$12. \begin{bmatrix} \cos \theta & \sin \theta \\ \sin \theta & -\cos \theta \end{bmatrix}$$