

HPE DSI 311 Introduction to Machine Learning

Spring 2023

Instructor: Ioannis Konstantinidis

Quick review

Model evaluation

- Cross-validation (k-fold)
- Metrics and Scoring

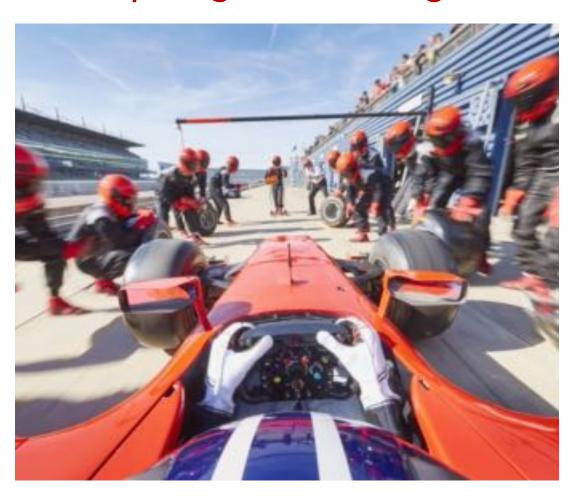
Supervised models for classification

- k-Nearest Neighbors
- Logistic regression
- Support Vector Machines
- Decision Trees
- Random Forests
- Gradient Boosting





Pit stop: organizational guidelines



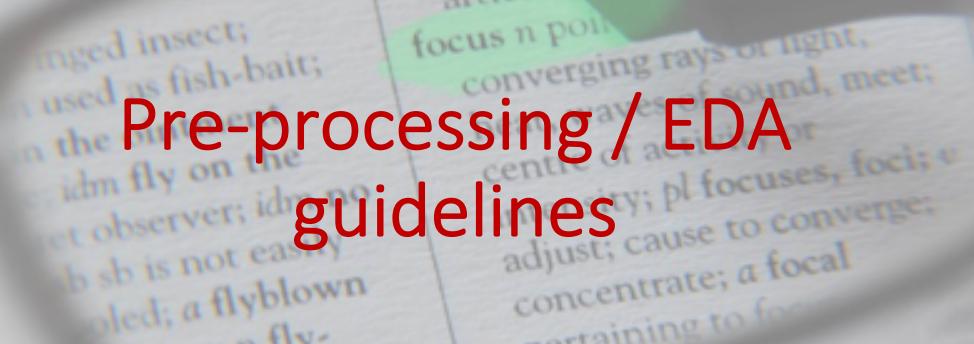
Data pre-processing and exploratory data analysis (EDA)

- Data cleaning and tidying up
- Numerical summaries
- Graphical summaries

Data transformations

- Scaling (standard/MinMax)
- Feature Extraction (PCA / dimension reduction)





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Cleaning data

No incomplete, incorrect, inaccurate, or irrelevant parts

- identifying missing values
- matching similar but not identical values (created by typos)
- correcting character encodings (for international data)
- filling in structural missing values
- parsing dates and numbers
- ...



EDA checklist

Sanity checks:

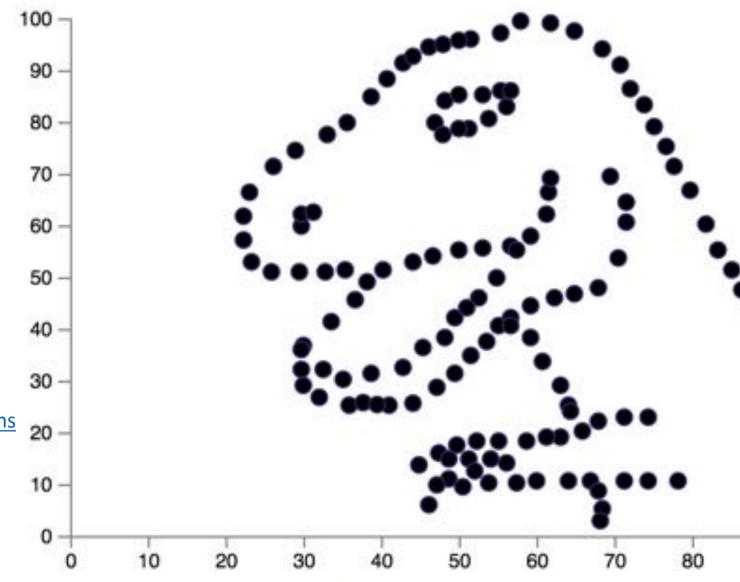
- Look at the top and the bottom of your data tables
- Check your univariate statistics
 - Numerical Summaries
- Check your bivariate plots
 - Graphical Summaries

Reasons for making plots

- Setting expectations for what the data should look like.
- Checking deviations from what you might expect
- Numerical summaries don't give the whole picture



https://www.autodesk.com/research/publications/same-stats-different-graphs



Data transformations are data processing tasks

- They come after pre-processing the data
- They come after EDA

EDA and data pre-processing tasks are done to make the learning process possible

Feature organization transformations are done to improve the learning process







Why mess with the data values?



Some algorithms rely on distance/similarity

 kNN and SVM rely on computing distance / similarity to the nearest neighbors or the support vectors, respectively.

• Tree-based algorithms on the other hand (e.g., decision trees, random forests) do not rely on finding distance / similarity to any specific points (they use comparisons to fixed thresholds instead).

Temp and humidity:

• F value range is about 0 - 100

• % value range is about 0 - 100

A change of one unit in temperature value counts the same as a change of one unit in humidity values

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- F value range is about 0 100
- % value range is about 0 100

A change of one unit in temperature value counts the same as a change of one unit in humidity values

But this is an accident, due to the arbitrary choice of units

Temp and humidity:

C value range is about 0 - 40

decimal value range is about 0 - 1

A change of one unit in temperature value counts as a LOT less than a change of one unit in humidity values

The relative influence of a variable on the total similarity/distance should not depend on an arbitrary choice of units

-> Need to scale the data

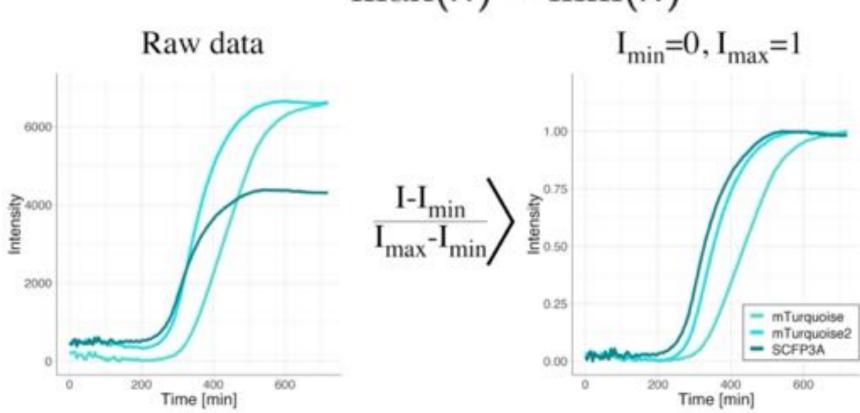


How to scale the data?



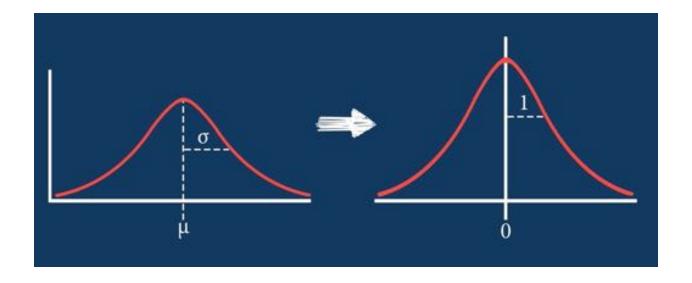
MinMaxScaler: uniform range of 0 - 1

$$x_{\text{norm}} = \frac{x - \min(x)}{\max(x) - \min(x)}$$



StandardScaler: centered at 0

$$x_{\text{stand}} = \frac{x - \text{mean}(x)}{\text{standard deviation }(x)}$$



Are the data normally distributed?

Fit once, and then reuse

- •Fit the scaler using available training data. For normalization, this means the training data will be used to estimate the minimum and maximum observable values. This is done by calling the *fit()* function.
- •Apply the scale to training data. This means you can use the normalized data to train your model. This is done by calling the transform() function.
- •Apply the scale to data going forward. This means you can prepare new data in the future on which you want to make predictions.



Hands-on Example:

Scaling

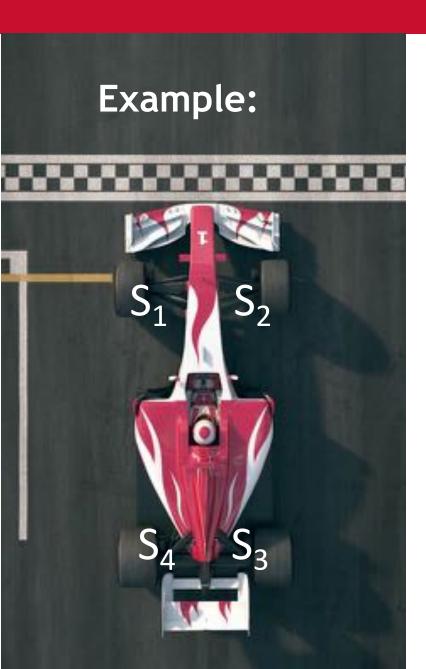






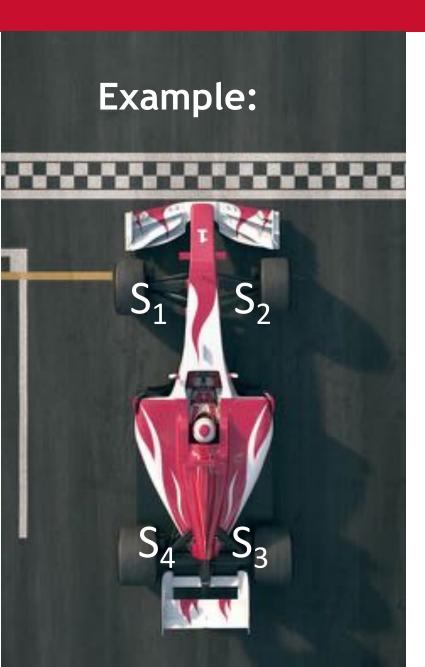
Why mess with the variables / columns?





Original variables

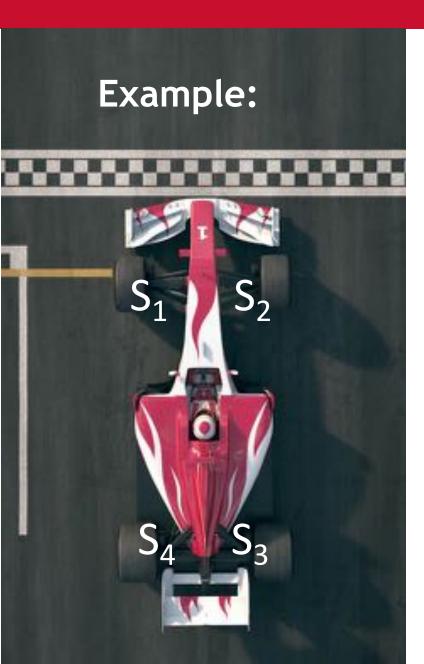
Four sensors measuring rotation speed (spin) at each wheel: S_1 , S_2 , S_3 , S_4



Four sensors measuring rotation speed (spin) at each wheel: S_1 , S_2 , S_3 , S_4

$$T_1 = (S_1 + S_2 + S_3 + S_4) / 4 = \frac{1}{4}S_1 + \frac{1}{4}S_2 + \frac{1}{4}S_3 + \frac{1}{4}S_4$$

This is a more reliable indicator of car speed



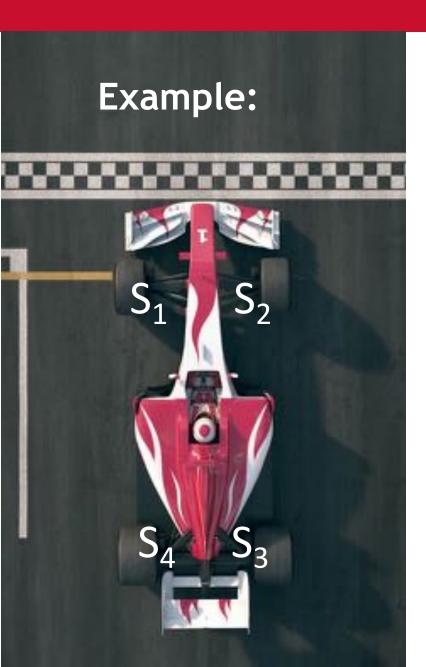
Four sensors measuring rotation speed (spin) at each wheel: S_1 , S_2 , S_3 , S_4

New **composite** measure (feature):

$$T_1 = (S_1 + S_2 + S_3 + S_4) / 4 = \frac{1}{4}S_1 + \frac{1}{4}S_2 + \frac{1}{4}S_3 + \frac{1}{4}S_4$$

This is a more reliable indicator of car speed

$$T_2 = 0.5 \left\{ \left(\frac{S_1 + S_3 + S_4}{3} \right) - S_2 \right\} = \frac{1}{6} S_1 - \frac{1}{2} S_2 + \frac{1}{6} S_3 + \frac{1}{6} S_4$$
If this starts to veer away from zero, then tire #2 is spinning faster than the others (possible flat)



Four sensors measuring rotation speed (spin) at each wheel: S_1 , S_2 , S_3 , S_4

New composite measure (feature):

$$T_1 = (S_1 + S_2 + S_3 + S_4) / 4 = \frac{1}{4}S_1 + \frac{1}{4}S_2 + \frac{1}{4}S_3 + \frac{1}{4}S_4$$

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New composite measure (feature):

$$T_2 = 0.5 \left\{ \left(\frac{S_1 + S_3 + S_4}{3} \right) - S_2 \right\} = \frac{1}{6} S_1 - \frac{1}{2} S_2 + \frac{1}{6} S_3 + \frac{1}{6} S_4$$
If this starts to veer away from zero, then tire #2 is spinning faster than the others (possible flat)

Similarly,

$$T_3 = 0.5 \left\{ \left(\frac{S_1 + S_2 + S_4}{3} \right) - S_3 \right\}$$

$$T_4 = 0.5 \left\{ \left(\frac{S_1 + S_2 + S_3}{3} \right) - S_4 \right\}$$

Example:

Features

Original measures (variables):

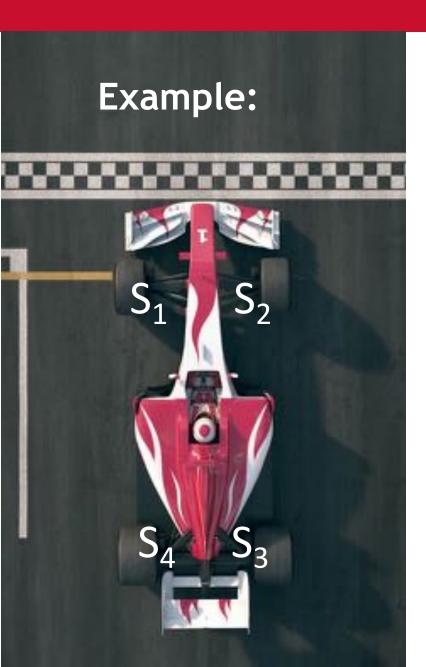
$$S_1, S_2, S_3, S_4$$

$$T_{1} = \frac{1}{4}S_{1} + \frac{1}{4}S_{2} + \frac{1}{4}S_{3} + \frac{1}{4}S_{4}$$

$$T_{2} = \frac{1}{6}S_{1} - \frac{1}{2}S_{2} + \frac{1}{6}S_{3} + \frac{1}{6}S_{4}$$

$$T_{3} = \frac{1}{6}S_{1} + \frac{1}{6}S_{2} - \frac{1}{2}S_{3} + \frac{1}{6}S_{4}$$

$$T_{4} = \frac{1}{6}S_{1} + \frac{1}{6}S_{2} + \frac{1}{6}S_{3} - \frac{1}{2}S_{4}$$



Original measures (variables):

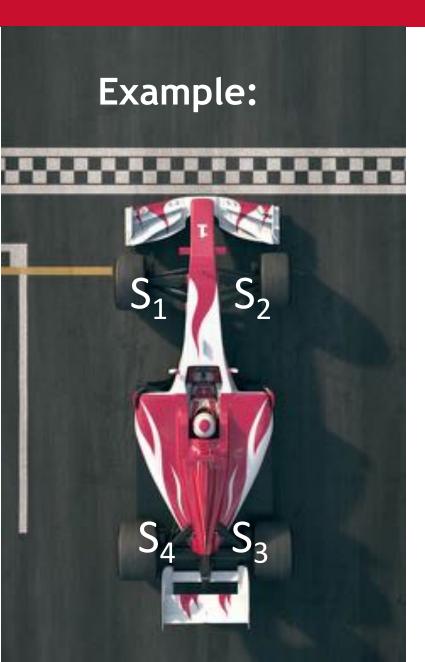
$$S_1, S_2, S_3, S_4$$

$$T_{1} = +\frac{1}{4}S_{1} + \frac{1}{4}S_{2} + \frac{1}{4}S_{3} + \frac{1}{4}S_{4}$$

$$T_{2} = +\frac{1}{6}S_{1} - \frac{1}{2}S_{2} + \frac{1}{6}S_{3} + \frac{1}{6}S_{4}$$

$$T_{3} = +\frac{1}{6}S_{1} + \frac{1}{6}S_{2} - \frac{1}{2}S_{3} + \frac{1}{6}S_{4}$$

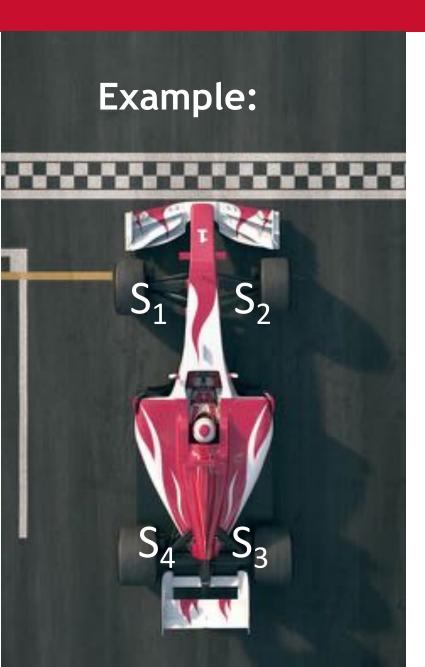
$$T_{4} = +\frac{1}{6}S_{1} + \frac{1}{6}S_{2} + \frac{1}{6}S_{3} - \frac{1}{2}S_{4}$$



Original measures (variables):

$$S_1, S_2, S_3, S_4$$

$$\begin{bmatrix} T_1 \\ T_2 \\ T_3 \\ T_4 \end{bmatrix} = \begin{bmatrix} +\frac{1}{4} & +\frac{1}{4} & +\frac{1}{4} & +\frac{1}{4} \\ +\frac{1}{6} & -\frac{1}{2} & +\frac{1}{6} & +\frac{1}{6} \\ +\frac{1}{6} & +\frac{1}{6} & -\frac{1}{2} & +\frac{1}{6} \\ +\frac{1}{6} & +\frac{1}{6} & +\frac{1}{6} & -\frac{1}{2} \end{bmatrix} \begin{bmatrix} S_1 \\ S_2 \\ S_3 \\ S_4 \end{bmatrix}$$



Original measures (variables):

$$S_1, S_2, S_3, S_4$$

$$T = W^{T}S, \qquad W^{T} = \begin{bmatrix} +\frac{1}{4} & +\frac{1}{4} & +\frac{1}{4} & +\frac{1}{4} \\ +\frac{1}{4} & -\frac{1}{4} & +\frac{1}{4} & +\frac{1}{4} \\ +\frac{1}{6} & -\frac{1}{2} & +\frac{1}{6} & +\frac{1}{6} \\ +\frac{1}{6} & +\frac{1}{6} & +\frac{1}{6} & -\frac{1}{2} \end{bmatrix}$$

Principal Component Analysis (PCA)

PCA is a method for computing new features from existing variables according to a generic principle.

PCA will compute the weight matrix W for the new composite measures T_i (which are called principal components) so the data are now measured according to these new composite measures

NOTES: The original variables must be centered (i.e., have mean zero)

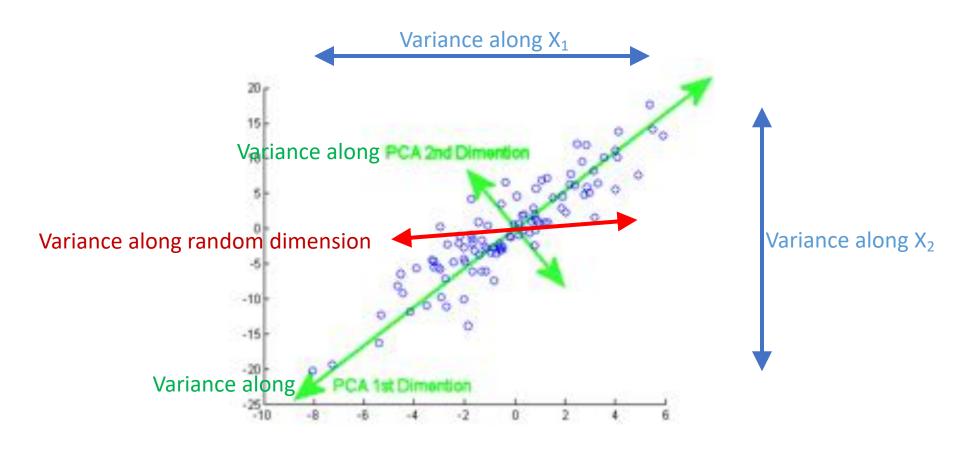
Original X (variables):

Observation ID	S ₁	S ₂	S ₃	S ₄
1				
N				

Transformed X (features/components):

Observation ID	T ₁	T ₂	T ₃	T ₄
1				
•••				
N				

PCA principle: PC₁ is the direction of maximum variance



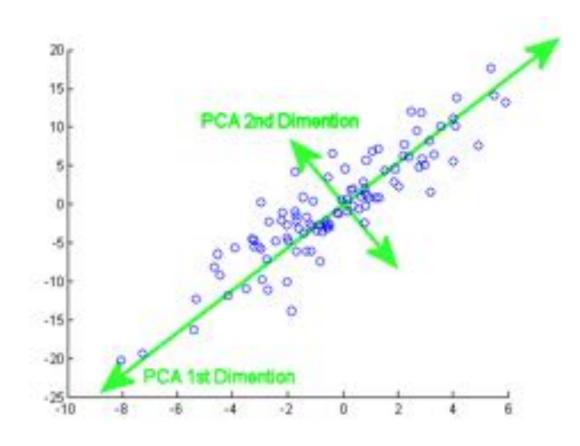
$$Var(X_1) + Var(X_2) = Var(PC_1) + Var(PC_2)$$

PCA principles, continued

Principal Components are orthogonal to each other

Principal Components are ordered

• every principal component captures less variance than the ones before, i.e., $Var(PC_1) \ge Var(PC_2) \ge ...$





Hands-on Example: PCA

https://jakevdp.github.io/PythonDataScienceHandbook/05.09-principal-component-analysis.html



What is the curse of dimensionality?



More dimensions, more problems

1-D

If I dropped my keys somewhere along the path between my car and my house, it would take only a few minutes to walk the straight path and find them.

2-D

If I dropped my keys somewhere in my yard while mowing my lawn, it could take me hours to search the whole yard to find them.

3-D

If a dropped my keys in one of the offices in PGH while going door-to-door delivering girl scout cookies, it would take days to search all the building floors to find them.



Dimension Reduction with PCA

Work with only the top few principal components, since they capture most of the variance



Homework Assignment #2 Due Sunday (February 19), 11:59 pm (Central)

