

Please construct context-free grammars **without  $\epsilon$ -productions** from the following languages (10%).

a)  $\{\omega \mid \omega \in (a,b,c)^* \text{ and the numbers of a's and b's and c's occurred in } \omega \text{ are **even**}\}$

b)  $\{a^i b^j \mid i \geq (2j+1) \text{ and } j \geq 0\}$

c)  $\{\omega \mid \omega \in (a,b,c)^* \text{ and the numbers of a's and b's occurred in } \omega \text{ are **odd**}\}$

d)  $\{a^i b^j \mid i \geq (j+1) \text{ and } j \geq 0\}$

e)  $\{\omega \mid \omega \in (a,b,c)^*, \omega \text{ is **lead by a** and the numbers of a's and b's occurred in } \omega \text{ are **even**}\}$

f)  $\{a^{2i} b^{2j} \mid j \geq i \geq 1\}$

g)  $\{\omega \mid \omega \in (a,b,c)^* \text{ and } \omega \text{ **starts with a and ends with b**, the numbers of a's and c's occurred in } \omega \text{ are **even**}\}$

h)  $\{a^i b^j c^k \mid j \geq (i+k+1) \text{ and } i \geq 0, k \geq 1\}$

j)  $\{\omega \mid \omega \in (a,b,c)^* \text{ and } \omega \text{ starts with a or b, ends with c, and the numbers of a's and b's and c's occurred in } \omega \text{ are **even**}\}$

$$k) a^{2i-1}b^{2j-1}c^{2k-1} \ (i \geq 1, j \geq i+k, k \geq 1)$$